

Title: Large Extra Dimensions and Darkness From String Theory

Date: May 19, 2007 11:00 AM

URL: <http://pirsa.org/07050035>

Abstract:

Large Extra dimensions and darkness from
String theory.



Large Extra dimensions and dark matter from
String theory.

Large Extra dimensions and darkness from
String theory.



Large Extra dimensions and darkness from
String theory :
Motivations

Large Extra dimensions and darkness from
String theory:

Motivations: * Moduli Stabilisation.

Large Extra dimensions and darkness from
String theory;

Motivations: * Moduli Stabilisation.
* Large Volume;

Large Extra dimensions and darkness from
String theory:

Motivations:

- * Moduli Stabilisation.
- * Large Volume;

Large Extra dimensions and darkness from String theory:

- Motivations:
- * Moduli Stabilisation.
 - * Large Volumes $\mathcal{V}$
 - $1/\mathcal{V}$ expansion parameter.

Large Extra dimensions and darkness from String theory:

motivations: * Moduli Stabilisation.

* Large Volumes $\mathcal{V}$

- $1/\mathcal{V}$ expansion parameter.
- Phenomenology;

Large Extra dimensions and darkness from String theory:

motivations: * Moduli Stabilisation.

* Large Volume D

• $1/D$ expansion parameter.

• Phenomenology;

*

Large Extra dimensions and darkness from String theory:

Motivations:

- * Moduli Stabilisation.

- * Large Volumes $\mathcal{V}$

- $1/\mathcal{V}$ expansion parameter.

- Phenomenology: $M_P^2 = M_S^2 \mathcal{V} \rightarrow$ units of l_s .

Large Extra dimensions and darkness from String theory:

motivations: * Moduli Stabilisation.

* Large Volumes $\mathcal{V}$

• $1/\mathcal{V}$ expansion parameter.

• Phenomenology: $M_P^2 = M_*^2 \mathcal{V}$ units of l_s .



Large Extra dimensions and darkness from String theory:

Motivations: * Moduli Stabilisation.

* Large Volumes $\mathcal{V}$

• $1/\mathcal{V}$ expansion parameter.

• Phenomenology: $M_P^2 = M_*^2 \mathcal{V}$ units of $ls.$

* ADD $M_* \sim 1 TeV$
SLED

Large Extra dimensions and darkness from String theory:

Notations: * Moduli Stabilisation.

* Large Volumes $\mathcal{V}$

• $1/\mathcal{V}$ expansion parameter.

• Phenomenology; $M_P^2 = M_*^2 \mathcal{V}$ units of l_s .

* ADD $M_s \sim 1 \text{ TeV}$
SLED

* Intermediate scale:

Large Extra dimensions and darkness from String theory:

Motivations:

- * Moduli Stabilisation.

- * Large Volumes $\mathcal{V}$

- $1/\mathcal{V}$ expansion parameter.

- Phenomenology; $M_P^2 = M_*^2 \mathcal{V}$ $\rightarrow$ units of L_s .

- * ADD $M_* \sim 1 \text{ TeV}$
 - SLED

- * Intermediate scale: $M_* \sim 10^{11} \text{ GeV}$.

Large Extra dimensions and darkness from String theory:

Notations: * Moduli Stabilisation.

* Large Volumes $\mathcal{V}$

• $1/\mathcal{V}$ expansion parameter.

• Phenomenology; $M_P^2 = M_*^2 \mathcal{V}$ $\rightarrow$ units of l_s .

* ADD $M_* \sim 1 \text{ TeV}$
SLED

* Intermediate scale: $M_* \sim 10^{16} \text{ GeV}$
 $\underline{m_{\text{KK}}} = M_*^2 / M_P \sim \text{TeV}.$

$$\frac{m_x}{M_P} = 10^{-15} / M_P \sim \text{TeV}.$$

$$* M_G = M_{GUT} \sim 10^{16} \text{ GeV}.$$

$$\frac{m_{3/2}}{M_p} = 10^{-10} / M_p \sim \text{TeV}.$$

$$* M_S = M_{GUT} \sim 10^{16} \text{ GeV.} \quad (\text{GUT})$$

$$\frac{m_{1/2}}{M_P} = 10^{-16} / M_P \sim \text{TeV}.$$

$$* M_S = M_{\text{GUT}} \sim 10^{16} \text{ GeV. (GUT, inflation).}$$

$$\frac{m_{3/2}}{M_P} = 10^{-11} / M_P \sim \text{TeV}.$$

$$* M_S = M_{\text{GUT}} \sim 10^{16} \text{ GeV. (GUT, inflation).}$$

$$\frac{m_{3/2}}{M_{\text{Pl}}} = 10^{-10} / M_{\text{Pl}} \sim \text{TeV}.$$

* $M_s = M_{\text{GUT}} \sim 10^{16} \text{ GeV}$. (GUT, inflation).

How to get large V ?

* ADD $M_S \sim 1 \text{ TeV}$
SLED

units of L_S .

* Intermediate scale: $M_S \sim 10^{16} \text{ GeV}$
 $m_{\nu_2} = M_U^2 / M_P \sim \text{TeV}$.

* $M_S = M_{GUT} \sim 10^{16} \text{ GeV}$. (GUT, inflation).

How to get large ν ?

* $M_s = M_{\text{GUT}} \sim 10^{16} \text{ GeV}$. (GUT, inflation).

How to get large V ? Type IIB

* $M_s = M_{\text{GUT}} \sim 10^{16} \text{ GeV}$. (GUT, inflation).

How to get large V ? Type IIB

Massless sector in 10D:

G_{MN} ; B_{MN} , λ_{MN} , A_{MNPQ} , $\tilde{\Phi}$, $\tilde{\psi}$, $\tilde{\chi}$, $\tilde{\nu}$

* $M_5 = M_{\text{GUT}} \sim 10^{16} \text{ GeV}$. (GUT, inflation).

How to get large V ? Type IIB

Masses of fields in 10D: $\mathcal{I}_{MN}, B_{MN}, A_{MN}, A_{MNPQ}, \tilde{\Phi}, \tilde{a}, \tilde{F}_{MN}$
 and $\langle \mathcal{I}_{mn} \rangle, \langle B_{mn} \rangle, \dots$ $m, n = 5, \dots, 9$

* $M_5 = M_{\text{GUT}} \sim 10^{16} \text{ GeV}$. (GUT, inflation).

How to get large V ? Type IIB

Massless sector in 10D:

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

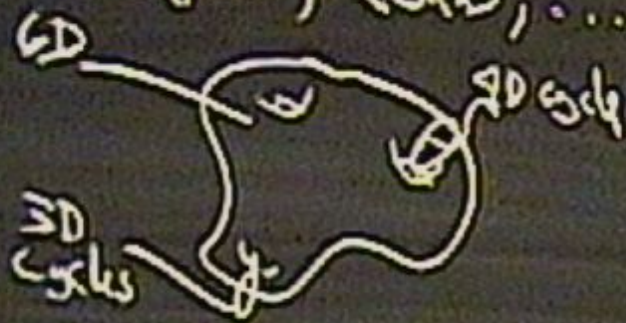
$g_{MN}; B_{MN}, \tilde{A}_{MN}, A_{MNPQ}, \tilde{\Phi}, \tilde{a}, \tilde{F}_{\mu\nu}$
 $m, n = 5, \dots, 9$

How to get large V ? Type IIB

Massless sector in 10D:

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

$g_{MN}; B_{MN}, \tilde{A}_{MN}, A_{MNPQ}, \tilde{\phi}, \phi, \text{fermions}$
 $m, n = 5, \dots, 9$



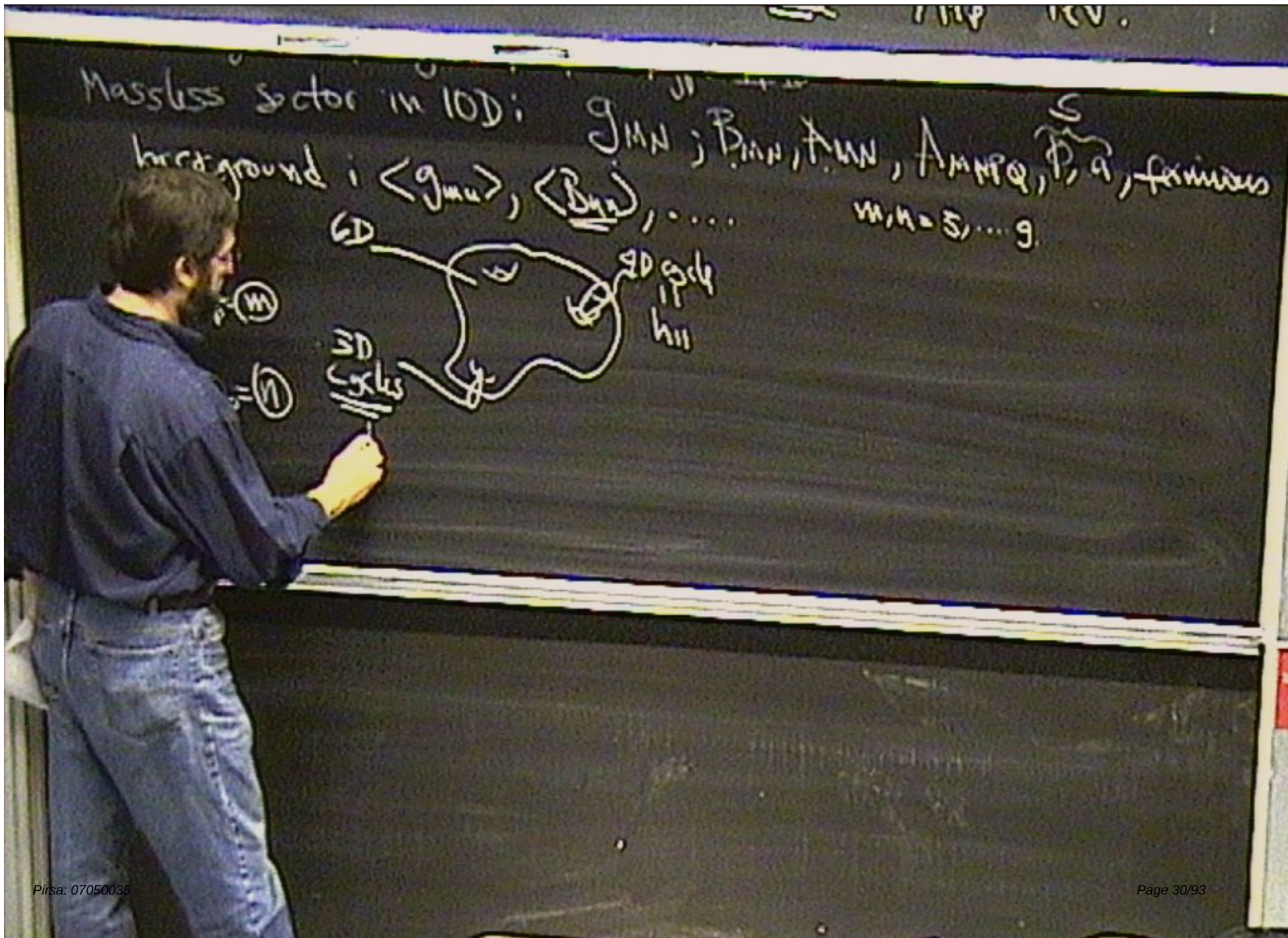
How to get large V ? Type IIB

Massless sector in 10D:

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

$g_{MN}; B_{MN}, X_{MN}, A_{MNPQ}, \tilde{\phi}, \alpha, \text{fermions}$
 $m, n = 5, \dots, 9$

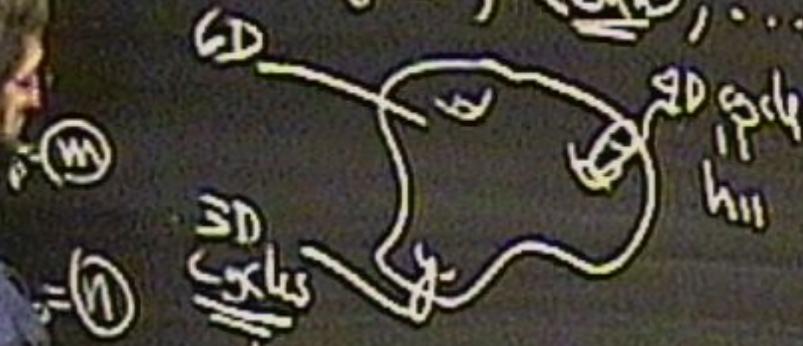




Massless sector in 10D:

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

$G_{MN}, B_{MN}, A_{MN}, A_{MNPQ}, \tilde{P}, a$, families
 $m, n = 5, \dots, 9$



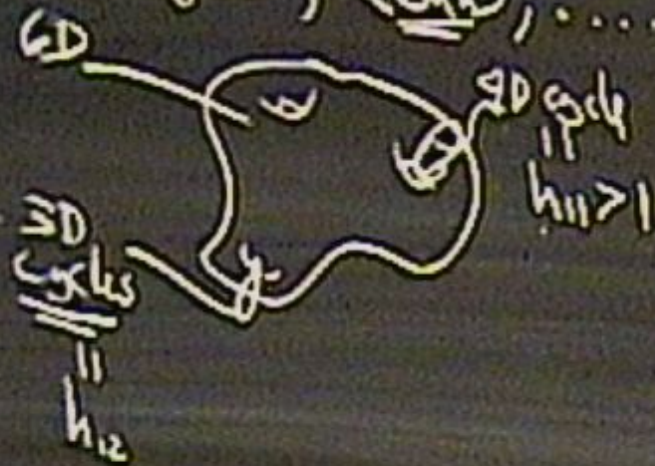
Massless sector in 10D:

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

$G_{MN}; B_{MN}, A_{MN}, A_{MNPQ}, \tilde{P}, a, \text{fermions}$
 $m, n = 5, \dots, 9$

$\int H_{10}^2 = (m)$

$\int F_{4,p}^2 = (n)$
 $\gamma_3 \parallel dA$



How to get large V ? Type IIB
 Massless sector in 10D: G_{MN} ; B_{MN} , $\tilde{A}_{MN}$, A_{MNPQ} , $\tilde{\Phi}$, α , fermions
 background: $\langle g_{\mu\nu} \rangle$, $\langle B_{\mu\nu} \rangle$, $\dots$ $m, n = 5, \dots, 9$

4D
 $\int H_{10}^2 = (M)$

4D
 $\int F_{4np}^2 = (N)$
 γ_5 γ_4

6D

3D
 cycles
 $\parallel$
 h_{12}

3D
 $g_{\mu\nu}$
 $h_{11} > 1$

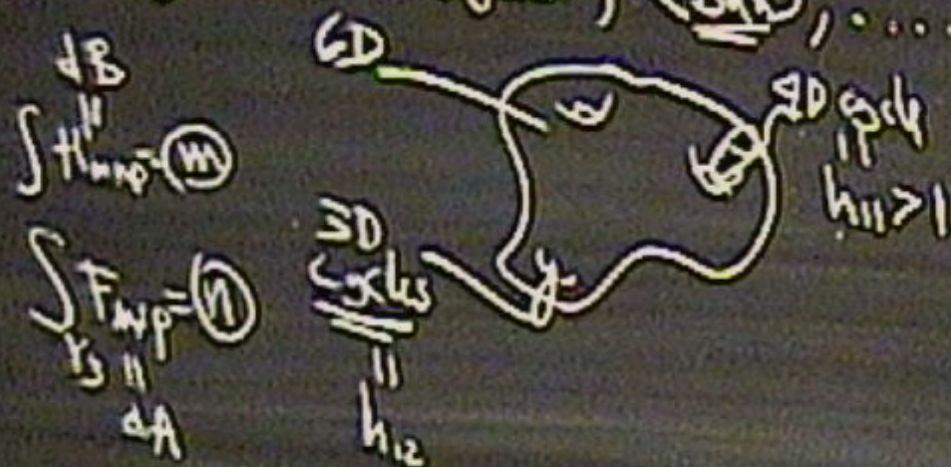


How to get large V ? Type IIB

Massless sector in IOD:

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

$G_{MN}; B_{MN}, A_{MN}, A_{MNPQ}, \tilde{\Phi}, a, \text{fermions}$
 $m, n = 5, \dots, 9$



How to get large V ? Type IIB

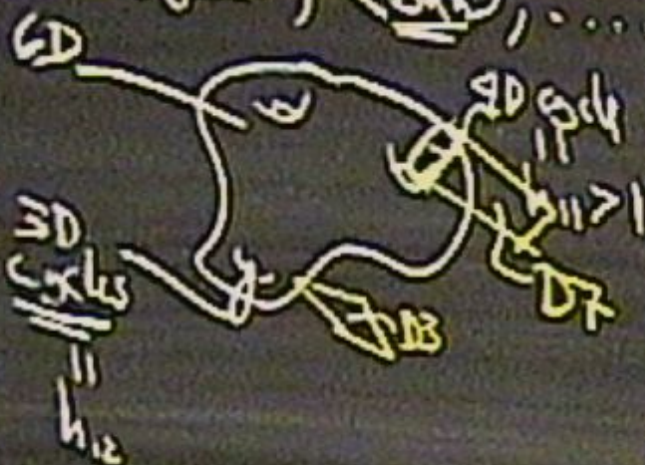
Massless sector in 10D:

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

$G_{MN}; B_{MN}, A_{MN}, A_{MNPQ}, \tilde{\Phi}, a, \text{fermions}$
 $m, n = 5, \dots, 9$

$$\int H_{\mu\nu\rho}^2 = (m)$$

$$\int F_{\mu\nu}^2 = (n)$$



How to get in
Massless sector

background: $\langle g_{\mu\nu} \rangle, \langle B_{\mu\nu} \rangle, \dots$

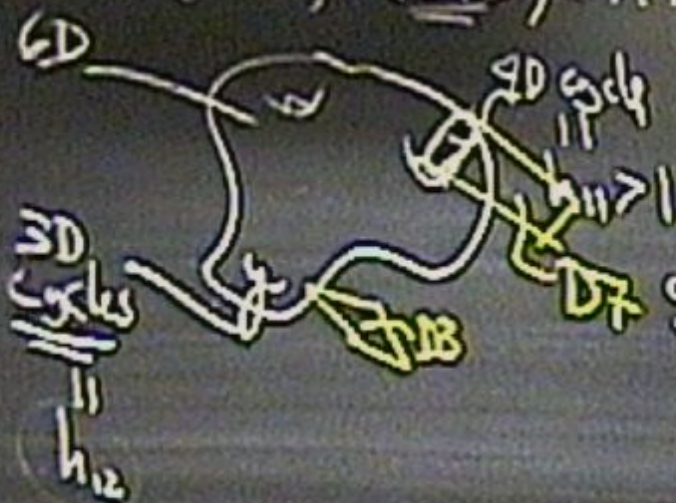
$\gamma^{\mu\nu} \Pi B$

$N; B_{MN}, A_{MN}, A_{MNPQ}, \tilde{\phi}, a, \text{fermions}$
 $M, N = 5, \dots, 9$

$$\int H_{10}^2 = (M)$$

$$\int F_{4np}^2 = (N)$$

$\gamma_3 \parallel dA$



gauge coupling $\sim \frac{1}{g_2} = \tau$ (size of cycle)

Large Extra dimensions and darkness from
string theory:

4D Effective Field Theory. N=1:

4D Effective Field Theory. N=1:

$$W = W_0 + A_\mu e^{a_\mu \tau_\mu}$$

K $\rightarrow$ fluxes $\rightarrow$ Nonpert on D7 branes

4D Effective Field Theory. N=1:

$$W = W_0(\psi, S) + A_\mu e^{a_\mu T_L} \rightarrow \text{Not part of D7 branes}$$

$\searrow$ $\nearrow$
feynman

$$K = K_{\text{us}} - 2 \log \mathcal{V} + K_F$$

4D Effective Field Theory. N=1:

$$W = W_0(\psi, s) + A_\mu e^{a_\mu \tau_\mu} \rightarrow \text{Nonpert on D7 branes}$$

$\searrow$ $\nearrow$
feynman

$$K = K_{\text{vs}} - 2 \log V + K_F$$

$$V = \lambda_{ijk} t_i t_j t_k, \quad \tau_i = \frac{\partial V}{\partial t_i}$$

4D Effective Field Theory. $N=1$:

$$W = W_0(\psi, S) + A_i e^{a_i \tau_i} \rightarrow \text{fermions} \rightarrow \text{Nonpert on D7 branes}$$

$$K = K_{\text{us}} - 2 \log V + K_F$$

Scalar potential: $V = \lambda_{ijk} t_i t_j t_k$; $\tau_i = \frac{\partial V}{\partial t_i}$
 $V(\psi, S, \tau_i)$; $a=1, \dots, h_2$
 $i=1, \dots, h_1$

4D Effective Field Theory. N=1:

$$W = W_0(\psi, S) + A_i e^{a_i T_i} \rightarrow \text{fermions} \rightarrow \text{Nonpert on D7 branes}$$

$$K = K_{\text{us}} - 2 \log V + K_F$$

Scalar potential: $V = \lambda_{ijk} t_i t_j t_k$; $T_i = \frac{\partial V}{\partial t_i}$

$$\underline{V(\psi, S, T_i)} ; \begin{matrix} a=1, \dots, h_2 \\ \lambda=1, \dots, h_n \end{matrix}$$

fixes ψ, S, T_i .

$$V = \frac{|D_{0,5} W|^2}{v^2} + \frac{e}{v} - \frac{e^{-\alpha_1 T_1} W_0}{v^2} + \frac{T_1 |W_0|^2}{v^3}$$

$$V = \frac{|D_{0,5} W|^2}{v^2} + \frac{e^{-2\alpha_5 T_5}}{v} - \frac{e^{-\alpha_5 T_5} W_0}{v^2} + \frac{\tau |W_0|^2}{v^3}$$

(Example: $v = T_b^{3/2} - T_s^{3/2}$)

$$V \approx \frac{|D_{0,s}W|^2}{V^3} + \underbrace{\frac{e^{-2\alpha_s \tau_s}}{V} - \frac{e^{-\alpha_s \tau_s} |W_0|}{V^2} + \frac{\tau |W_0|^2}{V^3}}_{V}$$

(Example: $V = \tau_b^{3/2} - \tau_s^{3/2}$)

Minimum: $D_{0,s}W = 0$

$$V = \frac{|D_{0,s}W|^2}{v^3} + \underbrace{\frac{e^{-2\alpha_s \tau_s}}{v} - \frac{e^{-\alpha_s \tau_s} W_0}{v^2} + \frac{\tau_s |W_0|^2}{v^3}}_{\text{Example: } v = \tau_b^{3/2} - \tau_s^{3/2}}$$

(Example: $v = \tau_b^{3/2} - \tau_s^{3/2}$)

Minimum: $D_{0,s}W = 0$

$$v \sim e^{\alpha_s \tau_s} W_0, \quad \tau_s \sim \frac{c}{\omega} > 1$$

$$V = \frac{|D_{0,s} W|^2}{v^2} + \underbrace{\frac{e^{-2a_s T_s}}{v} - \frac{e^{-a_s T_s} |W_0|}{v^2} + \frac{T |W_0|^2}{v^3}}_{\frac{v}{v^2} - \tau_b^{3/2} - \tau_s^{3/2}}$$

(Example: $v = \tau_b^{3/2} - \tau_s^{3/2}$)

Minimum: $D_{0,s} W = 0$

Subramanian,
Berglund, J. Conlon

$$v \sim e^{a_s T_s} W_0 ; \tau_s \sim c/v > 1$$

$$V = \frac{|D_{0,S} W|^2}{V^0} + \underbrace{\frac{e^{-2a_S T_S}}{V} - \frac{e^{-a_S T_S} |W_0|}{V^2} + \frac{T |W_0|^2}{V^3}}_{\frac{V}{\tau_b^{3/2} - \tau_S^{3/2}}}$$

(Example: $V = \tau_b^{3/2} - \tau_S^{3/2}$)

Minimum: $D_{0,S} W = 0$

Basubramanian,
Berglund, J. Conlon

$V \sim e^{a_S T_S} W_0$; $\tau_S \sim c/\tau_b > 1$

(J. Conlon) ✓
→ (JC + M. Cicoli)

e.g.: $\alpha_s \sim \frac{2\pi}{g_s N}$, $g_s N \sim 1 \Rightarrow \nu \sim 10^{30} \Rightarrow M_s \sim \text{TeV}$

e.g.: $a_s \sim \frac{2\pi}{g_s N}$; $N \sim 1 \Rightarrow V \sim 10^{30} \Rightarrow M_s \sim \text{TeV}$

$20 \Rightarrow V \sim 10^4 \Rightarrow M_s \sim M_{\text{GUT}}$

e.g.: $\alpha_s \sim \frac{2\pi}{g_s N}$; $N \sim 1 \Rightarrow \nu \sim 10^{20} \Rightarrow M_s \sim T + V$

$20 \Rightarrow \nu \sim 10^4 \Rightarrow M_s \sim M_{\text{conf}}$

4D Effective Field Theory. $N=1$:

$$W = W_0(\phi, S) + A_i e^{-a_i T_i}$$

$\downarrow$ fluxes

$$K = K_{\text{v.s.}} = 2 \log |z| + \underline{K_F} \rightarrow \text{Nonpert.}$$

Scalar potential: $V = V(\phi, S, T_i)$; $T_i = \dots$
 $a = 1, \dots, h$
 $\lambda = 1, \dots, h$

$\rightarrow$ units of
ls.

$\sim 10^{16}$ V
TeV.

$$\nabla(\psi, S, T) ; \alpha=1, \dots, h, z$$

$$\text{find } \psi, S, T, \lambda$$

$$\lambda=1, \dots, h$$

Minimum
Bilanzströme
Berglundy

$$D_{0,5} W = 0$$

$$V \sim e^{\frac{a}{T_0}} W_0 ; T_0 \sim c / \langle \mathbb{D} \rangle > 1$$

$$(J, \omega)$$

$$\rightarrow (JC + I)$$

$$V \approx \frac{|D_{0,5} W|}{v^0} + \frac{e}{v} - \frac{e}{v^2} W_0 + \frac{\frac{1}{2} |W_0|^2}{v^3}$$

(Example: $V = T_b^{3/4} \cdot T_s^{3/2}$)

Minimum: $D_{0,5} W = 0$
 Balasubramanian,
 Berglund; J. Conlon

$$V \sim e^{a T_s} W_0$$

(J. Conlon) ✓
 → (JC + M. Cridi)

k_1

c/a_0

$$V \approx \frac{|D_{0,S} W|}{v^2} + \frac{e}{v} - \frac{e}{v^2} W_0 + \frac{\tau |W_0|^2}{v^3}$$

(Example: $V = \tau_b^{3/2} \cdot \tau_s^{3/2}$)

$$K_F \sim \frac{g}{v}$$

Minimum: $D_{0,S} W = 0$

Balasubramanian,
Berglund, J. Conlon

$$v \sim e^{a\tau_s} W_0 ; \tau_s \sim c/\tau_s > 1$$

(J. Conlon) ✓
→ (JC + M. Cridi)

$$V \approx \frac{|D_{0,S} W|^2}{v^2} + \frac{e}{v} - \frac{e}{v^2} W_3 + \frac{\tau |W_0|^2}{v^3}$$

(Example: $V = \tau_b^{3/2} - \tau_s^{3/2}$)

Minimum: $D_{0,S} W = 0$

Belasubramanian,
Berglund; J. Conlon

$$v \sim e^{(a/\tau_s)} W_3$$

$$K_F \sim \frac{g}{v} + \frac{\tau}{v} + \dots$$

$$c/\tau_s > 1 \quad \text{gs loops}$$

(J. Conlon) ✓
→ (JC + M. Cicoli)



e.g.: $a_s \sim \frac{2\pi}{g_s N}$; $N \sim 1 \Rightarrow \nu \sim 10^{30} \Rightarrow M_s \sim \text{TeV}$

$20 \Rightarrow \nu \sim 10^4 \Rightarrow M_s \sim M_{\text{GUT}}$

$\times M_s \sim \text{TeV}$, $m_{3/2} \sim 10^{-3} \text{ eV}$

e.g.: $a_s \sim \frac{2\pi}{g_s N}$; $N \sim 1 \Rightarrow \nu \sim 10^{30} \rightarrow M_s \sim \text{TeV}$

$20 \Rightarrow \nu \sim 10^4 \rightarrow M_s \sim M_{\text{GUT}}$

$\times M_s \sim \text{TeV}$, $m_{3/2} \sim \underline{10^{-3} \text{ eV}}$, $m_{\tilde{t}_6} \sim 10^{-26} \text{ GeV}$.

(soft terms)

e.g.: $a_s \sim \frac{2\pi}{g_s N}$; $N \sim 1 \Rightarrow \nu \sim 10^{30} \Rightarrow M_s \sim \text{TeV}$

$20 \Rightarrow \nu \sim 10^4 \Rightarrow M_s \sim M_{\text{GUT}}$

$\times M_s \sim \text{TeV}$, $m_{3/2} \sim \underline{10^{-3} \text{ eV}}$, $m_{\tau_6} \sim 10^{-26} \text{ GeV}$.

(soft terms, $m_0 \gg \text{TeV}$, $\underline{M_X}$ small).

$$20 \Rightarrow V \sim 10^4 \rightarrow M_S \sim M_{GUT}$$

$$\times M_S \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^{-3}} \text{ eV}, \quad m_{T_b} \sim 10^{-26} \text{ GeV},$$

$$\left[(\text{soft terms}, \quad m_0 \gg \text{TeV}, \quad \underline{M_k} \text{ small}) \right] \leftarrow$$

$$20 \Rightarrow V \sim 10^4 \rightarrow M_S \sim M_{\text{GUT}}$$

$$\times M_S \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^{-3}} \text{ eV}, \quad m_{\tilde{\tau}_6} \sim 10^{-26} \text{ GeV}.$$

$$\left[(\text{soft terms}, \quad m_0 \gg \text{TeV}, \quad \underline{M_{\text{GUT}} \text{ small}}) \right] \leftarrow$$

$\rightarrow M_S \sim 10^{11} \text{ GeV}.$

$$2D \Rightarrow V \sim 10^4 \rightarrow M_S \sim M_{\text{GUT}}$$

$$\times M_S \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^{-3}} \text{ eV}, \quad m_{T_b} \sim 10^{-26} \text{ GeV}.$$

$$\left[(\text{soft terms } m_0 \gg \text{TeV}, \underline{M_X \text{ small}}) \right] \leftarrow$$

$$\rightarrow M_S \sim 10^{11} \text{ GeV}.$$

Aside: large 2 dimensions?

4D Effective Field Theory. $N=1$:

$$W = W_0(\phi, S) + A_\alpha e^{-a_\alpha T_i}$$

$\downarrow$ fluxes

$$K = K_{\text{us}} - 2 \log \mathcal{V} + \underbrace{\left(\frac{K_F}{\mathcal{V}} \right)}_{\text{Nonpert on D7 brane}}$$

Scalar potential: $V = \lambda_{ijk} t_i t_j t_k$; $T_i = \frac{\partial \mathcal{V}}{\partial t_i}$

$$\frac{V(\phi, S, T_i)}{\text{fix } \phi, S, T_i} ; \begin{matrix} a=1, \dots, h, 2 \\ i=1, \dots, h \end{matrix}$$

eg: $a_3 \sim \frac{2\pi}{g_3 N}$, $N=1 \Rightarrow V \sim 10^{20} \Rightarrow M_s \sim \text{TeV}$

$20 \Rightarrow V \sim 10^4 \Rightarrow M_s \sim M_{\text{Planck}}$

* $M_s \sim \text{TeV}$, $m_{3/2} \sim \underline{10^3 \text{ eV}}$, $m_{T_6} \sim 10^{-26} \text{ GeV}$

$\left[\text{soft terms } m_0 \gg \text{TeV}, M_{\text{GUT}} \text{ small} \right] \leftarrow$

$\rightarrow M_s \sim 10^{11} \text{ GeV}$

A: large 2 dimensions?
 t_1 very large, T_1 small.

$$20 \Rightarrow V \sim 10^4 \rightarrow M_s \sim M_{\text{GUT}}$$

$$\times M_s \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^{-3}} \text{ eV}, \quad m_{\tilde{g}} \sim 10^{-26} \text{ GeV}.$$

$$\left[(\text{soft terms}, \quad m_0 \gg \text{TeV}, \quad \underline{M_X \text{ small}}) \right] \leftarrow$$

$$\rightarrow M_s \sim 10^{11} \text{ GeV}.$$

Aside: large 2 dimensions?

t_1 very large, T_1 small.

e.g.: $V = t_1 t_2^2 + t_2^3 + \dots$

$$20 \Rightarrow V \sim 10^4 \rightarrow M_S \sim M_{\text{GUT}}$$

$$\times M_S \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^{-3} \text{ eV}}, \quad m_{\tilde{g}} \sim 10^{-26} \text{ GeV}.$$

$$\left[(\text{soft terms } m_0 \gg \text{TeV}, \underline{M_X \text{ small}}) \right] \leftarrow$$

$$\rightarrow M_S \sim 10^{11} \text{ GeV}.$$

Aside: large 2 dimensions?

t_1 very large, T_1 small.

$$\text{e.g. } V = \underline{t_1} t_2^2 + t_2^3 + \dots \quad \left\{ \begin{array}{l} V \sim \sqrt{t_1} (T_2 - T_1) \\ \nearrow \text{No large volume.} \end{array} \right.$$

$$\gamma_i \frac{\partial V}{\partial t_i} = \underline{t_1^2} + \dots$$

$$20 \Rightarrow V \sim 10^4 \rightarrow M_5 \sim M_{\text{GUT}}$$

$$* M_5 \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^{-3} \text{ eV}}, \quad m_{T_6} \sim 10^{-26} \text{ GeV}.$$

$$\left[(\text{soft terms } m_0 \gg \text{TeV}, \underline{M_X \text{ small}}) \right] \leftarrow$$

$$\rightarrow M_5 \sim 10^{11} \text{ GeV}.$$

Aside: large 2 dimensions?

t_1 very large, T_1 sm

$$\text{e.g. } V = \underline{t_1} t_2^2 + t_2^3$$

$$\gamma_i \frac{\partial V}{\partial t_i} = \underline{t_1^2} + \dots$$

$$\sim \sqrt{t_1} (T_2 - T_1) - T_2^{3/2}$$

→ No large volume.

$$20 \Rightarrow V \sim 10^4 \rightarrow M_s \sim M_{\text{GUT}}$$

$$* M_s \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^{-3} \text{ eV}}, \quad m_{\tilde{g}} \sim 10^{-26} \text{ GeV}.$$

$$\left[(\text{soft terms } m_0 \gg \text{TeV}, \underline{M_X \text{ small}}) \right] \leftarrow$$

$$\rightarrow M_s \sim 10^{11} \text{ GeV}.$$

Aside: large 2 dimensions? X

t_1 very large, T_1 small.

$$\text{e.g. } V = \underline{t_1} t_2^2 + t_2^3 + \dots \quad \left\{ \begin{array}{l} \text{No large volume} \\ V \sim \sqrt{t_1} (T_2 - T_1) = T_2^{3/2} \end{array} \right.$$

$$\gamma_i \frac{\partial V}{\partial t_i} = \underline{t_1^2} + \dots$$

$g_s N$ $N=1 \Rightarrow V \sim 10^4 \rightarrow M_S \sim M_{\text{GUT}}$
 $\times M_S \sim \text{TeV}, \quad m_{3/2} \sim \underline{10^3 \text{ eV}}, \quad m_{\tilde{g}} \sim 10^{26} \text{ GeV}.$

$\left[\text{soft terms, } m_0 \gg \text{TeV}, \underline{M_{1/2} \text{ small}} \right] \leftarrow$

$\rightarrow M_S \sim 10^{11} \text{ GeV}$

Aside: large 2 dimensions? X
 t_1 very large, T_1 small.

e.g.: $V = t_1^2 + t_2^2 + \dots \quad \left\{ \begin{array}{l} V \sim \sqrt{t_1} (T_2 - T_1) \\ \gamma \frac{\partial V}{\partial t_1} = \frac{1}{t_1} + \dots \end{array} \right.$

$\rightarrow$ No large volume.

$\left(\frac{T_2}{T_1} \right)^{3/2}$
 large T_1, T_2

* $M_S = M_{GUT}$. (inflation !)



$$V \approx \frac{|D_{0,5} W|^2}{v^2}$$

(Example:

Minimum:

Elastostaticity,
Berglund, J. Coulon

(J. Coulon)

→ (JC + H. Gredl)

$$V = \frac{e}{v} - \frac{e}{v^2} W_0 + \frac{\tau |W_0|^2}{v^3}$$

$$W_0 ; \tau_s \sim c / \tau_s > 1 \quad g_s \text{ loops}$$

$$k_p \sim \frac{g}{v} + \frac{\tau}{v} + \dots$$

$$V \approx \frac{|D_{0,5} W|^2}{V^0} + \frac{e^{-2\alpha_5 T_5}}{V} - \frac{e^{-\alpha_5 T_5} W_0}{V^2} + \frac{T |W_0|^2}{V^3}$$

(Example: $V = \tau_b^{3/4} - \tau_s^{3/2}$)

Minimum: $D_{0,5} W = 0$

Belasubramanian,
Berglund, J. Conlon

$$V \sim e^{\alpha T_5} W_0 ; \quad T_5 \sim C/k$$

$$K_F \sim \frac{g}{V} + \frac{F}{V} + \dots$$

g_s loops

(J. Conlon) ✓
→ (JC + M. Cribeli)

$$V \approx \frac{|D_{0,5} W|^2}{v^2} + \underbrace{\frac{e^{-2\alpha_5 \tau_5}}{v} - \frac{e^{-\alpha_5 \tau_5} W_0}{v^2} + \frac{\tau_5 |W_0|^2}{v^3}}_{K_F \sim \frac{g}{v} + \frac{\tau}{v} + \frac{|W|^2}{v}}$$

(Example: $V = \tau_b^{3/2} - \tau_s^{3/2}$)

Minimum: $D_{0,5} W = 0$

Belasitskii, Birlund, J. Conlon

$V \sim e^{a\tau_s} W_0$; $\tau_s \sim c/\tau_s > 1$ g_s loops

(J. Conlon) ✓
→ (JC + M. Cicoli)

* $M_s = M_{GOT}$; (inflation !)



* $M_s = M_{GUT}$: (inflation !)



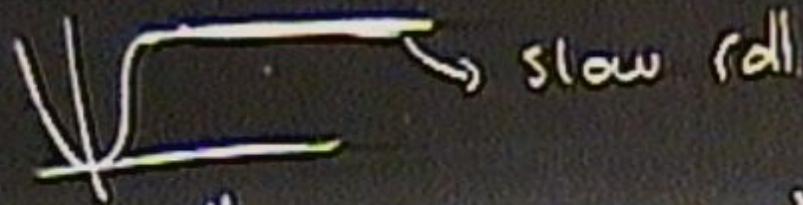
* $M_S = M_{GUT}$. (inflation !)



* $M_S = M_{GUT}$. (inflation !)



* $M_5 = M_{\text{GUT}}$: (inflation!)

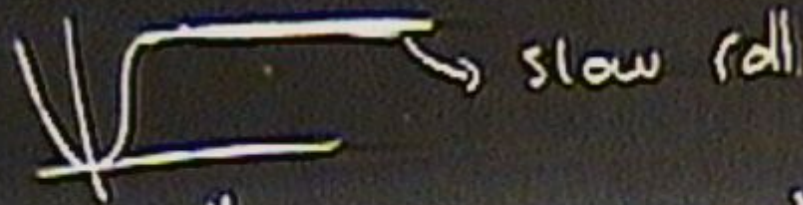


$\Rightarrow M_{\text{inf.}} \sim 10^{11} \text{ GeV} \rightarrow m_{3/2} \sim \frac{M_P}{\sqrt{V}}; M_5 = \frac{M_P}{\sqrt{V}}$

$M_{\text{KK}} = M_P / \sqrt{3}$

net (DF branes) $\sim \frac{m_{3/2}}{(2\pi T_1)} \sim \frac{m_{3/2}}{\log(M_P/m_{3/2})}$

* $M_S = M_{GUT}$. (inflation !)



* $M_S = M_{inf.} \sim 10^{11} \text{ GeV}$. $\rightarrow m_{3/2} \sim \frac{M_P}{\sqrt{V}}$; $M_S = \frac{M_P}{\sqrt{V}}$

$$M_{KK} = M_P / \sqrt{3}$$

(DF branes) $\sim \frac{m_{3/2}}{M_{GUT}} \sim \frac{m_{3/2}}{\log(M_P/m_{3/2})}$

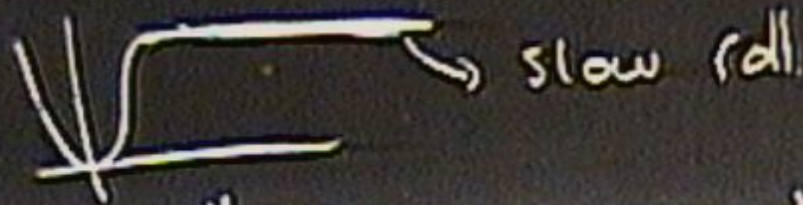
* $M_S = M_{\text{GUT}}$. (inflation !)



* $M_S = M_{\text{inf}} \sim 10^{11} \text{ GeV}$. $\rightarrow m_{3/2} \sim \frac{M_P}{\sqrt{V}}$; $M_S = \frac{M_P}{\sqrt{V}}$

$M_{\text{soft}} (\text{D7 branes}) \sim \frac{m_{3/2}}{(\frac{2\pi}{3})^{1/2}} \sim \frac{m_{3/2}}{\log(M_P/m_{3/2})}$

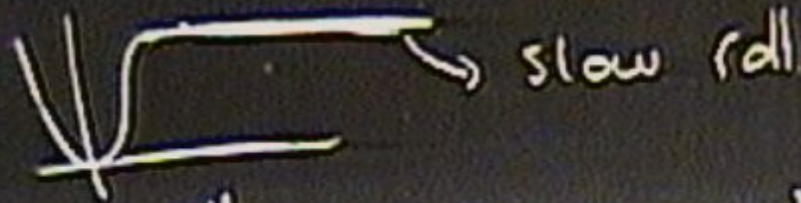
* $M_S = M_{GUT}$: (inflation!)



* $M_S = M_{inf.} \sim \underline{10^{11} \text{ GeV}}$. $\rightarrow m_{3/2} \sim \frac{M_P}{V}$; $M_S = \frac{M_P}{V}$

$M_{soft} \text{ (D7 branes)} \sim \frac{m_{3/2}}{(M_{Pl})^2} \sim \frac{m_{3/2}}{\log(M_P/m_{3/2})}$; $M_{KK} = M_P / V^{1/3}$
 ; 'axion, V-mass'

* $M_5 < M_{\text{GUT}}$: (inflation!)



$$M_5 = M_{\text{inf.}} \sim \underline{10^{11} \text{ GeV}} \rightarrow m_{3/2} \sim \frac{M_P}{\sqrt{V}}; M_5 = \frac{M_P}{\sqrt{V}}$$

$$M_{\text{KK}} = M_P / \sqrt{V^3}$$

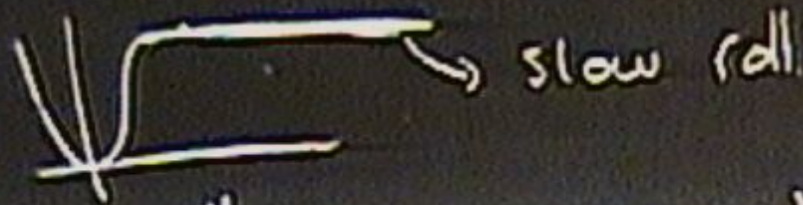
$M_{\text{soft}} (\text{D7 branes}) \sim$

$$\frac{m_{3/2}}{(2\pi)^2 \alpha'} \sim \frac{m_{3/2}}{\log(M_P/m_{3/2})}$$

Moduli: m_{τ_2}

} axion,
V-masses

* $M_S = M_{\text{GUT}}$. (inflation !)



* $M_S = M_{\text{inf.}} \sim \underline{10^{11} \text{ GeV}}$. $\rightarrow m_{3/2} \sim \frac{M_P}{V}$; $M_S = \frac{M_P}{V^{1/3}}$

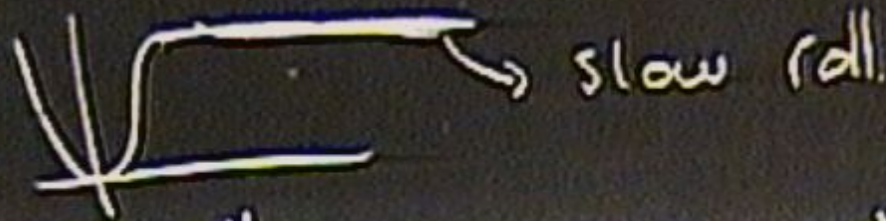
$M_{\text{soft}} (\text{D7 branes}) \sim \frac{m_{3/2}}{(\text{vol})^{1/4}} \sim \frac{m_{3/2}}{\log(M_P/m_{3/2})}$ $\checkmark$ $M_{\text{KK}} = M_P/V^{2/3}$

Moduli: $m_{T_2} \sim \frac{M_P}{V^{1/2}} \sim 1 \text{ MeV}$

$m_{T_1} \sim m_{3/2} \log(M_P/m_{3/2}) \sim 10^3 \text{ TeV}$

} axion, V-masses

* $M_5 = M_{\text{GUT}}$: (inflation !)



* $M_5 = M_{\text{inf.}} \sim \underline{10^{11} \text{ GeV}}$. $\rightarrow m_{3/2} \sim \frac{M_P}{V}$; $M_5 = \frac{M_P}{V}$

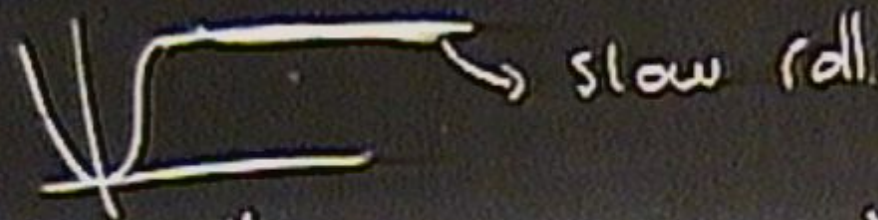
$$M_{\text{KK}} = M_P / V^{1/3}$$

$M_{\text{soft}} (\text{D7 branes}) \sim \frac{m_{3/2}}{(4\pi T_1)} \sim \frac{m_{3/2}}{\log(M_P/m_{3/2})}$

Moduli: $m_{T_1} \sim \frac{M_0}{V^{1/2}} \sim 1 \text{ MeV} \rightarrow m_{\phi_1} \sim 10^{11} \text{ GeV}$ } axion, V-masses

$m_{T_2} \sim m_{1/2} \log(M_P/m_{1/2}) \sim 10^3 \text{ TeV} \rightarrow m_{\eta} \sim \text{TeV}$

* $M_S = M_{GUT}$; (inflation !)



* $M_S = M_{int.} \sim \underline{10^{11} \text{ GeV}}$. $\rightarrow m_{3/2} \sim \frac{M_P}{V}$; $M_S = \frac{M_P}{V}$

$$M_{KK} = M_P / \sqrt{3}$$

$M_{soft} \text{ (D7 branes)} \sim \frac{m_{3/2}}{(\alpha' T_7)} \sim \frac{m_{3/2}}{\log(M_P/m_s)}$

Moduli: $m_{T_6} \sim \frac{M_P}{V^{1/2}} \sim 1 \text{ MeV}$ $\rightarrow m_{T_6} \sim 10^{11} \text{ GeV}$ } axion, & V-masses

$m_{T_7} \sim m_{3/2} \log(M_P/m_s) \sim 10^3 \text{ TeV} \rightarrow m_{T_7} \sim \text{TeV}$

$$\begin{aligned} \delta T_b &= \nu^{1/6} \Phi + \bar{\nu}^{2/3} \chi \\ \delta T_b &= \nu^{1/2} \Phi + \chi \\ &\quad \uparrow \quad \quad \uparrow \\ &\quad \text{heavy} \quad \text{light.} \end{aligned}$$

$$\delta T_b = \nu^{1/2} \Phi + \nu^{1/2} \chi$$

$$\delta T_b = \nu^{1/2} \Phi + \chi$$

heavy light.

Coupl.

matter: e^+, e^-, γ .

$$\lambda_{\chi\gamma\gamma} \sim \frac{1}{M_P \ln(M_P/m_\nu)} = \lambda_{ee\gamma} \frac{1}{M_P}$$

$$\leftarrow \lambda \Phi \gamma \gamma \sim \frac{1}{M_P} \sim \lambda \Phi e^+ e^-$$

$$\delta T_b = \nu^{1/2} \Phi + \bar{\nu}^{1/2} \chi$$

$$\delta T_b = \nu^{1/2} \Phi + \chi$$

heavy

light.

Couplings to matter: e^+, e^-, γ .

$$\tau_\chi \sim 10^{24-26} \text{ secs.} \leftarrow \lambda_{\chi\gamma\gamma} \sim \frac{1}{M_P \ln(M_P/m_\chi)} > \lambda_{ee\chi} \sim \frac{1}{M_P}$$

$$\tau_\Phi \sim 10^{17} \text{ sec.} \leftarrow \lambda_{\Phi\gamma\gamma} \sim \frac{1}{M_P} \sim \lambda_{\Phi ee}$$

$$\delta T_b = \nu^{1/6} \Phi + \nu^{2/3} \chi$$

$$\delta T_b = \nu^{1/2} \Phi + \chi$$

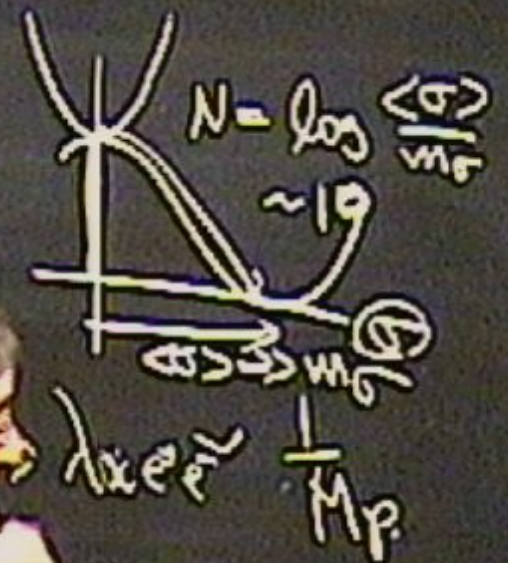
↑
heavy

↑
light.

Couplings to matter: e^+, e^-, γ .

$$\tau_\chi \sim 10^{24-26} \text{ secs.} \leftarrow \lambda_{\chi\gamma\gamma} \sim \frac{1}{M}$$

$$\tau_\Phi \sim 10^{17} \text{ sec.} \leftarrow \lambda_{\Phi\gamma\gamma} \sim \frac{1}{M}$$



$$\delta T_b = \nu^{1/2} \Phi + \nu^{1/2} \chi$$

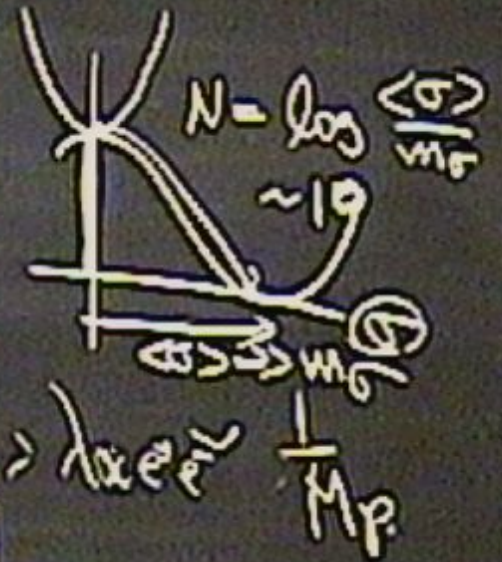
$$\delta T_b = \nu^{1/2} \Phi + \chi$$

$\uparrow$ heavy $\uparrow$ light.

Couplings to matter: e^+, e^-, γ .

$$\tau_\chi \sim 10^{24-26} \text{ secs.} \leftarrow \lambda_{\chi\gamma\gamma} \sim \frac{1}{M_P \ln(M_P/m_\chi)} > \lambda_{ee\chi} \sim \frac{1}{M_P}$$

$$\tau_\Phi \sim 10^{17} \text{ sec.} \leftarrow \lambda_{\Phi\gamma\gamma} \sim \frac{1}{M_J} \sim \lambda_{\Phi ee}$$



$$\delta T_b = \nu^{1/6} \Phi + \nu^{2/3} \chi$$

$$\delta T_b = \nu^{1/2} \Phi + \chi$$

Couplings

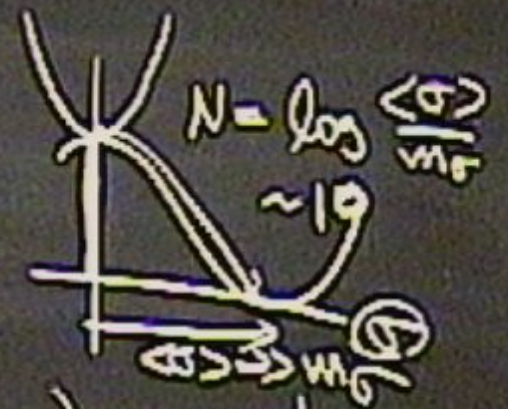
$\tau_h \sim 10^5$

$\tau_h \sim$

heavy matter: e^+, e^-, χ .
light.

$$\lambda_{\chi \nu \nu} \sim \frac{1}{M_P} \left(\frac{M_P}{M_P} \right) \sim \lambda_{\chi e^+ e^-} \sim \frac{1}{M_P}$$

$$\lambda_{\Phi \chi \tau} \sim \frac{1}{M_P} \sim \lambda_{\Phi e^+ e^-}$$



$$\delta T_b = \nu^{1/2} \Phi + \nu^{3/2} \chi$$

$$\delta T_b = \nu^{1/2} \Phi + \chi$$

↑
heavy

↑
light

Coupl

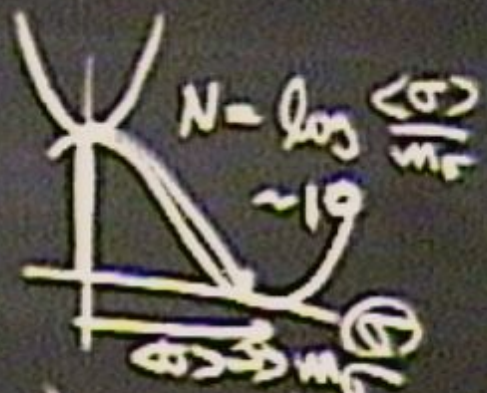
T_{in}

matter: e^+, e^-, γ

res. ←

$$\nu\gamma \sim \frac{1}{M_P \ln(E_\gamma/m_\nu)} : \lambda e e \sim \frac{1}{M_P}$$

$$\leftarrow \lambda \Phi \gamma \gamma \sim \frac{1}{M_P} \sim \lambda \Phi e e$$



$$\delta T_b = \nu^{1/6} \Phi + \nu^{2/3} \chi$$

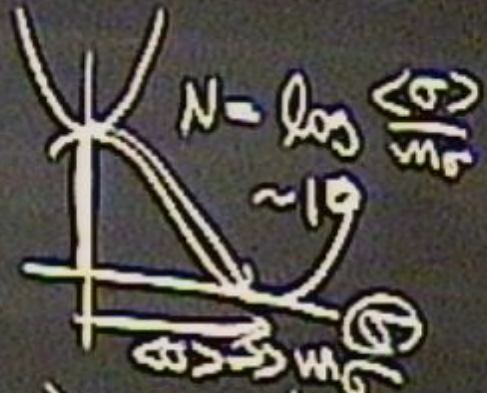
$$\delta T_b = \nu^{1/2} \Phi + \chi$$

Couplings
 $\tau_x \sim 10^{24}$

heavy
 after: e^+, e^-, γ

$$\leftarrow \lambda_{\chi \nu \gamma} \sim \frac{1}{M_P} \left(\frac{M_P}{m_\nu} \right), \lambda_{\chi e^+ e^-} \sim \frac{1}{M_P}$$

$$\uparrow \hat{\tau}_x \leftarrow \lambda_{\Phi \chi \gamma} \sim \frac{1}{M_P} \sim \lambda_{\Phi e^+ e^-}$$



$$\delta T_b = \nu^{1/2} \Phi + \nu^{2/3} \chi$$

$$\delta T_b = \nu^{1/2} \Phi + \chi$$

heavy

light.

Couplings to matter: e^+, e^-, γ .

$$\tau_\chi \sim 10^{24-26} \text{ secs.}$$

$$\leftarrow \lambda_{\chi \gamma \gamma} \sim$$

$$\frac{1}{M_P} \left(\frac{M_P}{m_\chi} \right)^2$$

$$\lambda_{\chi e^+ e^-} \sim \frac{1}{M_P}$$

$$\tau_\Phi \sim 10^{13} \text{ sec.}$$

$$\leftarrow \lambda_{\Phi \gamma \gamma} \sim$$

$$\frac{1}{M_P} \sim \lambda_{\Phi e^+ e^-}$$

