Title: The emerging theory of Strong Coupled quark-gluon Plasma

Date: May 22, 2007 11:40 AM

URL: http://pirsa.org/07050050

Abstract:

# The emerging theory of Strongly coupled Quark-Gluon Plasma (sQGP)

Edward Shuryak

Department of Physics and Astronomy

State University of New York

Stony Brook NY 11794 USA

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#### Outline

emerging theory of strongly coupled quark-gluon plasma (sQGP) at T=200-400 MeV, RHIC domain (bits of history and brief summary of main arguments)

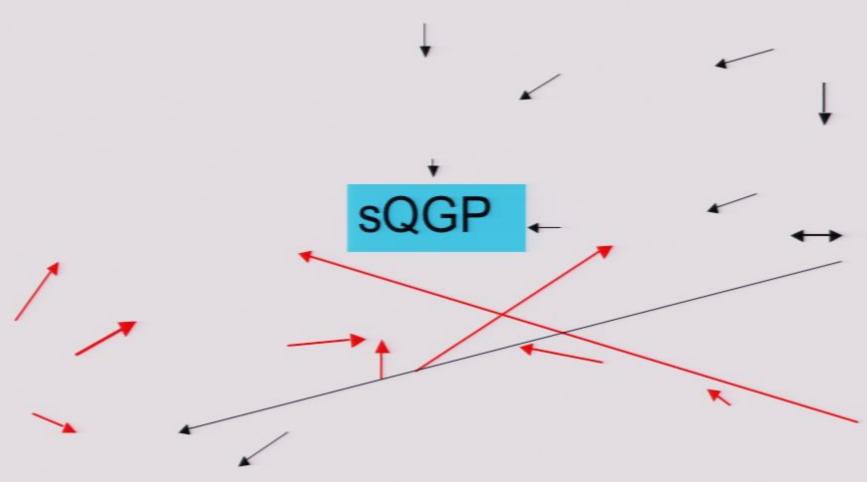
- classical molecular dynamics (MD) of Non-Abelian plasma => eqn describing rotation of color vectors
- electric and magnetic quasiparticles (EQPs and MQPs) are fighting for dominance
- Comparison to AdS/CFT correspondence (Between strongly coupled N=4 SYM and classical MD):

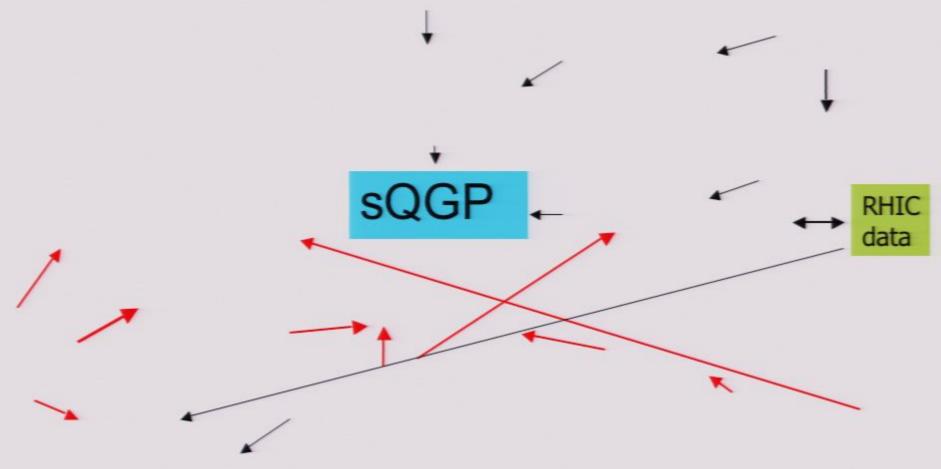
based on 3 papers: B.Gelman, I.Zahed, ES, PRC74, 044908, 044909 (2006)

F.Liao, ES, hep-ph/0611131, PRC 07

M duality=>Flux tubes; (J.F.Liao,ES, in progress)

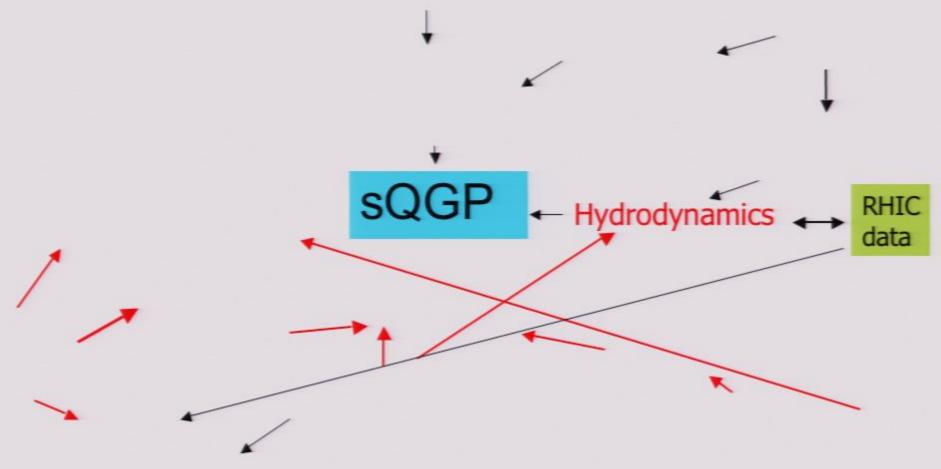
Monopole condensation theory (M.Cristoforetti, ES)





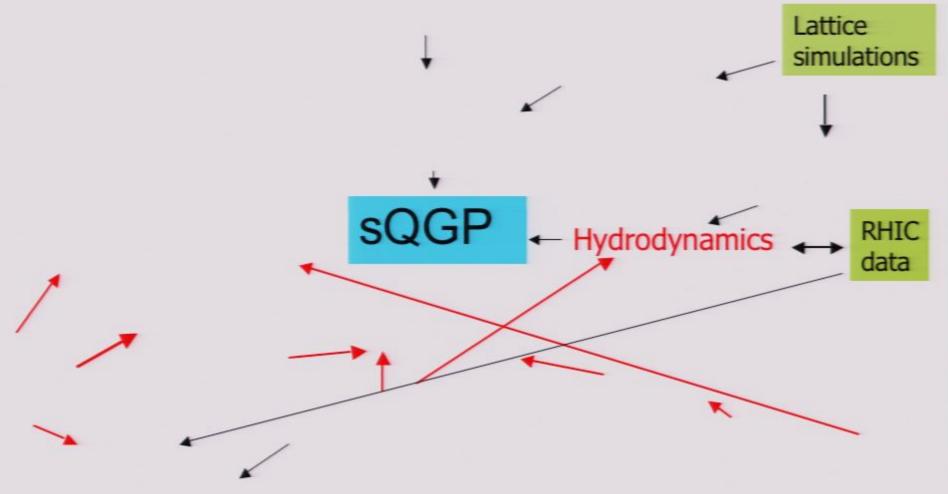
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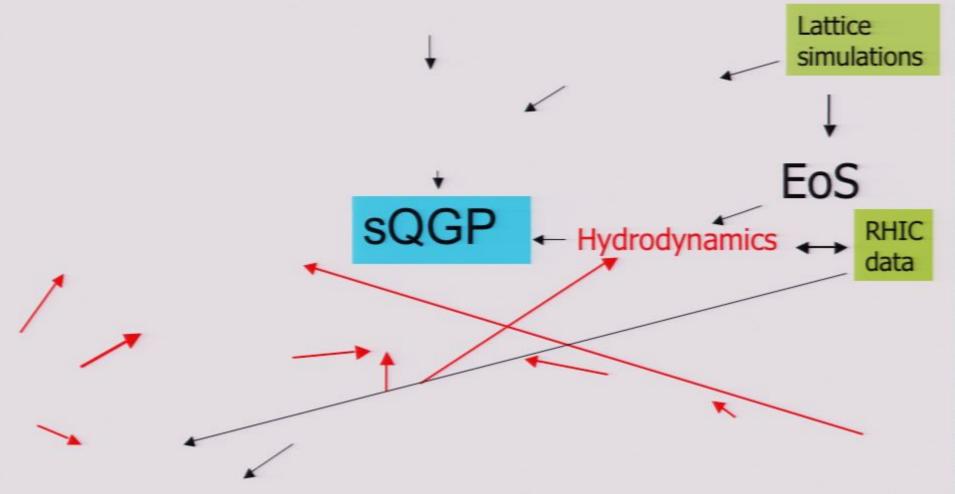
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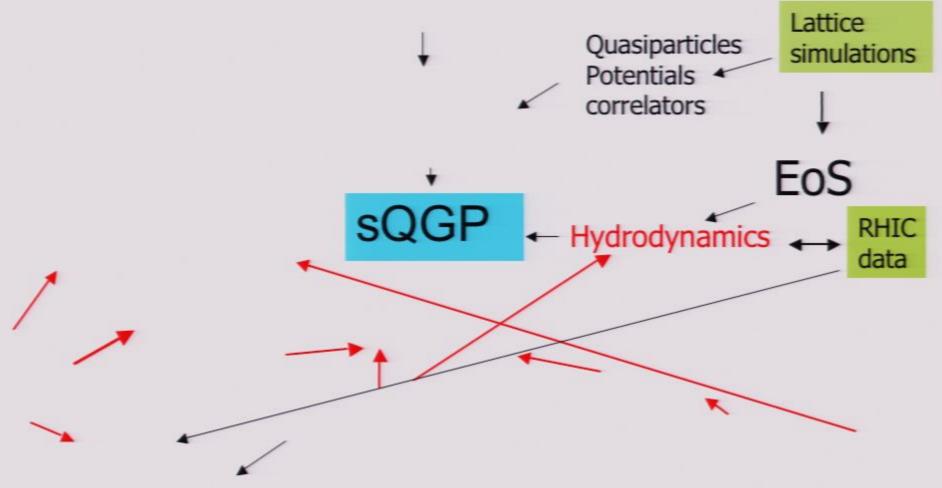
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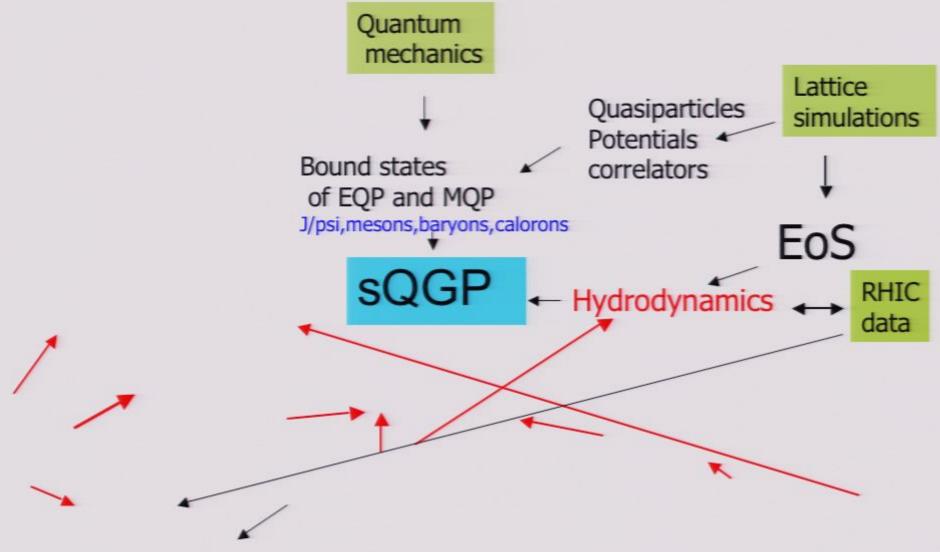
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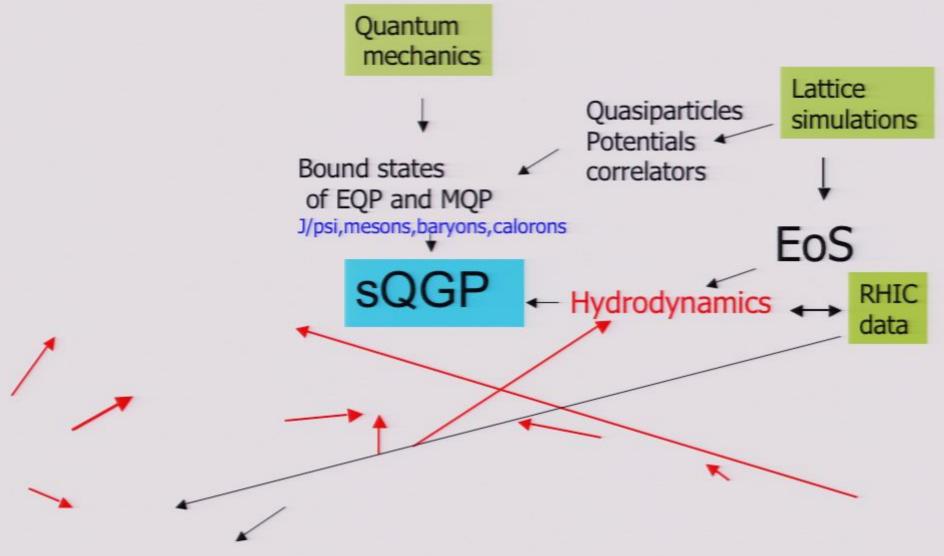


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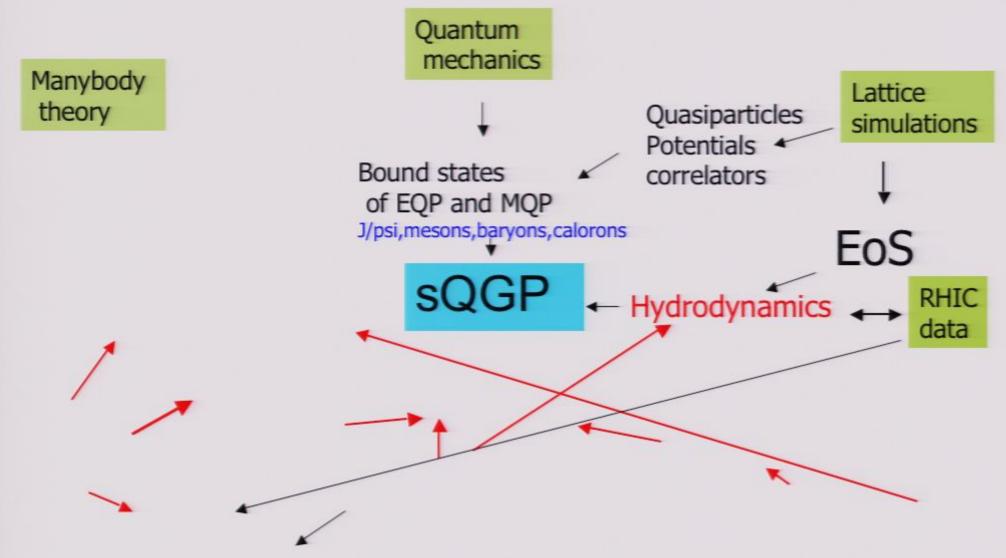
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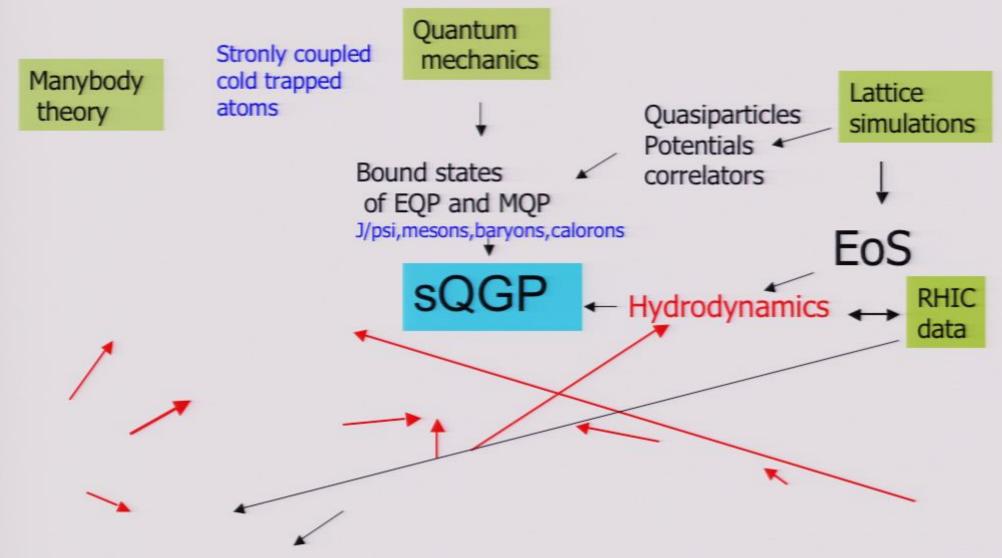


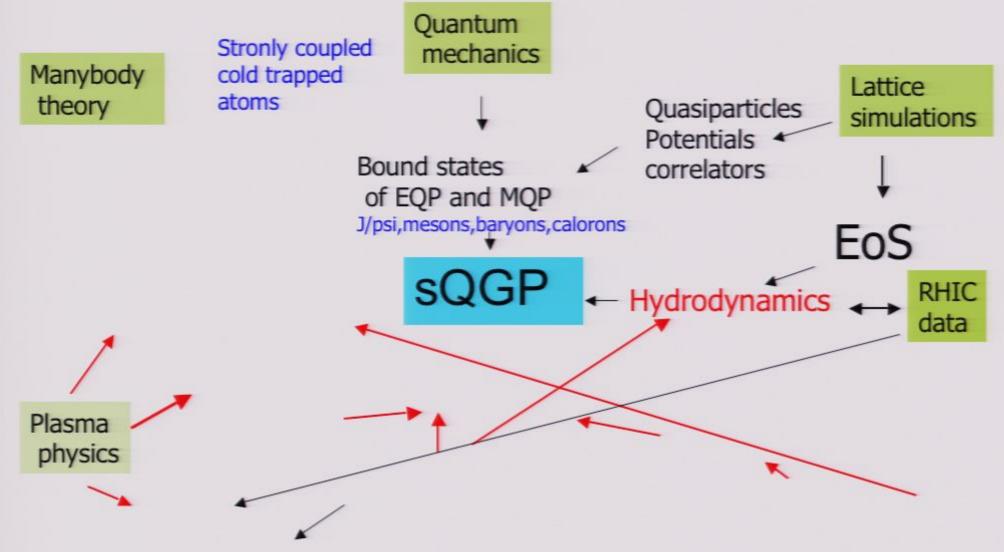




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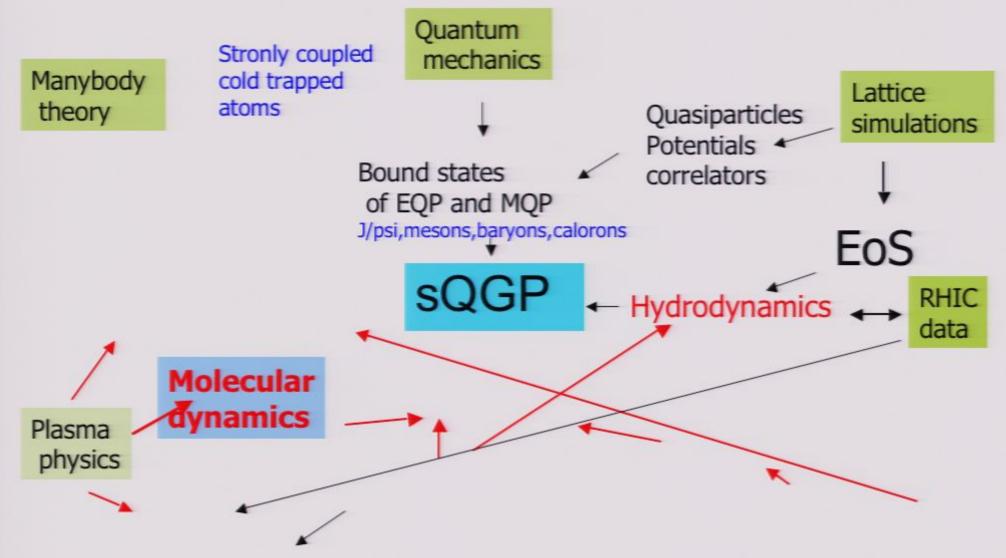


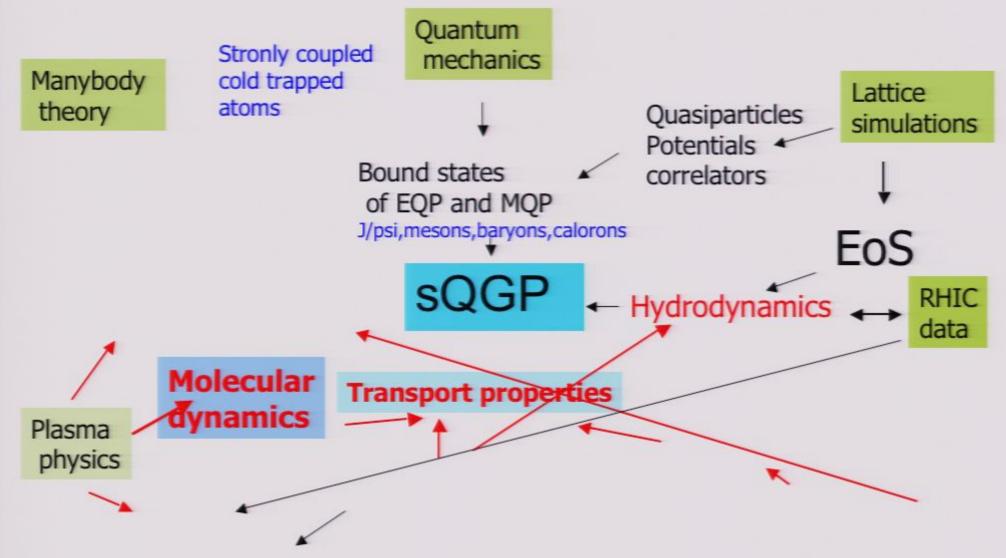


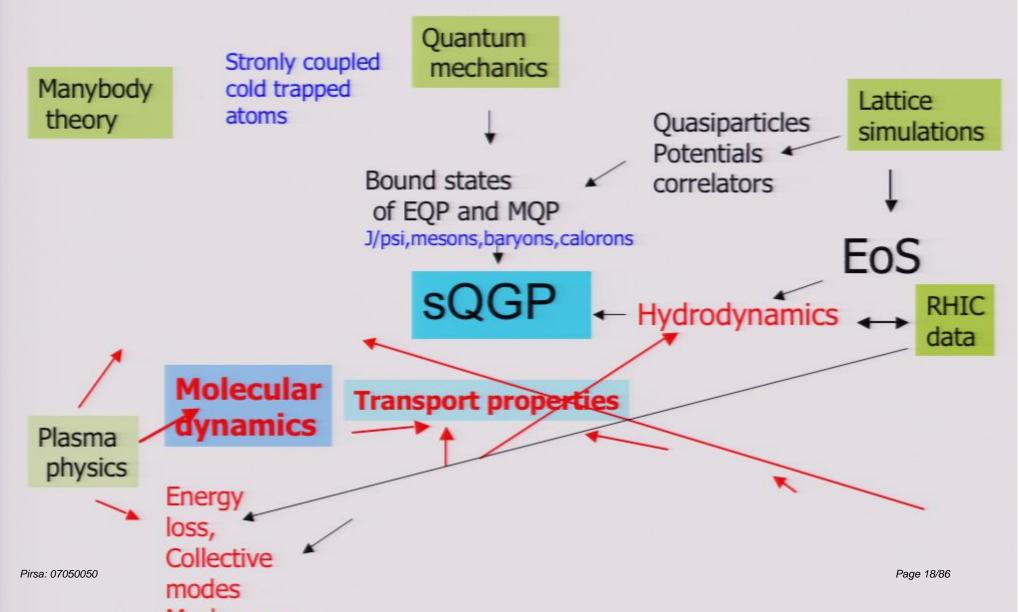


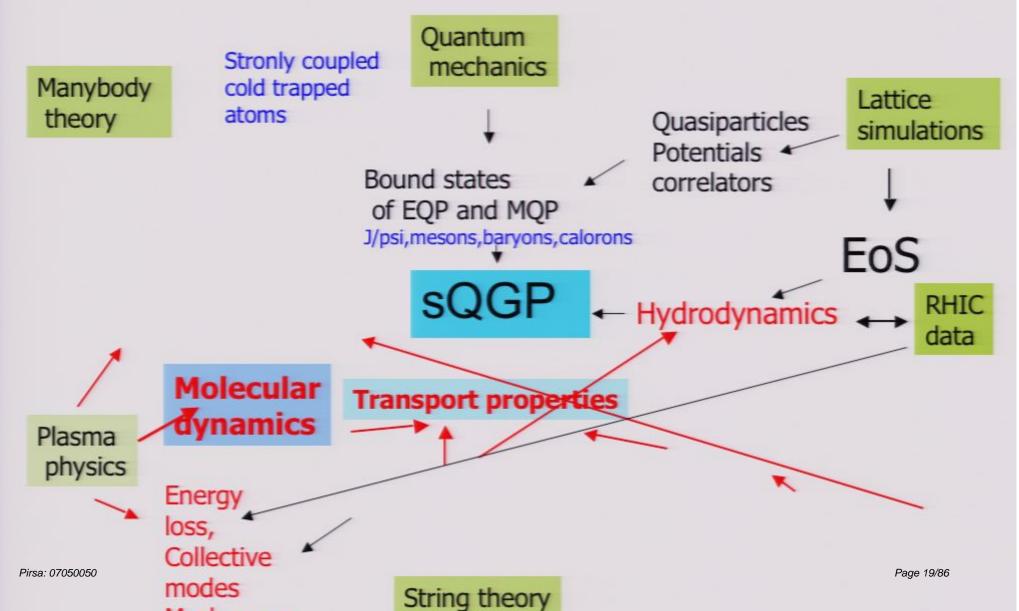
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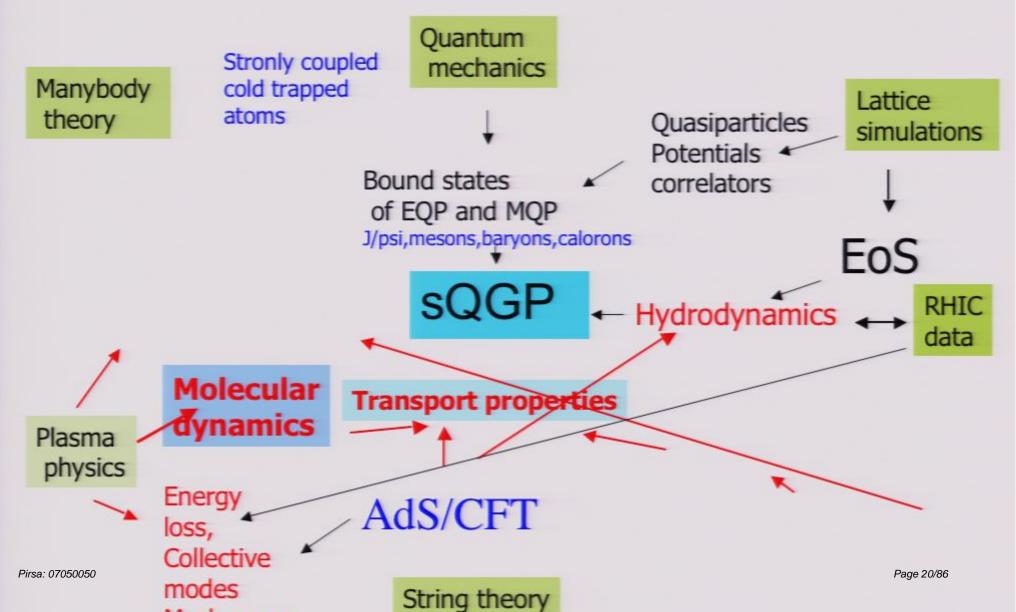
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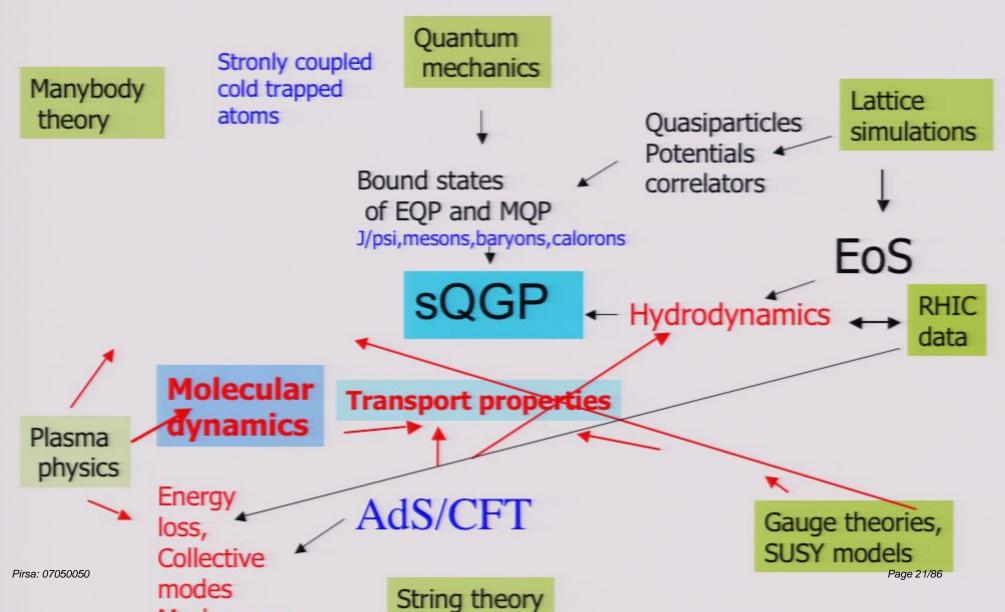


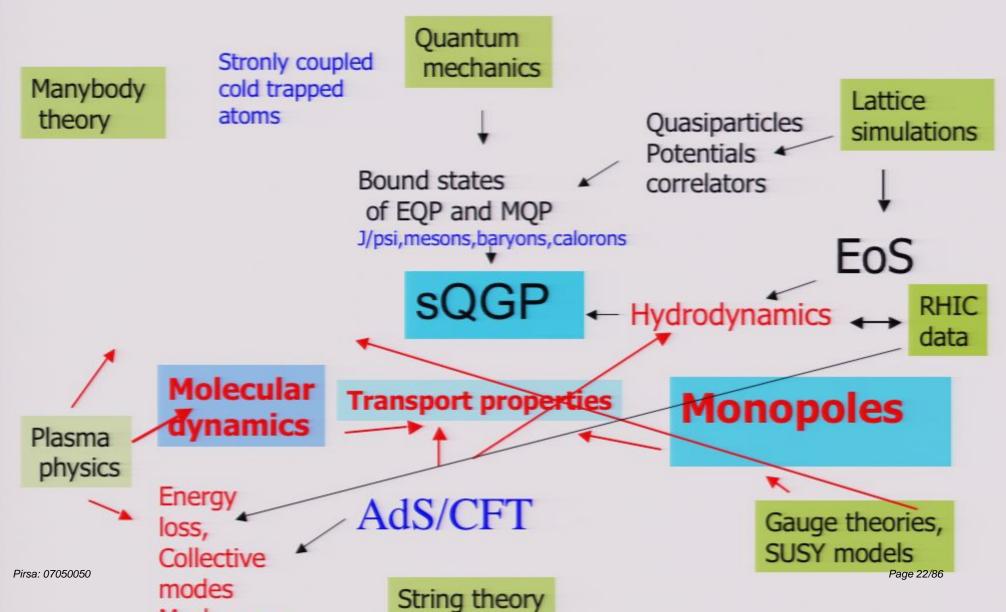


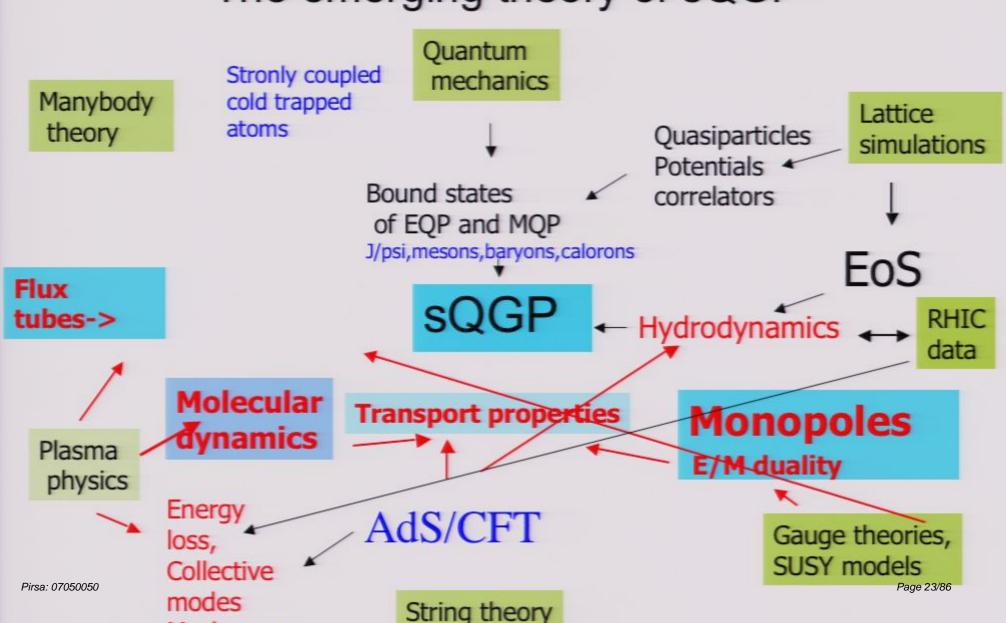


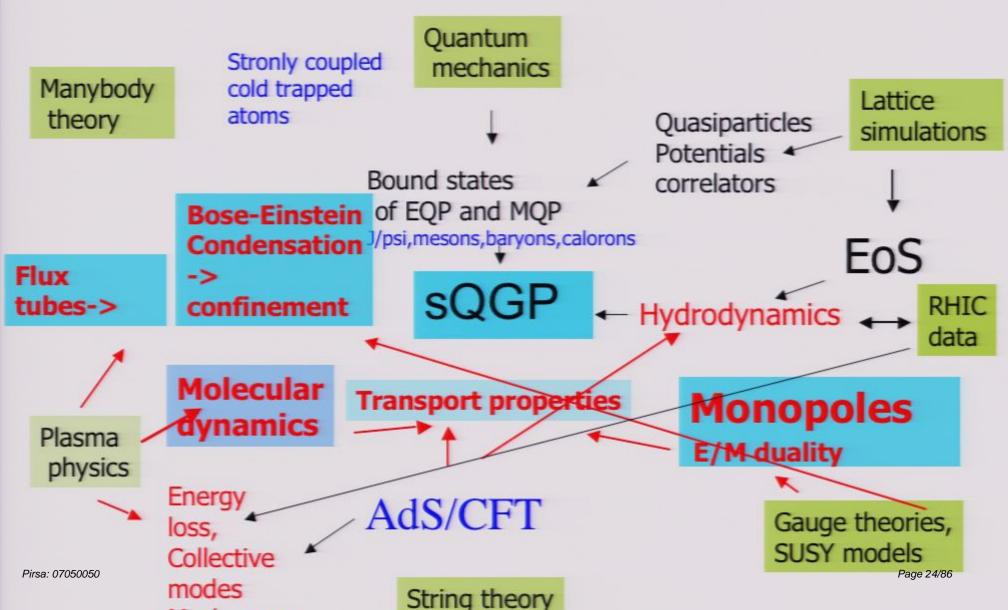


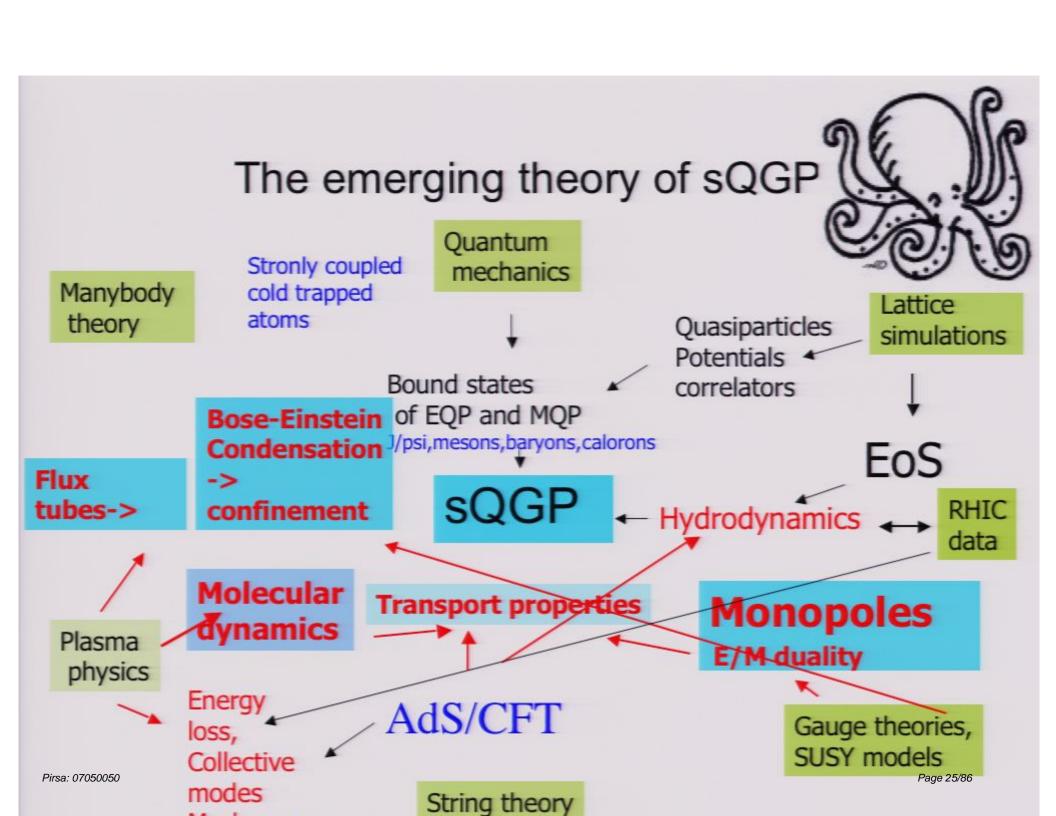






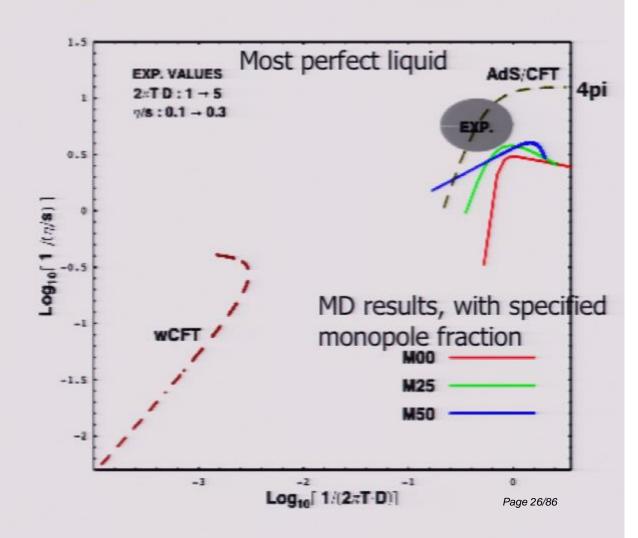






log(inverse viscosity s/eta)- vs. log(invesre diffusion const D\*2piT) (avoids messy discussion of couplings)

- RHIC data: very small viscosity and D
- vs theory -AdS/CFT and MD(soon to be explained)

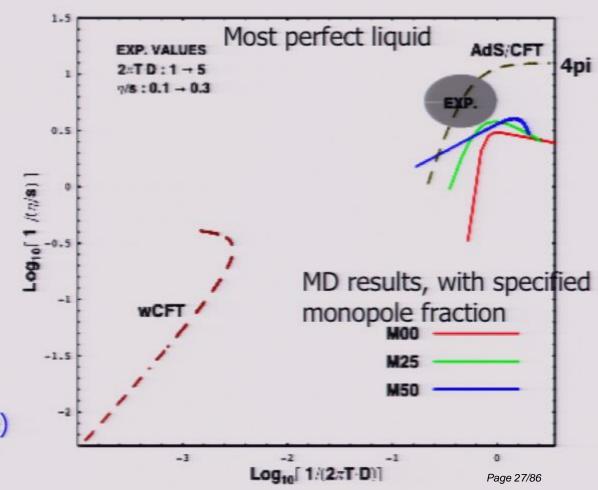


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Weak coupling end =>
(Perturbative results shown here)
Both related to mean free path



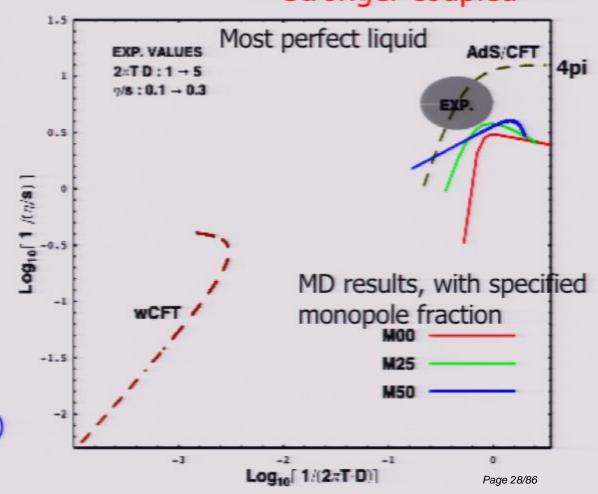
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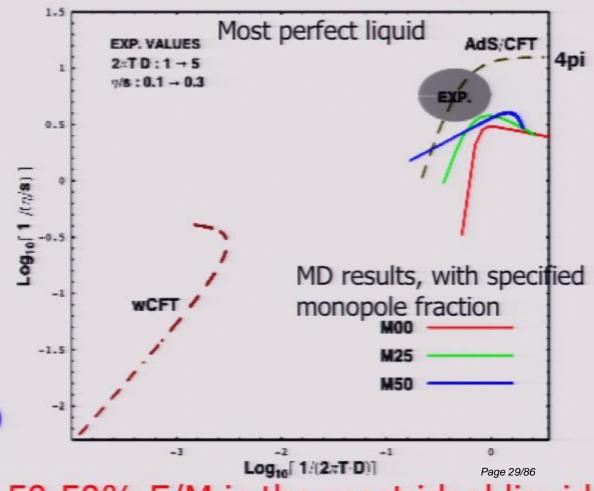


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50-50% E/M is the most ideal liquid

# Magdeburg hemispheres

1656

Air:

P=p(inside)-p(atm)

QCD:

 $P=\#(n.d.f)T^4-B$ 



- •"We cannot pump the QCD vacuum out, but we can pump in something else, namely the Quark-Gluon Plasma" my arguments from 1970's
- QGP was expected to be much simpler than the QCD vacuum, weakly coupled. We now see it is also quite complicated => sOGP...

- Hydro for e+e- as a spherical explosion (ES,PLB 34 (1971) 509)
- => killed by AF in 73 and discovery of jets in e+e- in 76

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ES+Hung, prc57 (1998) 1891, radial flow at PbPb at SPS (with separate freezeout surfaces)

worked! (but nobody cared as cascades did the same)

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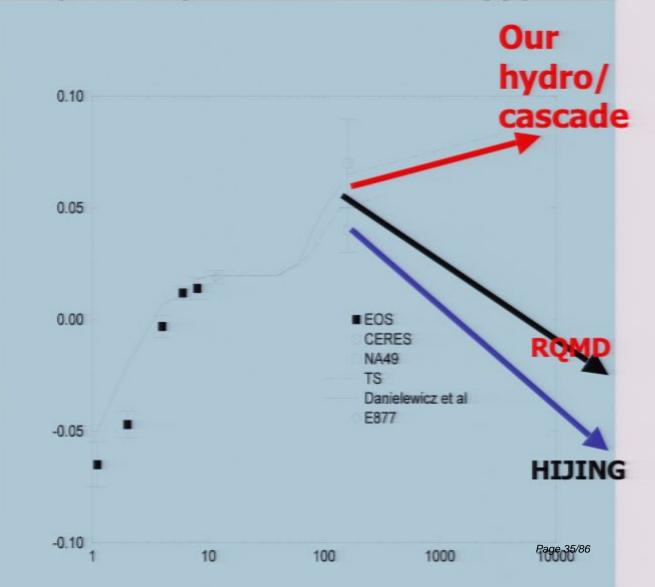
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ES+Hung, prc57 (1998) 1891, radial flow at PbPb at SPS (with separate freezeout surfaces)

Worked! (but nobody cared as cascades did the same)

✓ ES+D.Teaney (99-01) radial and elliptic flows at RHIC worked like a clock! From my QM99 ("RHIC predictions") talk, the ellipticity v2 vs energy

Qualitative
difference
with string
cascades
(RQMD)
and
parton
cascades
(HIJING)



# Sonic boom from quenched jets

Casalderrey, ES, Teaney, hep-ph/0410067; H. Stocker...

- the energy deposited by jets into liquid-like strongly coupled QGP goes into conical shock waves and flow to Mach angle
- One can solve relativistic hydrodynamics and got the flow picture, not too close to the head
- AdS/CFT allows complete treatement (not yet done in full)

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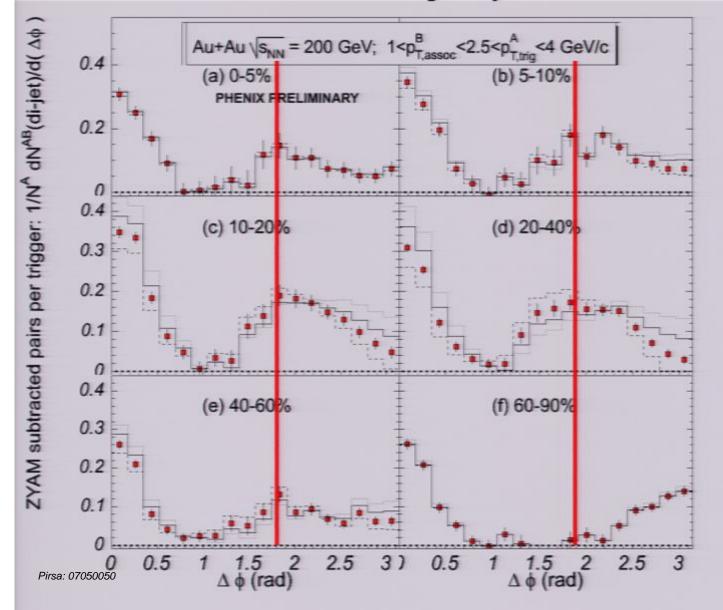
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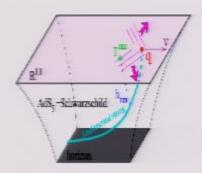
## PHENIX jet pair distribution



Note: it is only projection of a cone on phi

Red line expected Mach
directiton for
<Cs>=.3

#### Freiss, Gubser et al: Mach cone from jets in AdS/CFT



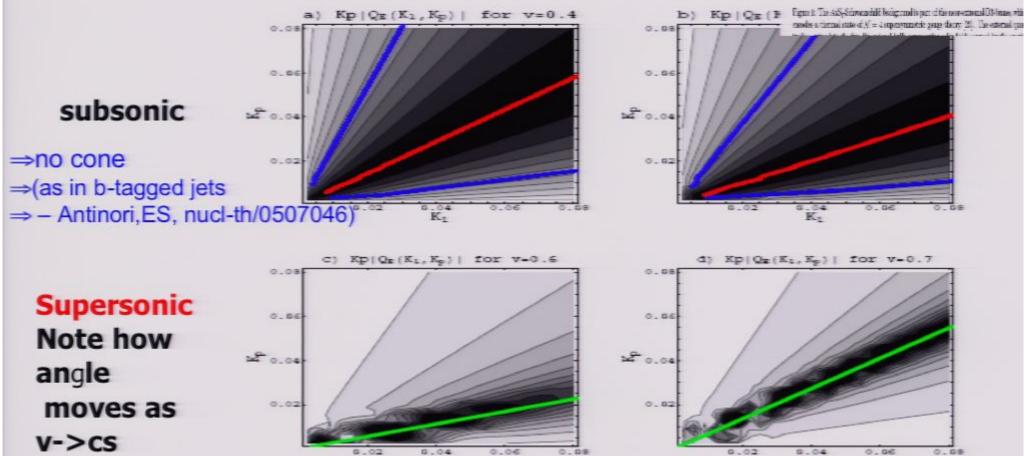


Figure 4: Contour plots of  $K_{\perp}|Q_E^K|$  for various values of v at low momenta. The Pirsa: 07050050 line shows the Mach angle. The red curve shows where  $K_{\perp}|Q_E^K|$  is m. Rage 39/86 zed fo  $K = \sqrt{K_1^2 + K_2^2}$ . The blue curves show where  $K_{\perp}|Q_E^K|$  takes on half its maximum variance.

### 2 Mach cones in strongly coupled plasmas (thanks to B.Jacak)

#### PHYSICAL REVIEW E 68, 056409 (2003)

#### Compressional and shear wakes in a two-dimensional dusty plasma crystal

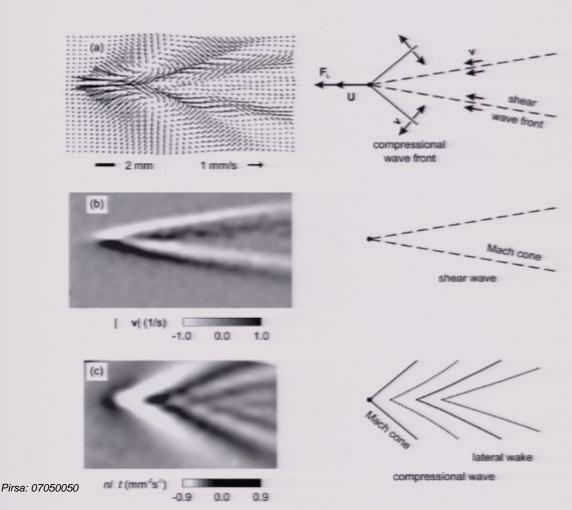
V. Nosenko,\* J. Goree,† and Z. W. Ma Department of Physics and Astronomy, The University of Iowa, Iowa City, Iowa 52242, USA

#### D. H. E. Dubin

Department of Physics, University of California at San Diego, La Jolla, California 92093, USA

#### A. Piel

Institut für Experimenteile und Angewandte Physik, Christian-Albrechts Universität, Kiel, Germany (Received 9 July 2003; published 24 November 2003)



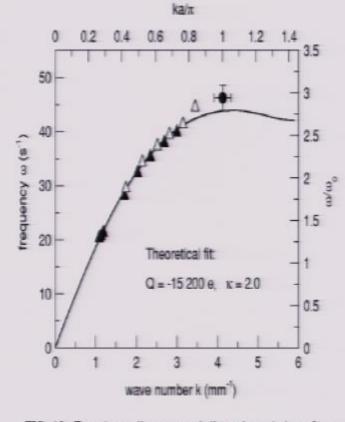


FIG. 13. Experimentally measured dispersion relation of comoressional waves. The points were calculated using the theoretical Page 40/86

# Two main differences between sQGP and electrodynamical plasmas:

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# Two main differences between sQGP and electrodynamical plasmas:

Electrons have the same charge -e at all time, but our quasiparticles (quarks, gluons,...)

have colors which vary in time =>

Gelman, Zahed, ES: Wong eqn for color vectors

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Electrons have the same charge -e at all time, but our quasiparticles (quarks, gluons,...) have COIOIS which vary in time => Gelman, Zahed, ES: Wong eqn for color vectors

There are not only "electric" but also magnetically charged quasiparticles, monopoles and dyons =>

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• For SU(2) charge Q is a unit vector,  $\vec{Q} = (Q^1, Q^2, Q^3)$ 

$$\begin{aligned} dx_i/dt &= p_i/m, \\ dp_i/dt &= (g^2/4\pi) \sum \vec{Q}_i \cdot \vec{Q}_j/r_{ij}^2, \\ d\vec{Q}_i/dt &= (g^2/4\pi) \sum \vec{Q}_i \times \vec{Q}_j/|r_{ij}| \end{aligned}$$

• Note:  $d\vec{Q}_i^2/dt = 0$ 

Wong eqn can be rewritten as x-p canonical pairs, 1 pair for SU(2), 3 for SU(3), etc. known as Darboux variables. We did SU(2) color => Q is a unit vector on O(3)

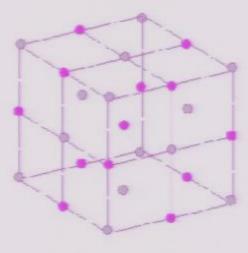
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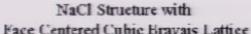
## Classical strongly coupled plasmas

As Gamma= <|Epot|>/<Ekin> grows gas => liquid => solid

- This is of course for +/- Abelian charges,
- But ``green" and ``anti-green" quarks do the same!

#### **NaCl Structure**



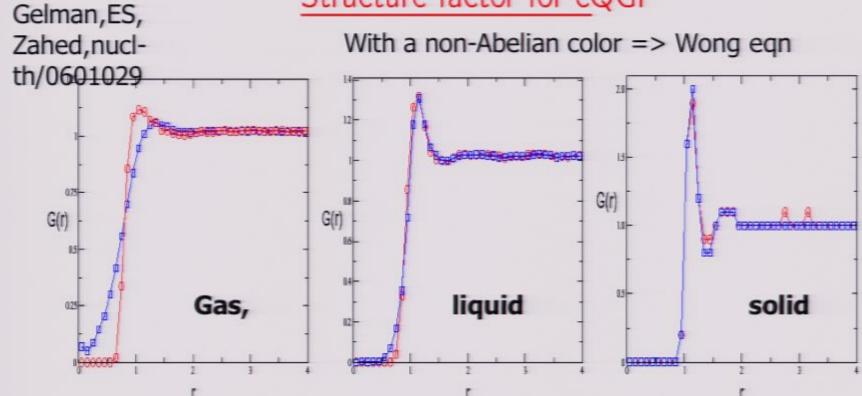




local order would be preserved in a liquid also,
 as it is in molten solts (strongly coupled Two-Component

Plasma with <pot>/<kin>=0(60) (which is an order of magn. larger than in sQGP)

#### Structure factor for cQGP



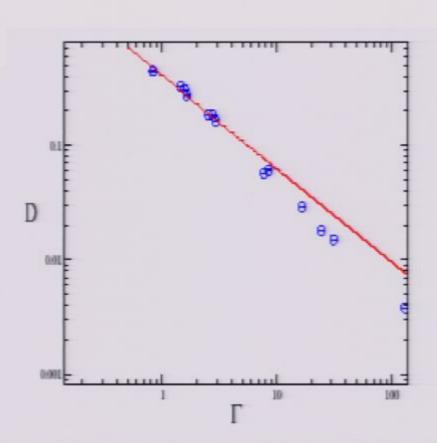
- $G_d$  correlation function for  $\Gamma=0.83,31.3,131$ , respectively; red circles correspond to  $t^*=0$ , and blue squares correspond to  $t^*=6$
- $\Gamma = 0.83$  is a weak correlation between the particles; relaxes rather quickly with time
- The correlation is more robust for  $\Gamma = 31.3$  (*liquid*)
- For  $\Gamma = 131$  correlation is very stable (solid)

# The stronger is coupling, the smaller is diffusion const!

$$D(\tau) = \frac{1}{3N} \left\langle \sum_{i=1}^{N} \vec{v}_i(\tau) \cdot \vec{v}_i(0) \right\rangle$$

$$D = \int_0^\infty D(\tau) \, d\tau$$

$$D \approx \frac{0.4}{\Gamma^{4/5}}$$



Pil(Compare it to AdS/CFT result by Casalderrey-Teaney D\sim 1/lambda.^.5)

# Shear viscosity

Green-Kubo relation for viscosity

$$\eta = \int_0^\infty \eta(\tau) \, d\tau$$

$$\eta(\tau) = \frac{1}{3 \, TV} \left\langle \sum_{x < y} \sigma_{xy}(\tau) \, \sigma_{xy}(0) \right\rangle$$

 $\sum_{x < y}$ —a sum over the three pairs of distinct tensor components (xy, yz and zx); the stress-energy tensor are given by

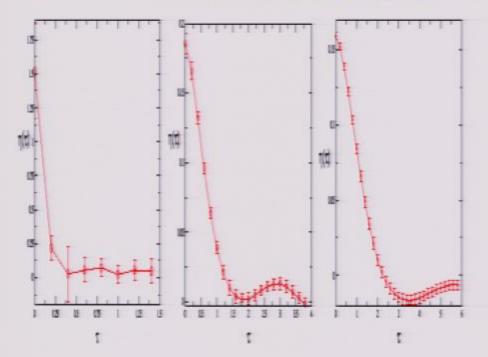
$$\sigma_{xy} = \sum_{i=1}^{N} m_i v_{ix} v_{iy} + \frac{1}{2} \sum_{i \neq j} r_{ij,x} F_{ij,y}$$

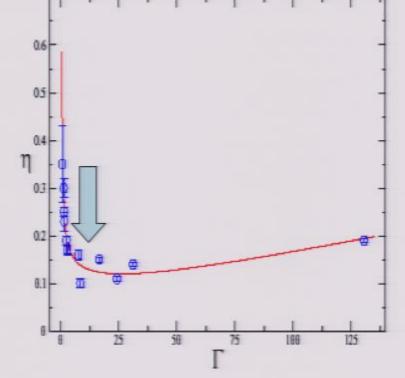
 $ec{F}_{ij}$  is the force on particle i due to particle j

### Viscosity does not disappear but has a minimum

QGP coupling (blue arrow) seems to be about the best liquid one can possibly make

translated to sQGP => eta/s= 3 or so <<1





• Stress-tensor autocorrelation correlation function  $\eta(t)$  for  $\Gamma=$ 

0.83, 31.3, 131

$$\eta \approx 0.001 \,\Gamma + \frac{0.242}{\Gamma^{0.3}} + \frac{0.072}{\Gamma^2}$$

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# sQGP= new type of plasma, containing competing electric / magnetic quasiparticles

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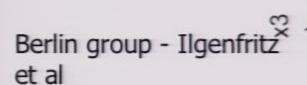


# Why Higgsing and monopoles?

- SUSY gauge theories have large degenerate moduli spaces with Energy=0, with rich variety of Higgsing and magnetic objects
- QCD at T can be viewed as a superposition as all of them, with some weight W(<A\_0>)
- Magnetic screening mass is nonzero: in fact lattice told us it exceeds electric for T<1.4Tc</li>
- Monopoles/dyons can be traced on the lattice directly, especially while Nc of them make calorons (finite T instantons)

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One can see monopoles/dyons
In lattice gauge theory simulations

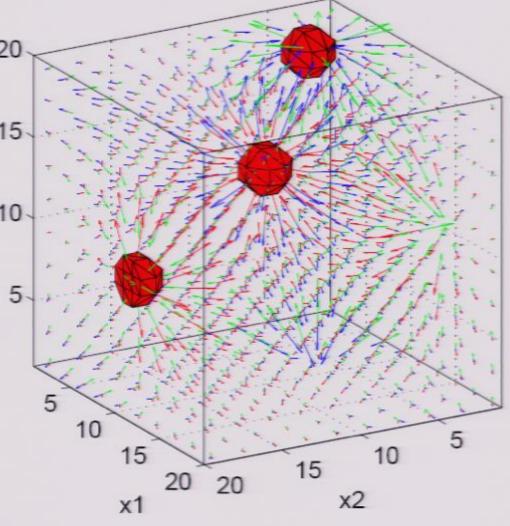


Red, blue and green U(1) fields

3 dyons with corresp.

Field atrengths, SU(3),

Each (1,-1,0) charges



# New (compactified) phase diagram describing an electric-vs-magnetic competition

Dirac condition (old units e^2=alpha)

$$\frac{eg}{\hbar c} = \frac{n}{2}$$

<- n=2 adjoint

Т

00

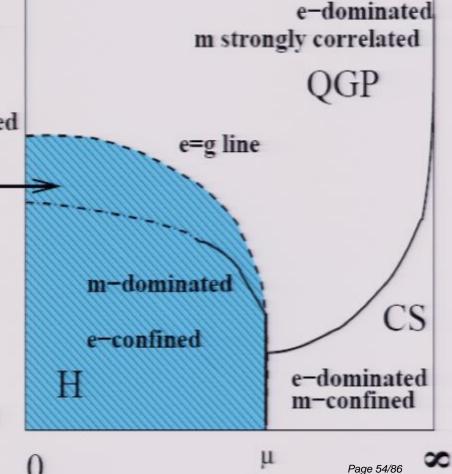
Thus at the e=g line

$$e^2/\hbar c = g^2/\hbar c = 1$$

m-dominated e strongly correlated

Near deconfinement line g->0 in IR (Landau's U(1) asymptotic freedom)

=> e-strong-coupling



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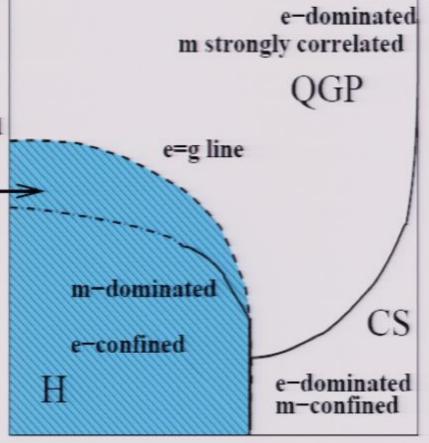
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## => e-strong-coupling

Why is this diagram better? =>

Three 0705005 re e-flux tubes in all blue region, not only in the

refined abased to fact, their are marriagelly subsuced at To



ш

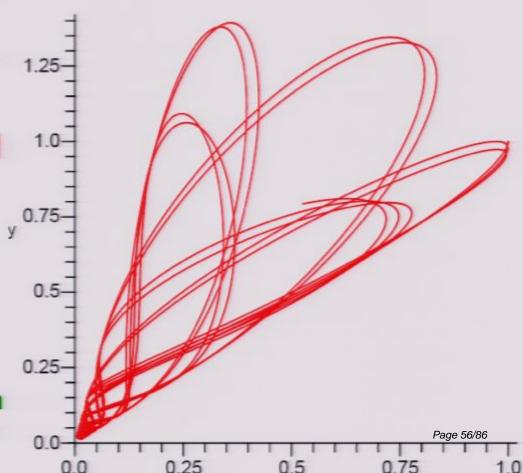
### How MQPs+EQPs move?

(2 pedagogical examples before we deal with a plasma)

(1) one MQP (dyon)+one static e-charge

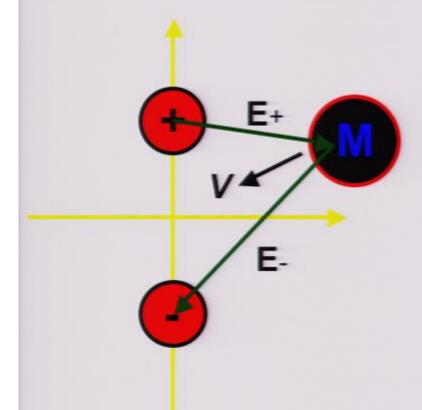
A.Poincare => the motion is restricted to a cone
angular momentum of the field J from ExB|| to r J=hbar\*(n/2) <= Dirac g\_e g\_m/hbar c=N/2
=> Monopoles of any sign repel from a charge because Their rotation makes a repelling dipole (also think of quantum mech.=> localization energy!

Here is my solution for a dyon (with a bital on solution for a dyon (with a bital on





# Second (and now entirely new) problem: static eDipole+MPS



Note that Lorentz force is O(v)!

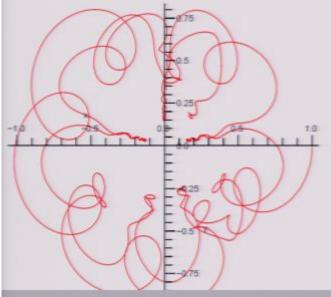
$$M\frac{d^2\vec{r}}{dt^2} = \frac{g}{c}\vec{E} \times \frac{d\vec{r}}{dt}$$

$$\vec{E} = e \left[ \frac{\vec{r} - a\vec{z}}{|\vec{r} - a\vec{z}|^3} - \frac{\vec{r} + a\vec{z}}{|\vec{r} + a\vec{z}|^3} \right]$$

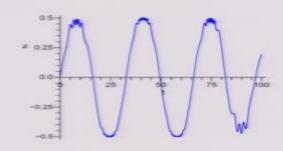
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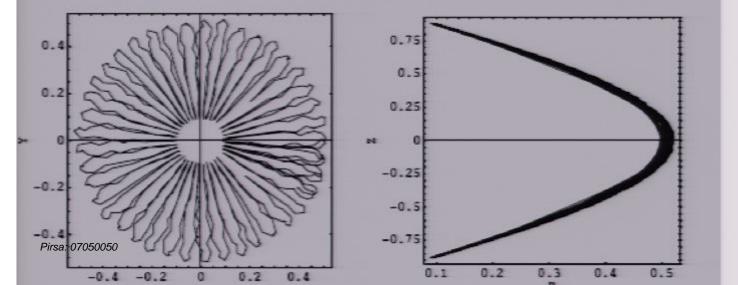
## We found that **two charges** play pingpong by a monopole without even

moving!



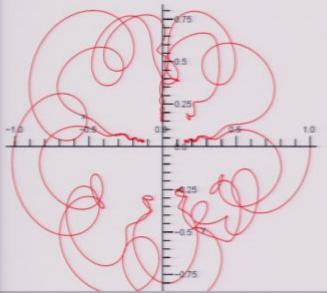
Chaotic, regular and escape trajectories for a monopole, all different in initial condition by 1/1000 only!



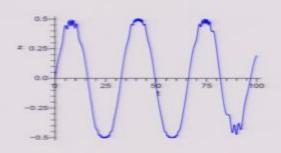


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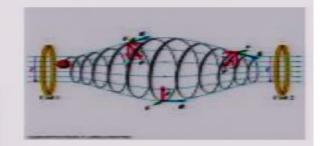
moving!

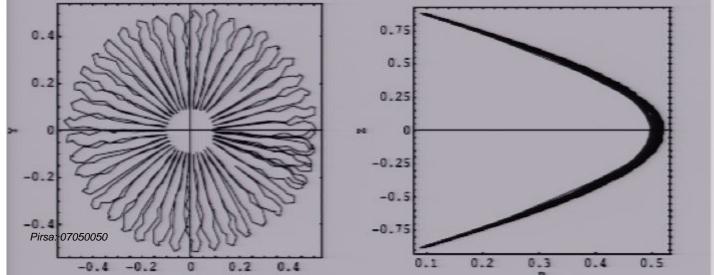


Chaotic, regular and escape trajectories for a monopole, all different in initial condition by 1/1000 only!



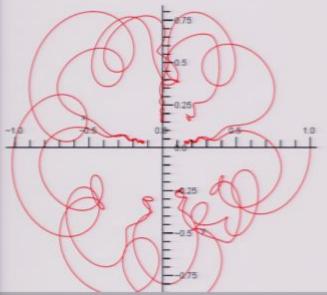
Dual to Budker's magnetic bottle



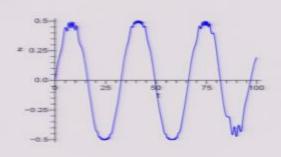


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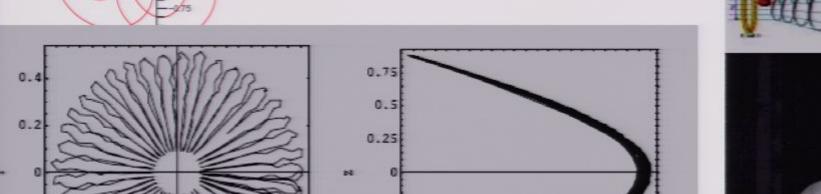
moving!



Chaotic, regular and escape trajectories for a monopole, all different in initial condition by 1/1000 only!



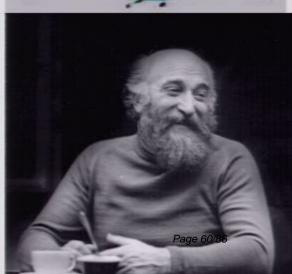
Dual to Budker's magnetic bottle



-0.25

-0.5

-0.75

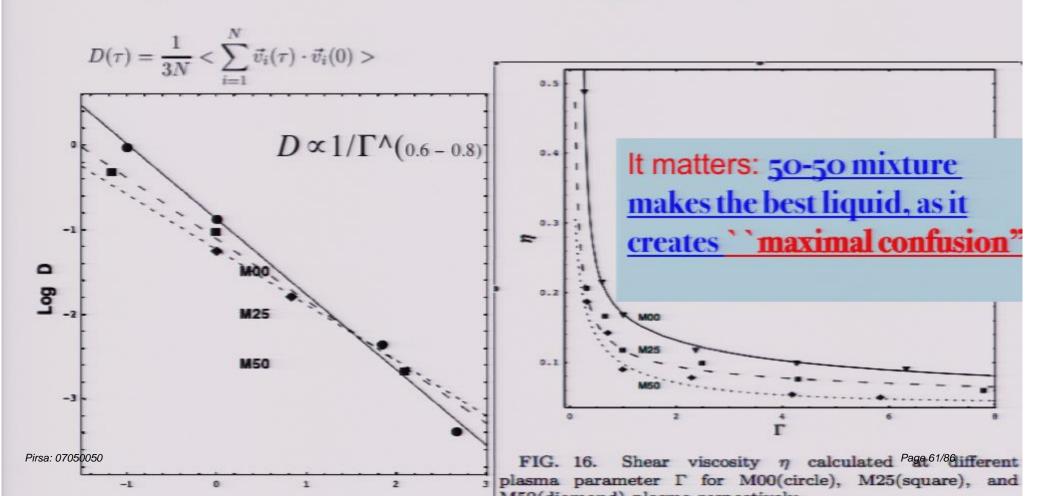


## MD simulation for plasma with monopoles

(Liao, ES hep-ph/0611131)

monopole admixture M50=50% etc

again diffusion decreases indefinitely, viscosity does not



### We identified 3 collective modes

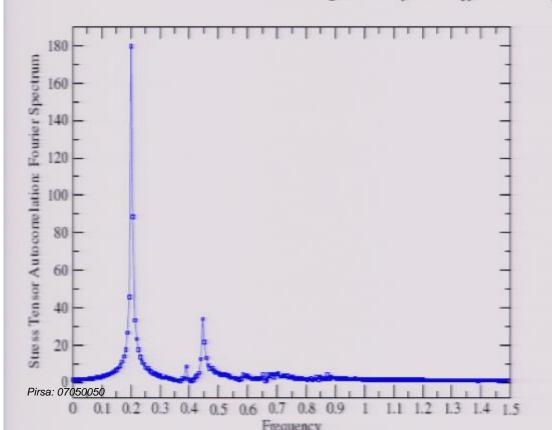
(1000 particles in a stable spherical drop)

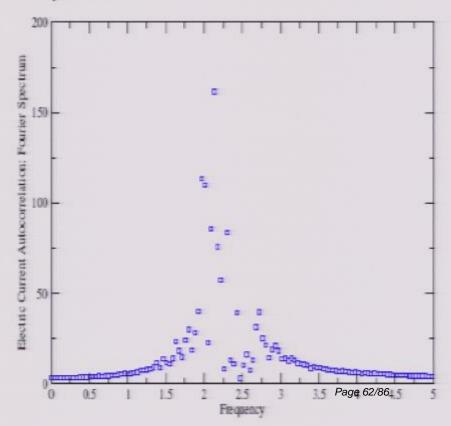
I=0 breathing =>diffusion; I-2 quadrupole => shear viscosity, I=1 plasmon => conductivity

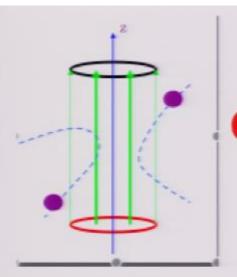
and studied the dependence of their fequencies and

widths on coupling...

Quadrupole (phonon) and plasmon

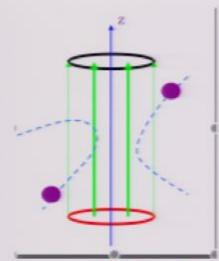






(with J.F.Liao)

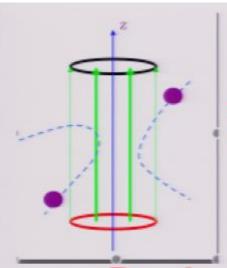
Pirsa: 07050050 Page 63/86



(with J.F.Liao)

 Dual superconductivity as a confinement mechanism ('tHooft, Mandelstam 1980's) => monopole condensation at T < Tc => electric flux tubes dual to Abrikosov vortices

Pirsa: 07050050 Page 64/86

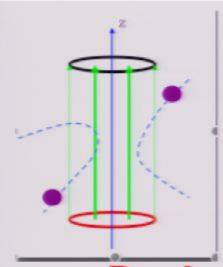


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But at T>Tc (uncondenced) MQPs do the same! Due to Lorentz force MQPs are reflected from a region with E field => pressure => flux tubes compression in plasma

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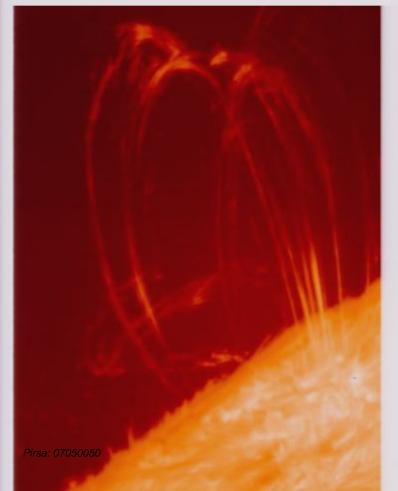
Pirsa: 07050050

Page 66/86

(work without any superconductor!)

Pirsa: 07050050 Page 67/86

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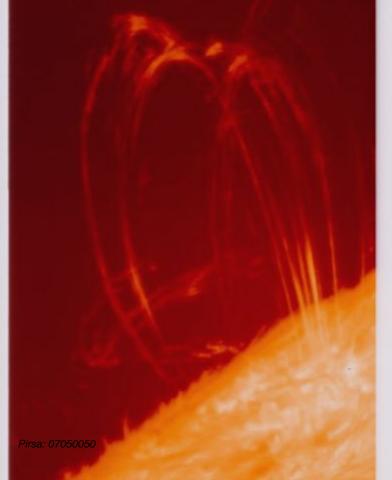


where classical electrons rotate around it

B: about 1 kG,

Lifetime: few months

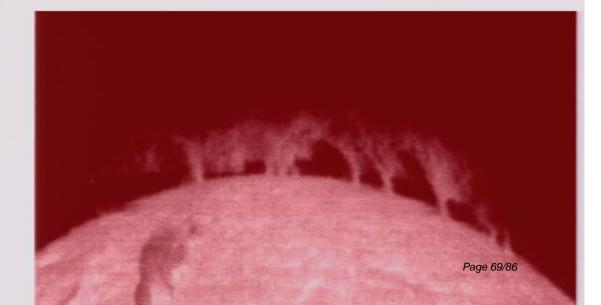
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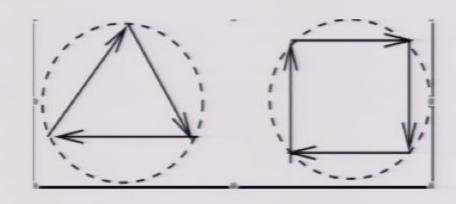


# Bose-Einstein condensation of strongly interacting particles (=monopoles)

(with M.Cristoforetti, Trento)

Feynman theory for liquid He4: divergent polygons
 BEC if y=exp(-S)>yc = .16 or so (1/Nnaighbours)

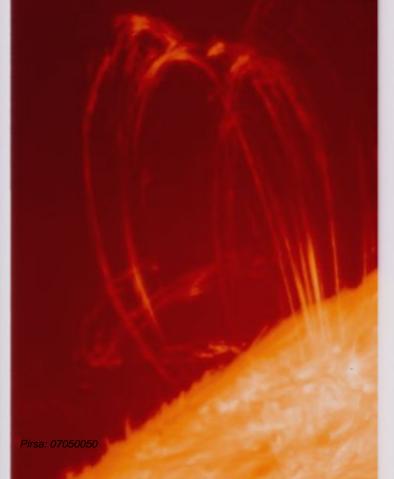
We calculated ``instantons" for lparticles jumping paths in a liquid and solid He4 incuding realistic atomic potentials: no supersolid phase?



For charged Bose gas (monopoles) the action for the jump can be calculated similarly

Marco is doing Path Integral simulations with permutations numerically, to better define

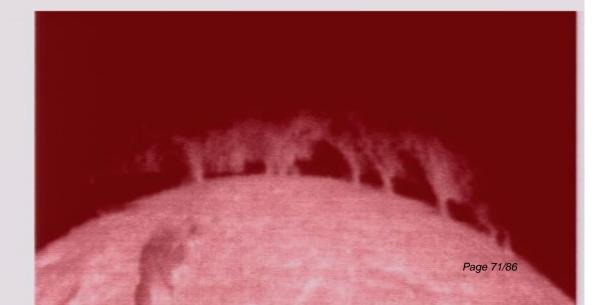
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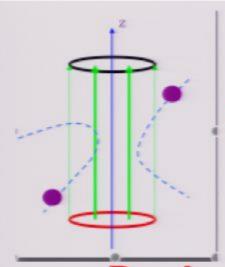


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Pirsa: 07050050

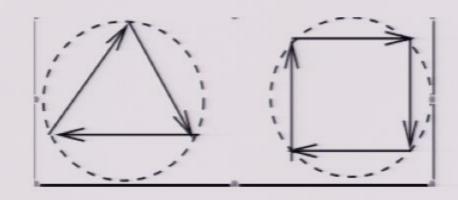
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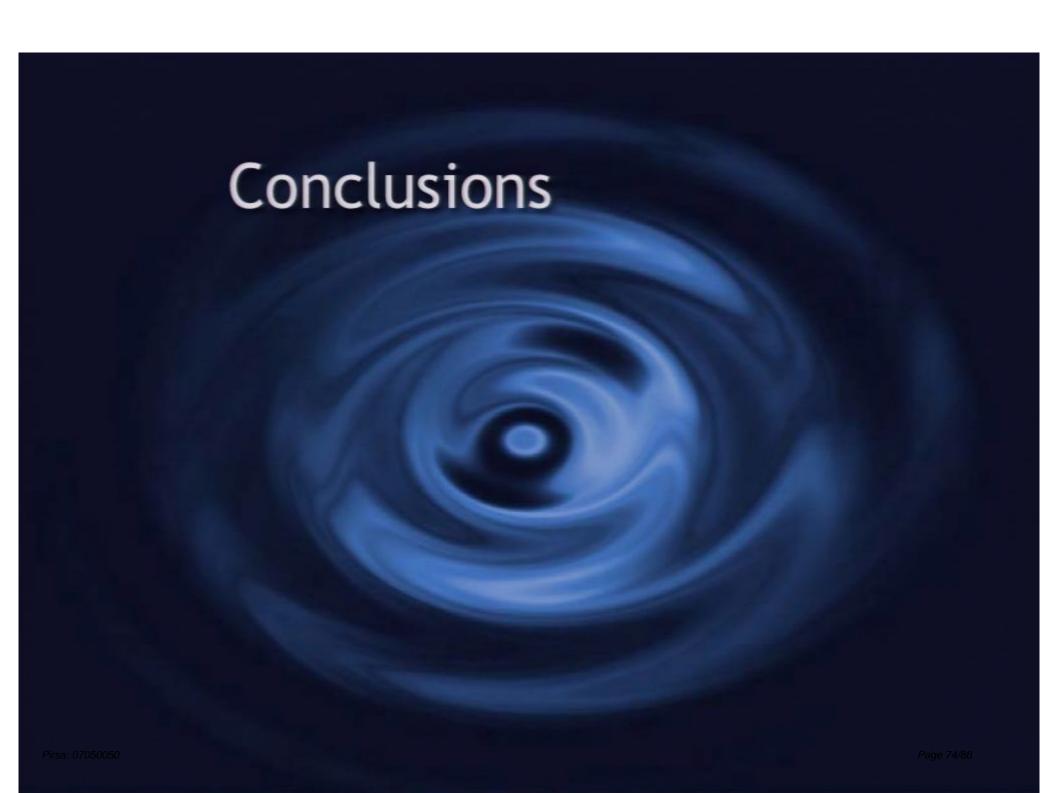
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Strongly coupled QGP has been produced at RHIC



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Strong jet quenching

Pirsa: 07050050 Page 77/86

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Pirsa: 07050050

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Pirsa: 07050050 Page 80/86

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- Heavy quark diffusion is quenched, conical flow seen



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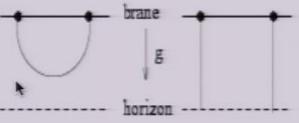
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    - RHIC data on transport (eta,D), ADS/CFT and classical MD all ely

# A gift by the string theorists: AdS/CFT correspondence, the only way to calculate at VERY strong coupling

- The  $\mathcal{N}=4$  SUSY Yang Mills gauge theory is conformal (CFT) (the coupling does not run). At finite T it is a QGP phase at ANY coupling. If it is weak it is like high-T QCD => gas of quasiparticles. What is it like when the coupling gets strong  $\lambda = g^2 N_c \gg 1$ ?
- AdS/CFT correspondence by Maldacena turned the strongly coupled gauge theories to a classical problem of gravity in 10 dimensions
- Example: a modified Coulomb's law (by -- Maldacena)

$$V(L) = -\frac{4\pi^2}{\Gamma(1/4)^4} \frac{\sqrt{\lambda}}{L}$$

 $e^{irs}$  becomes a sreened potential at finite T



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