

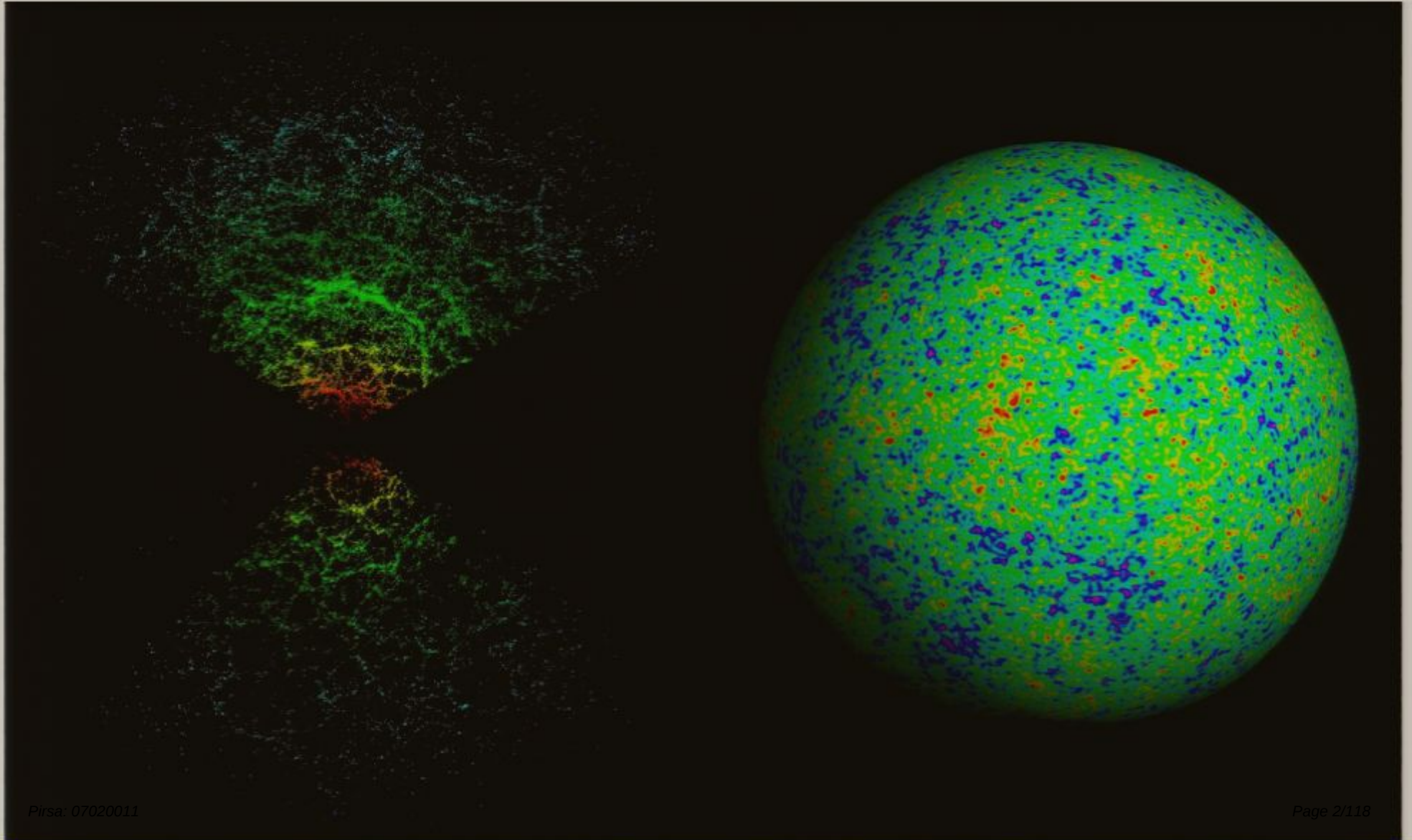
Title: New cosmic maps & measurements

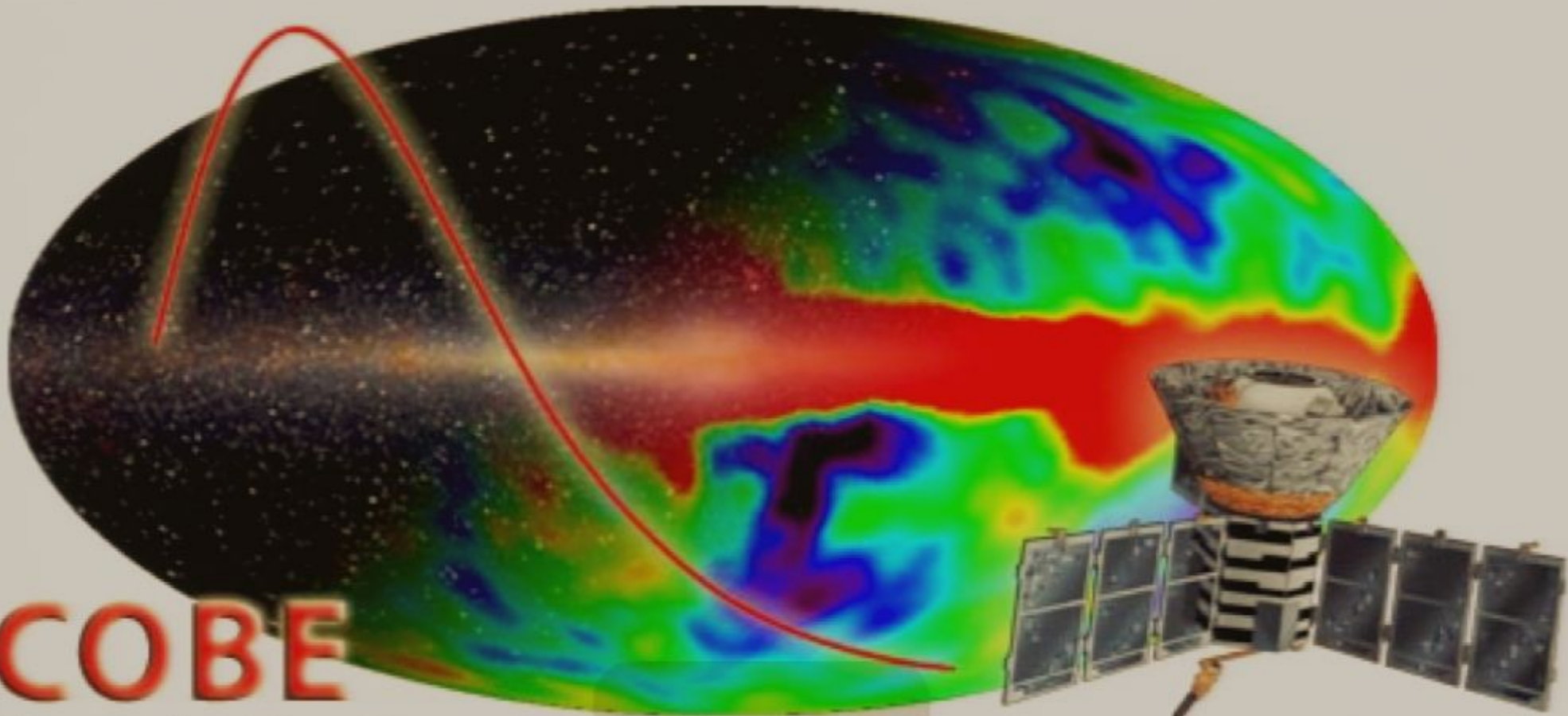
Date: Feb 01, 2007 11:00 AM

URL: <http://pirsa.org/07020011>

Abstract: I first summarize how the recent avalanche of precision measurements involving the cosmic microwave background, galaxy clustering, the Lyman alpha forest, gravitational lensing, supernovae Ia and other tools probes has transformed our understanding of our universe. I then discuss key open problems such as the nature of dark matter, dark energy and the early universe.

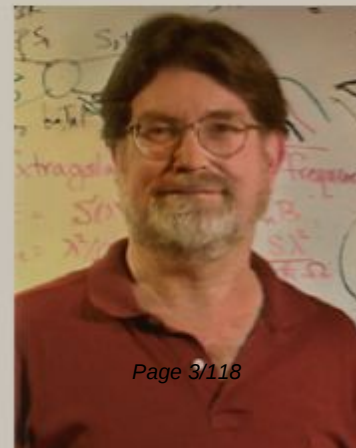
New cosmic maps & measurements



A large graphic showing a satellite (COBE) on the right, with a red line indicating its orbit around Earth. The background is a colorful map of the Cosmic Microwave Background (CMB) showing temperature fluctuations in shades of blue, green, yellow, and red.

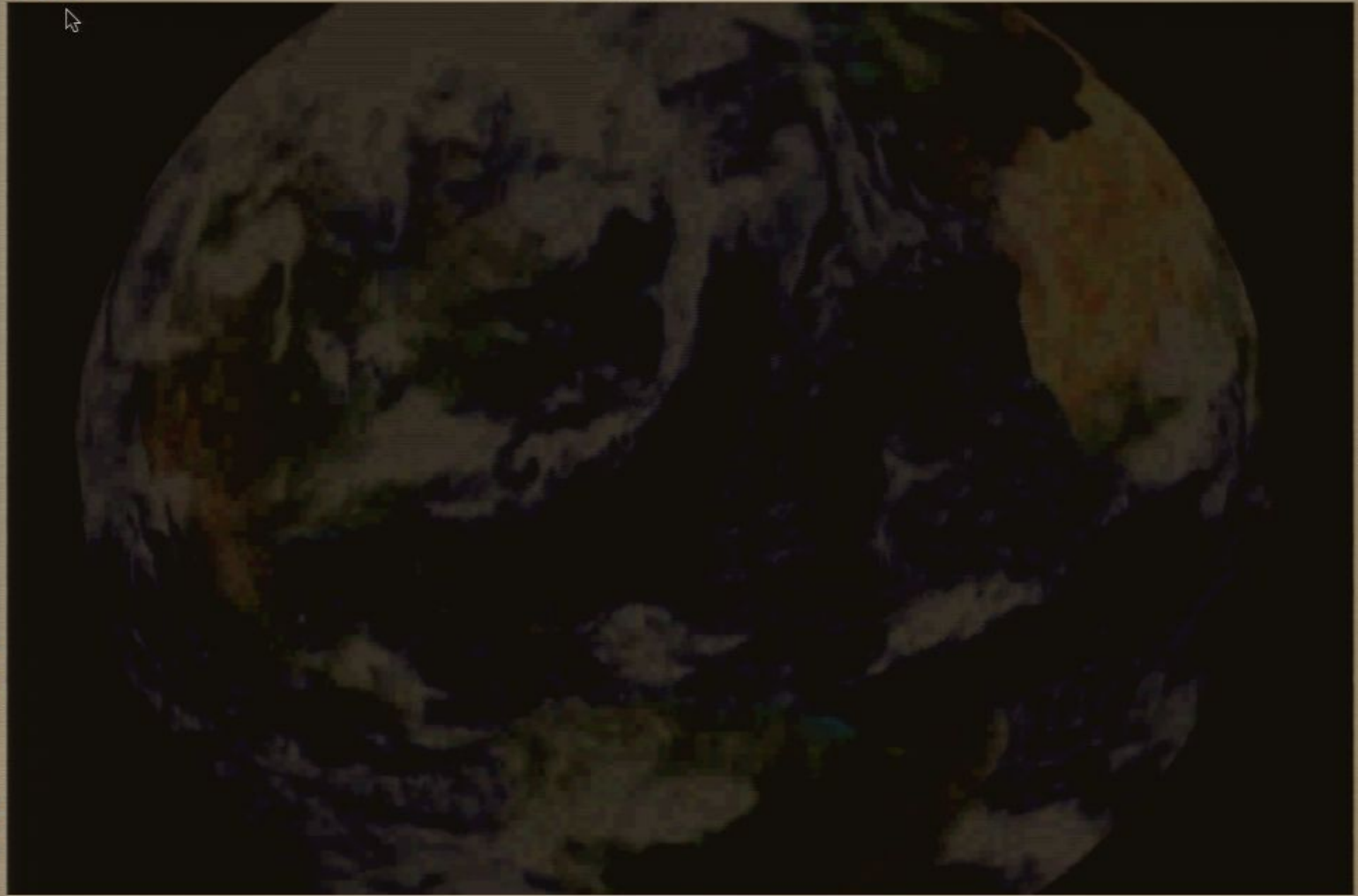
COBE

Cosmic Background Explorer



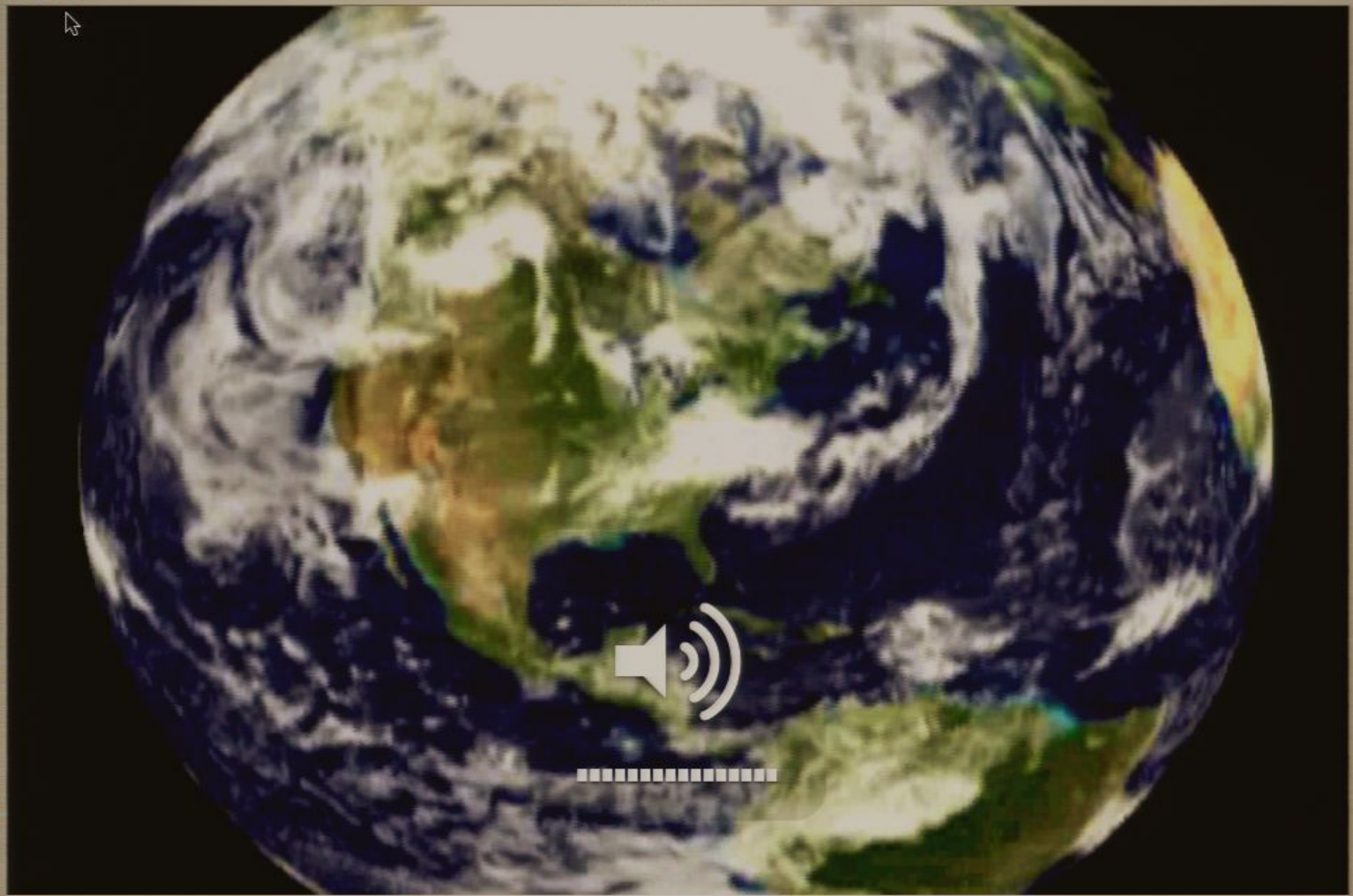
What have
we learned?

Mapping_Universe.mov

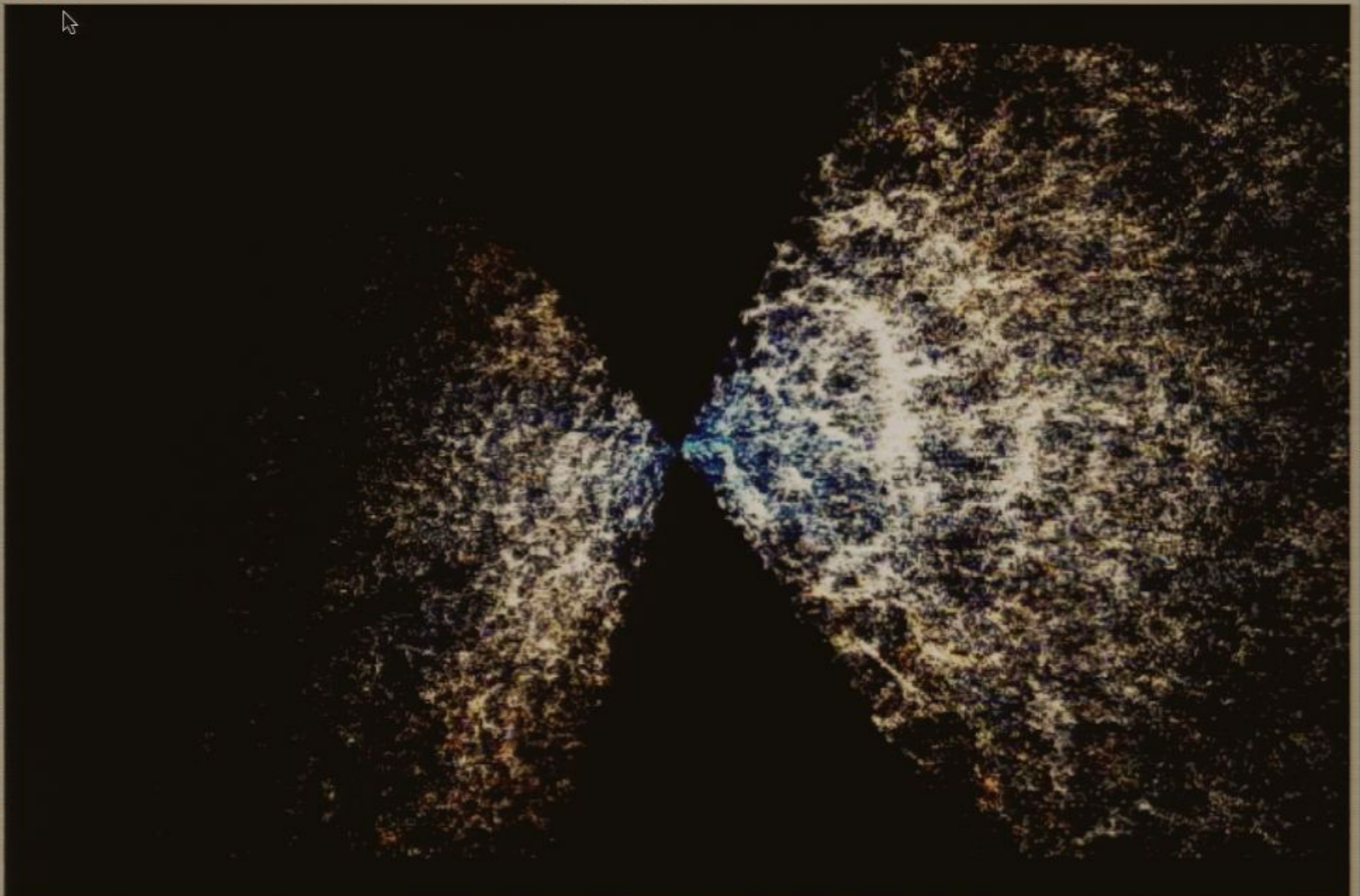


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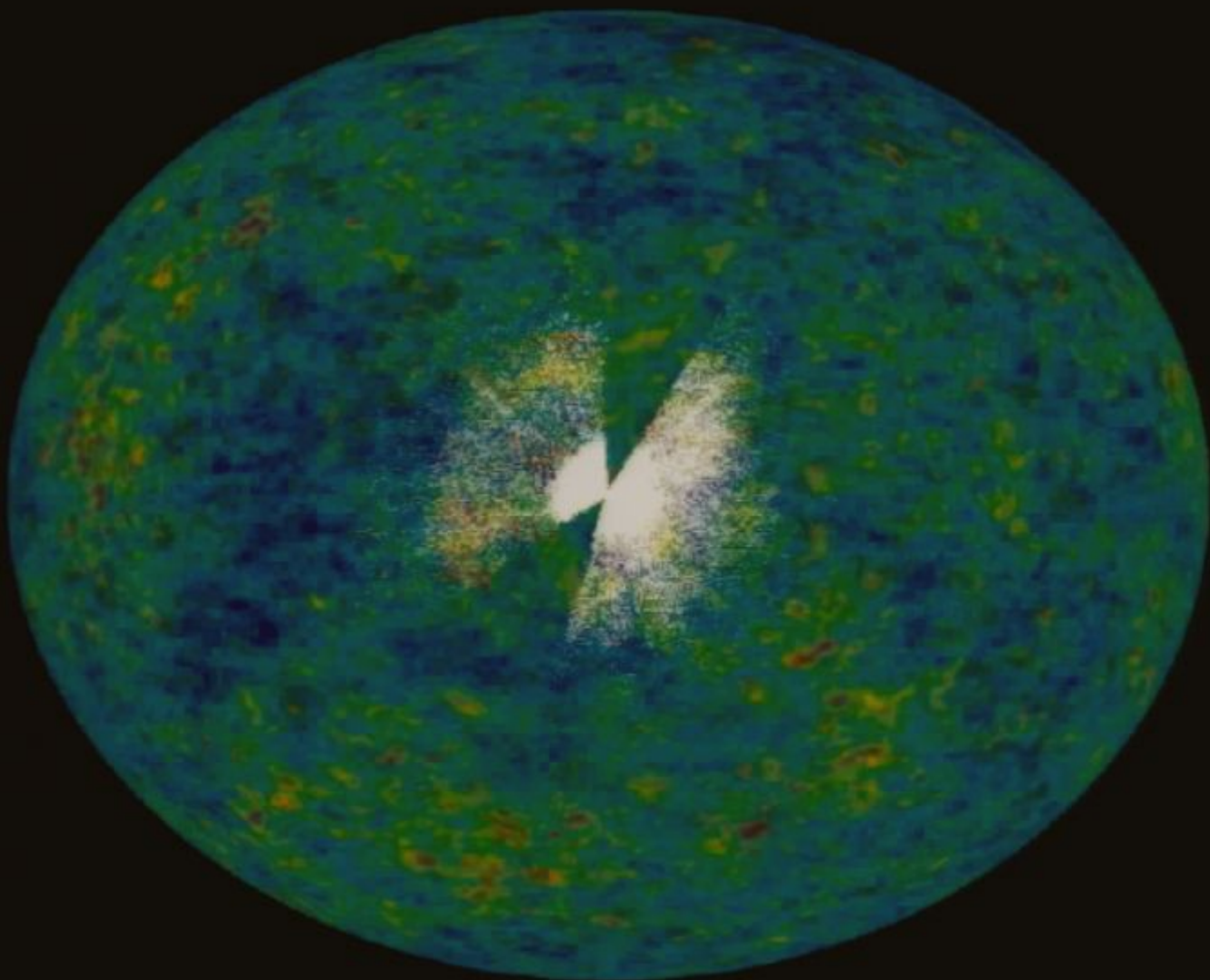
Mapping_Universe.mov



Mapping_Universe.mov



0.0



Brief History of our Universe

Fluctuation generator

Fluctuation amplifier

INFLATION

CMB
last scattering

fraction
of a second

379,000
years

first
stars

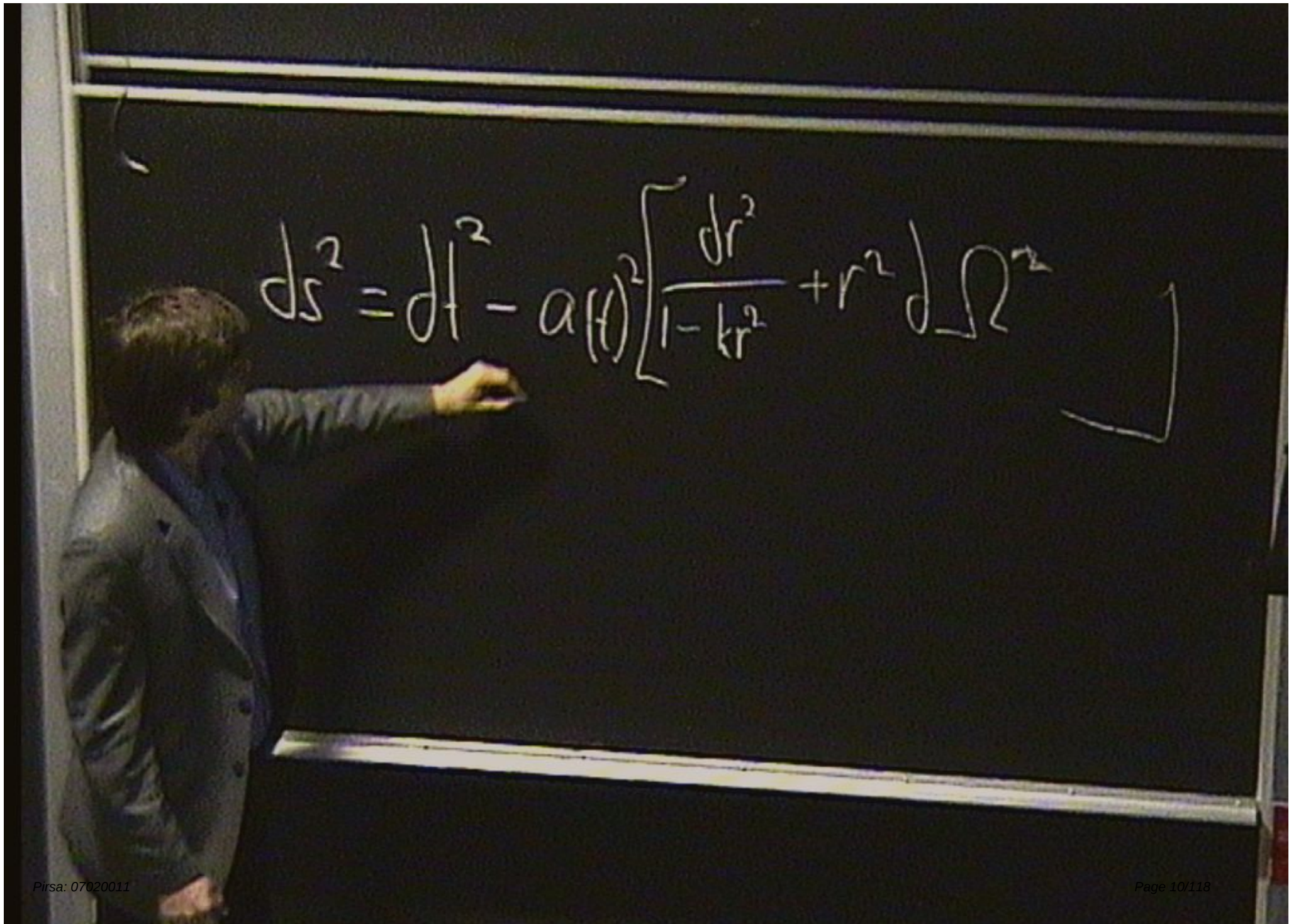
present
day

Hot
Dense
Smooth

Cool
Rarefied
Clumpy

400
~~~200~~ million  
years

13.7 billion  
years

A person is standing on the left side of a large blackboard, pointing with their right hand towards the equation written on it. The equation is a metric tensor for a Schwarzschild spacetime. The blackboard is dark, and the equation is written in white chalk. The person is wearing a dark jacket and has their back to the camera.
$$ds^2 = dt^2 - a(t)^2 \left[ \frac{dr^2}{1 - kr^2} + r^2 d\Omega^2 \right]$$

$$ds^2 = dt^2 - a(t)^2 \left[ \frac{dr^2}{1 - kr^2} + r^2 d\Omega^2 \right]$$

Fluctuation generator

To 0th order:

Fluctuation amplifier

INFLATION

CMB  
last scattering

fraction  
of a second

386  
~~379,000~~  
years

first  
stars

present  
day

Hot  
Dense  
Smooth

$H(z)$

Cool  
Rarefied  
Clumpy

400  
~~~200~~  
million
years

13.7 billion
years

Fluctuation generator

To 1st order:

Fluctuation amplifier

INFLATION

CMB
last scattering

fraction
of a second

386
~~379,000~~
years

first
stars

present
day

Hot
Dense
Smooth

$H(z)$

$P(k,z)$

Cool
Rarefied
Clumpy

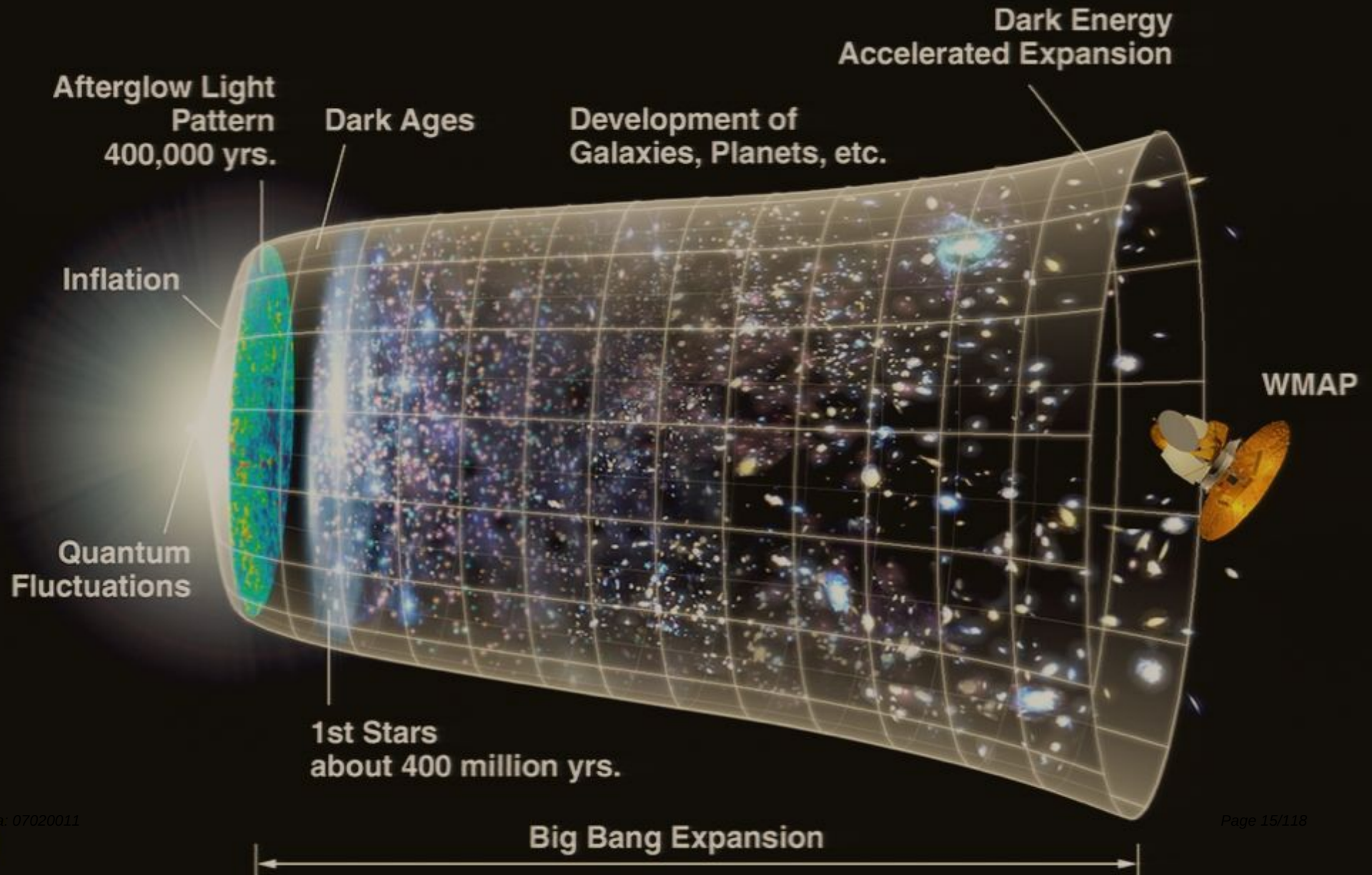
400
~~~200~~ million  
years

13.7 billion  
years

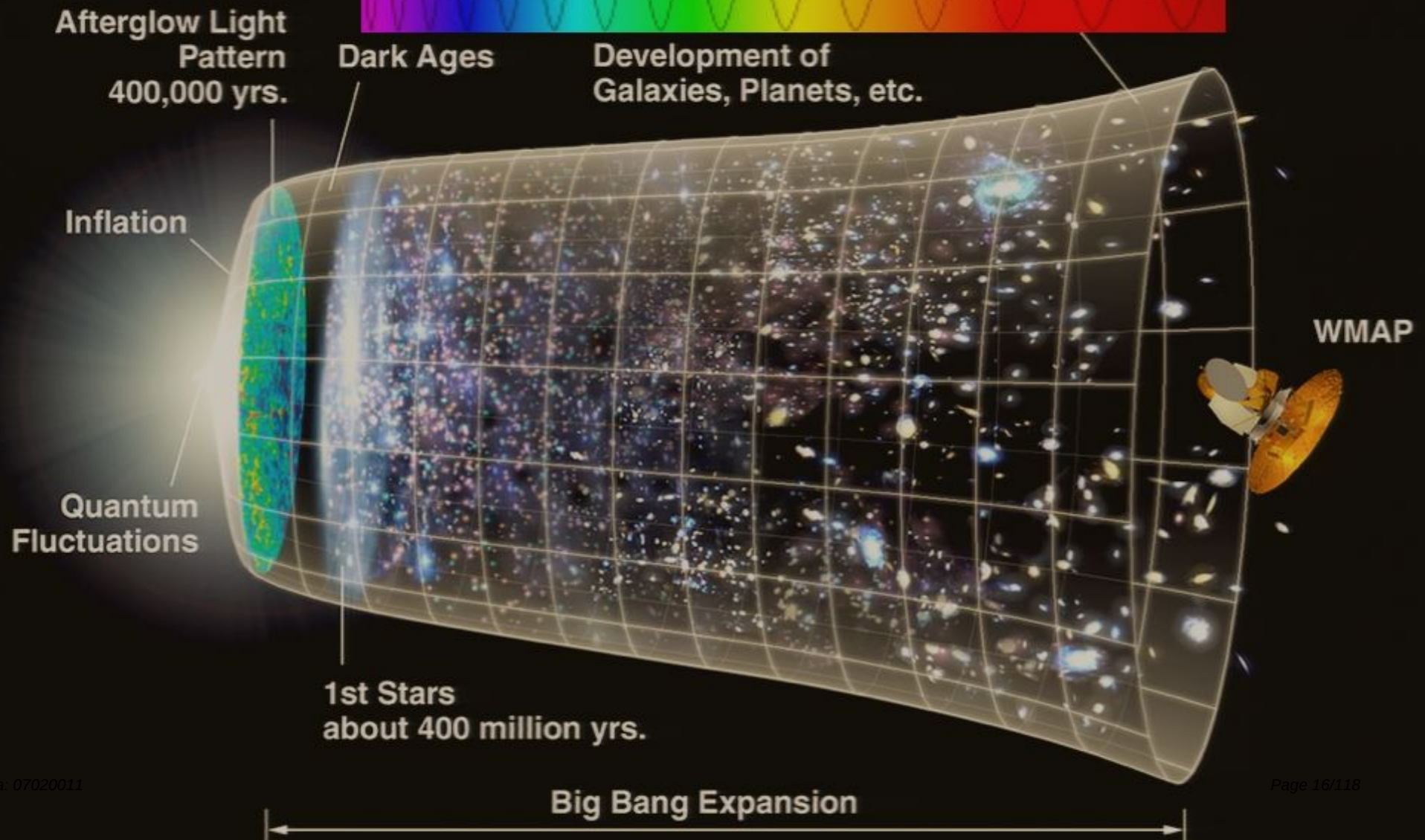
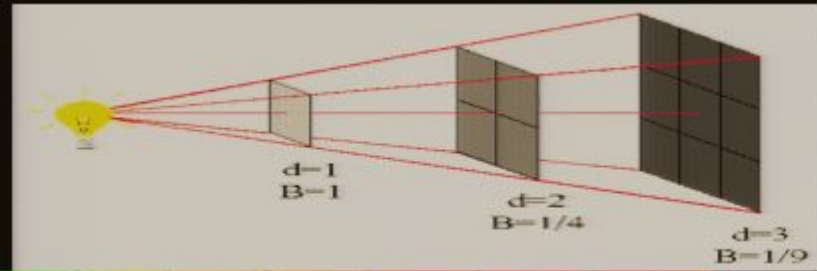
0th order:

# Measuring Expansion:

$$a(t) \Leftrightarrow H(z)$$



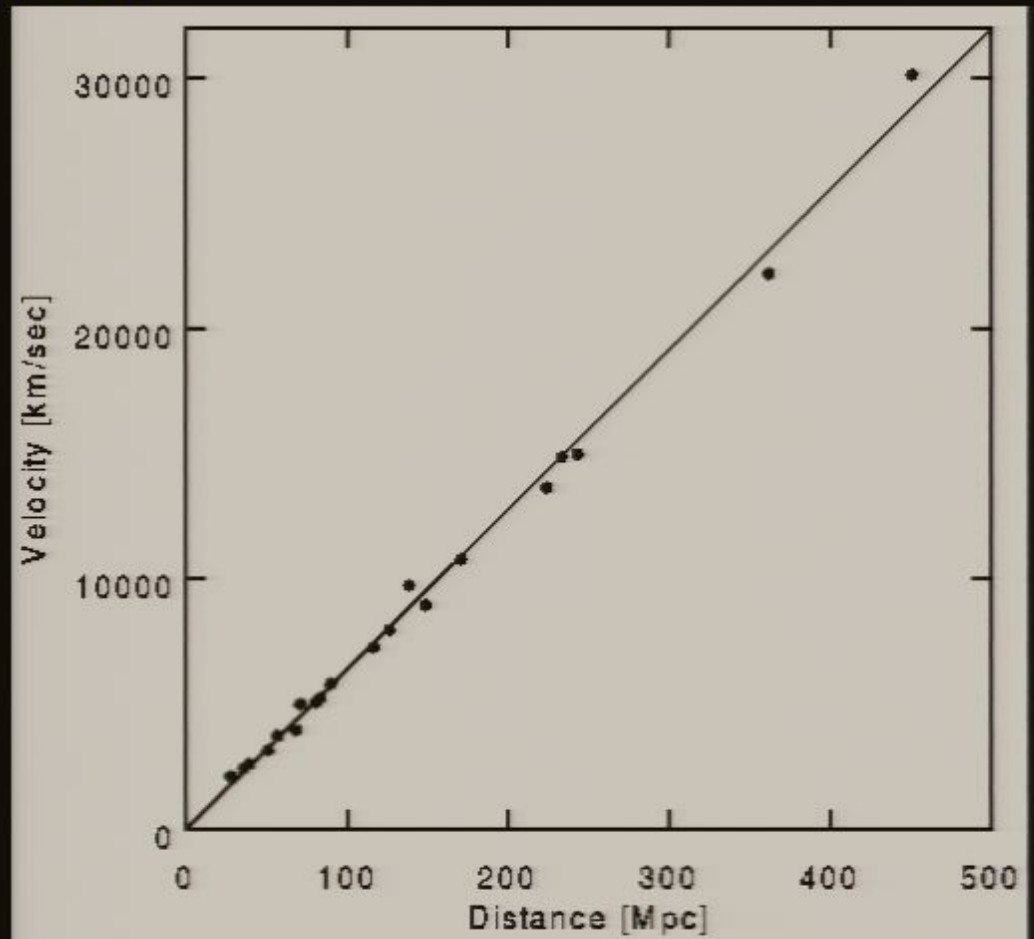
Distant light is {  
-dimmed →  
-redshifted ↓



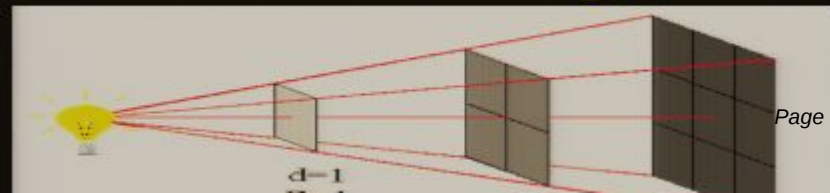
Distant light is {  
-dimmed  
-redshifted



Redshift



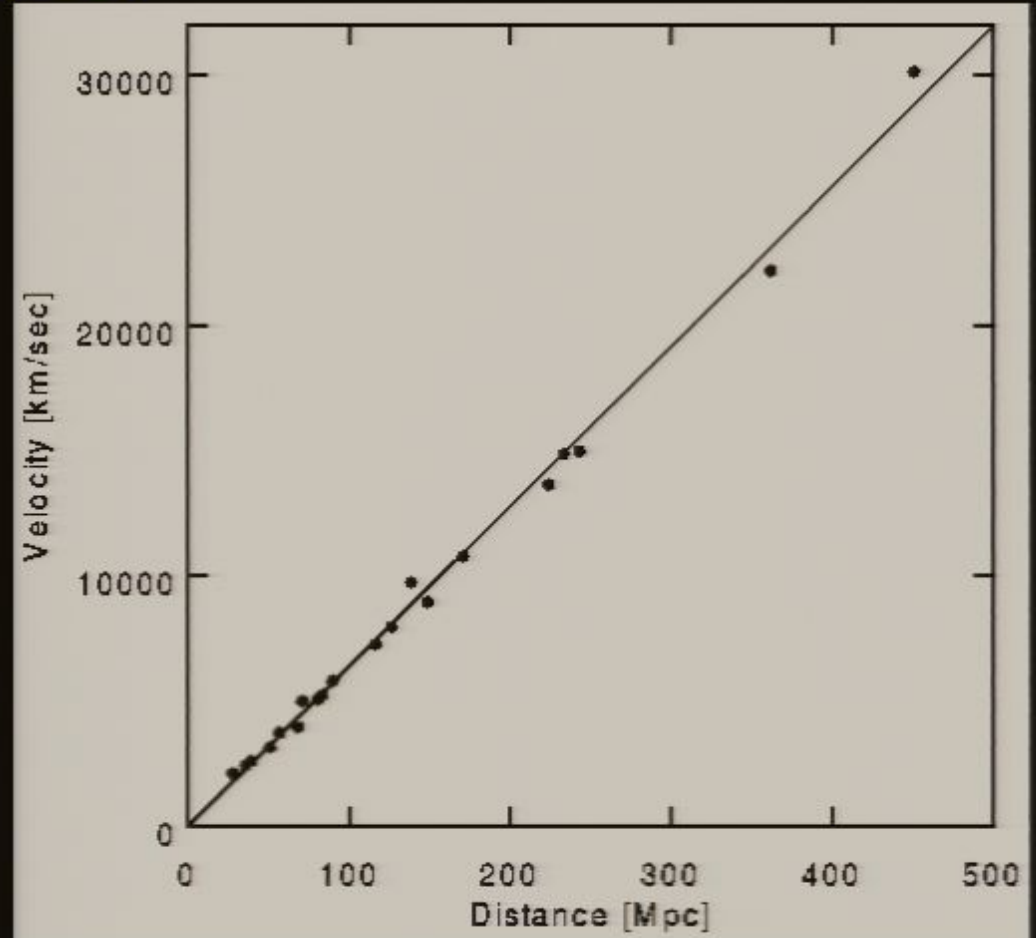
Dimming



Distant light is {  
-dimmed  
-redshifted

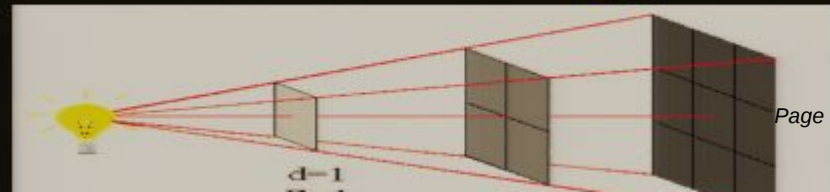


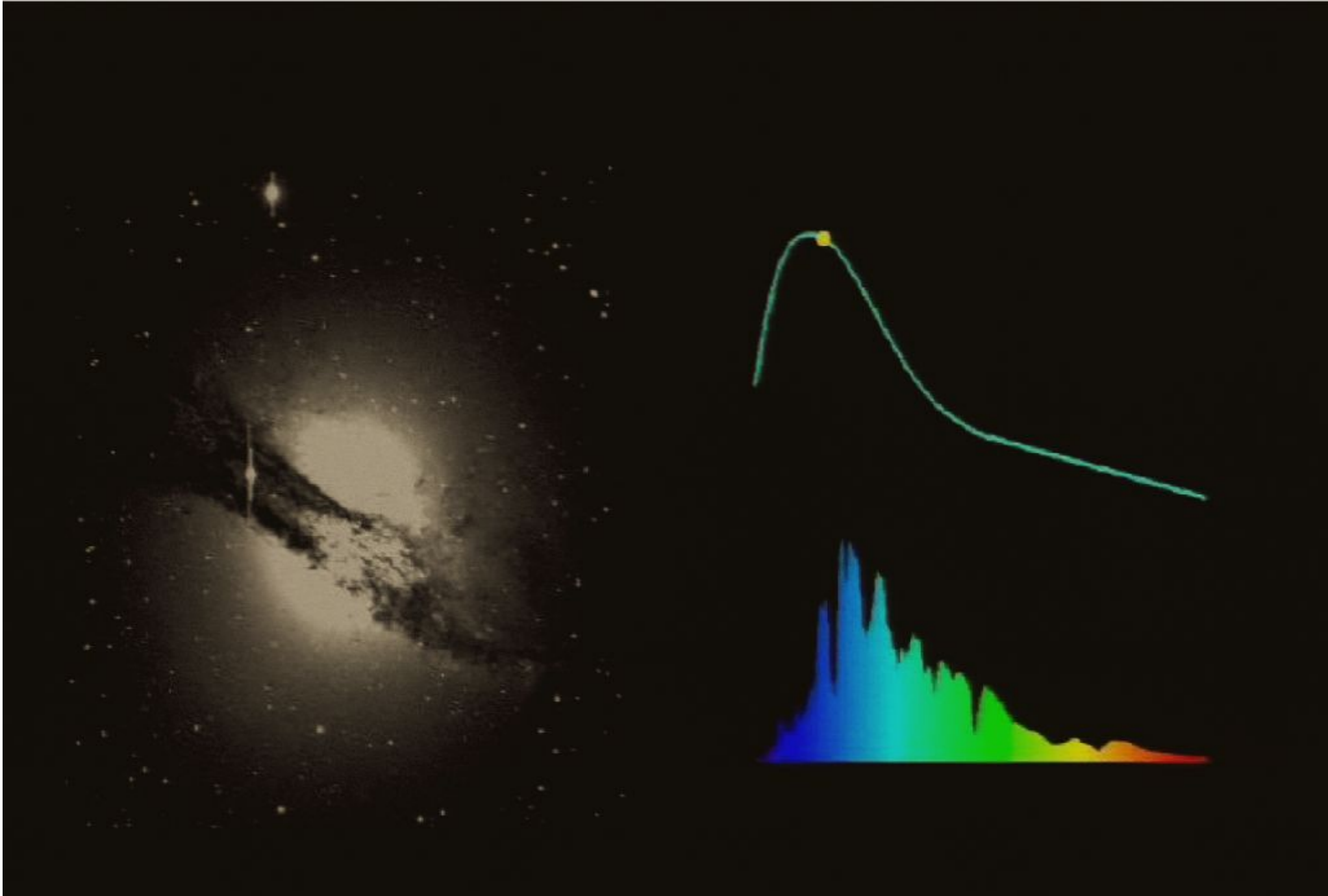
Redshift



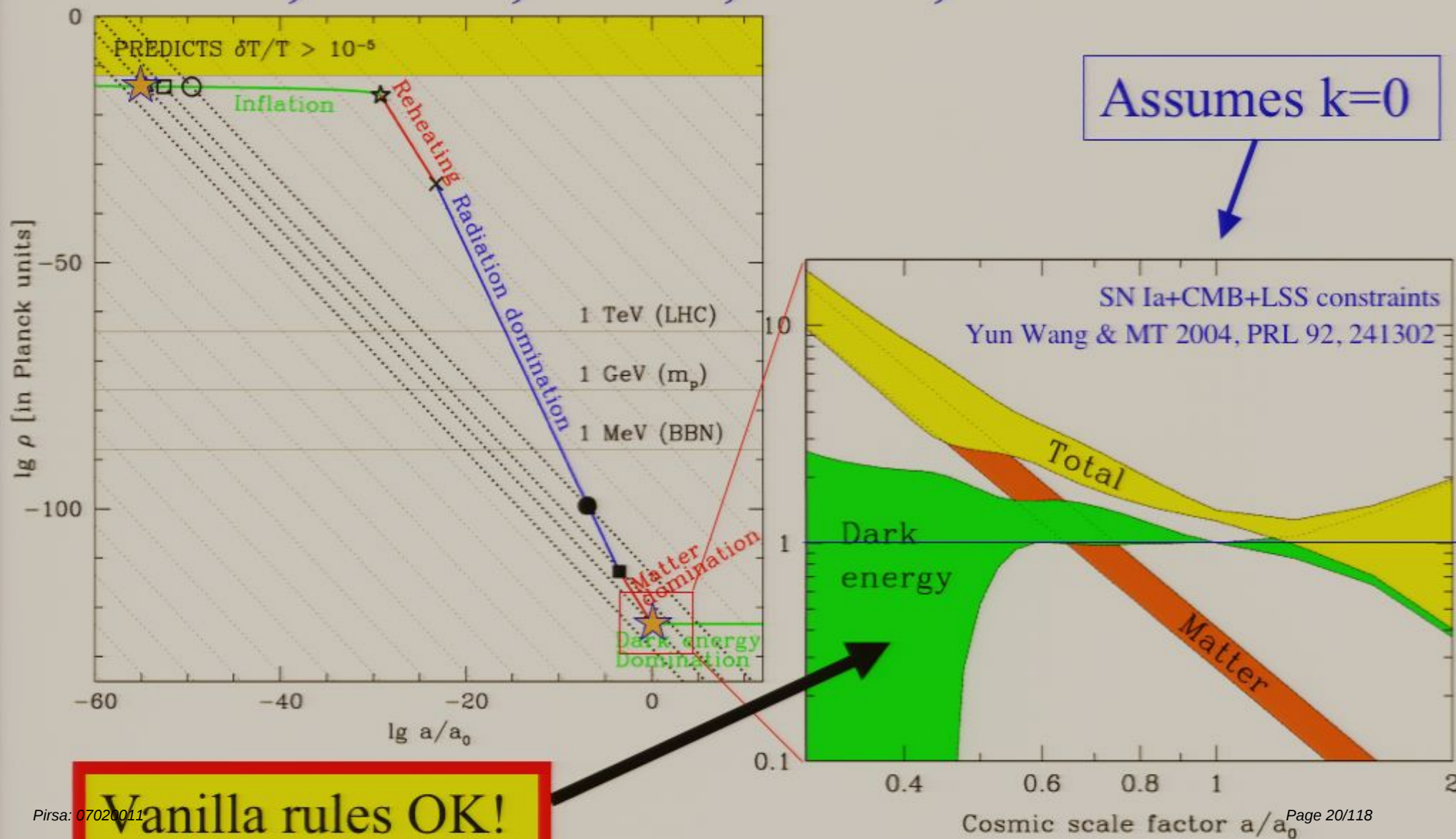
Dimming

Standard candles,  
rulers or clocks

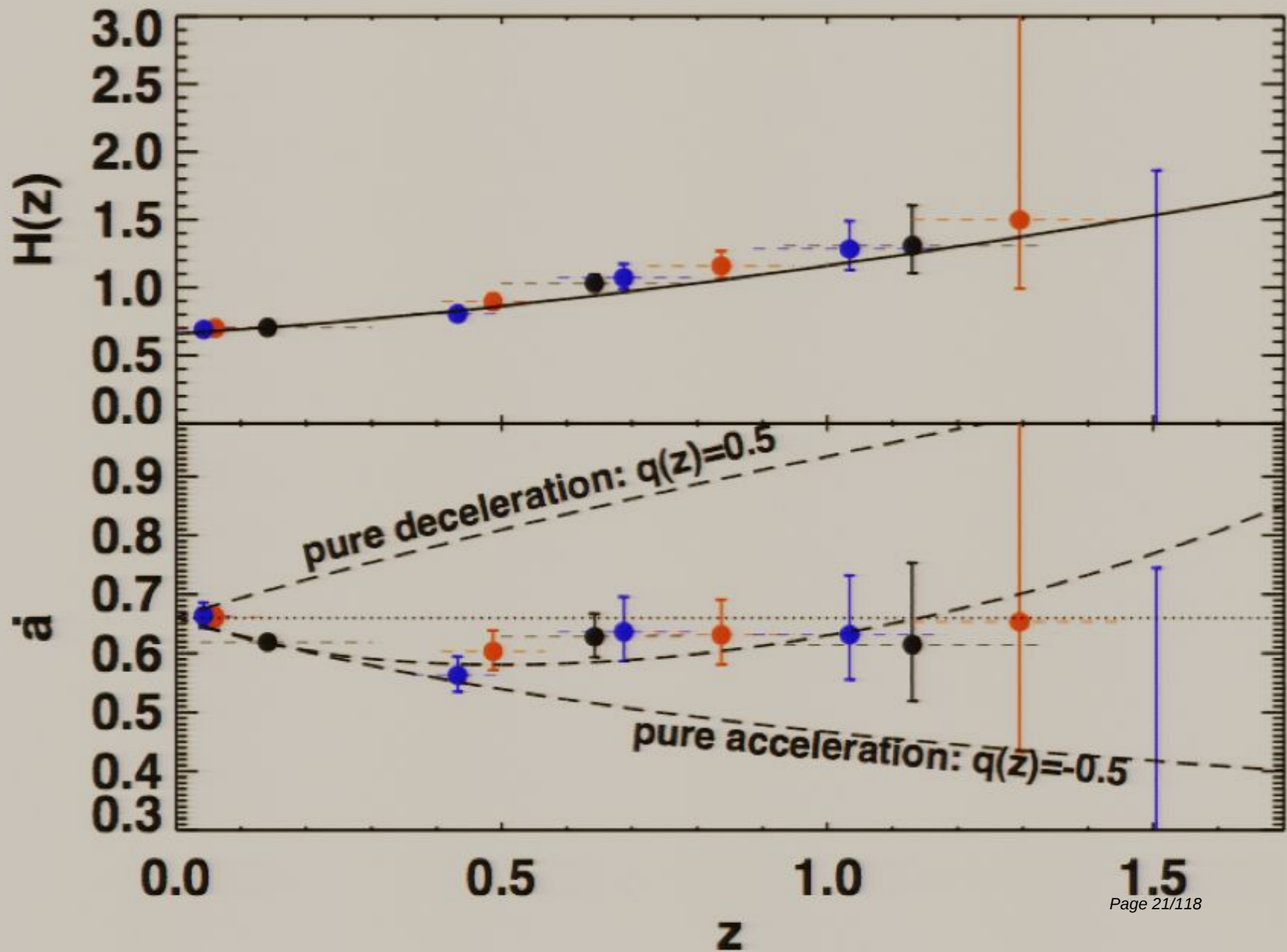




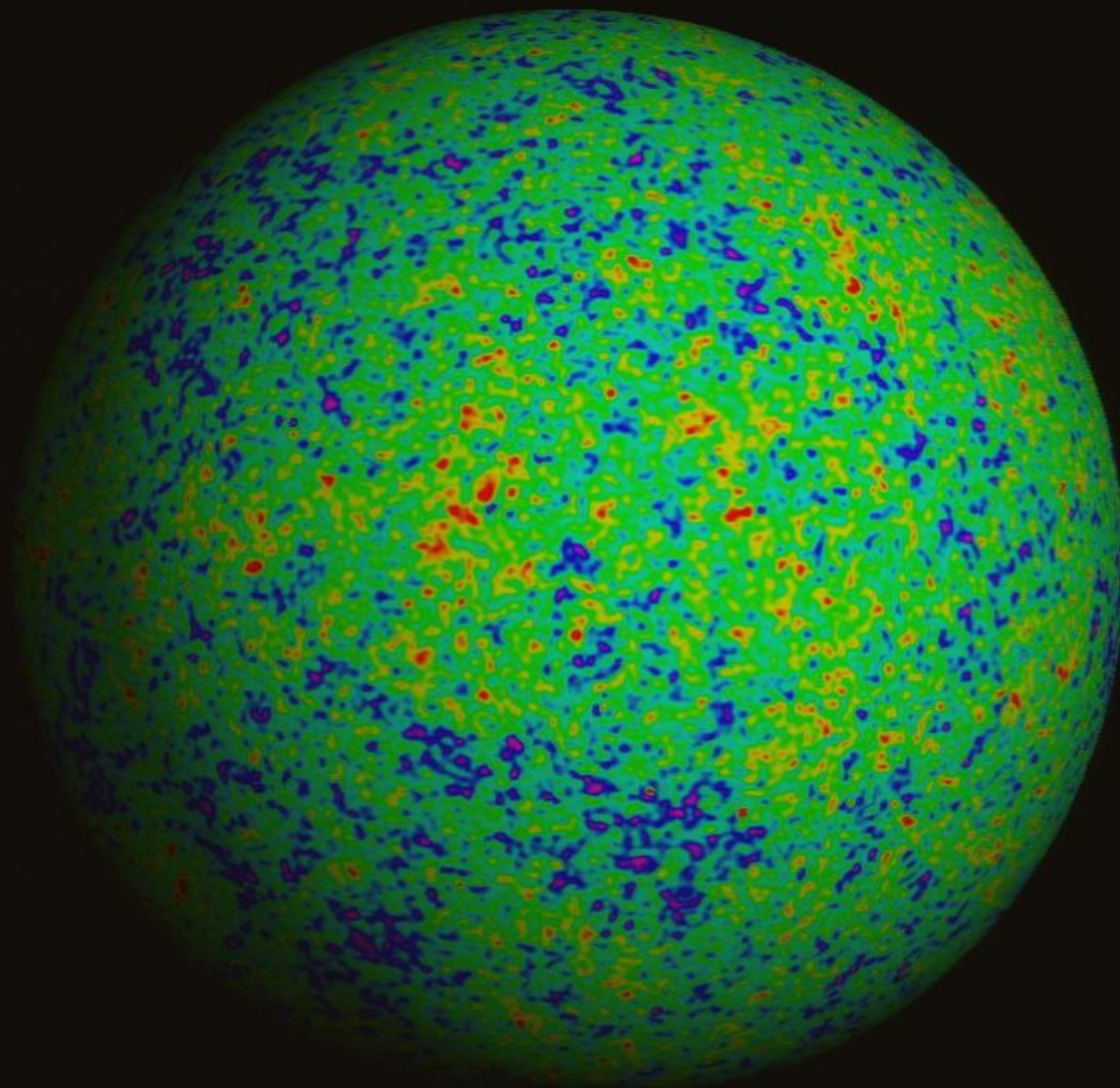
# What we've learned about $H(z)$ from SN Ia, CMB, BAO, BBN, etc:



Riess et al, astro-ph/0611572

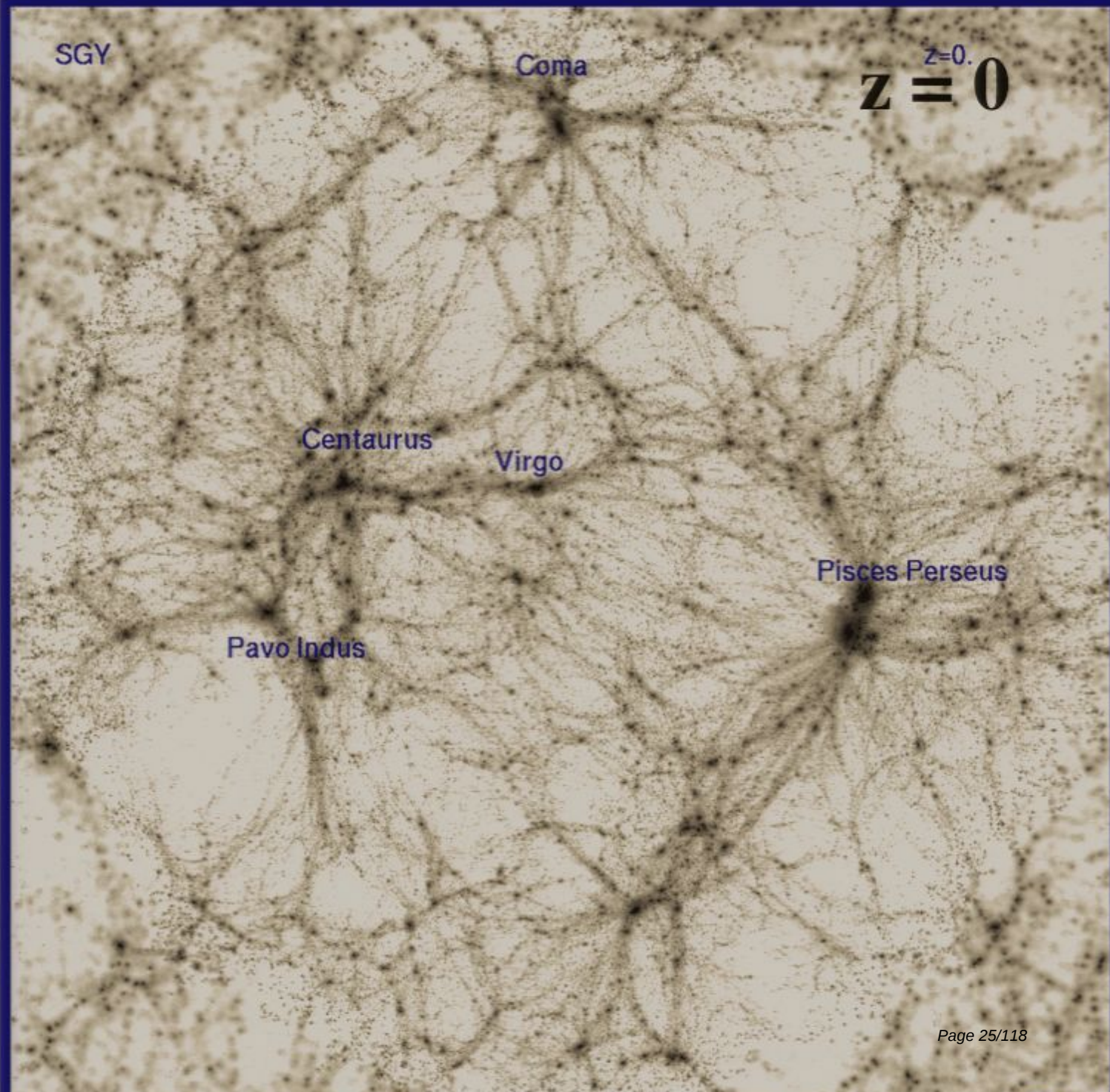


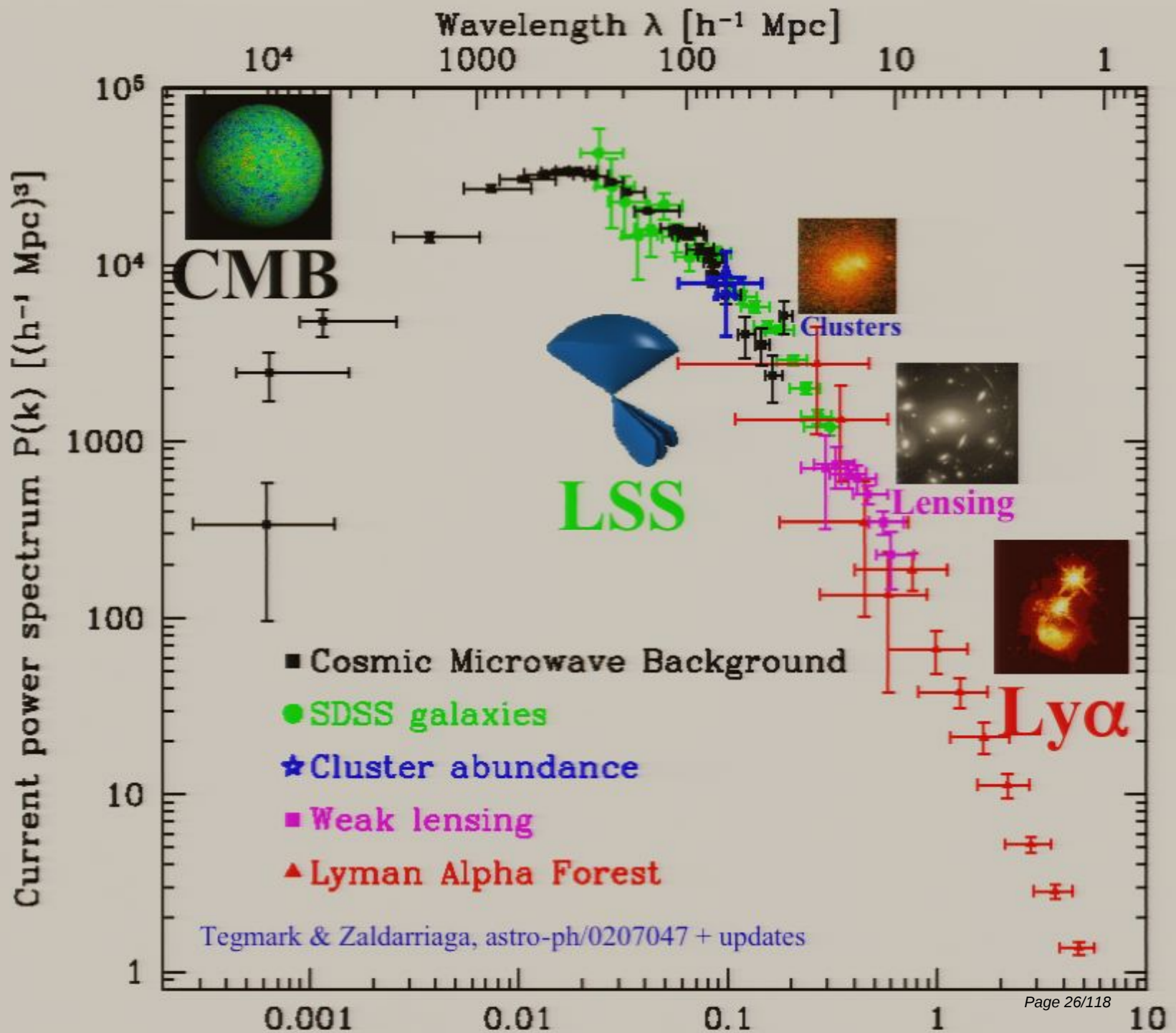
# 1st order: measuring clustering

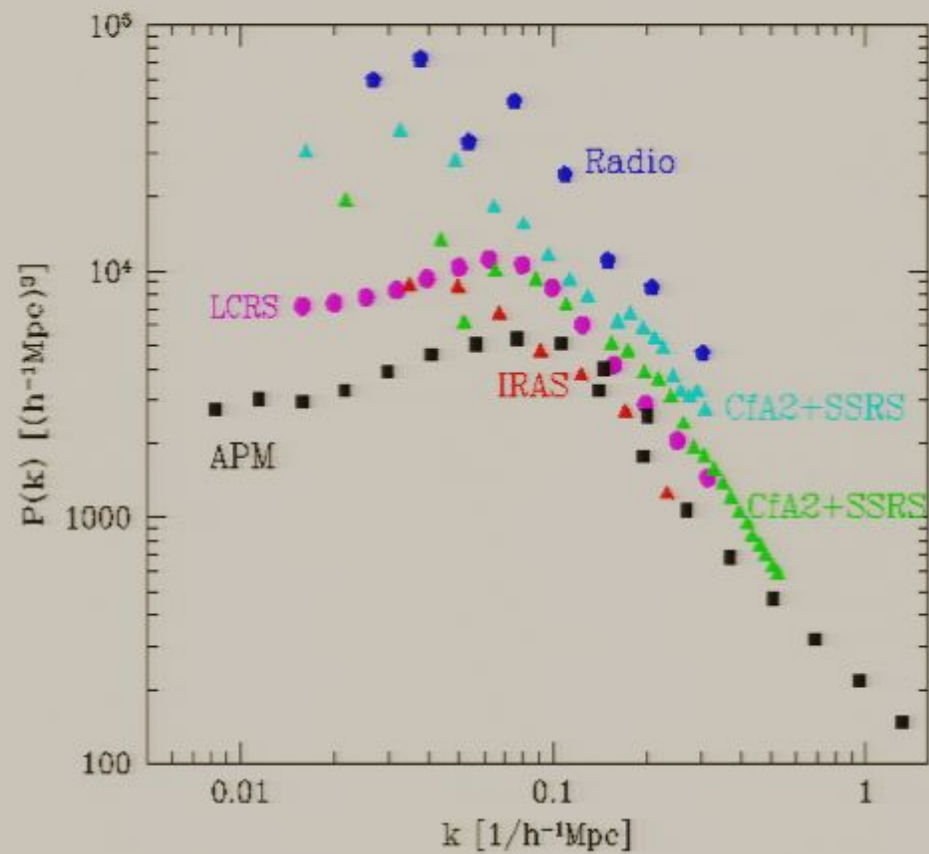


**$z = 1000$**



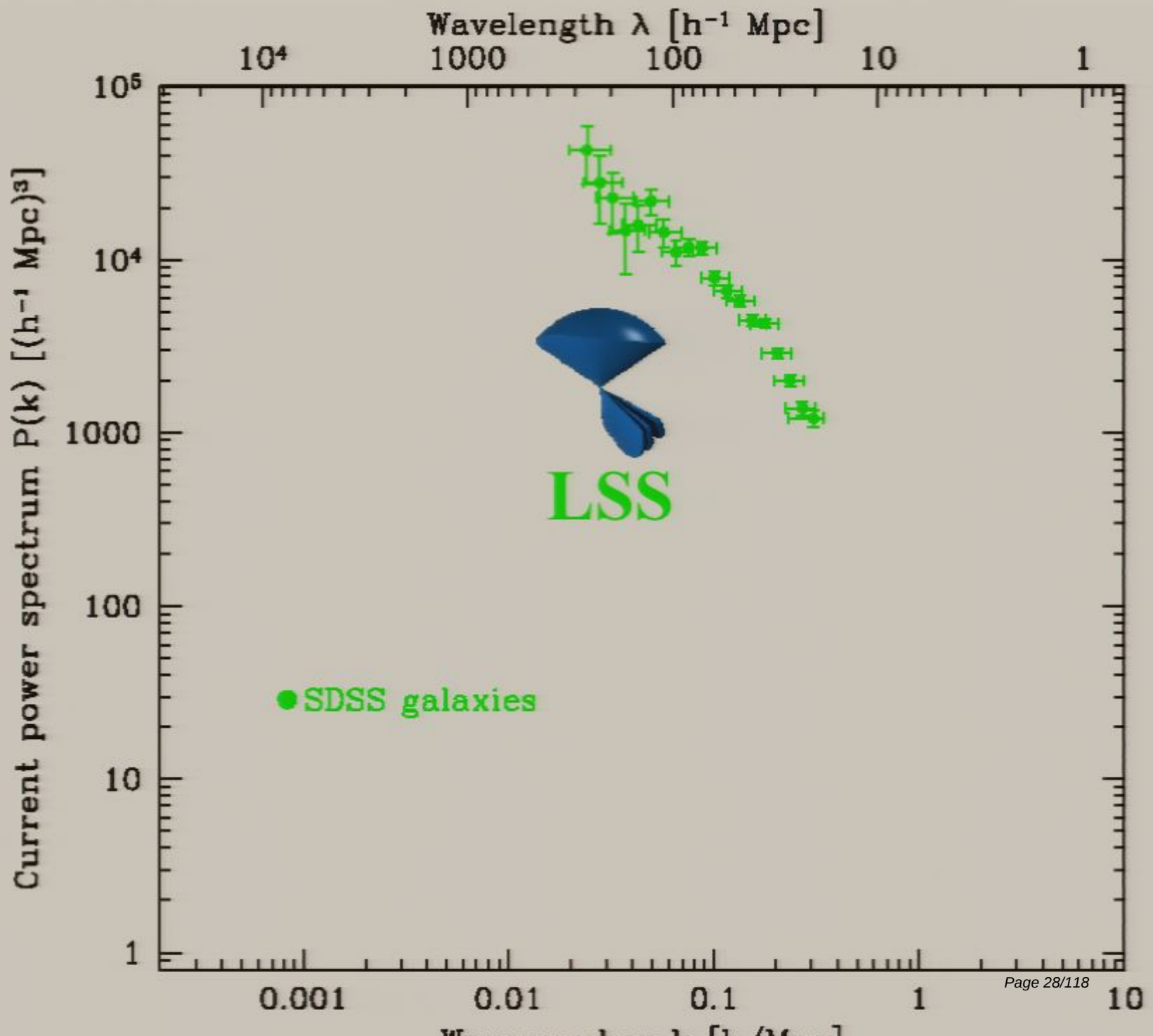


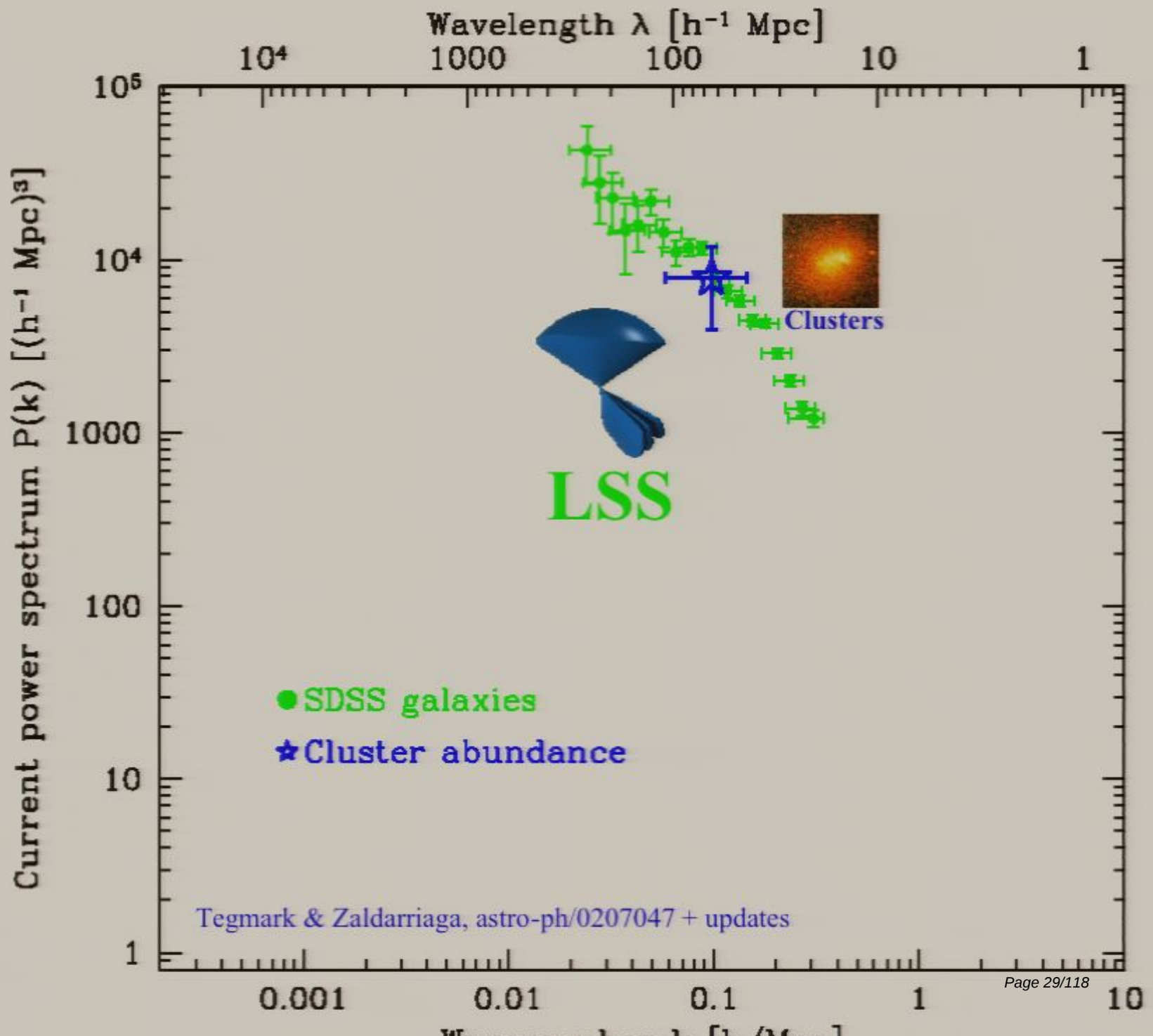


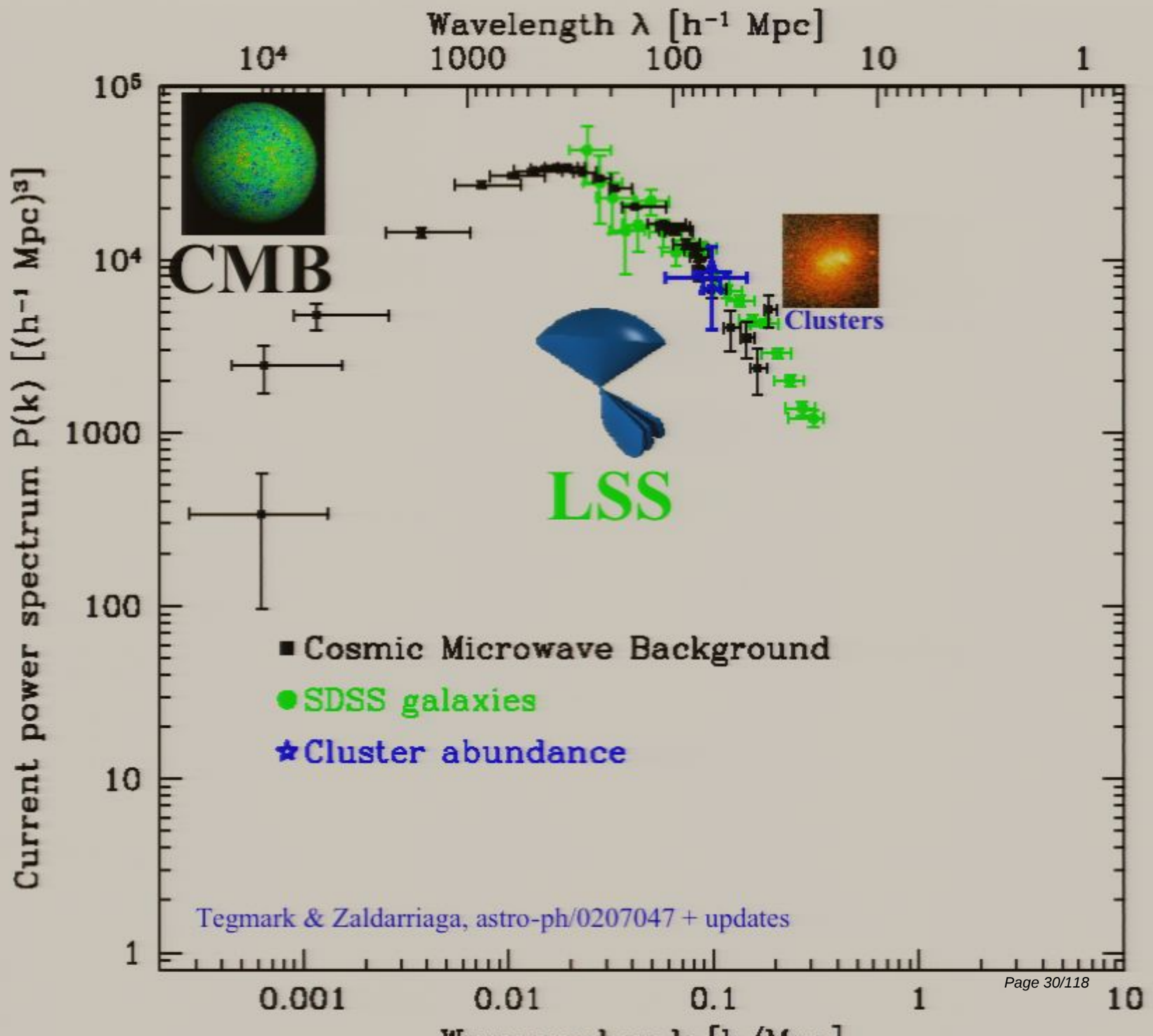


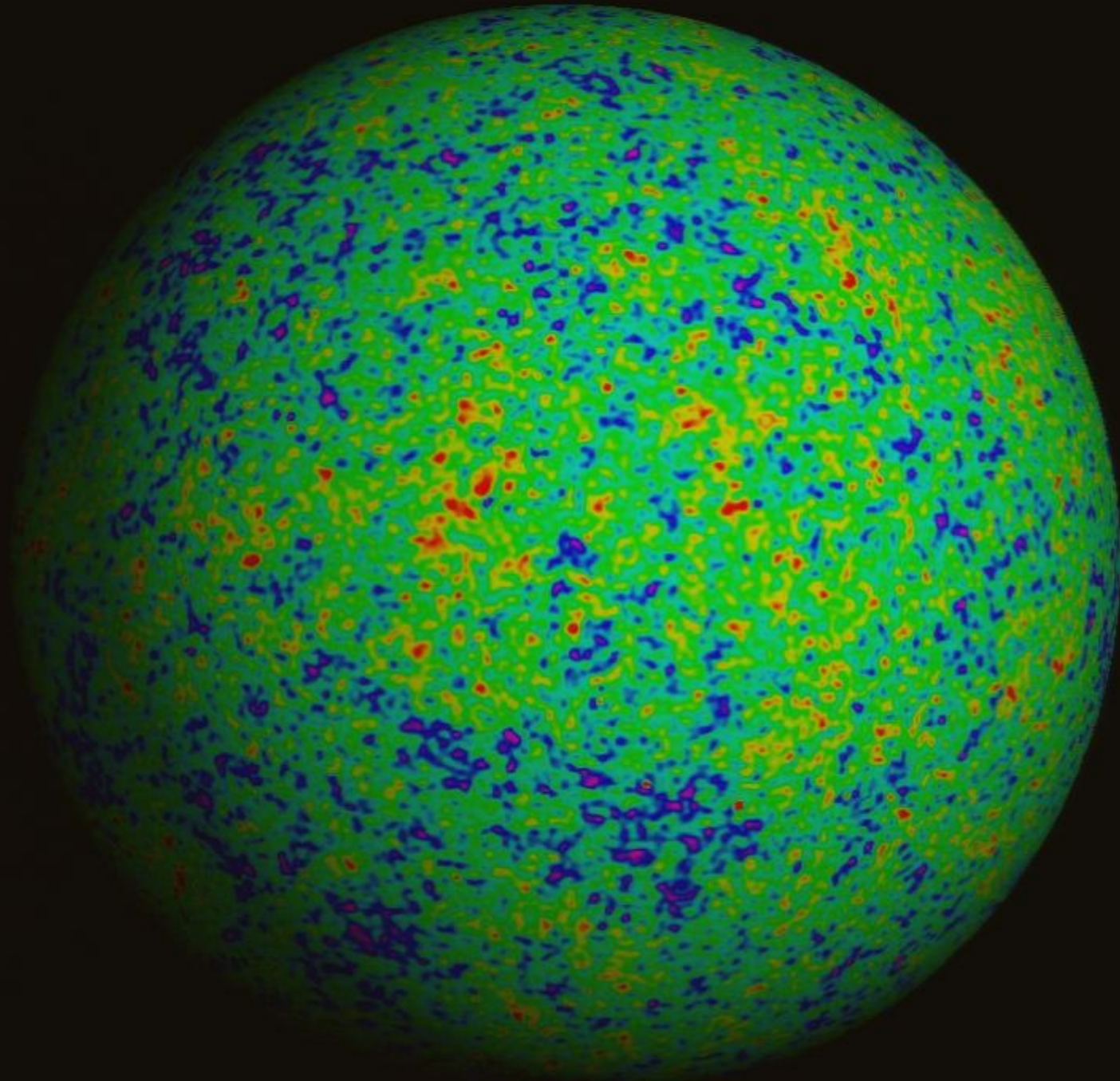
Galaxy power spectrum measurements 1999  
(Based on compilation by Michael Vogeley)

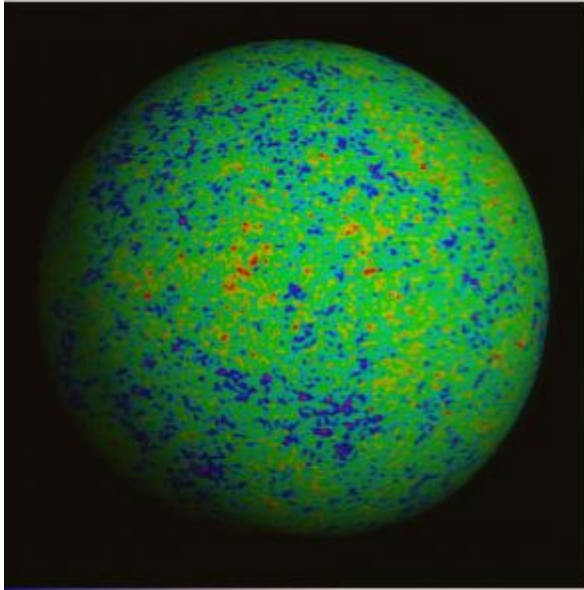




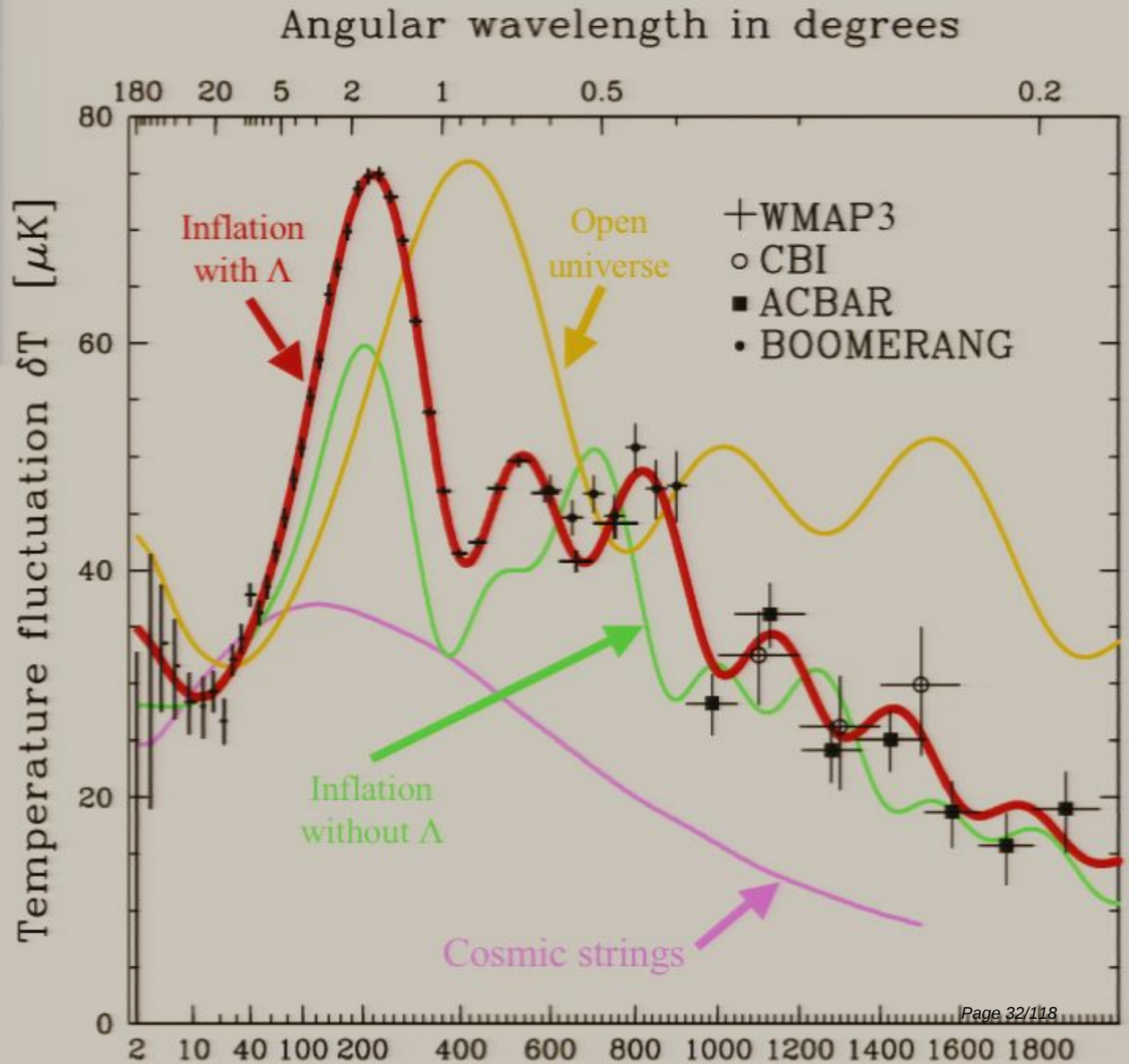


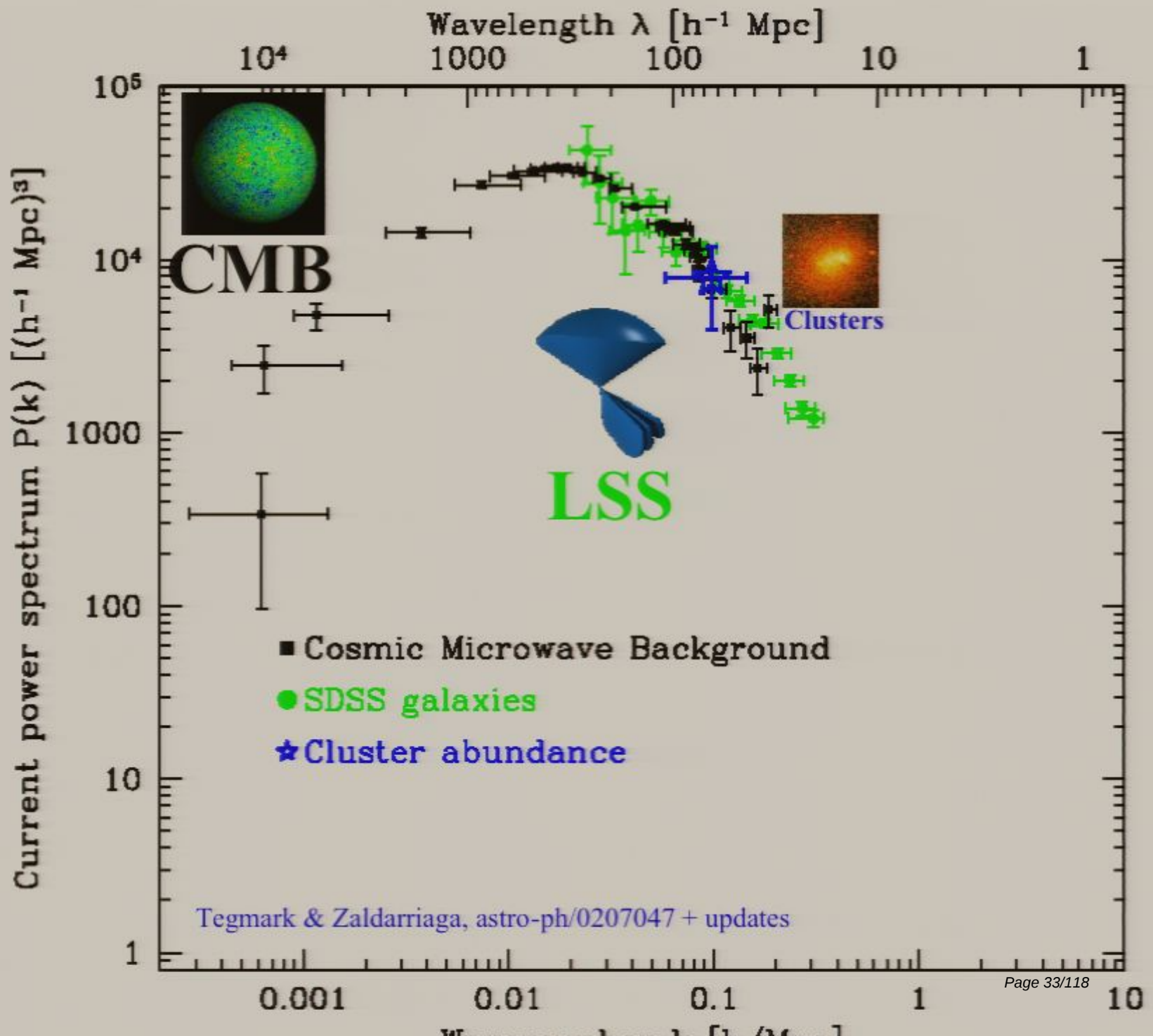


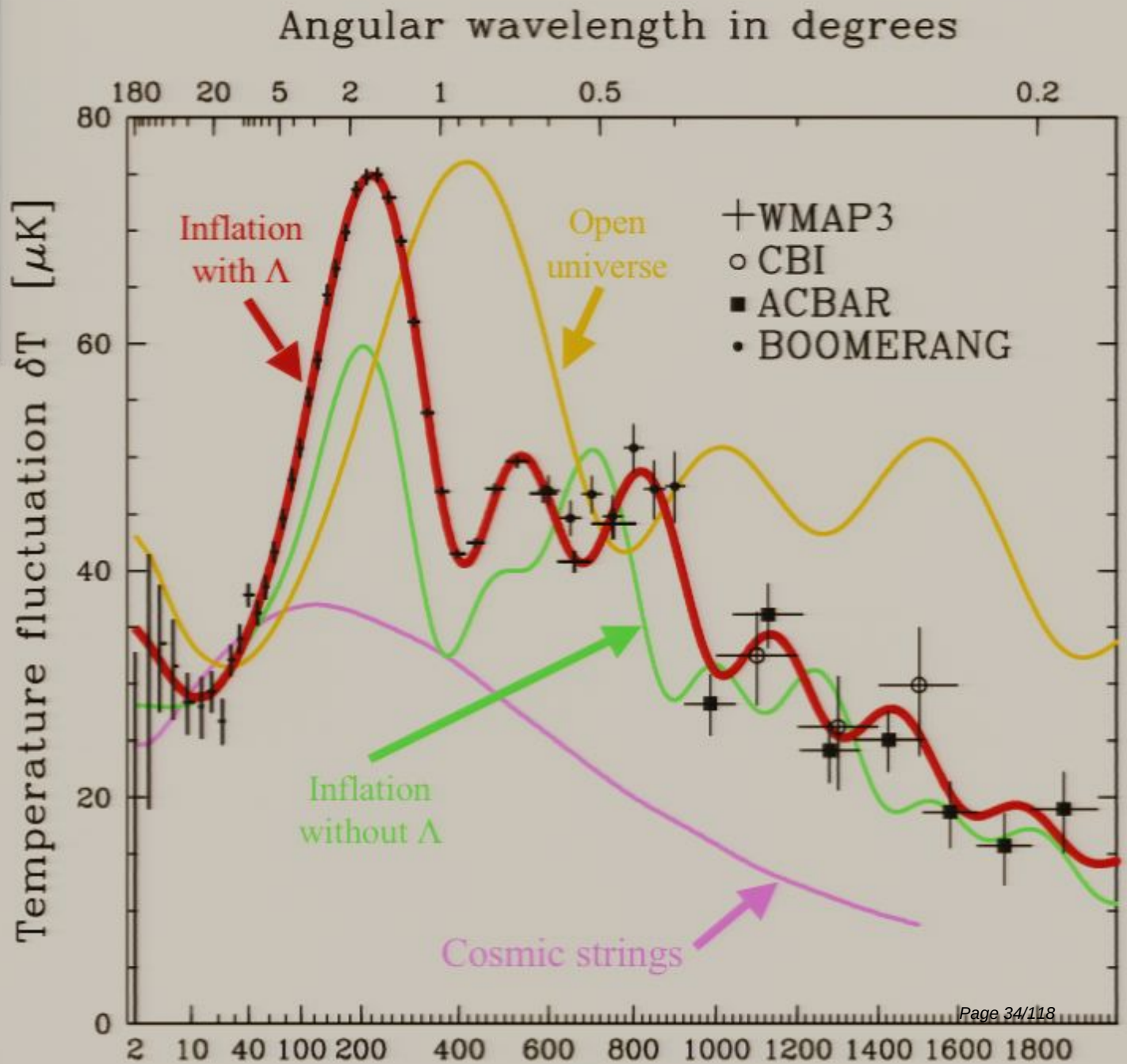
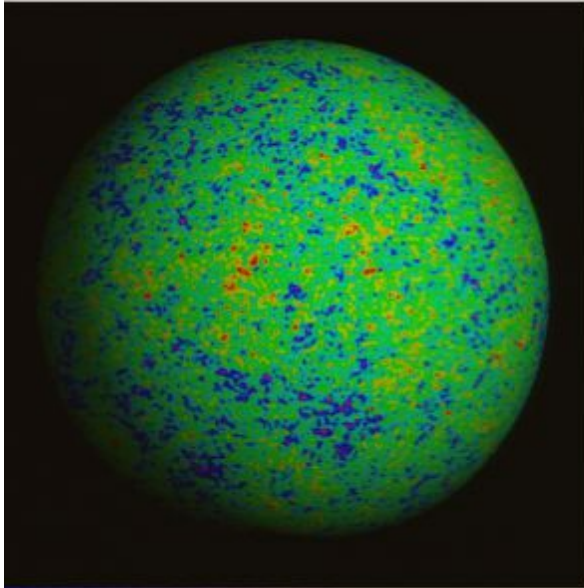




Smith & Kaiser 2005 (Science) + WMAP3

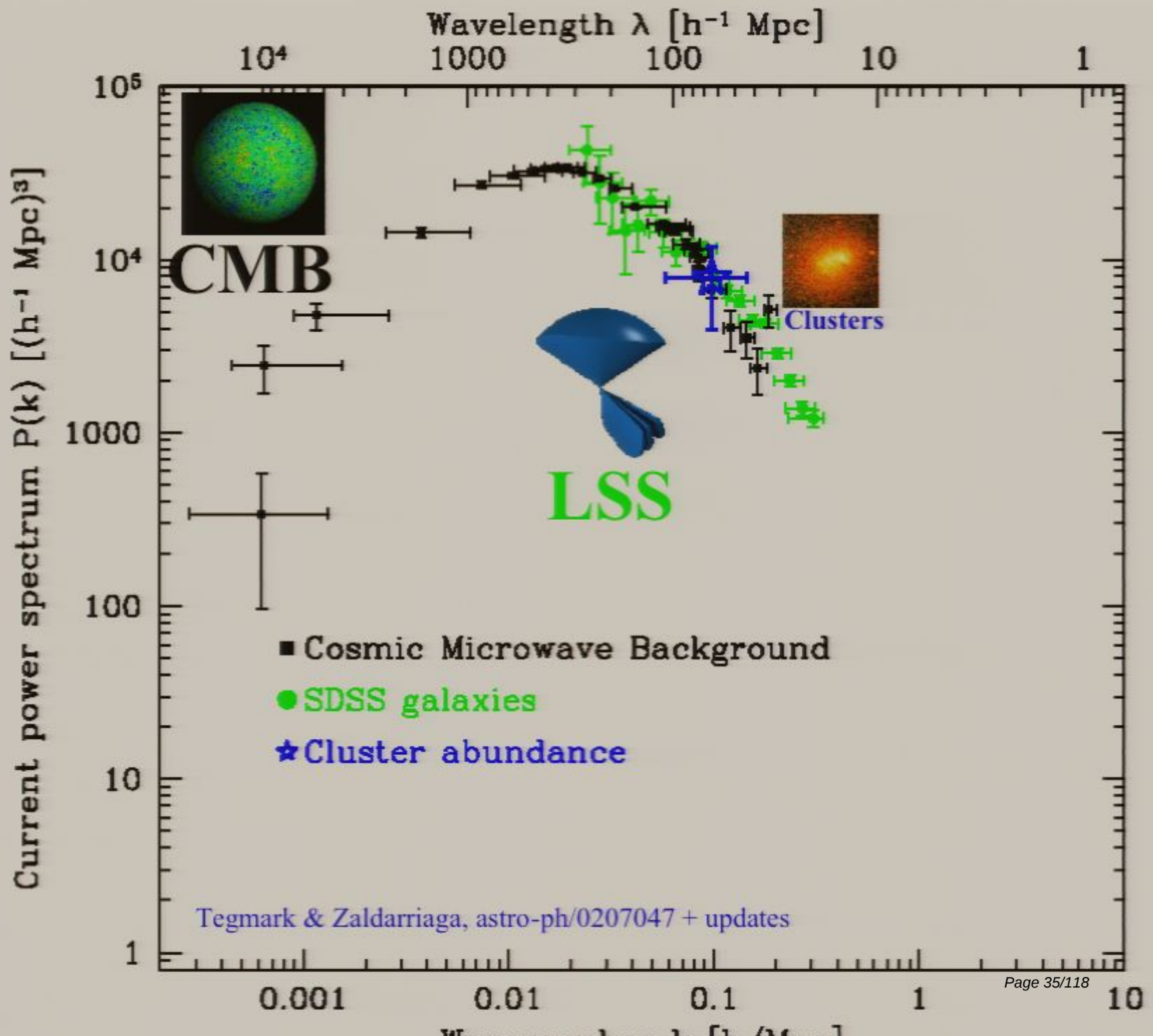


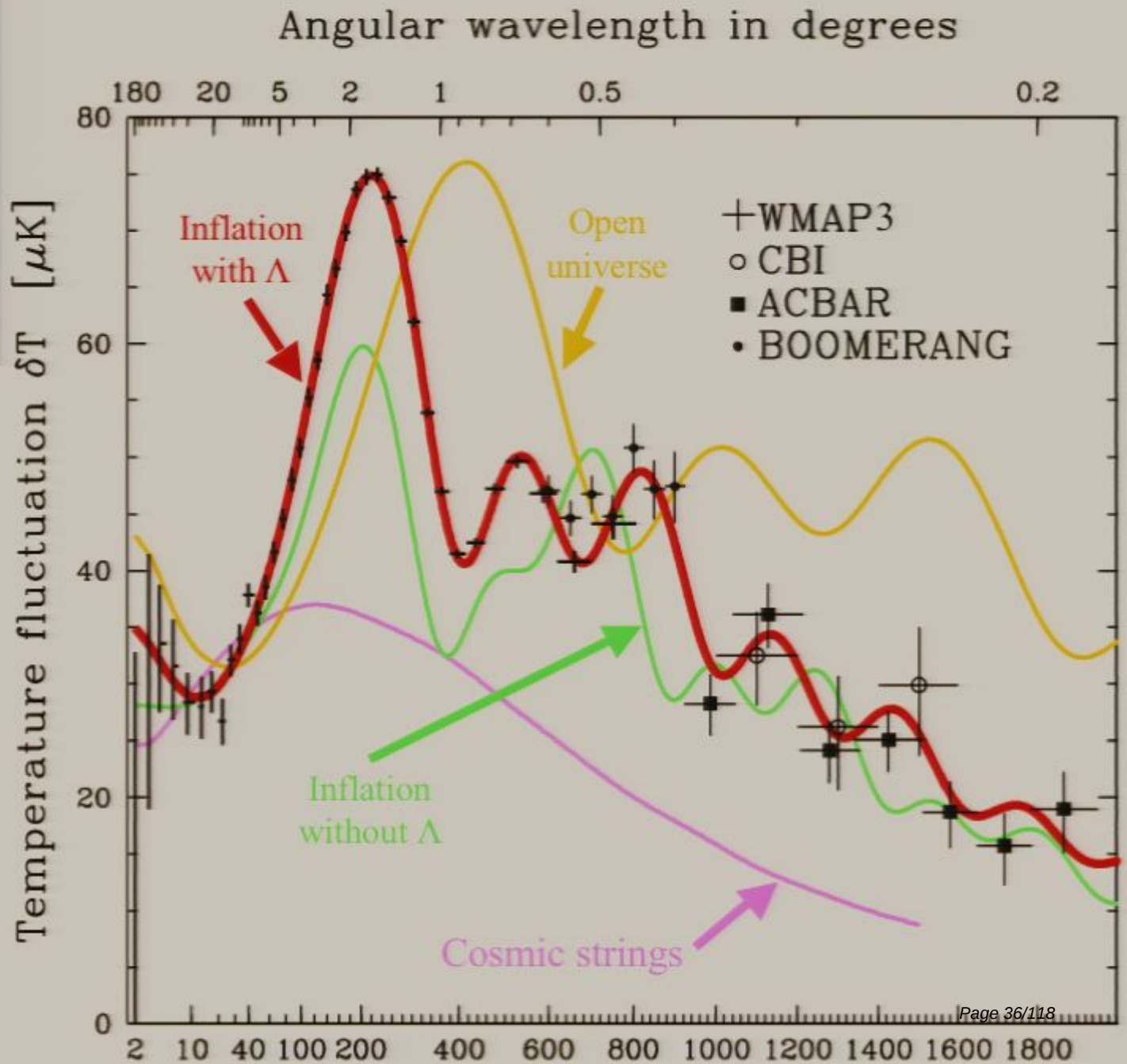
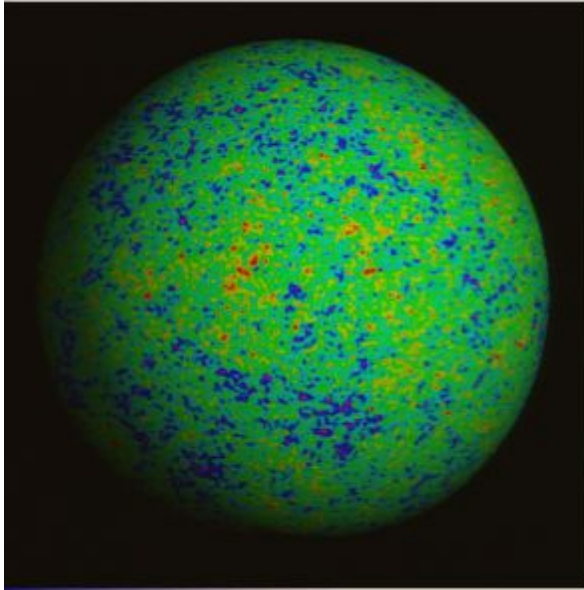




Smith & Kaiser 2005 (Science) + WMAP3

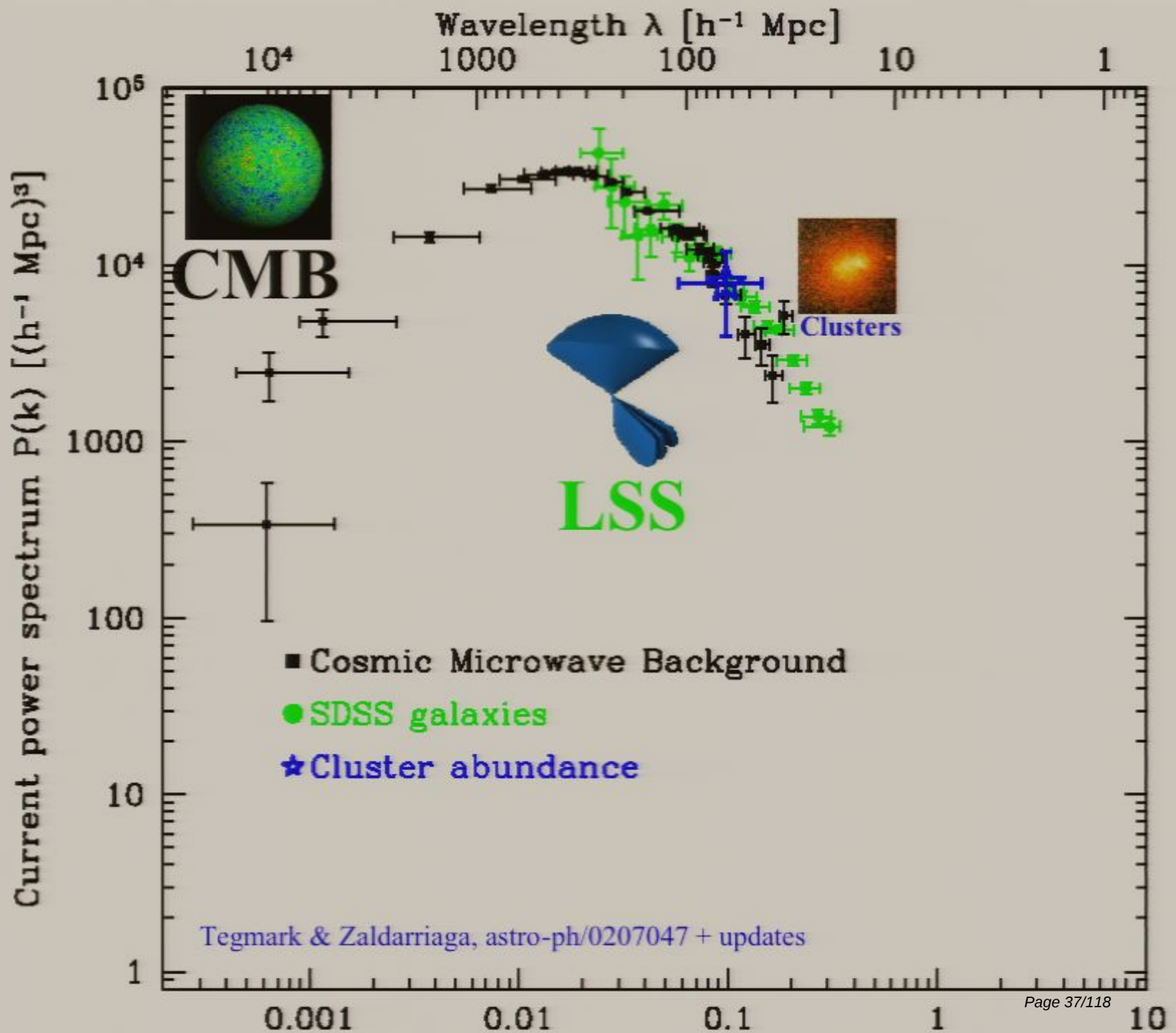


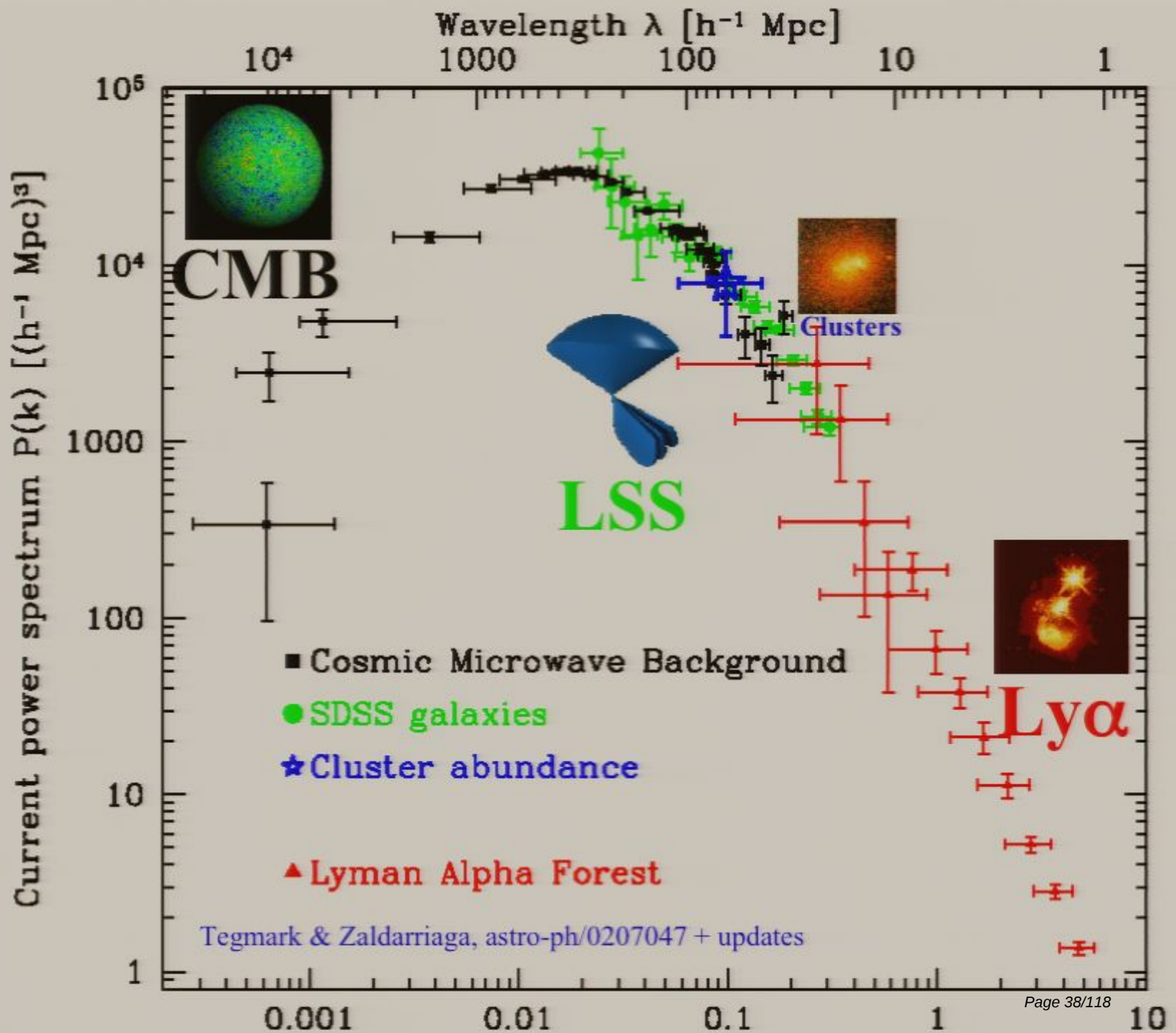


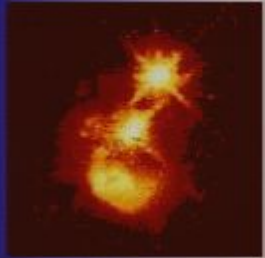


Smith & Kaiser 2005 (Science) + WMAP3









Ly $\alpha$ F



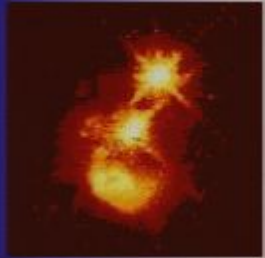
Quasar



You



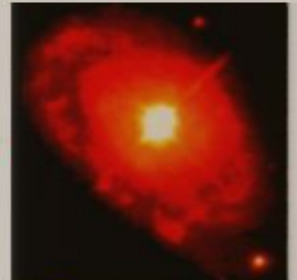
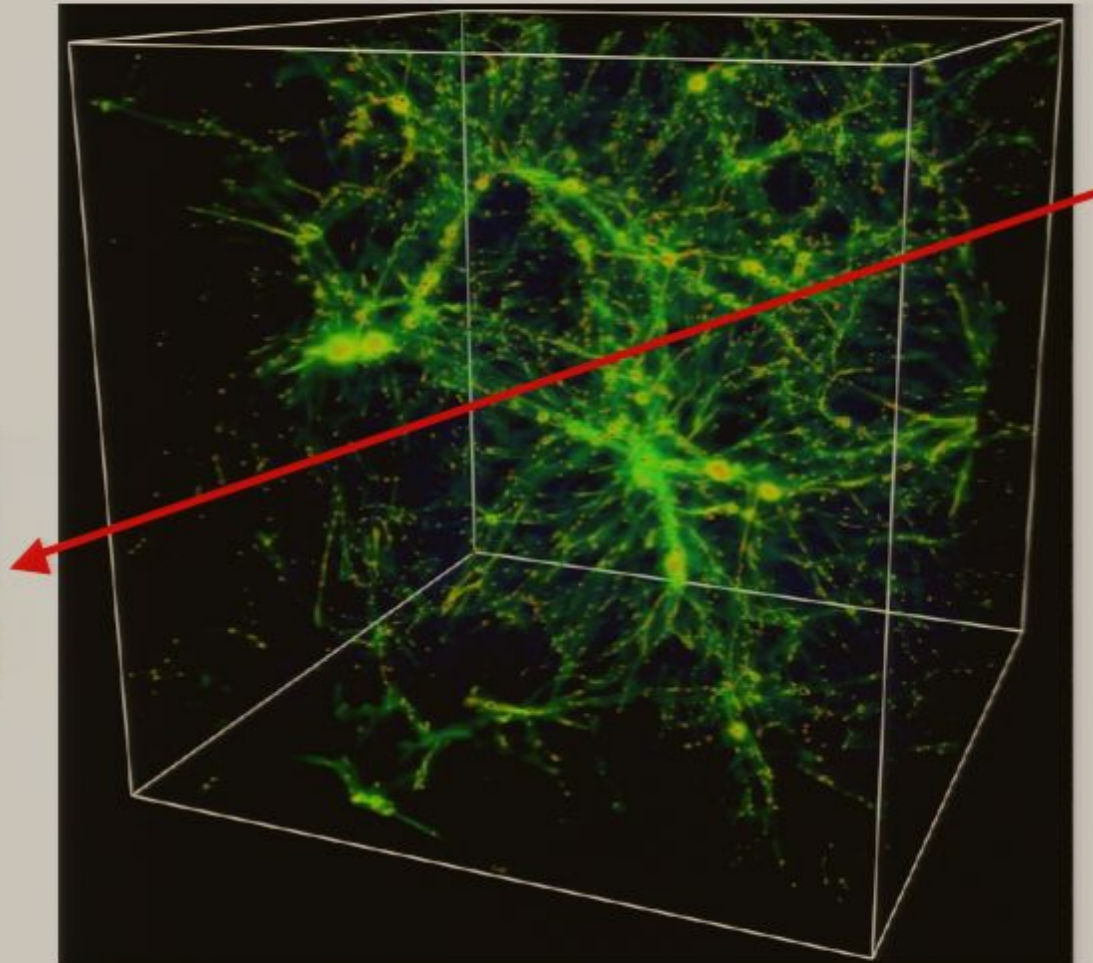
# Lyman Alpha Forest Simulation: Cen et al 2001



Ly $\alpha$ F

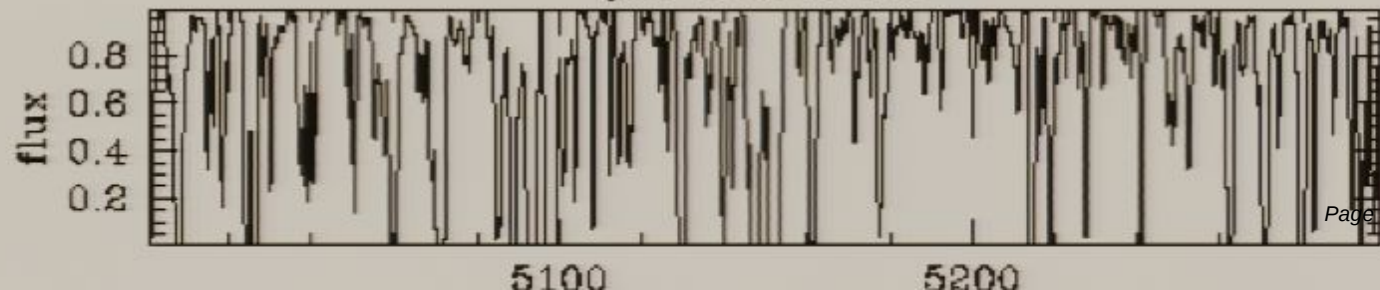


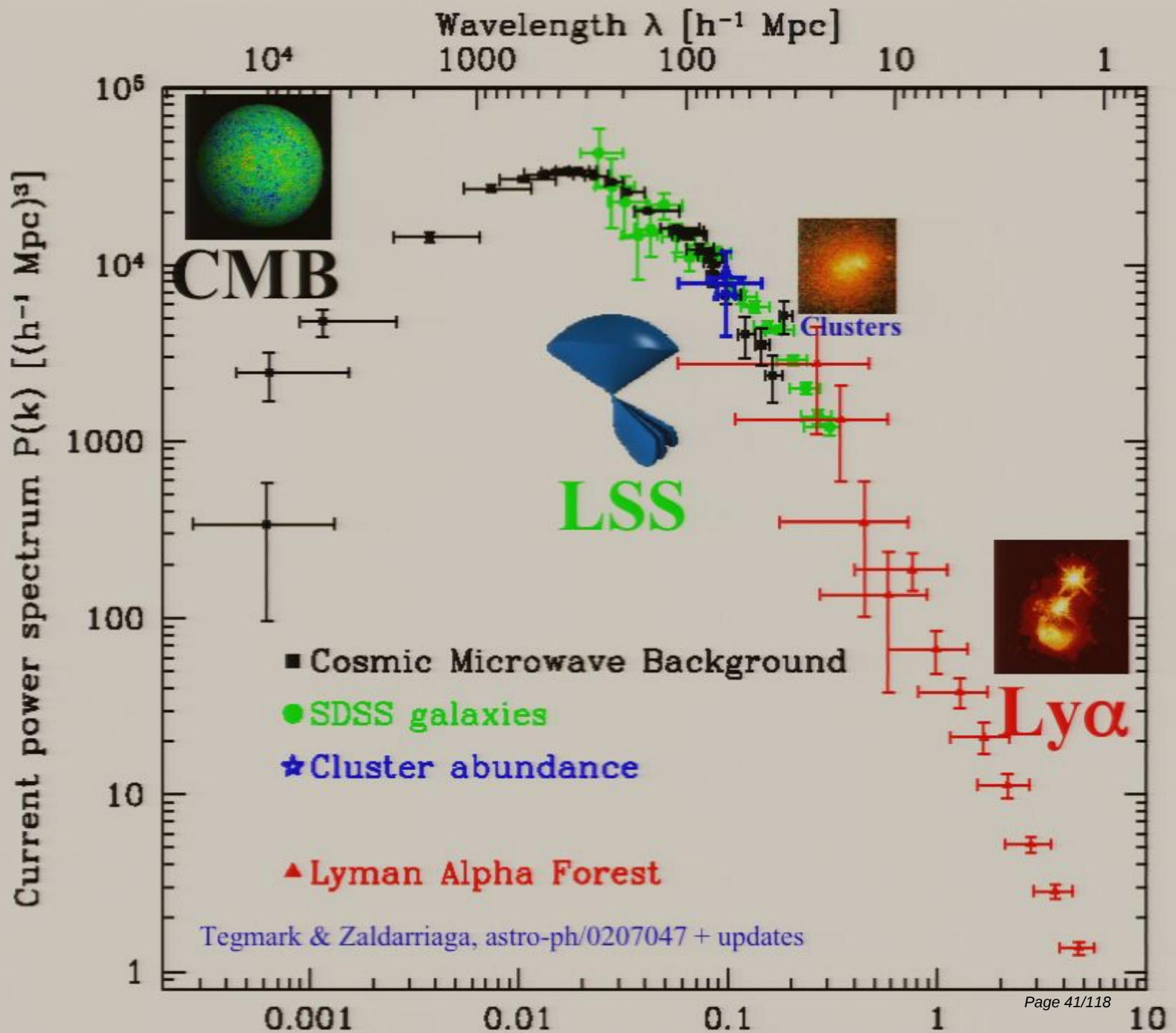
You

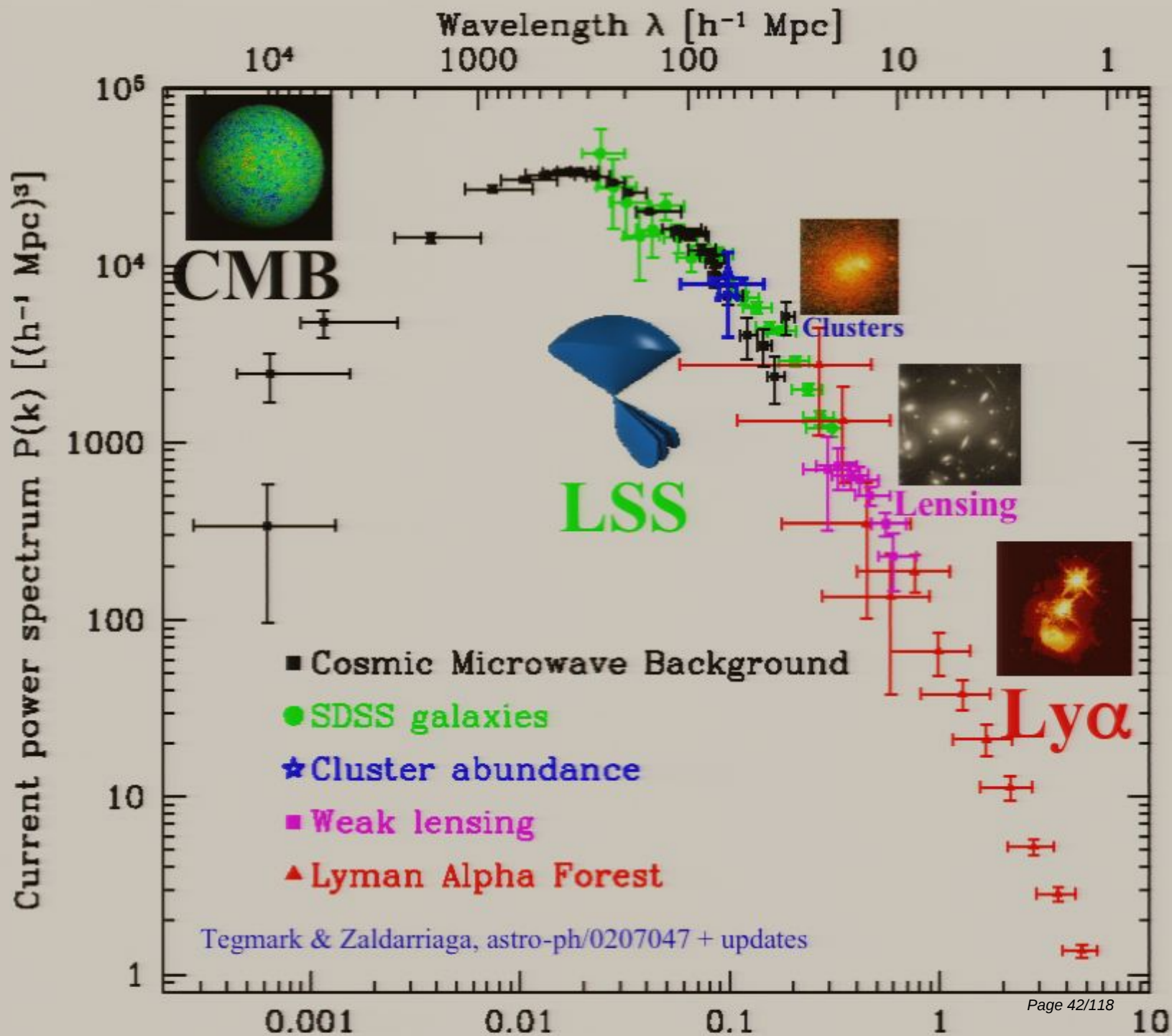


Quasar

QSO 1422+2301

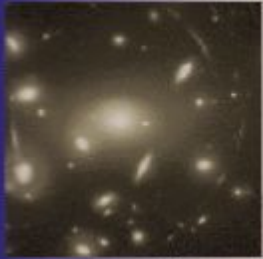






# **GRAVITATIONAL LENSING:** **A1689 imaged by Hubble ACS, Broadhurst et al 2004**





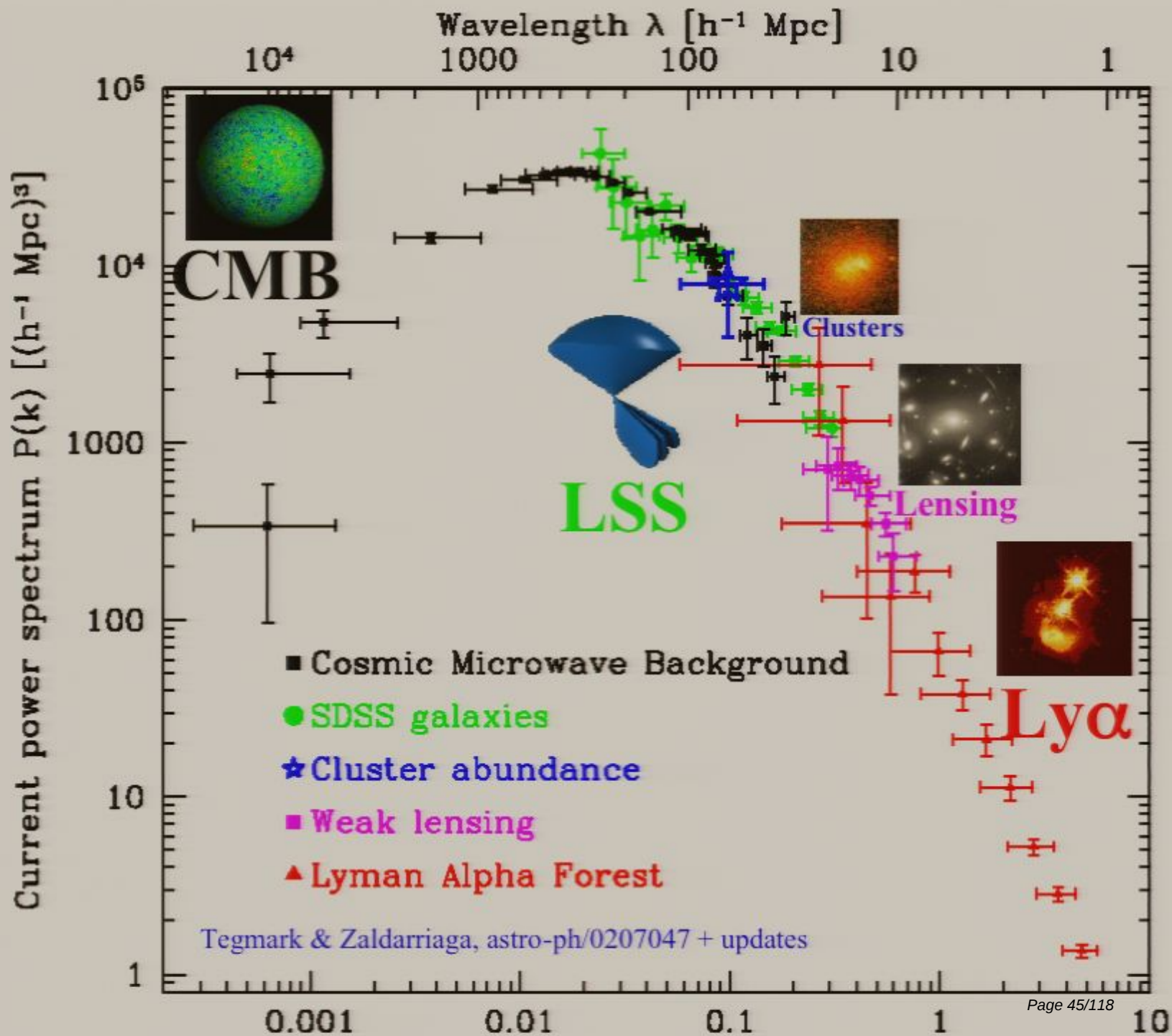
# Lensing

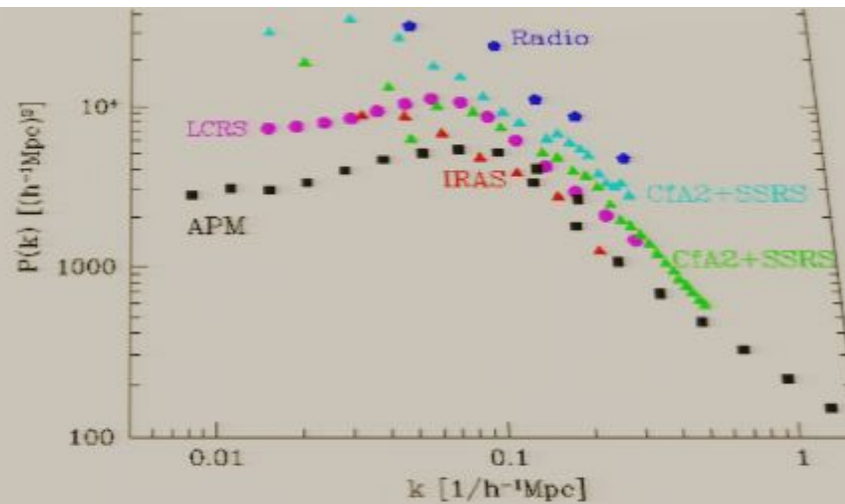
WHAT YOU HAVE:



WHAT YOU SEE:



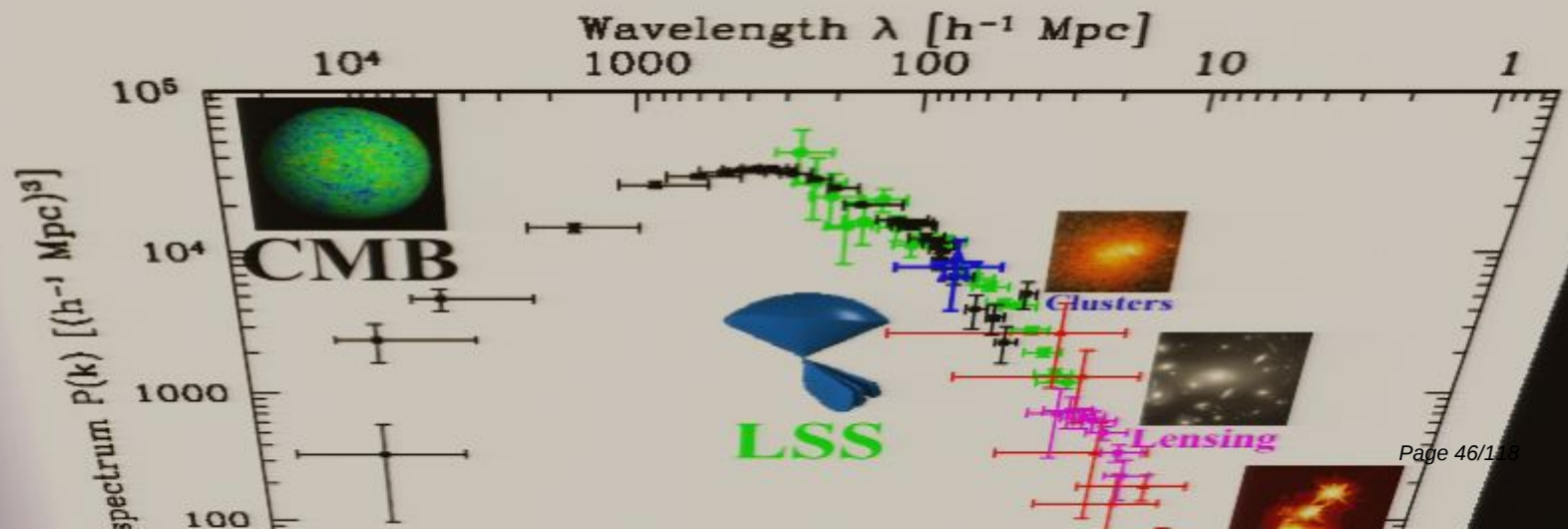


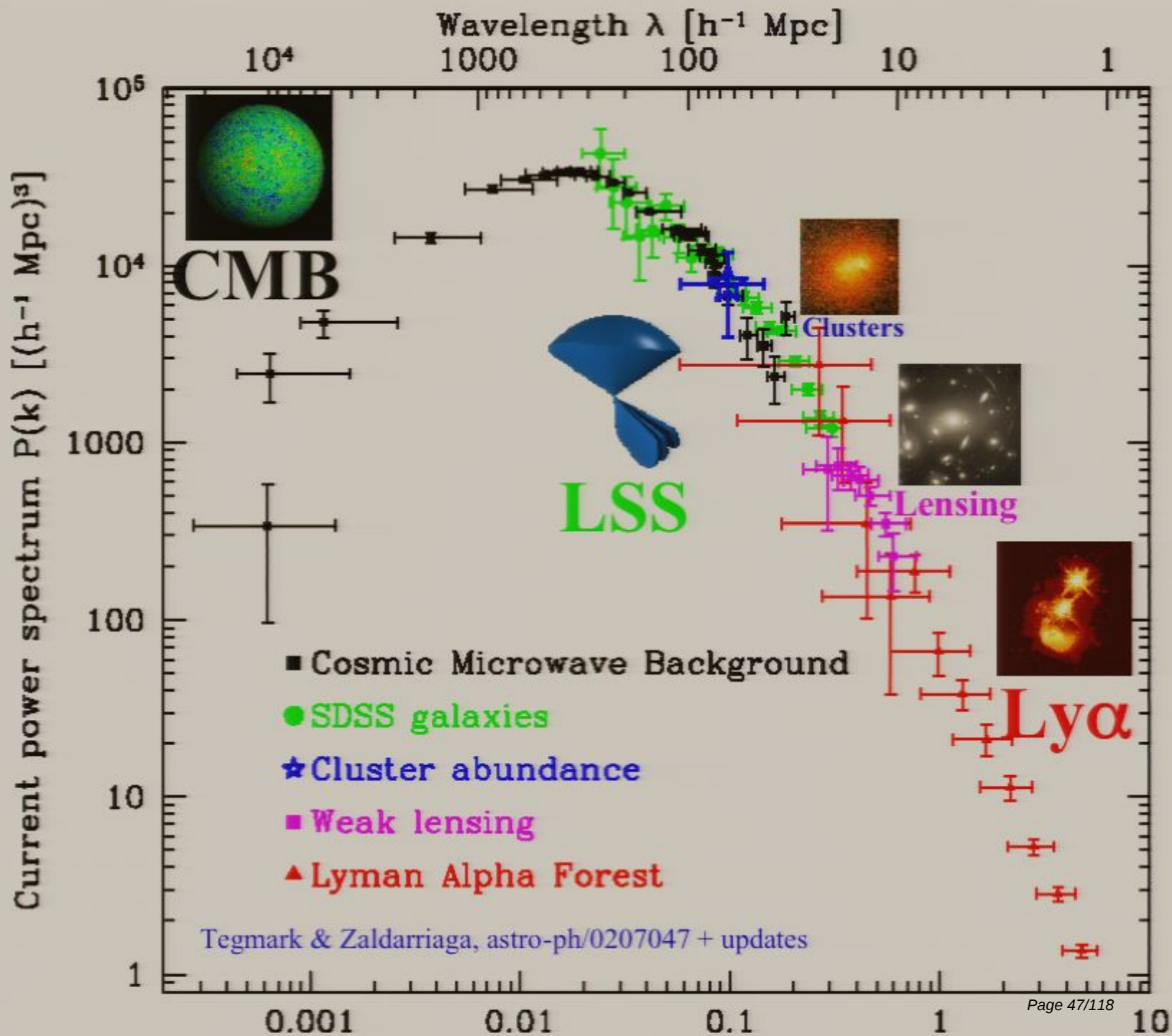


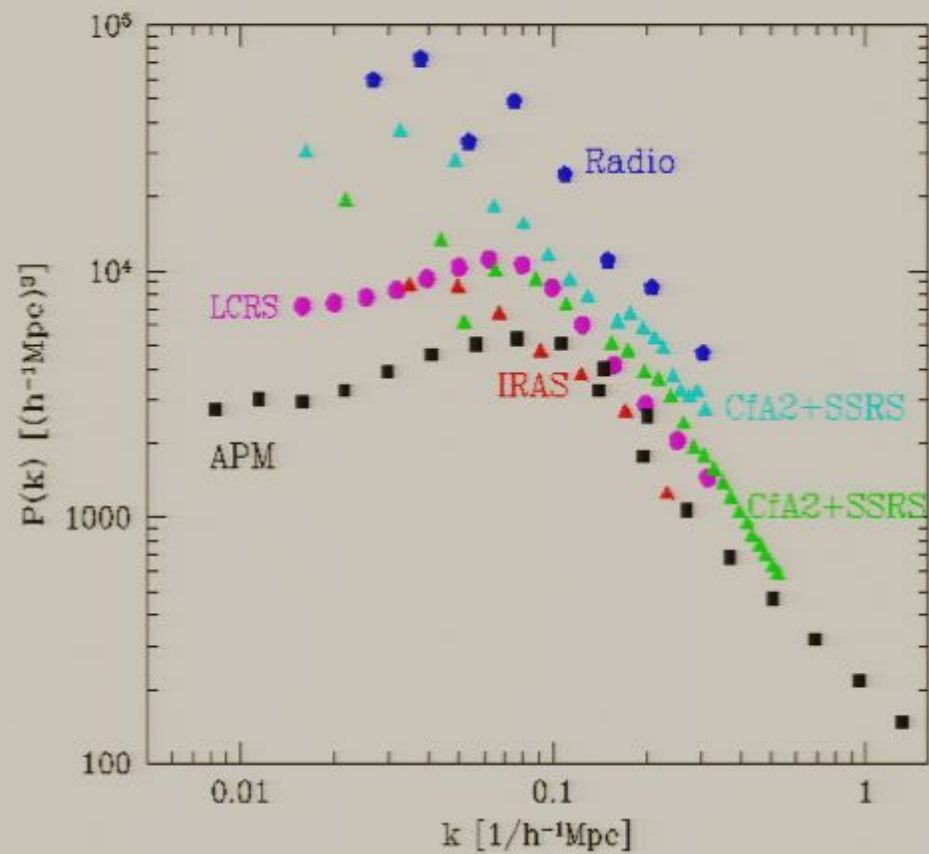
Galaxy power spectrum measurements 1999  
(Based on compilation by Michael Vogeley)



Max Tegmark  
Dept. of Physics, MIT  
tegmark@mit.edu  
Perimeter Seminar  
February 1, 2007

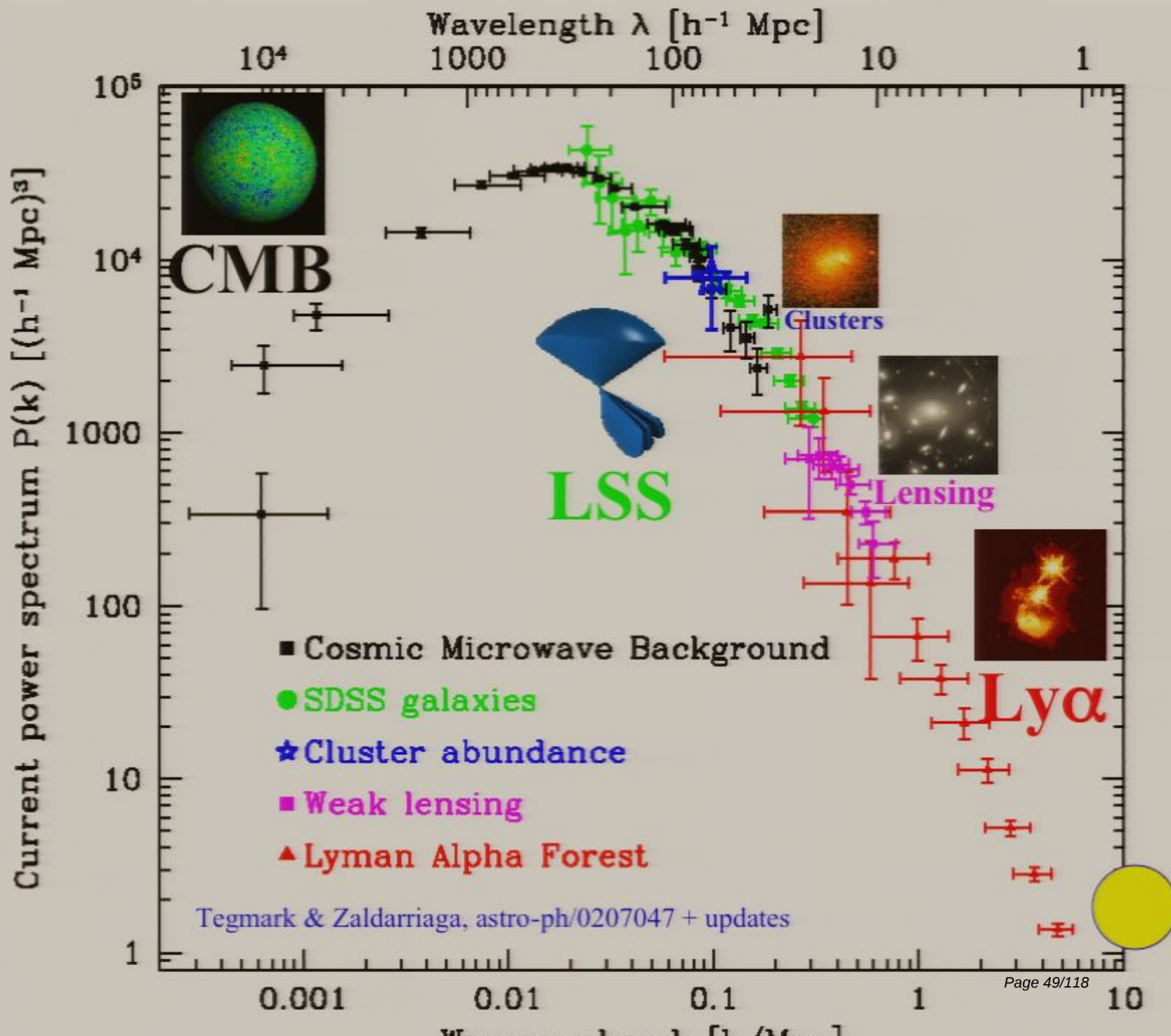






Galaxy power spectrum measurements 1999  
(Based on compilation by Michael Vogeley)





But the best is  
yet to come...

Precision, 21cm tomography, ...

Last scattering surface

Our observable universe



$z=1100$

$z=50$

$z=7$

$z=5$

$z=3$

$z=2$

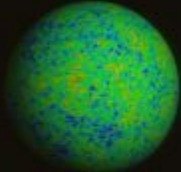
$z=1$



21cm tomography

# Summary: WHAT DO WE REALLY KNOW?

## Evidence for Big Bang:

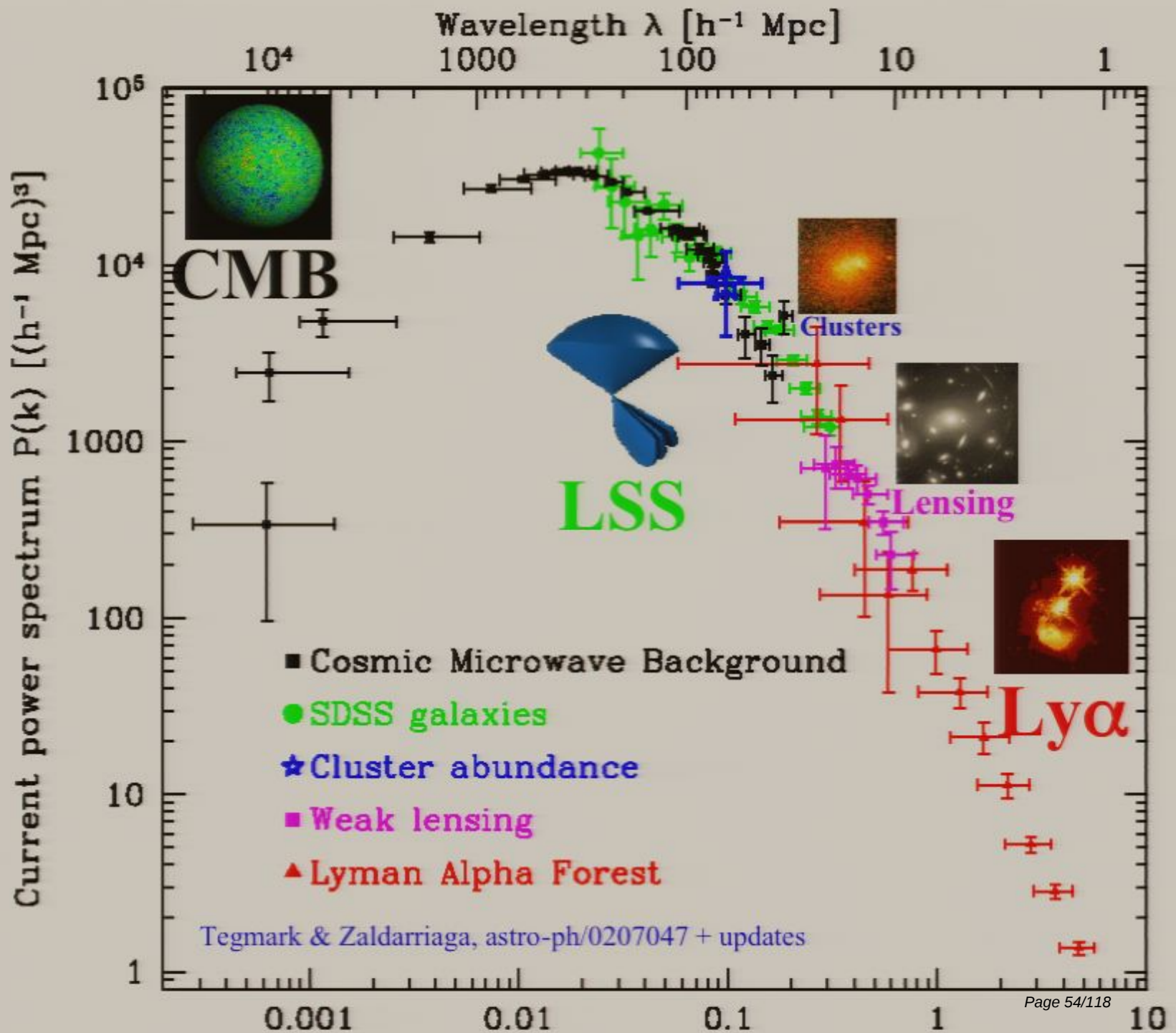
- Observed galaxy recession (Hubble's law)
- Existence of CMB 
- Correct predictions of big bang nucleosynthesis
- Darkness of night sky! (Olber)
- Distant objects look younger

*Plenty enough bang  
for most people to  
call "big" ...*

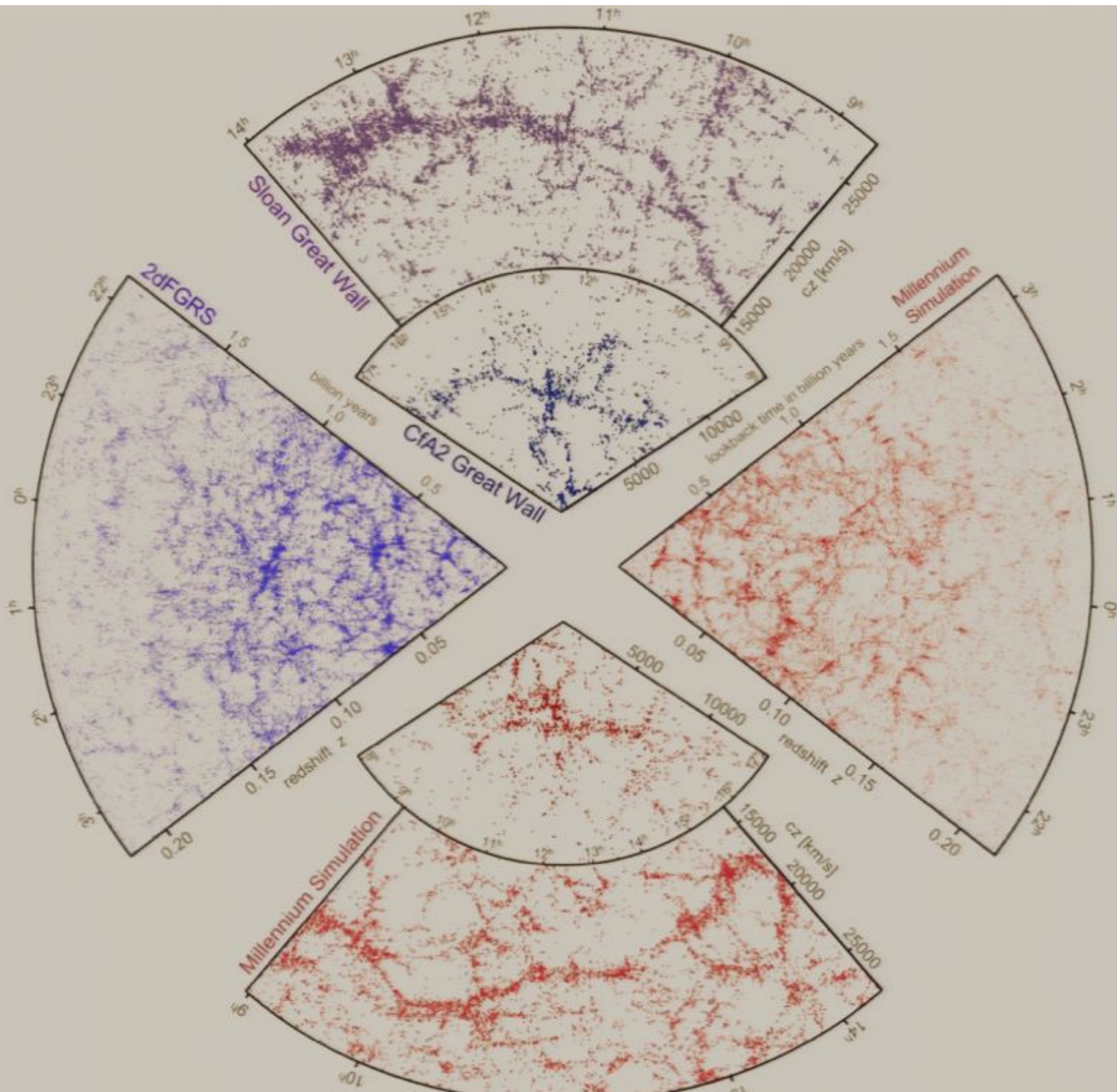
## Evidence for *what*, exactly?

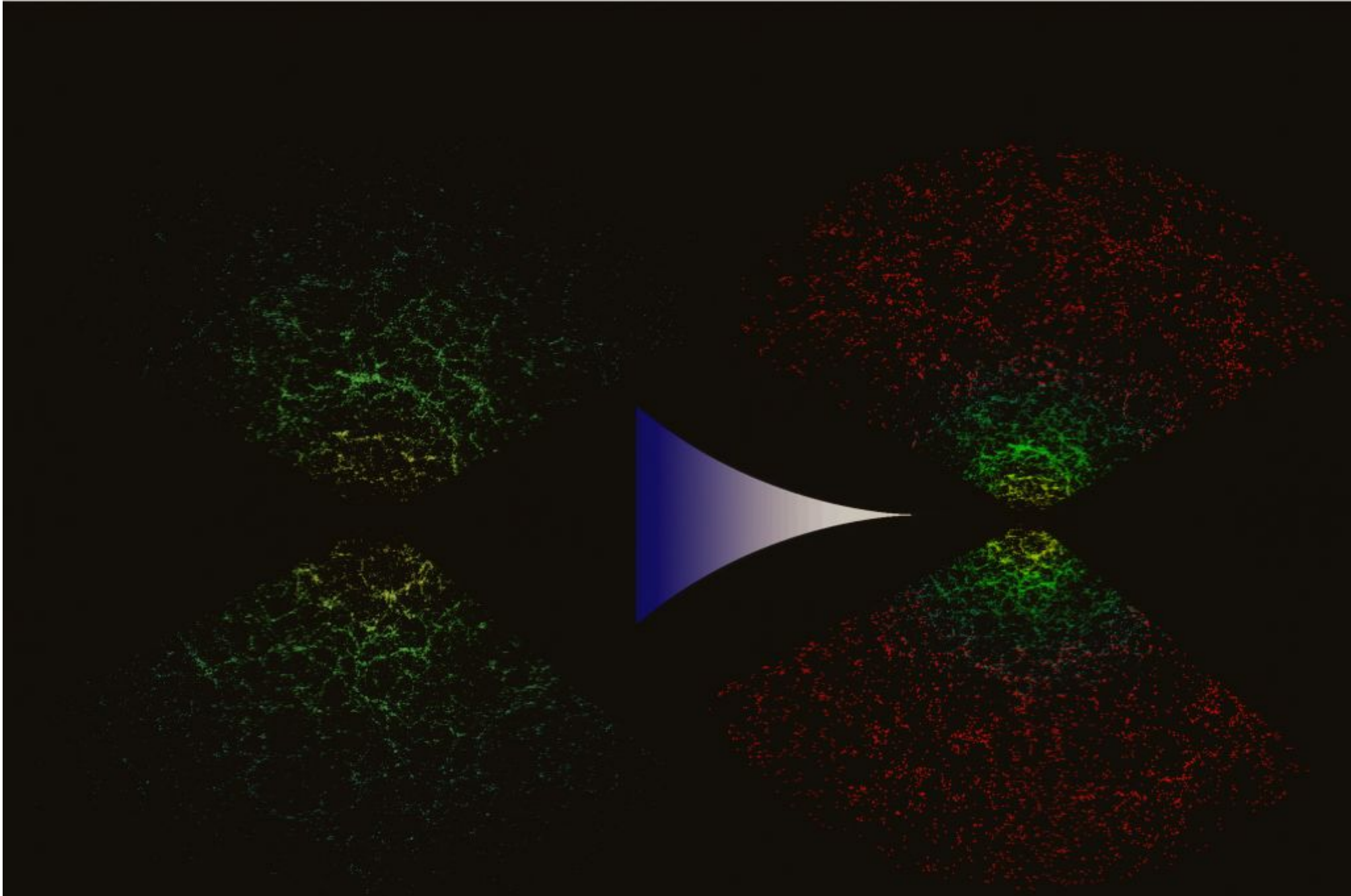
Our entire observable universe was once as hot as the core of the Sun, doubling its size in a under a second.

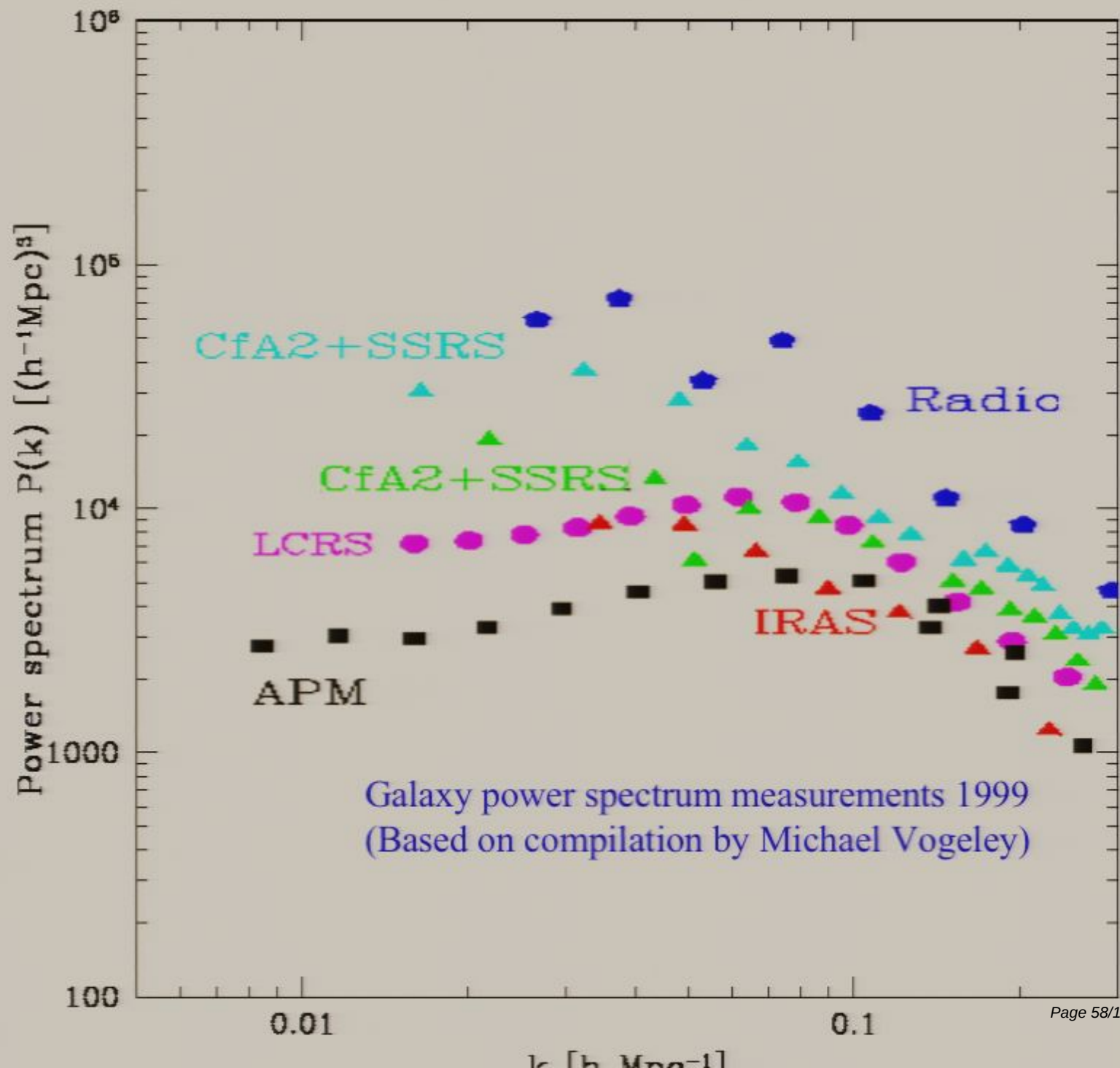
- *Not* evidence for a singularity

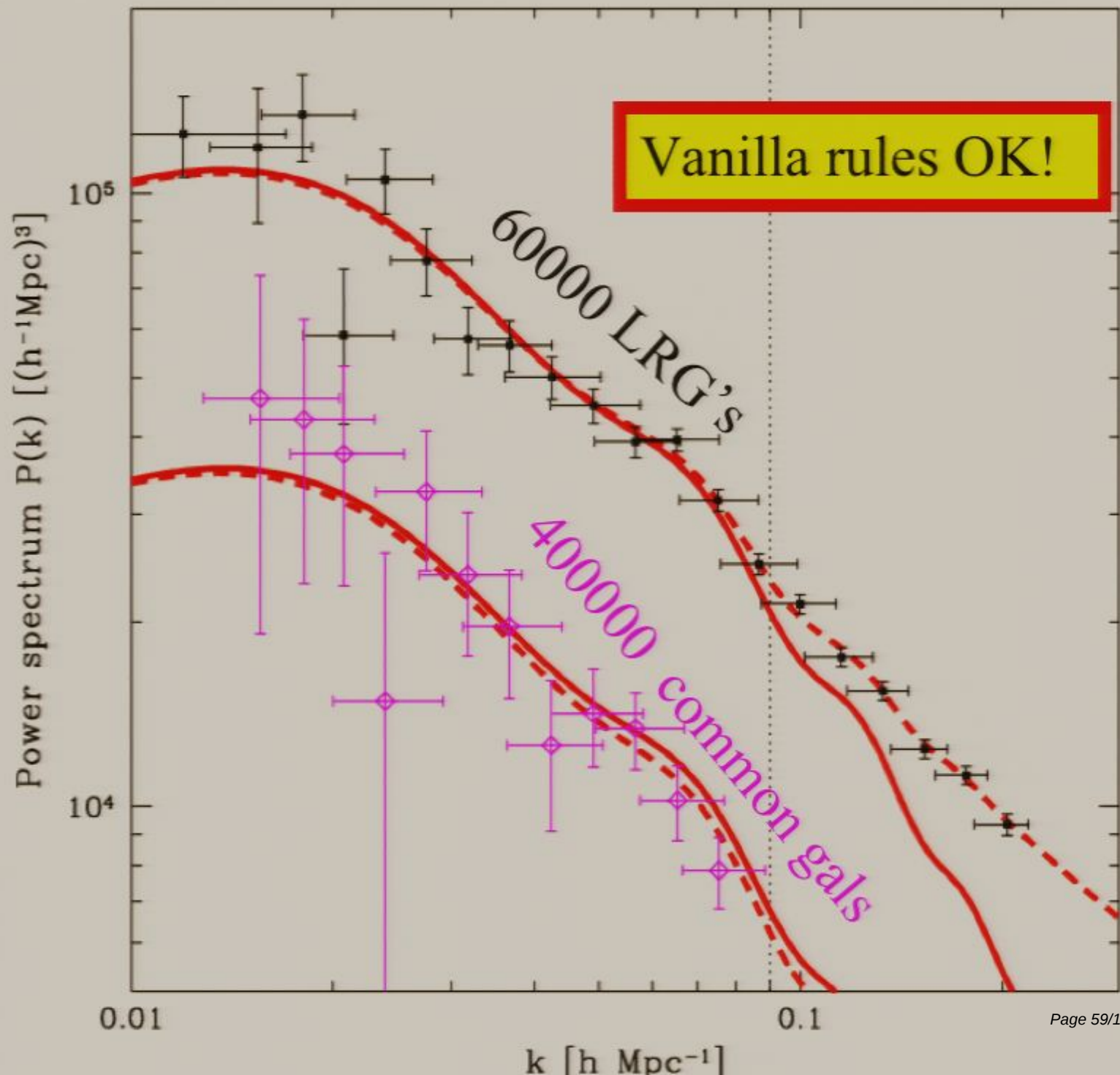


# Galaxy clustering progress





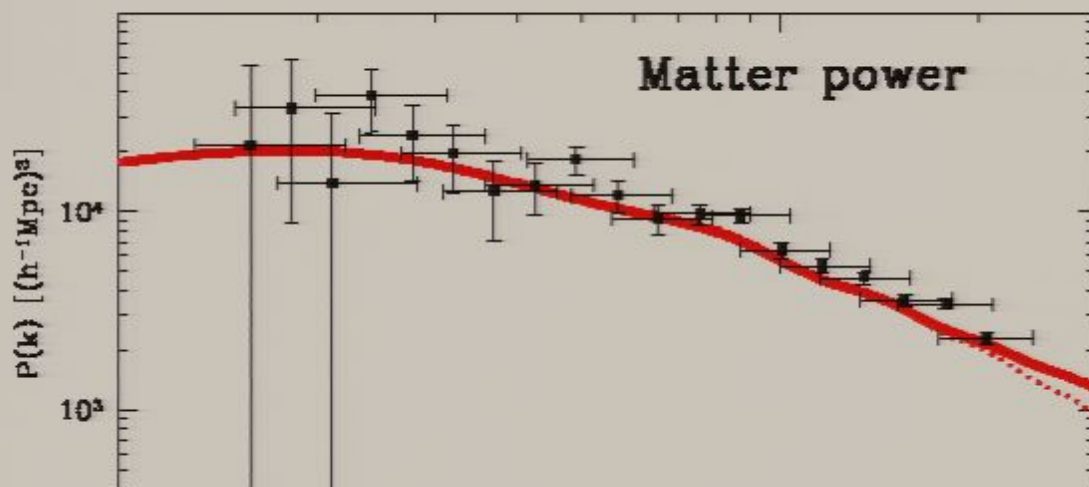
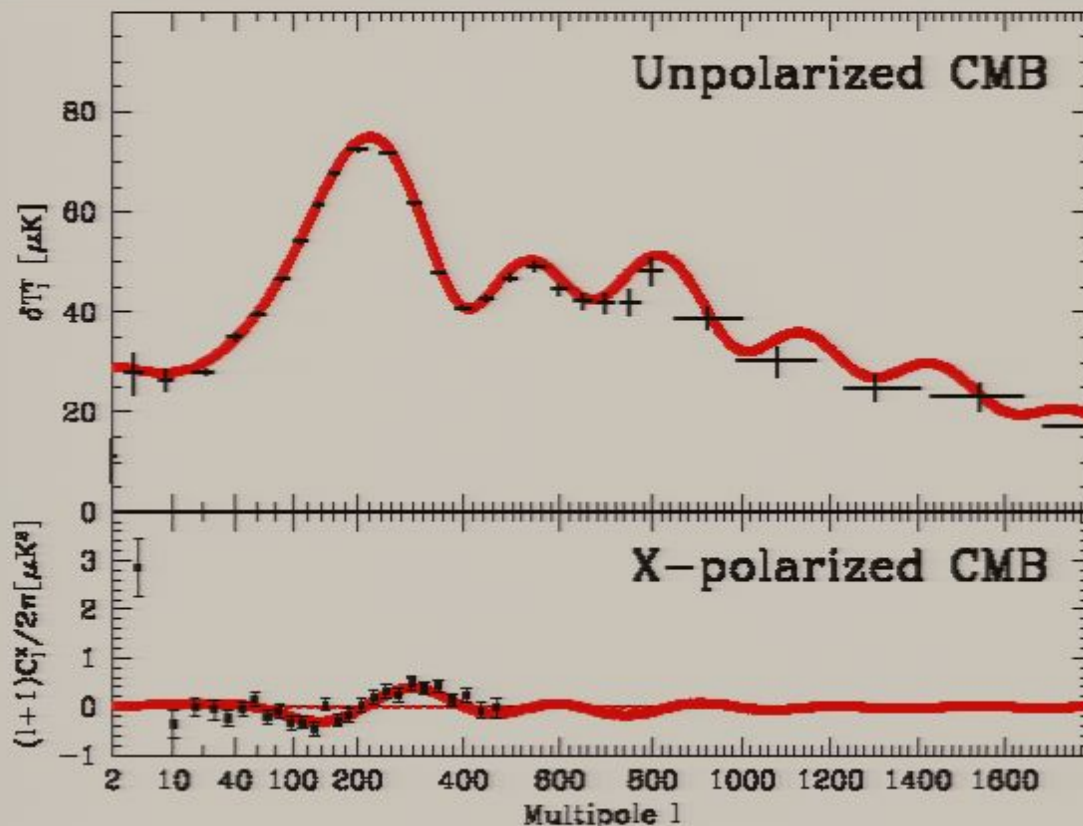




# Cosmological parameters

par movies

Max' power spectrum movies



$$\tau = 0.000$$

$$\Omega_k = 0.000$$

$$\Omega_\Lambda = 0.65$$

$$\omega_d = 0.13$$

$$\omega_b = 0.023$$

$$f_\nu = 0.000$$

$$n_s = 0.97$$

$$n_t = 0.000$$

$$A_s = 0.65$$

$$A_t = 0.000$$

$$b = 1.0$$

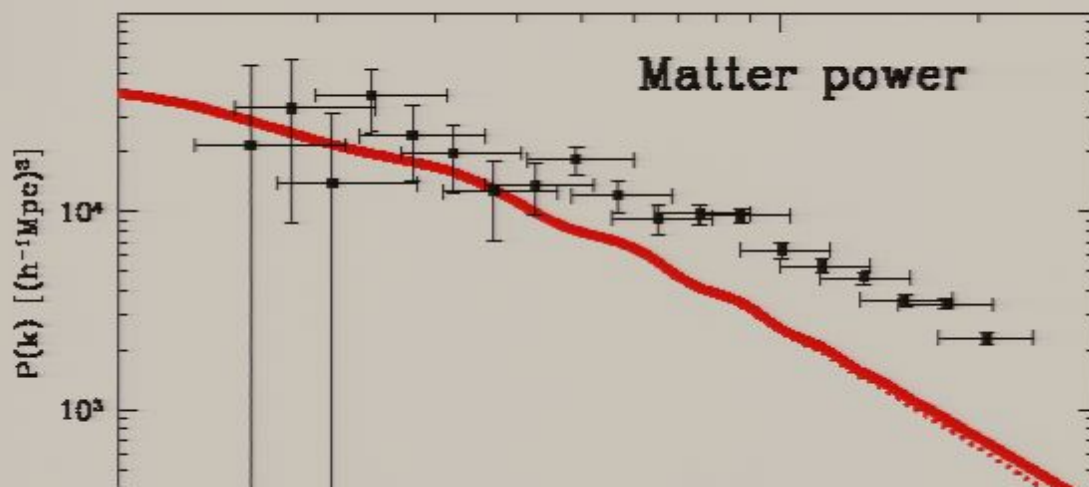
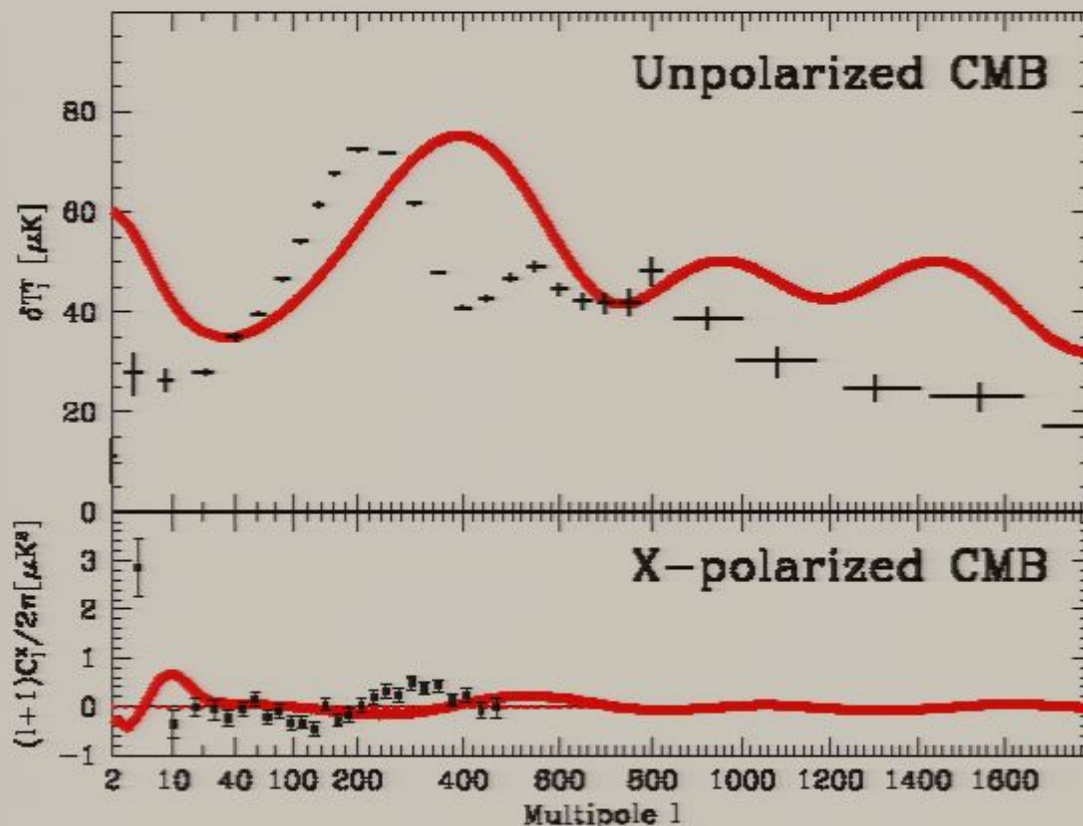
$$w = -1.000$$

$$\alpha = 0.000$$

$$h = 0.66$$

$$\chi^2 = 0.000$$

Max' power spectrum movies



$$\tau = 0.10$$

$$\Omega_k = 0.25$$

$$\Omega_\Lambda = 0.69$$

$$\omega_d = 0.12$$

$$\omega_b = 0.023$$

$$f_\nu = 0.000$$

$$n_s = 0.96$$

$$n_t = 0.000$$

$$A_s = 0.77$$

$$A_t = 0.000$$

$$b = 1.0$$

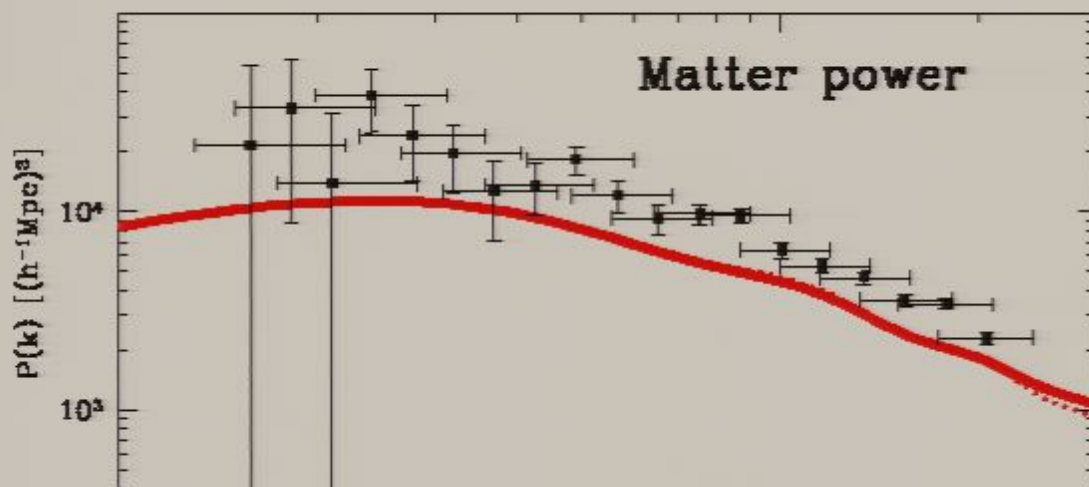
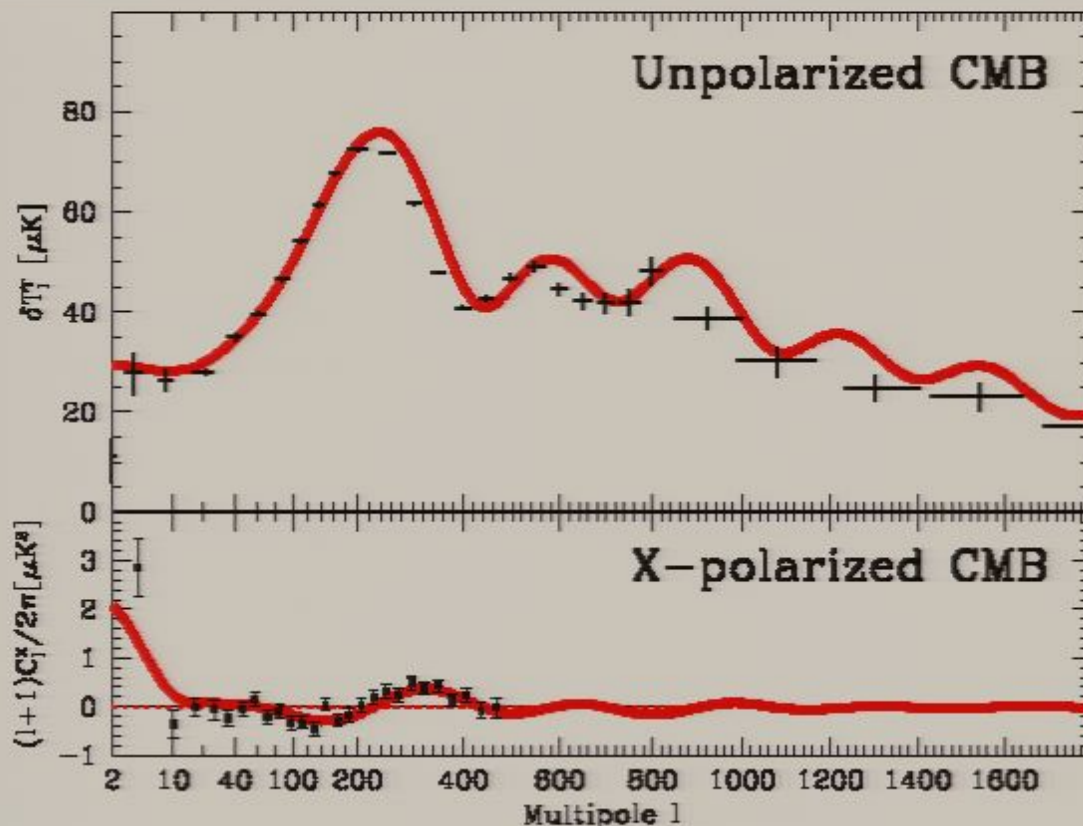
$$w = -1.000$$

$$\alpha = 0.000$$

$$h = 1.5$$

$$\chi^2 = 0.000$$

Max' power spectrum movies



$$\tau = 0.10$$

$$\Omega_k = 0.000$$

$$\Omega_\Lambda = 0.30$$

$$\omega_d = 0.12$$

$$\omega_b = 0.023$$

$$f_\nu = 0.000$$

$$n_s = 0.96$$

$$n_t = 0.000$$

$$A_s = 0.77$$

$$A_t = 0.000$$

$$b = 1.0$$

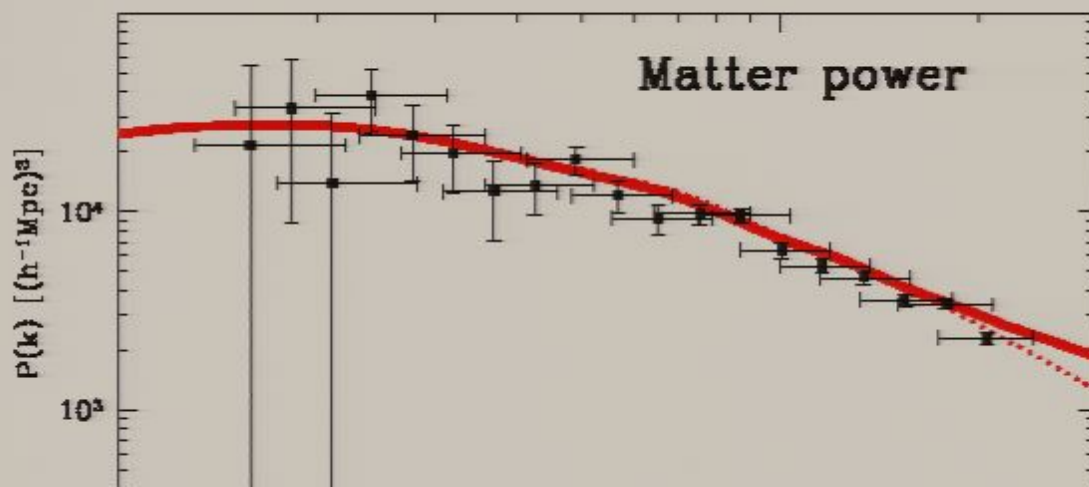
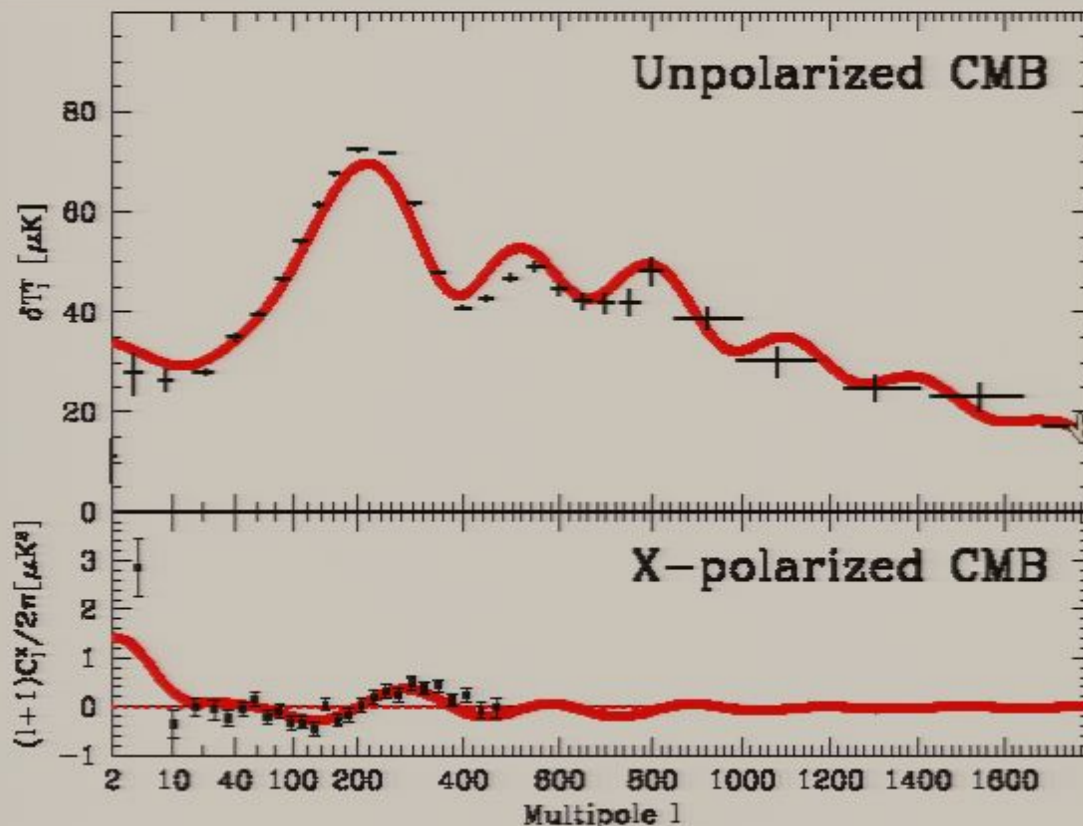
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$$\alpha = 0.000$$

$$h = 0.45$$

$$\chi^2 = 0.000$$

Max' power spectrum movies



$$\tau=0.10$$

$$\Omega_k=0.000$$

$$\Omega_\Lambda=0.69$$

$$\omega_d=0.13$$

$$\omega_b=0.014$$

$$f_\nu=0.000$$

$$n_s=0.96$$

$$n_t=0.000$$

$$A_s=0.77$$

$$A_t=0.000$$

$$b=1.0$$

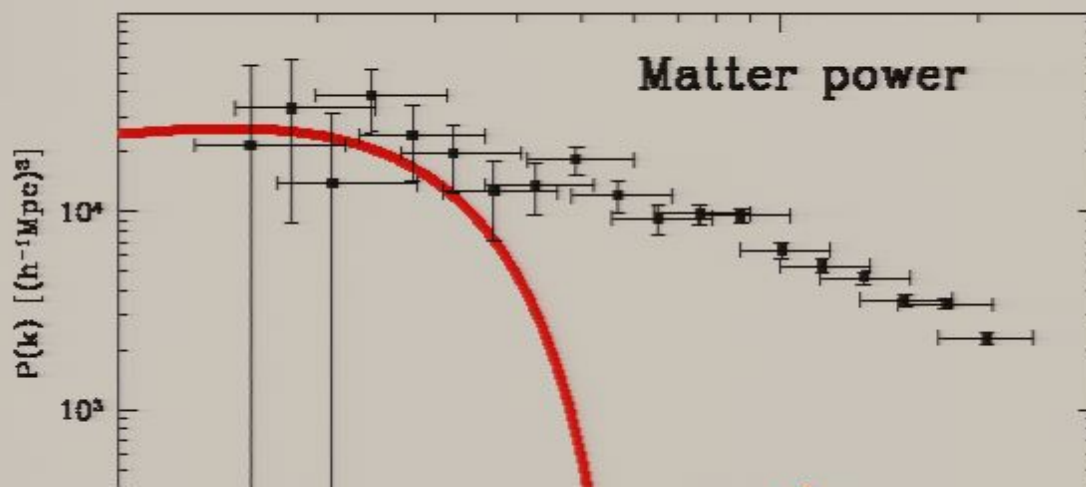
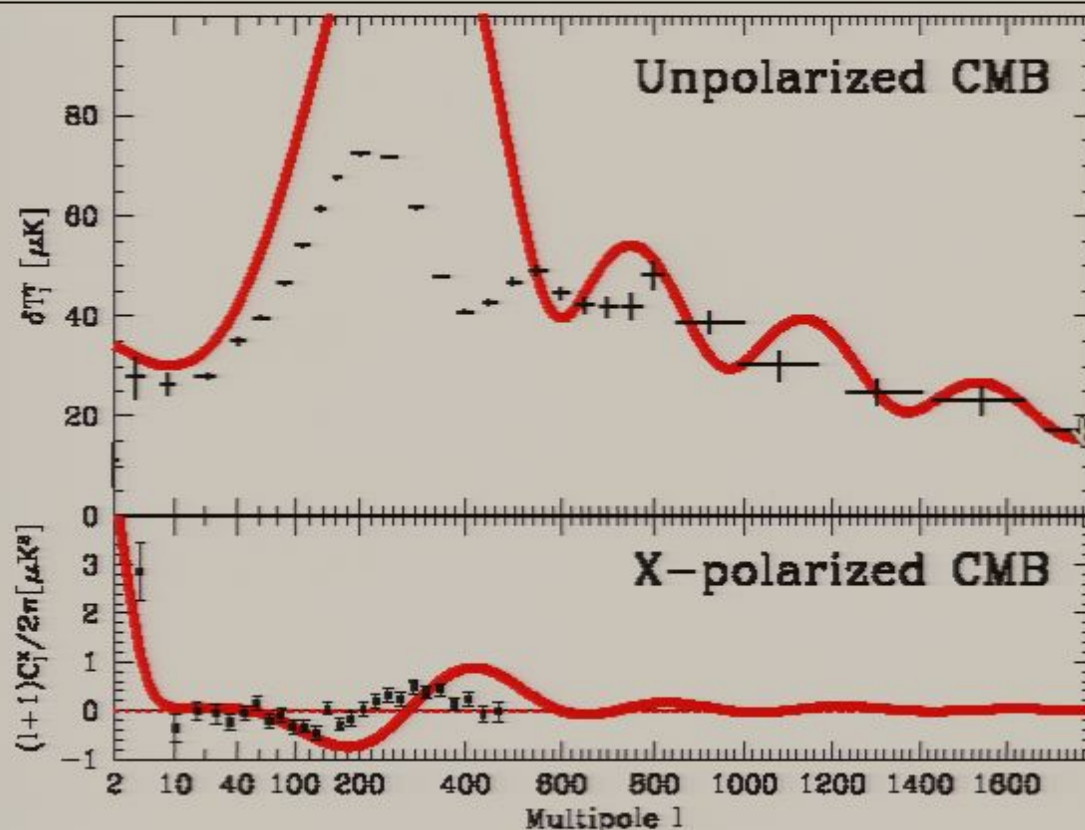
$$w=-1.000$$

$$\alpha=0.000$$

$$h=0.68$$

$$\chi^2=0.000$$

Max' power spectrum movies



$$\tau = 0.10$$

$$\Omega_k = 0.000$$

$$\Omega_\Lambda = 0.69$$

$$\omega_d = 0.014$$

$$\omega_b = 0.13$$

$$f_\nu = 0.000$$

$$n_s = 0.96$$

$$n_t = 0.000$$

$$A_s = 0.77$$

$$A_t = 0.000$$

$$b = 1.0$$

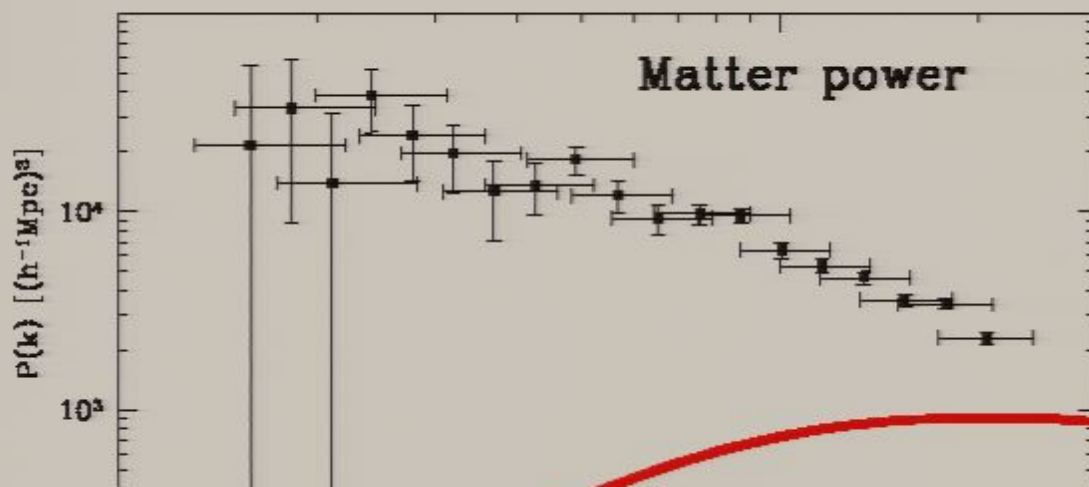
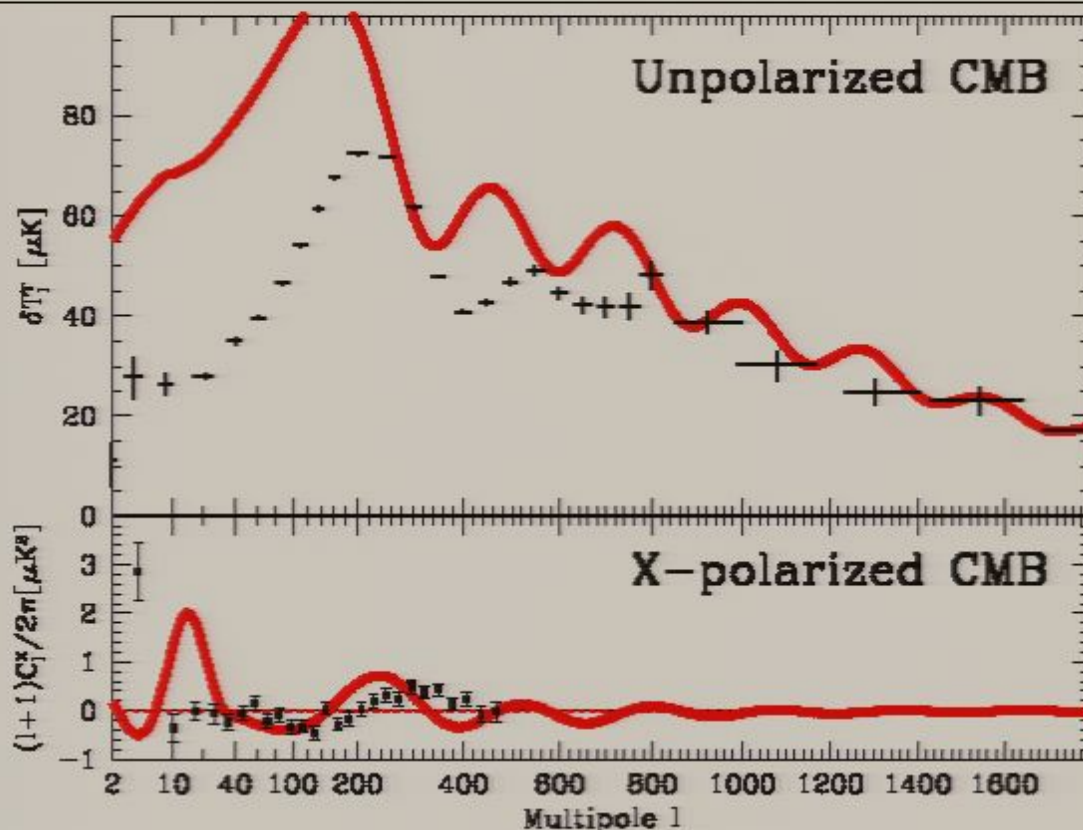
$$w = -1.000$$

$$\alpha = 0.000$$

$$h = 0.68$$

$$\chi^2 = 0.000$$

Max' power spectrum movies



$$\tau = 0.10$$

$$\Omega_k = 0.000$$

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$$n_s = 0.96$$

$$n_t = 0.000$$

$$A_s = 0.77$$

$$A_t = 0.000$$

$$b = 1.0$$

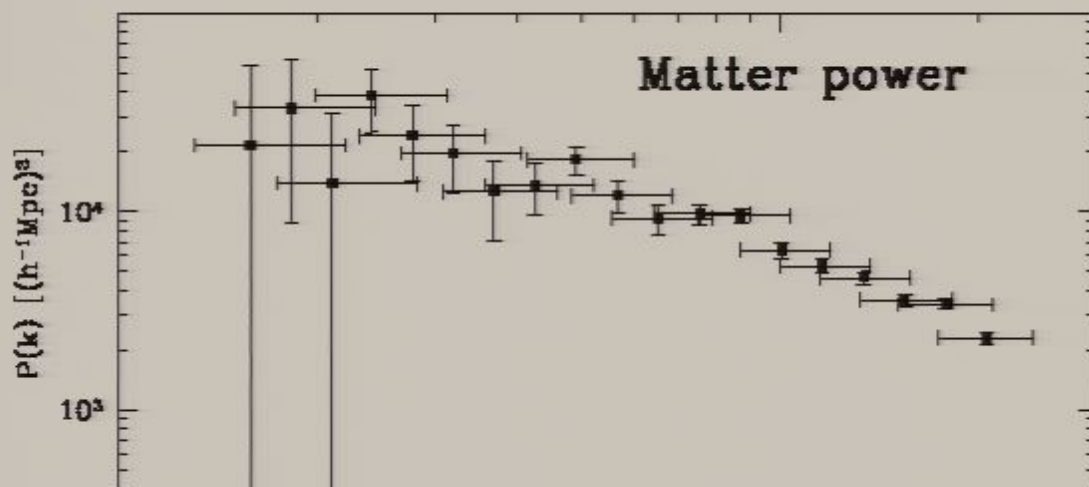
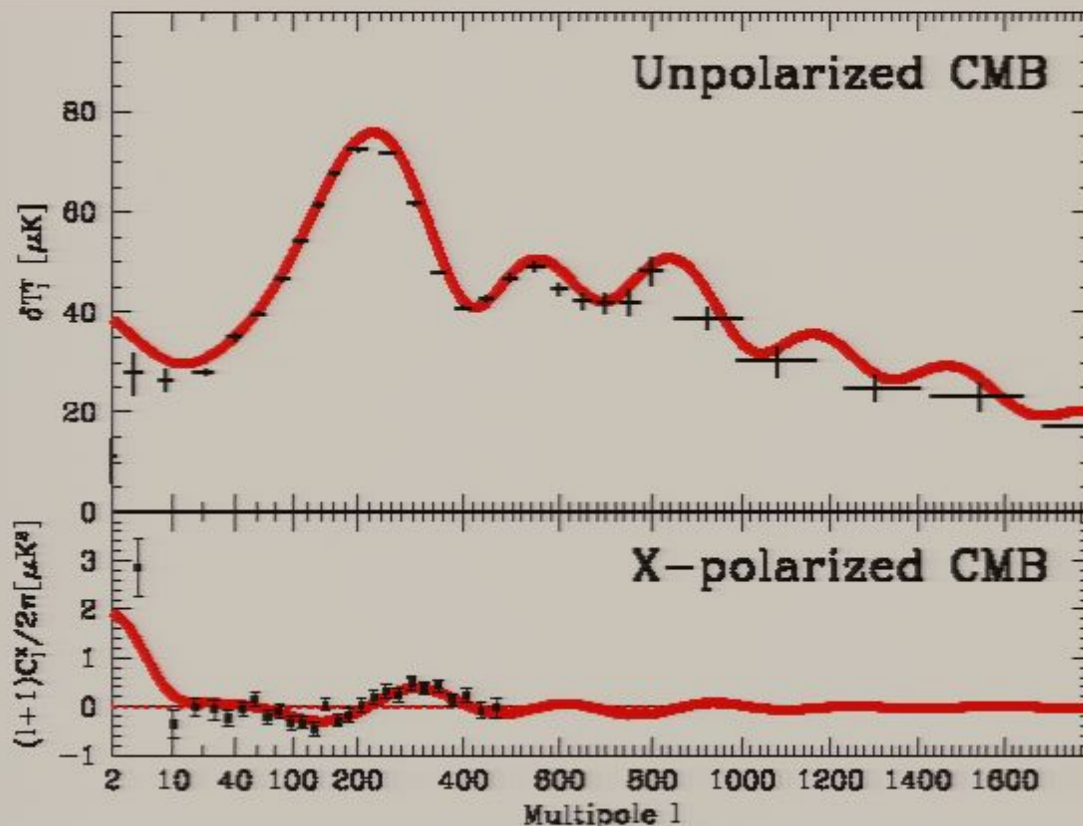
$$w = 0.000$$

$$\alpha = 0.000$$

$$h = 0.68$$

$$\chi^2 = 0.000$$

Max' power spectrum movies



$$\tau = 0.10$$

$$\Omega_k = 0.000$$

$$\Omega_\Lambda = 0.69$$

$$\omega_d = 0.12$$

$$\omega_b = 0.023$$

$$f_\nu = 0.000$$

$$n_s = 0.96$$

$$n_t = 0.000$$

$$A_s = 0.77$$

$$A_t = 0.000$$

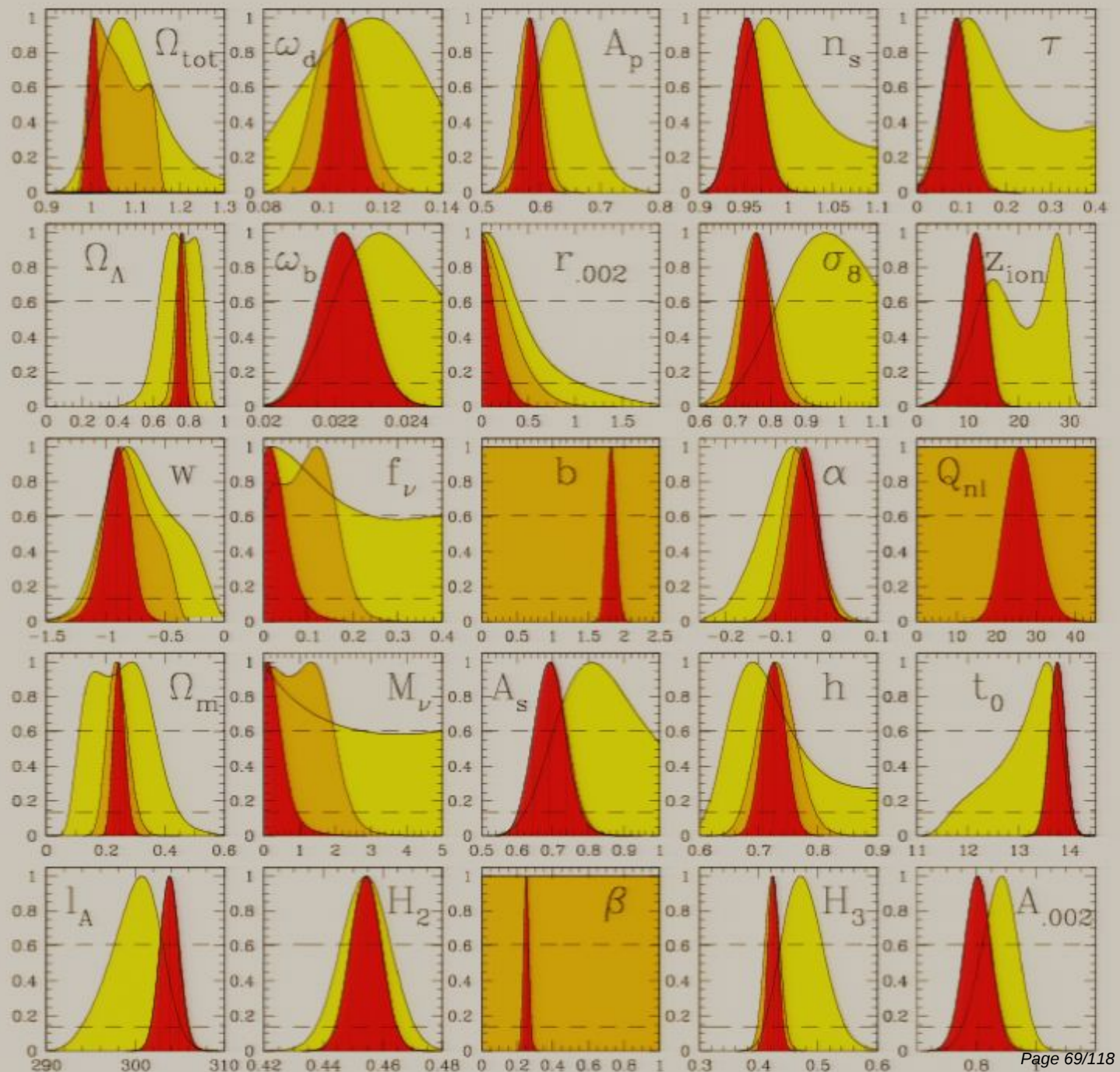
$$b = 1.0$$

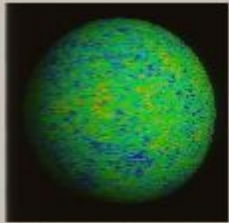
$$w = -1.400$$

$$\alpha = 0.000$$

$$h = 0.68$$

$$\chi^2 = 0.000$$





CMB

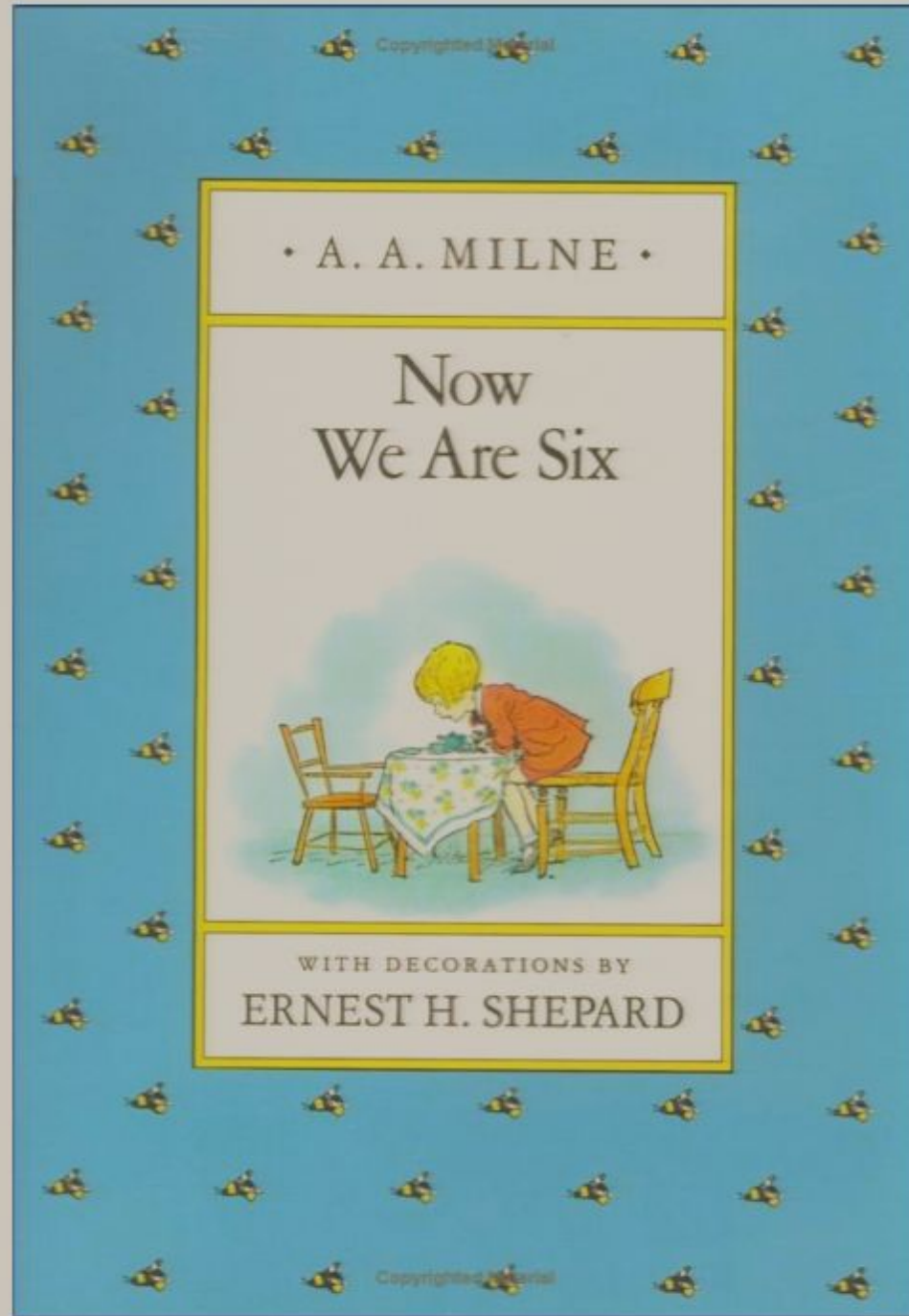
+



LSS

| Parameter                                                       | Value                                                 | Meaning                                   | Definition                                                                                                                                                                                           |
|-----------------------------------------------------------------|-------------------------------------------------------|-------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Matter budget parameters:</b>                                |                                                       |                                           |                                                                                                                                                                                                      |
| $\Omega_{\text{tot}}$                                           | $1.000^{+0.000}_{-0.000}$                             | Total density/critical density            | $\Omega_{\text{tot}} = \Omega_m + \Omega_b + 1 - \Omega_\Lambda$                                                                                                                                     |
| $\Omega_\Lambda$                                                | $0.701^{+0.007}_{-0.007}$                             | Dark energy density parameter             | $\Omega_\Lambda \approx h^{-2} \rho_\Lambda (1.88 \times 10^{-26} \text{ kg/m}^3)$                                                                                                                   |
| $\omega_b$                                                      | $0.022^{+0.0007}_{-0.0007}$                           | Baryon density                            | $\omega_b = \Omega_b h^2 \approx \rho_b / (1.88 \times 10^{-26} \text{ kg/m}^3)$                                                                                                                     |
| $\omega_c$                                                      | $0.033^{+0.0001}_{-0.0001}$                           | Cold dark matter density                  | $\omega_c = \Omega_c h^2 \approx \rho_c / (1.88 \times 10^{-26} \text{ kg/m}^3)$                                                                                                                     |
| $\omega_m$                                                      | $< 0.013$ (95%)                                       | Matter mixture density                    | $\omega_m = \Omega_m h^2 \approx \rho_m / (1.88 \times 10^{-26} \text{ kg/m}^3)$                                                                                                                     |
| $w$                                                             | $-0.98^{+0.087}_{-0.102}$                             | Dark energy equation of state             | $p_\Lambda/p_\Lambda$ (approximated as constant)                                                                                                                                                     |
| <b>Seed fluctuation parameters:</b>                             |                                                       |                                           |                                                                                                                                                                                                      |
| $A_s$                                                           | $0.008^{+0.000}_{-0.000}$                             | Scalar fluctuation amplitude              | Primordial scalar power at $k = 0.002 \text{ Mpc}^{-1}$                                                                                                                                              |
| $n$                                                             | $< 0.30$ (95%)                                        | Tensor-to-scalar ratio                    | Tensor-to-scalar power ratio at $k = 0.002 \text{ Mpc}^{-1}$                                                                                                                                         |
| $n_s$                                                           | $0.963^{+0.016}_{-0.016}$                             | Scalar spectral index                     | Primordial spectral index at $k = 0.002 \text{ Mpc}^{-1}$                                                                                                                                            |
| $n_s + 1$                                                       | $0.960^{+0.016}_{-0.016}$                             | Tensor spectral index                     | $n_s = -n/k$ assumed                                                                                                                                                                                 |
| $\alpha$                                                        | $-0.000^{+0.027}_{-0.027}$                            | Running of spectral index                 | $\alpha = dn_s/d \ln k$ (approximated as constant)                                                                                                                                                   |
| <b>Nonlinear parameters:</b>                                    |                                                       |                                           |                                                                                                                                                                                                      |
| $\tau$                                                          | $0.081^{+0.026}_{-0.026}$                             | Reionization optical depth                |                                                                                                                                                                                                      |
| $b$                                                             | $1.806^{+0.074}_{-0.069}$                             | Galaxy bias factor                        | $b = \langle \delta_{\text{galaxy}}(k) \rangle / \langle \delta(k) \rangle^{1/2}$ at large scales, where $\delta(k)$ refers to today                                                                 |
| $\bar{Q}_{\text{NL}}$                                           | $30.3^{+4.1}_{-4.1}$                                  | Nonlinear correction parameter (20)       | $\bar{P}_\delta(k) = P_{\text{linear}}(k)k^2 / (1 + \bar{Q}_{\text{NL}}(k^2))$ ( $1 \leq k \leq 1.76$ )                                                                                              |
| <b>(Other popular parameters (determined by those above))</b>   |                                                       |                                           |                                                                                                                                                                                                      |
| $h$                                                             | $0.738^{+0.019}_{-0.019}$                             | Hubble parameter                          | $h = \sqrt{\Omega_b + \omega_c + \omega_m} / (\Omega_{\text{tot}} - \Omega_\Lambda)$                                                                                                                 |
| $\Omega_m$                                                      | $0.279^{+0.016}_{-0.017}$                             | Matter density/critical density           | $\Omega_m = \Omega_{\text{tot}} - \Omega_\Lambda$                                                                                                                                                    |
| $\Omega_b$                                                      | $0.0419^{+0.0019}_{-0.0019}$                          | Baryon density/critical density           | $\Omega_b = \omega_b / h^2$                                                                                                                                                                          |
| $\Omega_c$                                                      | $0.429^{+0.016}_{-0.016}$                             | CDM density/critical density              | $\Omega_c = \omega_c / h^2$                                                                                                                                                                          |
| $\Omega_m$                                                      | $< 0.024$ (95%)                                       | Neutrino density/critical density         | $\Omega_\nu = \omega_\nu / h^2$                                                                                                                                                                      |
| $\Omega_k$                                                      | $-0.0030^{+0.0030}_{-0.0030}$                         | Spatial curvature                         | $\Omega_k = 1 - \Omega_{\text{tot}}$                                                                                                                                                                 |
| $\omega_m$                                                      | $0.0272^{+0.0044}_{-0.0044}$                          | Matter density                            | $\omega_m = \omega_b + \omega_c + \omega_\nu = \Omega_m h^2$                                                                                                                                         |
| $f_\nu$                                                         | $< 0.190$ (95%)                                       | Dark matter neutrino fraction             | $f_\nu = \rho_\nu / \rho_g$                                                                                                                                                                          |
| $A_s$                                                           | $< 0.21$ (95%)                                        | Tensor fluctuation amplitude              | $A_s = \tau / A_s$                                                                                                                                                                                   |
| $M_{\text{pl}}$                                                 | $< 0.34$ (95%) eV                                     | Sum of neutrino masses                    | $M_{\text{pl}} \approx (94.4 \text{ eV}) \times \omega_\nu$ (10%)                                                                                                                                    |
| $A_{\text{QCD}}$                                                | $0.801^{+0.043}_{-0.043}$                             | WMAP2 normalization parameter             | $A_s$ scaled for $h = 0.002 \text{ Mpc}^{-1}$ , $A_{\text{QCD}} = 25^{n-1} A_s$ if $n \neq 0$                                                                                                        |
| $r_{\text{QCD}}$                                                | $< 0.34$ (95%)                                        | Tensor-to-scalar ratio (WMAP2)            | Tensor-to-scalar power ratio at $k = 0.002 \text{ Mpc}^{-1}$                                                                                                                                         |
| $\tau_{\text{QCD}}$                                             | $0.738^{+0.016}_{-0.016}$                             | Density fluctuation amplitude             | $\tau_{\text{QCD}} = (4\pi \int_0^{\infty} \frac{dk}{k} (10^9 \text{ yr} - 1 \text{ yr}) \delta^2 P(k) \frac{h^2 \Omega_b}{(2\pi)^3})^{1/2}$ , $\tau \leq k \leq 65 \text{ h}^{-1} \text{ Mpc}^{-1}$ |
| $\tau_{\text{QCD}}^{\text{QCD}}$                                | $0.026^{+0.024}_{-0.024}$                             | Velocity fluctuation amplitude            |                                                                                                                                                                                                      |
| <b>Cluster history parameters:</b>                              |                                                       |                                           |                                                                                                                                                                                                      |
| $\tau_{\text{eq}}$                                              | $361^{+115}_{-102}$                                   | Matter-radiation equality redshift        | $\tau_{\text{eq}} = 2407 h_{\text{eq}} - 1$                                                                                                                                                          |
| $\tau_{\text{rec}}$                                             | $3600^{+500}_{-500}$                                  | Recombination redshift                    | $\tau_{\text{rec}}(\omega_m, \omega_b)$ given by eq. (18) of [106]                                                                                                                                   |
| $\tau_{\text{ion}}$                                             | $11.1^{+1.2}_{-1.2}$                                  | Reionization redshift (average)           | $\tau_{\text{ion}} \approx 920 \cdot 0.01 \omega_b / \omega_m^{1/2} \Omega_b^{1/2}$ (assuming average reionization, [107])                                                                           |
| $\tau_{\text{acc}}$                                             | $0.870^{+0.010}_{-0.010}$                             | Acceleration redshift                     | $\tau_{\text{acc}} = [(-3w - 1) \Omega_b / \Omega_m]^{-1/3} - 1$ , if $w < -1/3$                                                                                                                     |
| $\tau_{\text{eq}}$                                              | $0.0034^{+0.0040}_{-0.0040}$                          | Matter-radiation equality time            | $\tau_{\text{eq}} \approx (0.745 \text{ Gyr}) \times h^{-1} \int_{\tau_{\text{eq}}}^{\infty} \frac{dt}{a(t)} [H(t)/(1 + w(t))]^{1/2}$ [108]                                                          |
| $\tau_{\text{rec}}$                                             | $0.3955^{+0.0040}_{-0.0040}$                          | Recombination time                        | $\tau_{\text{rec}} \approx (0.785 \text{ Gyr}) \times h^{-1} \int_{\tau_{\text{rec}}}^{\infty} \frac{dt}{a(t)} [H(t)/(1 + w(t))]^{1/2}$ [108]                                                        |
| $\tau_{\text{ion}}$                                             | $0.42^{+0.20}_{-0.20}$                                | Reionization time                         | $\tau_{\text{ion}} \approx (0.785 \text{ Gyr}) \times h^{-1} \int_{\tau_{\text{ion}}}^{\infty} \frac{dt}{a(t)} [H(t)/(1 + w(t))]^{1/2}$ [108]                                                        |
| $\tau_{\text{acc}}$                                             | $0.74^{+0.25}_{-0.25}$                                | Acceleration time                         | $\tau_{\text{acc}} \approx (0.785 \text{ Gyr}) \times h^{-1} \int_{\tau_{\text{acc}}}^{\infty} \frac{dt}{a(t)} [H(t)/(1 + w(t))]^{1/2}$ [108]                                                        |
| $\tau_{\text{now}}$                                             | $13.76^{+0.12}_{-0.12}$                               | Age of Universe now                       | $\tau_{\text{now}} \approx (0.745 \text{ Gyr}) \times h^{-1} \int_{\tau_{\text{now}}}^{\infty} \frac{dt}{a(t)} [H(t)/(1 + w(t))]^{1/2}$ [108]                                                        |
| <b>Fundamental parameters (independent of observing epoch):</b> |                                                       |                                           |                                                                                                                                                                                                      |
| $Q$                                                             | $1.945^{+0.001}_{-0.001} \times 10^{-5}$              | Primordial fluctuation amplitude          | $Q = \epsilon_h \approx A_s^{1/2} / h \approx 50 \cdot 22 h_{\text{eq}} / 7 \cdot \Omega_{\text{tot}}$                                                                                               |
| $\kappa$                                                        | $1.2^{+0.7}_{-0.3} \times 10^{-41}$                   | Dimensionless spatial curvature (106)     | $\kappa = (A_s / h^2 \Omega_b^2 \Omega_m^2)^{1/2} k$                                                                                                                                                 |
| $\rho_\Lambda$                                                  | $0.68^{+0.14}_{-0.14} \times 10^{-26} \text{ kg/m}^3$ | Dark energy density                       | $\rho_\Lambda \approx h^2 \Omega_\Lambda \approx (1.88 \times 10^{-26} \text{ kg/m}^3)$                                                                                                              |
| $\rho_{\text{baryo}}$                                           | $0.6^{+1.2}_{-1.2} \times 10^{-26} \text{ kg/m}^3$    | Matter formation density                  | $\rho_{\text{baryo}} = 1.88^2 Q^2 \tau^4$                                                                                                                                                            |
| $\epsilon$                                                      | $0.22^{+0.11}_{-0.11}$ eV                             | Matter mass per photon                    | $\epsilon = m_e / m_\gamma$                                                                                                                                                                          |
| $\epsilon_b$                                                    | $0.509^{+0.018}_{-0.018}$ eV                          | Baryon mass per photon                    | $\epsilon_b = m_p / m_\gamma$                                                                                                                                                                        |
| $\epsilon_c$                                                    | $2.03^{+0.11}_{-0.11}$ eV                             | CDM mass per photon                       | $\epsilon_c = m_c / m_\gamma$                                                                                                                                                                        |
| $\epsilon_\nu$                                                  | $< 0.26$ (95%) eV                                     | Neutrino mass per photon                  | $\epsilon_\nu = m_\nu / m_\gamma$                                                                                                                                                                    |
| $\eta$                                                          | $6.10^{+0.20}_{-0.20} \times 10^{-10}$                | Baryon/photon ratio                       | $\eta = n_b / n_\gamma = \epsilon_b / m_p$                                                                                                                                                           |
| $H_0$                                                           | $68.7^{+1.0}_{-1.0}$                                  | Expansion during matter domination        | $[1 + \tau_{\text{eq}}] (H_0 / h_{\text{eq}})^{1/2}$ [109]                                                                                                                                           |
| $\sigma_8$                                                      | $0.81^{+0.024}_{-0.024} \times 10^{-3}$               | Seed amplitude on galaxy scale            | Like $\sigma_8$ but on galaxy ( $M = 10^{12} M_\odot$ ) scale early on                                                                                                                               |
| <b>CMB anisotropy parameters:</b>                               |                                                       |                                           |                                                                                                                                                                                                      |
| $A_{\text{peak}}$                                               | $0.578^{+0.013}_{-0.013}$                             | Amplitude on CMB peak scale               | $A_{\text{peak}} = A_s \kappa^{-2\alpha}$                                                                                                                                                            |
| $A_{\text{QCD}}$                                                | $0.508^{+0.012}_{-0.012}$                             | Amplitude at pivot point                  | $A_{\text{QCD}}$ scaled to $h = 0.002 \text{ Mpc}^{-1}$ , $A_{\text{QCD}} = 0.26^{n-1} A_{\text{peak}}$ if $n \neq 0$                                                                                |
| $R_1$                                                           | $4.68^{+0.27}_{-0.24}$                                | 1st CMB peak ratio                        | $R_1(\Omega_{\text{tot}}, \Omega_b, \omega_m, \omega_c, \omega_\nu, \tau)$ given by (10)                                                                                                             |
| $R_2$                                                           | $0.920^{+0.0021}_{-0.0021}$                           | 2nd to 1st CMB peak ratio                 | $R_2 = (0.920 \Omega_b^2 \Omega_m^2 \omega_m^{-2} / (1 + (\omega_b / 0.0042)^{2-2n}))^{1/2}$ [110]                                                                                                   |
| $R_3$                                                           | $0.420^{+0.0099}_{-0.0099}$                           | 3rd to 1st CMB peak ratio                 | $R_3 = 2.171 + (\omega_b / 0.0042)^{1/2} - \tau_{\text{eq}} 0.509 \omega_m^{-1/2} / (1 + 0.03(1 - \omega_b / 0.071) \tau_{\text{eq}})$                                                               |
| $d_A(z_{\text{obs}})$                                           | $14.38^{+0.17}_{-0.17}$ Gpc                           | Comoving angular diameter distance to CMB | $d_A(z_{\text{obs}}) = \frac{1}{H_0} \sin \left[ \frac{1}{H_0} \int_{\tau_{\text{obs}}}^{\infty} \frac{dt}{a(t)} \frac{H(t)}{H(z_{\text{obs}})} \right] / \Omega_\Lambda^{1/2}$ [108]                |
| $\tau_{\text{obs}}(z_{\text{obs}})$                             | $0.186^{+0.0014}_{-0.0014}$ Gpc                       | Comoving sound horizon scale              | $\tau_{\text{obs}}(\omega_m, \omega_b)$ given by eq. (22) of [106]                                                                                                                                   |
| $\tau_{\text{QCD}}(z_{\text{obs}})$                             | $0.3872^{+0.0009}_{-0.0009}$ Gpc                      | Comoving acoustic damping scale           | $\tau_{\text{QCD}}(z_{\text{obs}}, \omega_b)$ given by eq. (28) of [106]                                                                                                                             |
| $\theta_{\text{QCD}}$                                           | $0.5104^{+0.0020}_{-0.0020}$                          | CMB acoustic angle scale fit (degrees)    | $\theta_{\text{QCD}}(\Omega_{\text{tot}}, \Omega_b, \omega_m, \omega_c, \omega_\nu)$ given by (11)                                                                                                   |
| $\theta_8$                                                      | $360.3^{+1.0}_{-1.0}$                                 | CMB acoustic angle scale                  | $\theta_8 = \pi \theta_{\text{QCD}}(z_{\text{obs}}) / \tau_8(z_{\text{obs}})$                                                                                                                        |

(Universe fact sheet handout)





$\sigma_8$

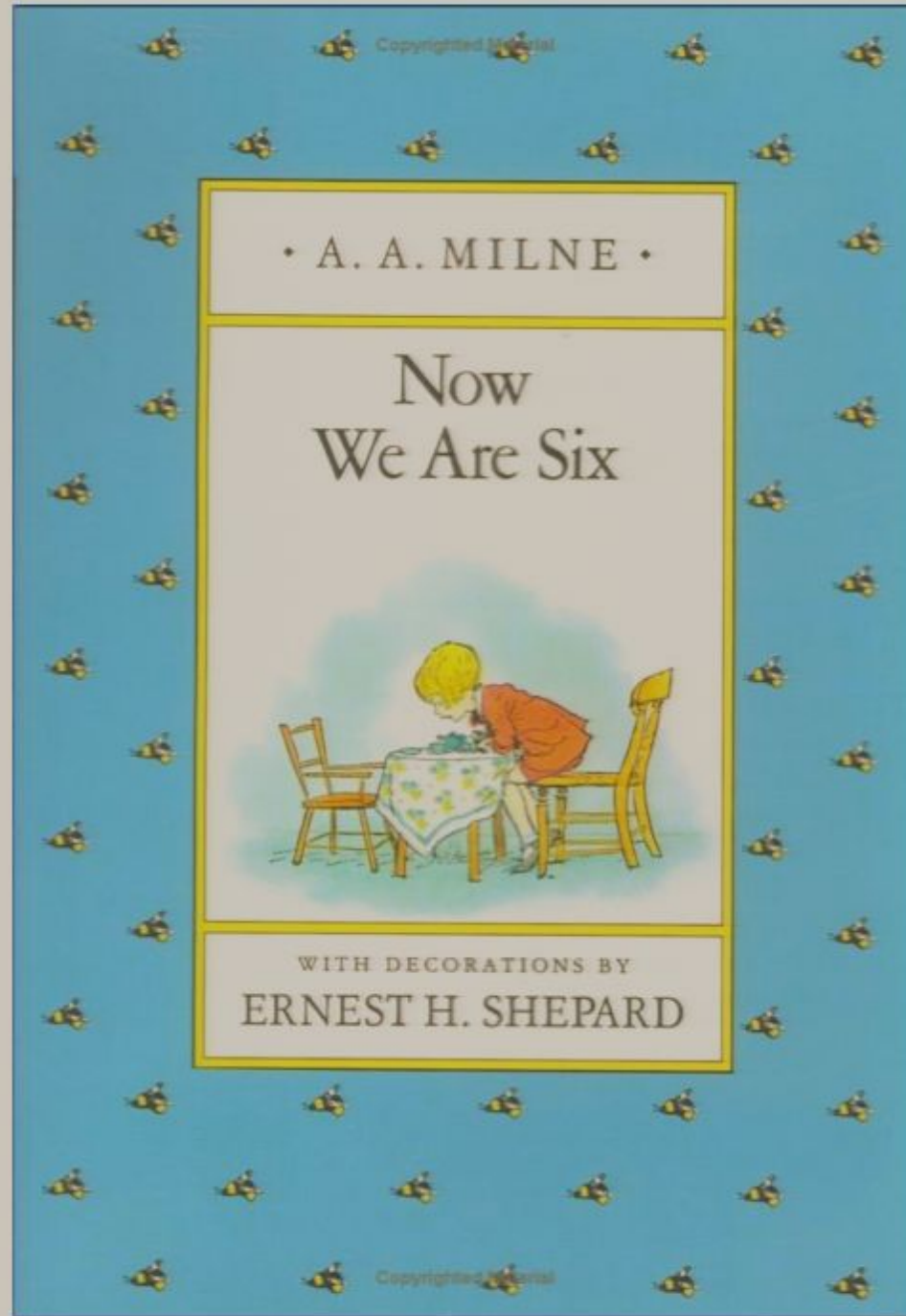
$n_s$

$\Omega_\Lambda$

$\omega_m$

$\omega_b$

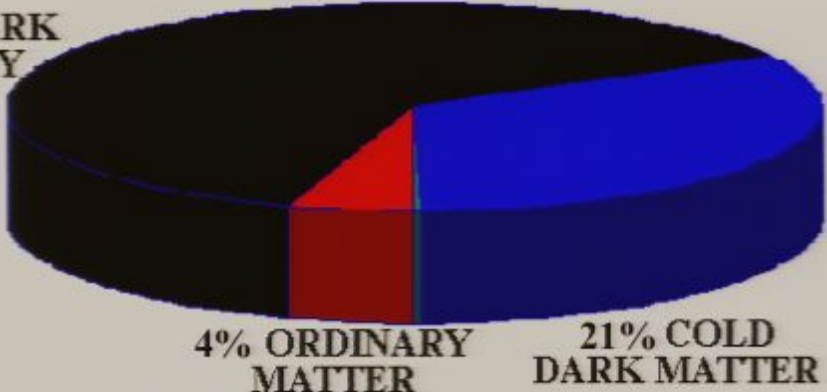
$\tau$



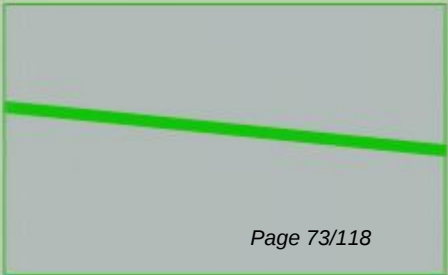
Using  
WMAP3 +  
SDSS LRGs:

- Ordinary Matter
- Dark Energy
- Cold Dark Matter
- Hot Dark Matter
- Photons
- Budget Deficit

75% DARK  
ENERGY



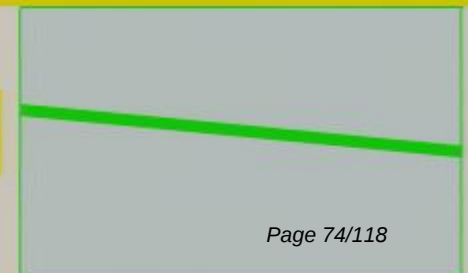
| Parameter                    | Value                        |                                |
|------------------------------|------------------------------|--------------------------------|
| Matter budget parameters:    |                              |                                |
| $\Omega_{\text{tot}}$        | $1.003^{+0.010}_{-0.009}$    | Total density/critical density |
| $\Omega_{\Lambda}$           | $0.761^{+0.017}_{-0.018}$    | Dark energy density parameter  |
| $\omega_b$                   | $0.0222^{+0.0007}_{-0.0007}$ | Baryon density                 |
| $\omega_c$                   | $0.1050^{+0.0041}_{-0.0040}$ | Cold dark matter density       |
| $\omega_{\nu}$               | $< 0.010$ (95%)              | Massive neutrino density       |
| $w$                          | $-0.941^{+0.087}_{-0.101}$   | Dark energy equation of state  |
| Seed fluctuation parameters: |                              |                                |
| $A_s$                        | $0.690^{+0.045}_{-0.044}$    | Scalar fluctuation amplitude   |
| $r$                          | $< 0.30$ (95%)               | Tensor-to-scalar ratio         |
| $n_s$                        | $0.953^{+0.016}_{-0.016}$    | Scalar spectral index          |
| $n_t + 1$                    | $0.9861^{+0.0096}_{-0.0142}$ | Tensor spectral index          |
| $\alpha$                     | $-0.040^{+0.027}_{-0.027}$   | Running of spectral index      |

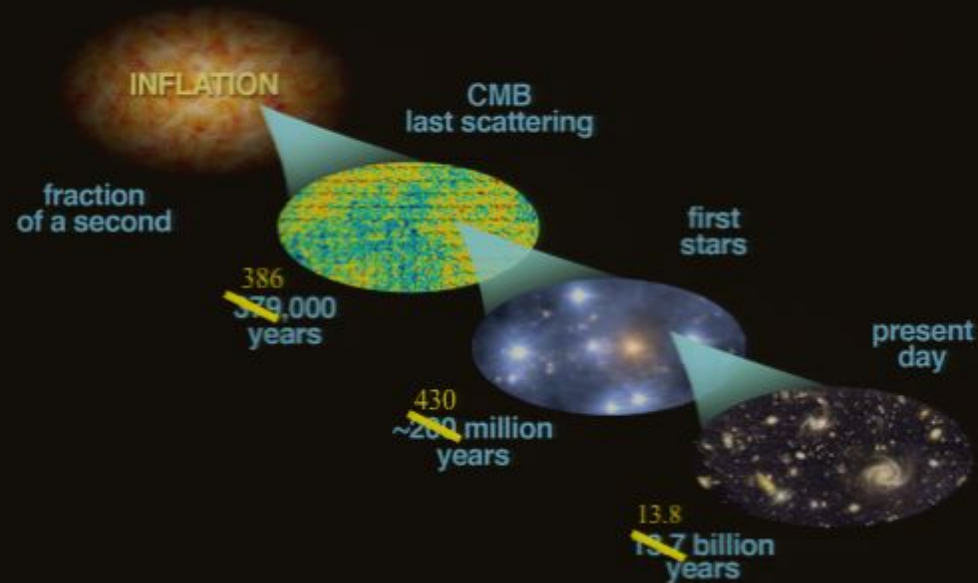


## No strong evidence against “vanilla”:



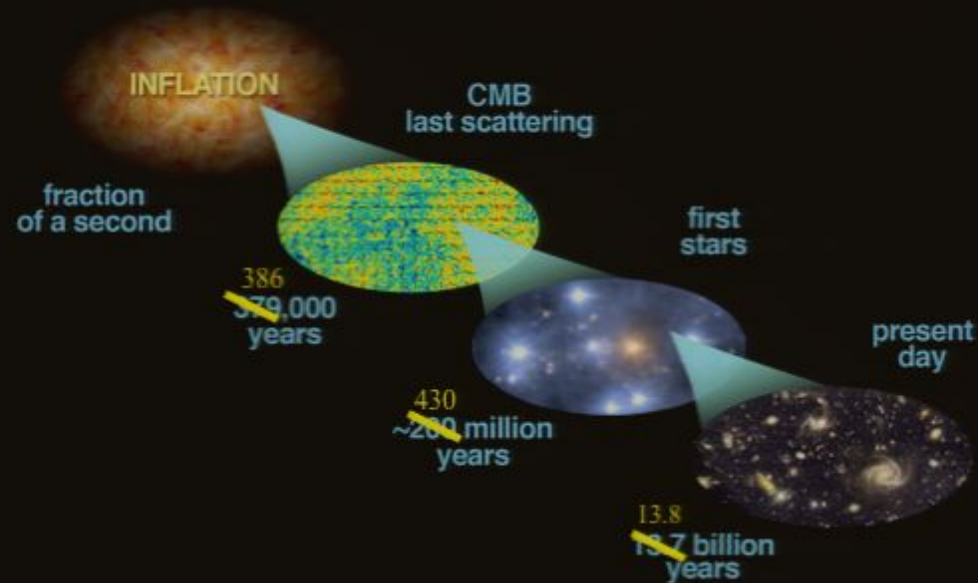
| Parameter                    | Value                        | Meaning                        |
|------------------------------|------------------------------|--------------------------------|
| Matter budget parameters:    |                              |                                |
| $\Omega_{\text{tot}}$        | 1                            | Total density/critical density |
| $\Omega_{\Lambda}$           | $0.755^{+0.019}_{-0.021}$    | Dark energy density parameter  |
| $\omega_d$                   | $0.1065^{+0.0045}_{-0.0044}$ | Dark matter density            |
| $\omega_b$                   | $0.0222^{+0.0007}_{-0.0007}$ | Baryon density                 |
| $\omega_{\nu}$               | 0                            | Massive neutrino density       |
| $w$                          | -1                           | Dark energy equation of state  |
| Seed fluctuation parameters: |                              |                                |
| $A_s$                        | $0.693^{+0.045}_{-0.045}$    | Scalar fluctuation amplitude   |
| $r$                          | 0                            | Tensor-to-scalar ratio         |
| $n_s$                        | $0.953^{+0.016}_{-0.016}$    | Scalar spectral index          |
| $n_t + 1$                    |                              | Tensor spectral index          |
| $\alpha$                     | 0                            | Running of spectral index      |





### Cosmic history parameters:

|                  |                                  |                                    |
|------------------|----------------------------------|------------------------------------|
| $z_{\text{eq}}$  | $3057^{+105}_{-102}$             | Matter-radiation Equality redshift |
| $z_{\text{rec}}$ | $1090.25^{+0.93}_{-0.91}$        | Recombination redshift             |
| $z_{\text{ion}}$ | $11.1^{+2.2}_{-2.7}$             | Reionization redshift (abrupt)     |
| $z_{\text{acc}}$ | $0.855^{+0.059}_{-0.059}$        | Acceleration redshift              |
| $t_{\text{eq}}$  | $0.0634^{+0.0045}_{-0.0041}$ Myr | Matter-radiation Equality time     |
| $t_{\text{rec}}$ | $0.3856^{+0.0040}_{-0.0040}$ Myr | Recombination time                 |
| $t_{\text{ion}}$ | $0.43^{+0.20}_{-0.10}$ Gyr       | Reionization time                  |
| $t_{\text{acc}}$ | $6.74^{+0.25}_{-0.24}$ Gyr       | Acceleration time                  |
| $t_{\text{now}}$ | $13.76^{+0.15}_{-0.15}$ Gyr      | Age of Universe now                |



### Cosmic history parameters:

|                  |                                  |                                    |
|------------------|----------------------------------|------------------------------------|
| $z_{\text{eq}}$  | $3057^{+105}_{-102}$             | Matter-radiation Equality redshift |
| $z_{\text{rec}}$ | $1090.25^{+0.93}_{-0.91}$        | Recombination redshift             |
| $z_{\text{ion}}$ | $11.1^{+2.2}_{-2.7}$             | Reionization redshift (abrupt)     |
| $z_{\text{acc}}$ | $0.855^{+0.059}_{-0.059}$        | Acceleration redshift              |
| $t_{\text{eq}}$  | $0.0634^{+0.0045}_{-0.0041}$ Myr | Matter-radiation Equality time     |
| $t_{\text{rec}}$ | $0.3856^{+0.0040}_{-0.0040}$ Myr | Recombination time                 |
| $t_{\text{ion}}$ | $0.43^{+0.20}_{-0.10}$ Gyr       | Reionization time                  |
| $t_{\text{acc}}$ | $6.74^{+0.25}_{-0.24}$ Gyr       | Acceleration time                  |
| $t_{\text{now}}$ | $13.76^{+0.15}_{-0.15}$ Gyr      | Age of Universe now                |

Other popular parameters (determined by those above):

|                           |                               |                                   |
|---------------------------|-------------------------------|-----------------------------------|
| $h$                       | $0.730^{+0.019}_{-0.019}$     | Hubble parameter                  |
| $\Omega_m$                | $0.239^{+0.018}_{-0.017}$     | Matter density/critical density   |
| $\Omega_b$                | $0.0416^{+0.0019}_{-0.0018}$  | Baryon density/critical density   |
| $\Omega_c$                | $0.197^{+0.016}_{-0.015}$     | CDM density/critical density      |
| $\Omega_\nu$              | $< 0.024$ (95%)               | Neutrino density/critical density |
| $\Omega_k$                | $-0.0030^{+0.0095}_{-0.0102}$ | Spatial curvature                 |
| $\omega_m$                | $0.1272^{+0.0044}_{-0.0043}$  | Matter density                    |
| $f_\nu$                   | $< 0.090$ (95%)               | Dark matter neutrino fraction     |
| $A_t$                     | $< 0.21$ (95%)                | Tensor fluctuation amplitude      |
| $M_\nu$                   | $< 0.94$ (95%) eV             | Sum of neutrino masses            |
| $A_{.002}$                | $0.801^{+0.042}_{-0.043}$     | WMAP3 normalization parameter     |
| $r_{.002}$                | $< 0.33$ (95%)                | Tensor-to-scalar ratio (WMAP3)    |
| $\sigma_8$                | $0.756^{+0.035}_{-0.035}$     | Density fluctuation amplitude     |
| $\sigma_8 \Omega_m^{0.6}$ | $0.320^{+0.024}_{-0.023}$     | Velocity fluctuation amplitude    |

| Fundamental parameters (independent of observing epoch): |                                                          |                                       |
|----------------------------------------------------------|----------------------------------------------------------|---------------------------------------|
| $Q$                                                      | $1.945^{+0.051}_{-0.053} \times 10^{-5}$                 | Primordial fluctuation amplitude      |
| $\kappa$                                                 | $1.3^{+3.7}_{-4.3} \times 10^{-61}$                      | Dimensionless spatial curvature [110] |
| $\rho_{\Lambda}$                                         | $1.48^{+0.11}_{-0.11} \times 10^{-123} \rho_{\text{Pl}}$ | Dark energy density                   |
| $\rho_{\text{halo}}$                                     | $6.6^{+1.2}_{-1.0} \times 10^{-123} \rho_{\text{Pl}}$    | Halo formation density                |
| $\xi$                                                    | $3.26^{+0.11}_{-0.11} \text{ eV}$                        | Matter mass per photon                |
| $\xi_b$                                                  | $0.569^{+0.018}_{-0.018} \text{ eV}$                     | Baryon mass per photon                |
| $\xi_c$                                                  | $2.69^{+0.11}_{-0.10} \text{ eV}$                        | CDM mass per photon                   |
| $\xi_{\nu}$                                              | $< 0.26 \text{ (95\%) eV}$                               | Neutrino mass per photon              |
| $\eta$                                                   | $6.06^{+0.20}_{-0.19} \times 10^{-10}$                   | Baryon/photon ratio                   |
| $A_{\Lambda}$                                            | $2077^{+135}_{-125}$                                     | Expansion during matter domination    |
| $\sigma_{\text{gal}}^*$                                  | $0.561^{+0.024}_{-0.023} \times 10^{-3}$                 | Seed amplitude on galaxy scale        |

Other popular parameters (determined by those above):

|                           |                               |                                   |
|---------------------------|-------------------------------|-----------------------------------|
| $h$                       | $0.730^{+0.019}_{-0.019}$     | Hubble parameter                  |
| $\Omega_m$                | $0.239^{+0.018}_{-0.017}$     | Matter density/critical density   |
| $\Omega_b$                | $0.0416^{+0.0019}_{-0.0018}$  | Baryon density/critical density   |
| $\Omega_c$                | $0.197^{+0.016}_{-0.015}$     | CDM density/critical density      |
| $\Omega_\nu$              | $< 0.024$ (95%)               | Neutrino density/critical density |
| $\Omega_k$                | $-0.0030^{+0.0095}_{-0.0102}$ | Spatial curvature                 |
| $\omega_m$                | $0.1272^{+0.0044}_{-0.0043}$  | Matter density                    |
| $f_\nu$                   | $< 0.090$ (95%)               | Dark matter neutrino fraction     |
| $A_t$                     | $< 0.21$ (95%)                | Tensor fluctuation amplitude      |
| $M_\nu$                   | $< 0.94$ (95%) eV             | Sum of neutrino masses            |
| $A_{.002}$                | $0.801^{+0.042}_{-0.043}$     | WMAP3 normalization parameter     |
| $r_{.002}$                | $< 0.33$ (95%)                | Tensor-to-scalar ratio (WMAP3)    |
| $\sigma_8$                | $0.756^{+0.035}_{-0.035}$     | Density fluctuation amplitude     |
| $\sigma_8 \Omega_m^{0.6}$ | $0.320^{+0.024}_{-0.023}$     | Velocity fluctuation amplitude    |

Fundamental parameters (independent of observing epoch):

|                         |                                                          |                                       |
|-------------------------|----------------------------------------------------------|---------------------------------------|
| $Q$                     | $1.945^{+0.051}_{-0.053} \times 10^{-5}$                 | Primordial fluctuation amplitude      |
| $\kappa$                | $1.3^{+3.7}_{-4.3} \times 10^{-61}$                      | Dimensionless spatial curvature [110] |
| $\rho_{\Lambda}$        | $1.48^{+0.11}_{-0.11} \times 10^{-123} \rho_{\text{Pl}}$ | Dark energy density                   |
| $\rho_{\text{halo}}$    | $6.6^{+1.2}_{-1.0} \times 10^{-123} \rho_{\text{Pl}}$    | Halo formation density                |
| $\xi$                   | $3.26^{+0.11}_{-0.11} \text{ eV}$                        | Matter mass per photon                |
| $\xi_b$                 | $0.569^{+0.018}_{-0.018} \text{ eV}$                     | Baryon mass per photon                |
| $\xi_c$                 | $2.69^{+0.11}_{-0.10} \text{ eV}$                        | CDM mass per photon                   |
| $\xi_{\nu}$             | $< 0.26 \text{ (95\%) eV}$                               | Neutrino mass per photon              |
| $\eta$                  | $6.06^{+0.20}_{-0.19} \times 10^{-10}$                   | Baryon/photon ratio                   |
| $A_{\Lambda}$           | $2077^{+135}_{-125}$                                     | Expansion during matter domination    |
| $\sigma_{\text{gal}}^*$ | $0.561^{+0.024}_{-0.023} \times 10^{-3}$                 | Seed amplitude on galaxy scale        |

# Standard model parameters:

Particle physics

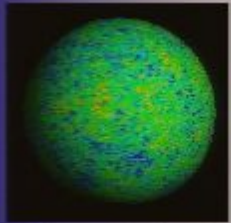
Cosmology

Required

Optional

| Parameter             | Meaning                                                                    | Measured value                    |
|-----------------------|----------------------------------------------------------------------------|-----------------------------------|
| $g$                   | Weak coupling constant at $M_Z$                                            | 0.6425                            |
| $\theta_W$            | Weinberg angle                                                             | 0.4908                            |
| $g_s$                 | Strong coupling constant                                                   | $\approx 1.2$                     |
| $\mu^2$               | Quadratic Higgs coefficient                                                | $\sim -10^{-33}$                  |
| $\lambda$             | Quartic Higgs coefficient                                                  | $\sim 17$                         |
| $G_e$                 | Electron Yukawa coupling                                                   | $2.94 \times 10^{-6}$             |
| $G_\mu$               | Muon Yukawa coupling                                                       | 0.000607                          |
| $G_\tau$              | Tauon Yukawa coupling                                                      | 0.0102156233                      |
| $G_u$                 | Up quark Yukawa coupling                                                   | $0.000016 \pm 0.000007$           |
| $G_d$                 | Down quark Yukawa coupling                                                 | $0.00003 \pm 0.00002$             |
| $G_c$                 | Charm quark Yukawa coupling                                                | $0.0072 \pm 0.0006$               |
| $G_s$                 | Strange quark Yukawa coupling                                              | $0.0006 \pm 0.0002$               |
| $G_t$                 | Top quark Yukawa coupling                                                  | $1.002 \pm 0.029$                 |
| $G_b$                 | Bottom quark Yukawa coupling                                               | $0.026 \pm 0.003$                 |
| $\sin \theta_{12}$    | Quark CKM matrix angle                                                     | $0.2243 \pm 0.0016$               |
| $\sin \theta_{23}$    | Quark CKM matrix angle                                                     | $0.0413 \pm 0.0015$               |
| $\sin \theta_{13}$    | Quark CKM matrix angle                                                     | $0.0037 \pm 0.0005$               |
| $\delta_{13}$         | Quark CKM matrix phase                                                     | $1.05 \pm 0.24$                   |
| $\theta_{\text{qcd}}$ | CP-violating QCD vacuum phase                                              | $< 10^{-9}$                       |
| $G_{\nu_e}$           | Electron neutrino Yukawa coupling                                          | $< 1.7 \times 10^{-11}$           |
| $G_{\nu_\mu}$         | Muon neutrino Yukawa coupling                                              | $< 1.1 \times 10^{-6}$            |
| $G_{\nu_\tau}$        | Tau neutrino Yukawa coupling                                               | $< 0.10$                          |
| ...                   | Neutrino mixing parameters                                                 |                                   |
| $\rho_\Lambda$        | Dark energy density                                                        | $(9.3 \pm 2.5) \times 10^{-124}$  |
| $\xi_b$               | Baryon mass per photon $\rho_b/n_\gamma$                                   | $(0.49 \pm 0.03) \times 10^{-28}$ |
| $\xi_c$               | Cold dark matter mass per photon $\rho_c/n_\gamma$                         | $(2.7 \pm 0.2) \times 10^{-28}$   |
| $\xi_\nu$             | Neutrino mass per photon $\rho_\nu/n_\gamma = \frac{3}{11} \sum m_{\nu_i}$ | $< 0.9 \times 10^{-28}$           |
| $Q$                   | Scalar fluctuation amplitude $\delta_H$ on horizon                         | $(2.0 \pm 0.2) \times 10^{-5}$    |
| $n_s$                 | Scalar spectral index                                                      | $0.98 \pm 0.02$                   |
| $\alpha_n$            | Running of spectral index $dn_s/d \ln k$                                   | $ \alpha  \lesssim 0.01$          |
| $r$                   | Tensor-to-scalar ratio $(Q_t/Q)^2$                                         | $\lesssim 0.36$                   |
| $n_t$                 | Tensor spectral index                                                      | Unconstrained                     |
| $\Omega_{\text{tot}}$ | Spatial curvature                                                          | $1.01 \pm 0.02$                   |
| $w$                   | Dark energy equation of state                                              | $-1 \pm 0.1$                      |

$$C = \hbar = G = k_b = q_e = 1$$



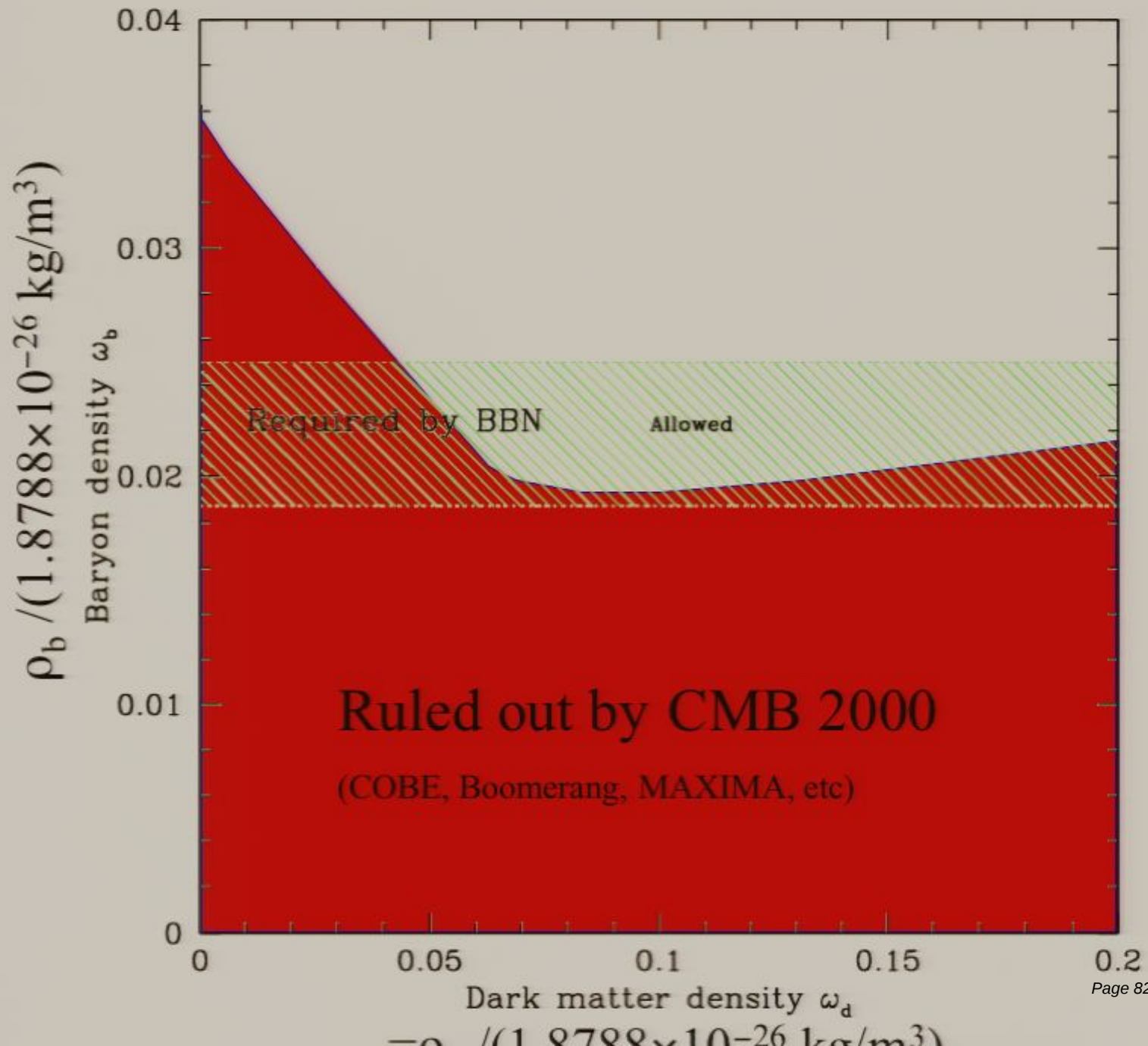
CMB

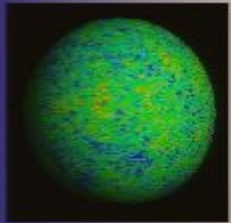
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P(k)

# How much dark matter is there?





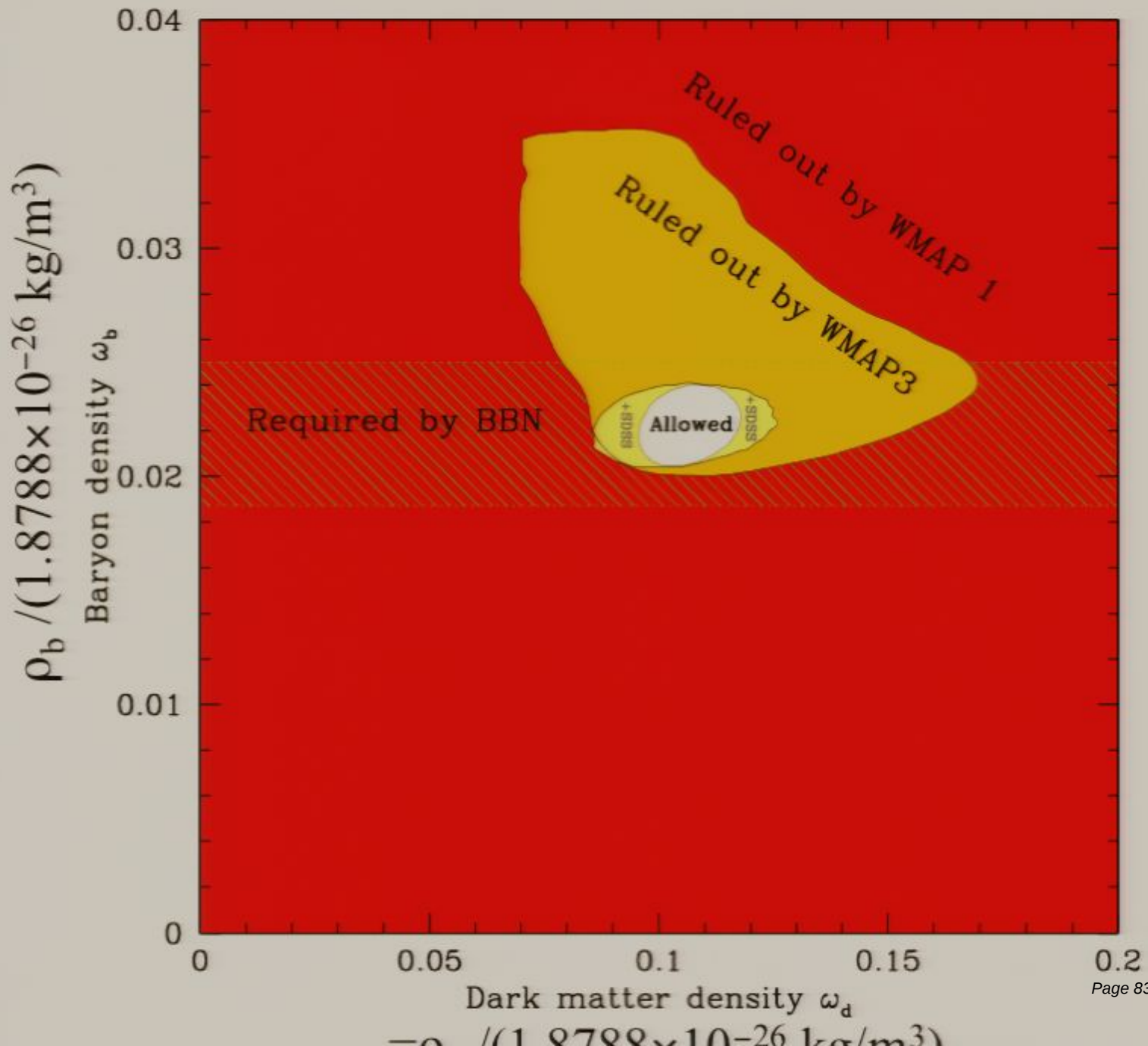
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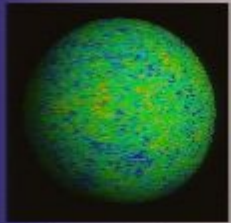
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P(k)

# How much dark matter is there?





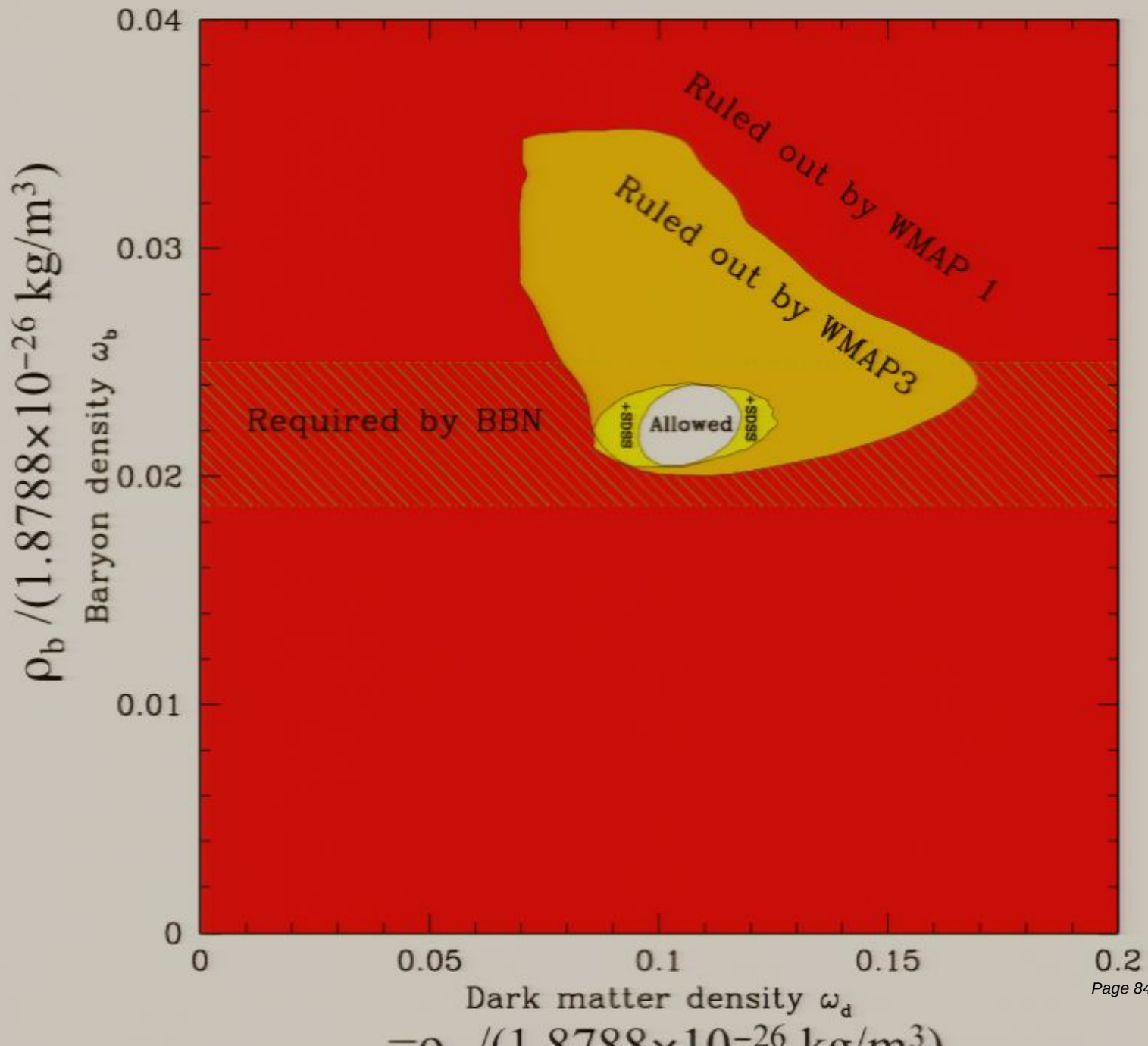
CMB

+



P(k)

# How much dark matter is there?

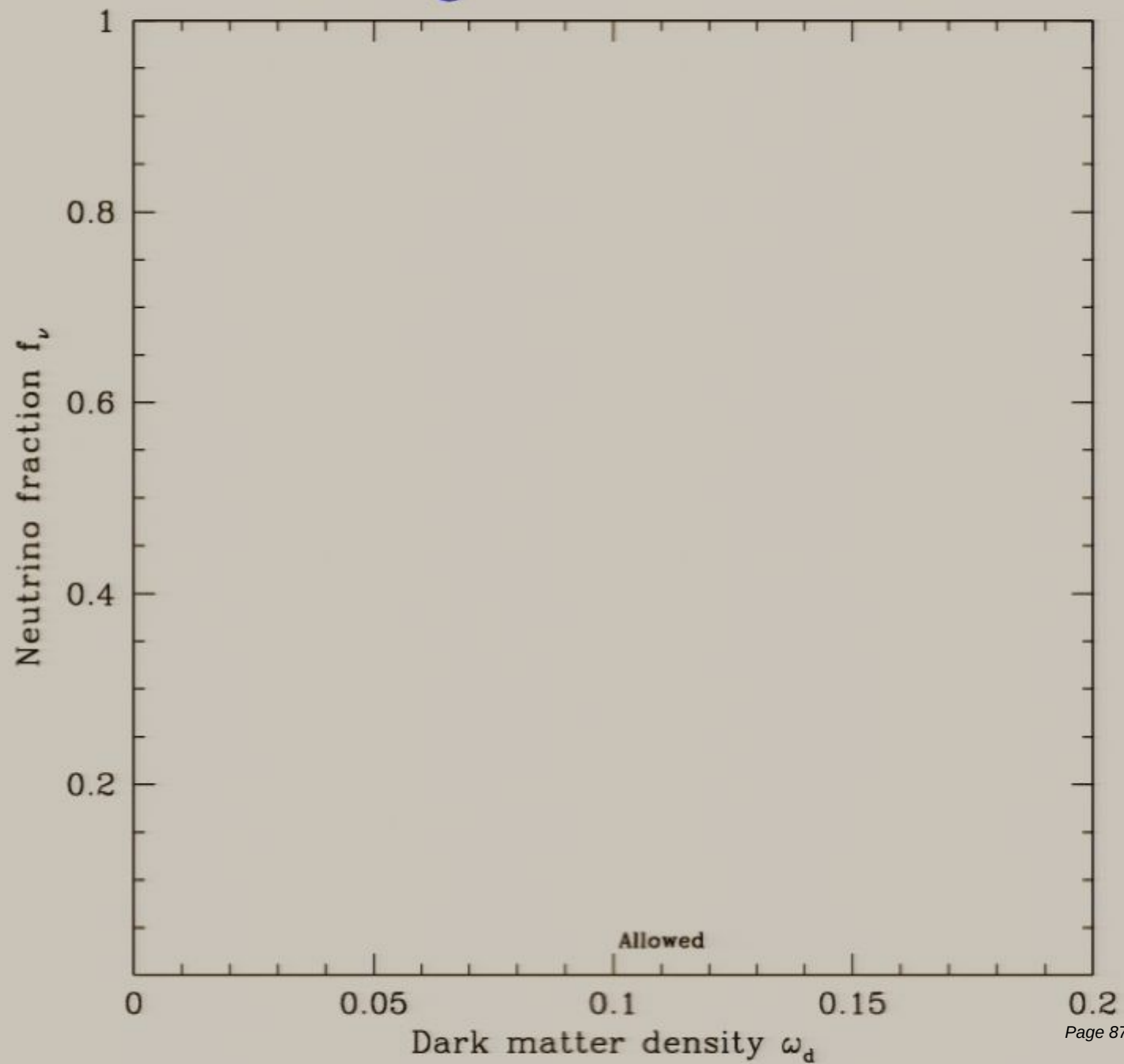


# Bullet Cluster, Clowe et al 2006, ApJ, 648, L109

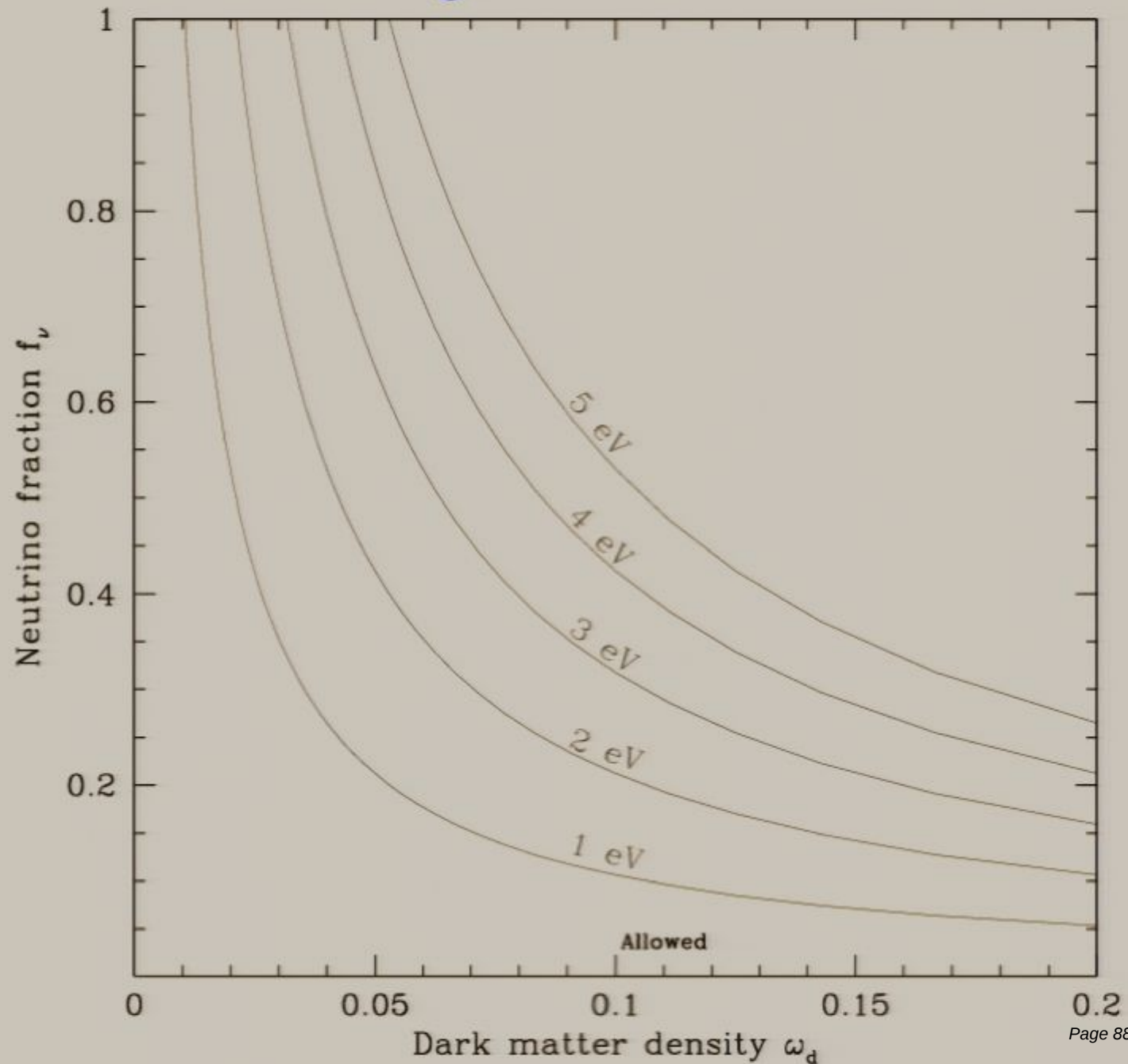


# Neutrinos

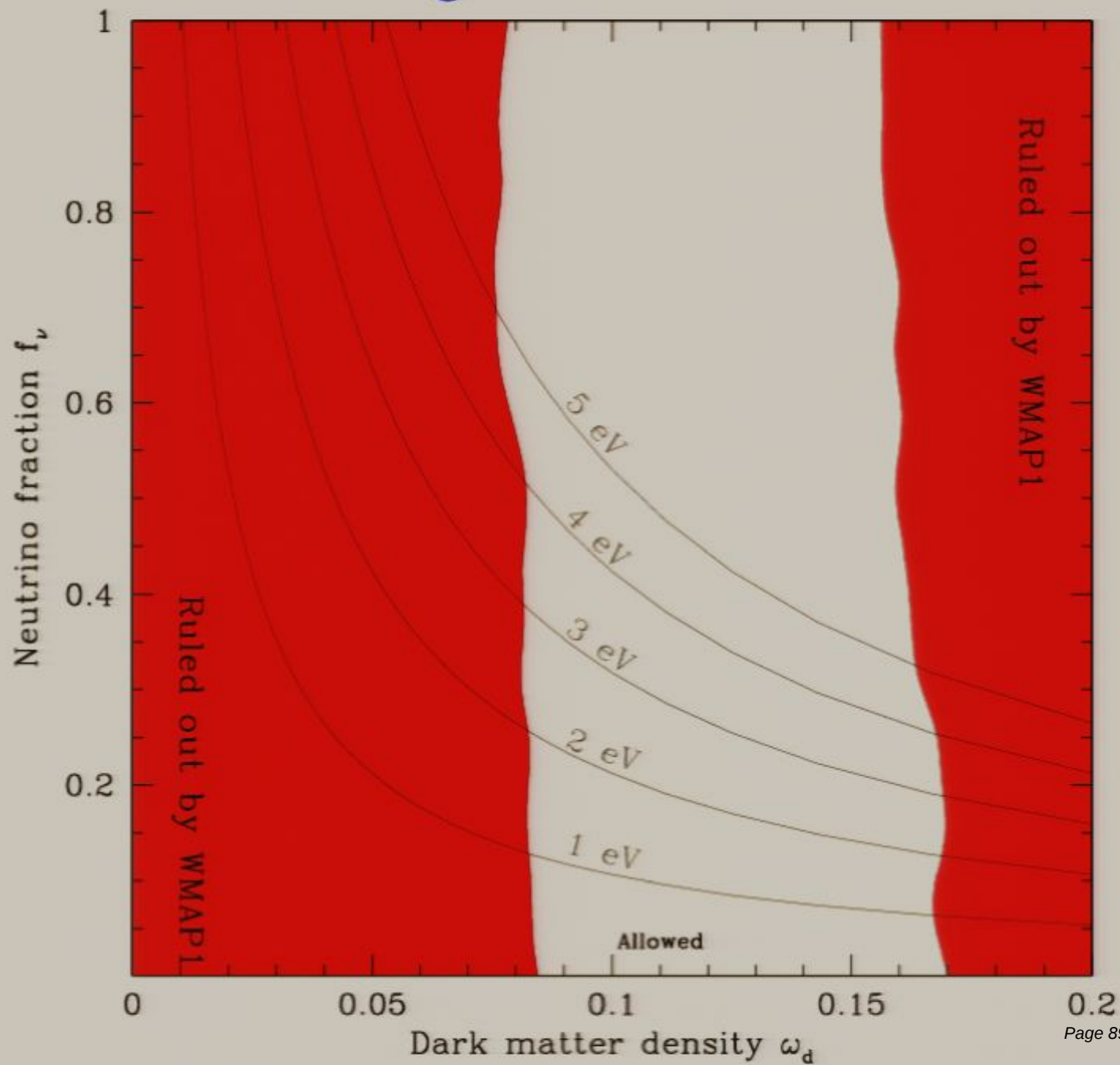
# Cosmological neutrino bounds



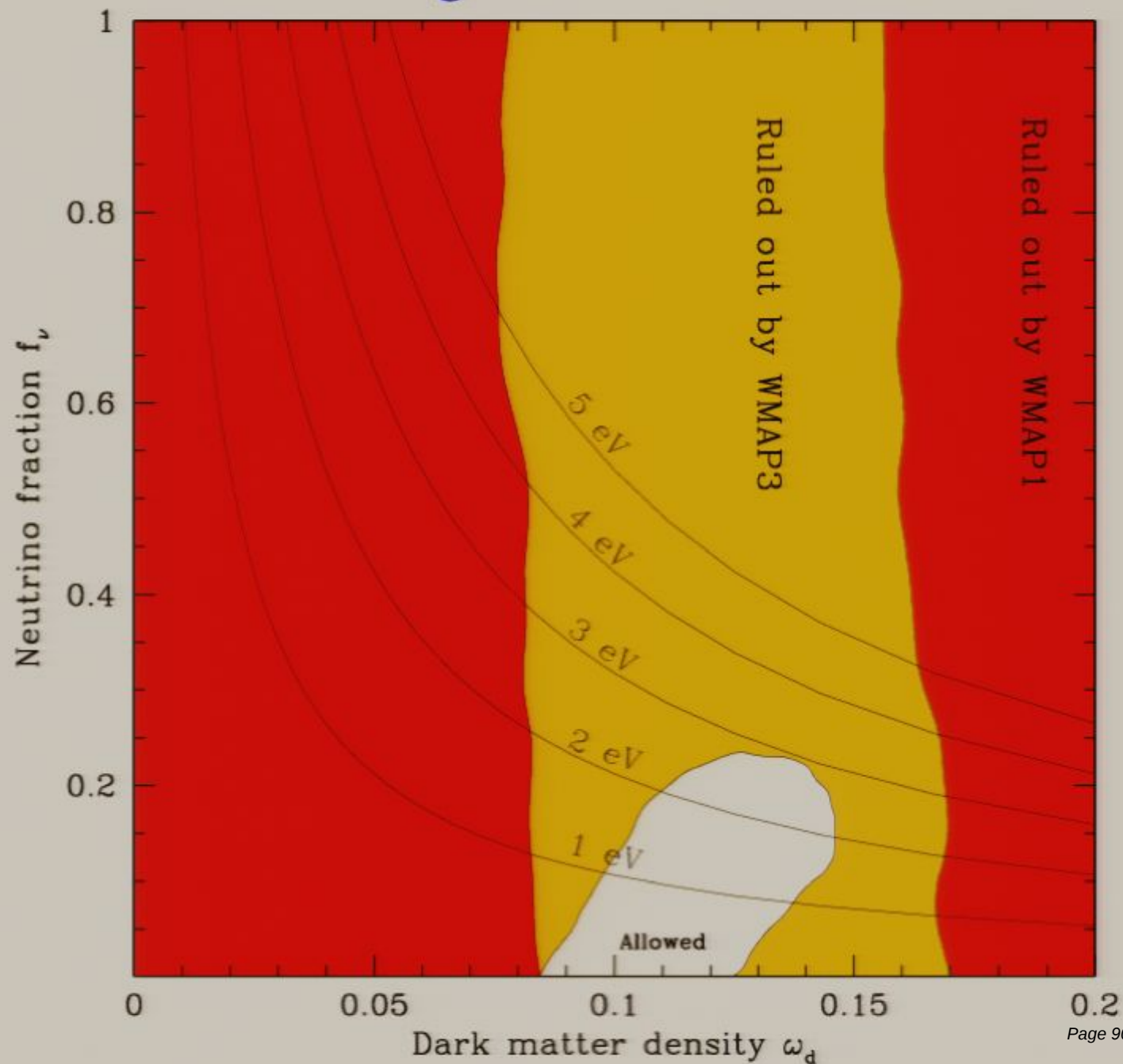
# Cosmological neutrino bounds



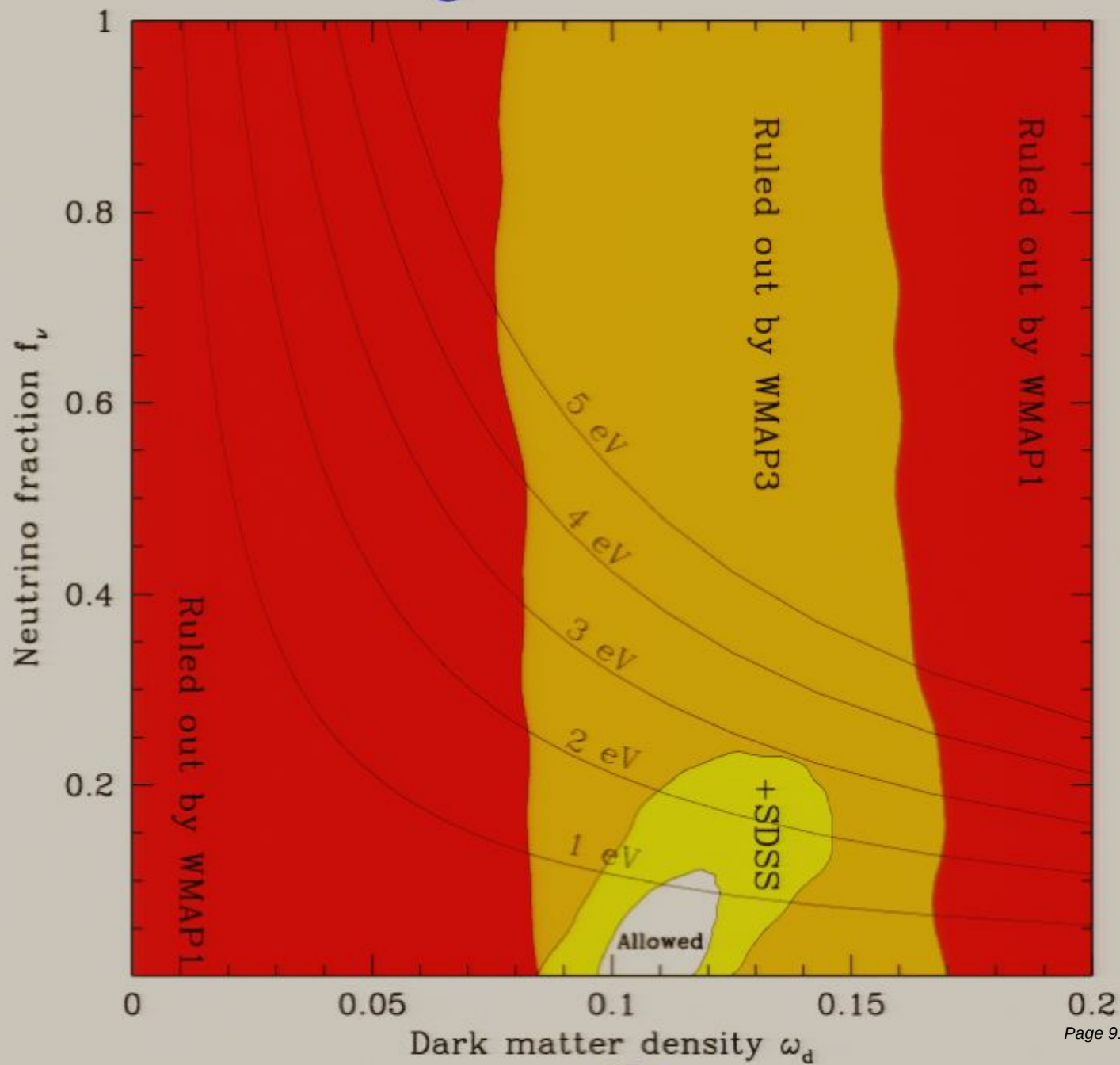
# Cosmological neutrino bounds



# Cosmological neutrino bounds

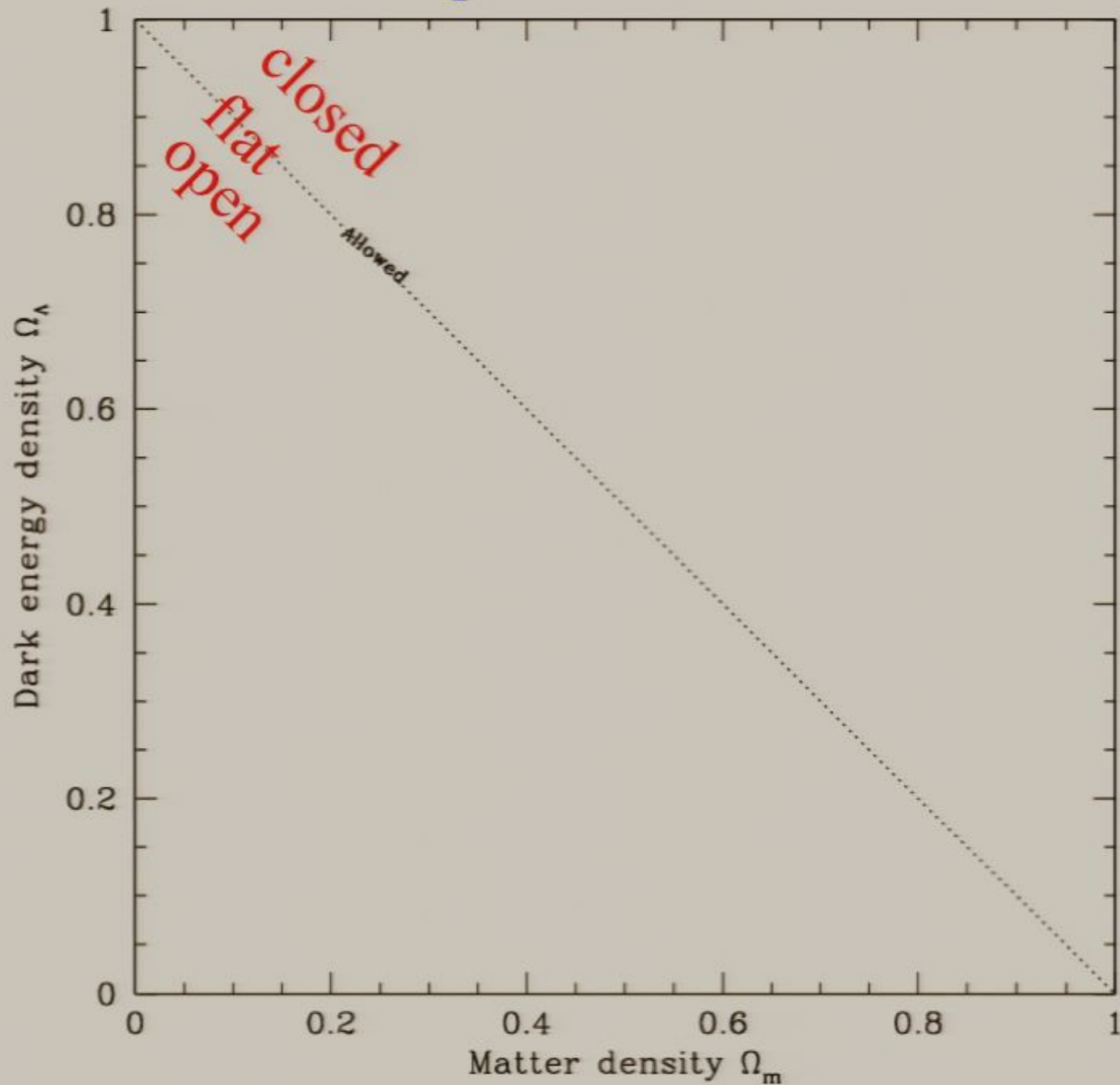


# Cosmological neutrino bounds

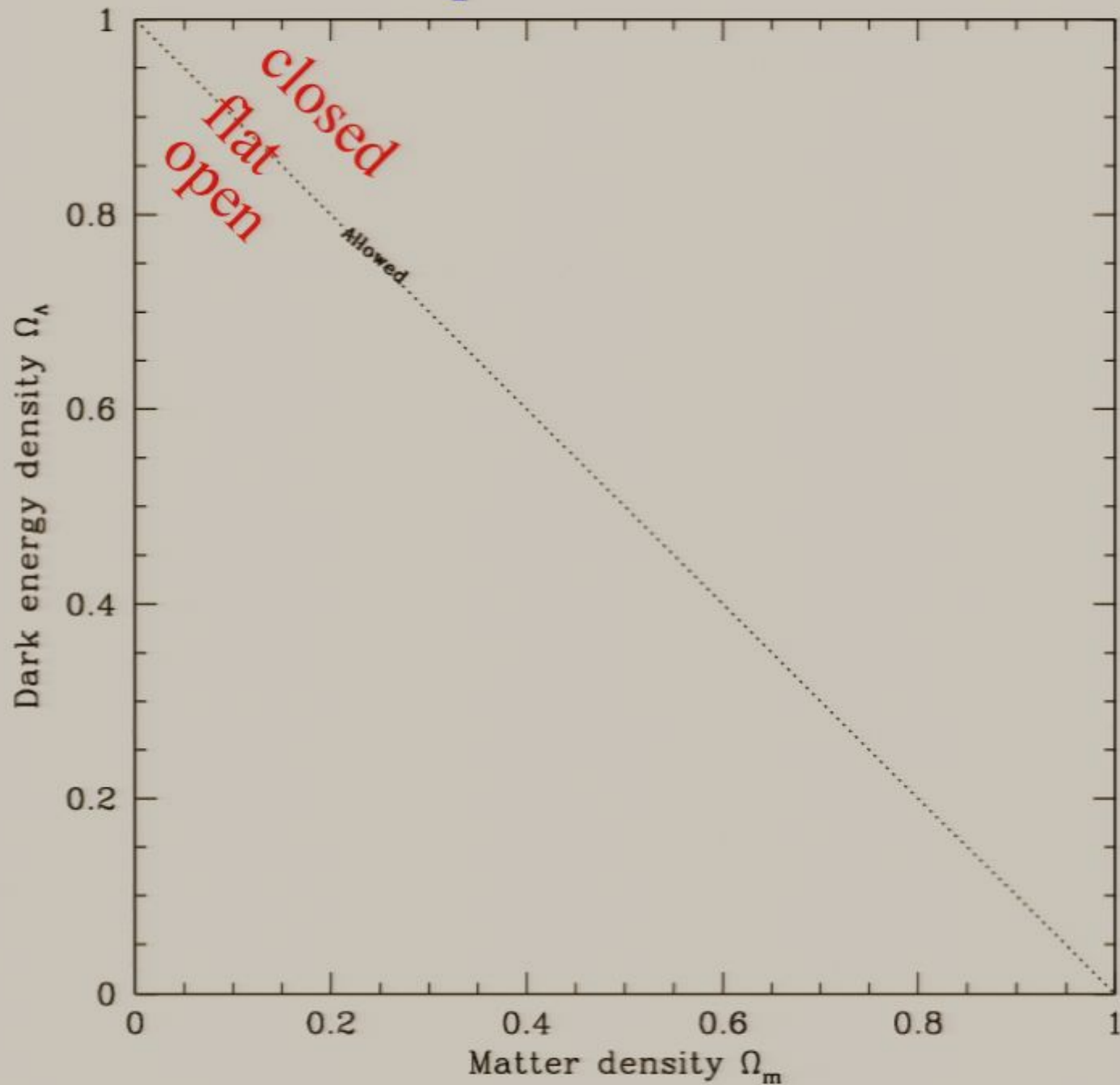


# Inflation

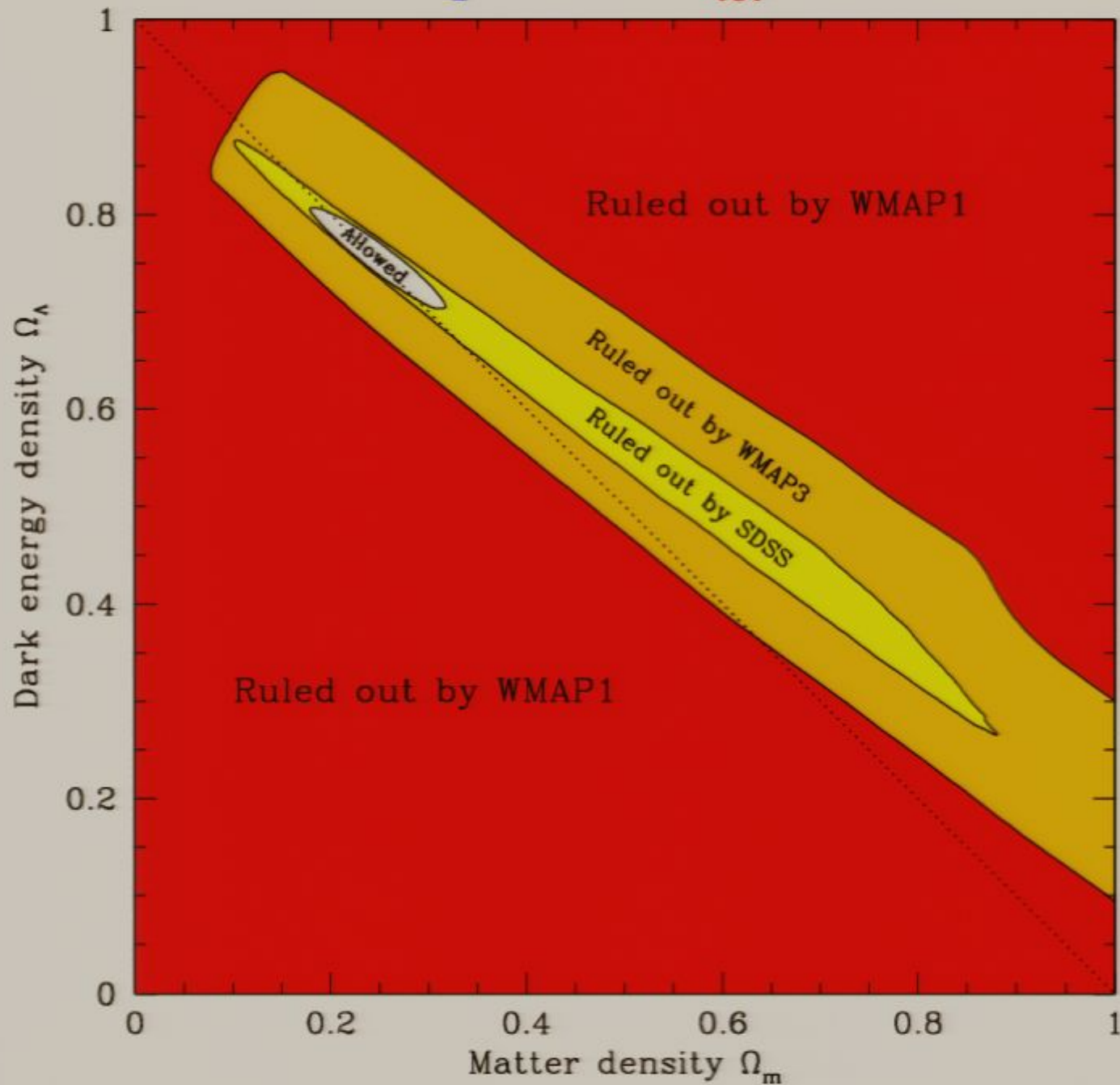
## How flat is space?

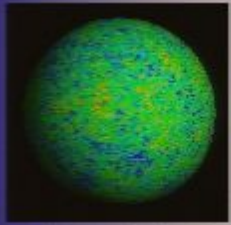


## How flat is space?



How flat is space?  $\Omega_{\text{tot}} = 1.003 \pm 0.010$



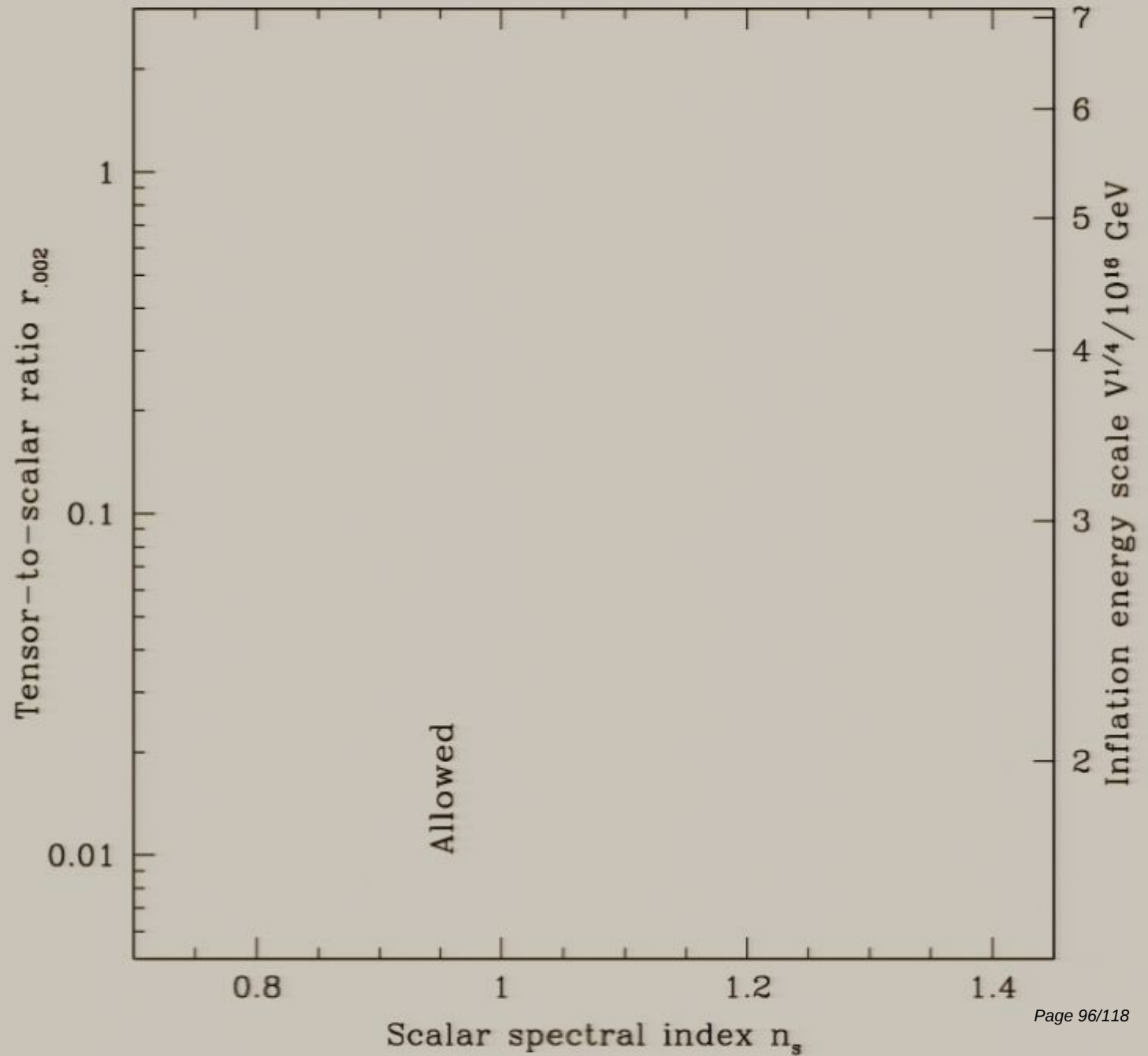


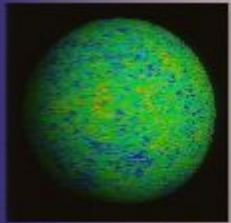
CMB

+



LSS



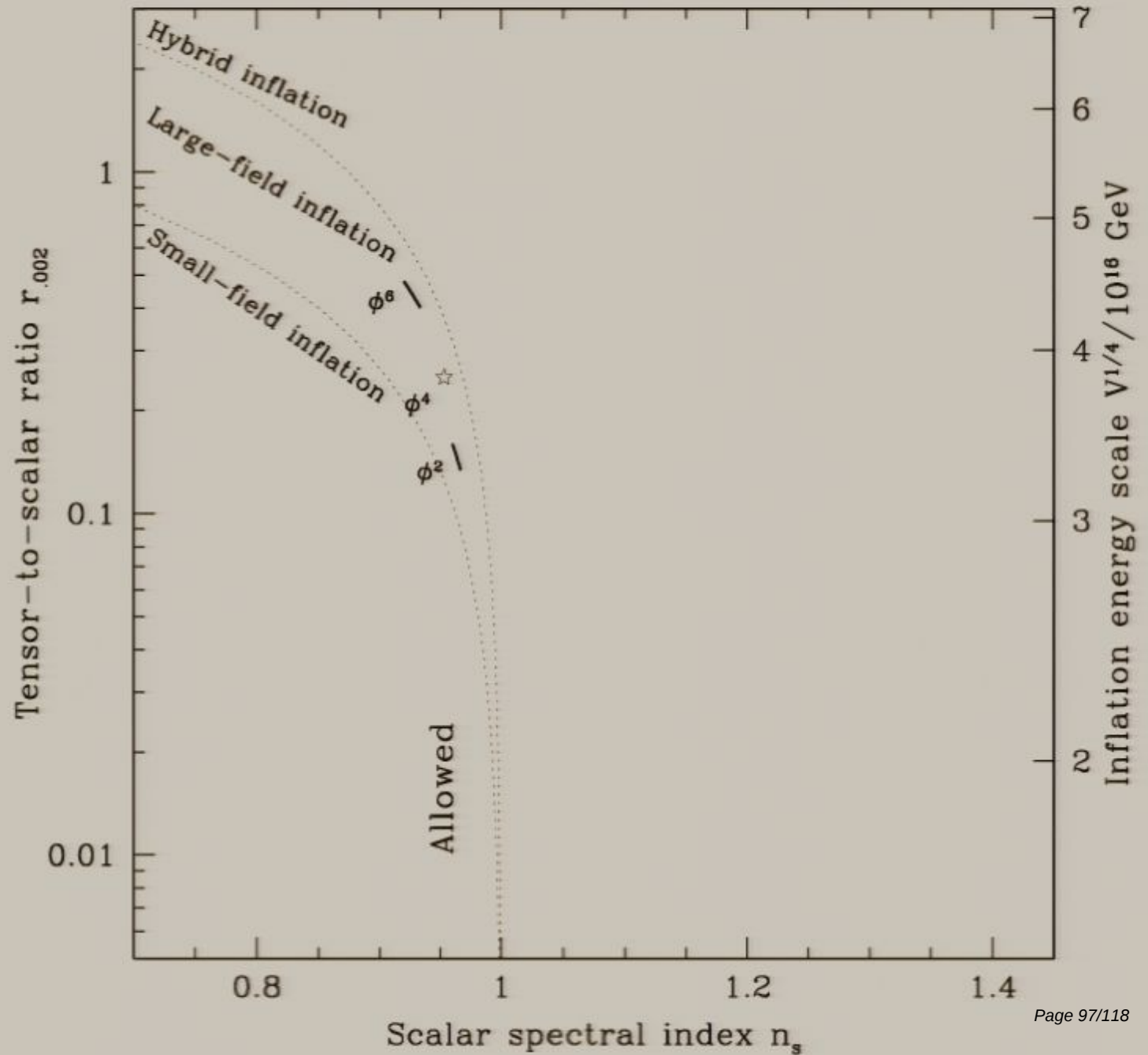


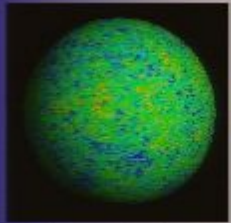
CMB

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LSS



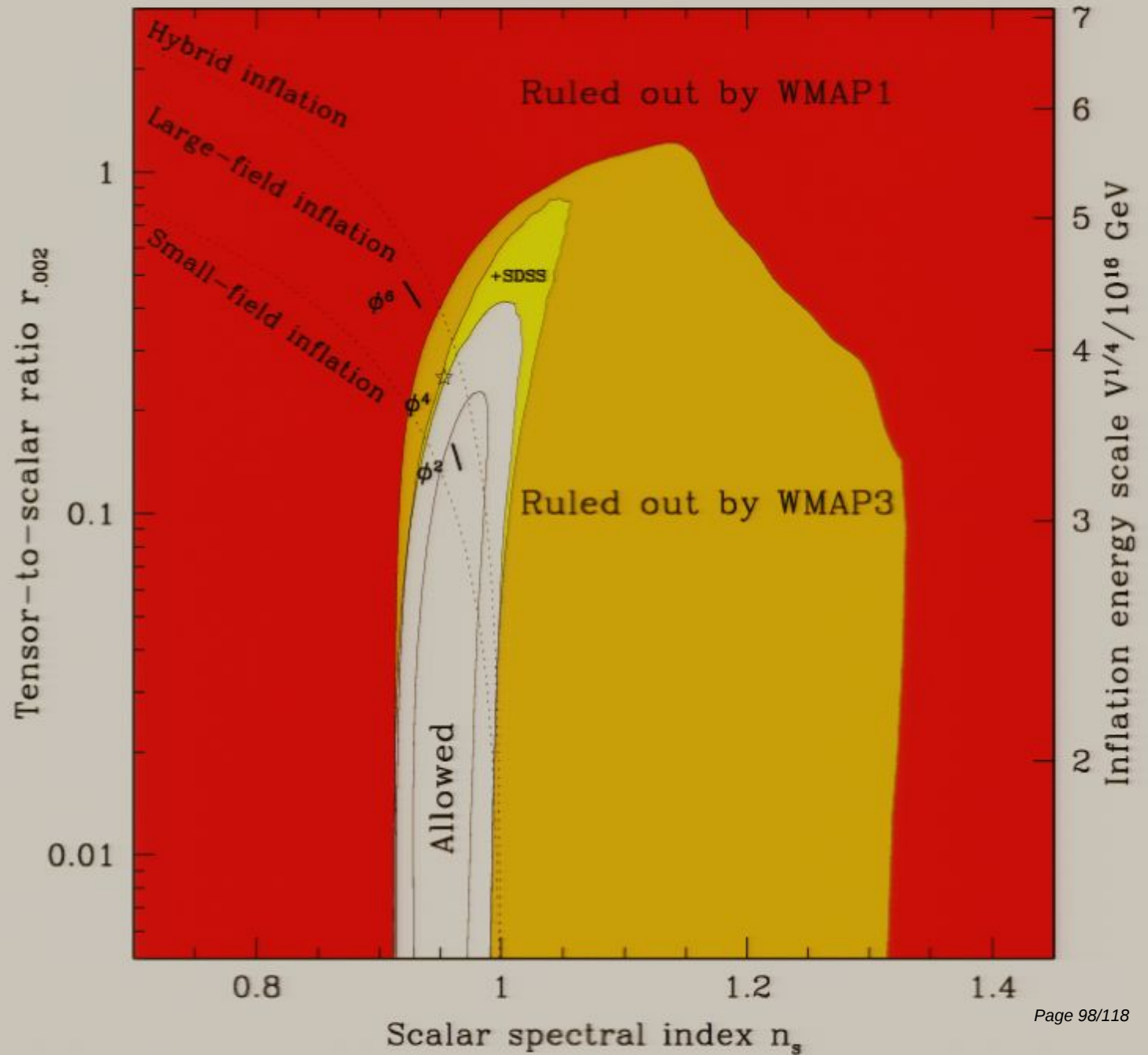


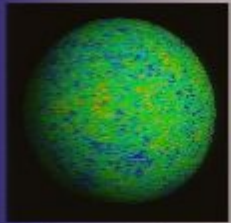
CMB

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LSS





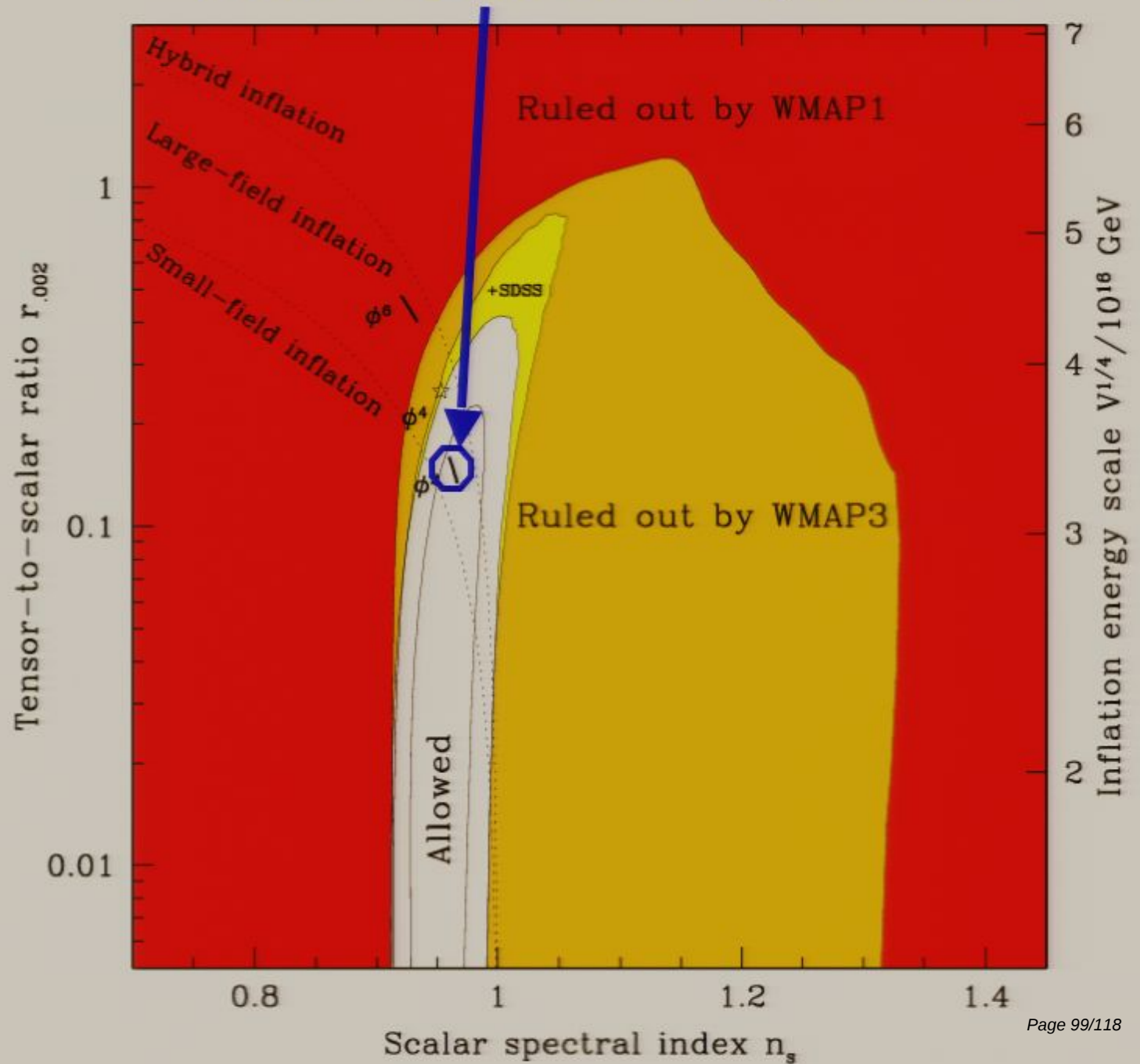
CMB

+

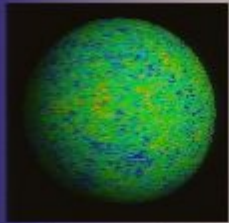


LSS

Planck + SDSS:  $\Delta n = 0.008$ ,  $\Delta r = 0.012$







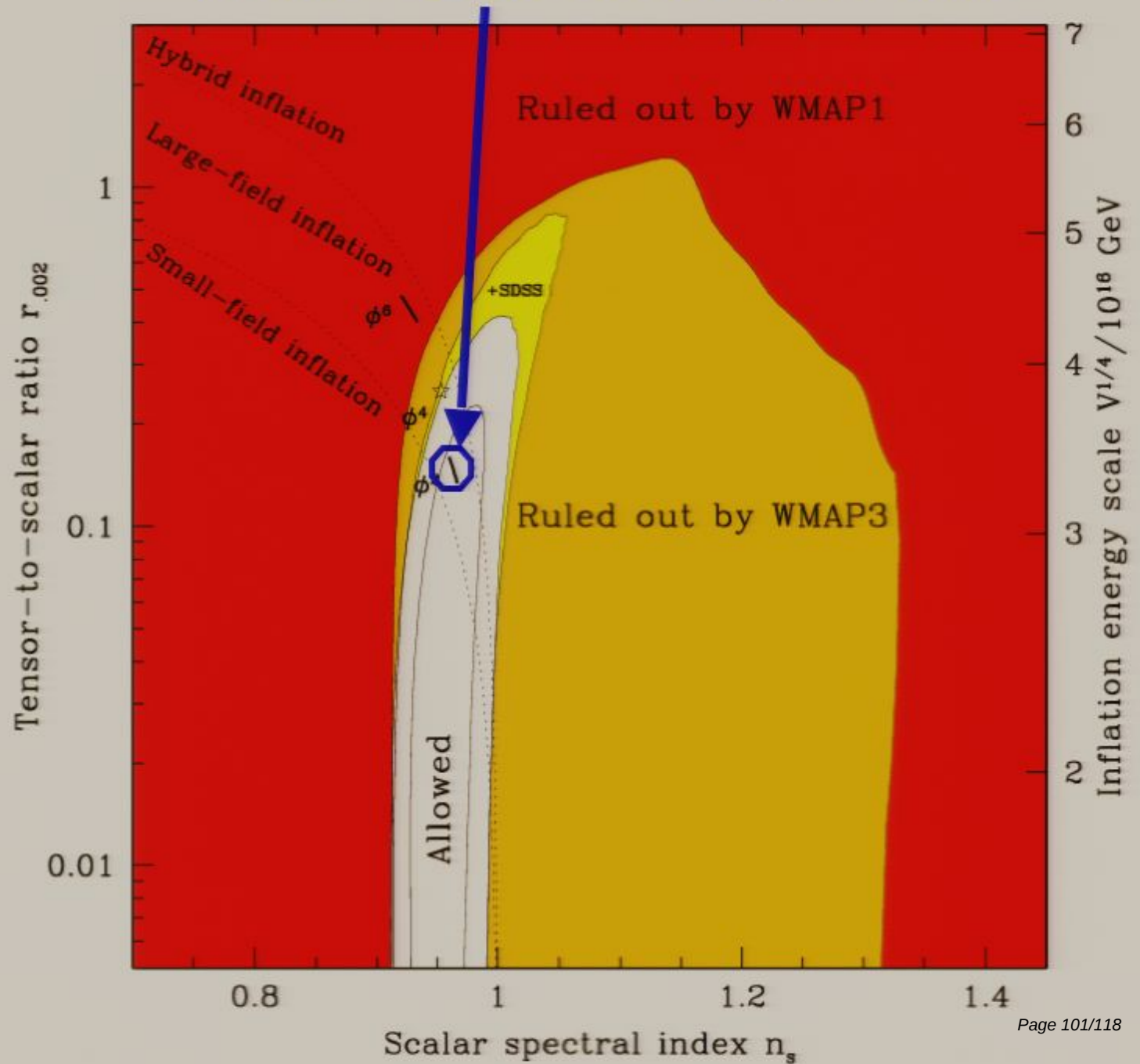
CMB

+



LSS

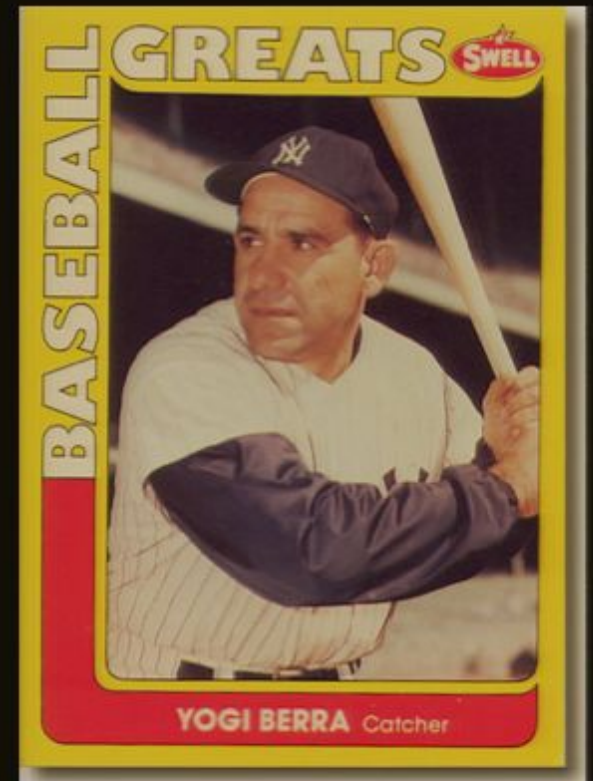
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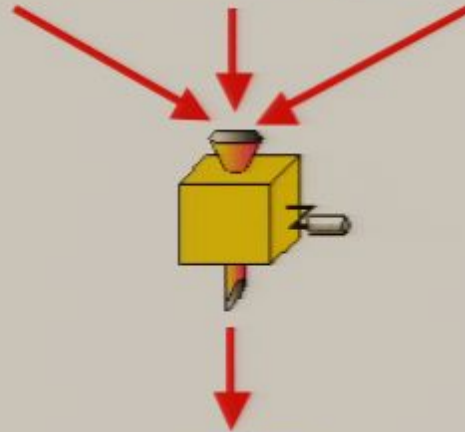
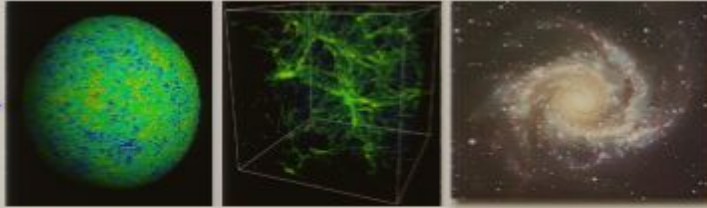
# THE FUTURE

*It's tough to make predictions,  
especially about the future.*

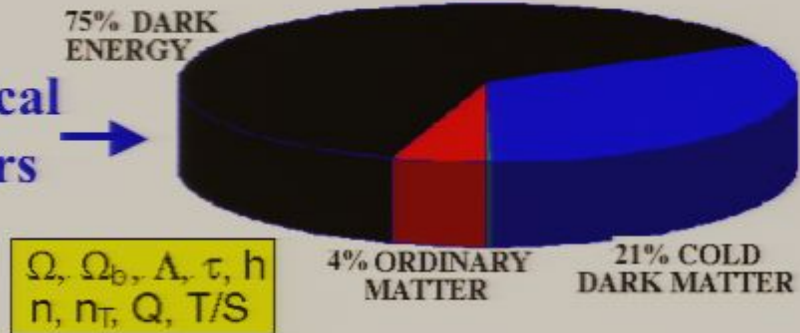
Yogi Berra



Cosmological  
data



Cosmological  
Parameters

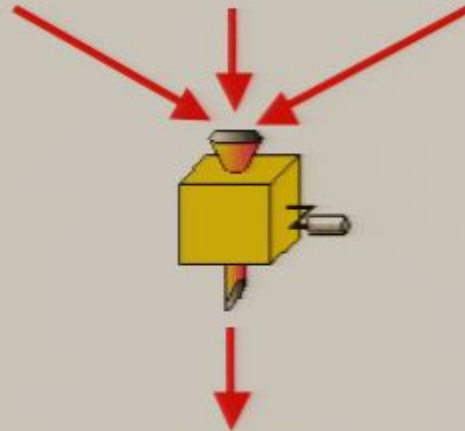
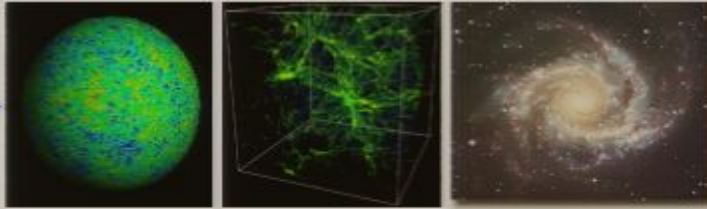




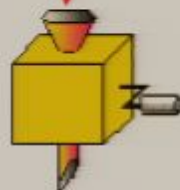
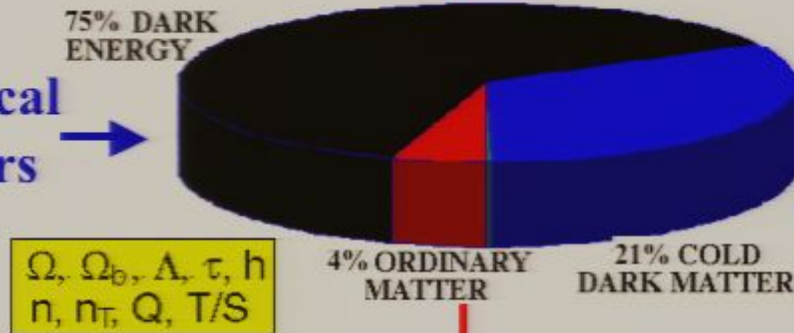
DRIVE-THRU

BURRITOS .99  
NOW HIRING LOSERS  
\$6 A HOUR

Cosmological  
data



Cosmological  
Parameters



Fundamental  
theory



Why these particular values?

Nature of dark matter?

Nature of dark energy?

Nature of early Universe?



## DARK ENERGY SUMMARY:

### Observation:

- Still no observed departures from “vanilla”
- #1 goal is searching for *any* non-vanilla behavior (density changing with time, clustering) (new mind w’ etc)

### Theory:

- Zillions of papers and models, wide open:
  - cosmological constant + ground state density?
  - evolving scalar field?
  - modified gravity?
- The least unsuccessful solution to the coincidence problem is probably anthropic - but fails if  $Q$  or dark matter density variable



## DARK MATTER SUMMARY:

### Observation:

- Still no observed departures from “vanilla” - observing this would be sensational (non-vanilla fluctuation growth, evidence of interaction)
- Indirect detection possible from annihilation
- Direct detection experiments may succeed
- LHC may discover SUSY

### Theory:

- Zillions of papers and models, wide open:
  - WIMP?
  - axion?
  - modified gravity??
- Why is its density comparable to that for baryons?



## INFLATION SUMMARY:

### Observation:

- Predictions of flatness and near-vanilla confirmed
- Still no observed departures from “vanilla”, i.e.,
  - departure from scale invariance
  - gravitational waves
  - non-Gaussianity
  - isocurvature
- Sensitivity will continue to improve dramatically

### Theory:

- Zillions of papers and models, wide open. But essentially all predict at least one kind of observable non-vanilla behavior.
- Inflation can be realized in string-theory landscape context
- Open problem how to compute probabilities



Table 1: Rough classification of inflation models.

| Fluctuation generation phase | Fluctuation source | Clock evolution       | Inflation ending | Inflation model | Observable          |                      |                 |               |
|------------------------------|--------------------|-----------------------|------------------|-----------------|---------------------|----------------------|-----------------|---------------|
|                              |                    |                       |                  |                 | Gravitational waves | Non-scale invariance | Non-Gaussianity | Iso-curvature |
| Expansion                    | Mainly clock field | Standard kinetic term | Clock field      | Classic         | +                   | +                    | -               | -             |
|                              |                    |                       | Other            | Hybrid          | -                   | +                    | -               | ?             |
|                              |                    | Other dynamics        |                  | DBI             | +                   | +                    | +               | ?             |
|                              |                    |                       |                  | Ghost           | -                   | -                    | +               | ?             |
|                              | Other              |                       |                  | Multi-field     | +                   | +                    | -?              | ?             |
|                              |                    |                       |                  | VDR             | -                   | +                    | +               | ?             |
|                              |                    |                       |                  | Curvaton        | -                   | +                    | +               | ?             |
| Contraction                  |                    |                       |                  | Ekpyrotic       | -                   | +                    | -               | -             |
|                              |                    |                       |                  | Pre-BB          | +                   | ?                    | ?               | ?             |



## INFLATION SUMMARY:

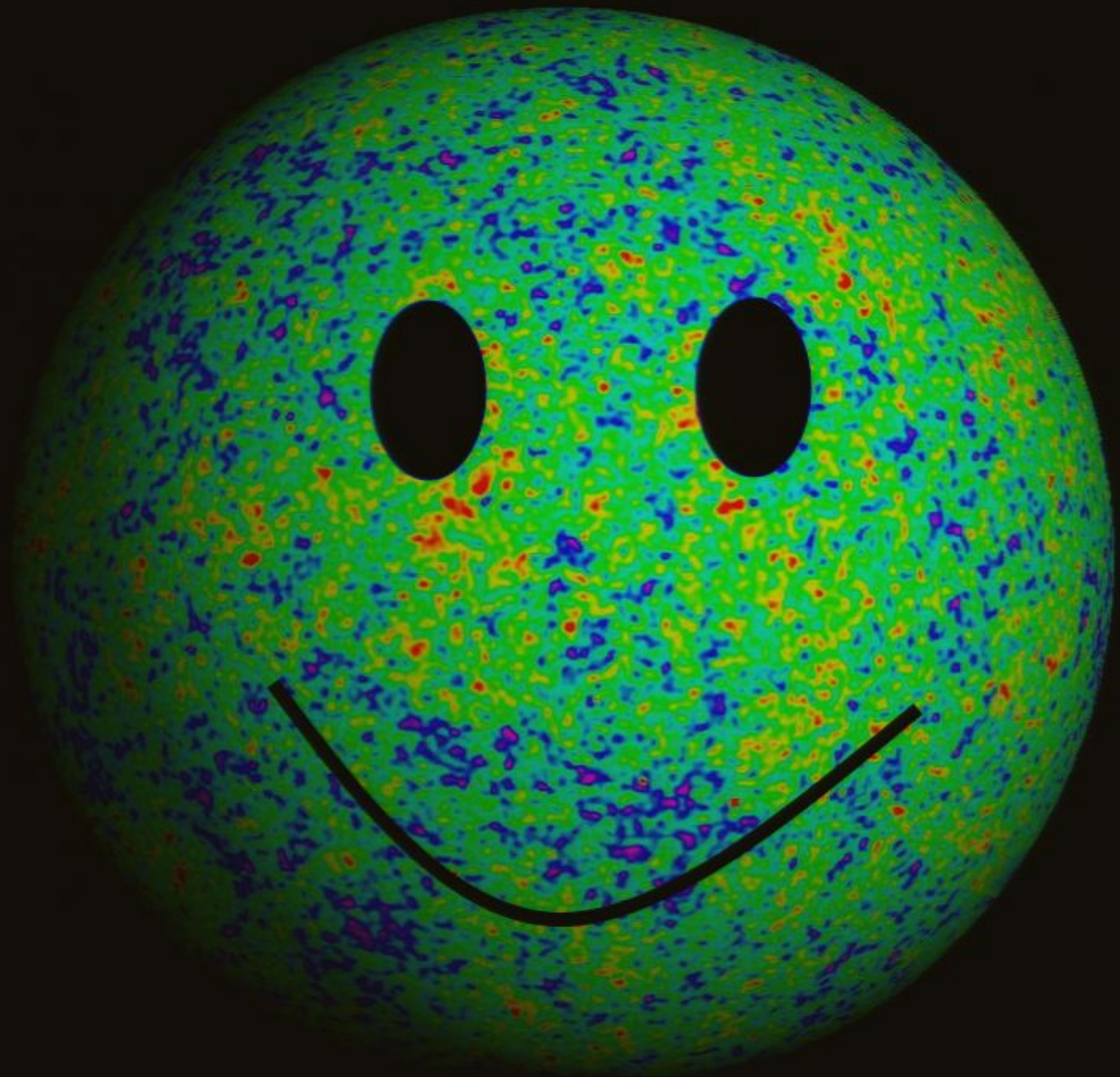
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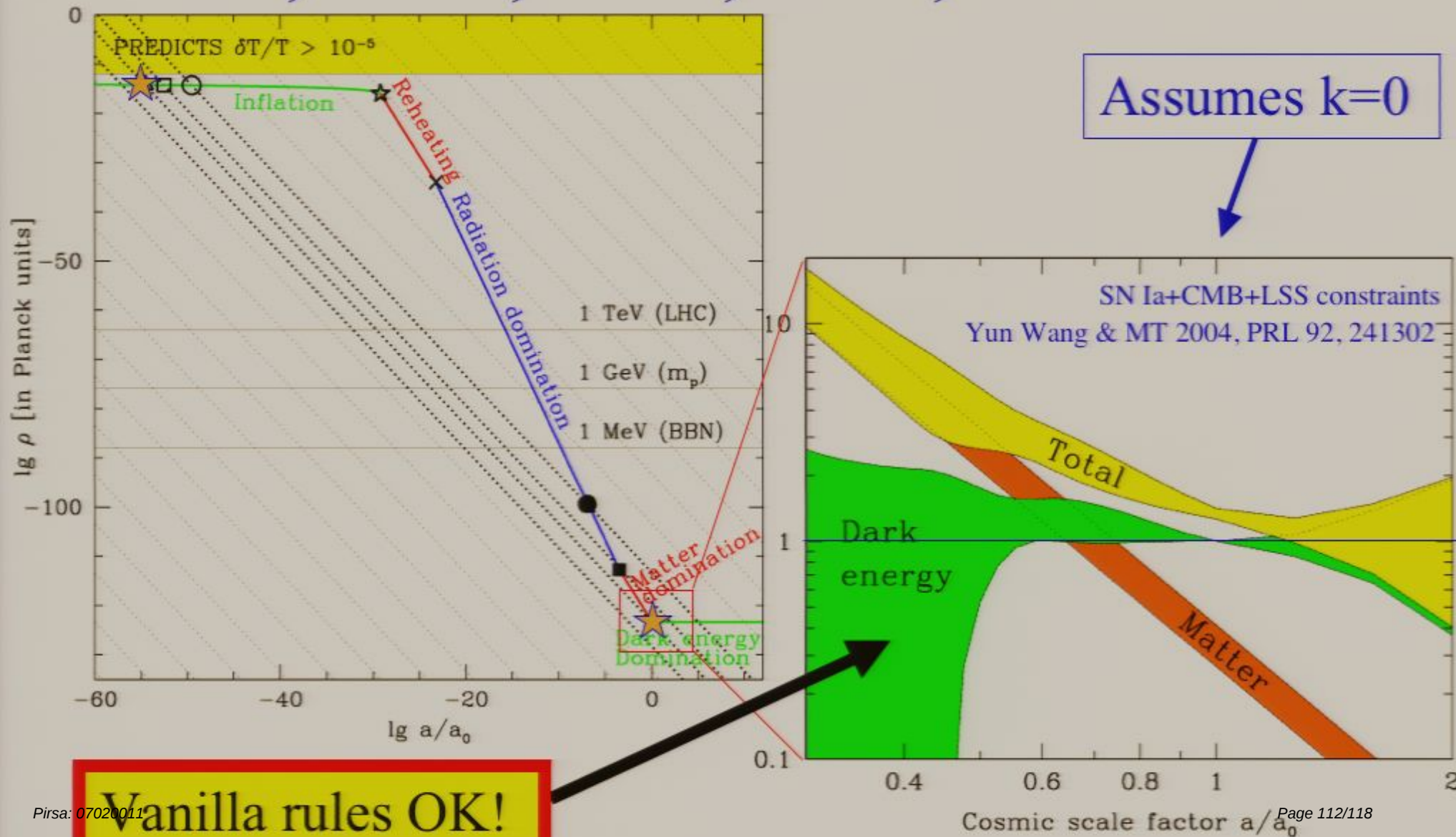
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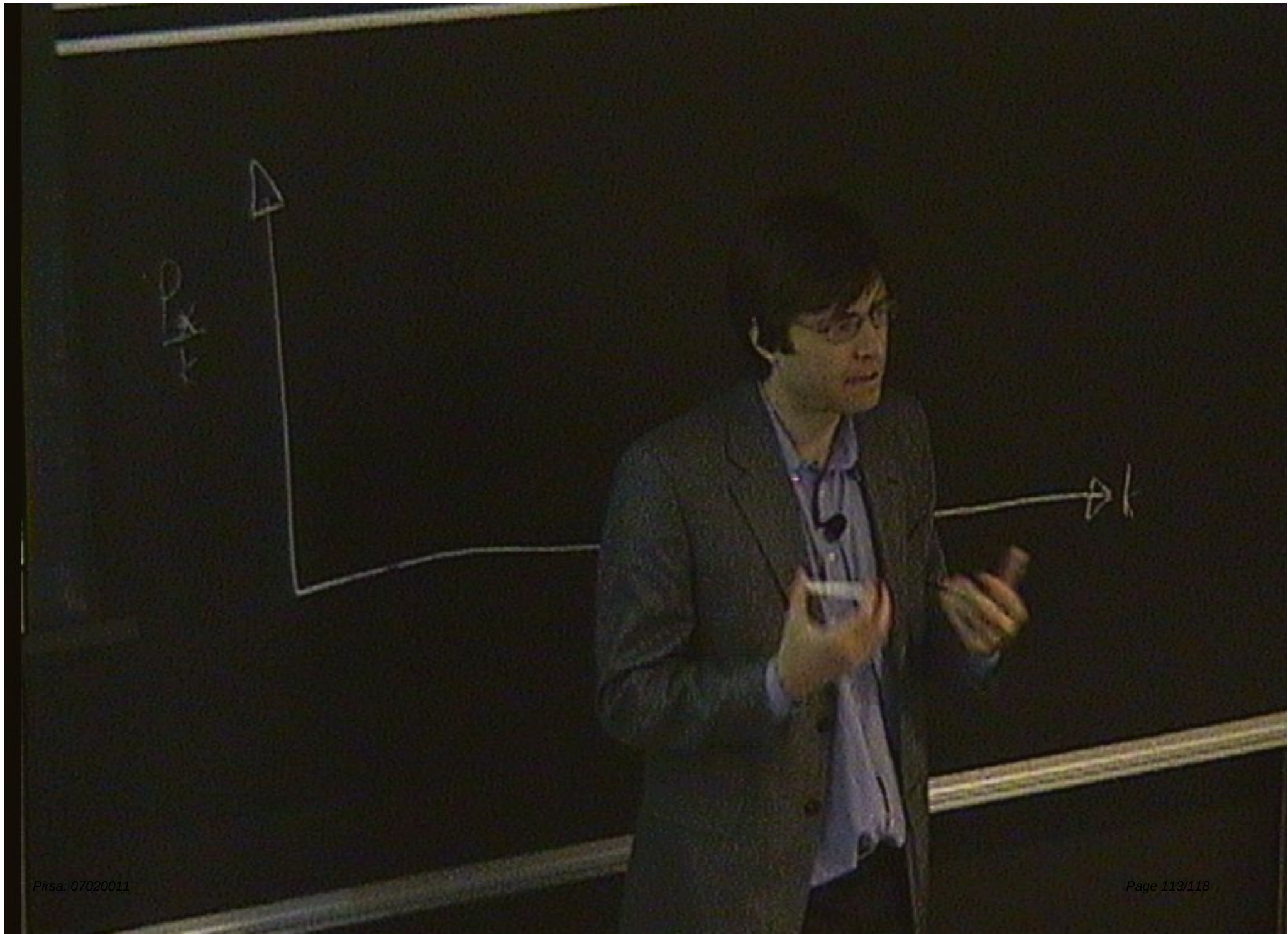
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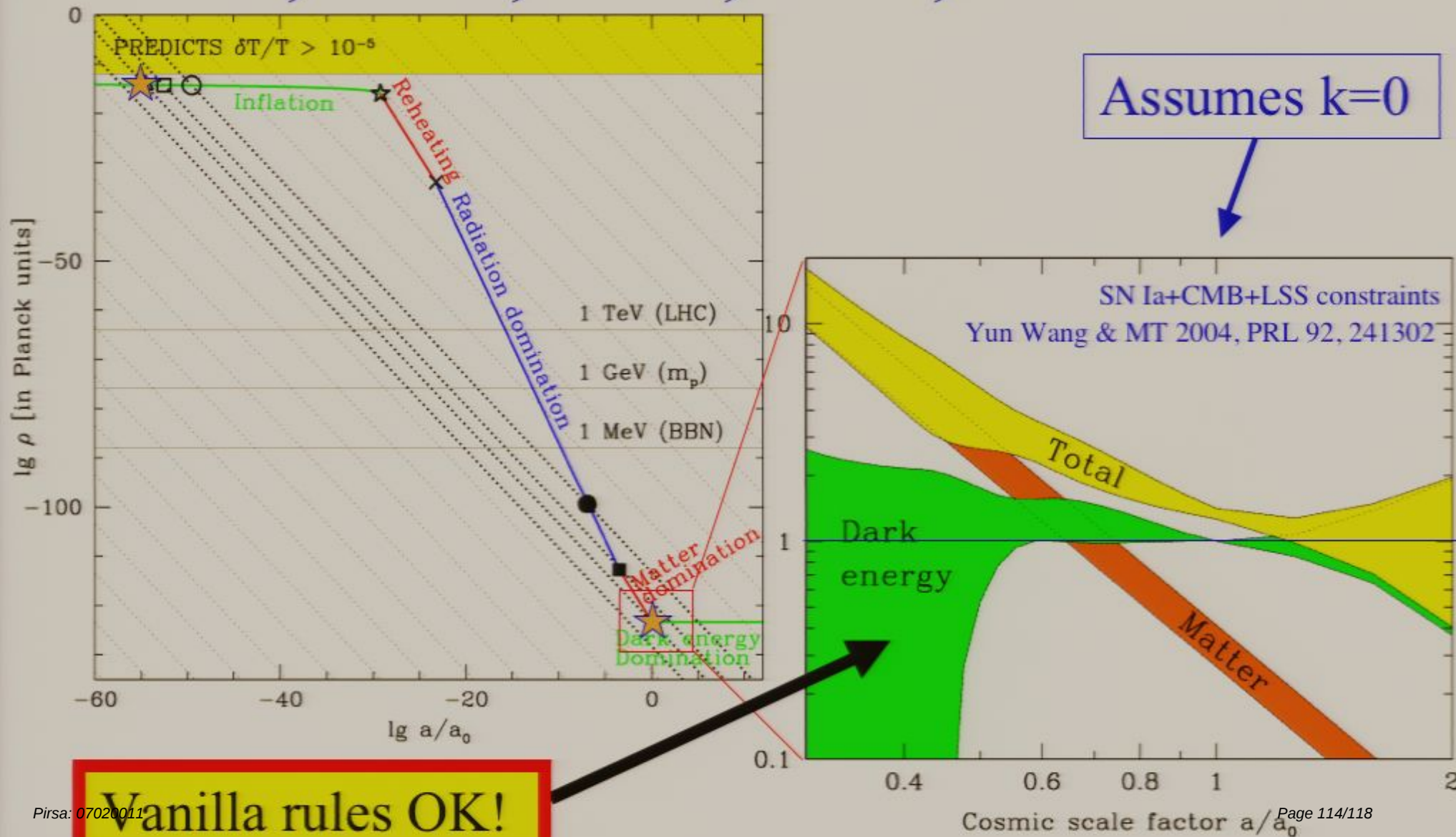


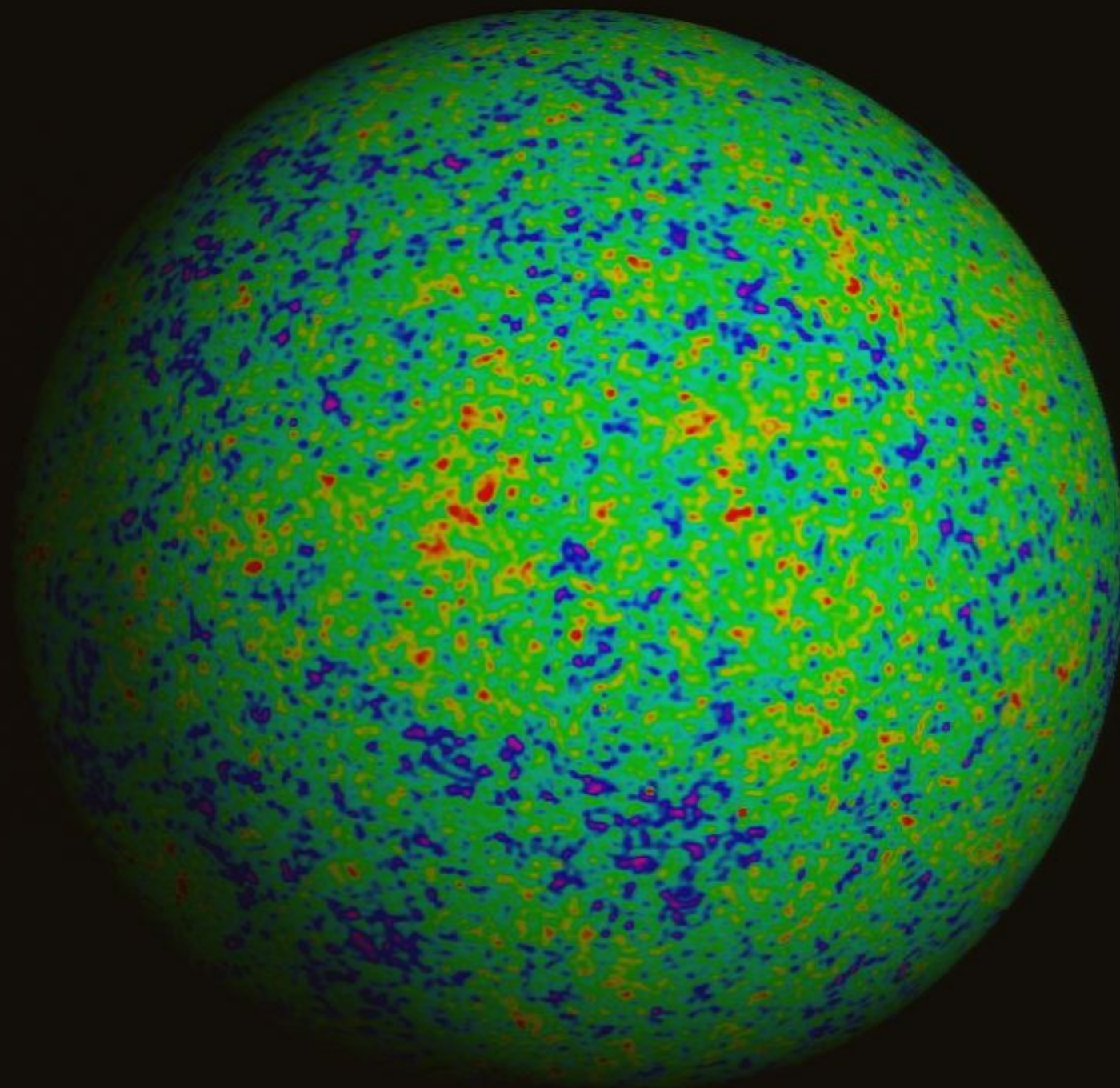
# What we've learned about $H(z)$ from SN Ia, CMB, BAO, BBN, etc:



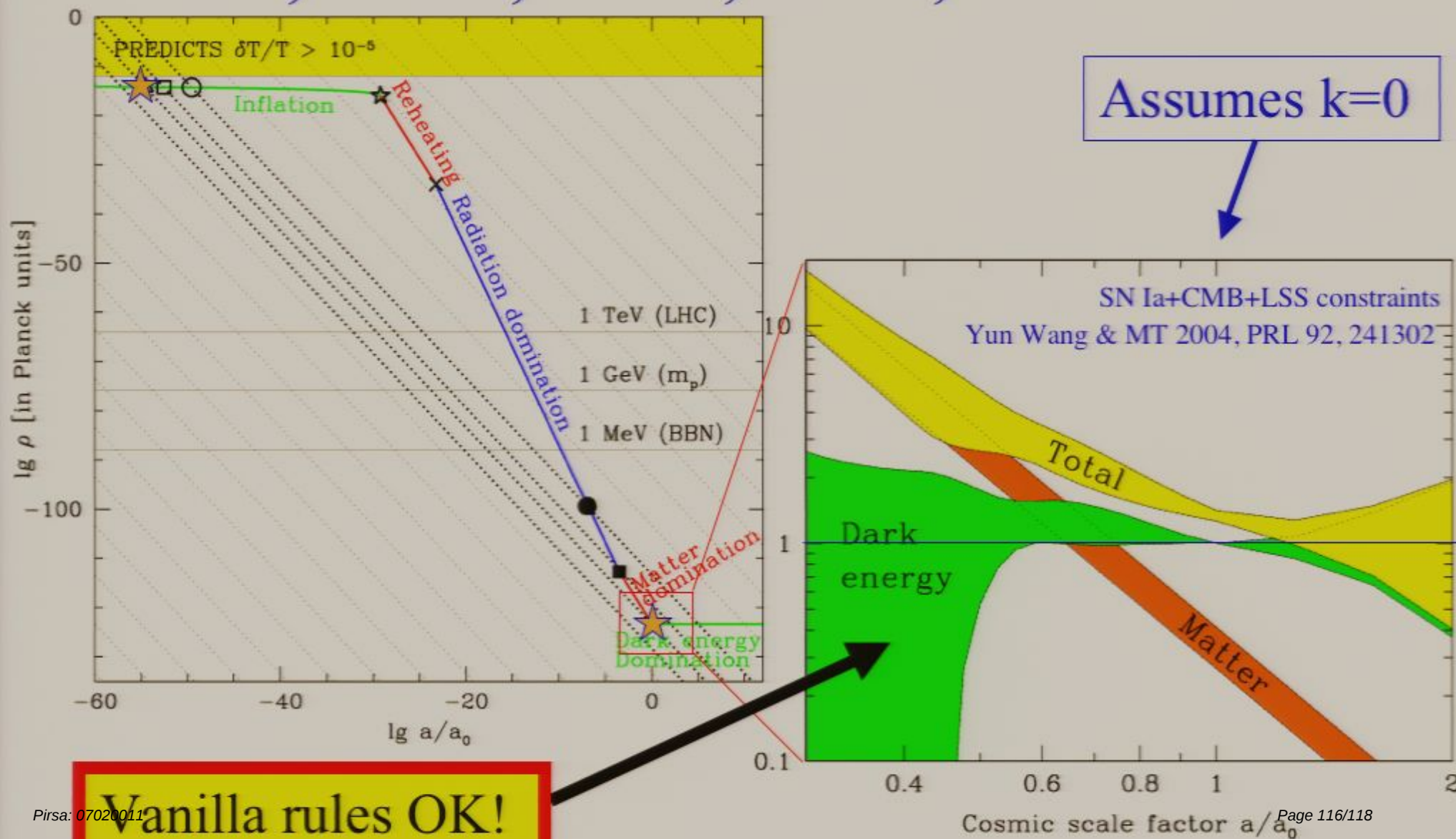


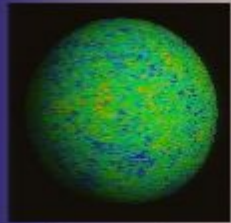
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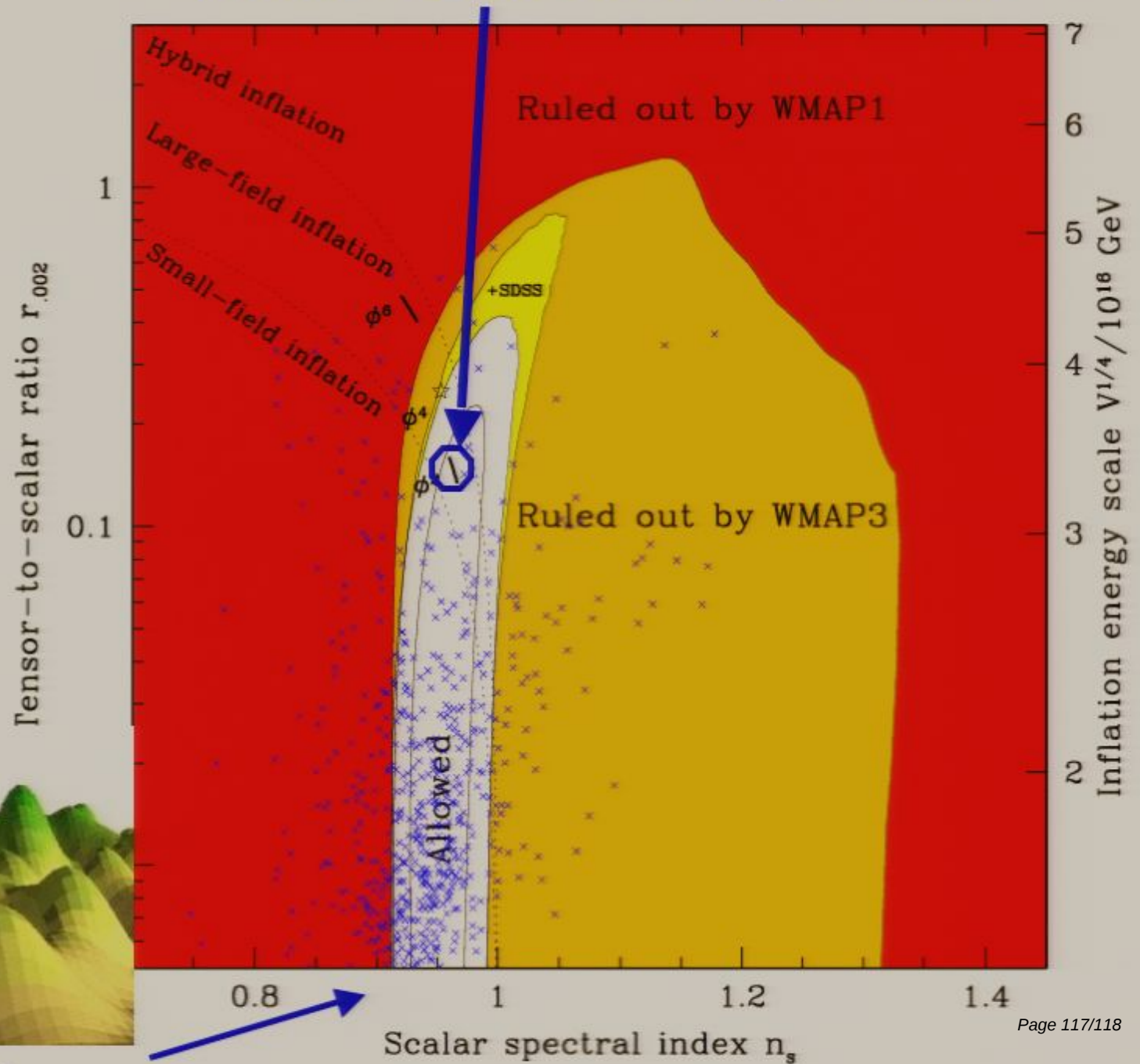
CMB

+



LSS

Planck + SDSS:  $\Delta n = 0.008$ ,  $\Delta r = 0.012$



# What we've learned about $H(z)$ from SN Ia, CMB, BAO, BBN, etc:

