

Title: Errors in the Trapped Ion Quantum Computer

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Abstract:

# Errors in Trapped Ion Quantum Processing

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University of Michigan  
Department of Physics and FOCUS Center

<http://iontrap.physics.lsa.umich.edu/>



US Disruptive  
Technology Office



US National  
Security Agency

Pirsa: 07060054



US Army  
Research Office

NSF

National Science  
Foundation



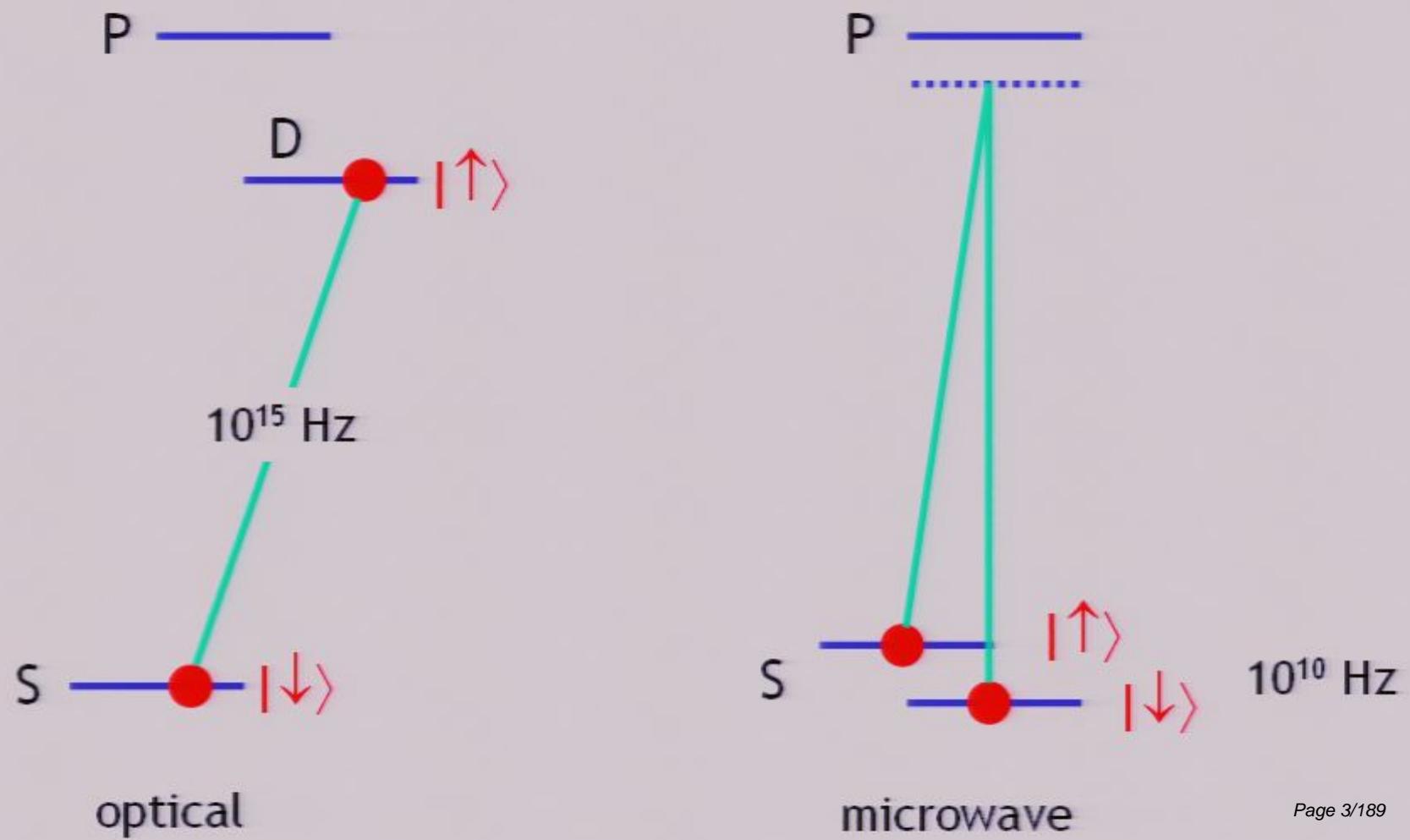
NSF  
FOCUS Center



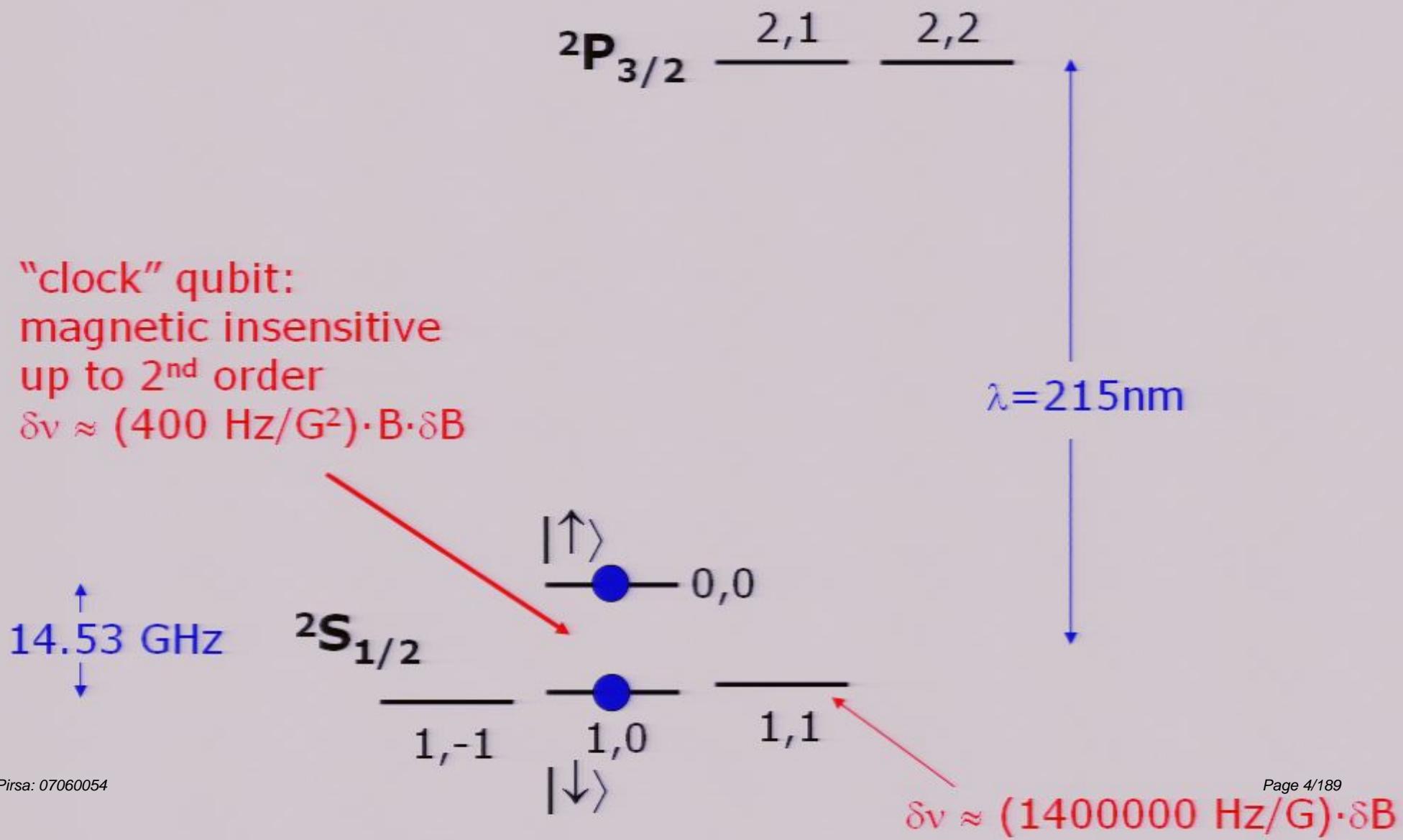
US Defense  
Advanced Research  
Projects Agency

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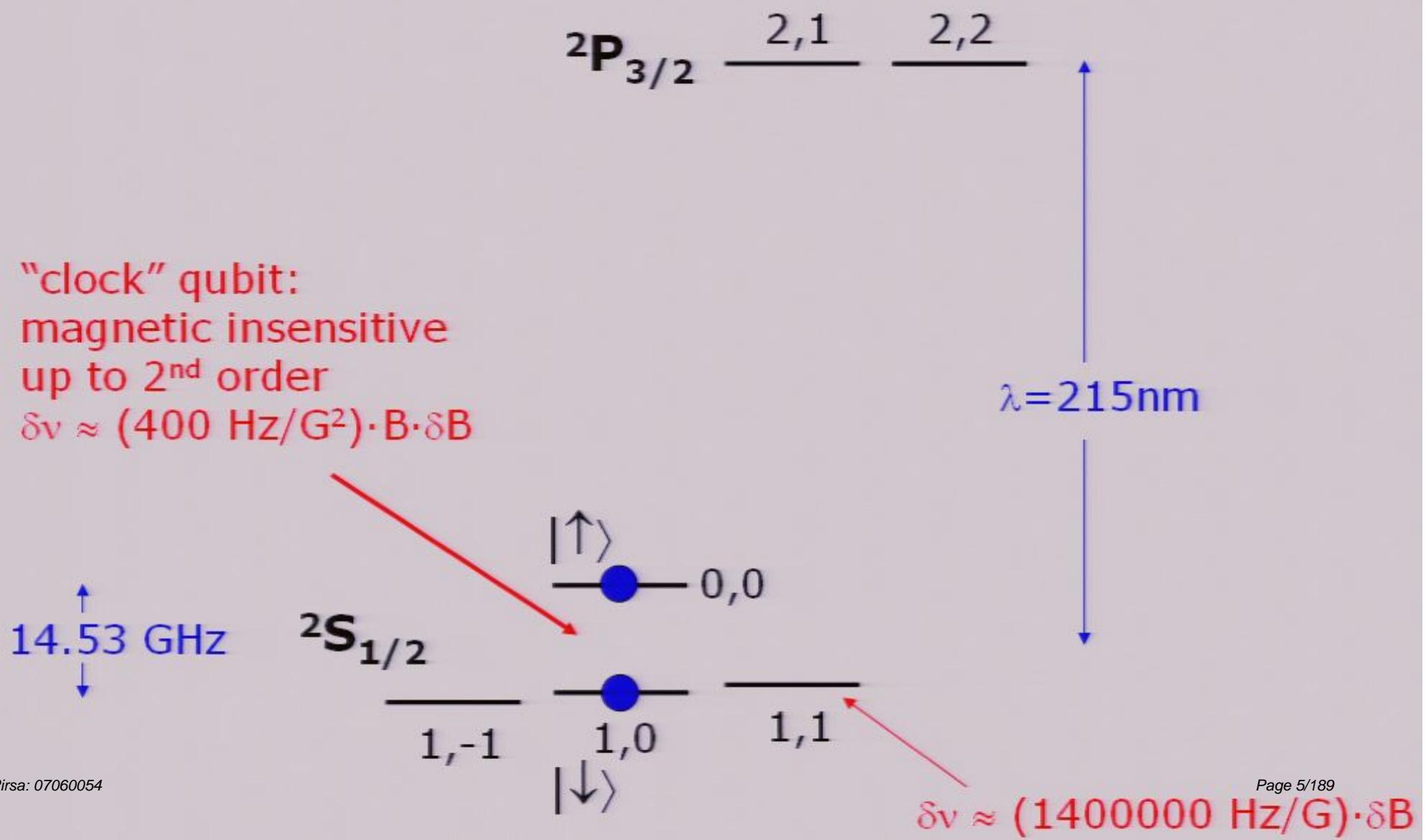
# Good atomic two-level systems



# $^{111}\text{Cd}^+$ atomic structure



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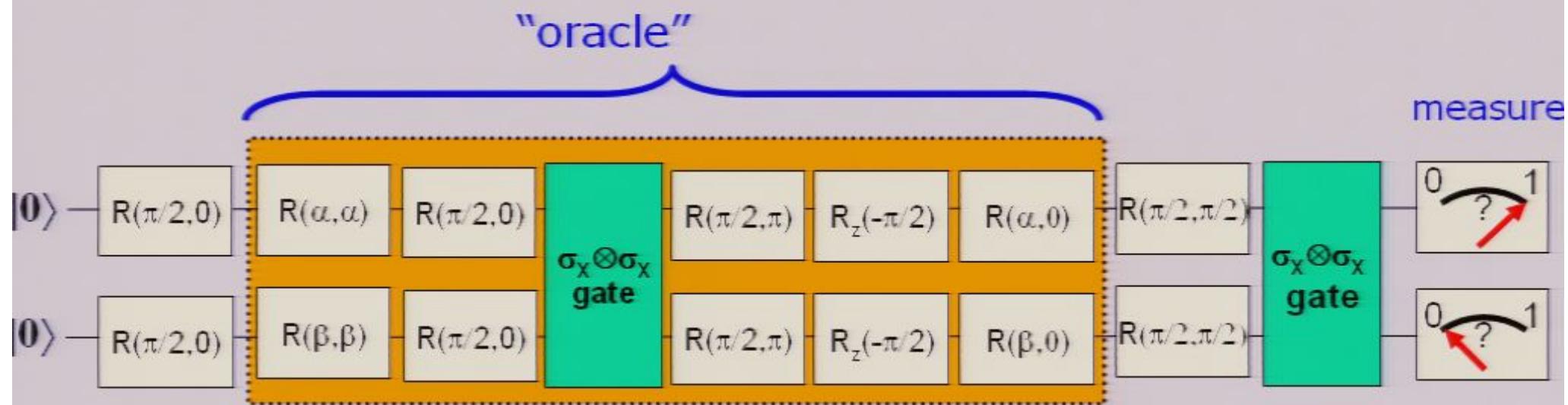


# Quantum Algorithms Demonstrated with Ions

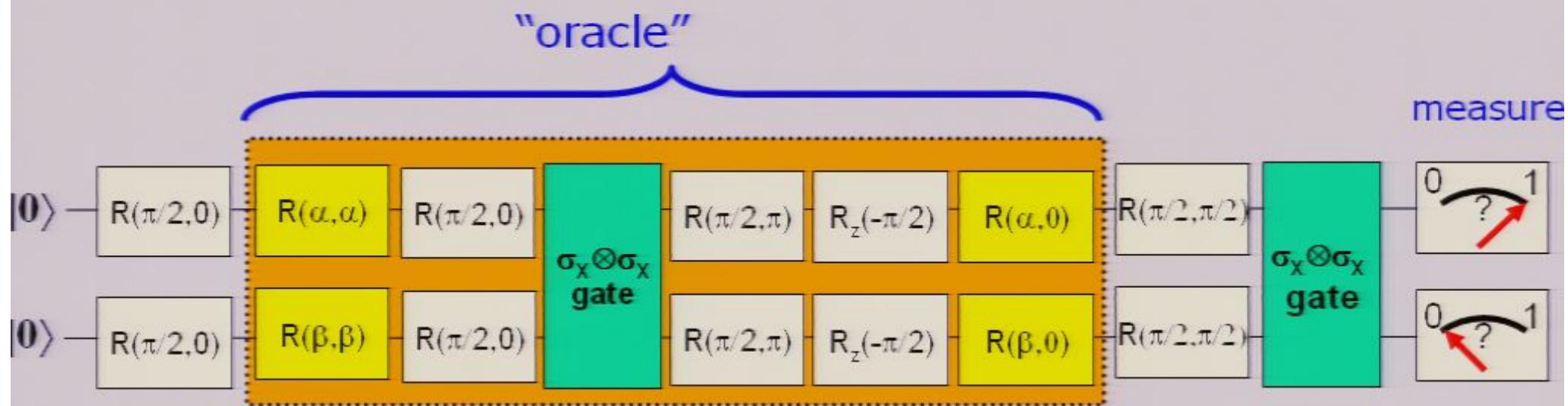
- \* Deutsch-Jozsa (is a function constant or balanced?) 1 qubit
- \* Dense coding (using one qubit to transmit 2 classical bits)
- \* Fast Fourier Transform: 3 qubits
- \* Quantum Teleportation: 3 qubits
- \* Grover (searching unsorted database): 2 qubits

NIST-Boulder  
Innsbruck  
Michigan

# Implementation of Grover's Search Algorithm on N=2 ions (4-element database)



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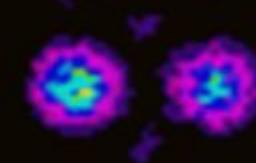


mark state with Bloch-sphere rotation angles

	$\alpha$	$\beta$
$ 00\rangle$	$\pi$	$\pi$
$ 01\rangle$	$\pi$	0
$ 10\rangle$	0	$\pi$
$ 11\rangle$	0	0

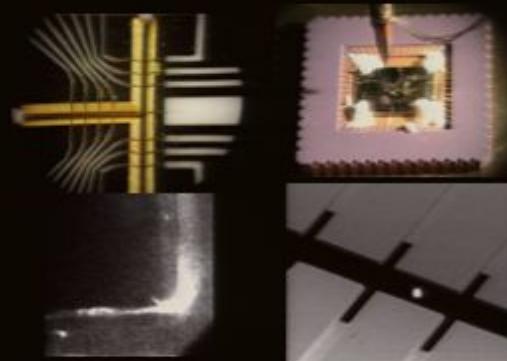
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

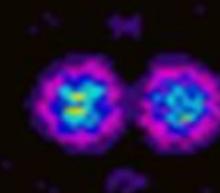
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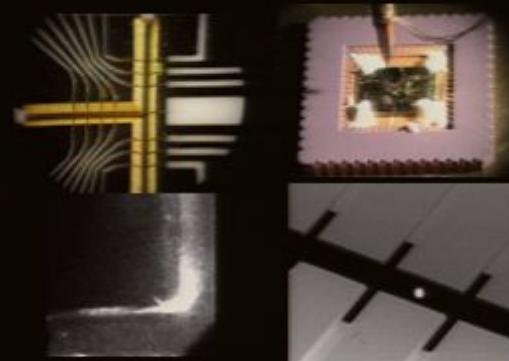
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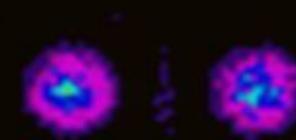
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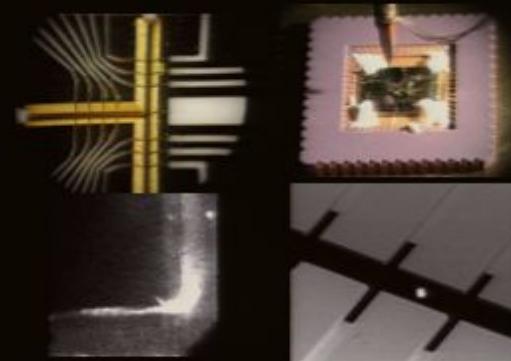
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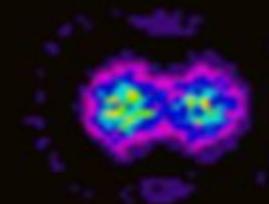
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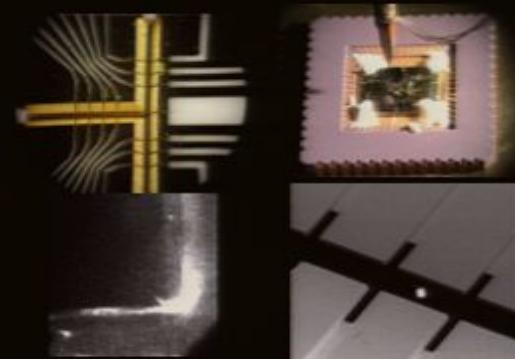
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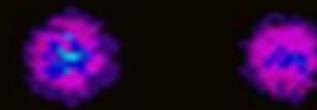


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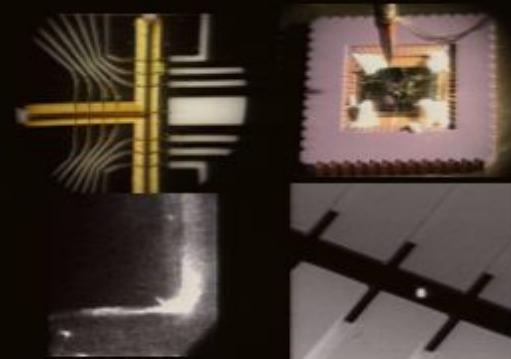
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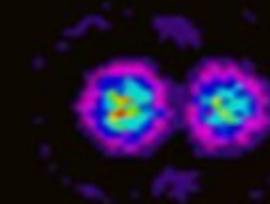
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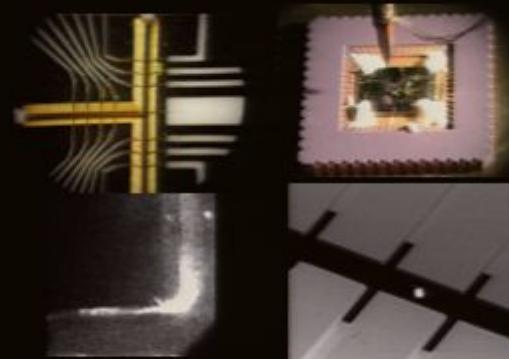
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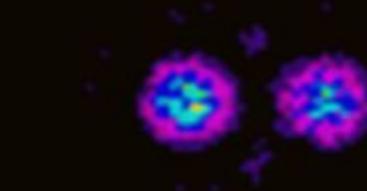
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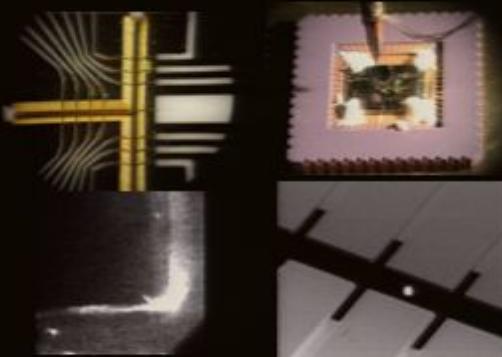
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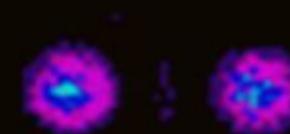
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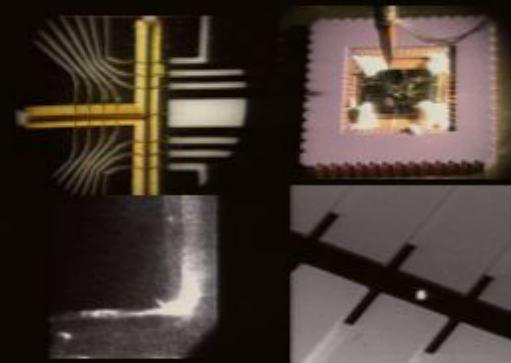
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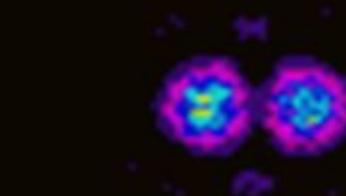
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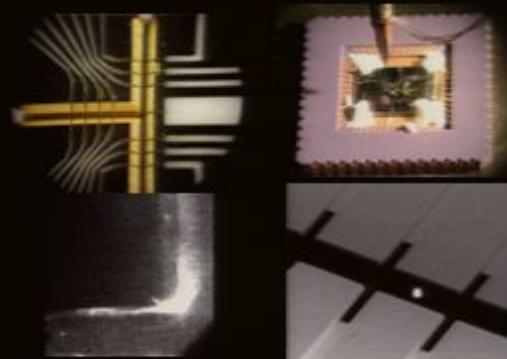
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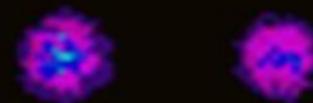
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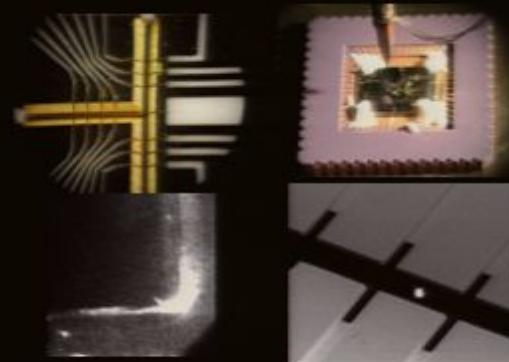
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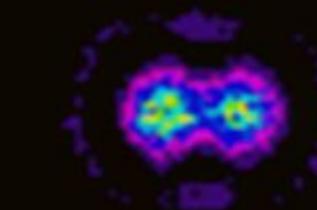
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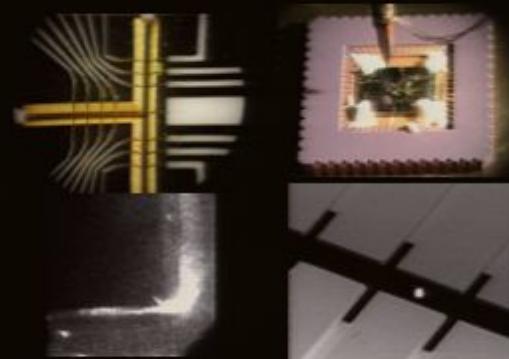
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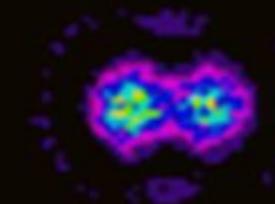
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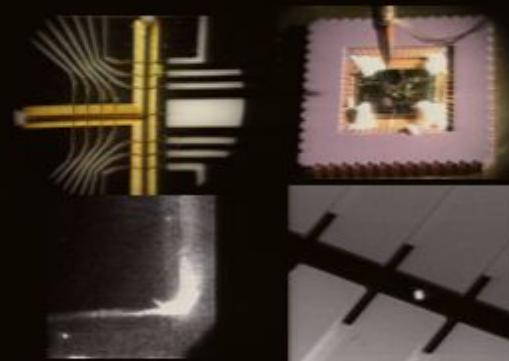
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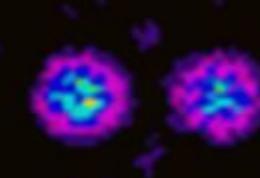


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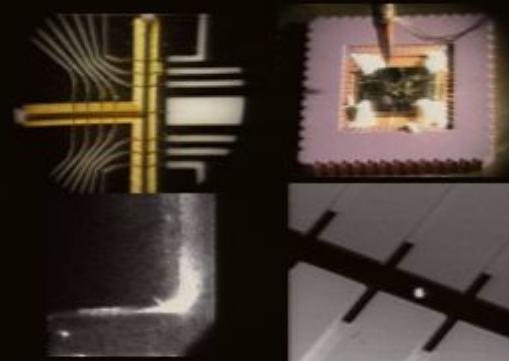
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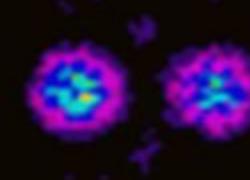


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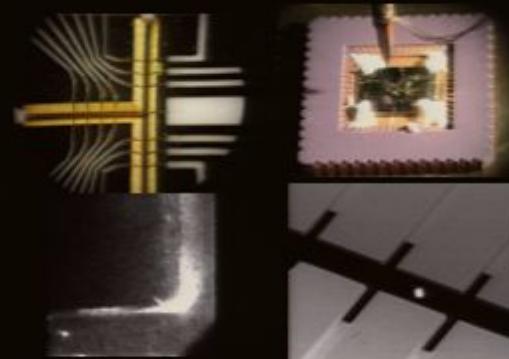
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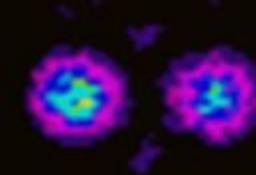


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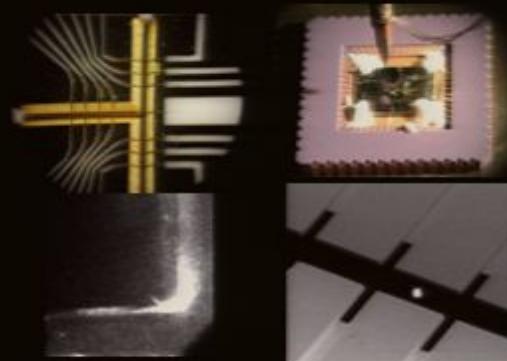
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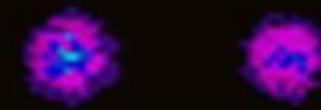


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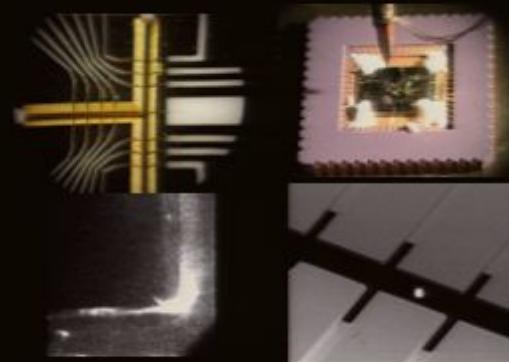
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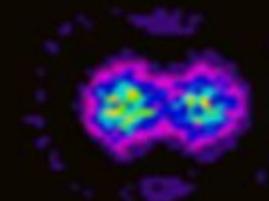
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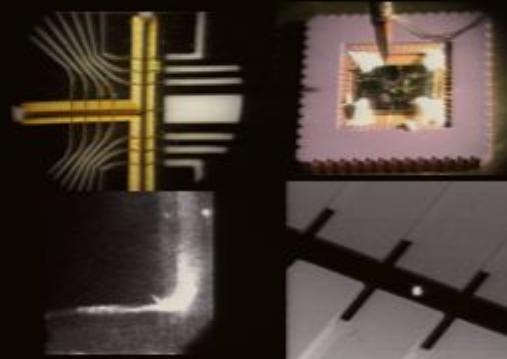
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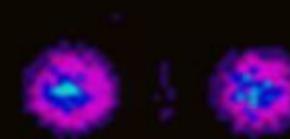


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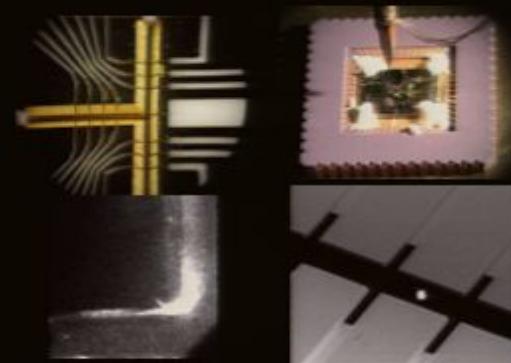
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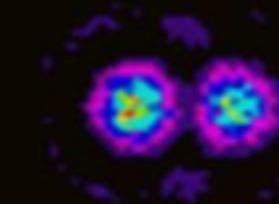
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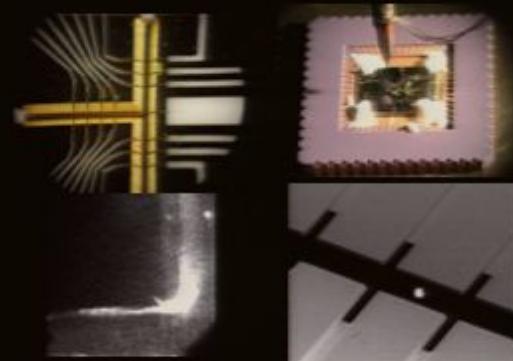
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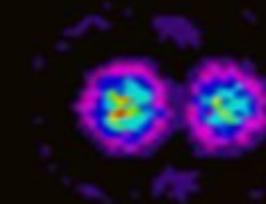
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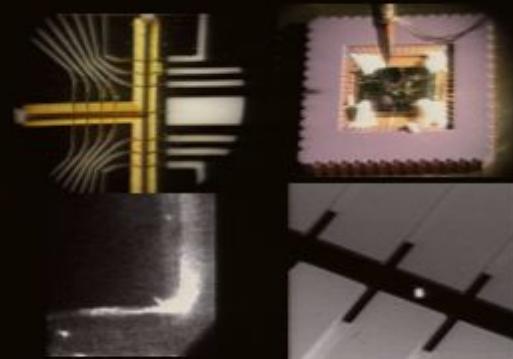
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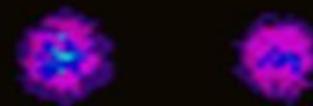


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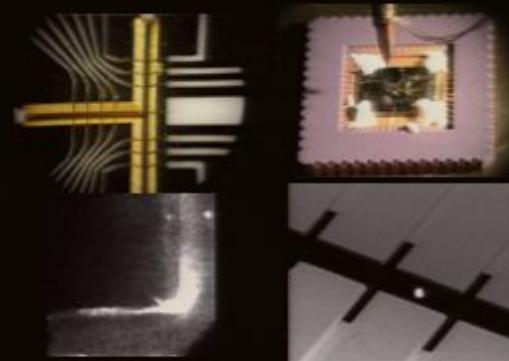
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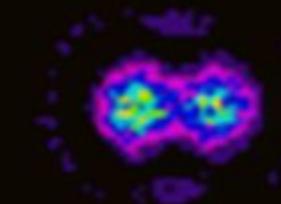
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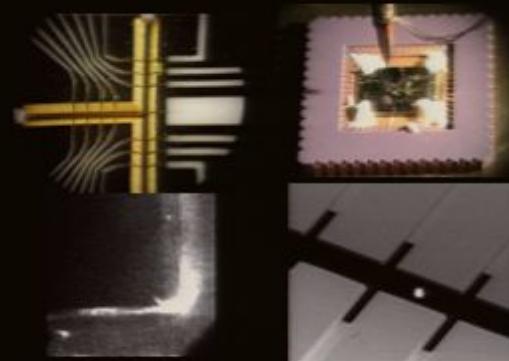
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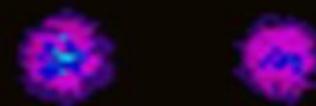
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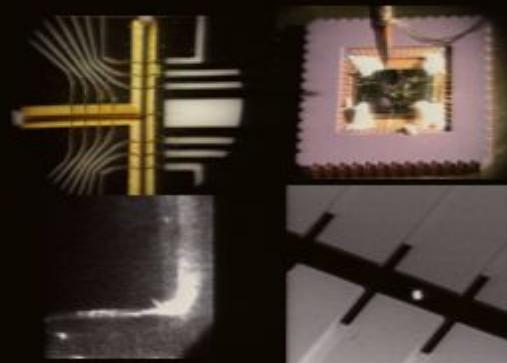
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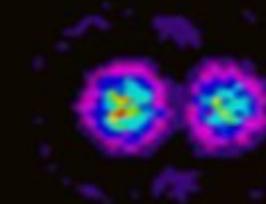
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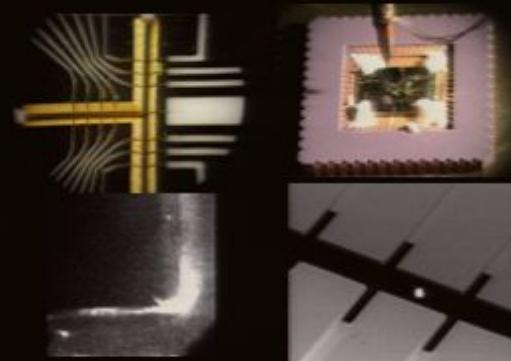
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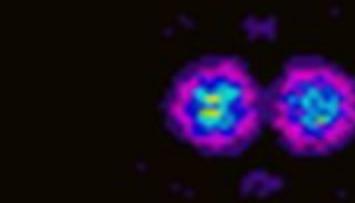
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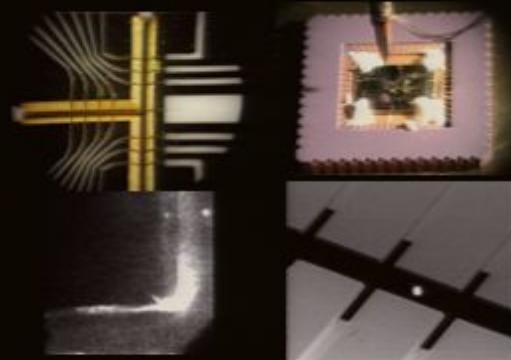
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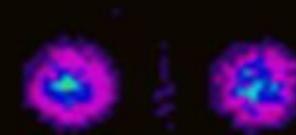
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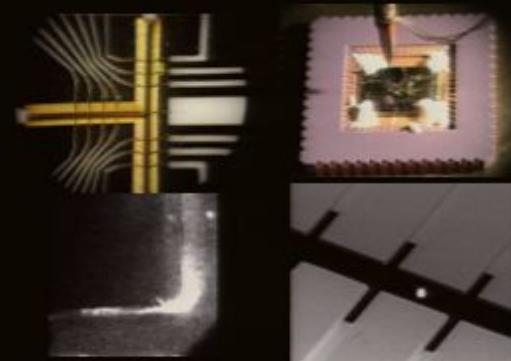
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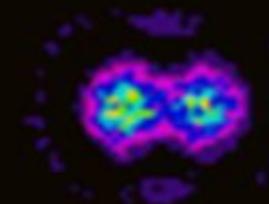
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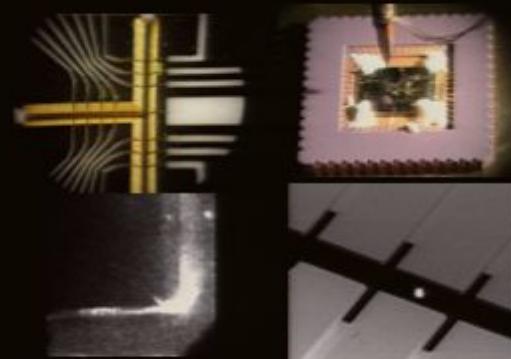
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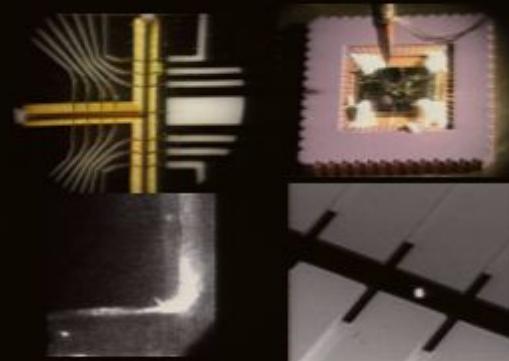
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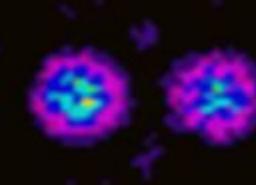


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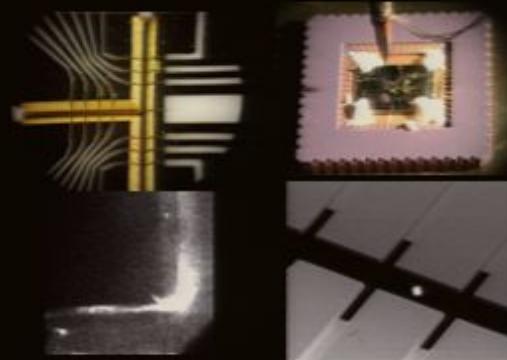
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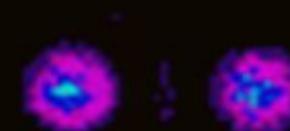
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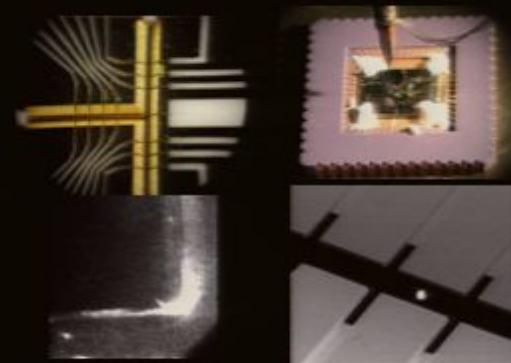
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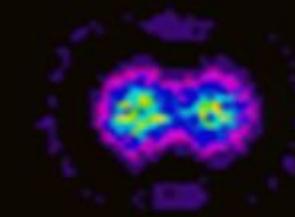
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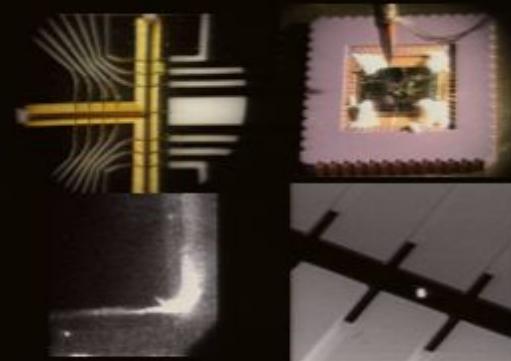
$\sim 1$  m

# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)
- Shuttling ions through advanced scalable trap structures
- Nonlocal entanglement through spontaneous emission (photons)



$\sim 10^{-6}$  m



$\sim 10^{-3}$  m

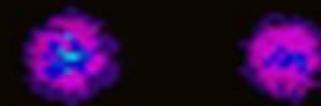


$\sim 1$  m

# Ion Trap Quantum Networks

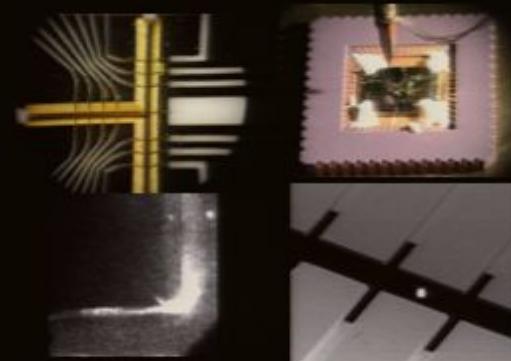
---

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

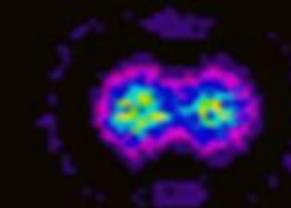
- Nonlocal entanglement through spontaneous emission (photons)



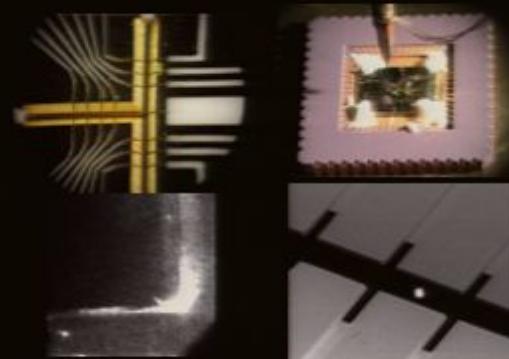
$\sim 1$  m

# Ion Trap Quantum Networks

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$\sim 10^{-6}$  m



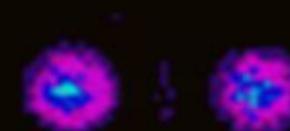
$\sim 10^{-3}$  m



$\sim 1$  m

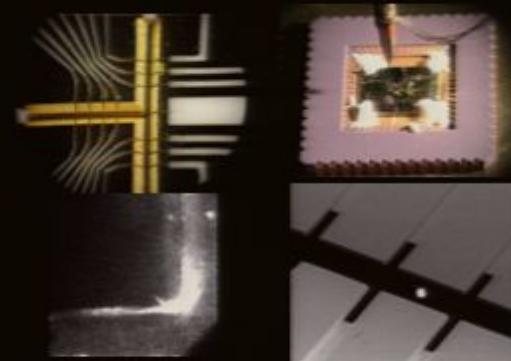
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

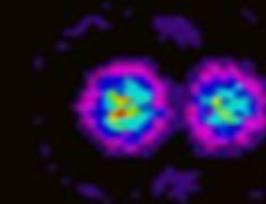
- Nonlocal entanglement through spontaneous emission (photons)



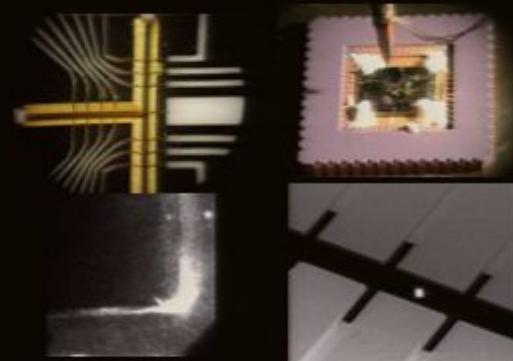
$\sim 1$  m

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$\sim 10^{-6}$  m



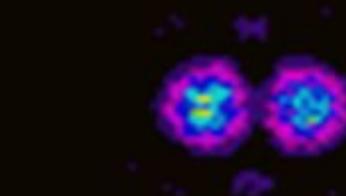
$\sim 10^{-3}$  m



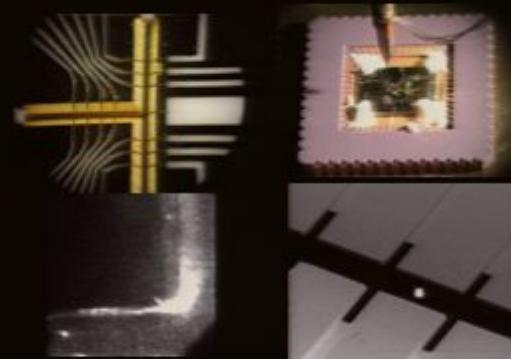
$\sim 1$  m

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$\sim 10^{-6}$  m



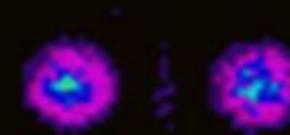
$\sim 10^{-3}$  m



$\sim 1$  m

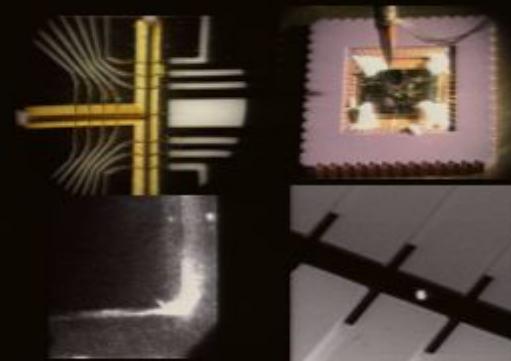
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

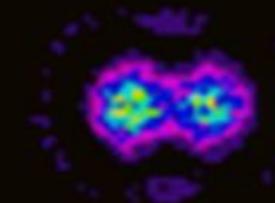
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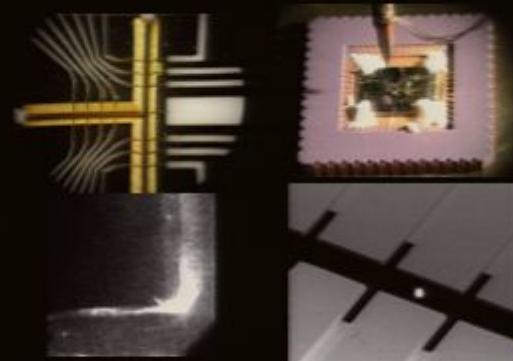
$\sim 1$  m

# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)
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$\sim 10^{-6}$  m



$\sim 10^{-3}$  m

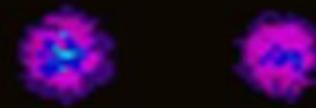


$\sim 1$  m

# Ion Trap Quantum Networks

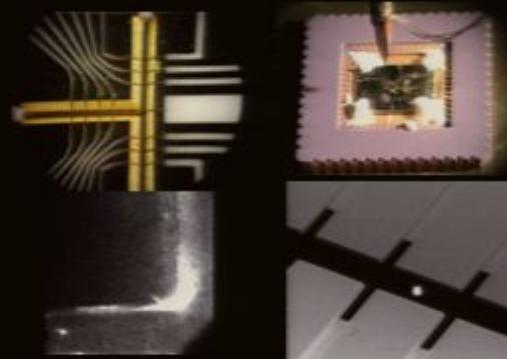
---

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

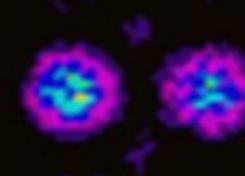
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$\sim 1$  m

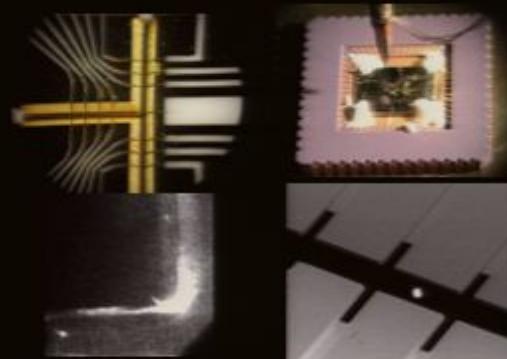
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

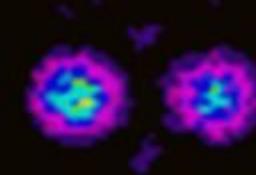
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$\sim 1$  m

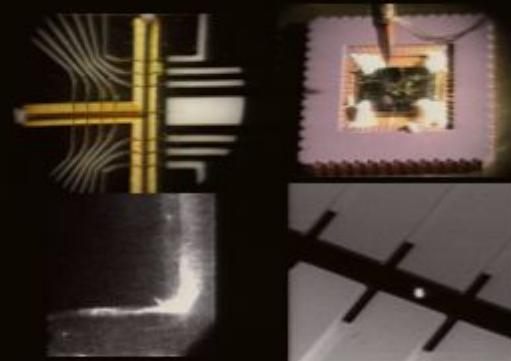
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

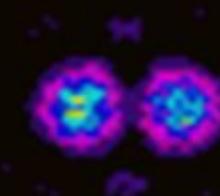
- Nonlocal entanglement through spontaneous emission (photons)



$\sim 1$  m

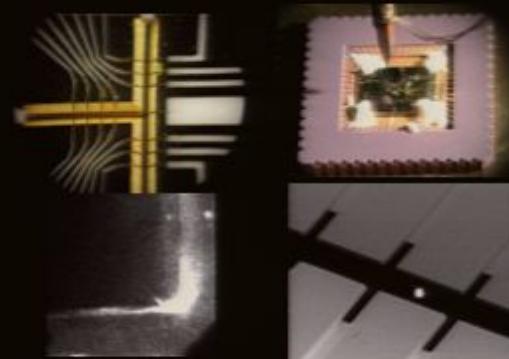
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

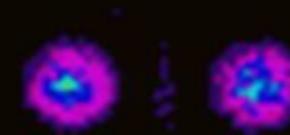
- Nonlocal entanglement through spontaneous emission (photons)



$\sim 1$  m

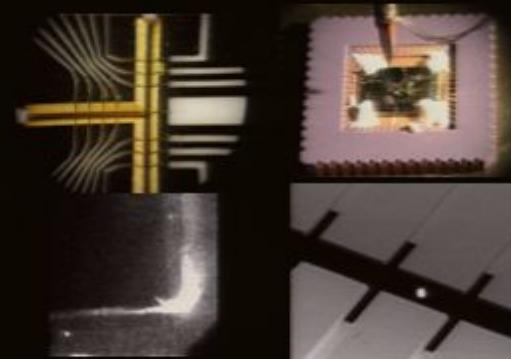
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$\sim 10^{-6}$  m

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$\sim 10^{-3}$  m

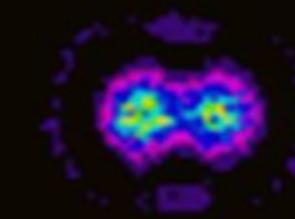
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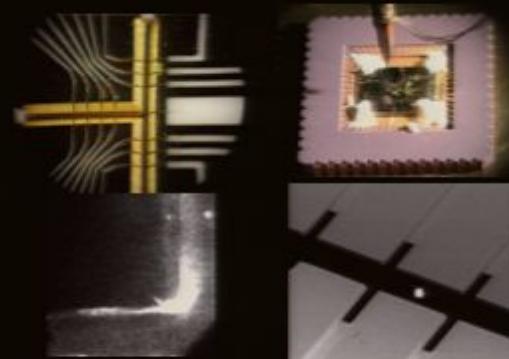
$\sim 1$  m

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$\sim 10^{-6}$  m



$\sim 10^{-3}$  m

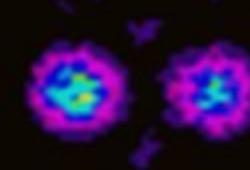


$\sim 1$  m

# Ion Trap Quantum Networks

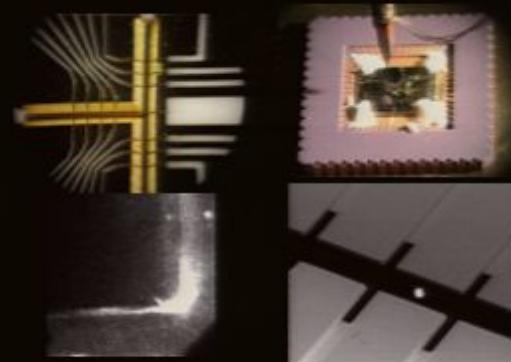
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$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

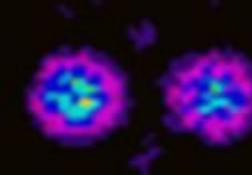
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$\sim 1$  m

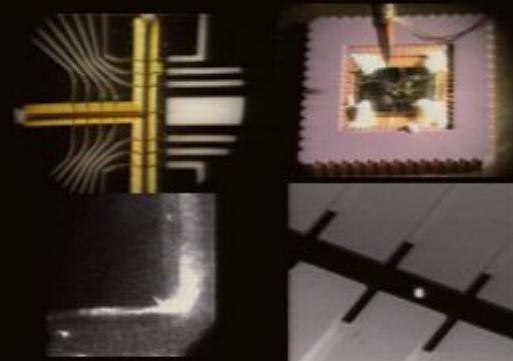
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$\sim 10^{-6}$  m

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$\sim 10^{-3}$  m

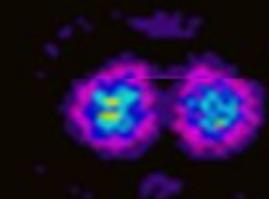
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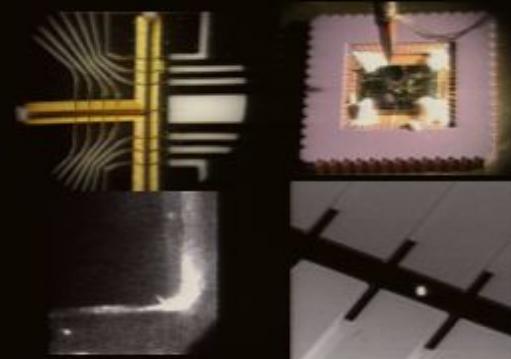
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



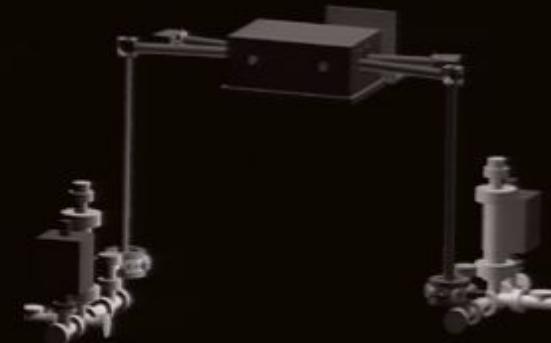
$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

- Nonlocal entanglement through spontaneous emission (photons)



$\sim 1$  m

# Ion Trap Quantum Networks

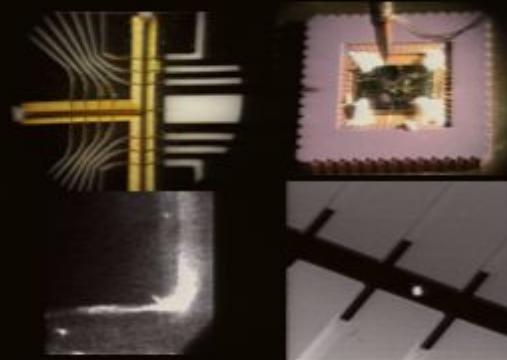
---

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

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$\sim 10^{-3}$  m

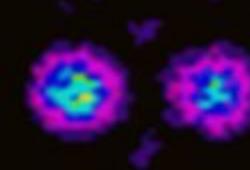
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$\sim 1$  m

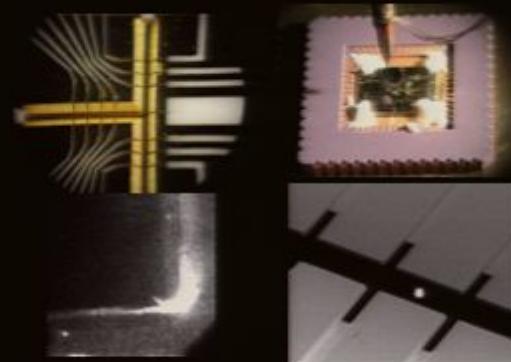
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$\sim 10^{-6}$  m

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$\sim 10^{-3}$  m

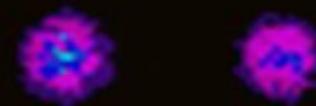
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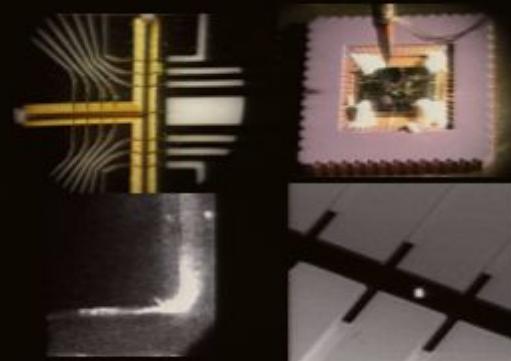
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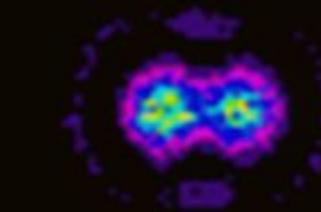
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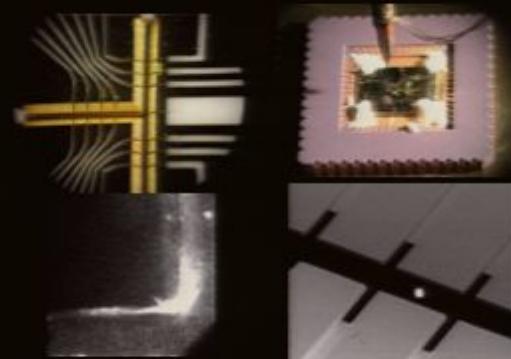
$\sim 1$  m

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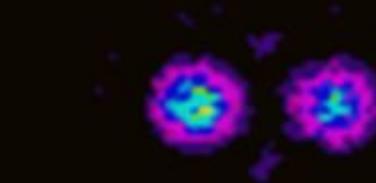
$\sim 10^{-3}$  m



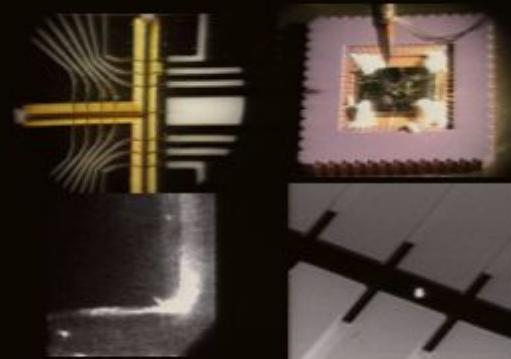
$\sim 1$  m

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$\sim 10^{-6}$  m



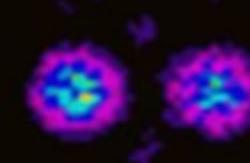
$\sim 10^{-3}$  m



$\sim 1$  m

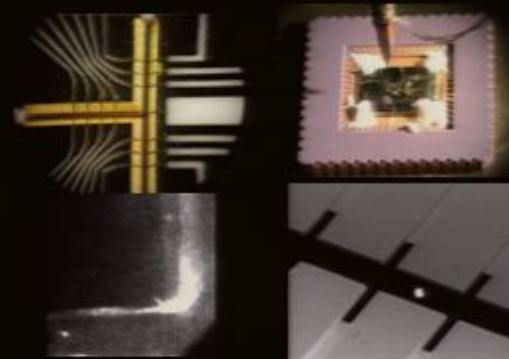
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$\sim 10^{-3}$  m

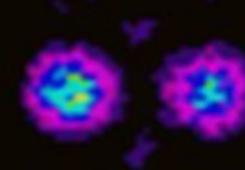
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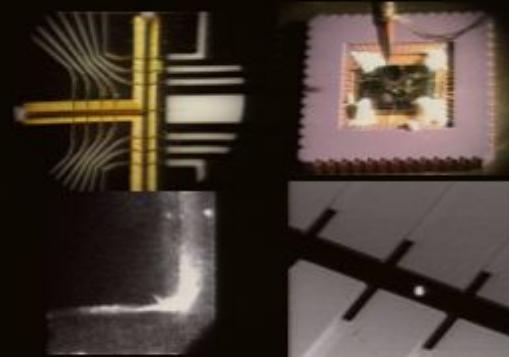
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$\sim 10^{-3}$  m

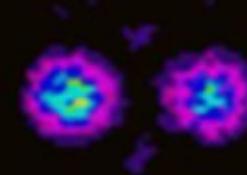
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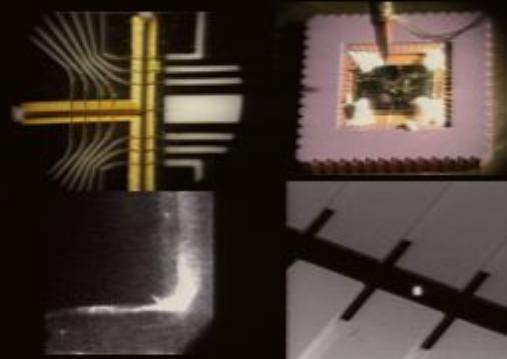
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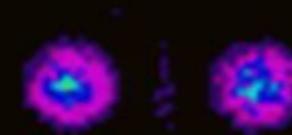
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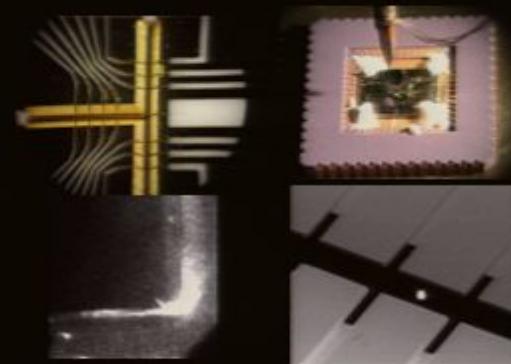
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$\sim 10^{-3}$  m

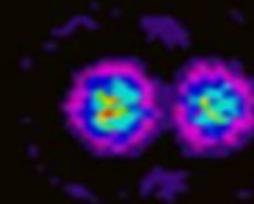
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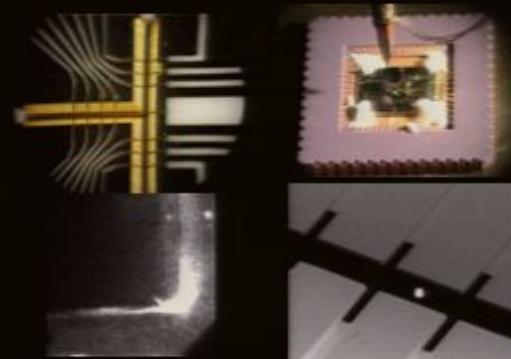
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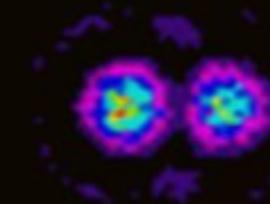
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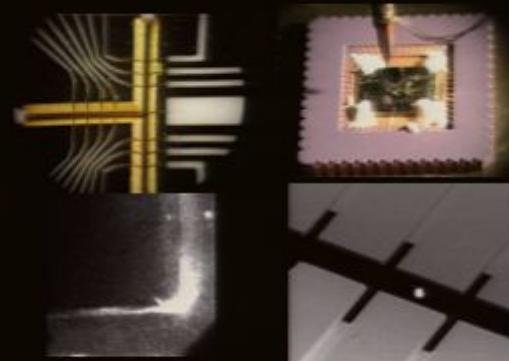
$\sim 1$  m

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$\sim 10^{-6}$  m



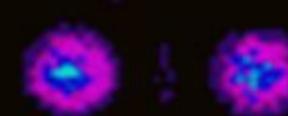
$\sim 10^{-3}$  m



$\sim 1$  m

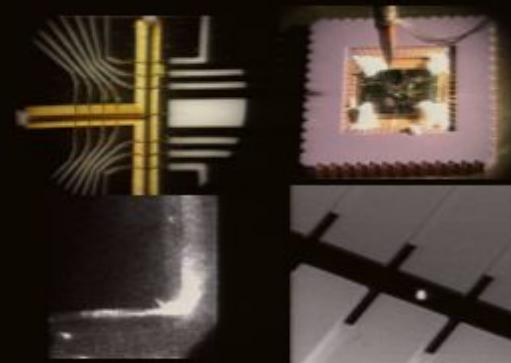
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$\sim 10^{-6}$  m

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$\sim 10^{-3}$  m

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$\sim 1$  m

# Cirac-Zoller Trapped Ion QC



# Cirac-Zoller Trapped Ion QC



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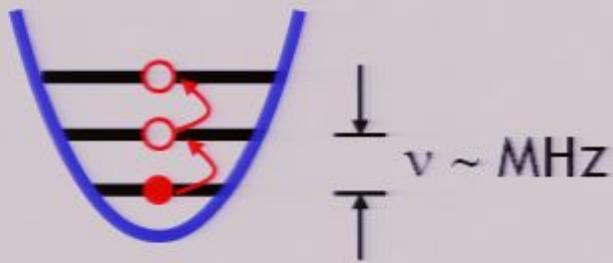
# Cirac-Zoller Trapped Ion QC



# Cirac-Zoller Trapped Ion QC

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## Decoherence of C.O.M. motion



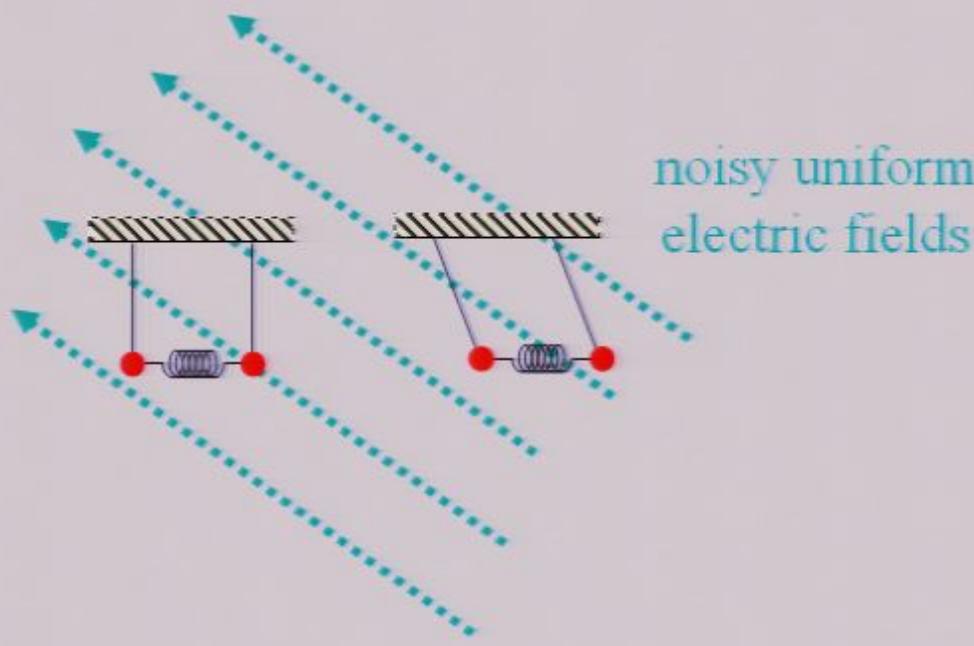
$$\gamma = d\langle n \rangle / dt$$

expect  $\gamma \sim 1 \text{ sec}^{-1}$  (blackbody rad.)

measure  $\gamma \sim 10^2 - 10^5 \text{ sec}^{-1}$

COM mode at  $\omega$

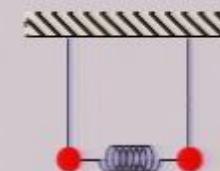
$$x_{\text{COM}} = x_1 + x_2$$



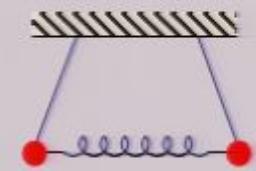
noisy uniform  
electric fields

“Stretch” mode at  $\omega\sqrt{3}$

$$x_{\text{STR}} = x_1 - x_2$$



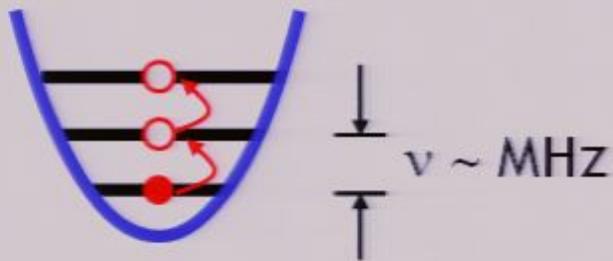
logical 0



logical 1

A decoherence-free  
subspace!

## Decoherence of C.O.M. motion



$$\gamma = d\langle n \rangle / dt$$

expect  $\gamma \sim 1 \text{ sec}^{-1}$  (blackbody rad.)

measure  $\gamma \sim 10^2 - 10^5 \text{ sec}^{-1}$

# Cirac-Zoller Trapped Ion QC



Internal states of these ions entangled

# Cirac-Zoller Trapped Ion QC



# Cirac-Zoller Trapped Ion QC



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# Cirac-Zoller Trapped Ion QC



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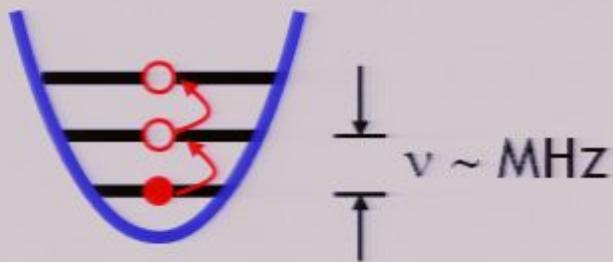
# Cirac-Zoller Trapped Ion QC



# Cirac-Zoller Trapped Ion QC



## Decoherence of C.O.M. motion



$$\gamma = d\langle n \rangle / dt$$

expect  $\gamma \sim 1 \text{ sec}^{-1}$  (blackbody rad.)

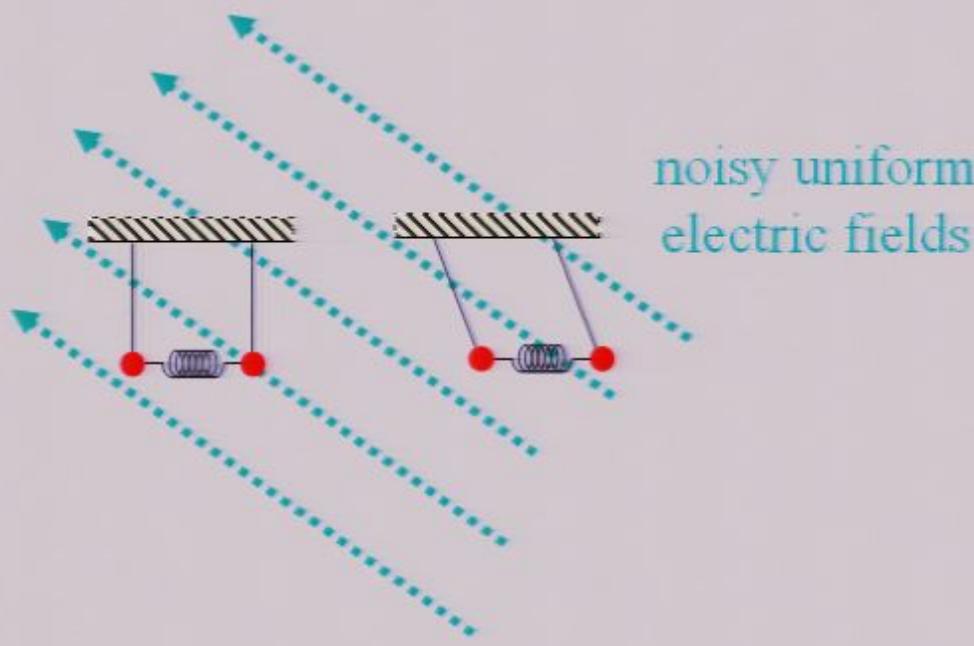
measure  $\gamma \sim 10^2 - 10^5 \text{ sec}^{-1}$

# Cirac-Zoller Trapped Ion QC



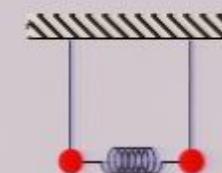
COM mode at  $\omega$

$$x_{\text{COM}} = x_1 + x_2$$

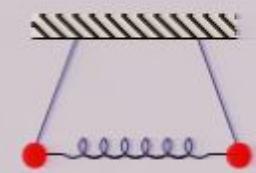


"Stretch" mode at  $\omega\sqrt{3}$

$$x_{\text{STR}} = x_1 - x_2$$



logical 0

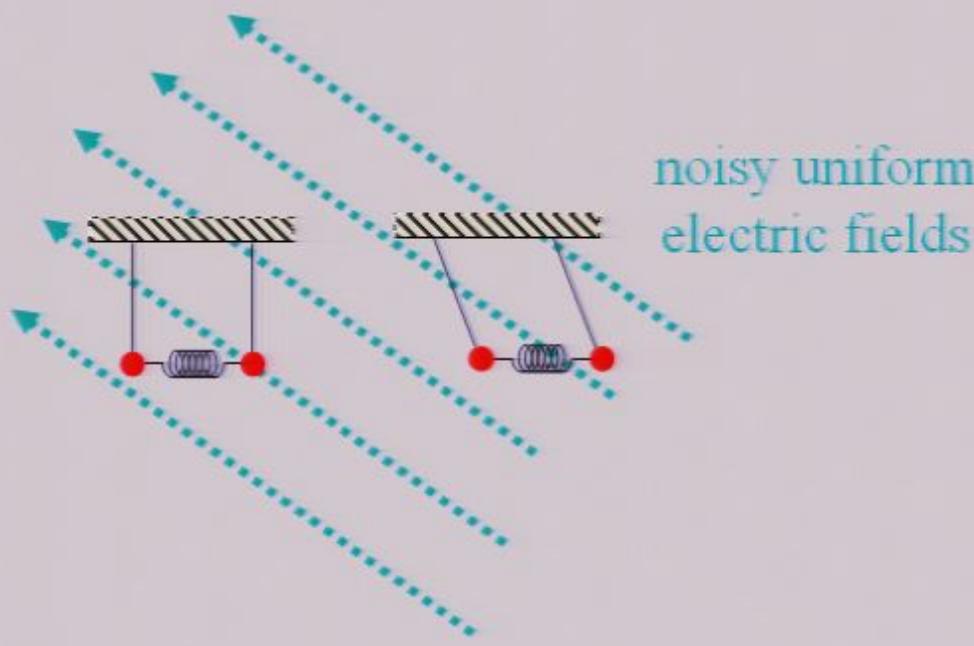


logical 1

A decoherence-free  
subspace!

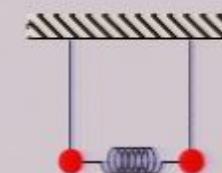
COM mode at  $\omega$

$$x_{\text{COM}} = x_1 + x_2$$

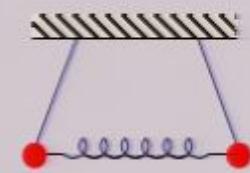


"Stretch" mode at  $\omega\sqrt{3}$

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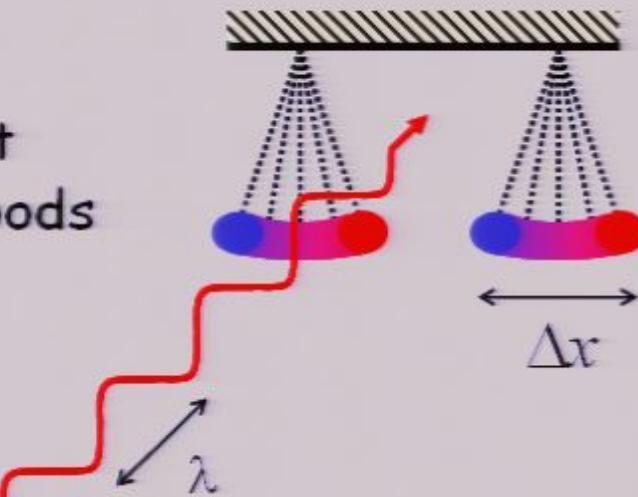
logical 0



logical 1

A decoherence-free  
subspace!

... but still not  
out of the woods



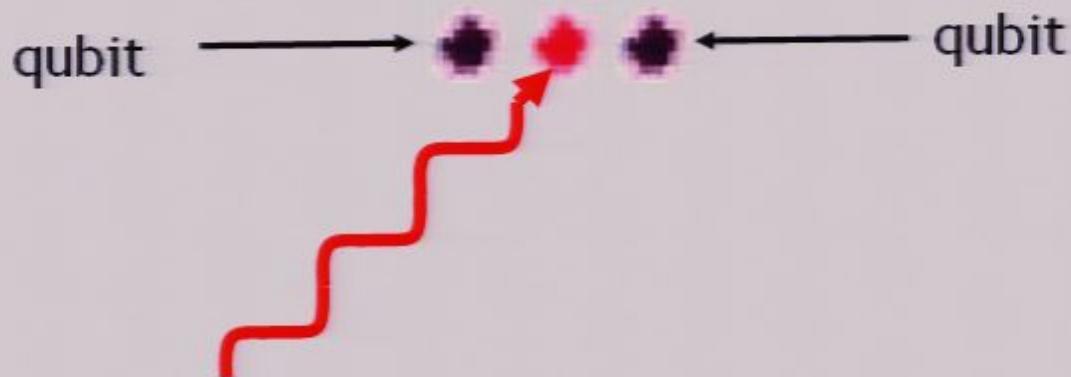
$x_{\text{STR}}$  fixed;  $x_{\text{COM}}$  random

$\Rightarrow e^{-(\Delta x/\lambda)^2}$  gate fidelity

Debye-Waller effect

“ion-in-the-middle” sympathetic laser cooling:

quench heating without disturbing internal state  
OR symmetric stretch mode

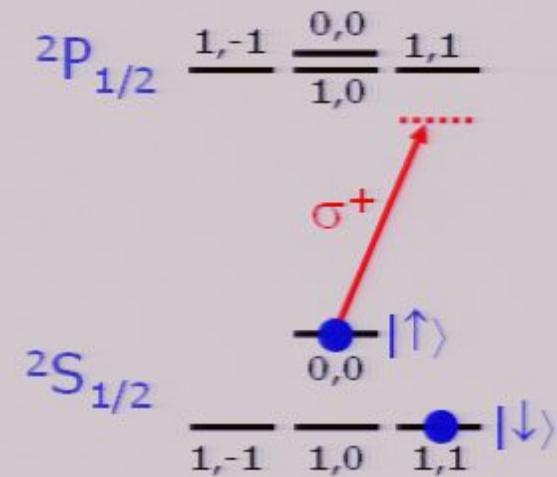


continuous cooling of middle ion  
eliminates C.O.M. heating from uniform fields  
(tight focusing, or different species)

## BETTER: Indirect use of motion for quantum gates

spin-dependent force:

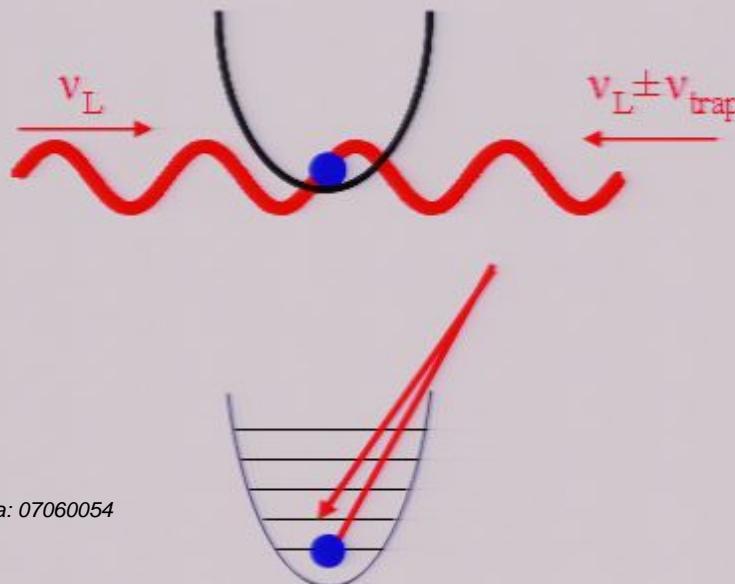
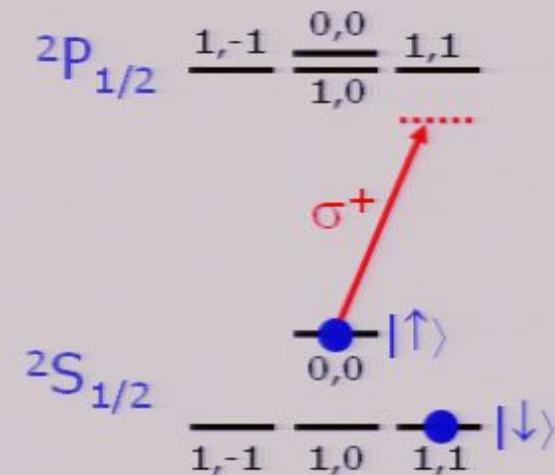
$$\text{Force} = F_0 |\uparrow \times \uparrow|$$



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spin-dependent force:

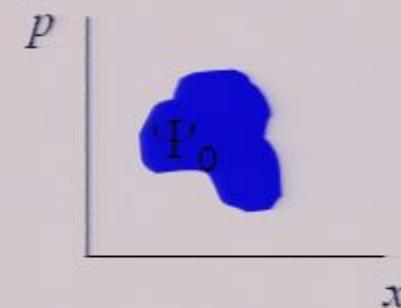
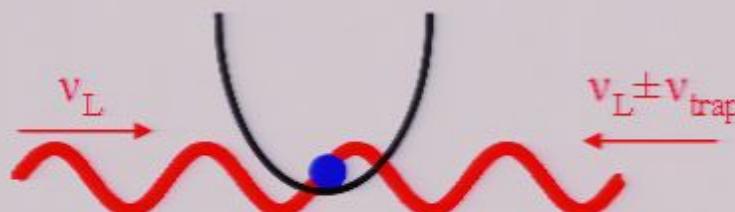
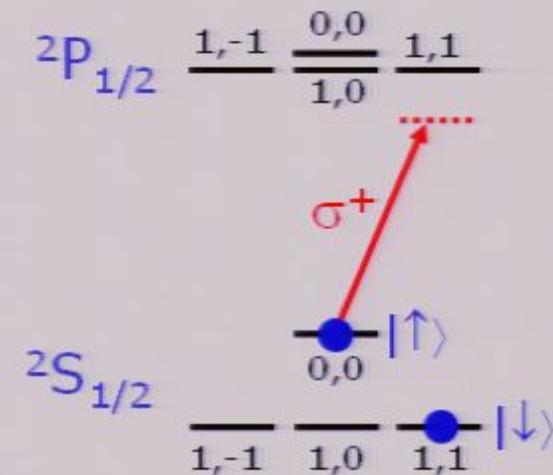
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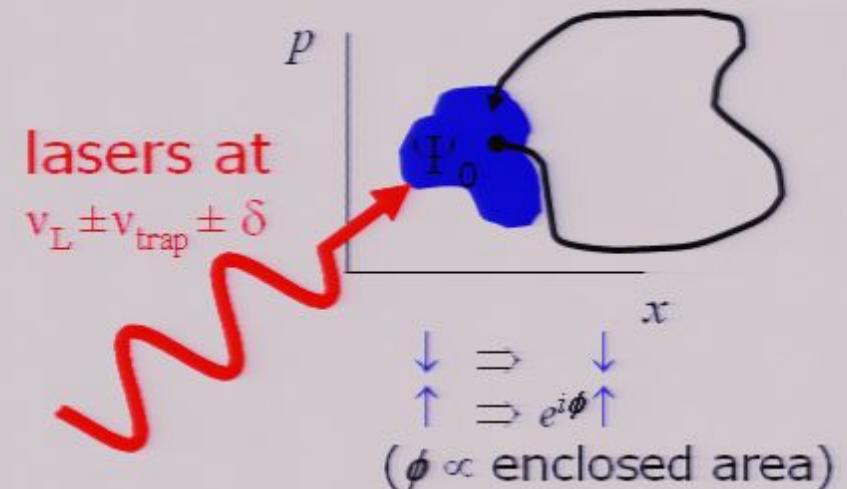
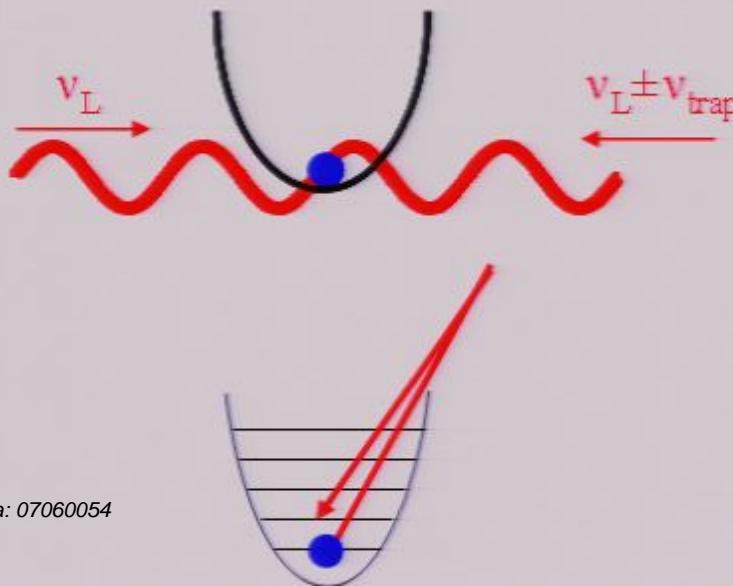
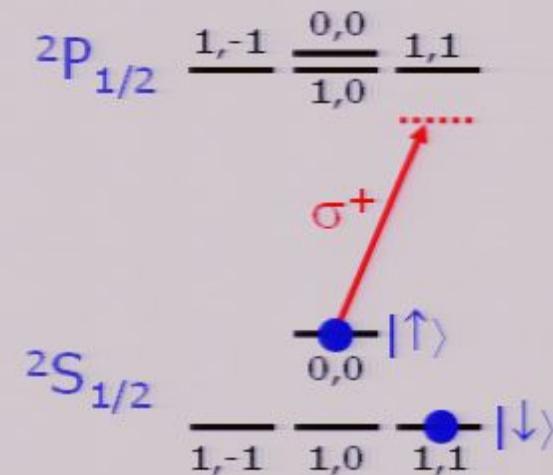
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# BETTER: Indirect use of motion for quantum gates

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N=2 ions

e.g., force on stretch mode only



$$H = \hbar\Omega\hat{\sigma}_z^2$$

$$\begin{array}{lcl} \downarrow\downarrow & \Rightarrow & \downarrow\downarrow \\ \downarrow\uparrow & \Rightarrow & e^{i\phi}\downarrow\uparrow \\ \uparrow\downarrow & \Rightarrow & e^{i\phi}\uparrow\downarrow \\ \uparrow\uparrow & \Rightarrow & \uparrow\uparrow \end{array}$$

$\phi = \pi/2$ :  $\pi$ -phase gate

Mølmer and Sørensen, PRL **82**, 1835 (1999)

Solano, de Matos Filho, Zagury, PRA **59**, R2539 (1999)

Milburn, Schneider, James, Fortschr. Phys. (2000)

Leibfried *et al.*, Nature **422**, 412 (2003)

Lucas, Steane, *et al.* (2005)

← F=97%

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$F=97\%$

N=6 ions

$$\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow + \downarrow\downarrow\downarrow\downarrow\downarrow\downarrow$$

Leibfried *et al.*, Nature **438**, 639-642 (2005)

Problem with  $\sigma_z \sigma_z$  gates:

With "clock" state qubits  
(no differential Zeeman shift),...

cannot realize a spin-dependent force  
(no differential AC Stark shift)

P. J. Lee, et al., Journal of Optics B 7, S371 (2005).

Solution: do  $\sigma_x \sigma_x$  gates instead!

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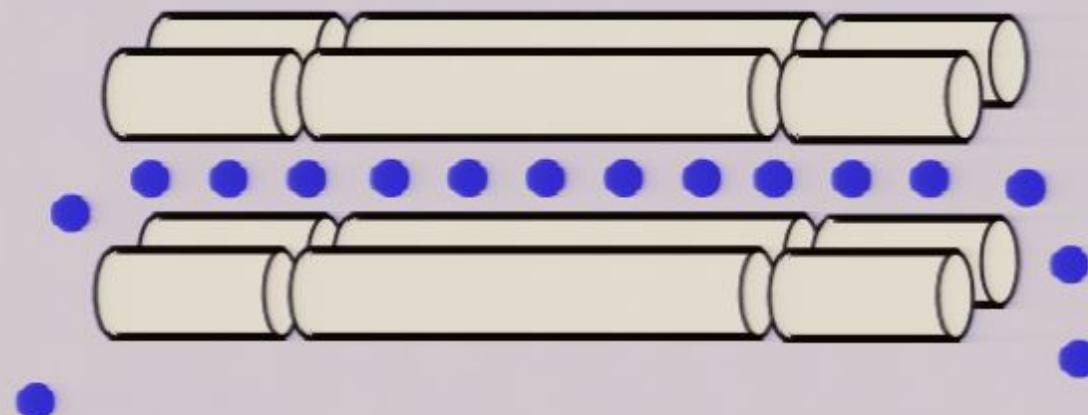
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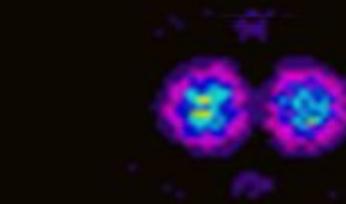
Haljan, et al., PRL 94, 153602 (2005); PRA 72, 062316 (2005)

# Scale up?

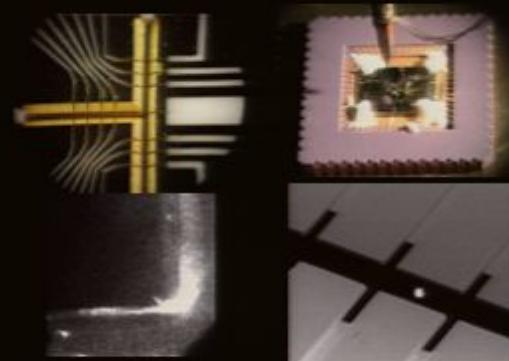


# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)
- Shuttling ions through advanced scalable trap structures
- Nonlocal entanglement through spontaneous emission (photons)



$\sim 10^{-6}$  m



$\sim 10^{-3}$  m

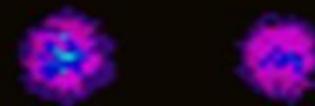


$\sim 1$  m

# Ion Trap Quantum Networks

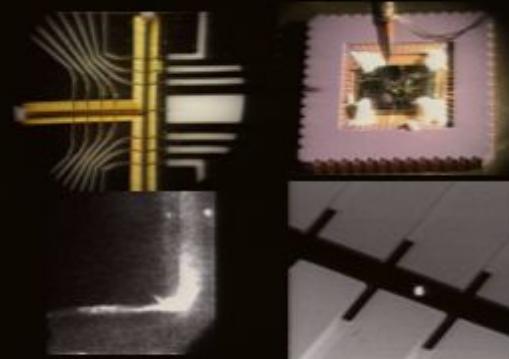
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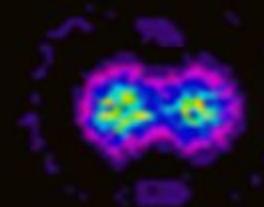


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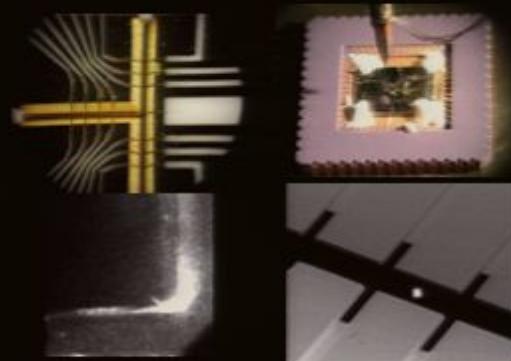
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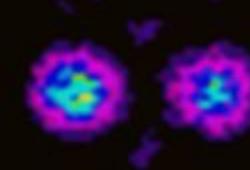
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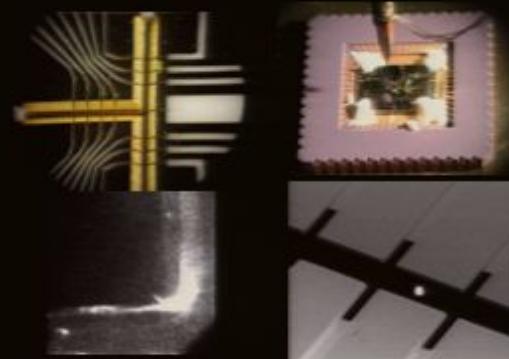
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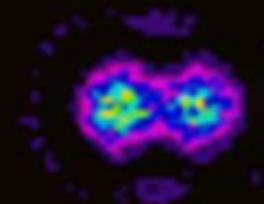


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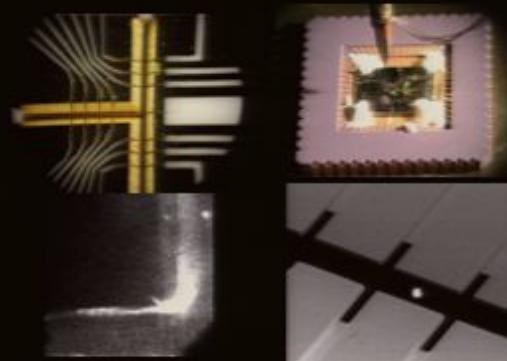
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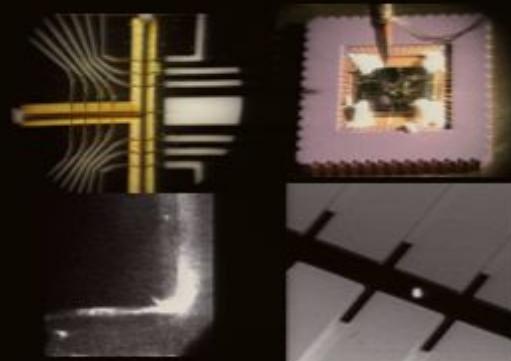
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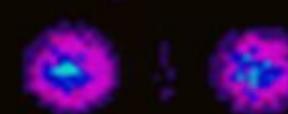
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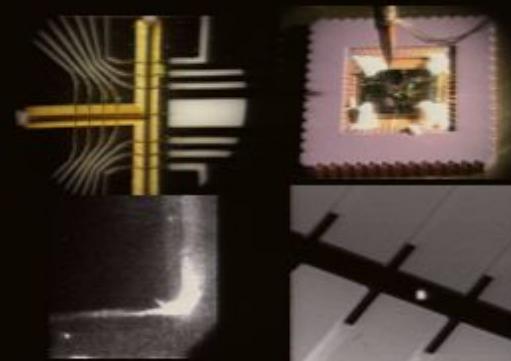
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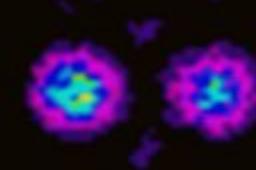
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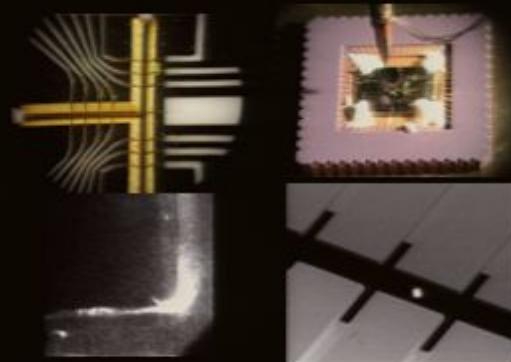
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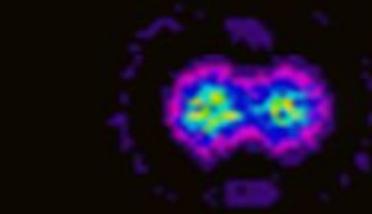
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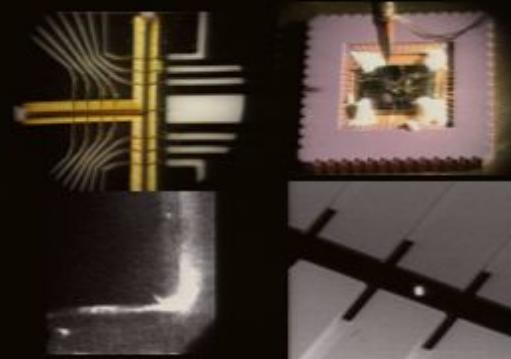
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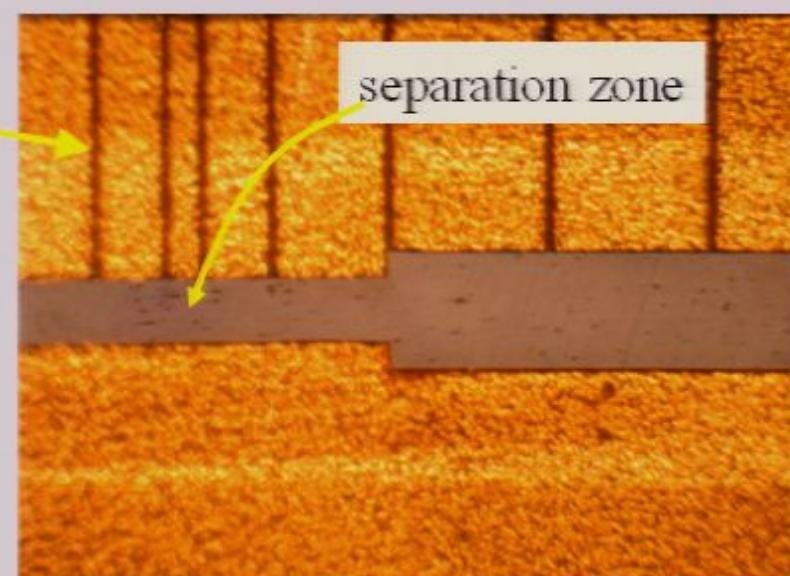
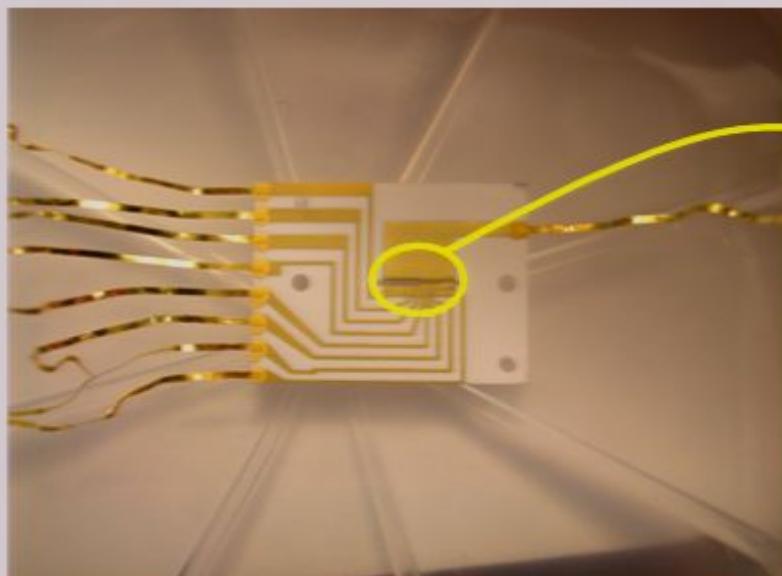
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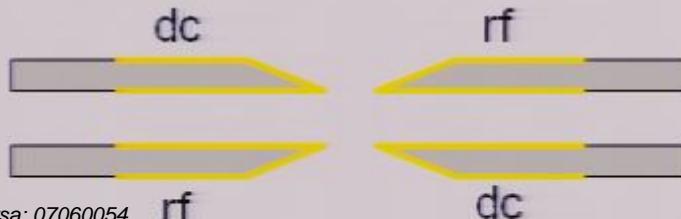
$\sim 1$  m

# (6-zone) alumina/gold trap

(D. Wineland, et al., NIST-Boulder)



view along axis:



## Multiqubit operations

- teleportation
- 3-qubit phase noise error correction
- FFT
- entanglement purification



68%

Trebuchet MS

20

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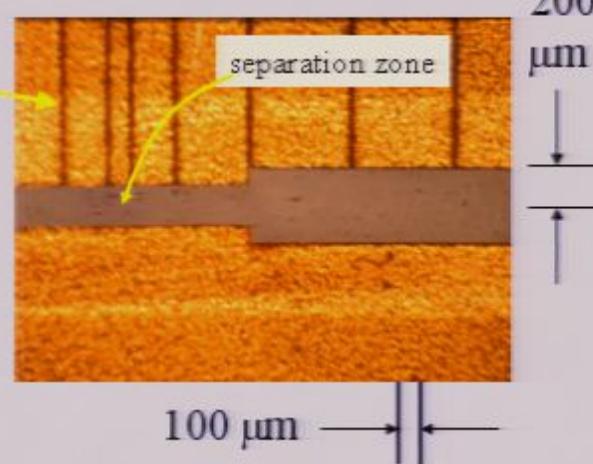
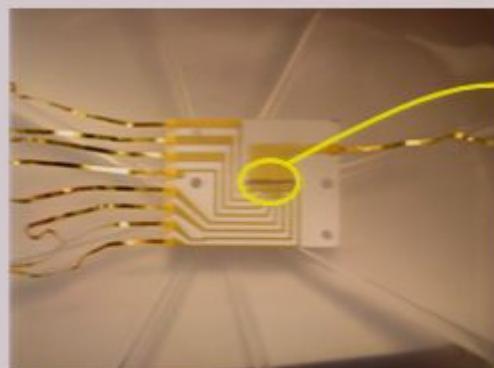


Design New Slide

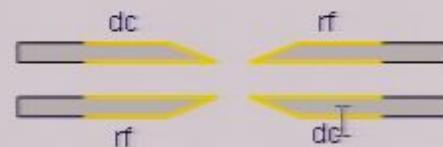
5 ······ 4 ······ 3 ······ 2 ······ 1 ······ 0 ······ 1 ······ 2 ······ 3 ······ 4 ······

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view along axis:



### Multiqubit operations

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- FFT
- entanglement purification
- ...

# Windows Media Player



File View Play Tools Help

Windows Media Player

Now Playing Library Rip Burn Sync Guide

Music Radio



Now Playing List

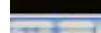
ike2 0:21



Total Time: 0...



ike2



Pista: 07060054



Stopped

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# Windows Media Player



File View Play Tools Help

Windows Media Player

Now Playing Library Rip Burn Sync Guide

Music Radio



Now Playing List

ike2

0:21



Total Time: 0...



## Wireless Network Connection

This connection has limited or no connectivity. You might not be able to access the Internet or some network resources. For more information, click this message.

Pista: 07060054

Stopped

Page 125/189

# Windows Media Player



File View Play Tools Help

Windows Media Player

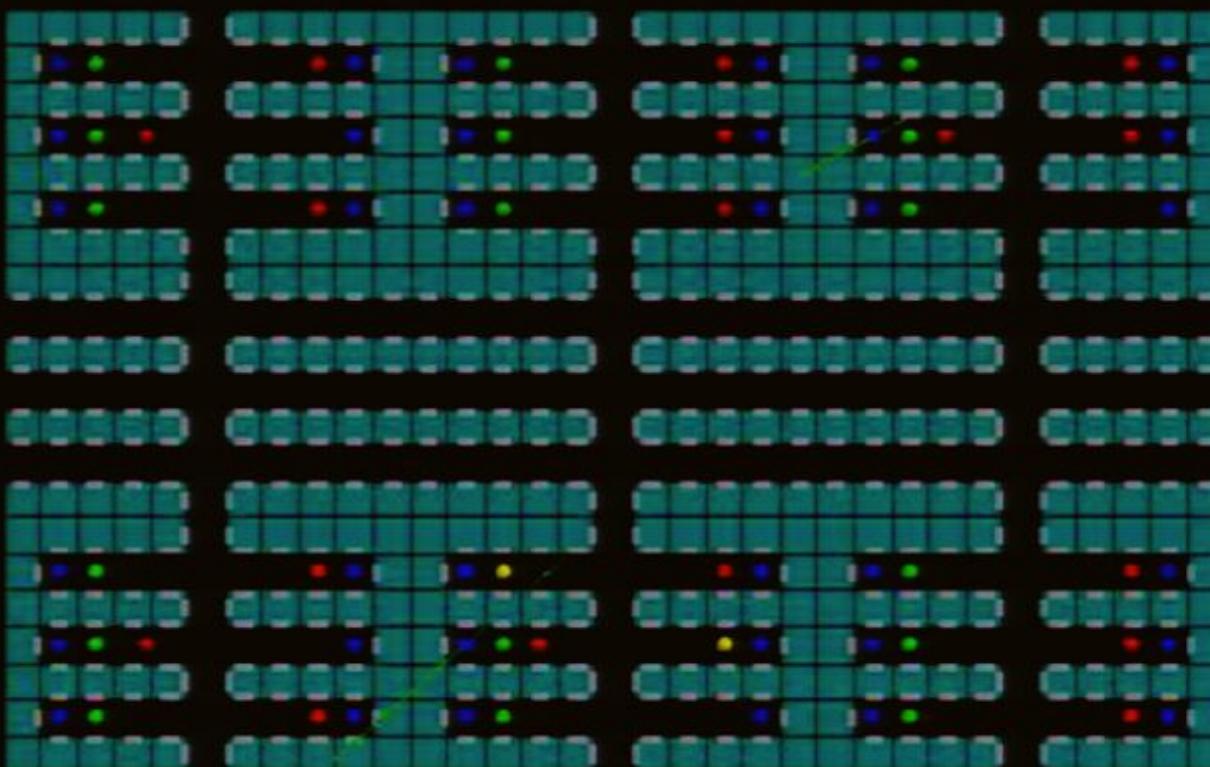
Now Playing Library Rip Burn Sync Guide

Music Radio



Now Playing List

ike2 0:21



### Legend

- Data
- Ancilla
- Sympathetic
- Damaged

Time- 0.045222 s  
Errors-

X: 1 Z: 0

Total: 1

### Message:

Correcting Lower Level

### Action:

move

Total Time: 0...



ike2

### Wireless Network Connection

This connection has limited or no connectivity. You might not be able to access the Internet or some network resources. For more information, click this message.

Pirsa: 07060054

Playlist Playlist1

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# Windows Media Player



File View Play Tools Help

Windows Media Player

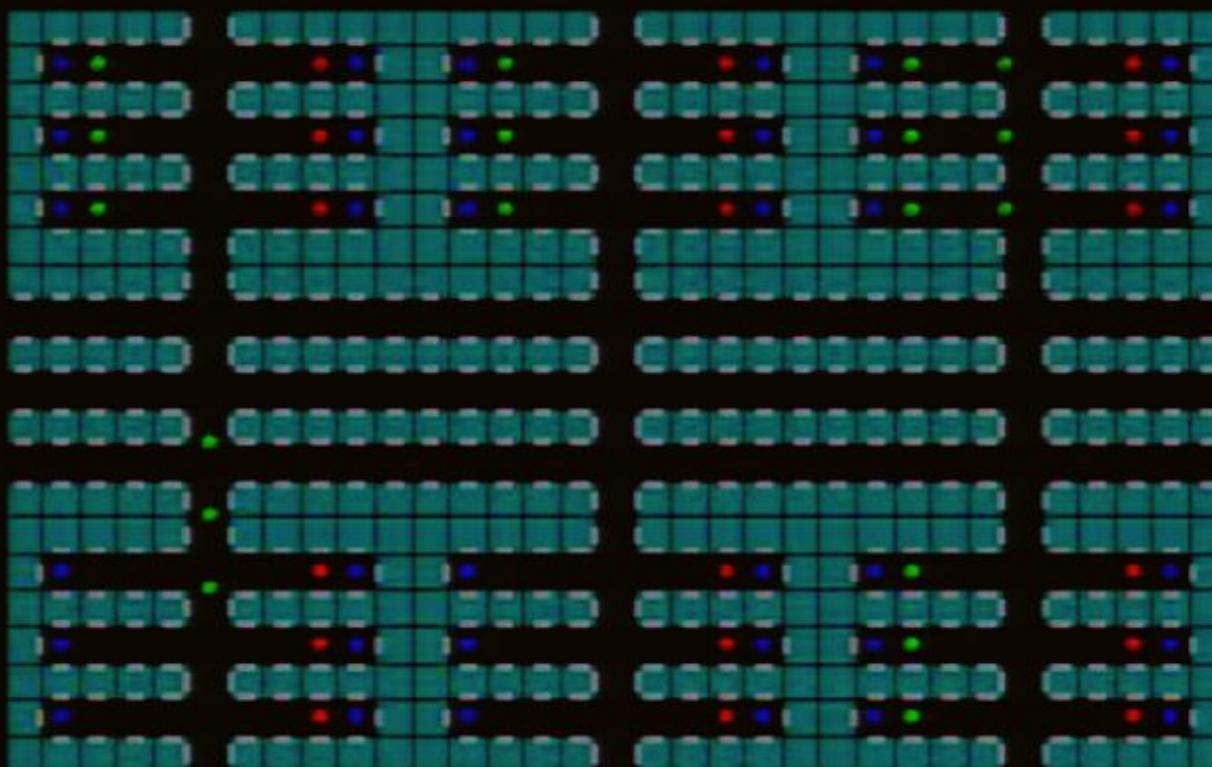
Now Playing Library Rip Burn Sync Guide

Music Radio



Now Playing List

ike2 0:21



## Legend

- Data
- Ancilla
- Sympathetic
- Damaged

Time- 0.012111 s  
Errors-

X: 0 Z: 0

Total: 0

## Message:

Connecting for ZWI

## Action:

move

Total Time: 0...



ike2

## Wireless Network Connection

This connection has limited or no connectivity. You might not be able to access the Internet or some network resources. For more information, click this message.

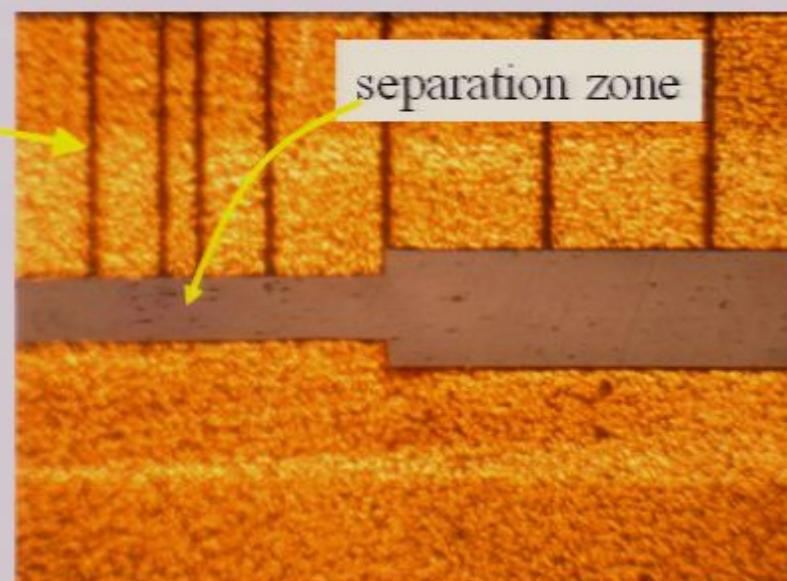
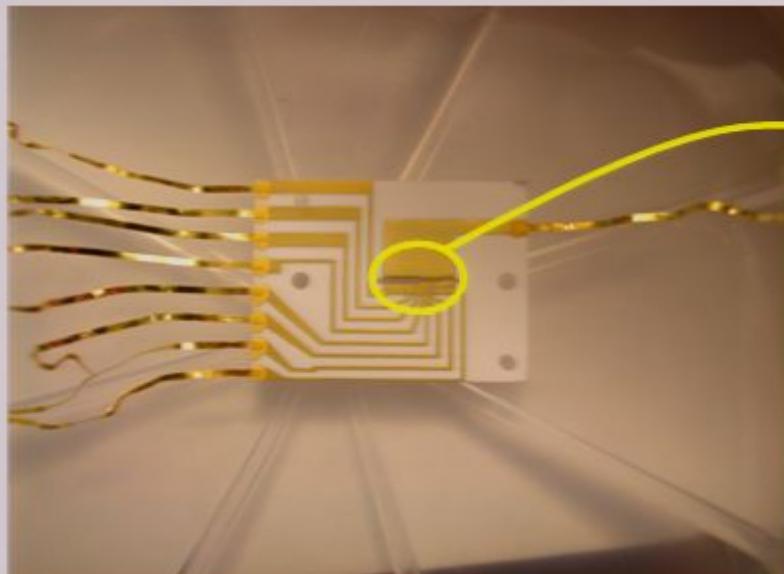
Pirosa: 07060054

Stopped

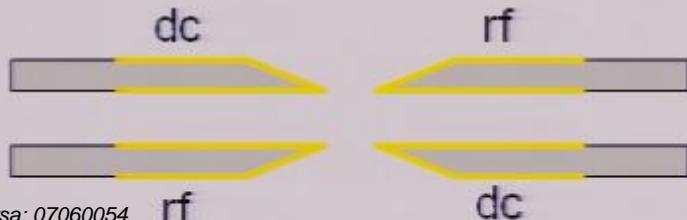
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(D. Wineland, et. al., NIST-Boulder)



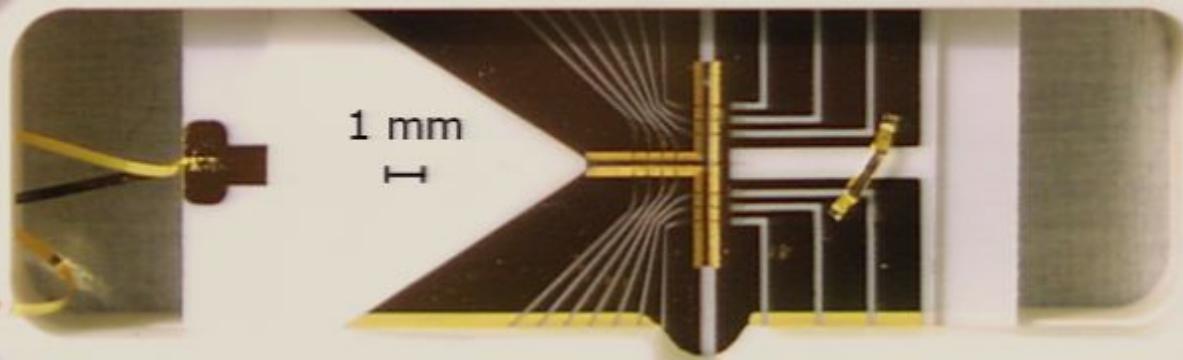
view along axis:



## Multiqubit operations

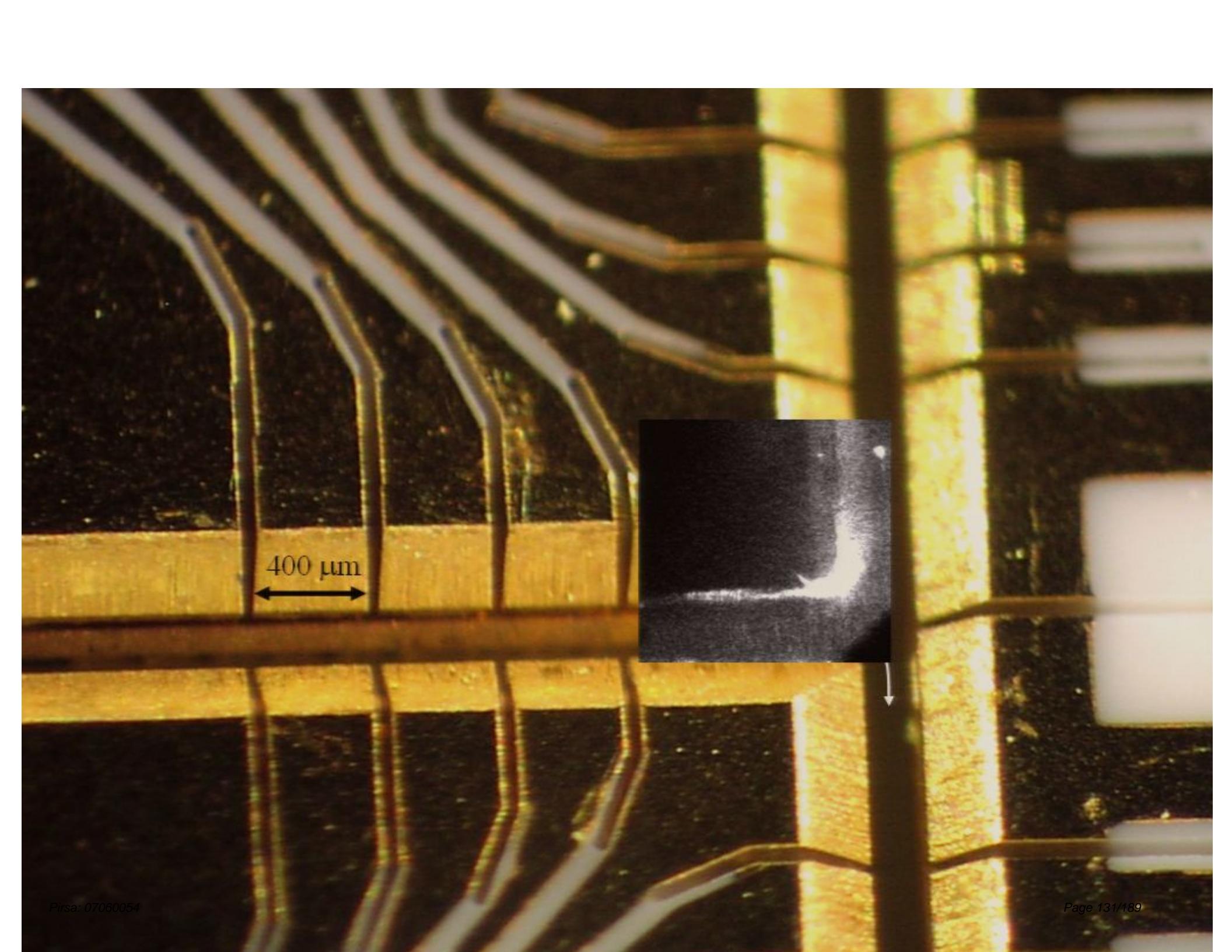
- teleportation
- 3-qubit phase noise error correction
- FFT
- entanglement purification

49-electrode, 10-zone  
“Tee” junction  
(W. Hensinger...)

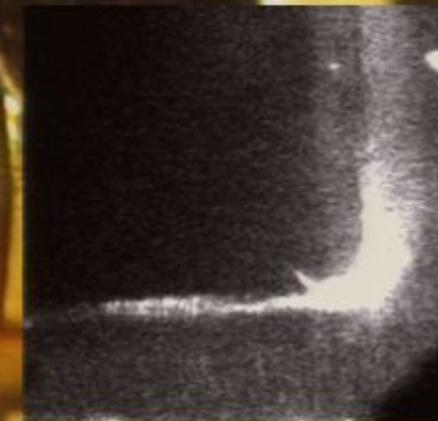


400  $\mu\text{m}$

A scanning electron micrograph showing a series of vertical, elongated, and slightly curved structures, likely gold-coated fibers or nanowires, arranged in a grid-like pattern. A horizontal double-headed arrow in the lower-left quadrant indicates a length of 400 micrometers. A white curly brace in the lower-right quadrant groups several of these structures together.



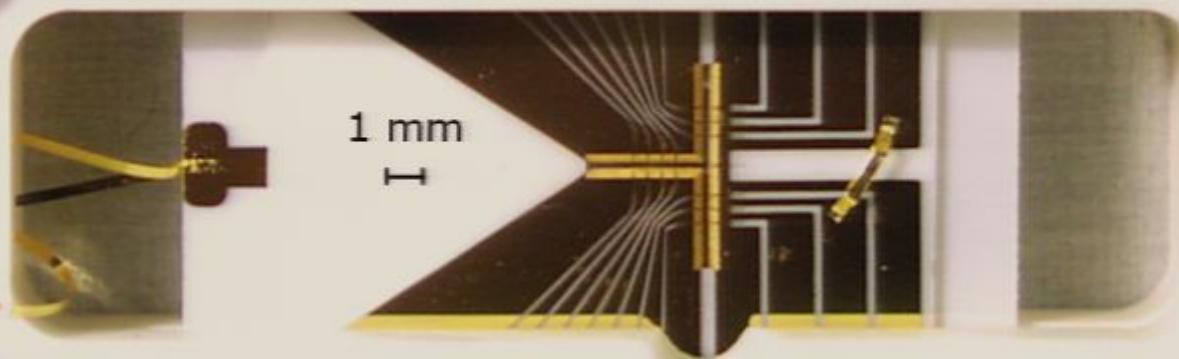
400  $\mu\text{m}$

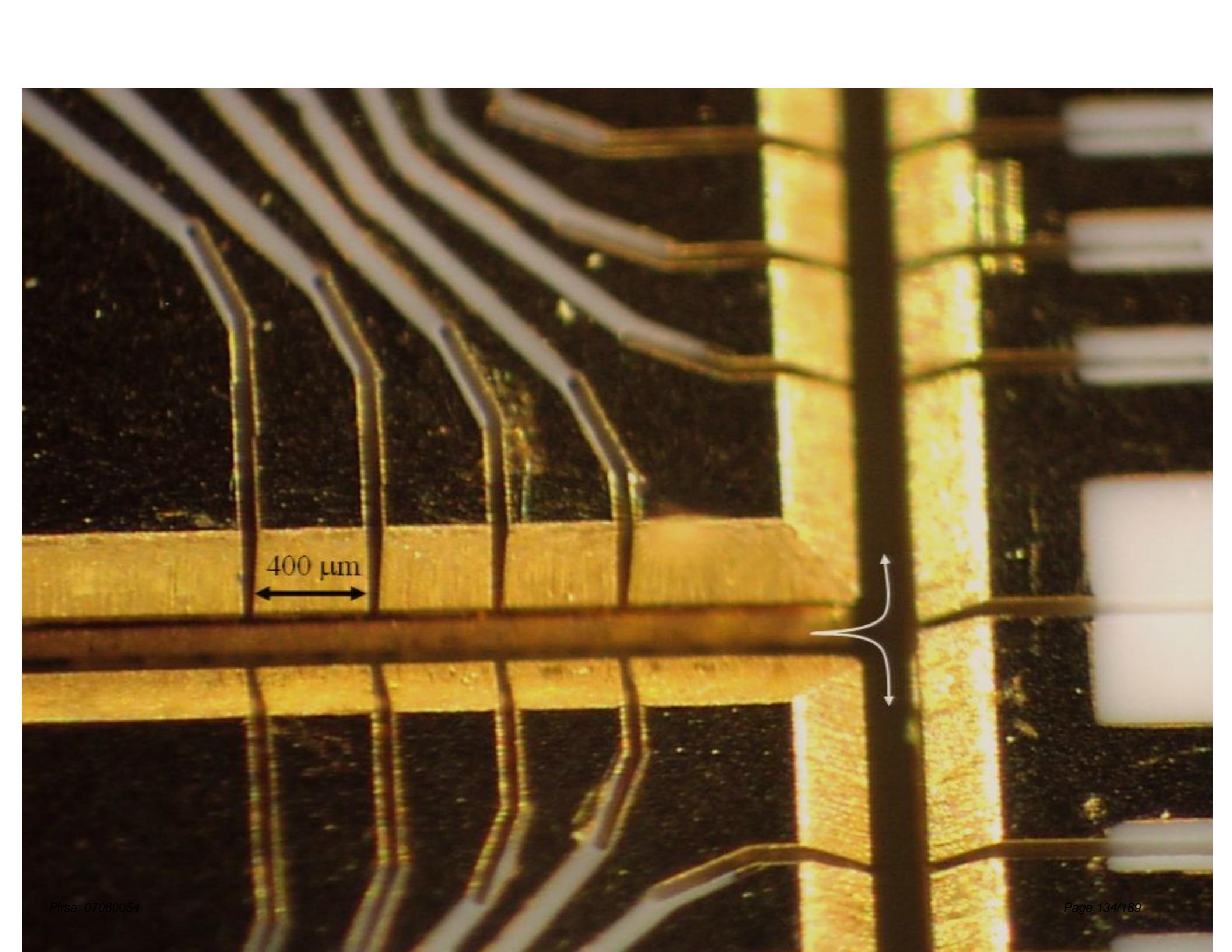


400  $\mu\text{m}$

A scanning electron micrograph showing a cross-section of a microfluidic device. The image features several parallel, curved, light-colored channels on a dark background. A horizontal double-headed arrow in the lower-left quadrant indicates a length of 400 micrometers. In the lower-right quadrant, there is a white curved arrow pointing clockwise, indicating a rotation or flow direction.

49-electrode, 10-zone  
“Tee” junction  
(W. Hensinger...)





400  $\mu\text{m}$

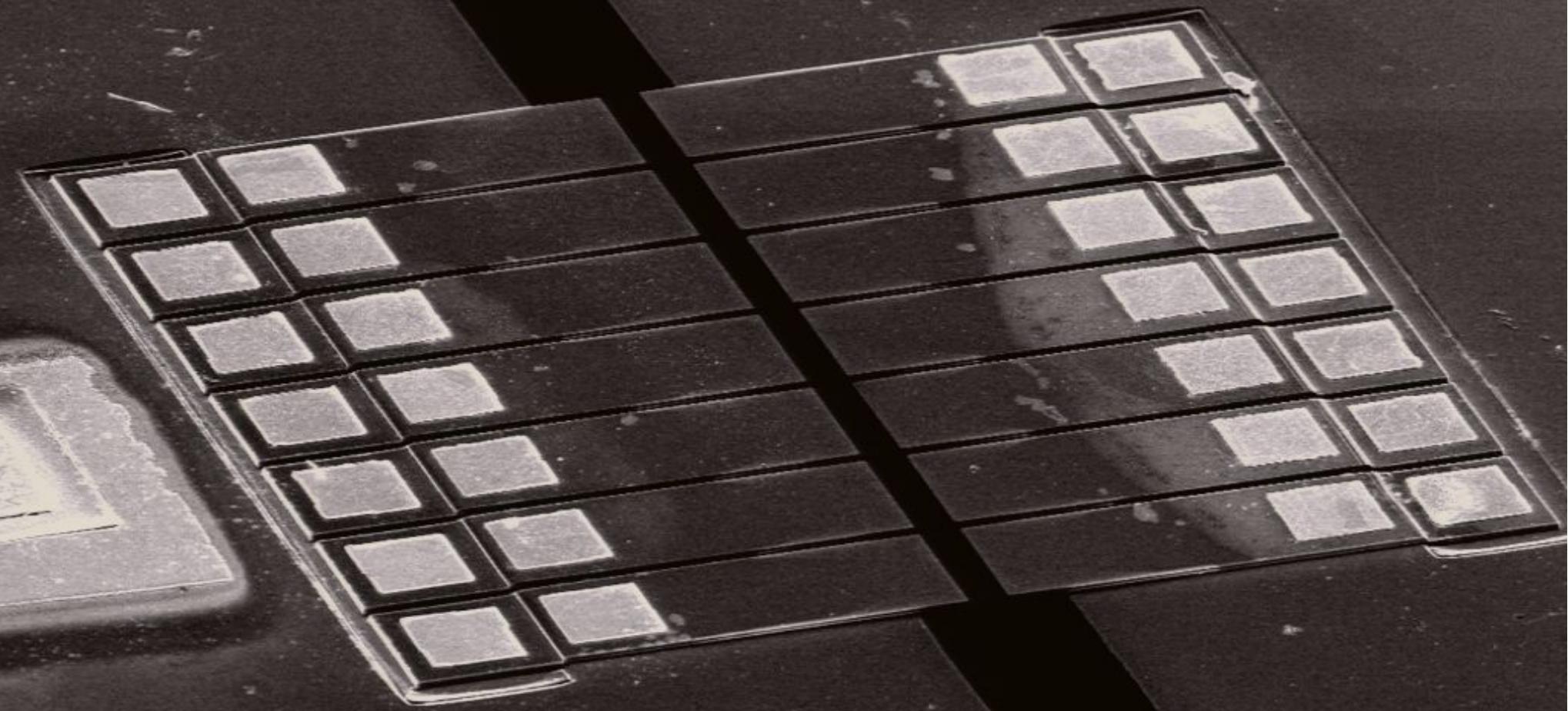


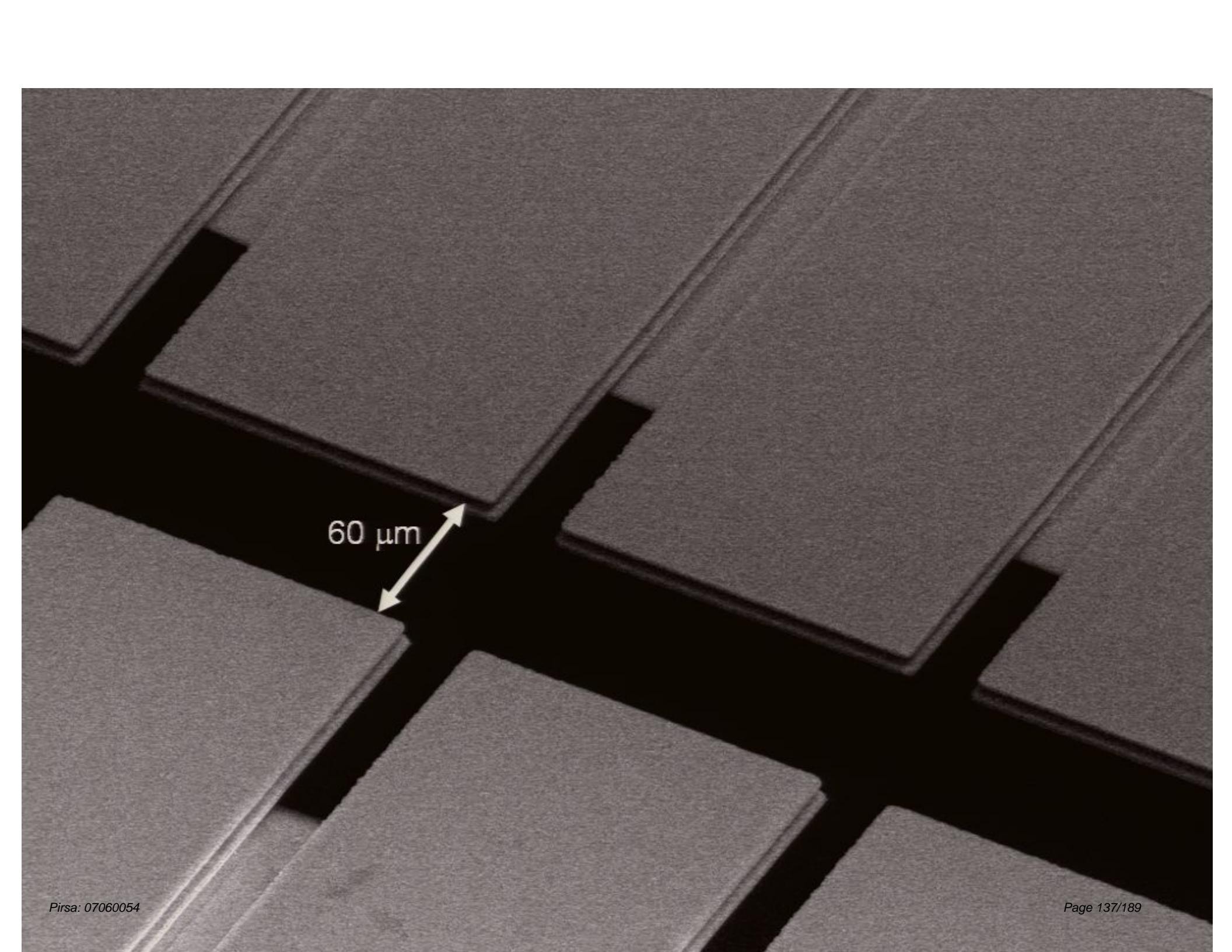
400  $\mu\text{m}$

A scanning electron micrograph showing a textured surface with vertical ridges and grooves. A scale bar in the lower-left corner indicates 400 micrometers. An inset image in the center-right shows a close-up view of the surface texture.

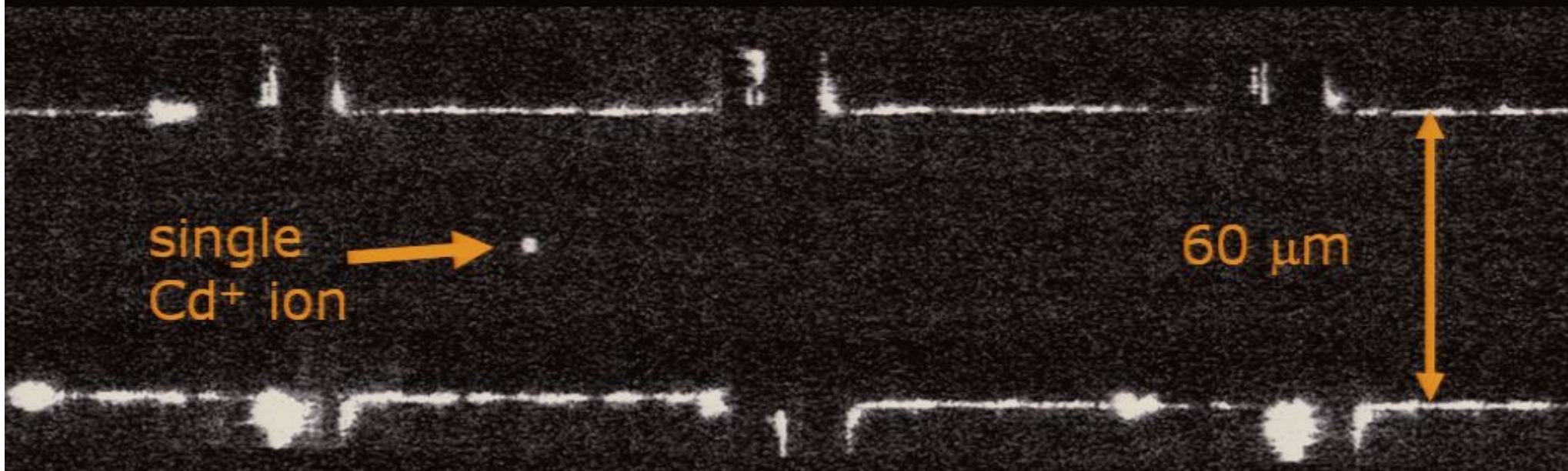
# GaAs Ion Trap

D. Stick, W. Hensinger, M. Madsen  
(Michigan and LPS/Maryland)





60  $\mu\text{m}$



$V_{RF} = 8V$  @ 16 MHz ( $Q \sim 50$ )

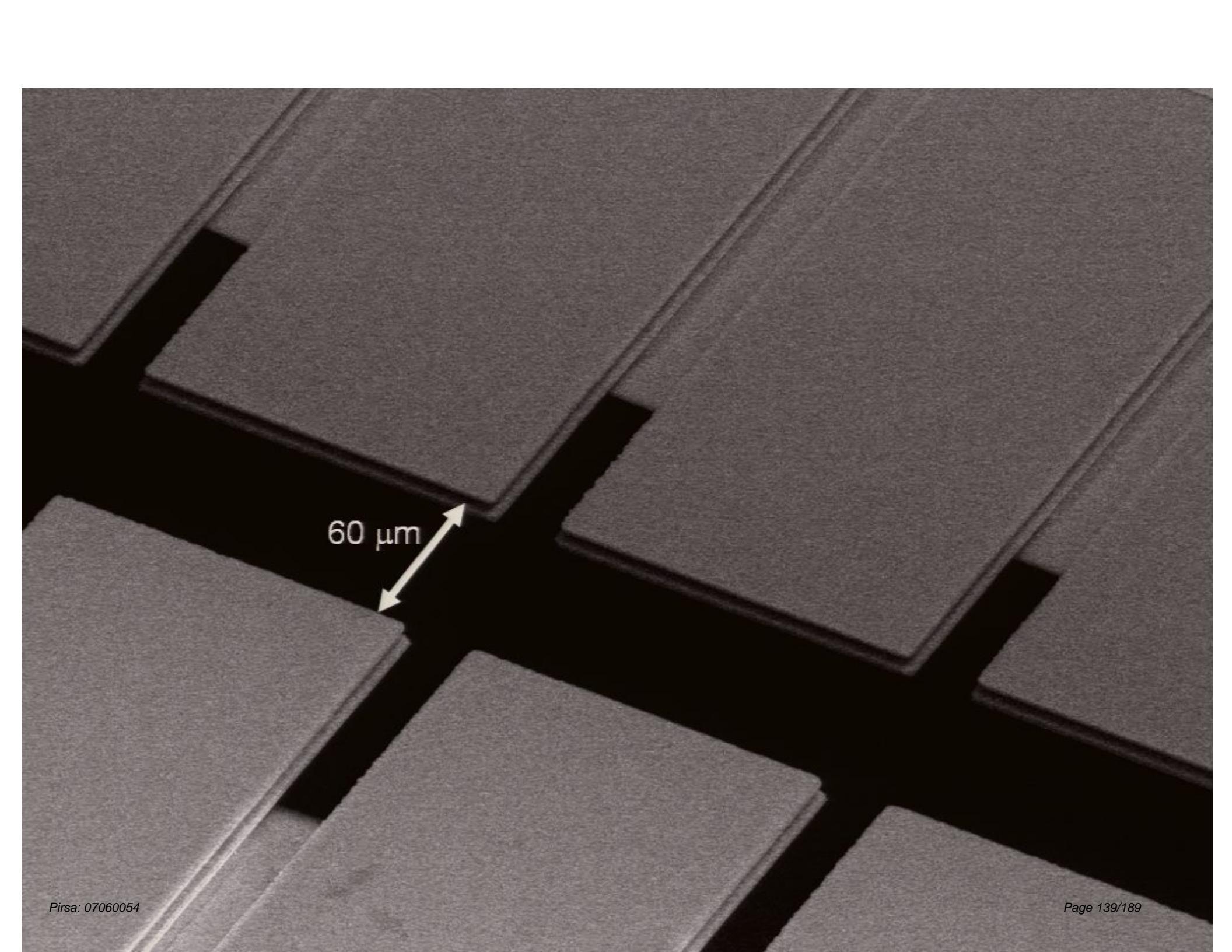
$V_{STATIC} = +1V$  (endcaps),  $-0.33V$  (middles)

Power  $\sim V_{RF}^2 \Omega^2 \sim V_{RF}^3$   
 $\sim 1\text{mW}$

Trap frequencies: 1.0 MHz, 3.3 MHz and 4.3 MHz

Trap depth: 0.08 eV

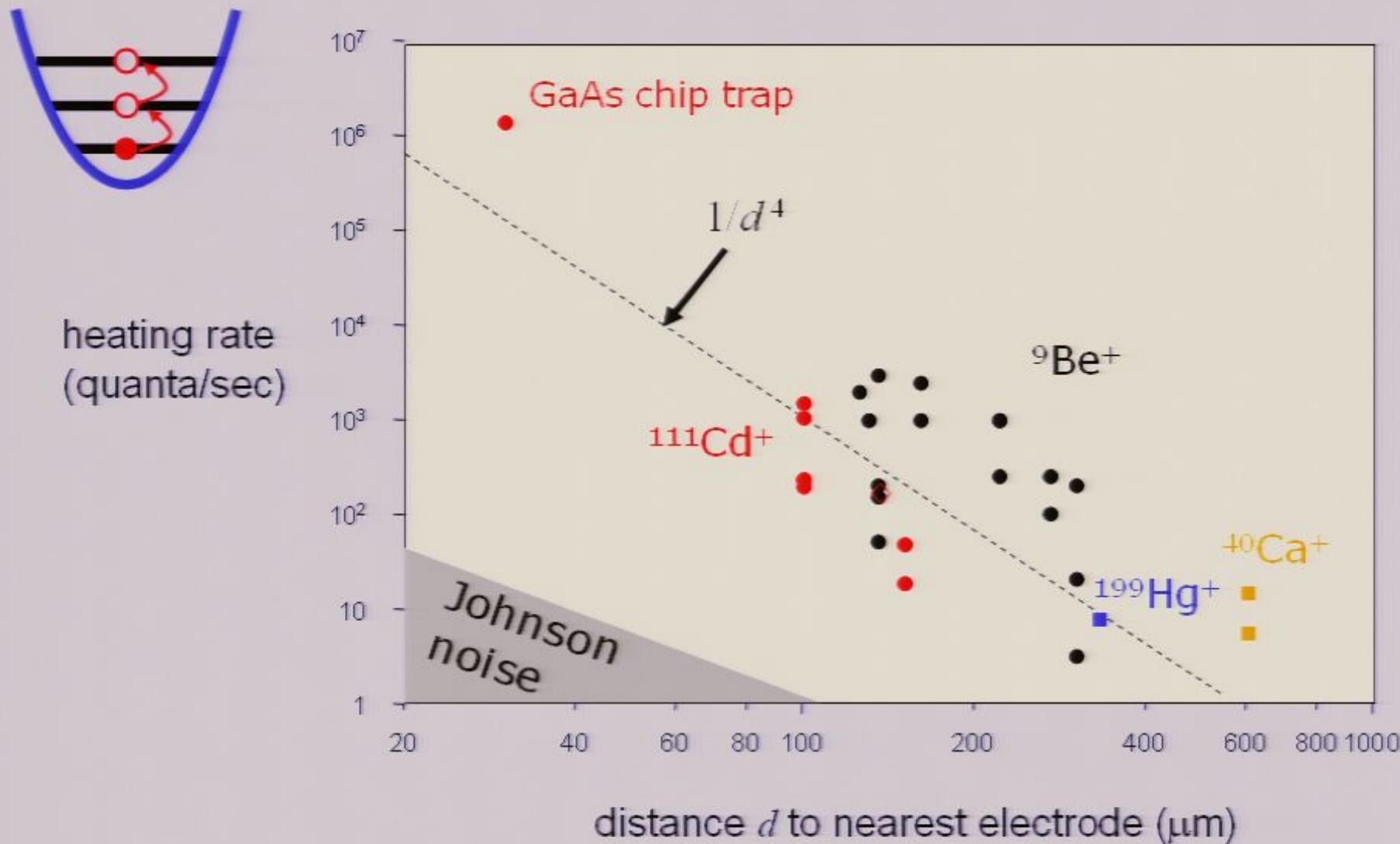
Lifetime w/o cooling: 0.1sec



60  $\mu\text{m}$

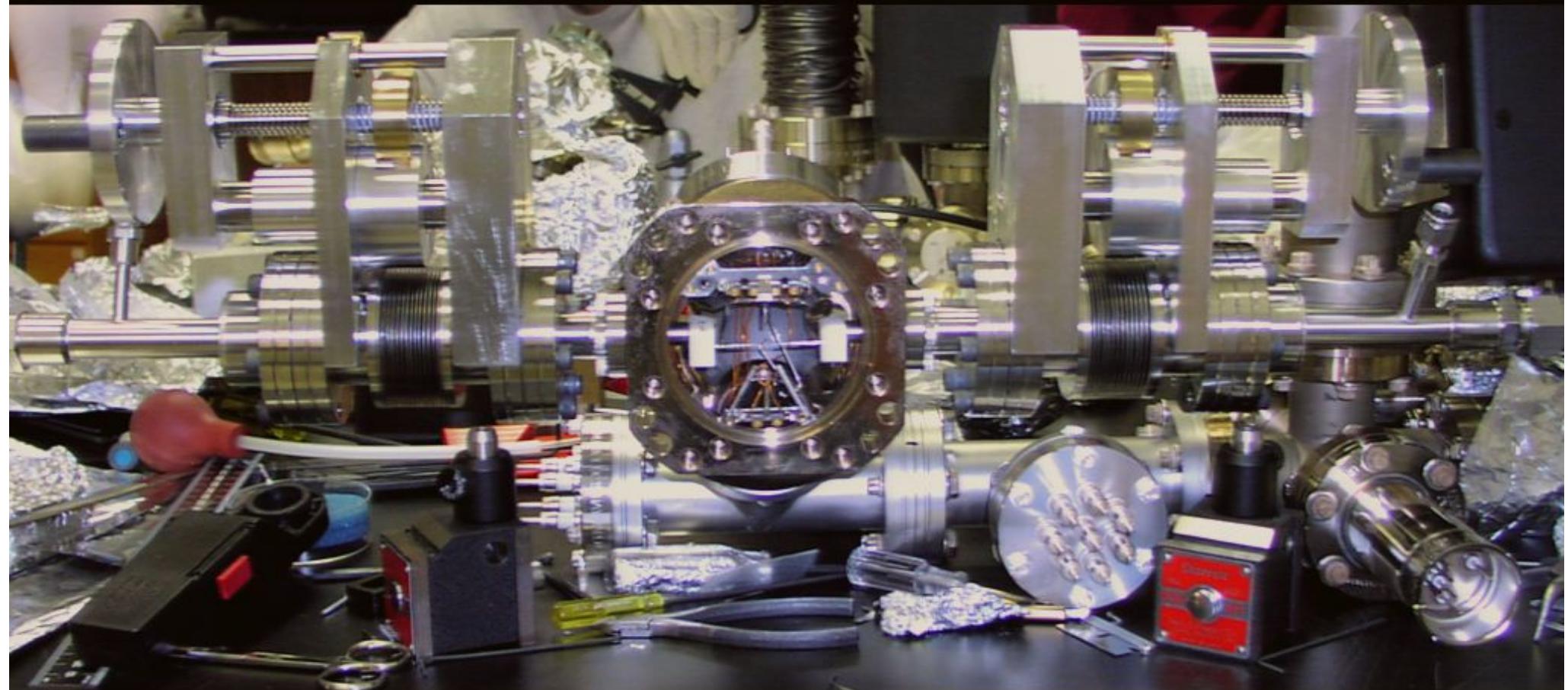
A scanning electron micrograph showing a close-up view of a textured, grey surface. The surface has a fine, repeating pattern of raised ridges and grooves. A white double-headed arrow is positioned in the lower-left quadrant, indicating a scale of 60 micrometers.

## Heating in Trapped Ions vs. Proximity to Electrodes



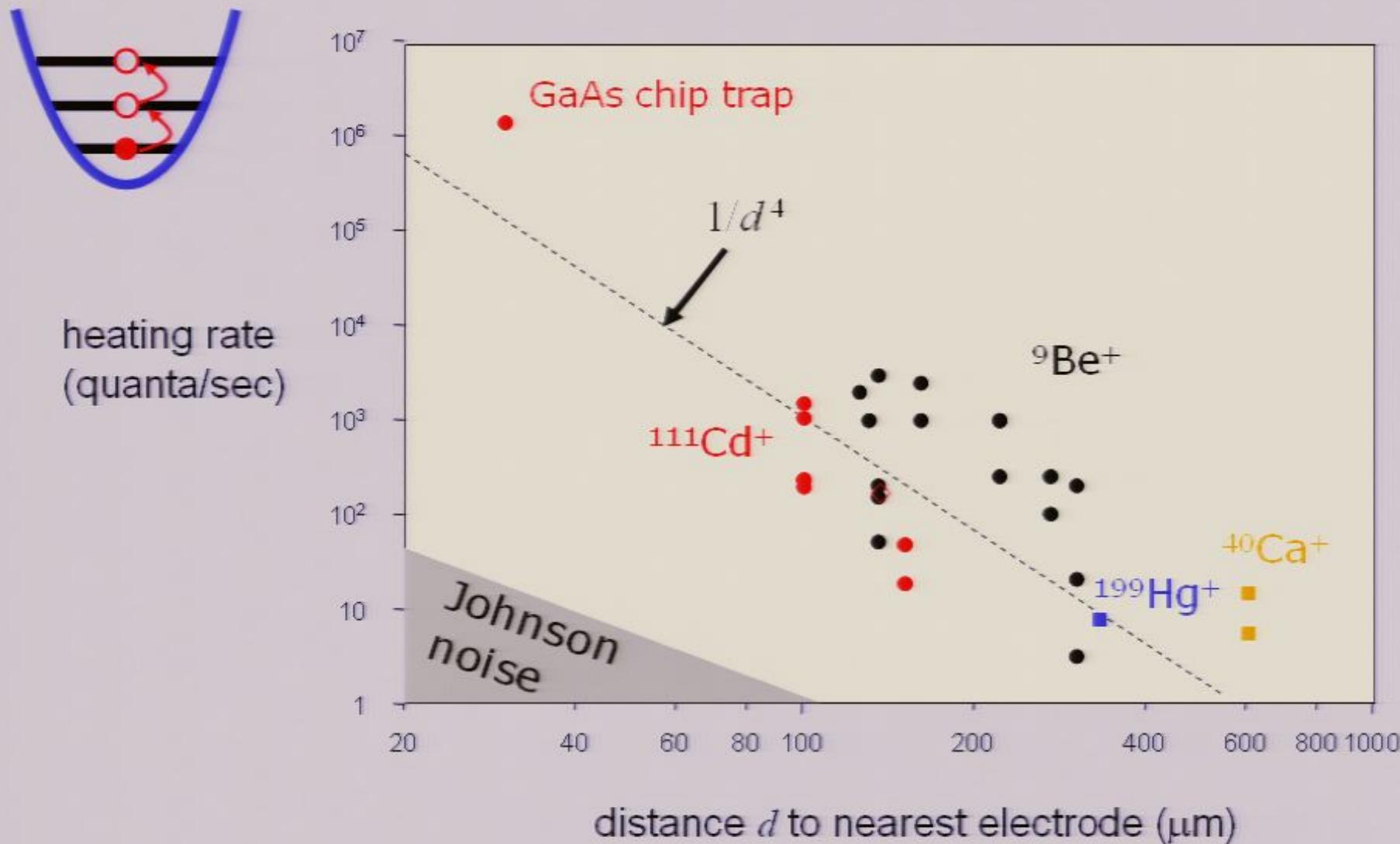
# "double needle" trap

(L. Deslauriers)



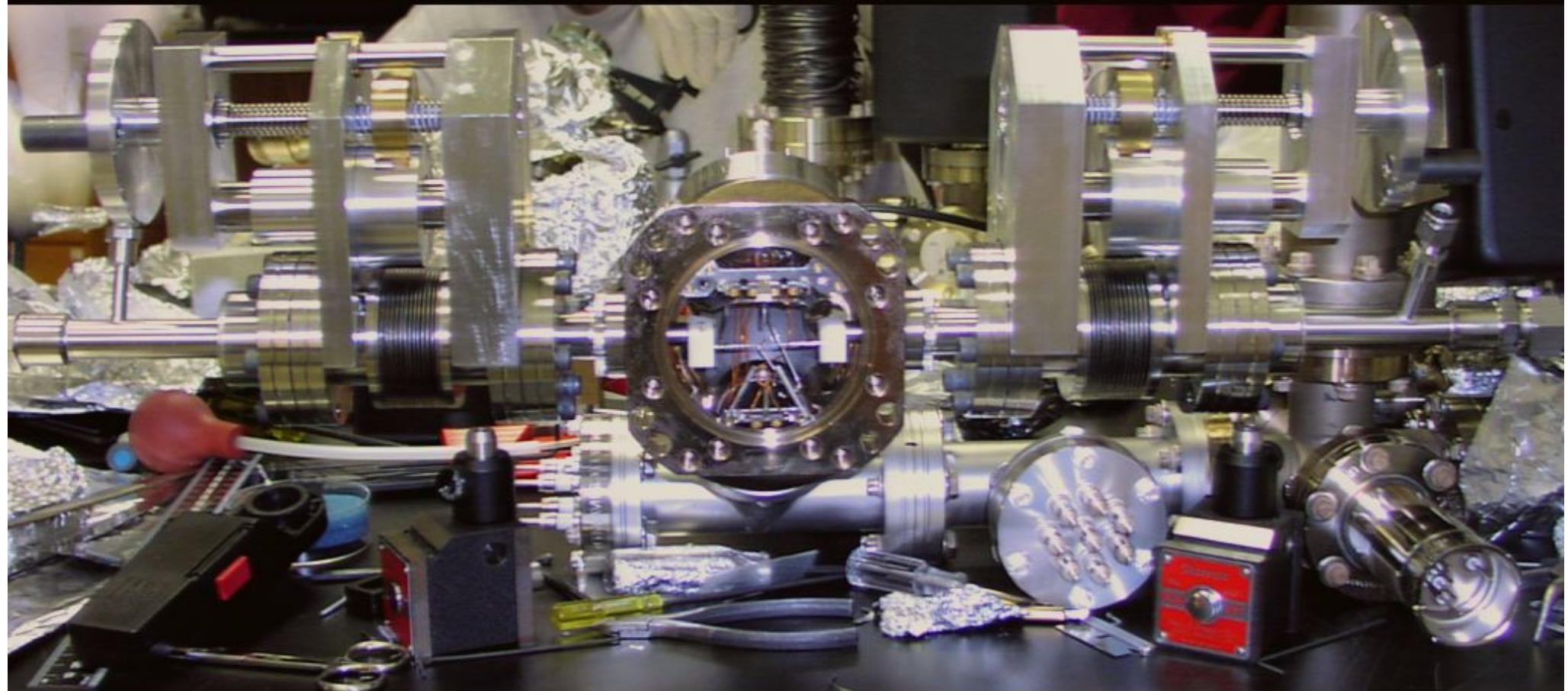
- 15  $\mu\text{m}$  diameter W tips
- adjustable separation
- cooling to 77K

## Heating in Trapped Ions vs. Proximity to Electrodes

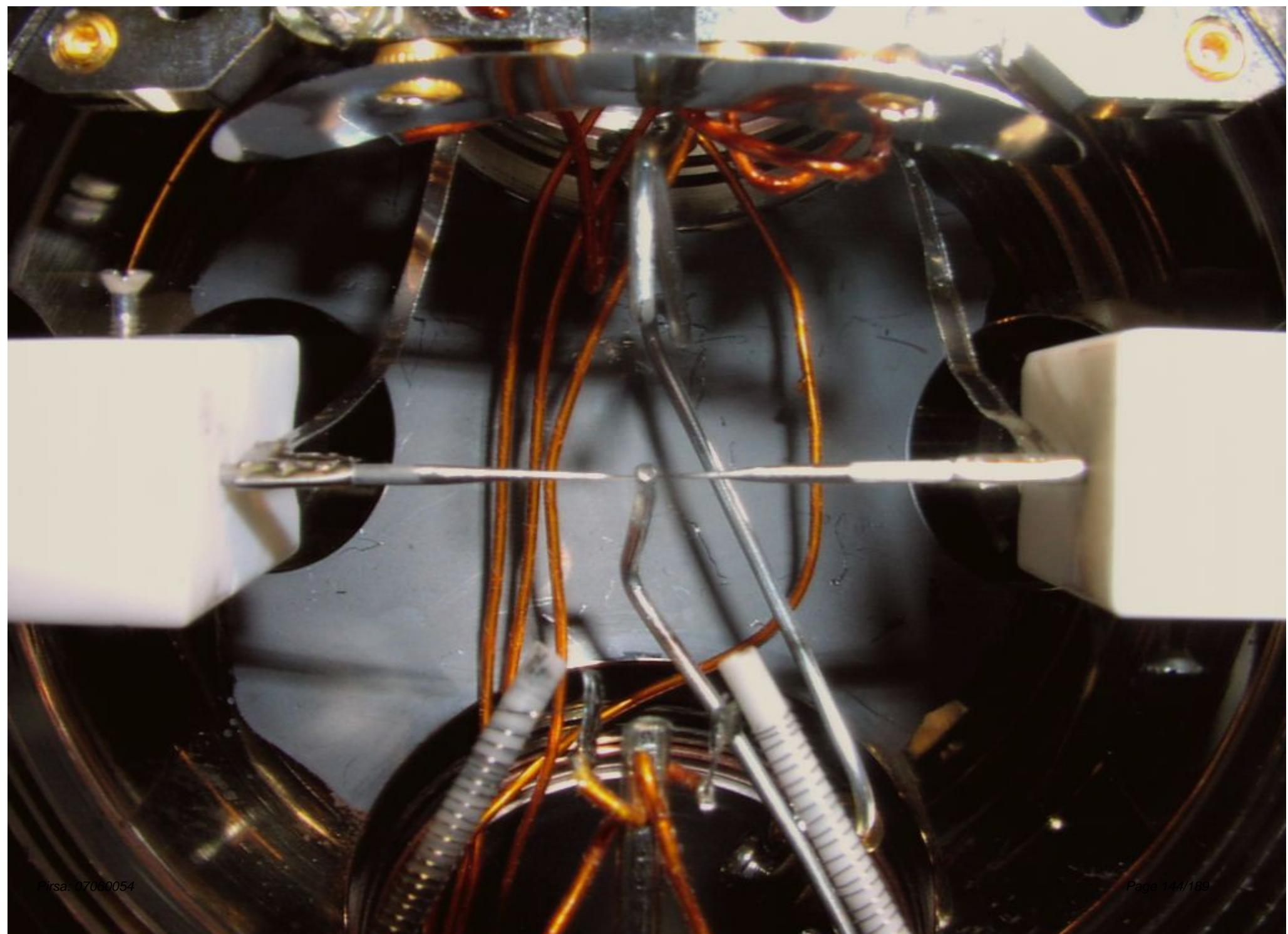


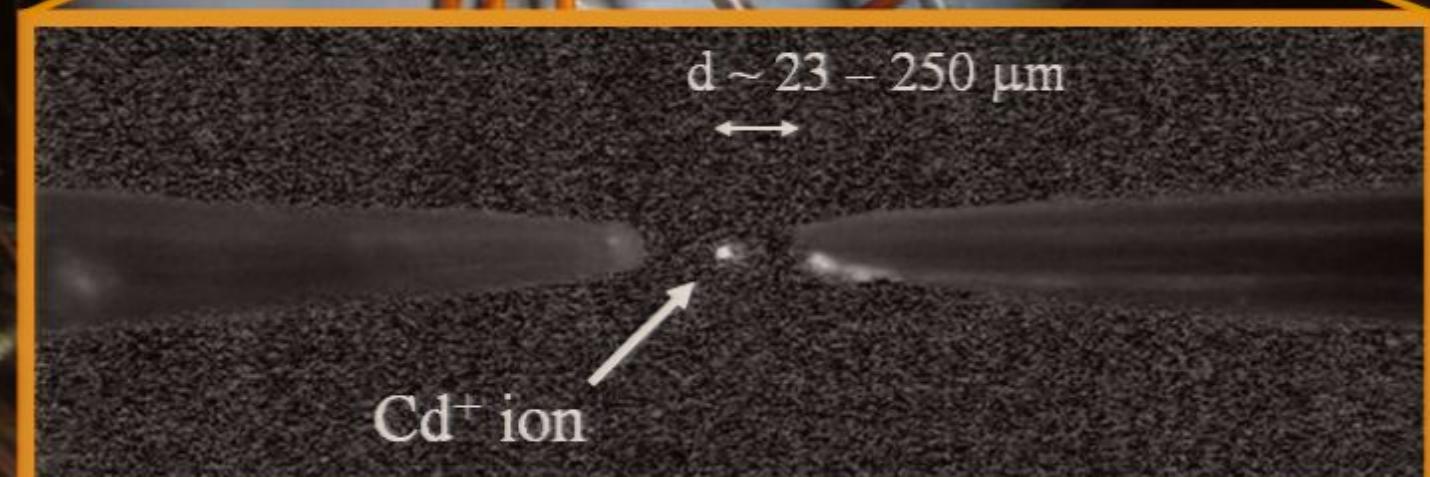
# "double needle" trap

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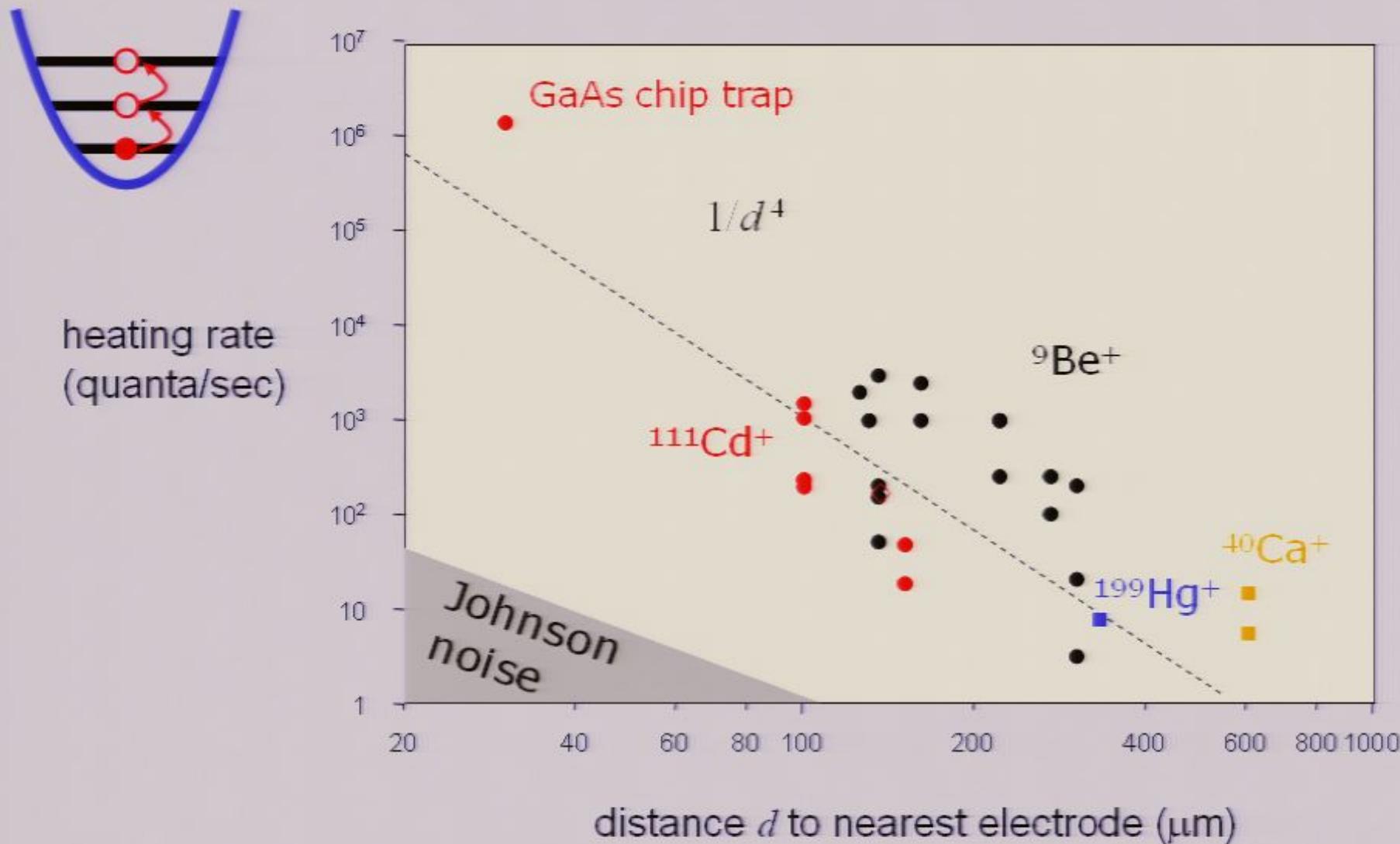


- 15  $\mu\text{m}$  diameter W tips
- adjustable separation
- cooling to 77K

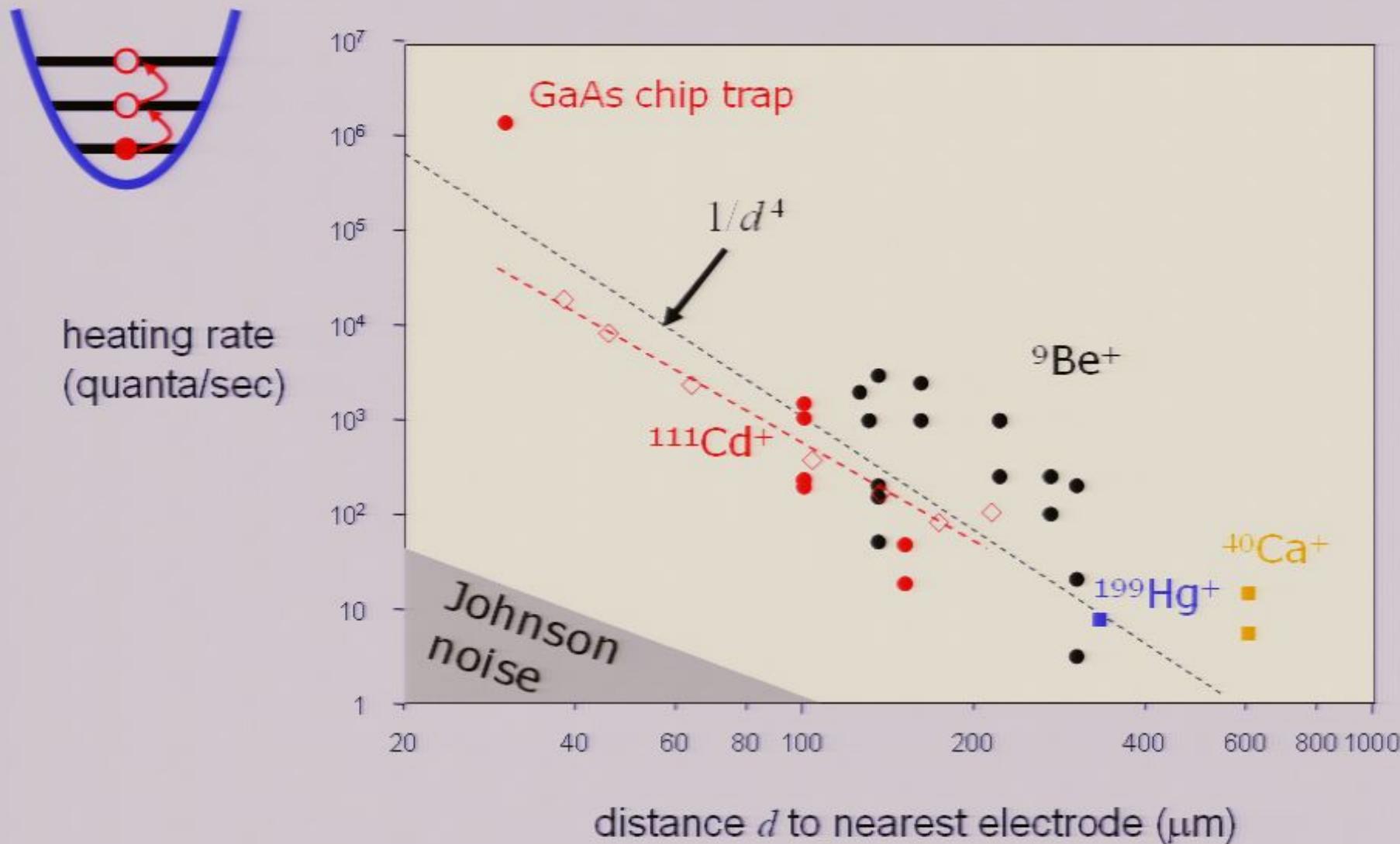




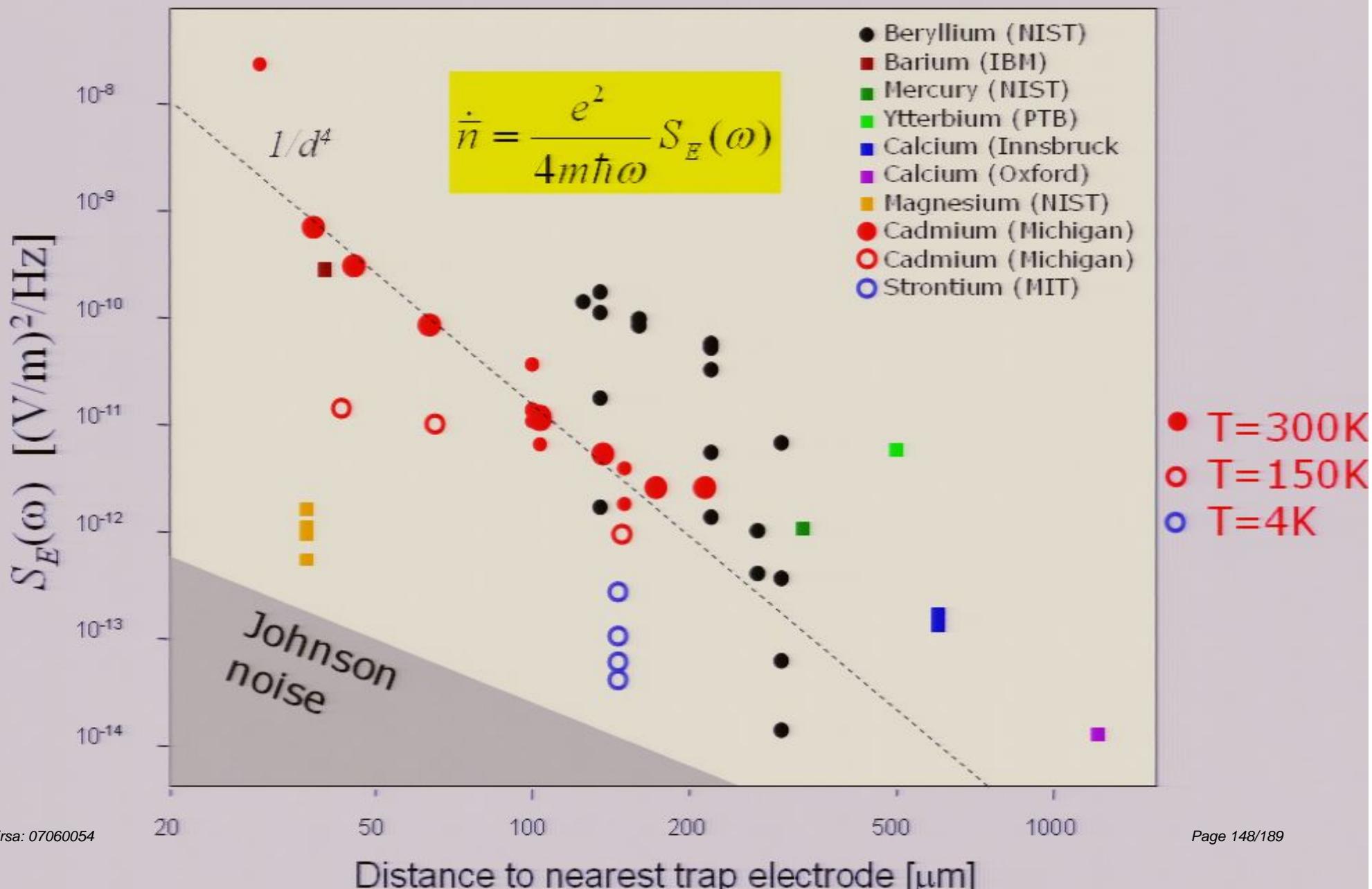
## Heating in Trapped Ions vs. Proximity to Electrodes



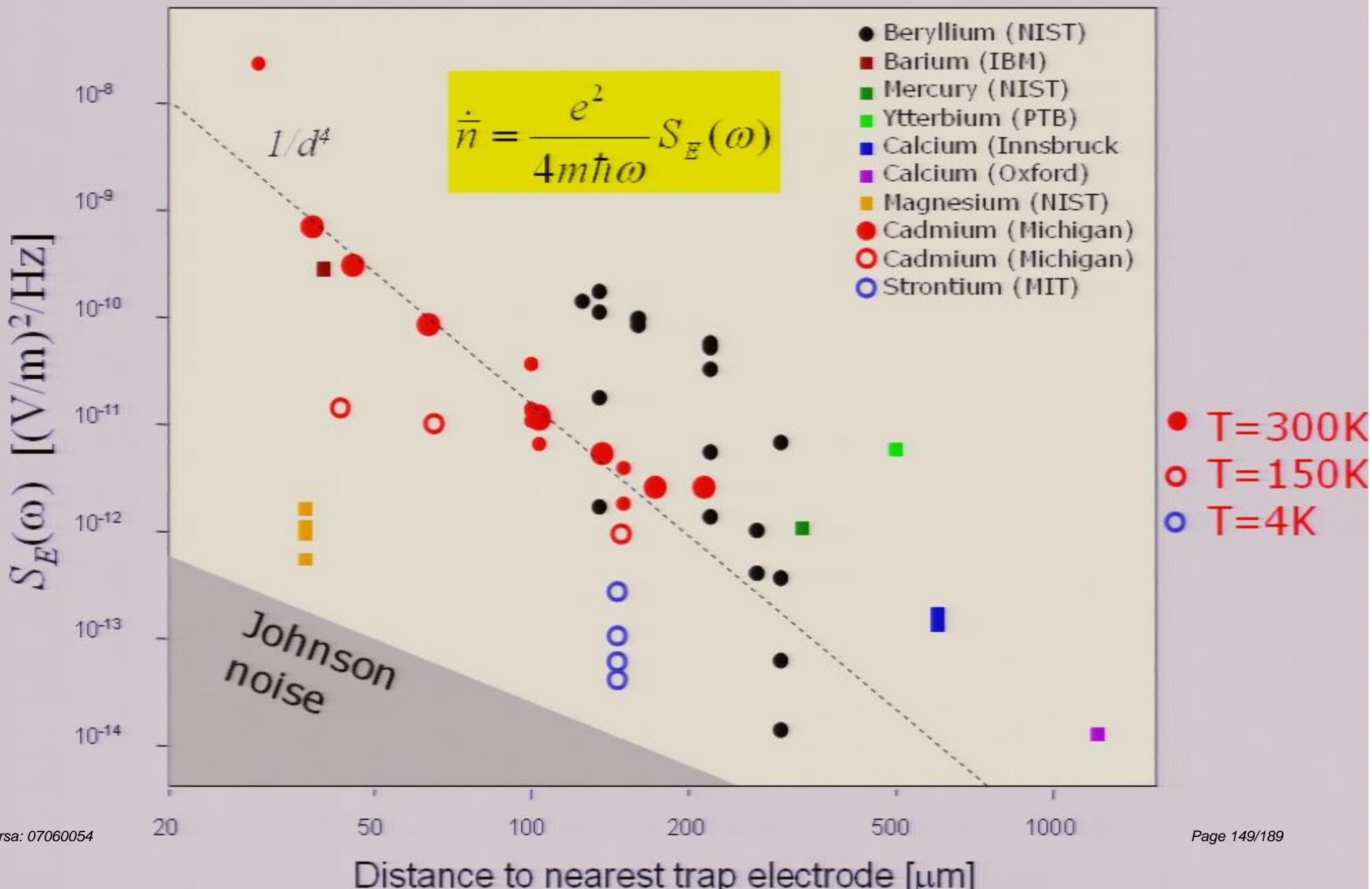
## Heating in Trapped Ions vs. Proximity to Electrodes



# Inferred Electric Field Noise

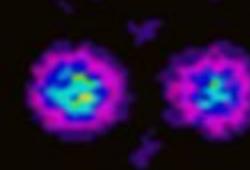


# Inferred Electric Field Noise



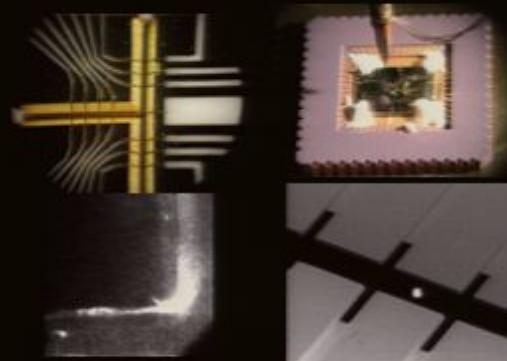
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

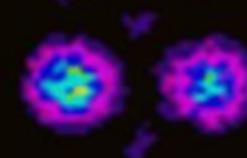
- Nonlocal entanglement through spontaneous emission (photons)



$\sim 1$  m

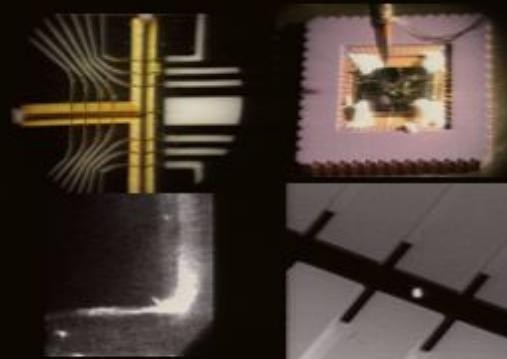
# Ion Trap Quantum Networks

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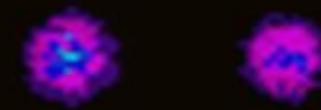


$\sim 1$  m

# Ion Trap Quantum Networks

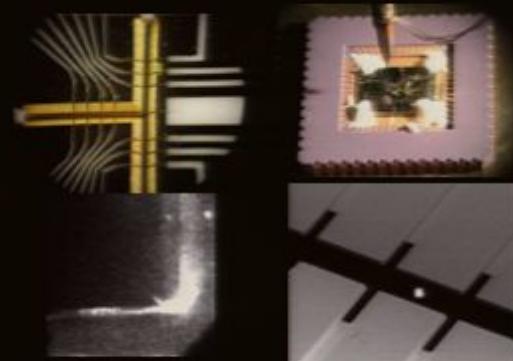
---

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

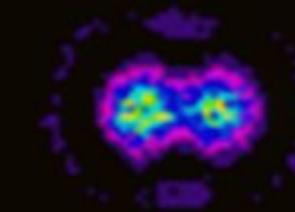
- Nonlocal entanglement through spontaneous emission (photons)



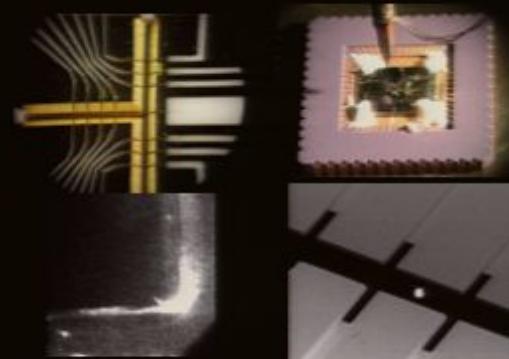
$\sim 1$  m

# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)
- Shuttling ions through advanced scalable trap structures
- Nonlocal entanglement through spontaneous emission (photons)



$\sim 10^{-6}$  m



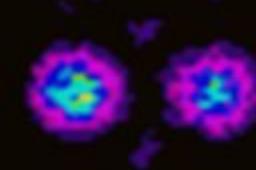
$\sim 10^{-3}$  m



$\sim 1$  m

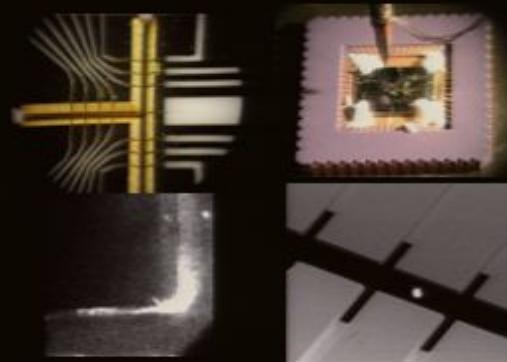
# Ion Trap Quantum Networks

- Local entanglement through the Coulomb interaction (phonons)



$\sim 10^{-6}$  m

- Shuttling ions through advanced scalable trap structures



$\sim 10^{-3}$  m

- Nonlocal entanglement through spontaneous emission (photons)

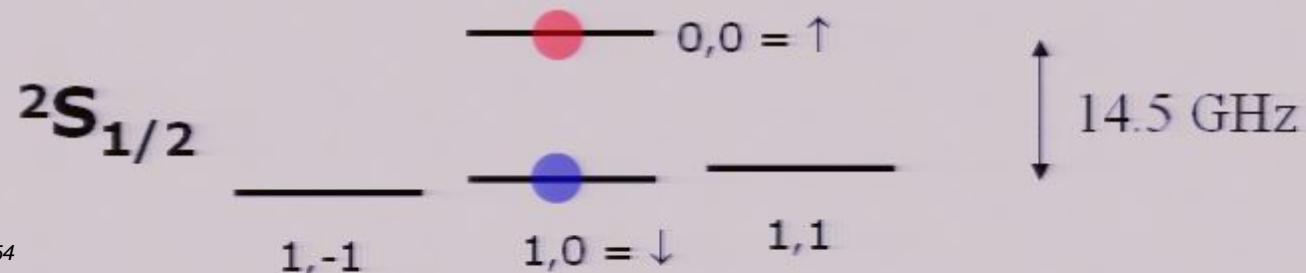


$\sim 1$  m

# Linking atoms with ~~phonons~~ photons

**111Cd<sup>+</sup>**

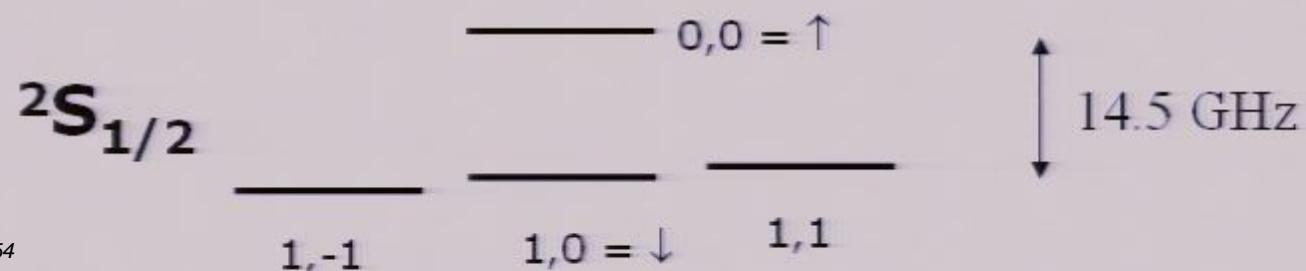
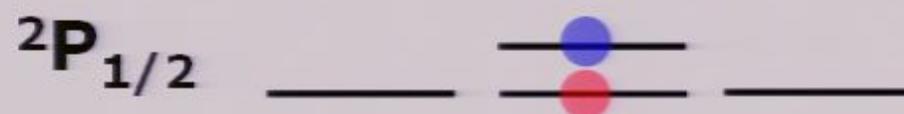
**<sup>2</sup>P<sub>1/2</sub>**    —    =    —



# Linking atoms with ~~phonons~~ photons

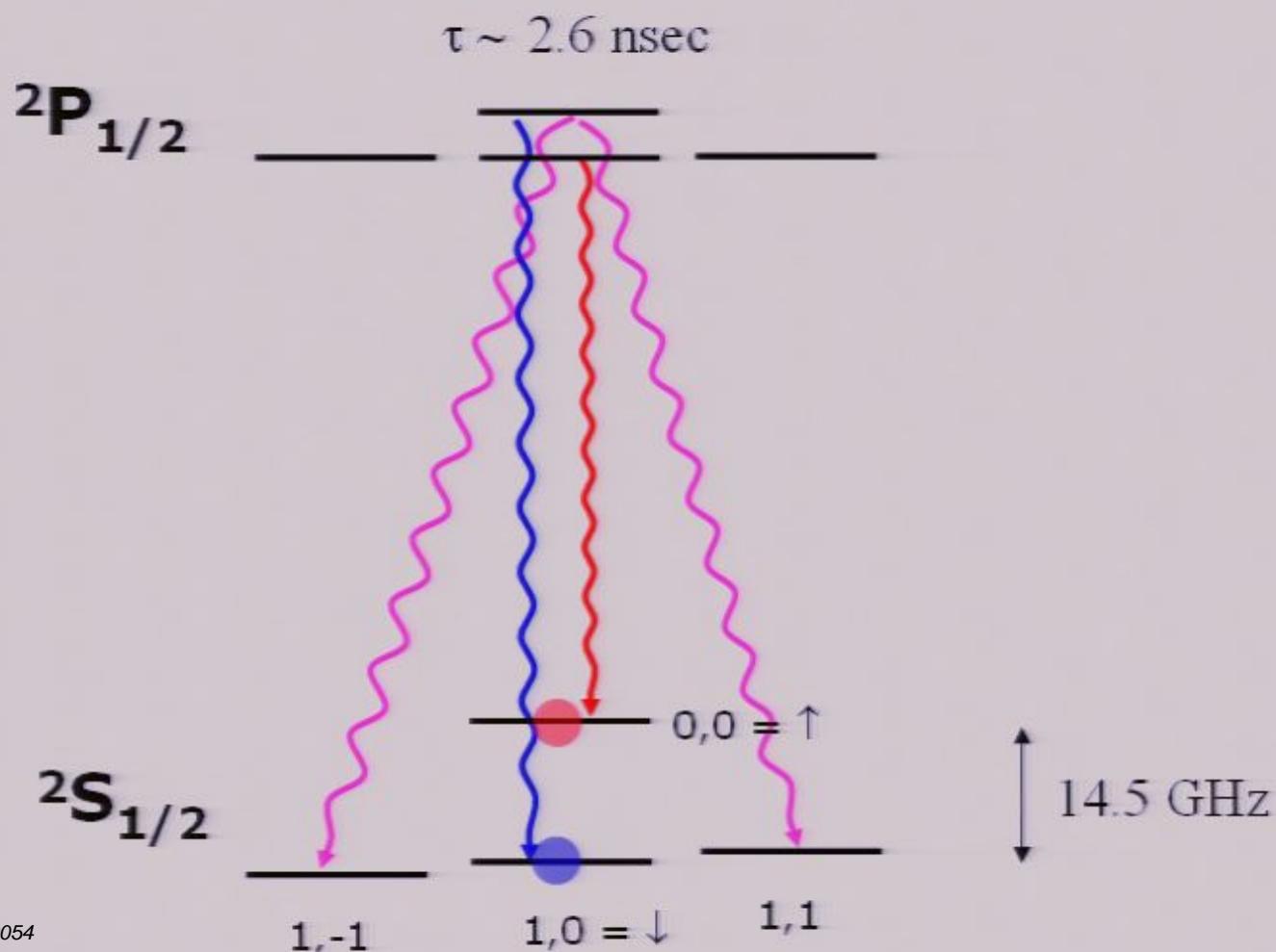
**111Cd<sup>+</sup>**

$\tau \sim 2.6$  nsec



# Linking atoms with ~~phonons~~ photons

**111Cd<sup>+</sup>**



# Linking atoms with ~~phonons~~ photons

**$^{111}\text{Cd}^+$**

$\tau \sim 2.6 \text{ nsec}$

$^2\text{P}_{1/2}$

select only  
 $\pi$ -polarization

Given photon emerges  
from polarizer

$$|\Psi\rangle = |\downarrow\rangle|\text{blue}\rangle + |\uparrow\rangle|\text{red}\rangle$$

(post-selected)

$^2\text{S}_{1/2}$

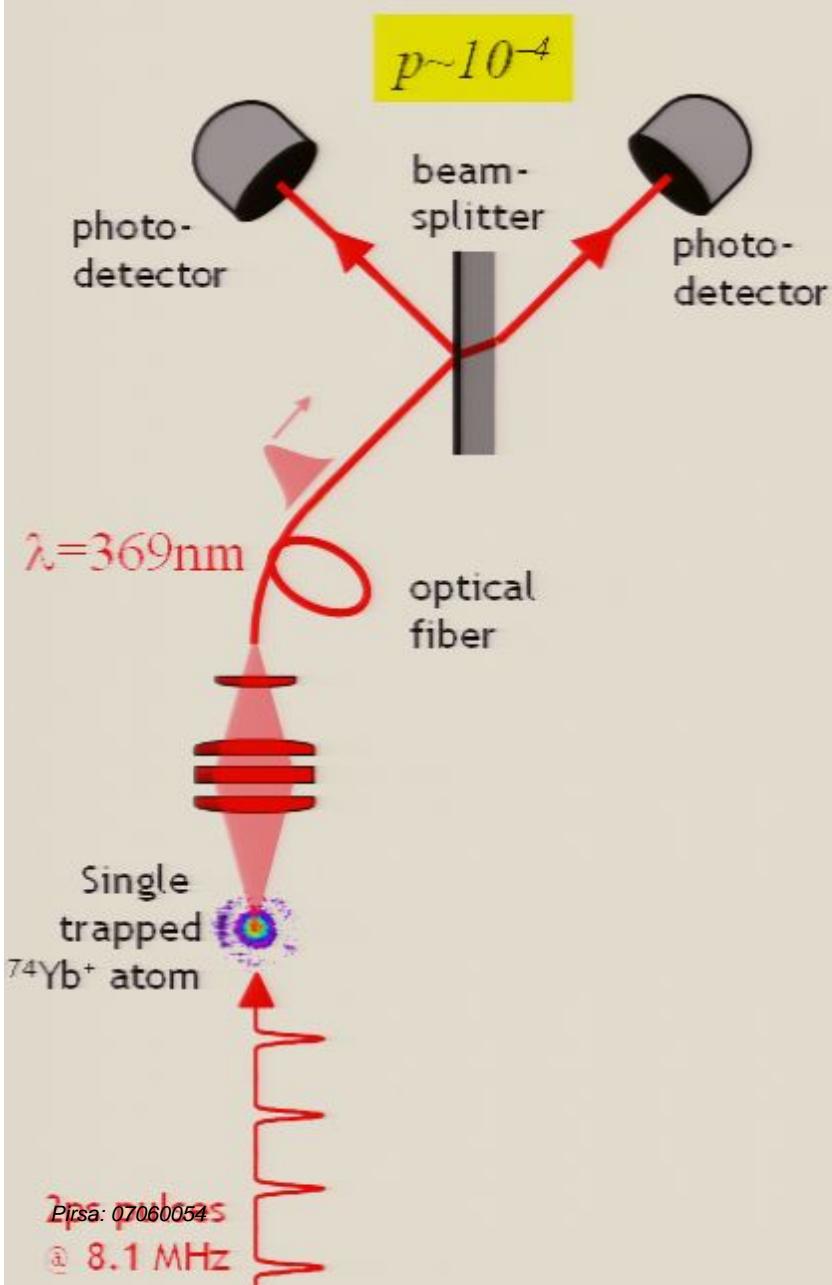
$0,0 = \uparrow$

14.5 GHz

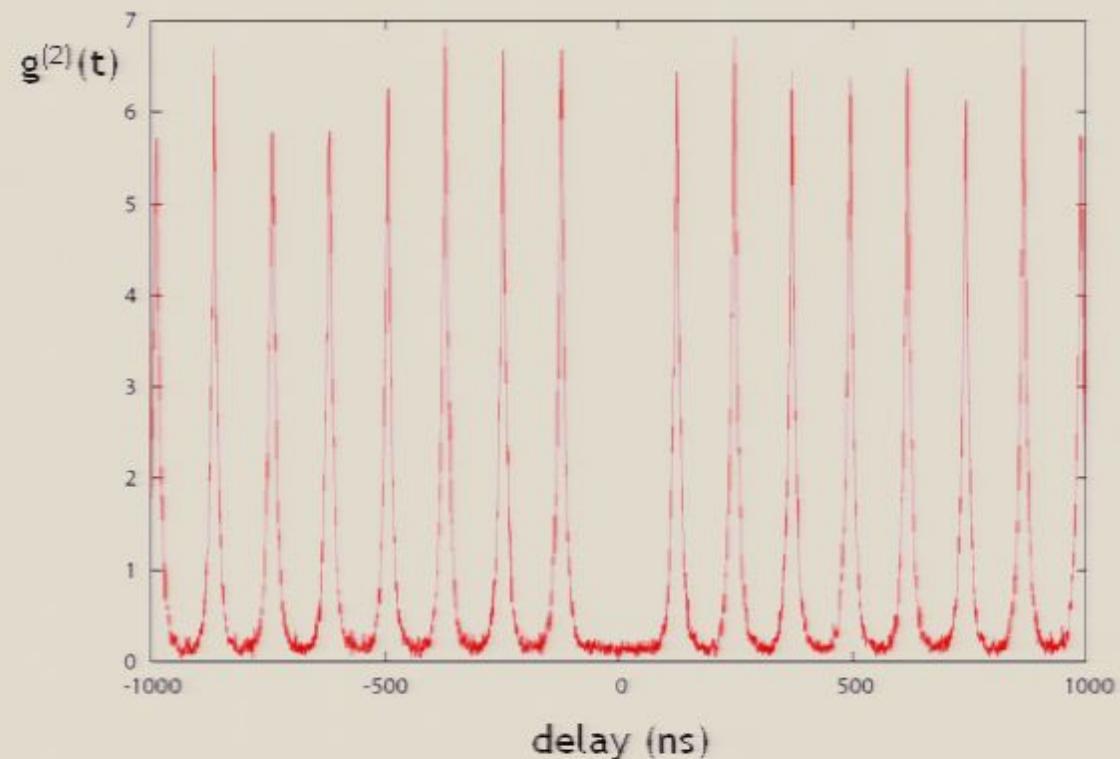
$1,-1$

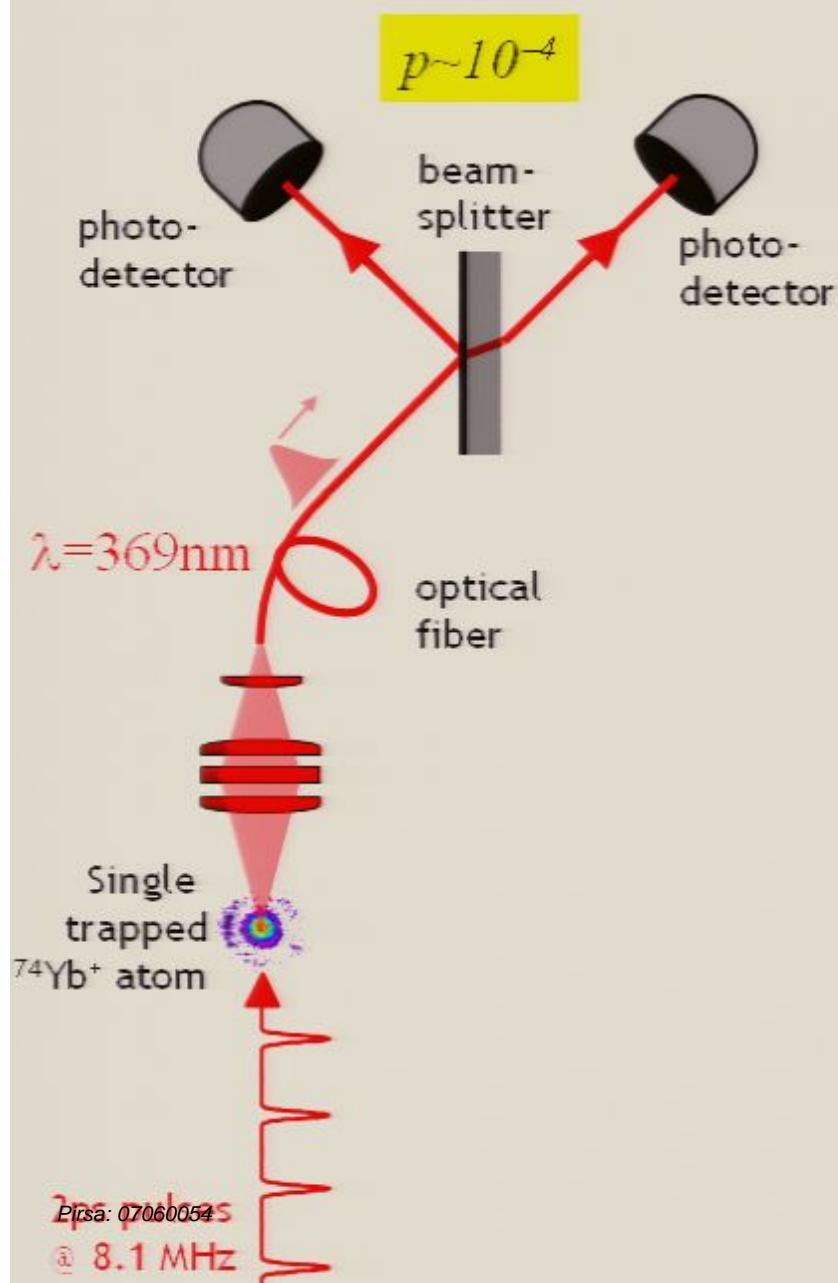
$1,0 = \downarrow$

$1,1$

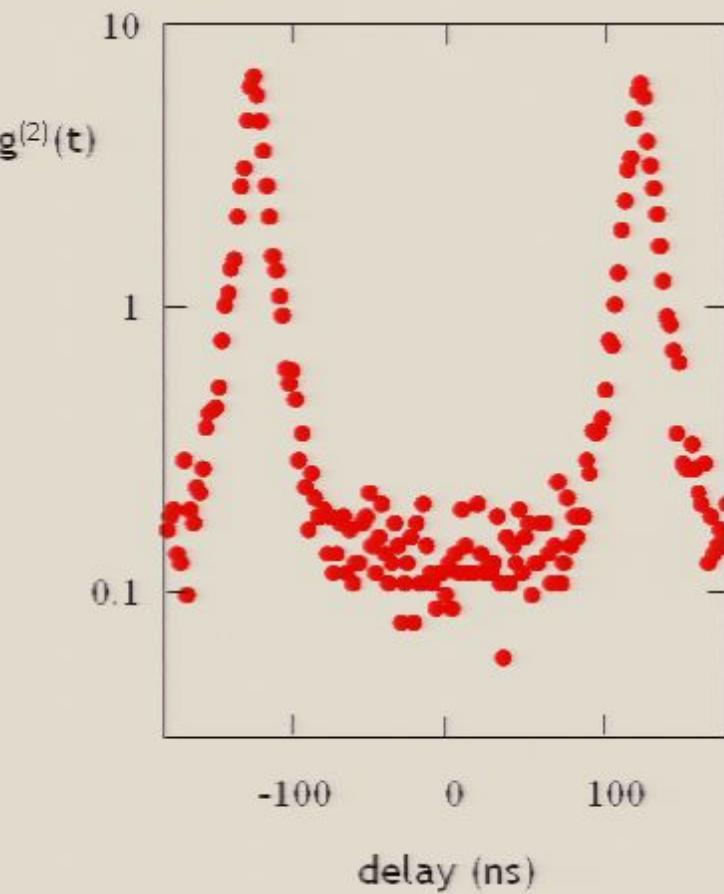


excellent probabilistic  
single photon source

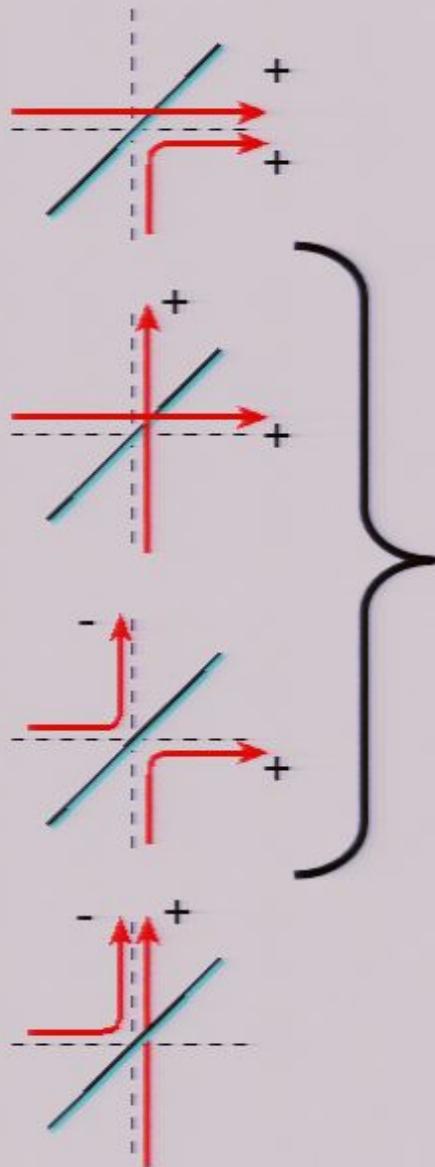




excellent probabilistic  
single photon source

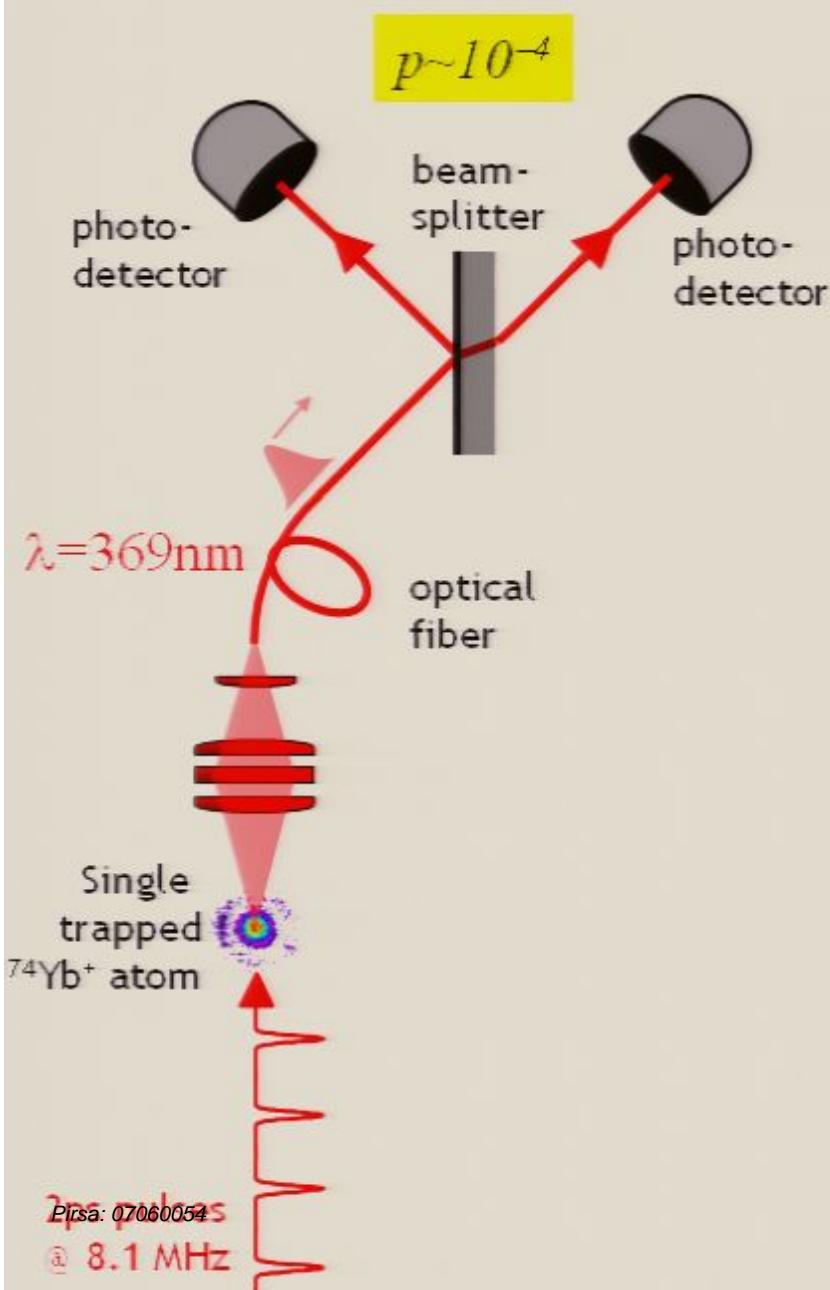


# Hong-Ou-Mandel Interference

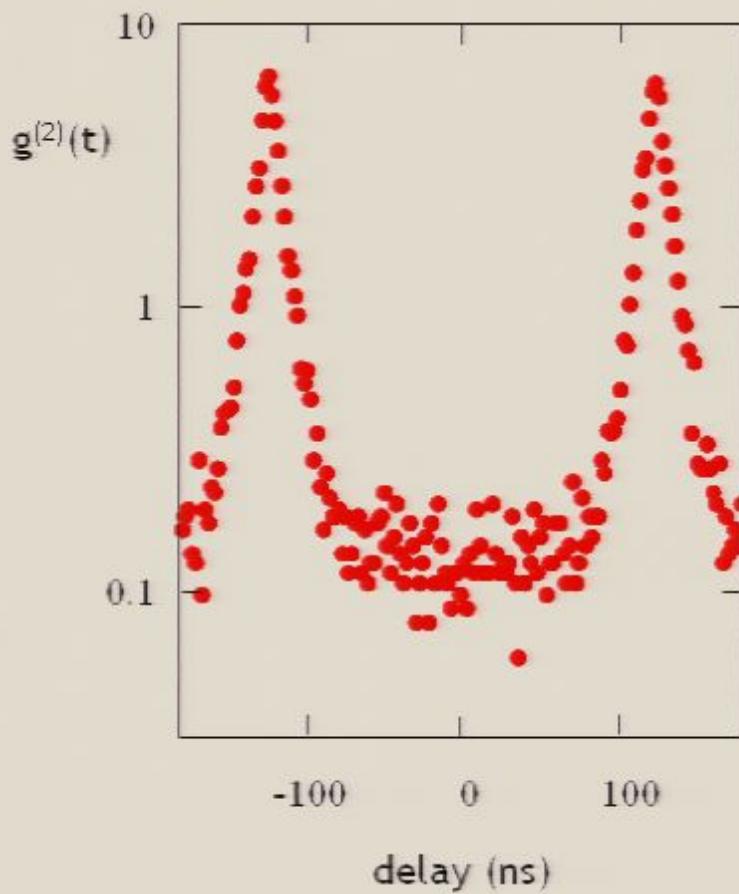


destructive interference  
of these paths

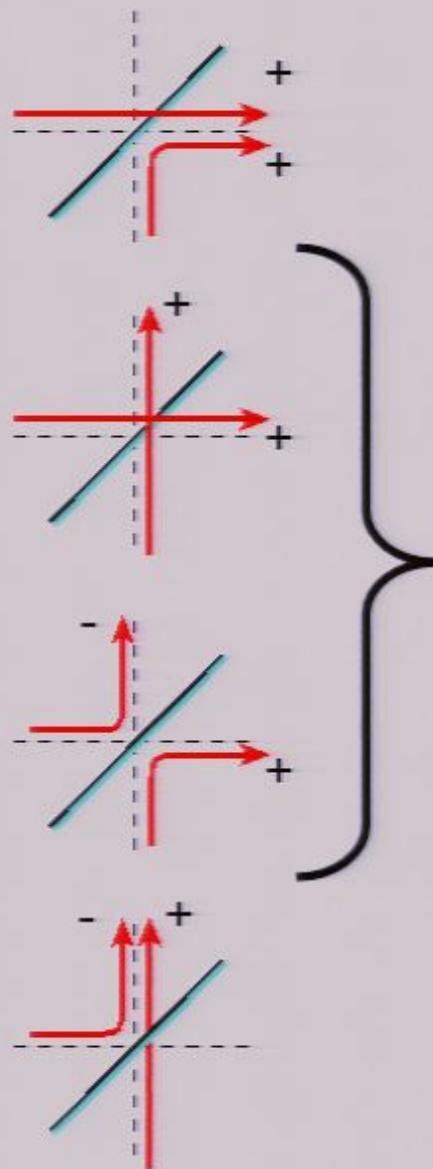
Hong, Ou, and Mandel, *PRL*, 59, 2044 (1987)



excellent probabilistic  
single photon source



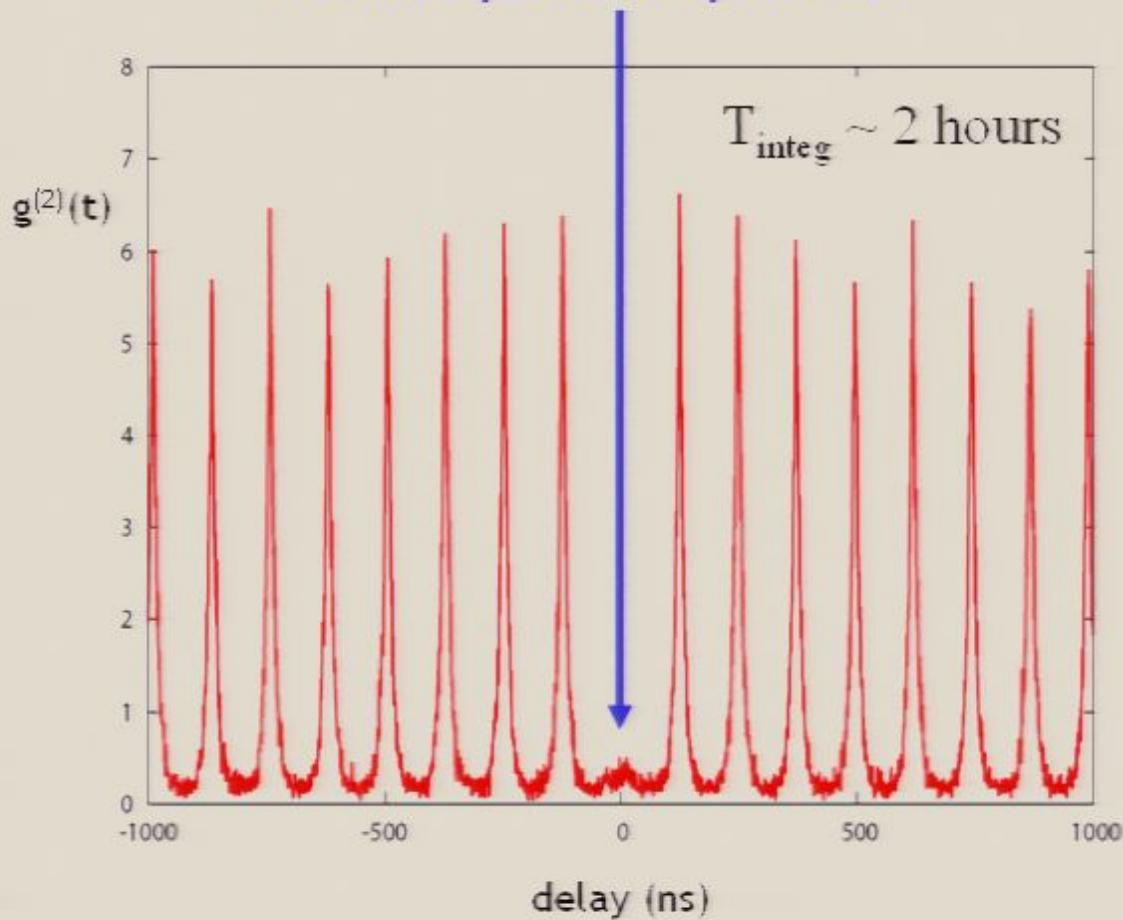
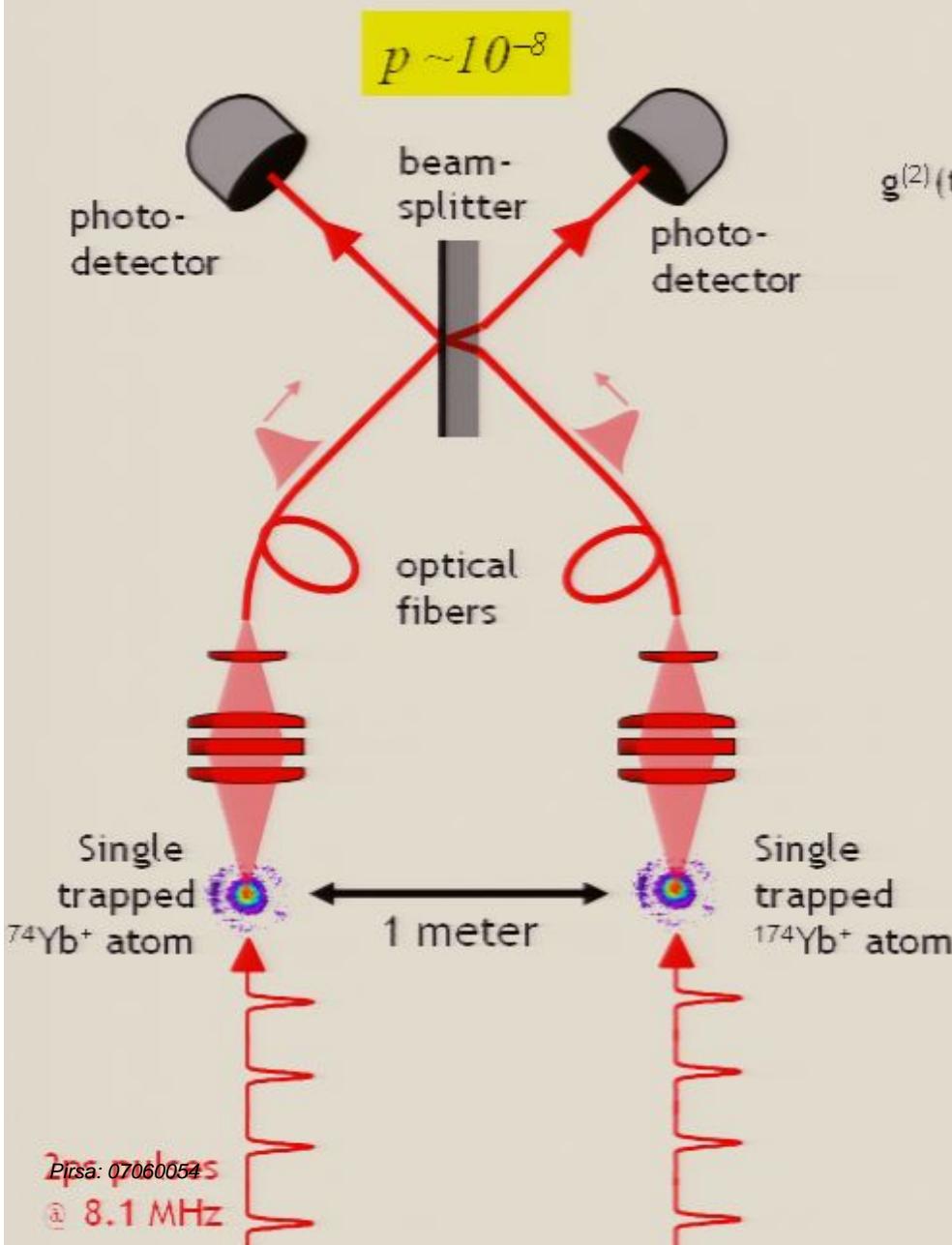
# Hong-Ou-Mandel Interference



destructive interference  
of these paths

Hong, Ou, and Mandel, *PRL*, 59, 2044 (1987)

## Quantum interference from two independent photons



**Hong, Ou, Mandel, PRL 59, 2044 (1987)**

Santori, et al., Nature, 419, 594 (2002)

Kaltenbaek, et al, PRL, 96, 240502 (2006)

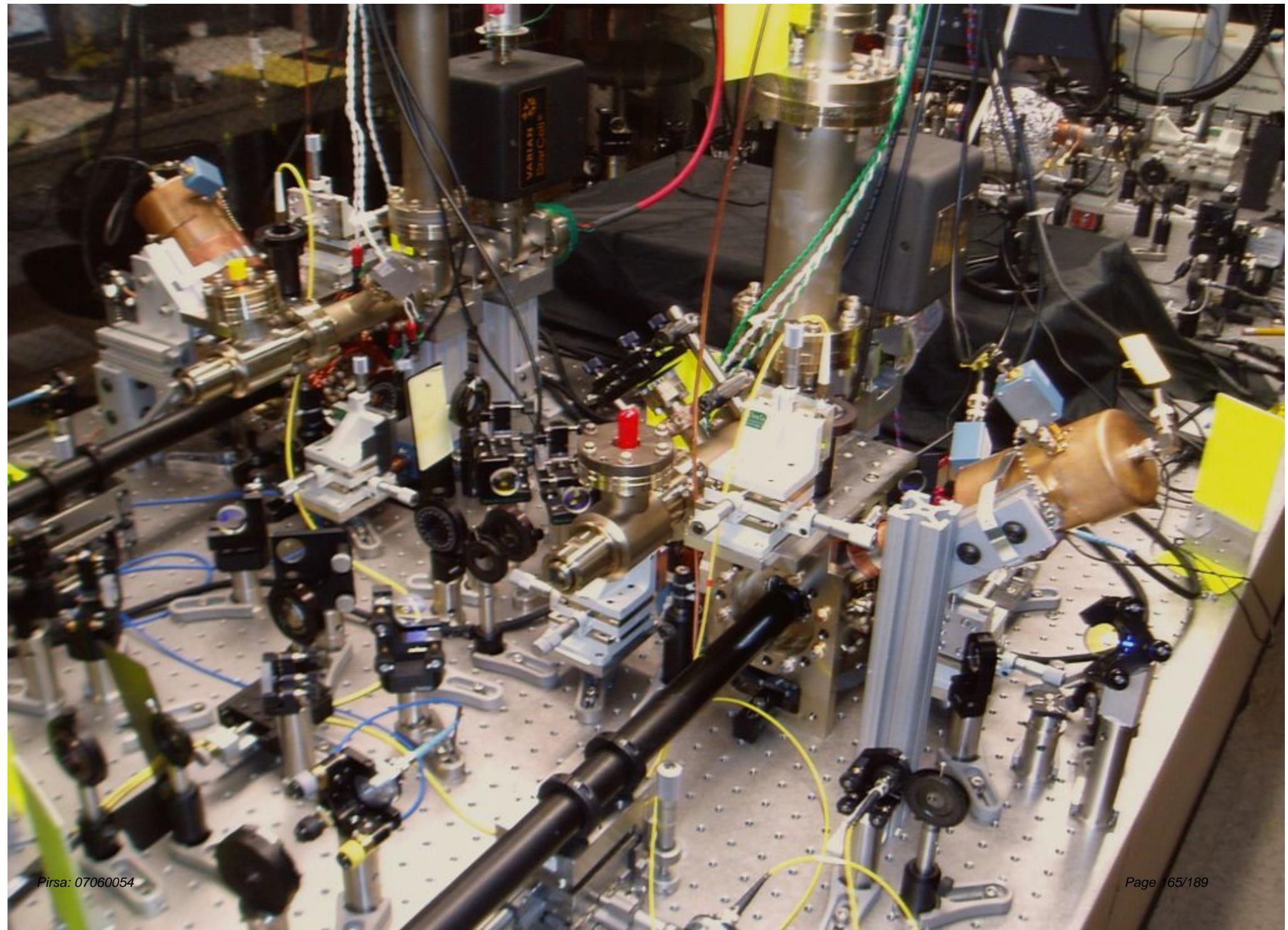
Legero, et al., PRL, 93, 070503 (2004).

Thompson, et al., Science, 313, 74 (2006).

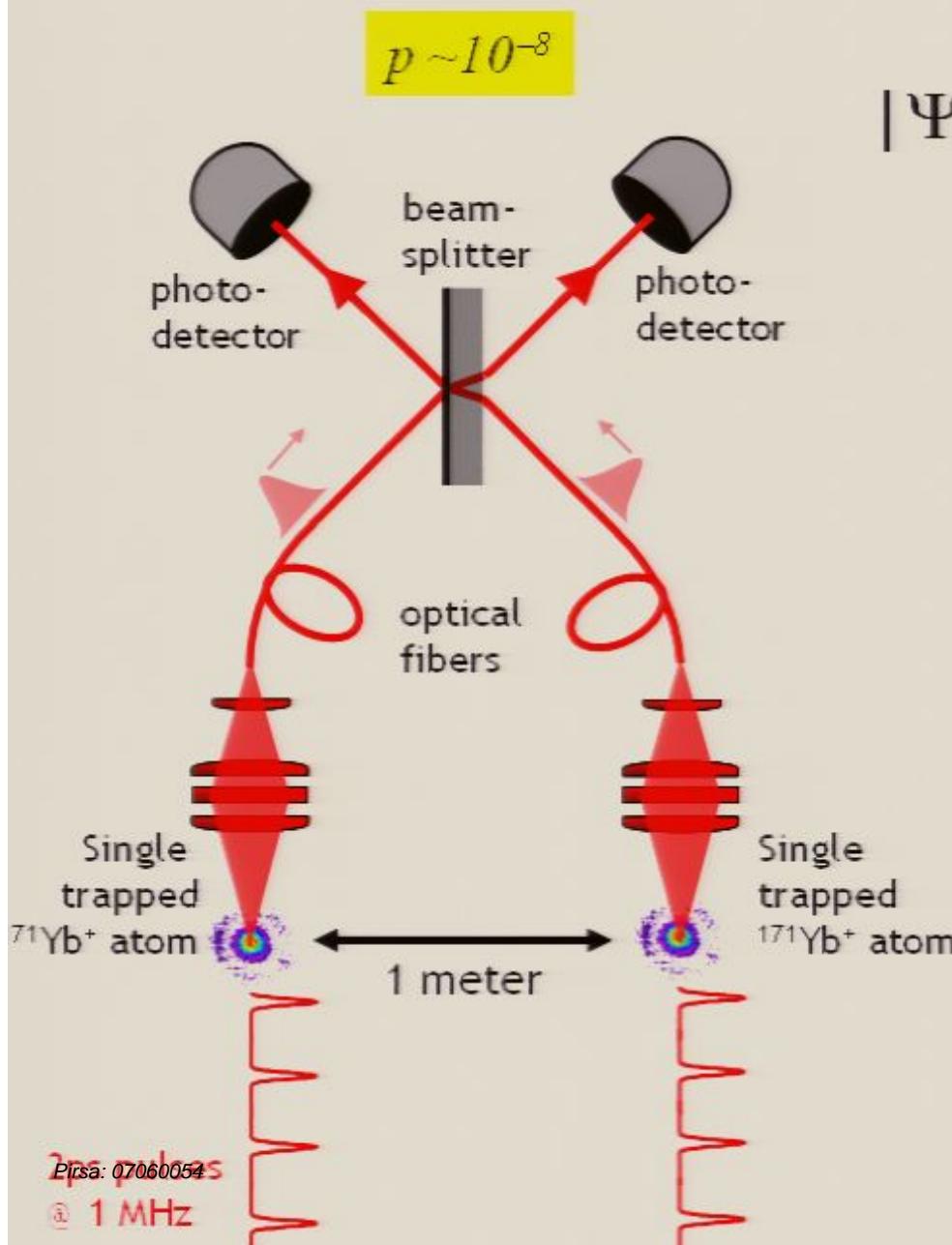
Felinto, et al. Nature Physics, 2, 844 (2006)

Beugnon, et al. Nature, 440, 779 (2006).

Pasca: 07060054  
© 8.1 MHz



Now with odd isotopes (having nuclear spin)

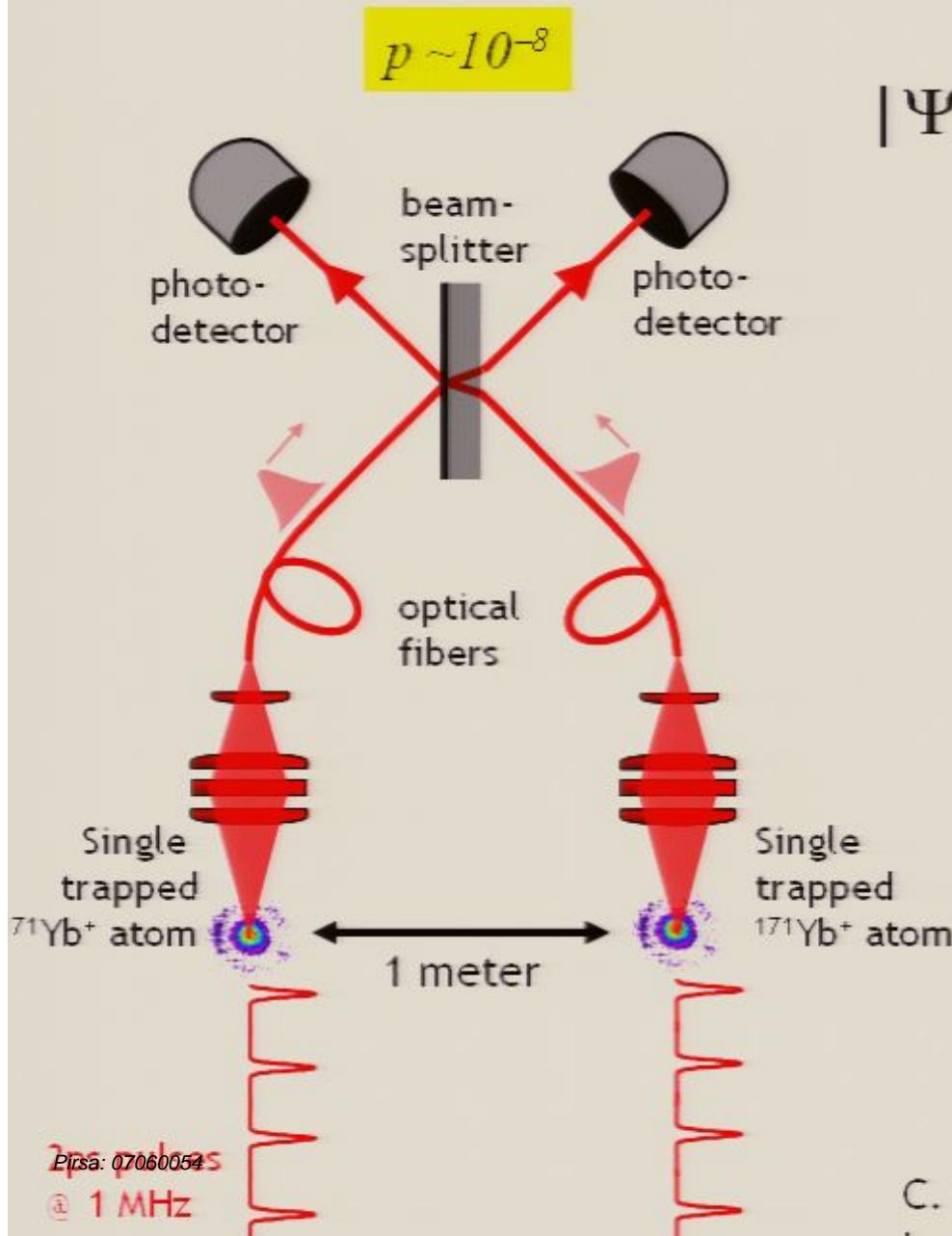


$$|\Psi\rangle = (|\downarrow\rangle_1 |\text{blue}\rangle_1 + |\uparrow\rangle_1 |\text{red}\rangle_1) \otimes (|\downarrow\rangle_2 |\text{blue}\rangle_2 + |\uparrow\rangle_2 |\text{red}\rangle_2)$$

$$\Rightarrow |\downarrow\rangle_1 |\uparrow\rangle_2 - |\uparrow\rangle_2 |\downarrow\rangle_2$$

...upon coincidence  
photon detection

Now with odd isotopes (having nuclear spin)



$$|\Psi\rangle = (|↓\rangle_1 |\text{blue}\rangle_1 + |↑\rangle_1 |\text{red}\rangle_1) \\ \otimes (|↓\rangle_2 |\text{blue}\rangle_2 + |↑\rangle_2 |\text{red}\rangle_2)$$

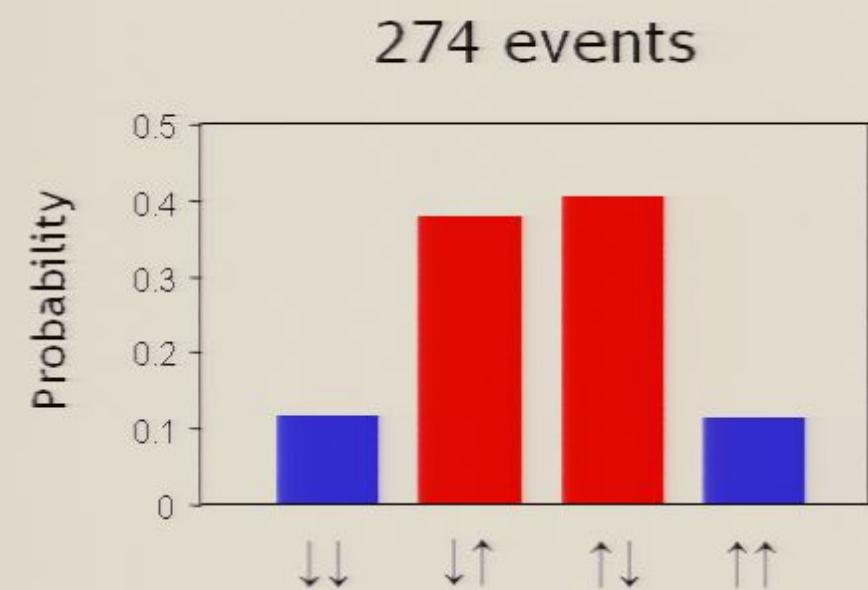
$$\Rightarrow |↓\rangle_1 |↑\rangle_2 - |↑\rangle_2 |↓\rangle_2$$

...upon coincidence  
photon detection

insensitive to

- interferometric phase noise
- ion motion

## Measured ion correlations given coincidence photons

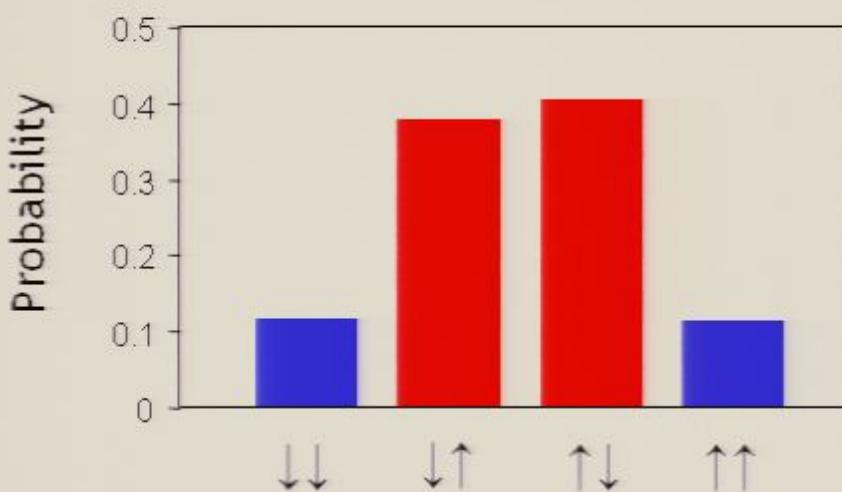


Measured ion correlations  
given coincidence photons

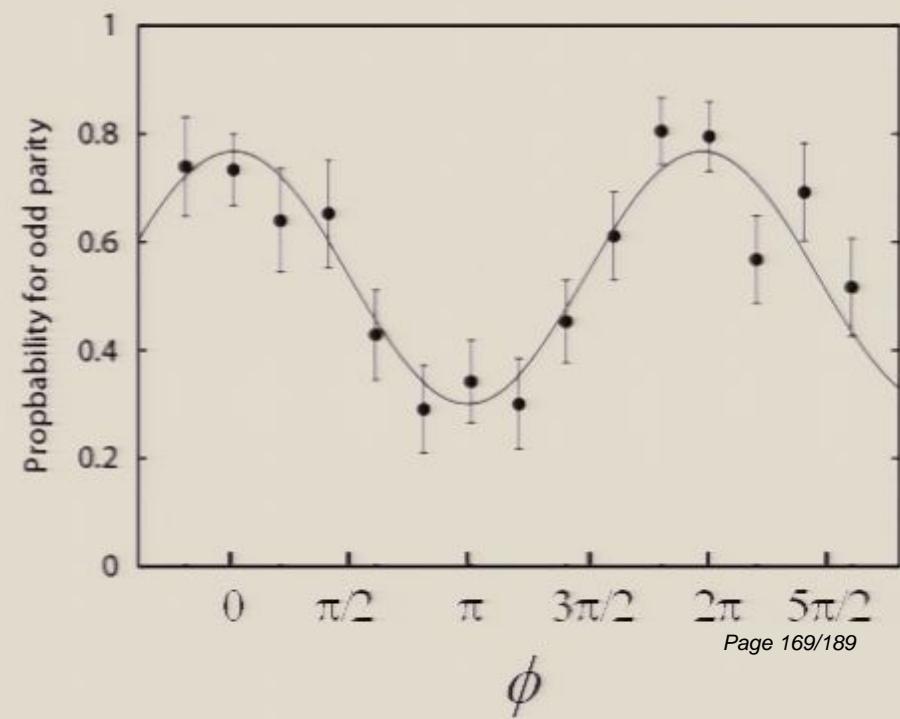
Rotate both qubits by  $\theta=\pi/2$ ,  
with phase difference  $\phi$

$$\begin{aligned} |\downarrow_1 \uparrow_2 - \uparrow_1 \downarrow_2 \rangle &\Rightarrow \\ \cos(\phi/2) (|\downarrow_1 \uparrow_2 - \uparrow_1 \downarrow_2 \rangle) \\ + \sin(\phi/2) (|\uparrow_1 \uparrow_2 - \downarrow_1 \downarrow_2 \rangle) \end{aligned}$$

274 events



502 events



## Measured density matrix:

$$\rho = \begin{pmatrix} \downarrow\downarrow & \downarrow\uparrow & \uparrow\downarrow & \uparrow\uparrow \\ 0.11 & ? & ? & ? \\ ? & 0.38 & -0.24 & ? \\ ? & -0.24 & 0.40 & ? \\ ? & ? & ? & 0.11 \end{pmatrix} \quad \begin{matrix} \downarrow\downarrow \\ \downarrow\uparrow \\ \uparrow\downarrow \\ \uparrow\uparrow \end{matrix}$$

$$\begin{aligned}\text{Fidelity } F &= \langle \Psi^- | \rho | \Psi^- \rangle \\ &= \frac{1}{2}(\rho_{\downarrow\downarrow, \downarrow\downarrow} + \rho_{\uparrow\uparrow, \uparrow\uparrow}) + |\rho_{\downarrow\uparrow, \uparrow\downarrow}| \\ &= 0.63(3)\end{aligned}$$

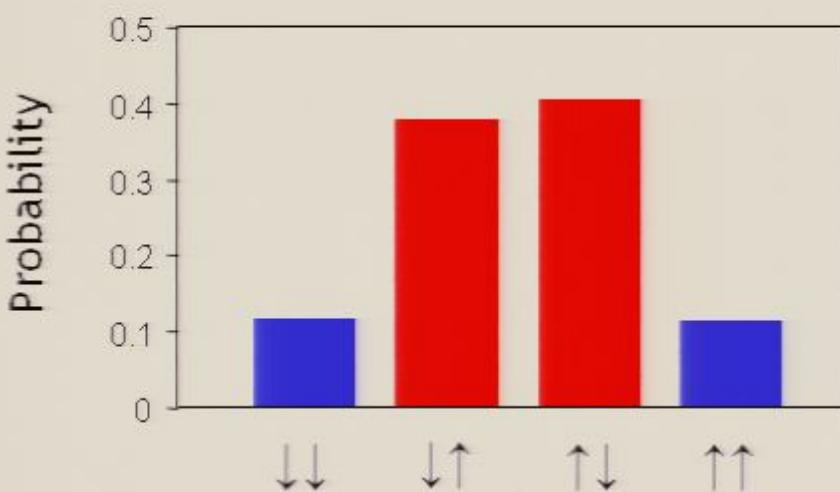
$$\text{Concurrence } C = 0.25(5)$$

Measured ion correlations  
given coincidence photons

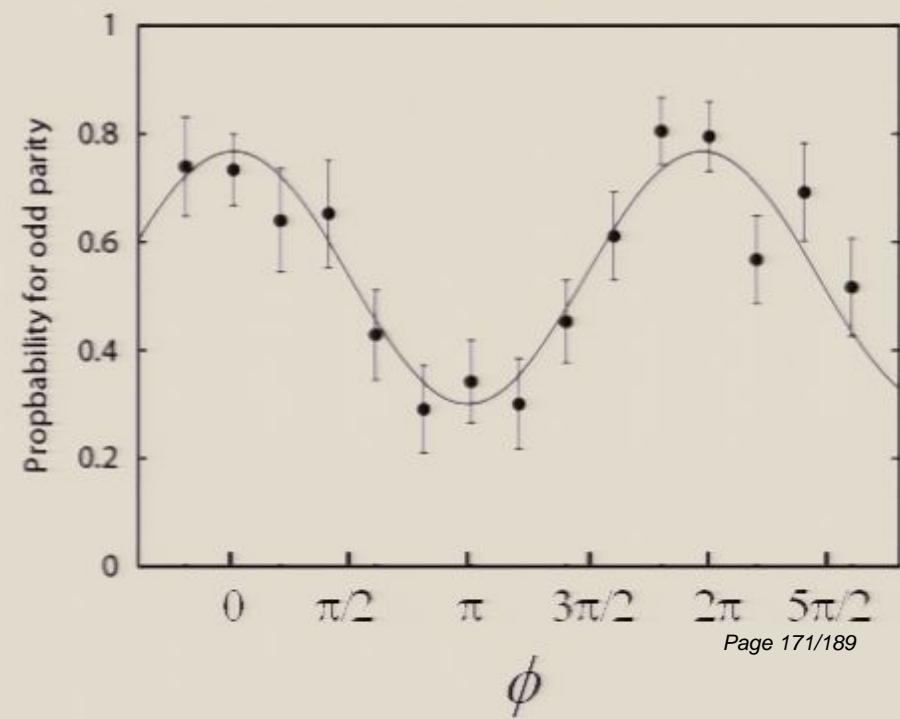
Rotate both qubits by  $\theta=\pi/2$ ,  
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$$\begin{aligned} |\downarrow_1 \uparrow_2 - \uparrow_1 \downarrow_2 \rangle &\Rightarrow \\ \cos(\phi/2) (|\downarrow_1 \uparrow_2 - \uparrow_1 \downarrow_2 \rangle) \\ + \sin(\phi/2) (|\uparrow_1 \uparrow_2 - \downarrow_1 \downarrow_2 \rangle) \end{aligned}$$

274 events



502 events



# Probability of heralding per attempt

$$p = \frac{1}{4} \left[ \frac{1}{2} (0.995)(0.8)(0.5)(0.2)(0.15)(0.02) \right]^2 = 3 \times 10^{-9}$$

Prob. of having singlet Bell state

radiation pattern

branching to  ${}^2D_{3/2}$  state

losses

excitation probability

fiber coupling efficiency

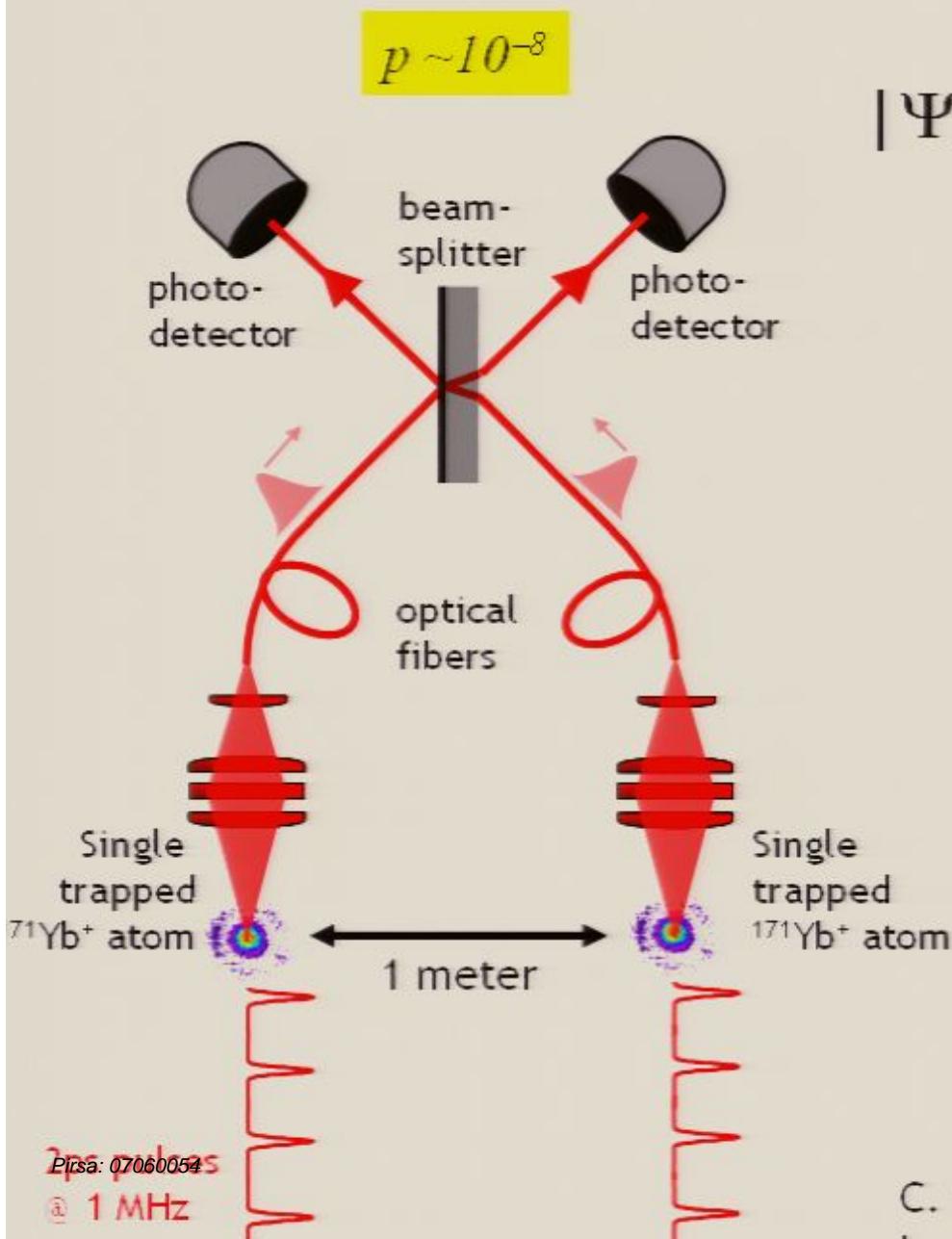
detector efficiency

solid angle

probability of 1 photon emitted and detected

# Rate of heralded entanglement

Now with odd isotopes (having nuclear spin)



$$|\Psi\rangle = (|\downarrow\rangle_1 |\text{blue}\rangle_1 + |\uparrow\rangle_1 |\text{red}\rangle_1) \otimes (|\downarrow\rangle_2 |\text{blue}\rangle_2 + |\uparrow\rangle_2 |\text{red}\rangle_2)$$

$$\Rightarrow |\downarrow\rangle_1 |\uparrow\rangle_2 - |\uparrow\rangle_2 |\downarrow\rangle_2$$

...upon coincidence  
photon detection

insensitive to

- interferometric phase noise
- ion motion

# Probability of heralding per attempt

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prob. of having singlet Bell state

radiation pattern

branching to  ${}^2D_{3/2}$  state

losses

excitation probability

fiber coupling efficiency

detector efficiency

solid angle

probability of 1 photon emitted and detected

The diagram illustrates the calculation of the probability  $p$  of heralding per attempt. The formula is:

$$p = \frac{1}{4} \left[ \frac{1}{2} (0.995)(0.8)(0.5)(0.2)(0.15)(0.02) \right]^2 = 3 \times 10^{-9}$$

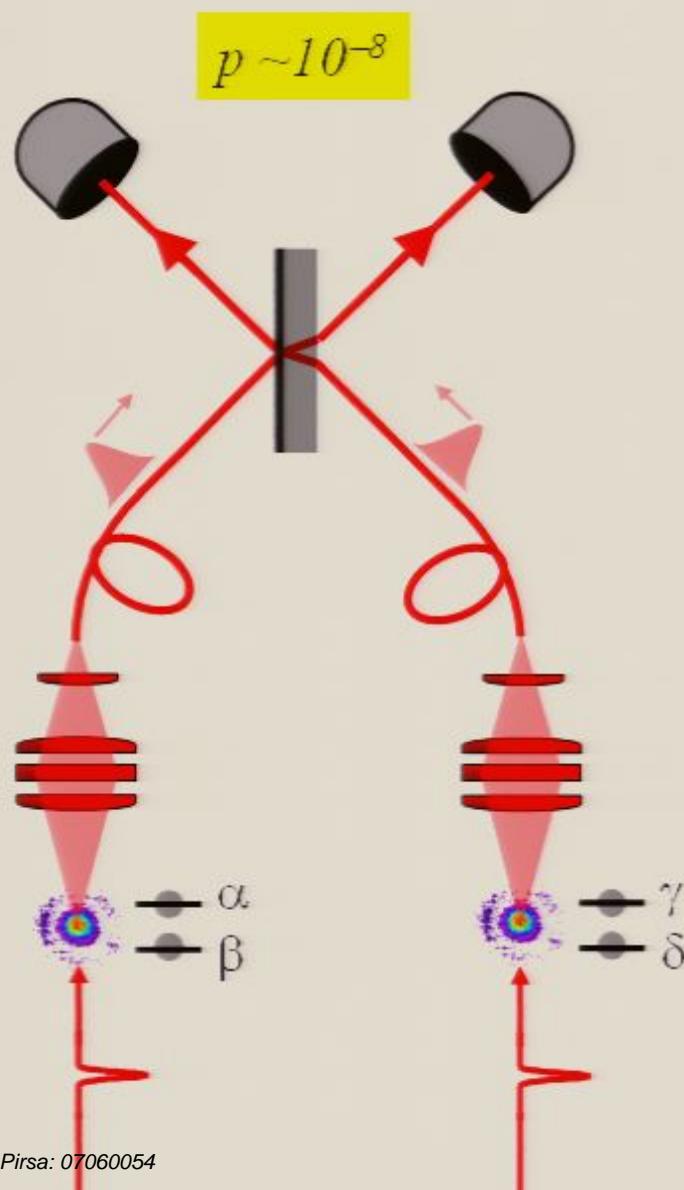
The factors in the formula are labeled as follows:

- Prob. of having singlet Bell state
- radiation pattern
- branching to  ${}^2D_{3/2}$  state
- losses
- excitation probability
- fiber coupling efficiency
- detector efficiency
- solid angle

A bracket above the formula groups the product of the branching factor ( $\frac{1}{2}$ ), excitation probability (0.995), losses (0.8), fiber coupling efficiency (0.5), detector efficiency (0.2), and solid angle (0.15 \* 0.02). Arrows point from each term in the formula to its corresponding label in the diagram below.

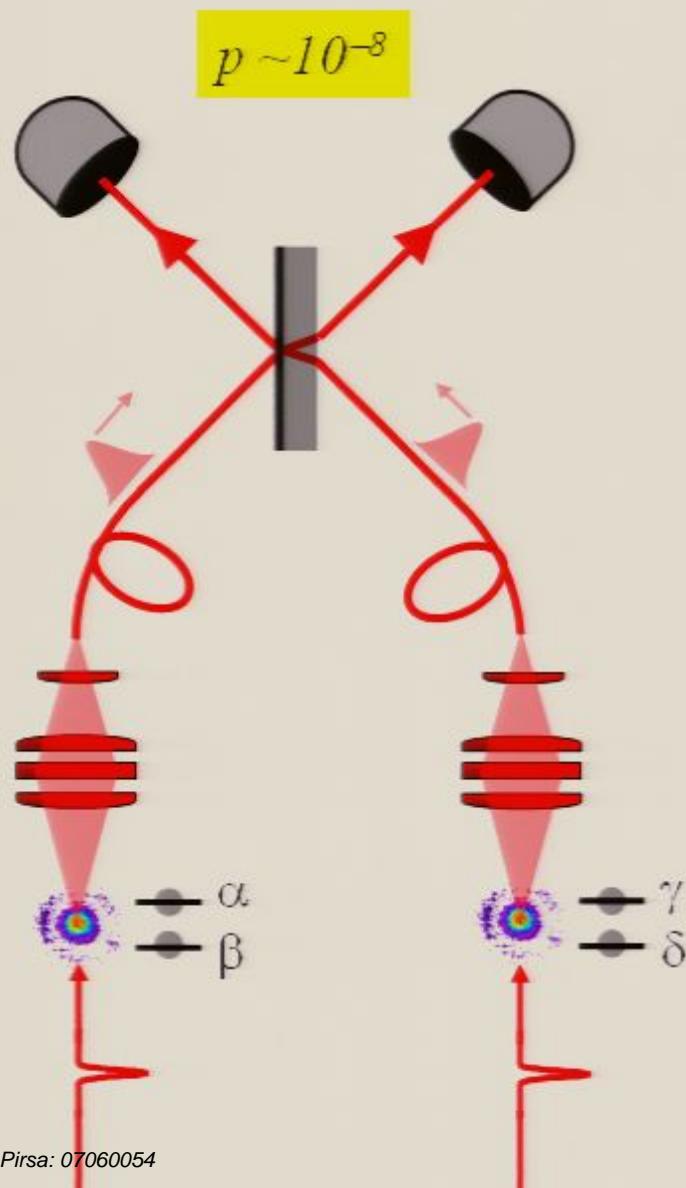
# Rate of heralded entanglement

# But there's more: Remote Gates



$$\begin{aligned} |\Psi\rangle &= (\alpha|\downarrow\rangle_1 + \beta|\uparrow\rangle_1) \otimes (\gamma|\downarrow\rangle_2 + \delta|\uparrow\rangle_2) \\ &\Rightarrow \alpha\delta|\downarrow\rangle_1|\uparrow\rangle_2 - \beta\gamma|\uparrow\rangle_1|\downarrow\rangle_2 \end{aligned}$$

# But there's more: Remote Gates

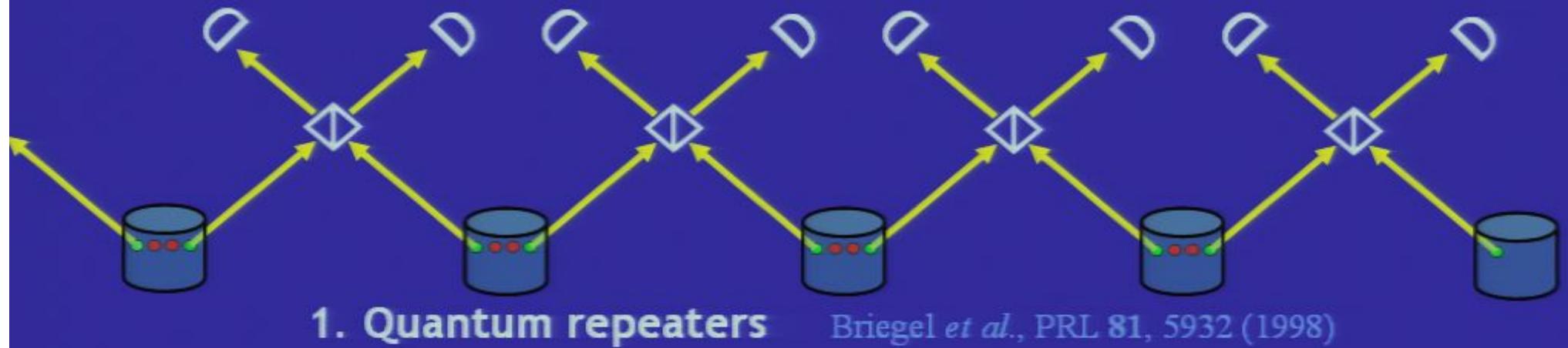


$$\begin{aligned} |\Psi\rangle &= (\alpha|\downarrow\rangle_1 + \beta|\uparrow\rangle_1) \otimes (\gamma|\downarrow\rangle_2 + \delta|\uparrow\rangle_2) \\ &\Rightarrow \alpha\delta|\downarrow\rangle_1|\uparrow\rangle_2 - \beta\gamma|\uparrow\rangle_1|\downarrow\rangle_2 \end{aligned}$$

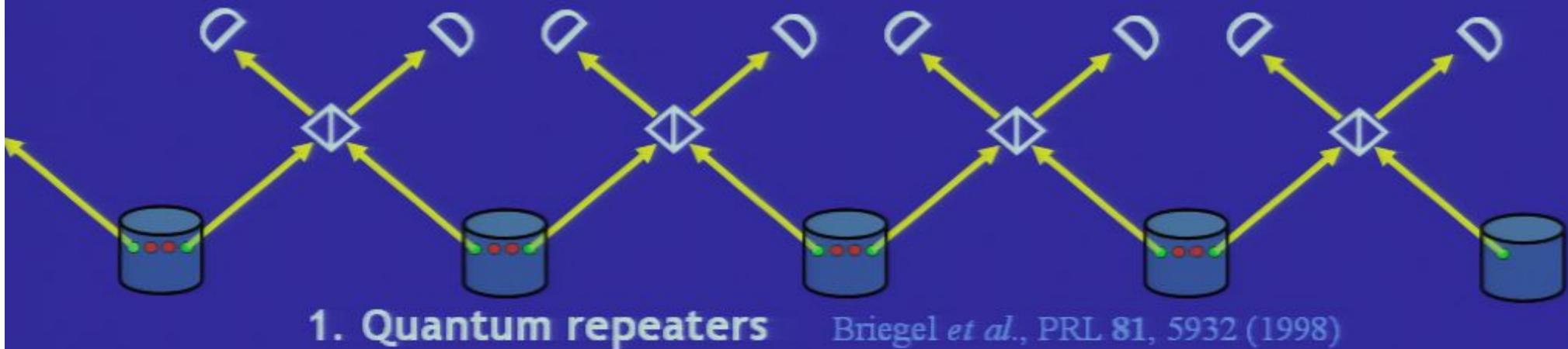
or equivalently,

$$|\Psi\rangle \Rightarrow (I - ZZ)|\Psi\rangle$$

# Quantum networking with probabilistic entanglement



# Quantum networking with probabilistic entanglement



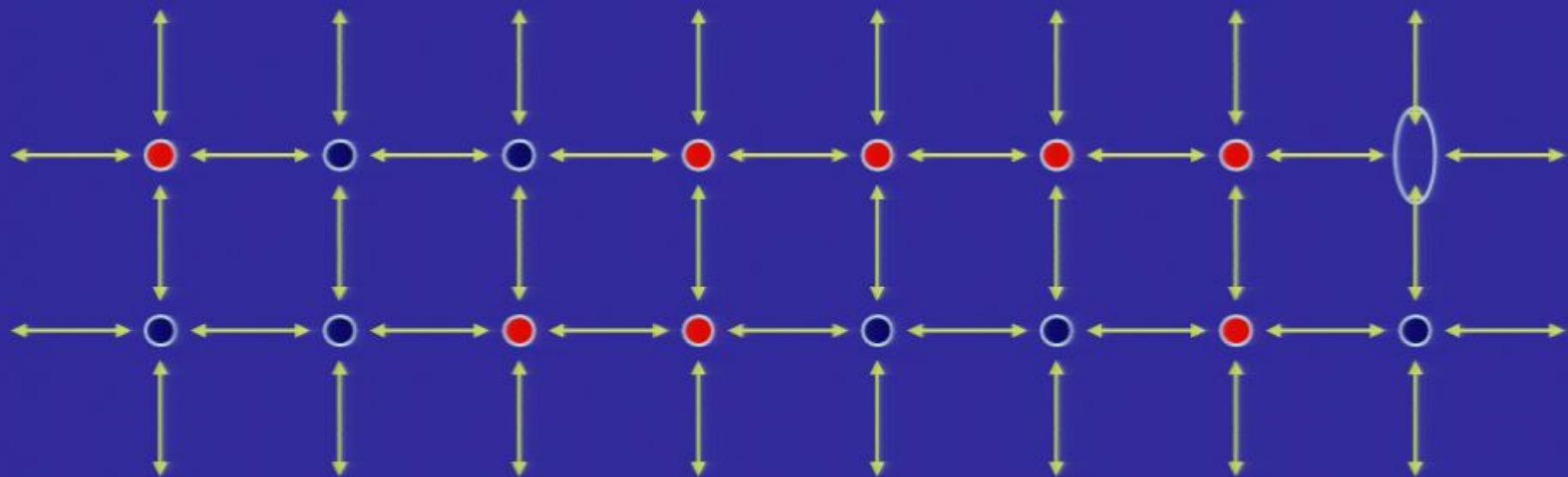
++                    ++                    ++

## 2. Distributed quantum computing with hybrid gates

Duan, et al., Quant. Inf. Comp. 4, 165 (2004)

Quantum computing exclusively  
with probabilistic entanglement

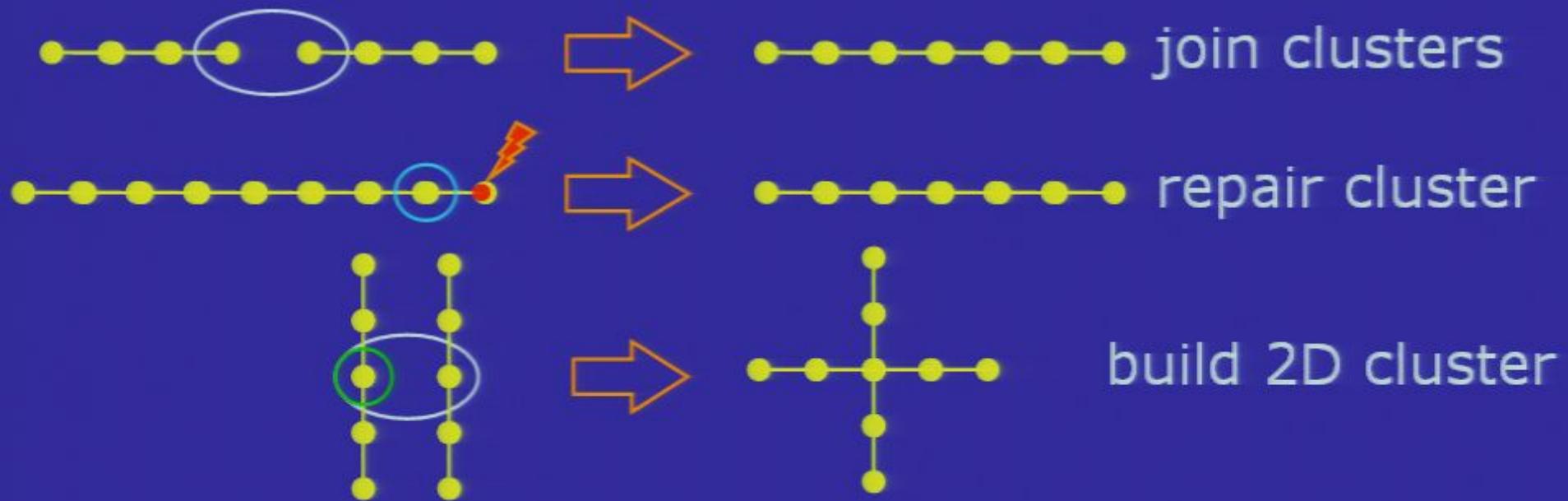
 KLM 409, 46, Nature (2001)



Cluster state quantum computing

Raussendorf and Briegel, PRL **86**, 910 (2001)

# Quantum computing using probabilistic gates



- Efficient computation is possible no matter how small  $p$
- Overhead scales efficiently both with  $1/p$  and  $n$

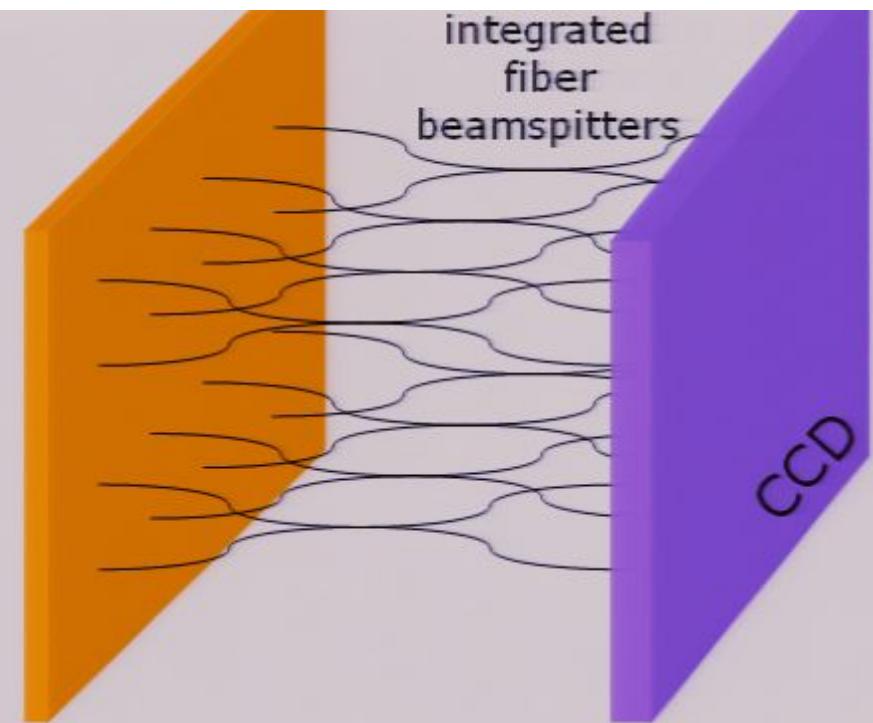
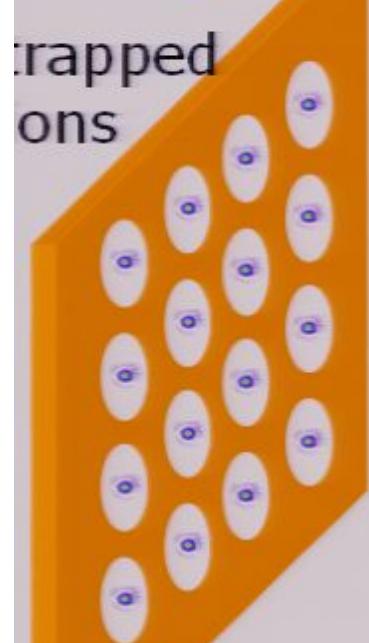
$$\text{time} \approx (1/p)^{\log(4/p)}$$

Duan and Raussendorf, PRL 95, 080503 (2005)

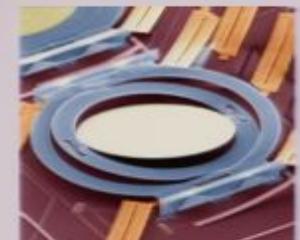
- cluster state link
- control phase flip
- Z - measurement
- X - measurement
- noise

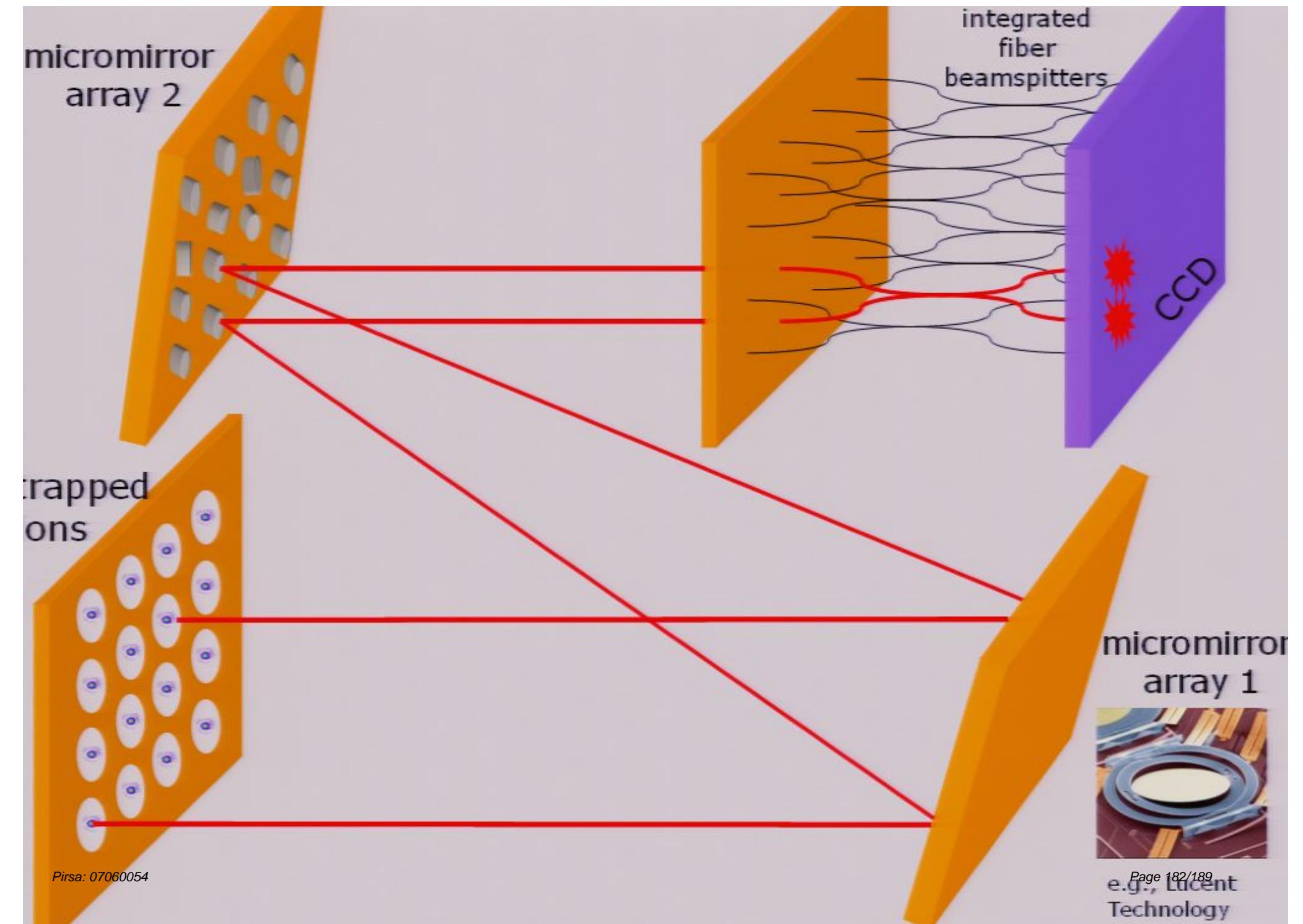
micromirror  
array 2

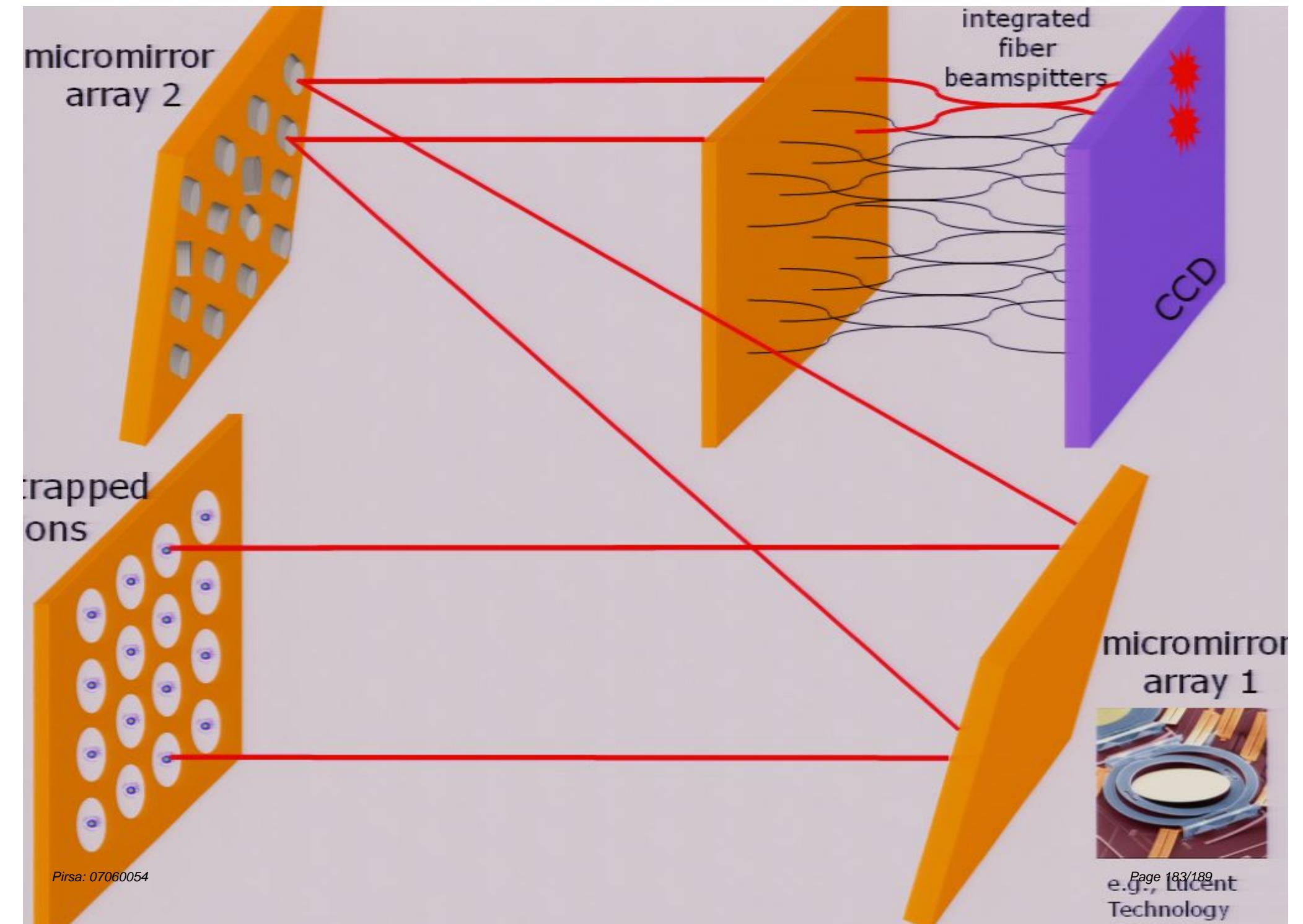
trapped  
ions



micromirror  
array 1







# University of Michigan

## Trapped Ion Quantum Computing

### Grad Students

Mark Acton  
Kathy-Anne Brickman  
Louis Deslauriers  
    to Stanford  
Simcha Korenblit  
Patricia Lee  
    to NIST-G'burg  
Martin Madsen  
    to Wabash Coll.  
David Moehring  
Steven Olmschenk  
Jon Sterk  
Yisa Rumala  
Daniel Stick  
Kelly Younge



<http://iontrap.physics.lsa.umich.edu/>

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Paul Haljan  
    to Simon Fraser U.  
Winfried Hensinger  
    to U. Sussex  
Ming-Shien Chang  
Peter Maunz  
Dzmitry Matsukevich

### Undergrads

Jacob Burress  
    to Missouri

Dan Cook  
David Hucul  
    to MIT

Rudy Kohn  
    to Texas  
Elizabeth Otto  
Mark Yeo

### Collaborators

Luming Duan (Michigan)  
Jim Rabchuk (W. Illinois)  
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# Joint Quantum Institute University of Maryland and NIST

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Louis Deslauriers  
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Simcha Korenblit  
Patricia Lee  
    to NIST-G'burg  
Martin Madsen  
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# University of Michigan

## Trapped Ion Quantum Computing

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# Probability of heralding per attempt

$$p = \frac{1}{4} \left[ \frac{1}{2} (0.995)(0.8)(0.5)(0.2)(0.15)(0.02) \right]^2 = 3 \times 10^{-9}$$

prob. of having singlet Bell state

radiation pattern

branching to  ${}^2D_{3/2}$  state

losses

excitation probability

fiber coupling efficiency

detector efficiency

solid angle

probability of 1 photon emitted and detected

# Rate of heralded entanglement

