

Title: Nonlinear Structure Formation and Apparent Acceleration: An Investigation

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Abstract: We present analytically solvable nonlinear models of structure formation in a Universe with only dust, using LTB solutions. We show that the luminosity distance-redshift relation has significant corrections at low redshift (Doppler effect). We discuss different possibilities that could further enhance this effect and mimic Dark Energy. We find negligible integrated effect, suppressed by $(L/R_{\{H\}})^3$ (where L is the size of the structure, and $R_{\{H\}}$ is the Hubble radius) and we make contact with cosmological perturbation theory.

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Motivation
 $D_L \rightarrow z$ in the Real
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Building the model
Light propagation

Backreaction?

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Large local effect
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Conclusions



Nonlinear Structures and Apparent Acceleration: An Investigation

Alessio Notari ¹

McGill University, Montréal

May 2007 / Talk @ “Origins of Dark Energy”

¹Talk based on:

Tirthabir Biswas (McGill U.) , Reza Mansouri (McGill U. & Sharif U., Iran) , A. N. astro-ph/0606703 (*Onion*)

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$D_L - z$ relation in the Real Universe.



- In Standard Cosmology we use the Friedmann-Lemaître-Robertson-Walker model.
- We compute D_L (or D_A) and z
- To fit the data we need a $p < 0$ term.
- To what extent is justified to use a *homogeneous* model?

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A good approximation?



- At $z \gg 1$ (CMB epoch, for example) tiny density fluctuations on all observed scales.
- It is a good approximation

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A good approximation?



- At $z \gg 1$ (CMB epoch, for example) tiny density fluctuations on all observed scales.
- It is a good approximation
- ..but at late times $\delta \equiv \frac{\delta\rho}{\rho} > 1$ for all scales $L \lesssim \mathcal{O}(10)/h\text{Mpc}$ (1% of Hubble radius)
- Superclusters upto few hundreds of Mpc (10% of Hubble radius), nonlinear objects
- Network with sponge-like structure: pancakes surrounding voids. Typical length $100 - 150\text{Mpc}/h$.

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SDSS data

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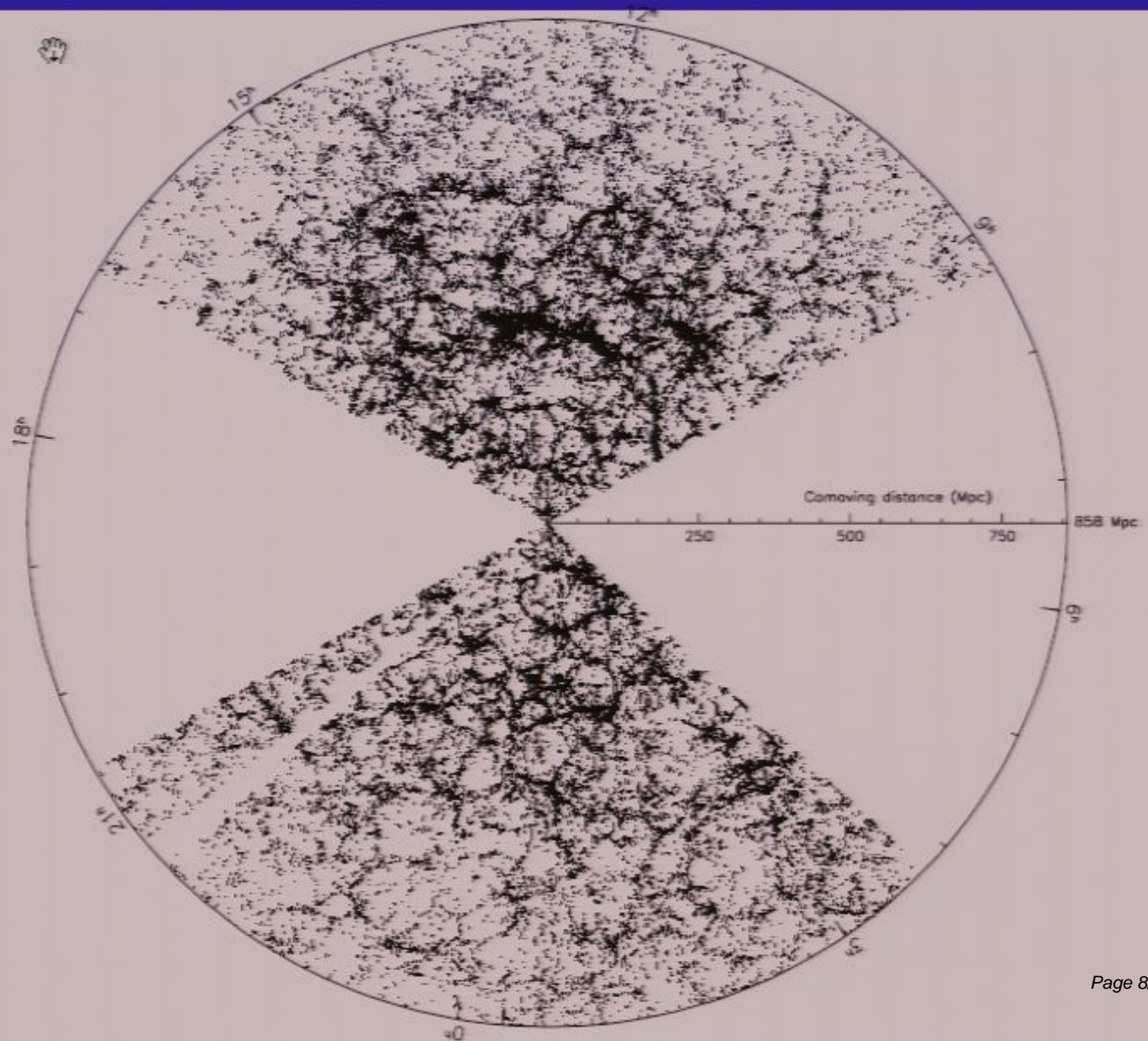
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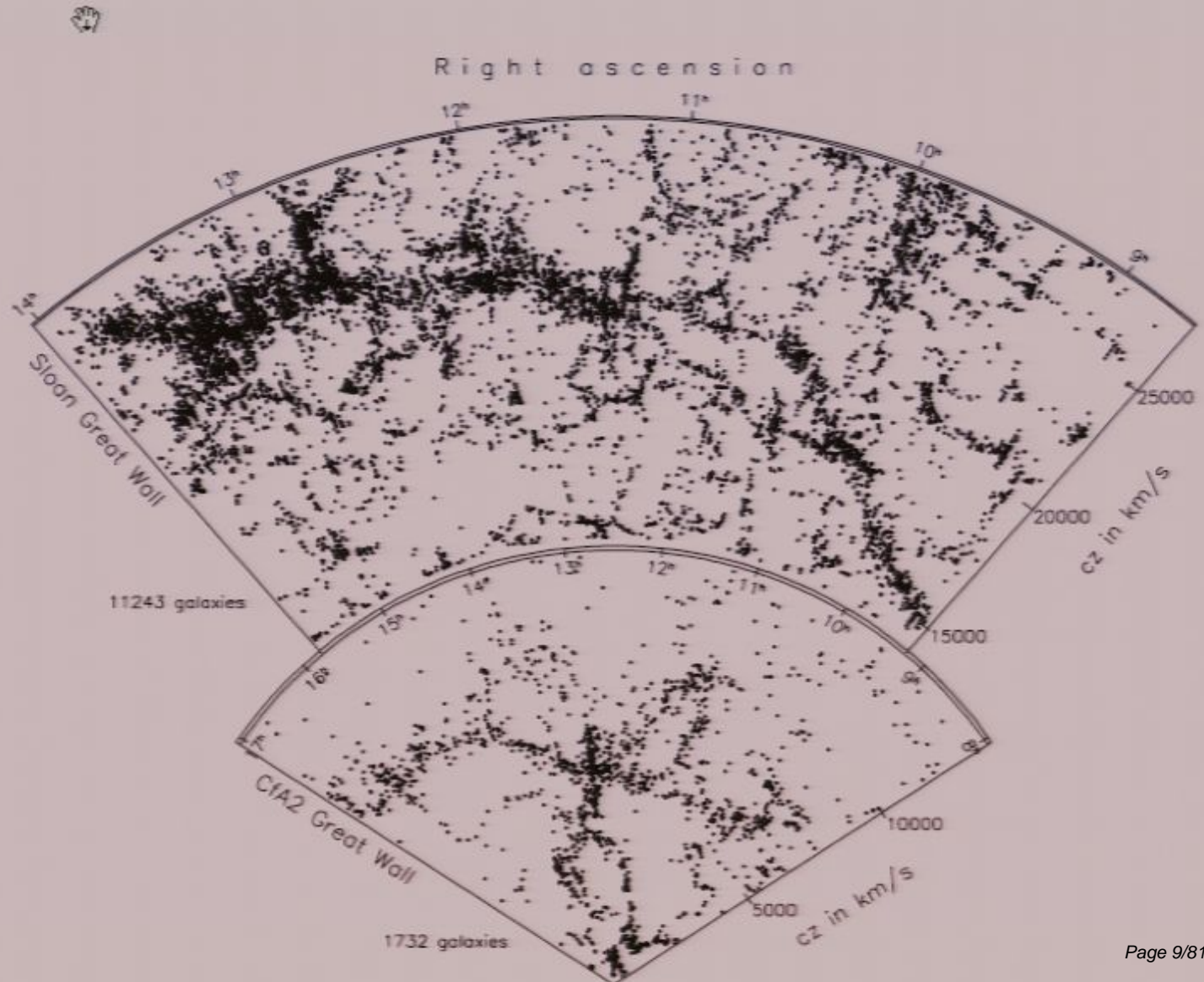
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Beyond FLRW



- So, consider $p = 0$ inhomogeneous models.
- Two motivations:
 - Can one mimick acceleration (with $p = 0$)?
 - In any case can we quantify deviations from FLRW?
- Difficult but well-defined questions

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- **Backreaction**

perturbations affect the background

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- **Backreaction**

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- **Light propagation**

Light meets voids and structures. Do they compensate?

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- **Backreaction**

perturbations affect the background

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Light meets voids and structures. Do they compensate?

- **Large local fluctuation**

What if we live in a local void?

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Backreaction

- Typically one looks at the average $\langle \rho(t, \mathbf{x}) \rangle_D$ at fixed comoving time t
- And defines $\frac{d}{dt} \langle \rho(t, \mathbf{x}) \rangle_D = -3 \frac{\dot{a}_D(t)}{a_D(t)} \langle \rho(t, \mathbf{x}) \rangle_D$
- Features:

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- Features:
 - $a_D(t)$ does *not* evolve as in FLRW (Buchert '97 and '00): gravity is nonlinear + local effects
 - It can accelerate in principle (Nambu and Tanimoto '05, Chuang, Gu, Hwang '05, A. N. '05, Kolb Matarrese Riotto '05)

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 - It can accelerate in principle (Nambu and Tanimoto '05, Chuang, Gu, Hwang '05, A. N. '05, Kolb Matarrese Riotto '05)
 - How large is the effect in real world?
 - (Hui & Seljak '95, Rasanen '04, Kolb Matarrese Notari Riotto '05) : 10^{-5} at second order in PT
 - (Rasanen '04): suggests large effect at nonlinear order. (A. N. '05, Kolb Matarrese Riotto '05): corrections become all of the same order at $z \approx 1$.
 - (Fry & Siegel '05): suggest 10^{-5} with Newtonian arguments.

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Problems with backreaction approach



- If there is a sizable effect, it is nonlinear
- PT is not able to calculate it
- Not completely clear how to connect $\mathbf{a}_D(t)$ to observable quantities

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- The observable is not $a_D(t)$, but $D_L - z$.
- A cone of light is focused close to structures, defocused far from them (D_L is different).
- Each photon is redshifted differently in empty space and close to structures (z is different).
- Do they compensate to give $D_L - z$ FLRW?
- Take into account that nonlinear voids occupy more volume than structures.

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- Suppose that we live in a peculiar local region (example: *local void*)
- \Rightarrow low z observations may be very different from average.

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Local fluctuations



- Suppose that we live in a peculiar local region (example: *local void*)
- \Rightarrow low z observations may be very different from average.
- Since acceleration is inferred **comparing low z with high z ...**
- Can this mimick acceleration ²?

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- \Rightarrow low z observations may be very different from average.
- Since acceleration is inferred **comparing low z with high z ...**
- Can this mimick acceleration ²?
- How much contrast δ and how large L is needed?

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Lemaître-Tolman-Bondi metrics



$$ds^2 = -dt^2 + \frac{R'^2(r, t)}{1 + 2k(r)r^2} dr^2 + R^2(r, t)(d\theta^2 + \sin^2 \theta d\varphi^2)$$

with comoving coordinates (r, θ, φ) and proper time t .

- Spherically symmetric (but one can also put Observer far from Center).
- Einstein equations:

$$\frac{1}{2} \frac{\dot{R}^2(r, t)}{R^2(r, t)} - \frac{GM(r)}{R^3(r, t)} = \frac{k(r)r^2}{R^2(r, t)},$$

$$4\pi\rho(r, t) = \frac{M'(r)}{R'(r, t)R^2(r, t)},$$

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LTB metrics



$$ds^2 = -dt^2 + \frac{R'^2(r, t)}{1 + 2k(r)r^2} dr^2 + R^2(r, t)(d\theta^2 + \sin^2 \theta d\varphi^2)$$

It has the solutions:

- For $k(r) > 0$ ($k(r) < 0$),

$$R = \frac{GM(r)}{2|k(r)|r^2} [\cos h(u) - 1], \quad (2.1)$$

$$t - t_b(r) = \frac{GM(r)}{[2|k(r)|r^2]^{3/2}} [\sin h(u) - u].$$

- $k(r) = 0$,

$$R(r, t) = \left[\frac{9GM(r)}{2} \right]^{1/3} [t - t_b(r)]^{2/3}.$$

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Choosing the functions

- “Gauge” choice: $M(r) = \frac{4\pi}{3} M_0^4 r^3$
- The idea is to describe structure formation
(start with $\delta(r, t_i) \ll 1$ and end up with $\delta(r, t_{\text{now}}) \gg 1$)³

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- We play with $k(r)$ to describe $\delta(r, t_I)$.
- $k = 0$ flat FLRW, $k = \pm 1$ open/closed FLRW, with $R(r, t) = r a(t)$.

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- We play with $k(r)$ to describe $\delta(r, t_I)$.
- $k = 0$ flat FLRW, $k = \pm 1$ open/closed FLRW, with $R(r, t) = r a(t)$.

$$k(r) \propto \frac{1}{r} k_0 \sin^2 \left(\frac{\pi r}{L} \right)$$

- Two parameters, L and k_0 .

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Choosing $A(r)$

- Roughly:

$$\rho(r, t) = \frac{M_0^4}{6\pi(\tilde{M}t)^2 [1 + \epsilon_0(t) \sin(\frac{2\pi r}{L})]}, \quad \epsilon_0(t) \propto k_0 t^{\frac{2}{3}}$$

$$\delta = \frac{\epsilon}{1 + \epsilon} = \frac{\epsilon_0(t) \sin(\frac{2\pi r}{L})}{1 + \epsilon_0(t) \sin(\frac{2\pi r}{L})}$$

- $\epsilon \ll 1$ linear growth
- ϵ not small: δ grows rapidly (as in Zel'dovich approx)
- We work before collapse (in real world there is virialization).

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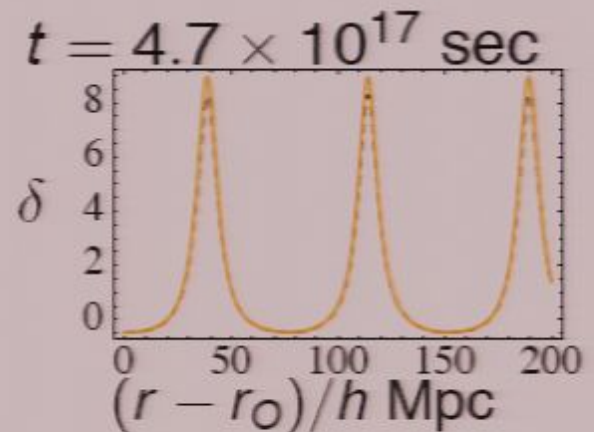
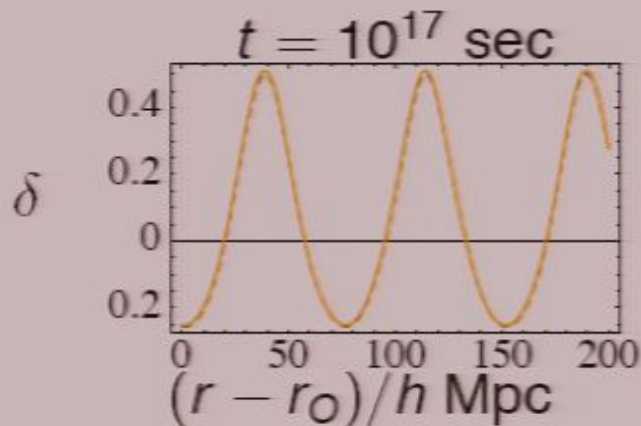
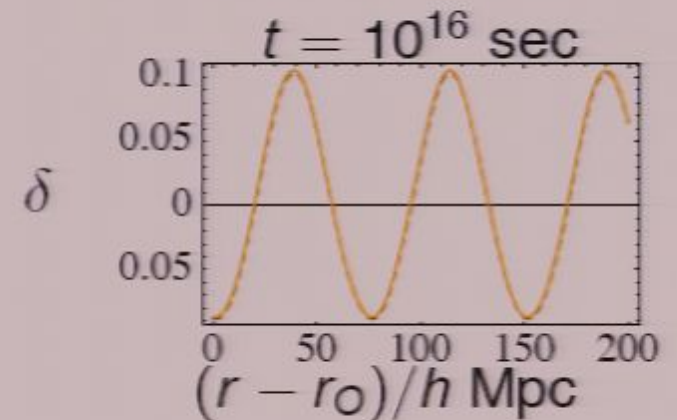
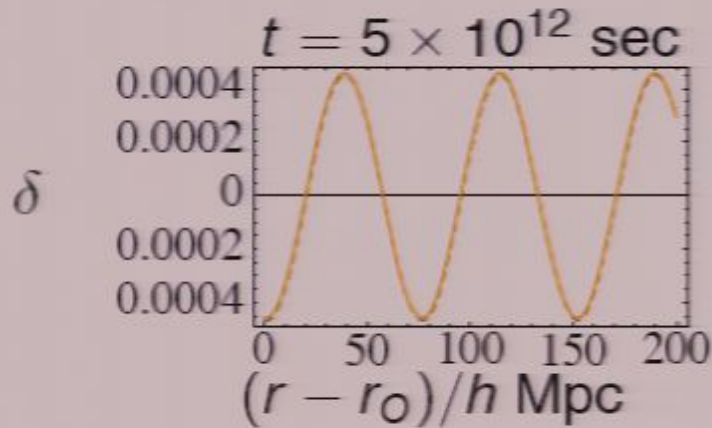
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Redshift



$$\frac{dz}{dr} = \frac{(1+z)\dot{R}'}{\sqrt{1+2E}}$$

- Analytical (small $k(r)$ but large δ) and numerical

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$$\frac{dz}{dr} = \frac{(1+z)\dot{R}'}{\sqrt{1+2E}}.$$

- Analytical (small $k(r)$ but large δ) and numerical
- The result:

$$1+z(r) \simeq (1+z_{\text{FLRW}}(r)) \exp \left[-\frac{2\epsilon_0(t)}{\pi} \left(\frac{L}{r_{\text{hor}}} \right) \cos \left(\frac{2\pi r}{L} \right) \right],$$

for observer at minimum or maximum of density

- For **small z** the correction is quite large:

$$z \simeq z_{\text{FLRW}} \left[1 - \frac{\epsilon}{\pi} \frac{L}{\delta r} \cos \left(\frac{2\pi r}{L} \right) \right],$$

where we have defined $\delta r \equiv r - r_0$.

- It's a **peculiar velocity correction**, radial correlated

Analytical and numerical results for z

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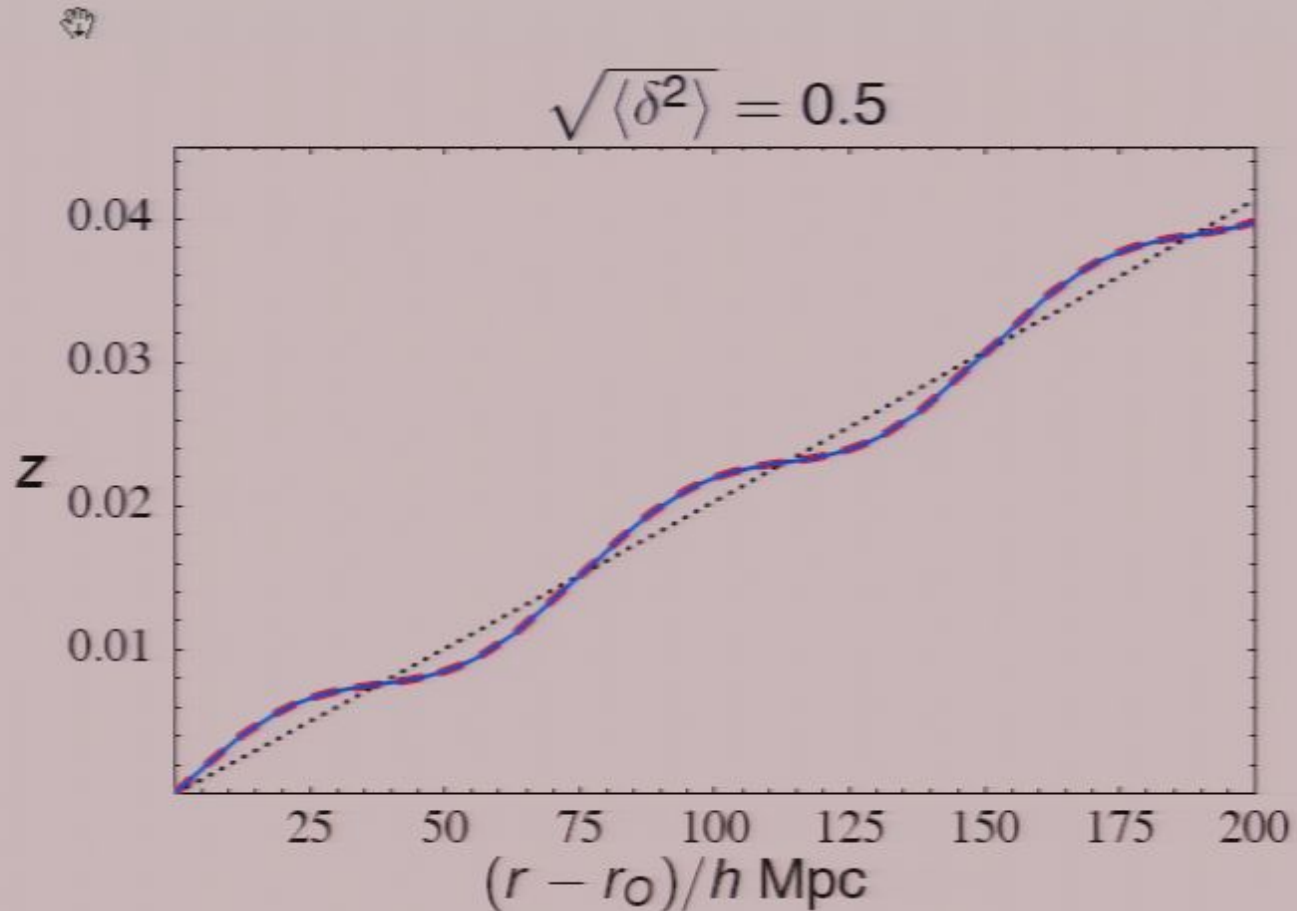


Figure: Redshift (z) along the geodesic of a photon arriving at $r = r_0$ at time $t = t_0$. In this plot $r_0 = 36.5L$, $t_0 = 3.3 \times 10^{17}$ sec.

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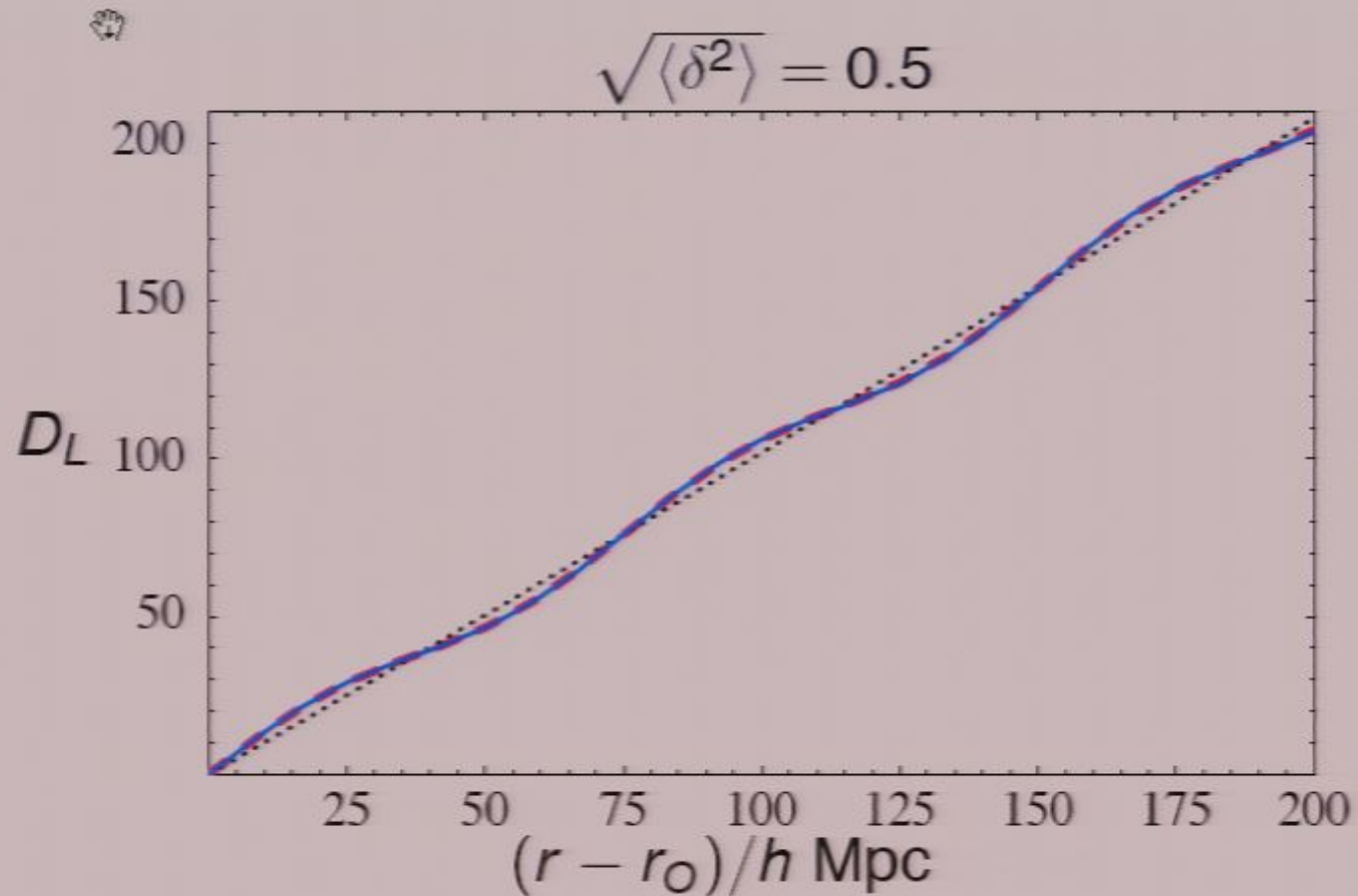


Figure: Luminosity distance (D_L) along the geodesic of a photon arriving at $r = r_0$ at time $t = t_0$. In this plot $r_0 = 36.5L$, $t_0 = 3.3 \times 10^{17}$ sec.

Is there backreaction?



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$$L = 54/h\text{Mpc} \ ; \ \sqrt{\langle \delta^2 \rangle} = 1.6$$

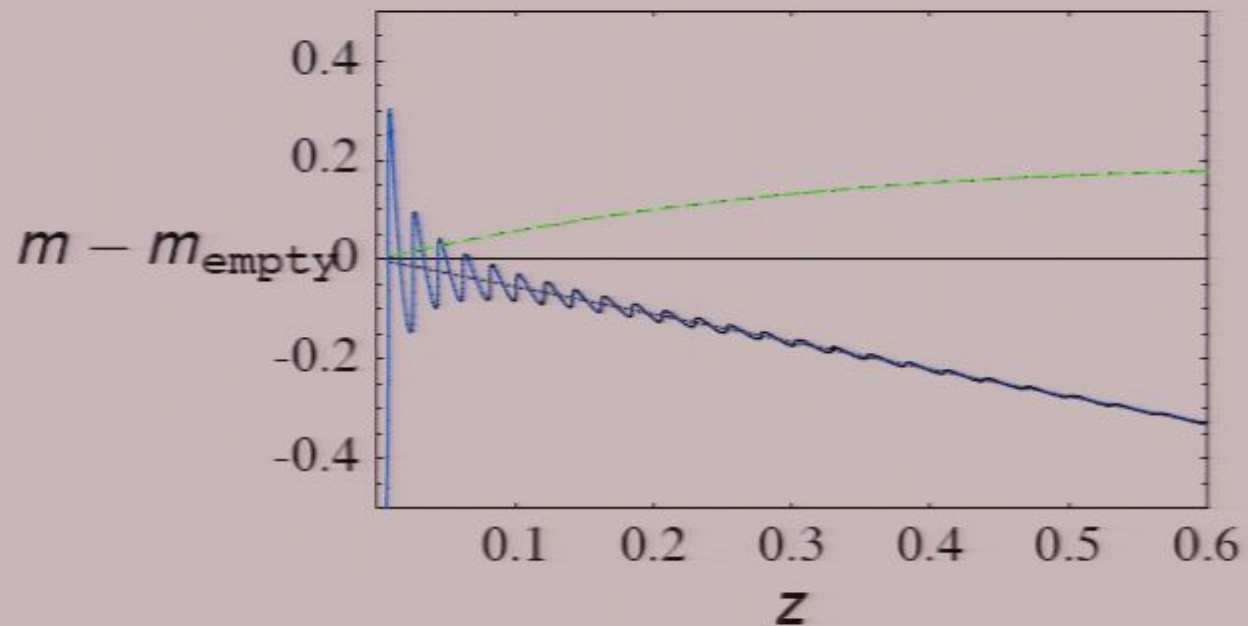


Figure: $m \equiv \text{Log}_{10}(D_L)$

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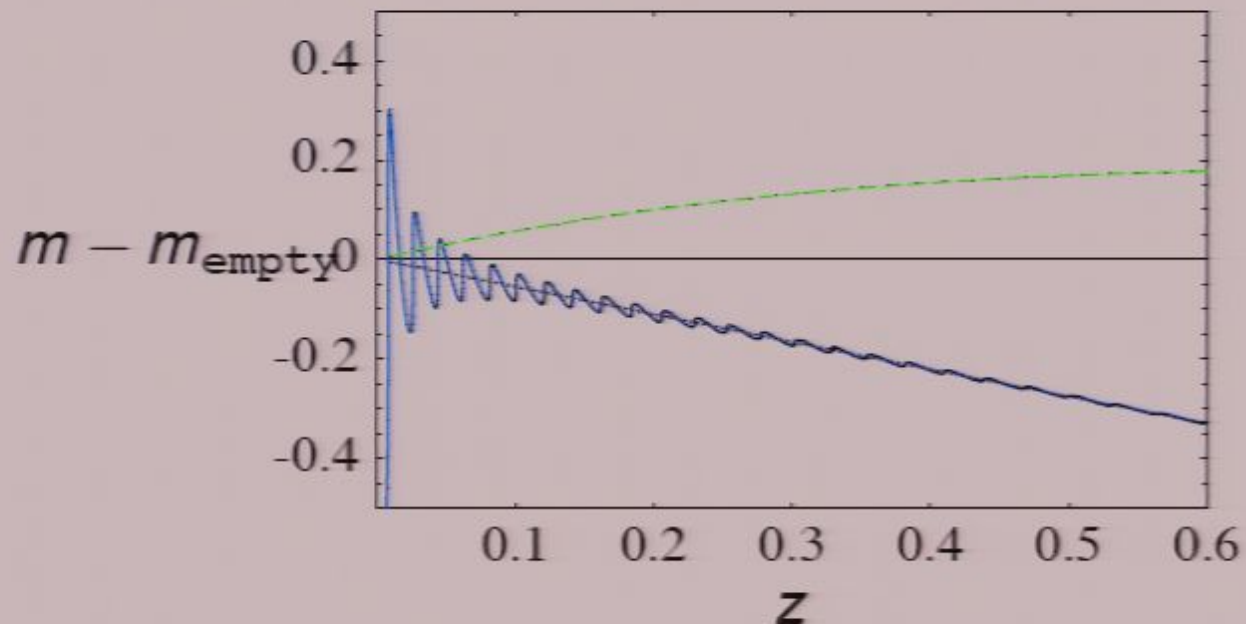


Figure: $m \equiv \text{Log}_{10}(D_L)$

- Is it because of the specific profile?
- Is it because of small "curvature" $k(r)$?

Swiss-Cheese model



- Carve a spherical patch from FLRW
- Replace it with LTB
- We can try also with large curvature $k(r)$ inside
 - Use $k'(0) = 0$ (No cusp in ρ at the center)
 - $k'(L) = k(L) = 0$ (matching conditions with FLRW)
 - Example $k(r) = k_0 \left[\left(\frac{r}{L} \right)^2 - 1 \right]$
- Void at the center, structure at the boundary

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$$L = 54/h\text{Mpc} \ ; \ \sqrt{\langle \delta^2 \rangle} = 1.6$$

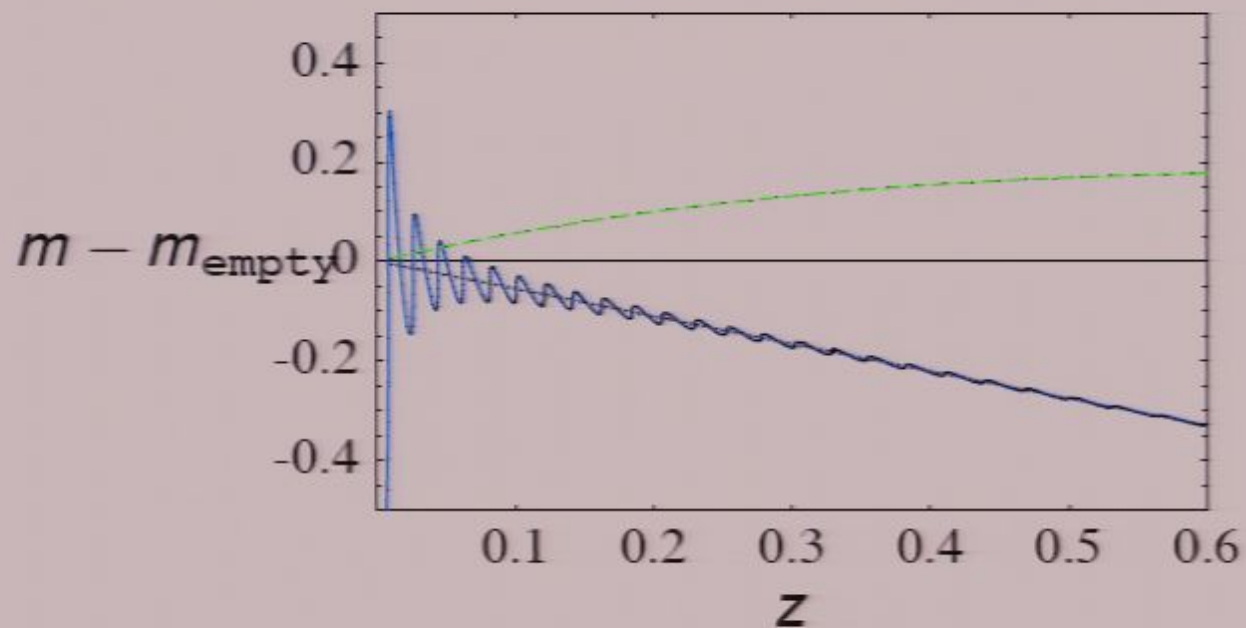


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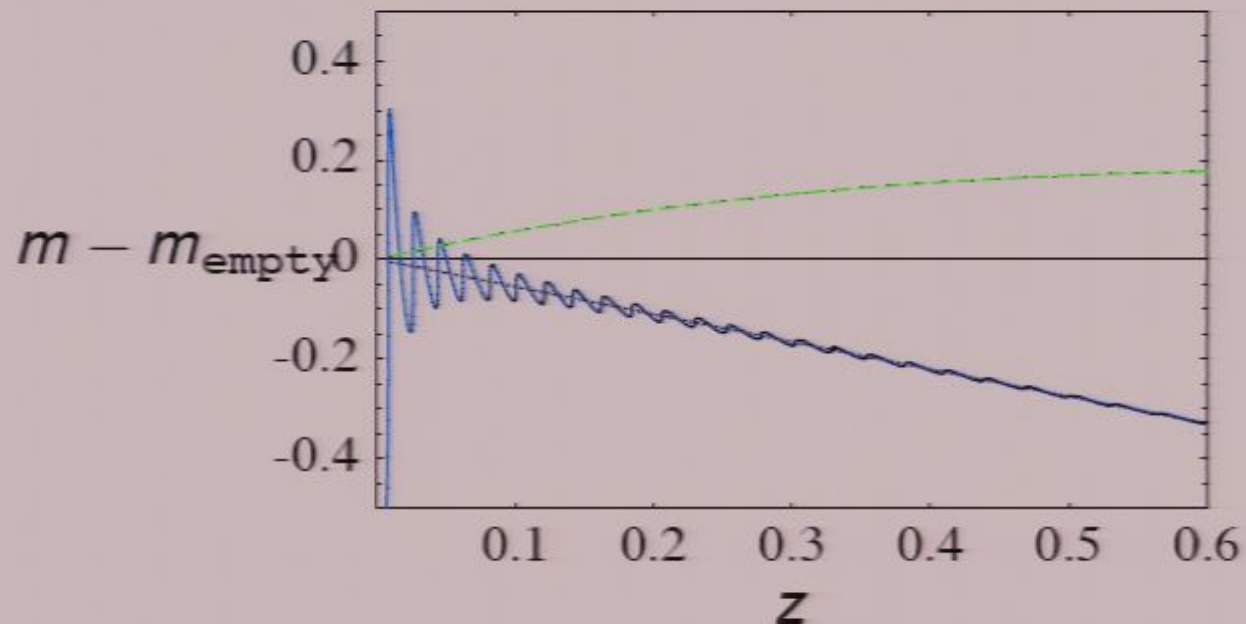


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 - Example $k(r) = k_0 \left[\left(\frac{r}{L} \right)^2 - 1 \right]$
- Void at the center, structure at the boundary
- Consider also nonlinear k
- Is there any large net effect for a photon travelling through a patch?
- Both Observer and Source in the FLRW region

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Net effect? Backreaction?

- We disentangled different effects making contact with usual Perturbation Theory (for small k) in Newtonian gauge

$$\Phi \propto \int dr r k(r) \propto k_0 \left(\frac{L}{r_H} \right)^2$$

- Integrated effect is usual Rees-Sciama effect: always $(L/r_H)^3$ also for large k (analytical and numerical)

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- And...there is no backreaction on the outside FLRW region by construction due to spherical symmetry (Birkhoff's theorem)
- So, LTB does not seem to give sizeable backreaction... maybe go to nonspherical models?

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Swiss-Cheese model: Doppler effect



- Doppler effect (motion of sources) Large effect at small z
- It goes like L/r_H

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Swiss-Cheese model: Doppler effect



- Doppler effect (motion of sources) Large effect at small z
- It goes like L/r_H
- Basic picture: sources attracted towards the outer dense shells.
- Inside the Void: collective radial velocity adds to expansion

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Are spherical models still interesting (at least for speculations..)?

- Use the large (collective Doppler) effect near Observer
- That's how LTB can mimick Acceleration!

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- Caution: Any Hubble diagram can be fit by LTB (assuming arbitrary density profile)! The whole point: is that realistic and testable ?

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- Our philosophy: Try to make contact with realistic cosmology
- What's the smallest L and δ that can possibly work?

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- That's how LTB can mimick Acceleration!
- Caution: Any Hubble diagram can be fit by LTB (assuming arbitrary density profile)! The whole point: is that realistic and testable ?
- Our philosophy: Try to make contact with realistic cosmology
- What's the smallest L and δ that can possibly work?
- Also: estimate the typical systematic correction to SN observations (See also Ali Vanderveld's talk)

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High and low z



- Evidence for acceleration comes from **mismatch** between:
 - measurements at low redshift ($0.03 \lesssim z \lesssim 0.07$)
 - high- z SN (roughly $0.4 \lesssim z \lesssim 1$)
- We choose large L (up to $z \approx 0.07$)
- \Rightarrow The local Bubble is different from the average ("Hubble Bubble").
- In the region ($z \gtrsim 0.3$):

$$D_{FLRW} \approx \frac{2}{H_{OUT}} (1 + z - \sqrt{1 + z}).$$

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Low z

- We use $h_{\text{OUT}} \approx 0.5$.
- We need larger local H_{IN} due to inhomogeneities
- We need a local patch, that at least extends up to $z \approx 0.07$ to have a linear Hubble diagram in $0.03 \leq z \leq 0.07$.

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Low z

- We use $h_{\text{OUT}} \approx 0.5$.
- We need larger local H_{IN} due to inhomogeneities
- We need a local patch, that at least extends up to $z \approx 0.07$ to have a linear Hubble diagram in $0.03 \leq z \leq 0.07$.
- Therefore: $L \gtrsim 400/h$ Mpc (diameter)
- Put Observer in a void

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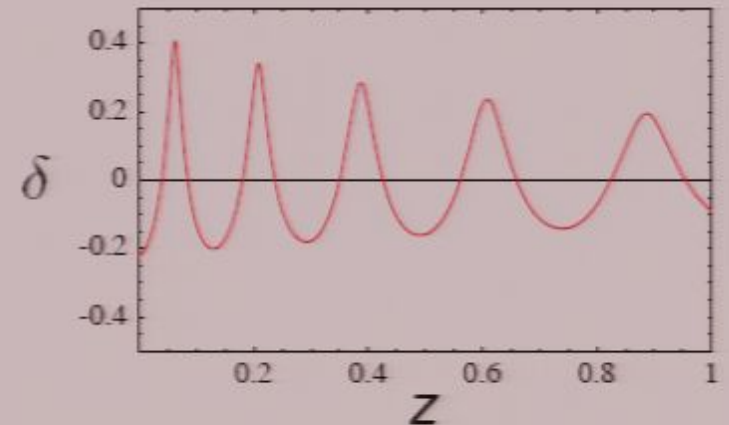
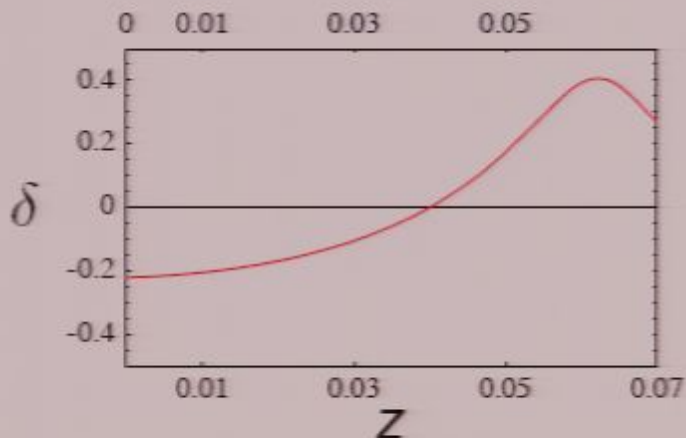
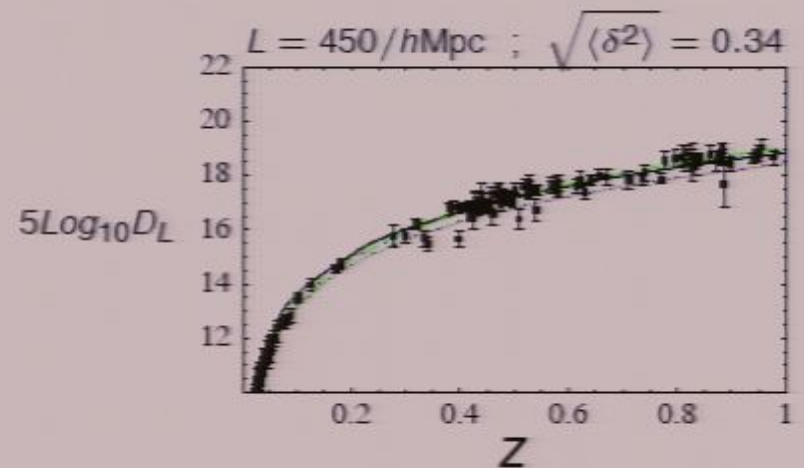
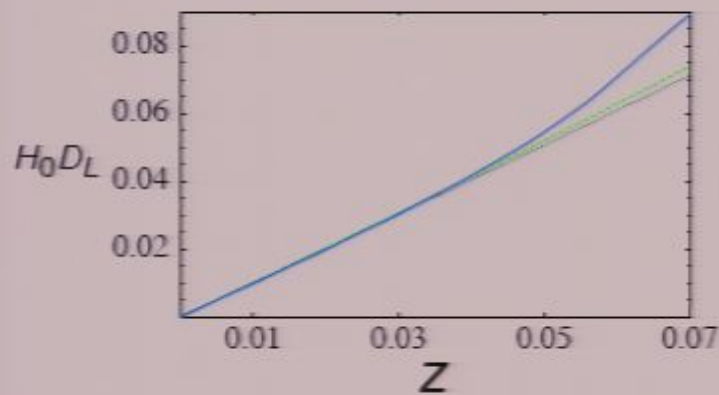
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$$L = 450/h\text{Mpc} ; \sqrt{\langle \delta^2 \rangle} = 0.34$$



SDSS data

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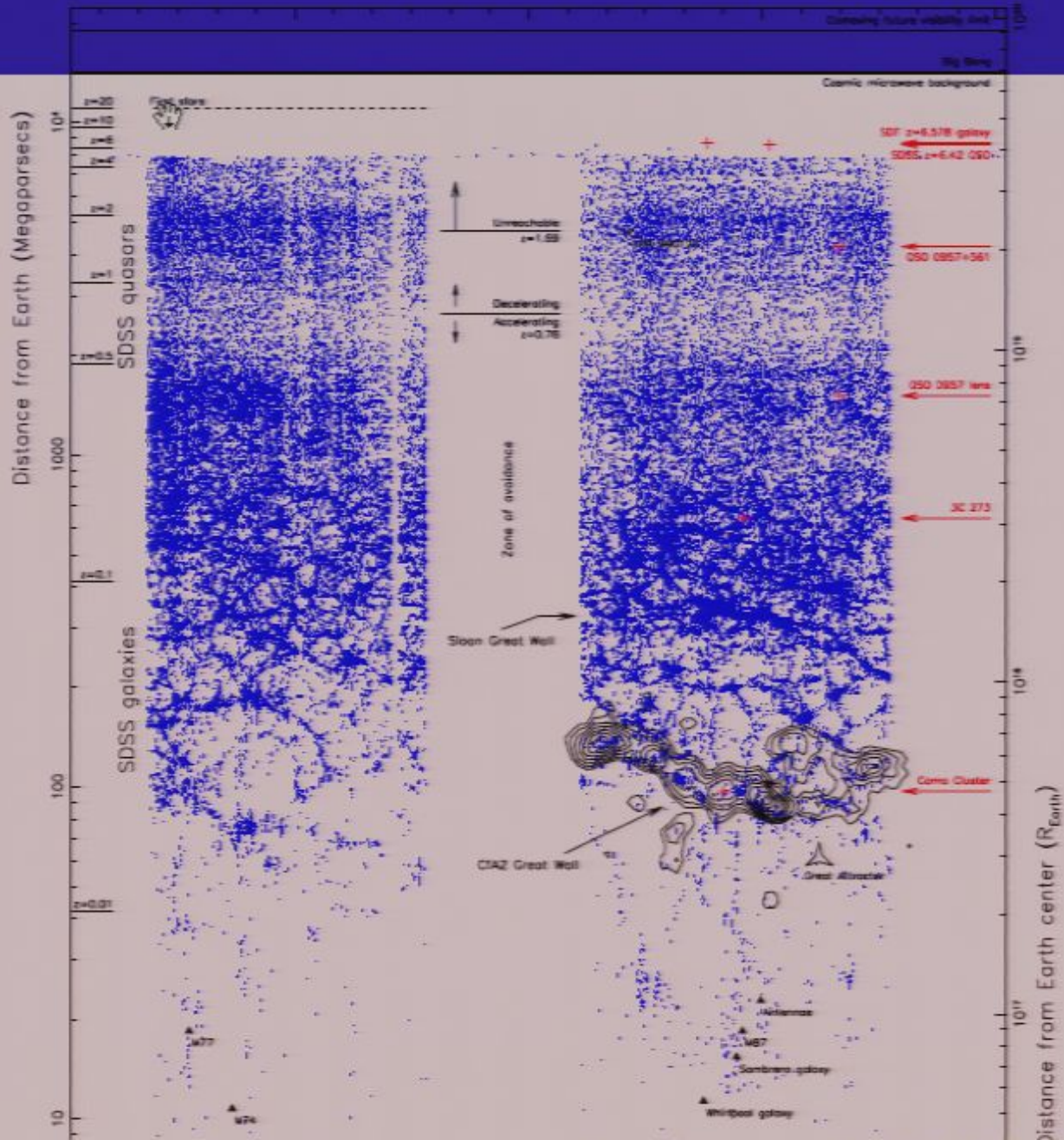
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$m - z$ plot

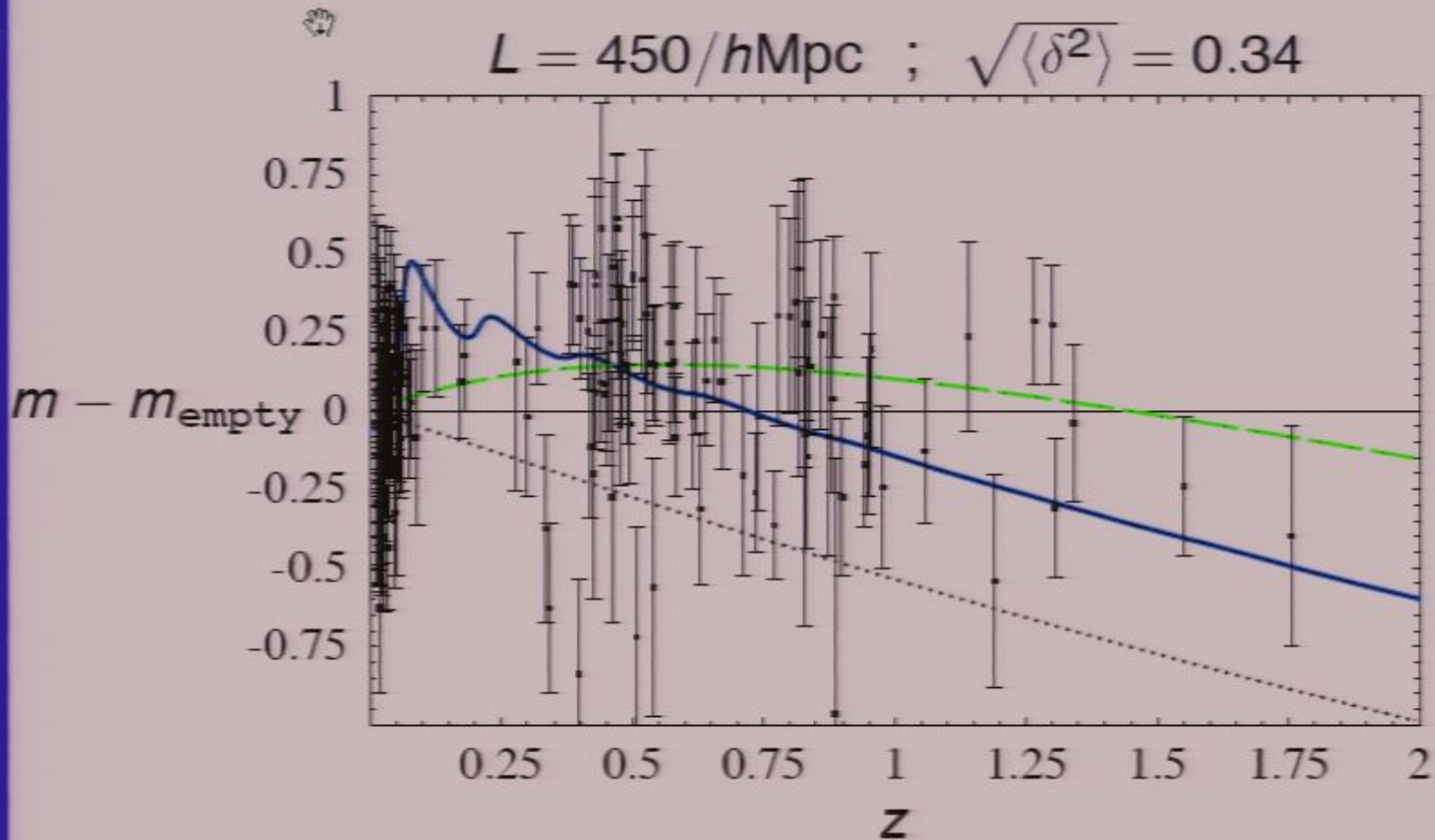


Figure: The blue solid line is our numerical solution, the black dotted line is the CDM model ($\Omega_m = 1$), and the green long-dashed line is the Λ CDM result (with $\Omega_\Lambda = 0.73$). We have

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Individual contributions to χ^2

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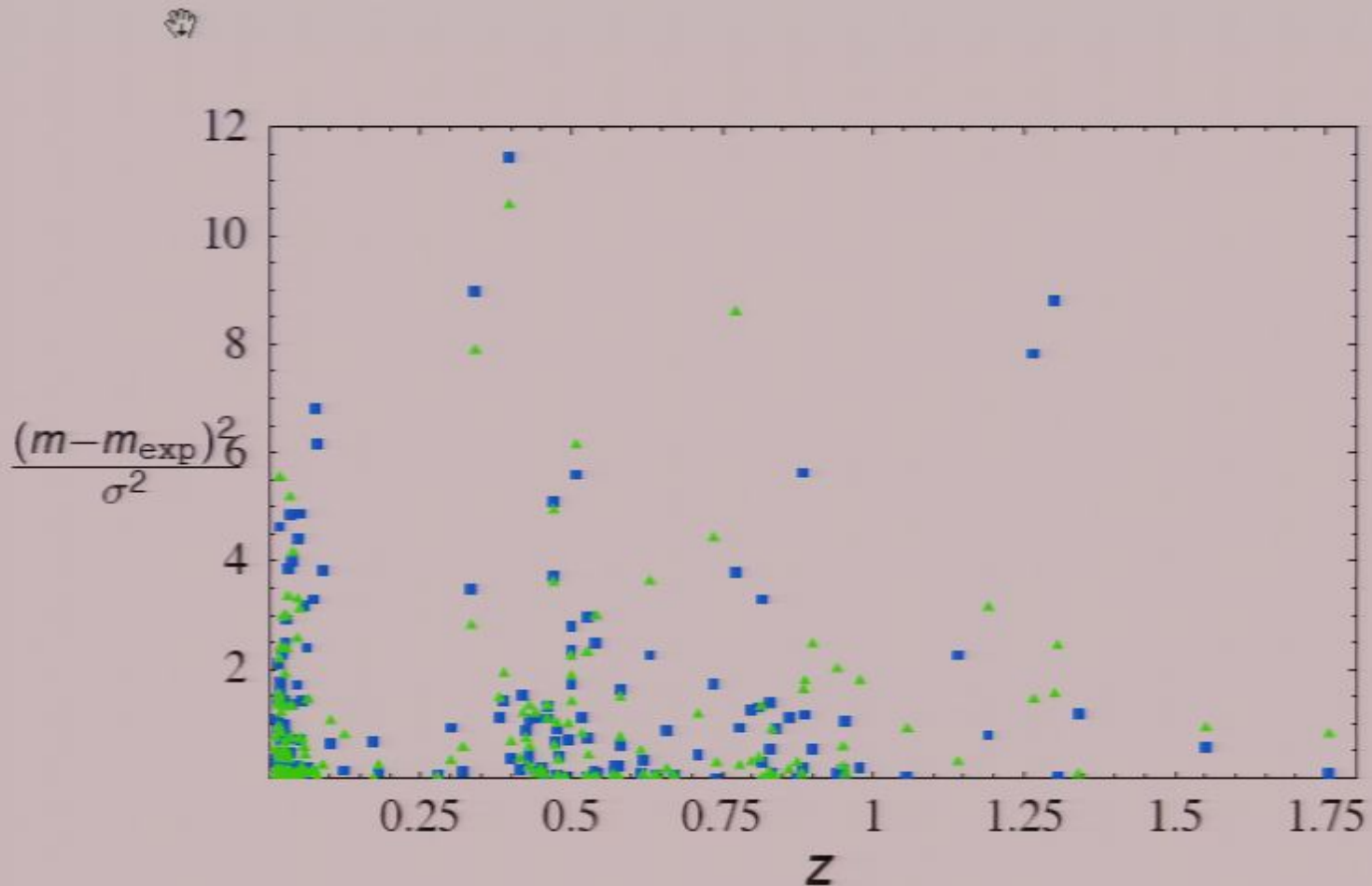


Figure: We show here the contribution to the χ^2 for each data point (gold data set of *Riess et al.*) Our model (blue boxes) is compared with Λ CDM with $\Omega_\Lambda = 0.73$ (green triangles).

χ^2 comparison



Table: Comparison with data (gold data set of *Riess et al.*)

Model	χ^2 (157 d.o.f.)
Λ CDM (with $\Omega_M = 0.27, \Omega_\Lambda = 0.73$)	178
EdS (with $\Omega_M = 1.00, \Omega_\Lambda = 0.00$)	325
Onion ($\sqrt{\langle \delta^2 \rangle} = 0.34$ on $L = 450/h\text{Mpc}$)	212

Table: Comparison with data (full data set of *Riess et al.*)

Model	χ^2 (186 d.o.f.)
Λ CDM (with $\Omega_M = 0.27, \Omega_\Lambda = 0.73$)	233
EdS (with $\Omega_M = 1.00, \Omega_\Lambda = 0.00$)	403
Onion ($\sqrt{\langle \delta^2 \rangle} = 0.34$ on $L = 450/h\text{Mpc}$)	273

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First acoustic peak in CMB



- We do not introduce curvature. But global H is low.
- Our model reduces to EdS model, already by $z \sim 0.2$
- For instance:

$$\Omega_{m,OUT} = 0.9, \quad h_{OUT} = 0.58,$$

+ standard baryon-to-matter ratio,
 $\Omega_{b,OUT}/\Omega_{m,OUT} = 0.13,$

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Assessment of the "Local Void" scenario



- Require δ quite large (~ 0.3) on $L \sim 400/h$ Mpc.

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- Require δ quite large (~ 0.3) on $L \sim 400/h$ Mpc.
- Expected value ($\delta \sim 0.02 - 0.05$).

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Assessment of the "Local Void" scenario



- Require δ quite large (~ 0.3) on $L \sim 400/h$ Mpc.
- Expected value ($\delta \sim 0.02 - 0.05$).
- Observer has to sit **near center** to avoid too large anisotropy
- In general we expect some anisotropy in $D_L - z$.

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- Observer has to sit **near center** to avoid too large anisotropy
- In general we expect some anisotropy in $D_L - z$.
- Full CMB spectrum?

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Similar Voids in the CMB?



- Surprising coincidence with work by Inoue and Silk '06 for CMB
 - alignment in low multipoles
 - non-gaussian circular cold spot
- They need 2 voids $L \approx 350/h$ Mpc and $\delta \approx -0.3$ to explain low- l anomalies
- And a third one at $z \approx 1$ for the cold spot.

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- They need 2 voids $L \approx 350/h$ Mpc and $\delta \approx -0.3$ to explain low- l anomalies
- And a third one at $z \approx 1$ for the cold spot.
- In fact, the cubic integrated $(L/r_H)^3$ effect gives a 10^{-5} effect on CMB

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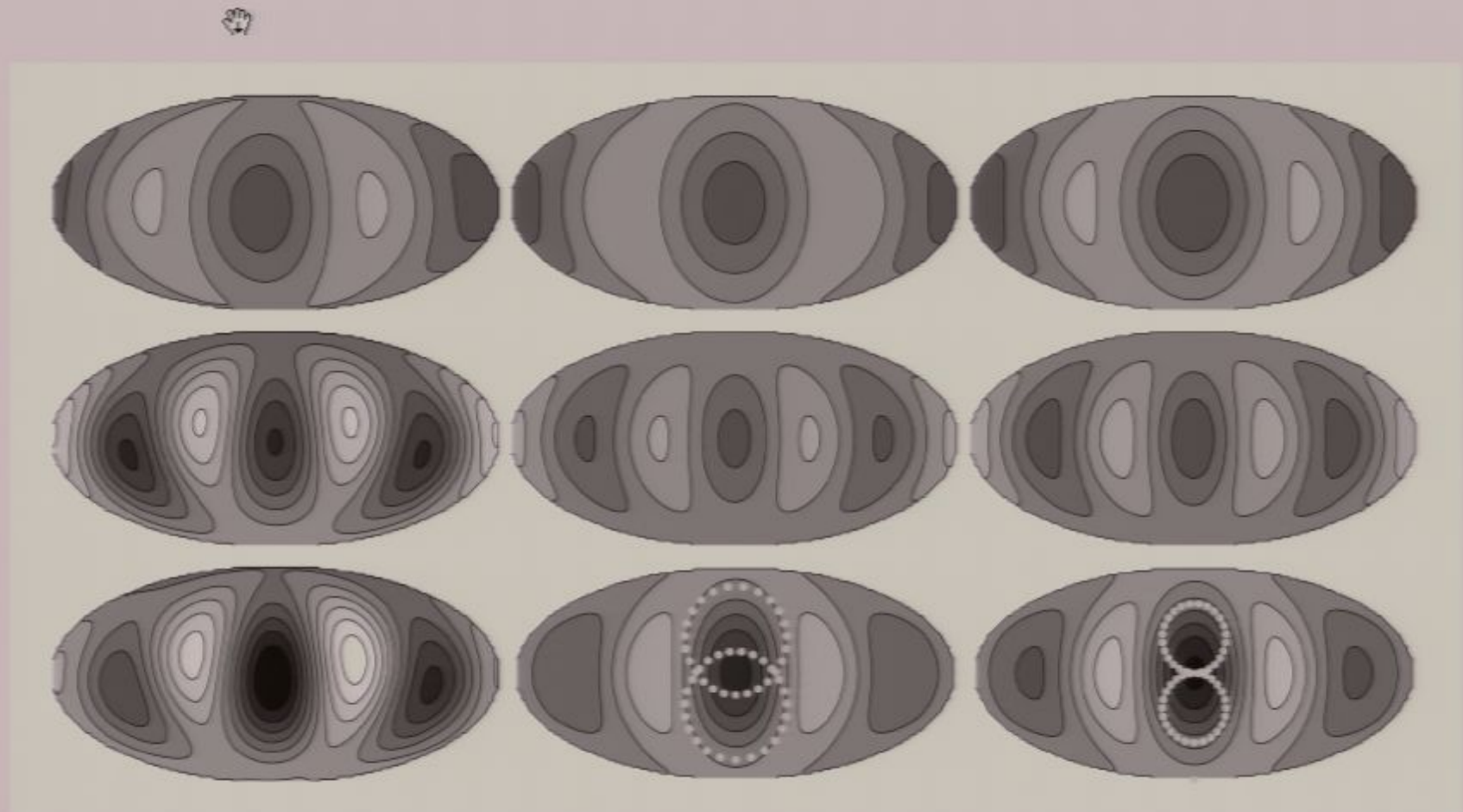
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(Inoue and Silk '05)

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Can such voids exist??



- **The real question:** How unlikely is the existence of such Voids? Nonlinear percolation of small voids (Inoue and Silk)?
- Does it require non-standard Structure Formation or non-standard Primordial features or nongaussianity?

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Can such voids exist??



- **The real question:** How unlikely is the existence of such Voids? Nonlinear percolation of small voids (Inoue and Silk)?
- Does it require non-standard Structure Formation or non-standard Primordial features or nongaussianity?
- Simulations agree with real data?
- J. Einasto '06 claims fraction of superclusters in real data (SDSS and 2dFGRS) 5 times larger than simulations (Millennium Run)
- $L=150$ Mpc/h, 25% local underdensity in the Southern Galactic Cap (2MASS) ?⁴

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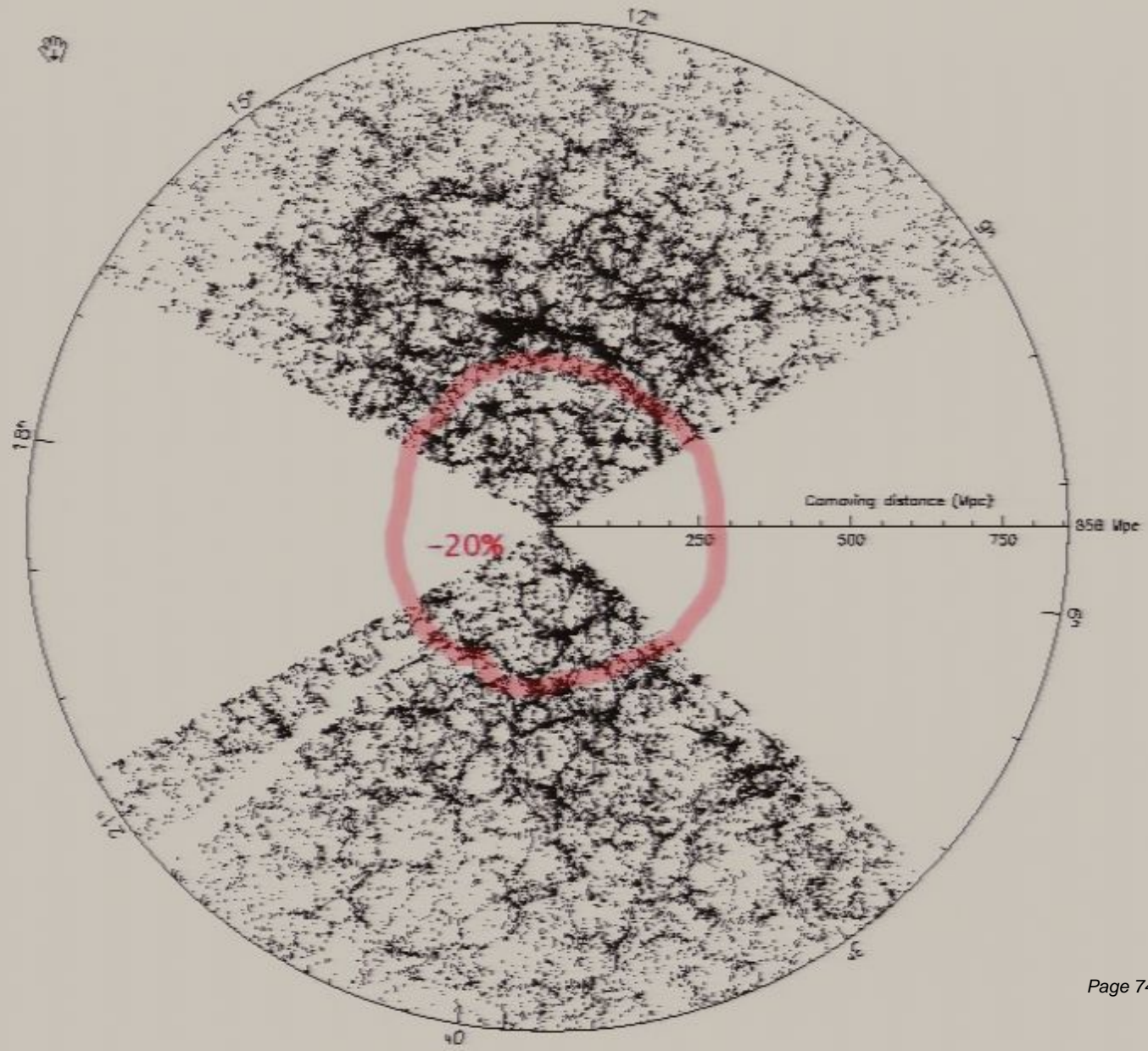
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Observations?

- Observers can hopefully answer (maybe already with present data?)

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Observations?

- Observers can hopefully answer (maybe already with present data?)
- **Also:** we have a sharp transition in the Hubble diagram

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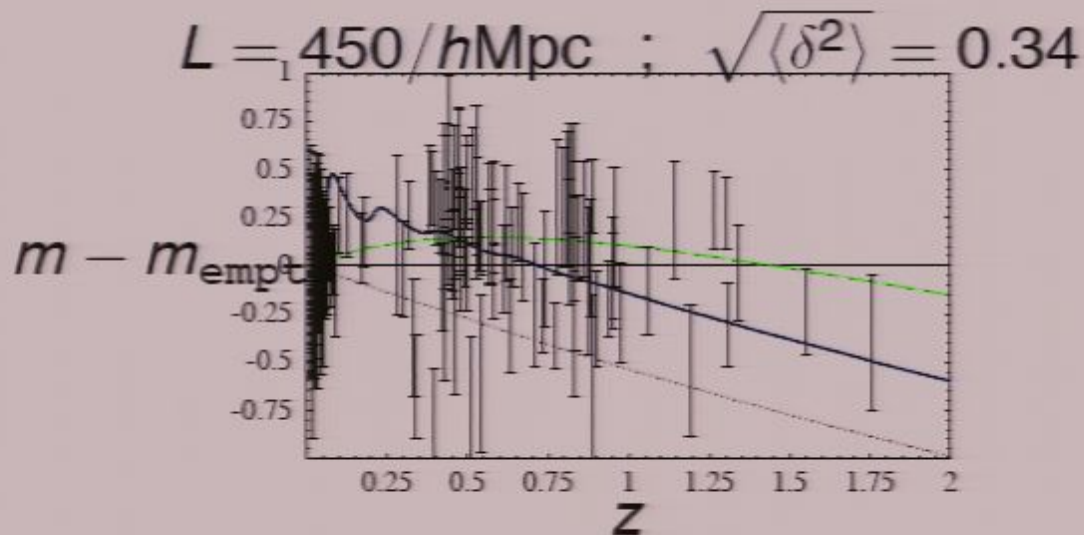
Large
Underdensity

Large local effect

Systematics in SN
observations

Conclusions

- Observers can hopefully answer (maybe already with present data?)
- **Also:** we have a **sharp transition in the Hubble diagram**



- **SDSS II** is definitely going to **discriminate this hypothesis ($L = 400/h$ and $\delta = -0.3$):** lots of data at intermediate redshift (40 SN)...very soon.

Observations?



- How unlikely is that we live near the Center of such a Void?
- We need to be **at most at 10Mpc** from the center (CMB dipole)
- Anisotropy in Hubble rate⁵?
- ISW? Maybe it is due to large Voids?

Inhomogeneity
and
acceleration

Motivation

$D_L \rightarrow z$ in the Real
Universe.

Three physical
effects

The Onion
model

Building the model

Light propagation

Backreaction?

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Outline



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 - $D_L - z$ in the Real Universe.
 - Three physical effects
- 2 The Onion model
 - Building the model
 - Light propagation
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- 5 Large Underdensity
 - Large local effect
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With lower value of δ

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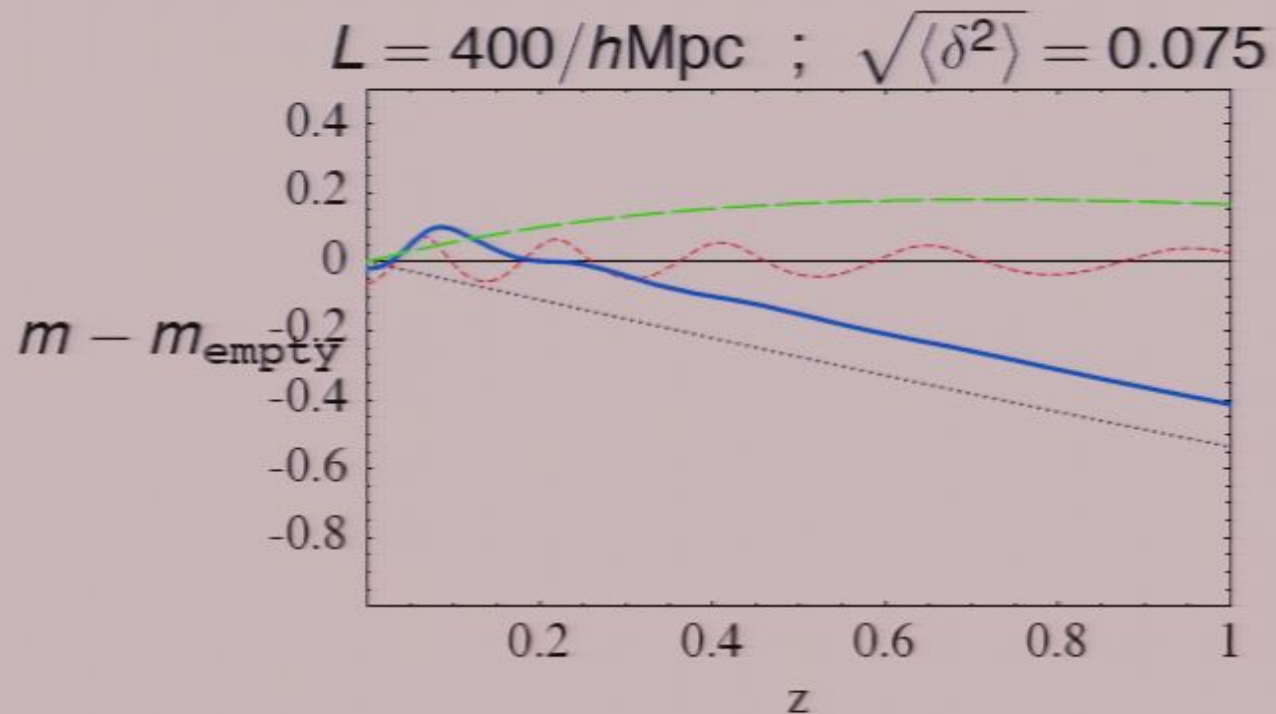


Figure: Magnitude residual from empty FLRW (Δm) vs. redshift (z). We have superimposed the red thin dashed line (density contrast seen by the photon).

Typical systematics $\delta \approx 0.025 \Rightarrow \Delta m \approx 0.05$

Conclusions



- We constructed **nonlinear** examples of structure formation (Onion and LTB Swiss-Cheese), and computed light propagation (D_L and z).
- Integrated effect/ backreaction negligible for acceleration. Spherical symmetry?
- We have shown how a **Large Local Fluctuation** can roughly **mimick acceleration** (Radius $\approx 200/h\text{Mpc}$, $\delta = 0.3$)
- In any case we have found a **typical systematic** of **$\Delta m \simeq 0.05$** (and a similar **anisotropy**).

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