

Title: Before the Big Bang: an Outrageous Solution to a Profound Cosmological Puzzle

Date: Sep 12, 2006 02:00 PM

URL: <http://pirsa.org/06090005>

Abstract:

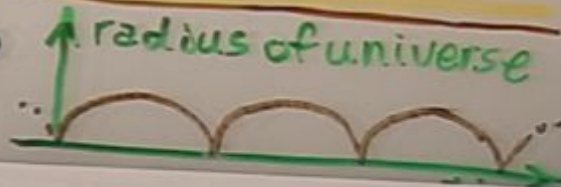
Before the

Big Bang

?

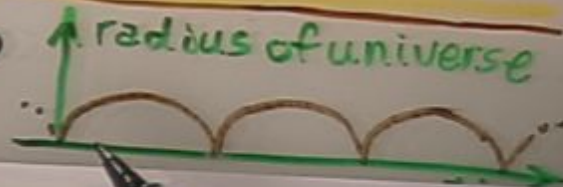
Before the Big Bang?
Some earlier (crazy?) ideas

Friedmann $k > 0$
cyclic model



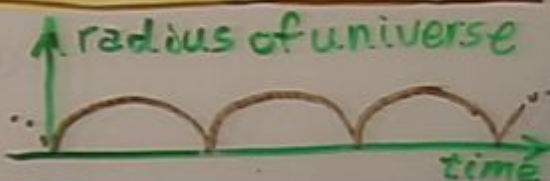
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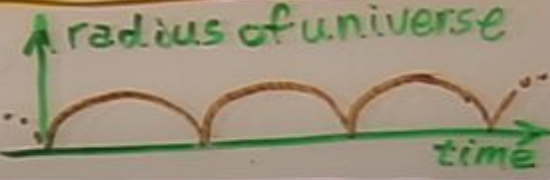
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Modifications: Tolman - each
cycle changed from previous
(greater max. radius) 2nd law?

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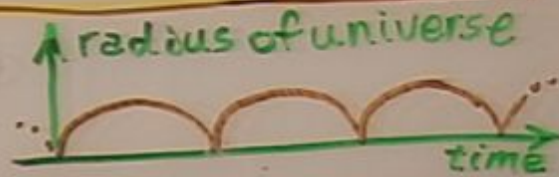


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Wheeler: constants of Nature may
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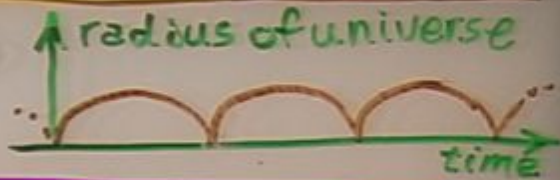
Wheeler: constants of Nature may
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Smolin:
each black-
hole sing.
is seed of
next universe



Geometry
doesn't
fit...

Friedmann $K > 0$
cyclic model



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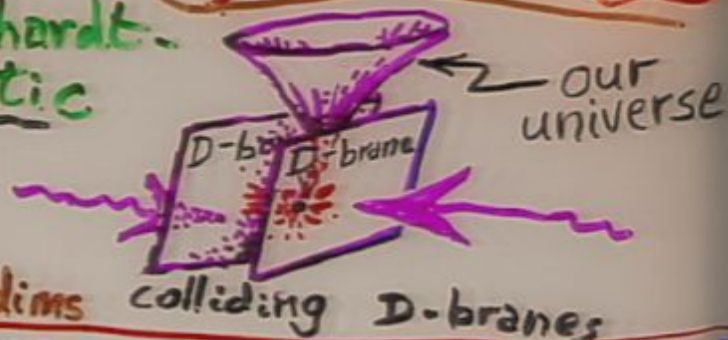
Smolin: each black-hole sing. is seed of next universe



Geometry doesn't fit

Turok-Steinhardt - Ekpyrotic

need to believe in extra (stringy) dims



Veneziano - maybe closest to my idea? (then Steinhardt-Turok)

Standard (Friedmann) cosmologies $\Lambda = 0$
1922

Big Crunch

$K=0$

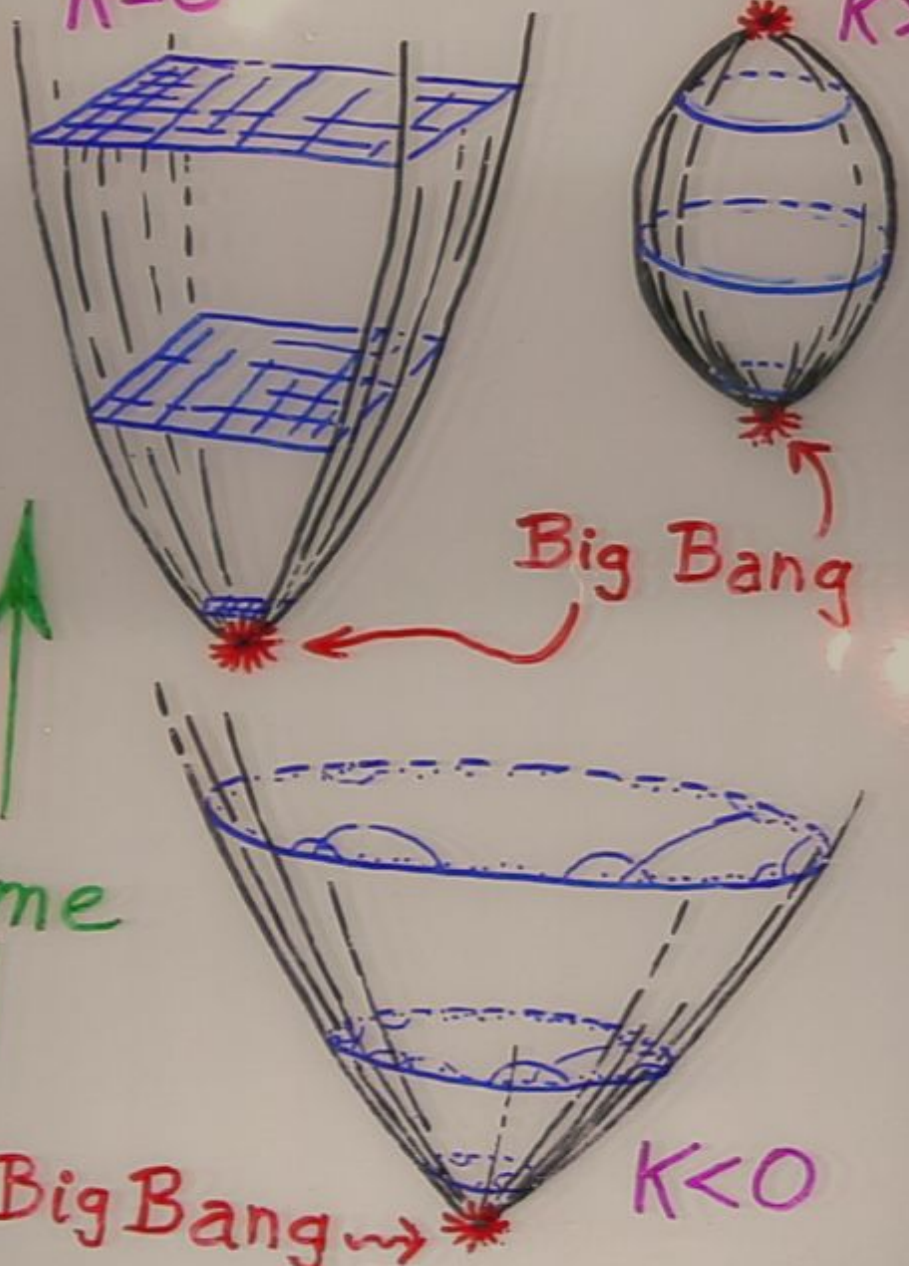
$K>0$

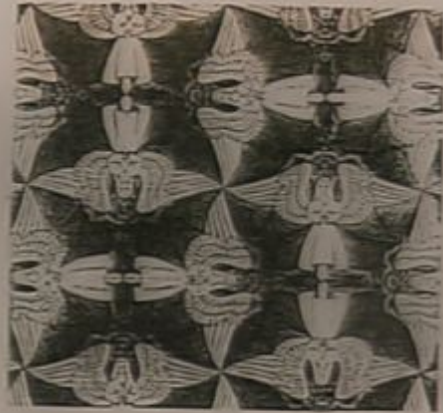
Big Bang

time

Big Bang

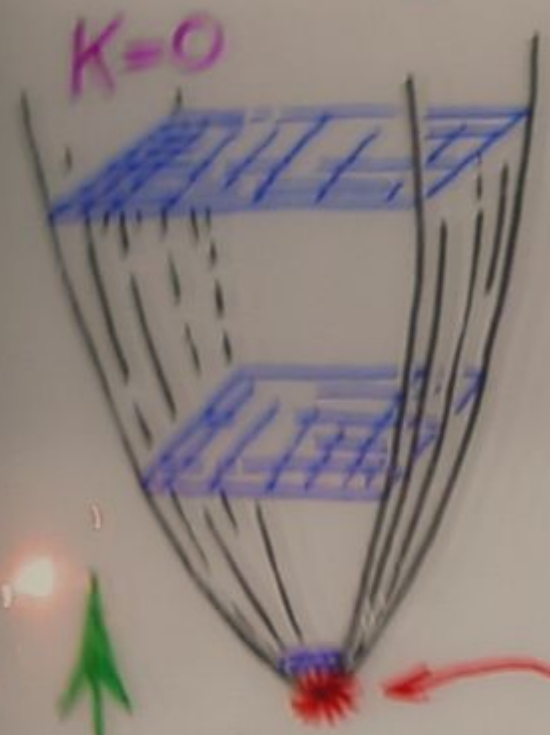
$K<0$





standard Friedmann cosmologies $\Lambda=0$

1922
Big Crunch

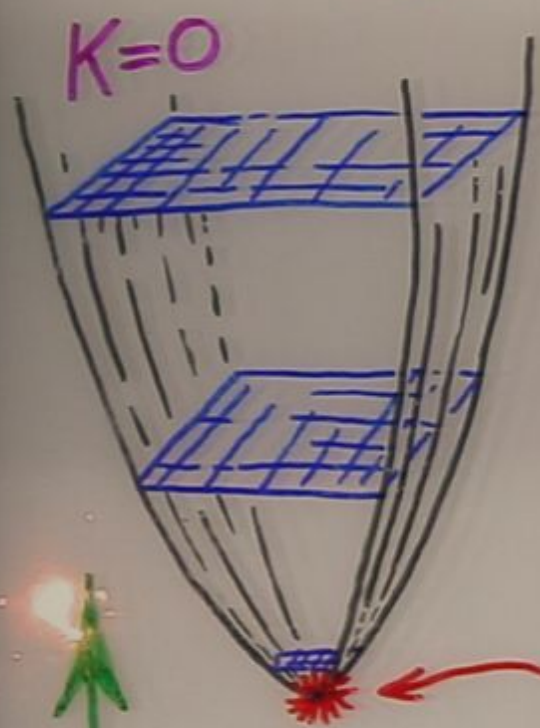


time

Big Bang

Standard (Friedmann) cosmologies $\Lambda = 0$
1922

Big Crunch



Big Bang

time ↑

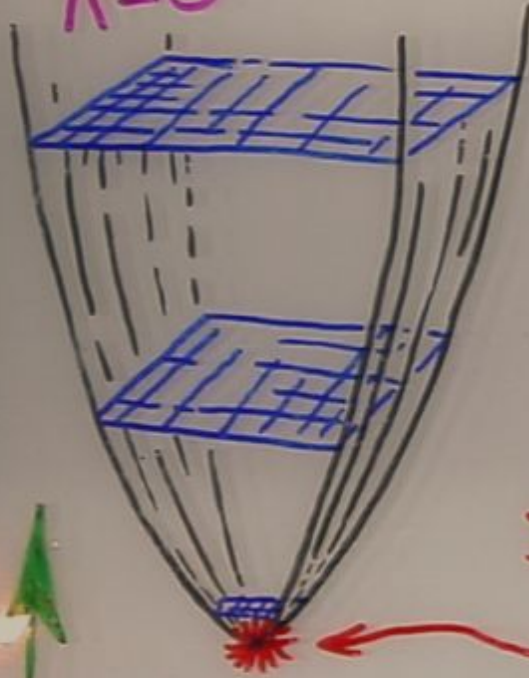
Standard (Friedmann) cosmologies $\Lambda = 0$

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Big Crunch

$K=0$

$K>0$



Big Bang

time

The 2nd law of thermodynamics



Entropy:

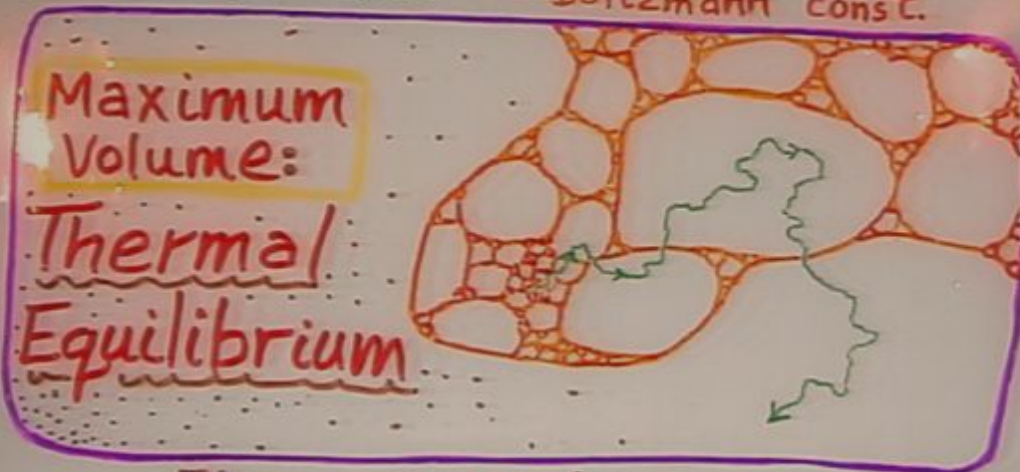
$$S = k \log V$$

increases

time

V = vol. in phase space

Boltzmann const.



Phase space (coarse-grained)

S
↑
entropy

The 2nd law of thermodynamics



The 2nd law of thermodynamics



→ time

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→ time

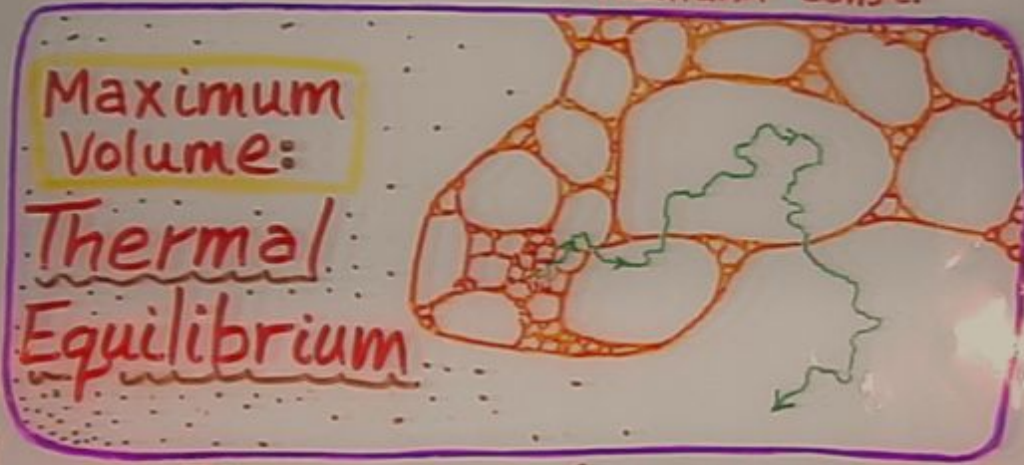
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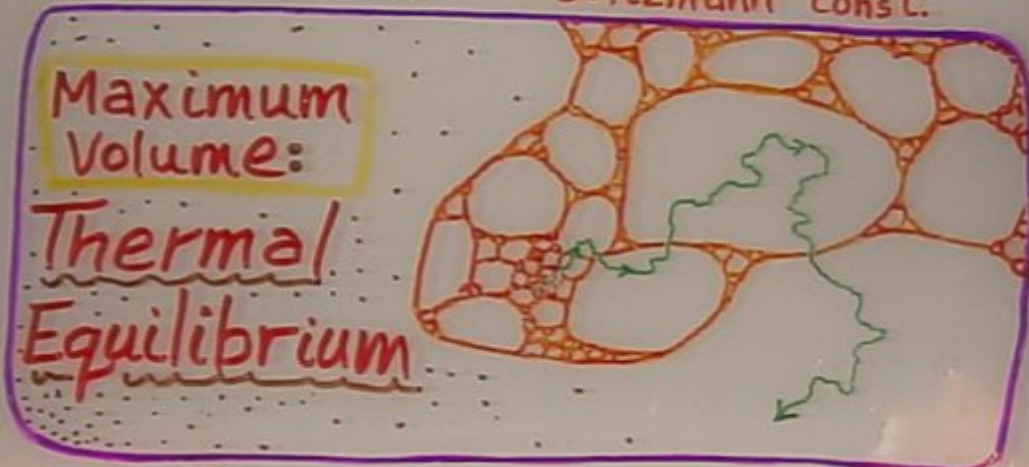
Boltzmann const.



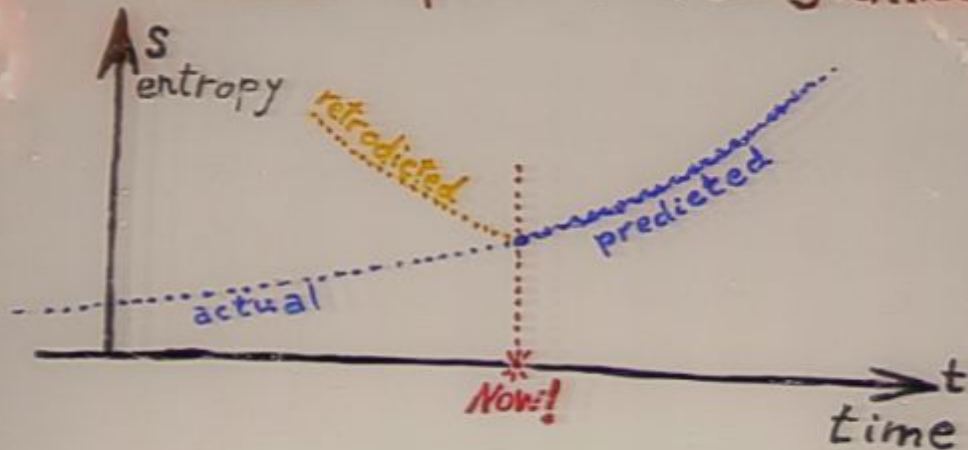
Phase space (coarse-grained)



Entropy: $S = k \log V$ → time
increases
 V = vol. in phase space ↑ Boltzmann const.



Phase space (coarse-grained)



The 2nd law of thermodynamics

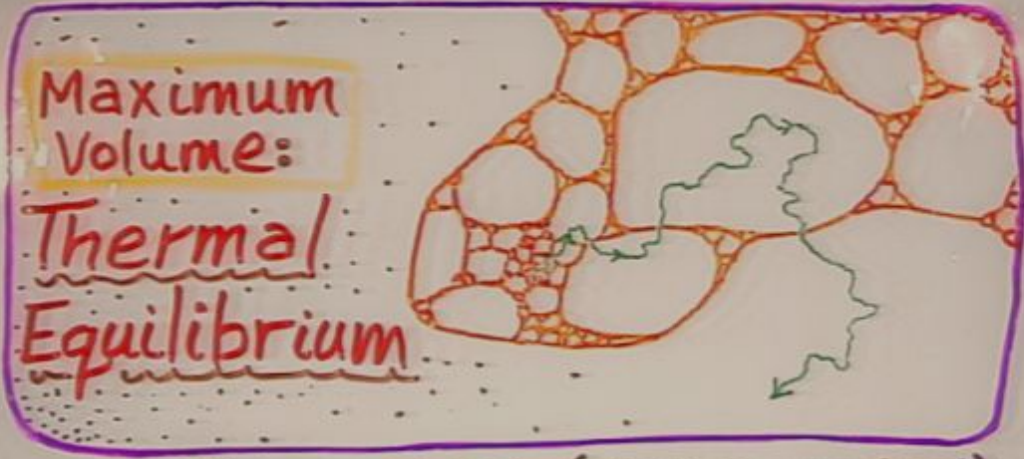


→ time

Entropy: $S = k \log V$ increases

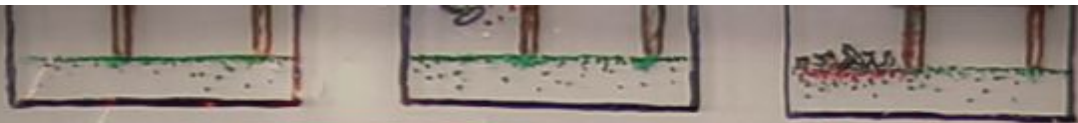
V = vol. in phase space

← Boltzmann const.

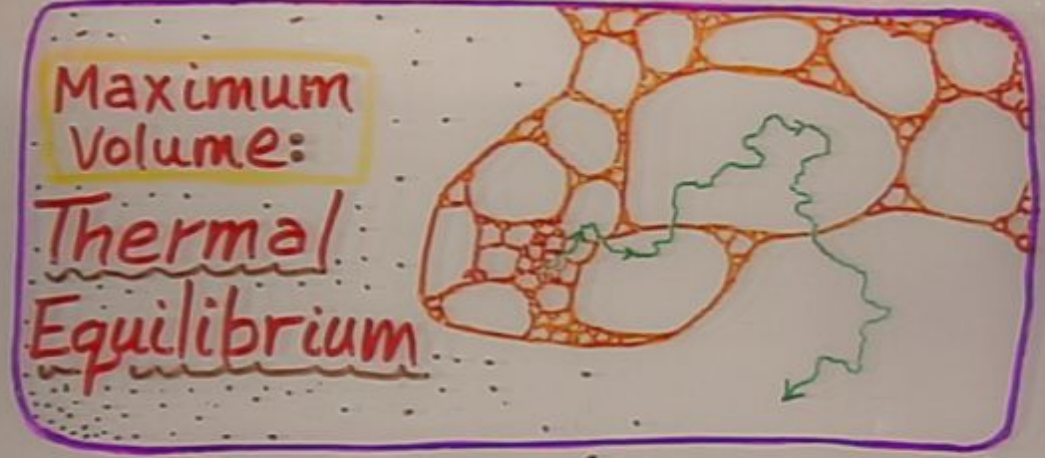


Phase space (coarse-grained)

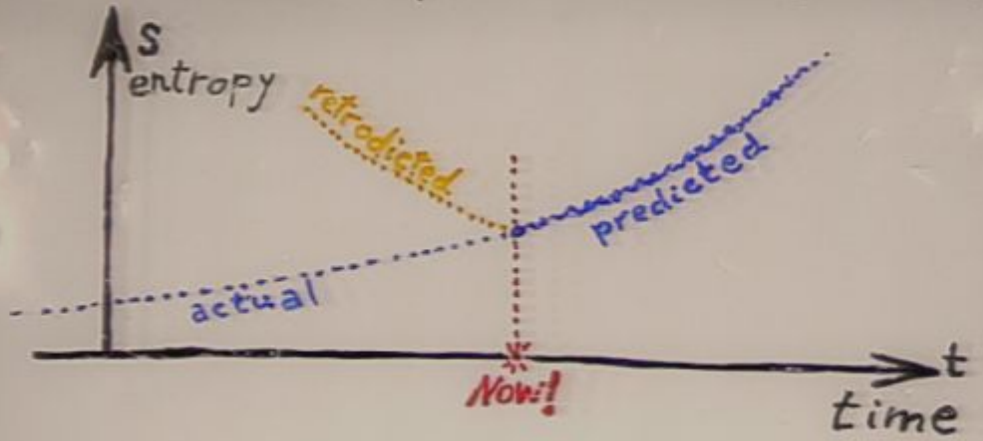
↑ S
entropy



Entropy: $S = k \log V$ increases \rightarrow time
V = vol. in phase space \leftarrow Boltzmann const.



Phase space (coarse-grained)



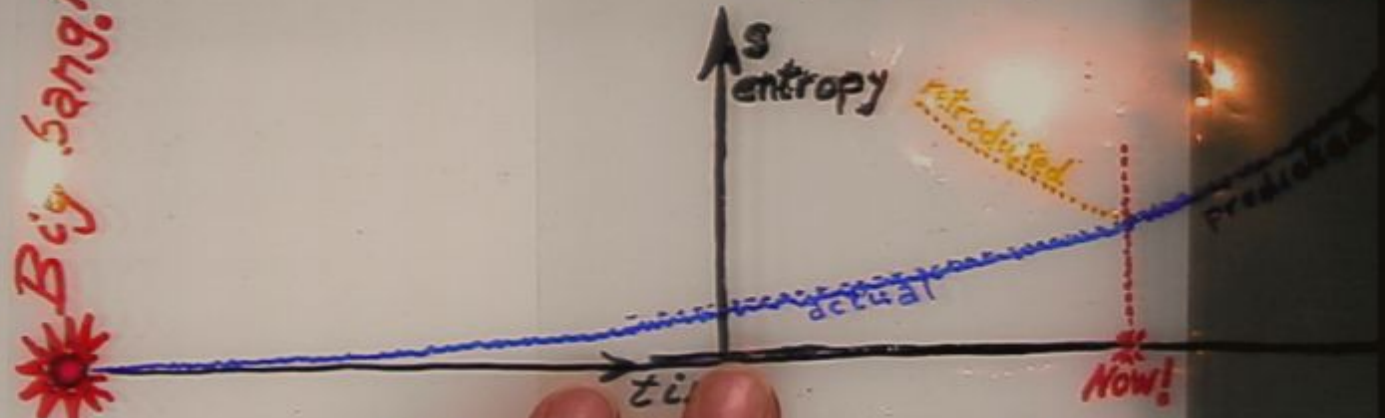
Entropy: $S = k \log V$
 $V = \text{vol. in phase space}$ Boltzmann

Maximum Volume:
Thermal Equilibrium



Phase space (coarse)

Big Bang!



To ensure that the entropy continues to go down in the past we need an enormous conspiracy in the time geometry

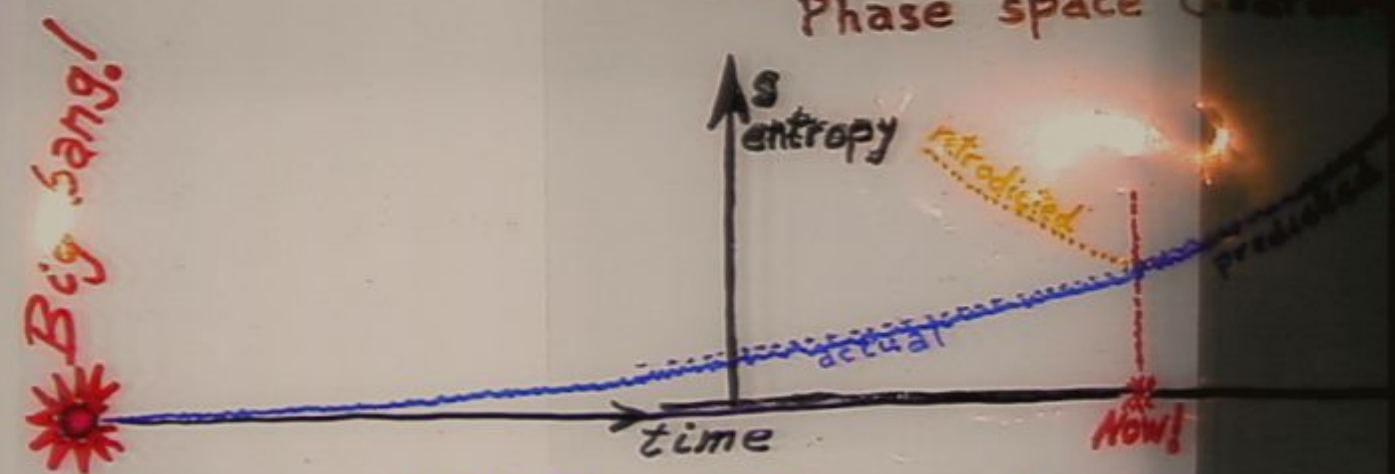
Entropy: $S = k \log V$ (inc)

V = vol. in phase space ← Boltzmann

Maximum Volume:
Thermal Equilibrium



Phase space (coordinates)



To ensure that the entropy continues to go down in the past, we need an enormous constraint on the space-time geometry at the Big Bang.

Cosmic Background Spectrum at the North Galactic Pole

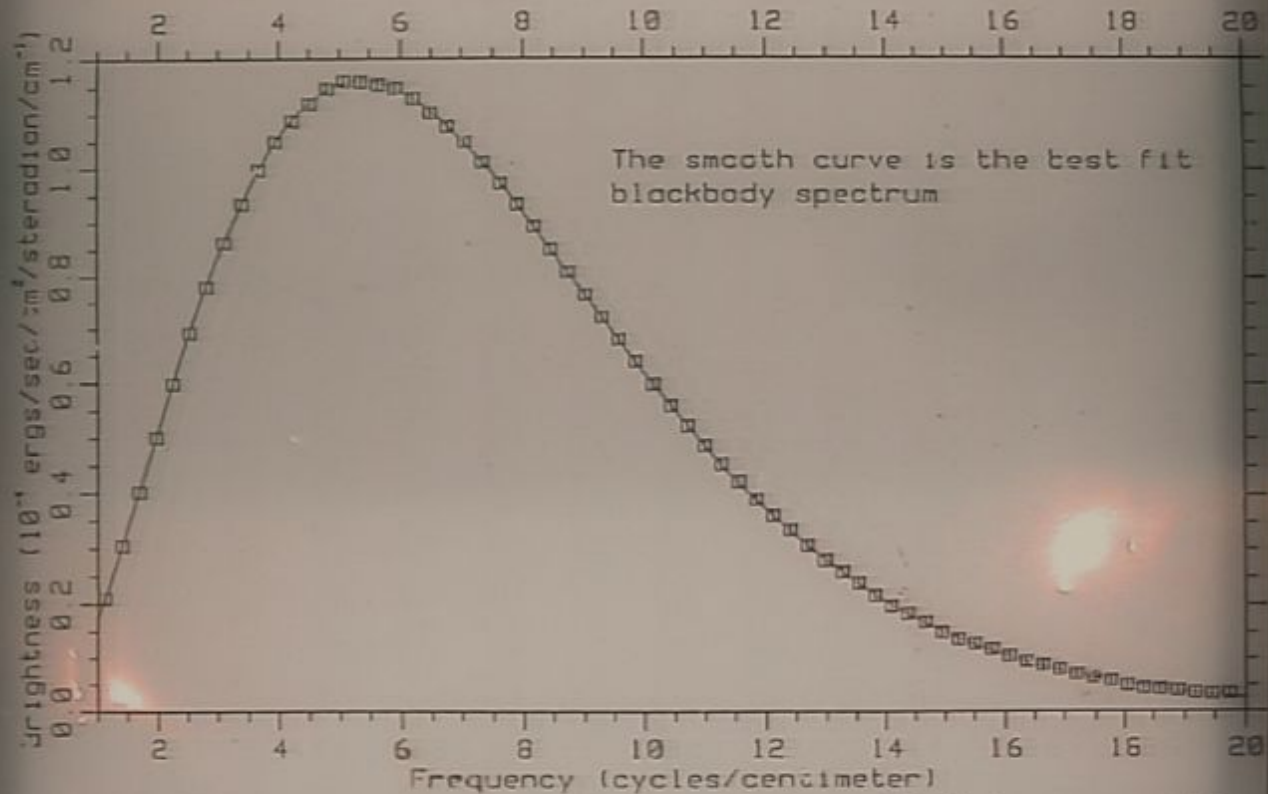


FIG. 9. The spectrum of the Cosmic Microwave Background Radiation as measured by the COBE satellite in the direction of the North Galactic Pole. Within the quoted errors, the spectrum is that of a perfect black body at radiation temperature 2.735 ± 0.05 K (Mather *et al.* 1990).

Entropy:

$$S = k \log V$$

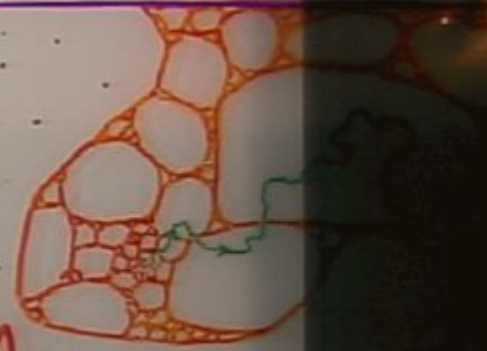
increase

V = vol. in phase space

Boltzmann const

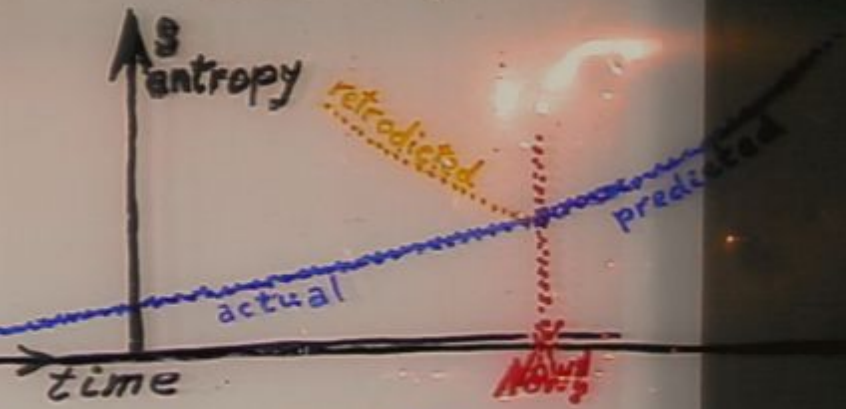
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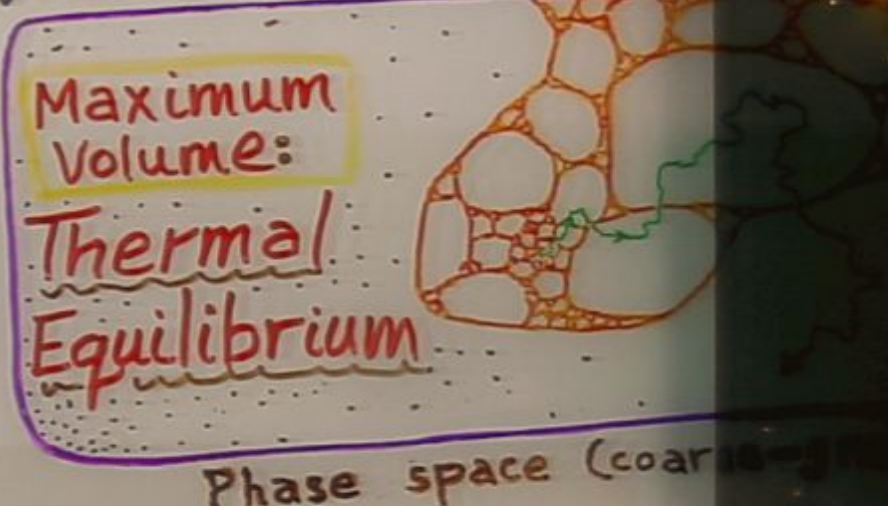
Phase space (coarse)

Big bang!



To ensure that the entropy continues to go down in the past, we need an enormous constraint on the space-time geometry at the **Big Bang**.

Entropy: $S = k \log V$ increases
 $V = \text{vol. in phase space}$ Boltzmann const.

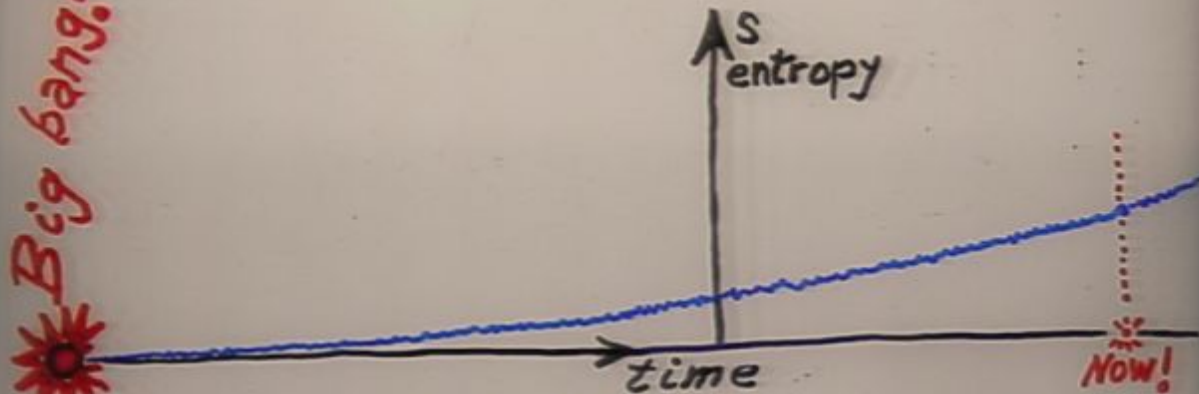


Big bang!



To ensure that the entropy continues to go down in the past, we need an enormous constraint on the space-time geometry at the Big Bang.

Big bang!



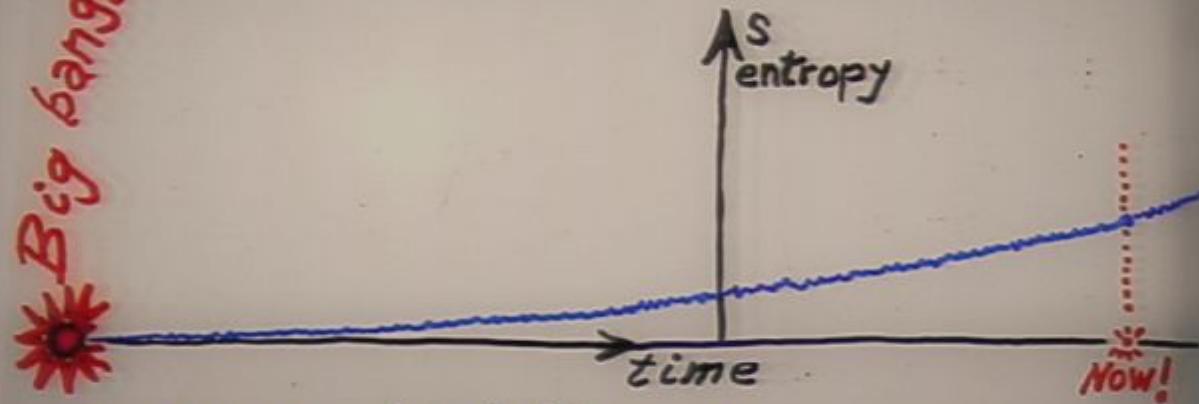
To ensure that the entropy continues to go down in the past, we need an enormous constraint on the space-time geometry at the **Big Bang**.

Why on the geometry? Conformal curvature ≈ 0
Because the matter itself was apparently in a thermal state (= maximum entropy) to get agreement with observation.

How do we estimate the contribution of the geometry?

How enormous is (was!) this constraint?

Big bang!



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Phase-space

Maximum Entropy
(thermal equilibrium)



Phase-space

Maximum Entropy
("thermal equilibrium")



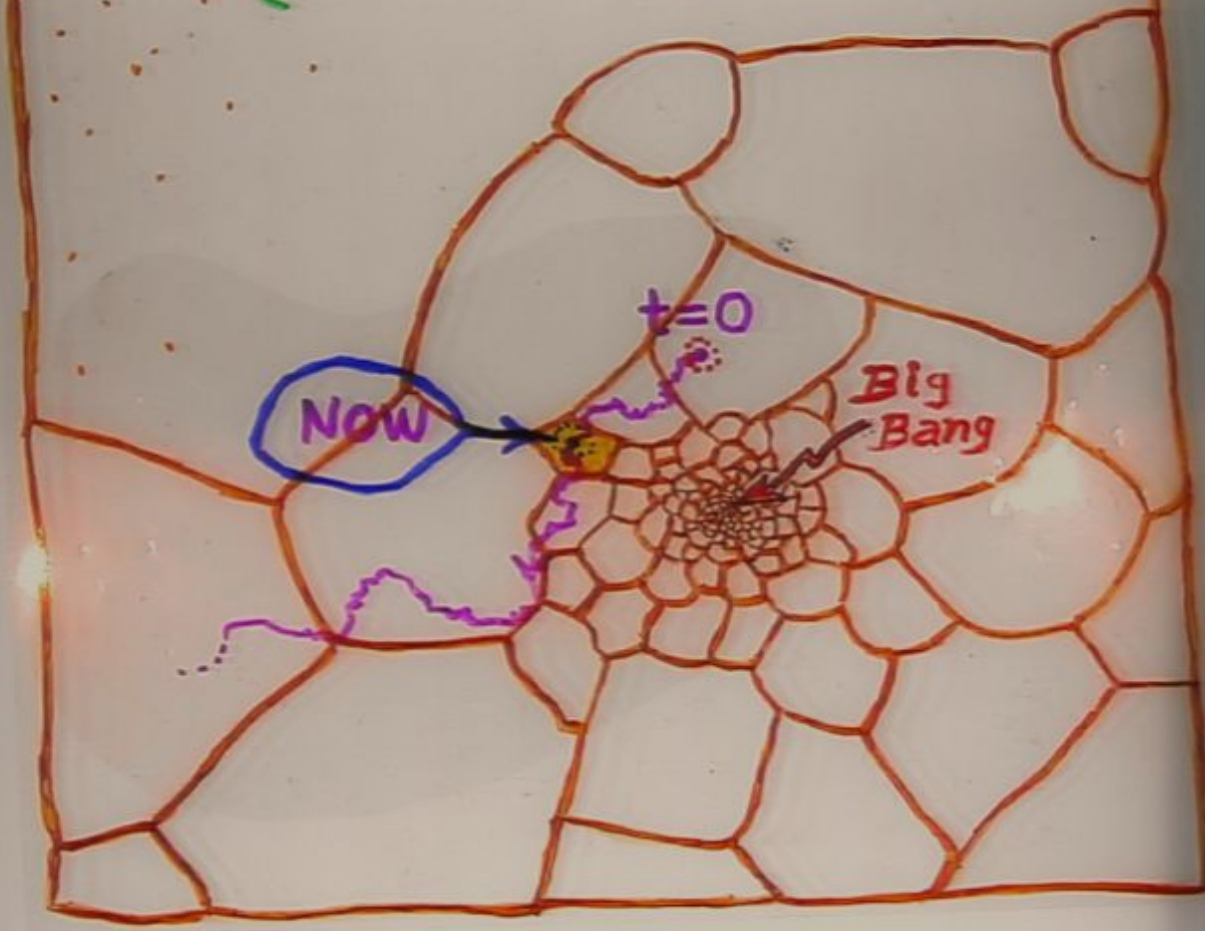




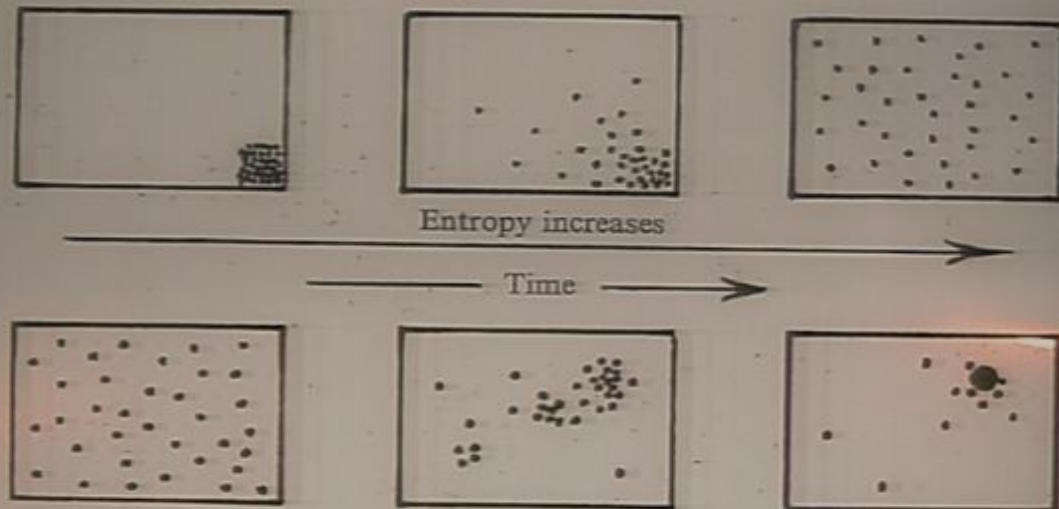
Phase of
Maximum Entropy
("thermal equilibrium")



Phase 1
Maximum Entropy
("thermal equilibrium")



Entropy increase



with gravity!

How we make use of the low-entropy reservoir available from gravitational clumping:
The sun is a hot spot in a dark background sky. Its very existence results from gravitational clumping.



The Earth gives back all the energy it receives from the Sun. But the energy received is in a SMALL number of high-energy photons (yellow) and sent away in a LARGE number of low-energy photons (infrared).

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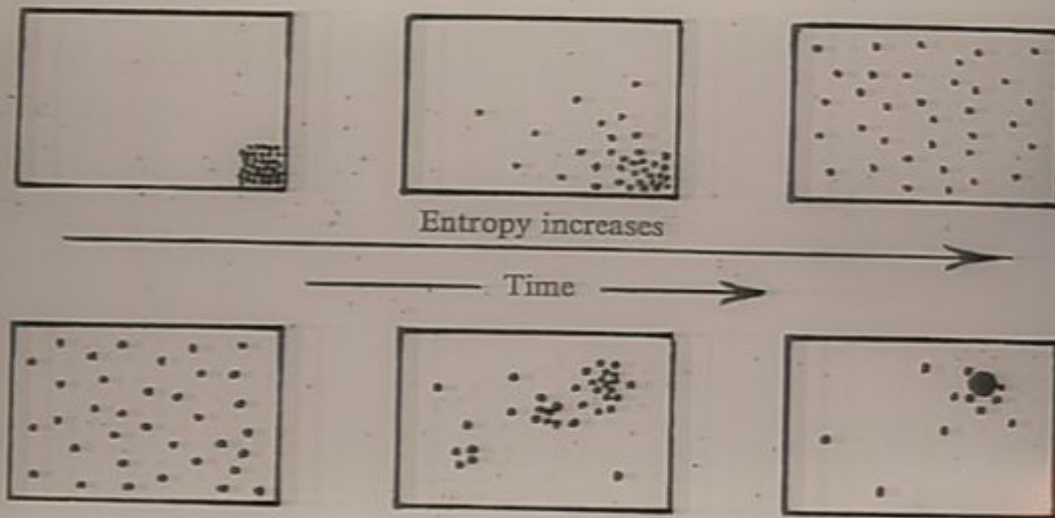
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Entropy increase



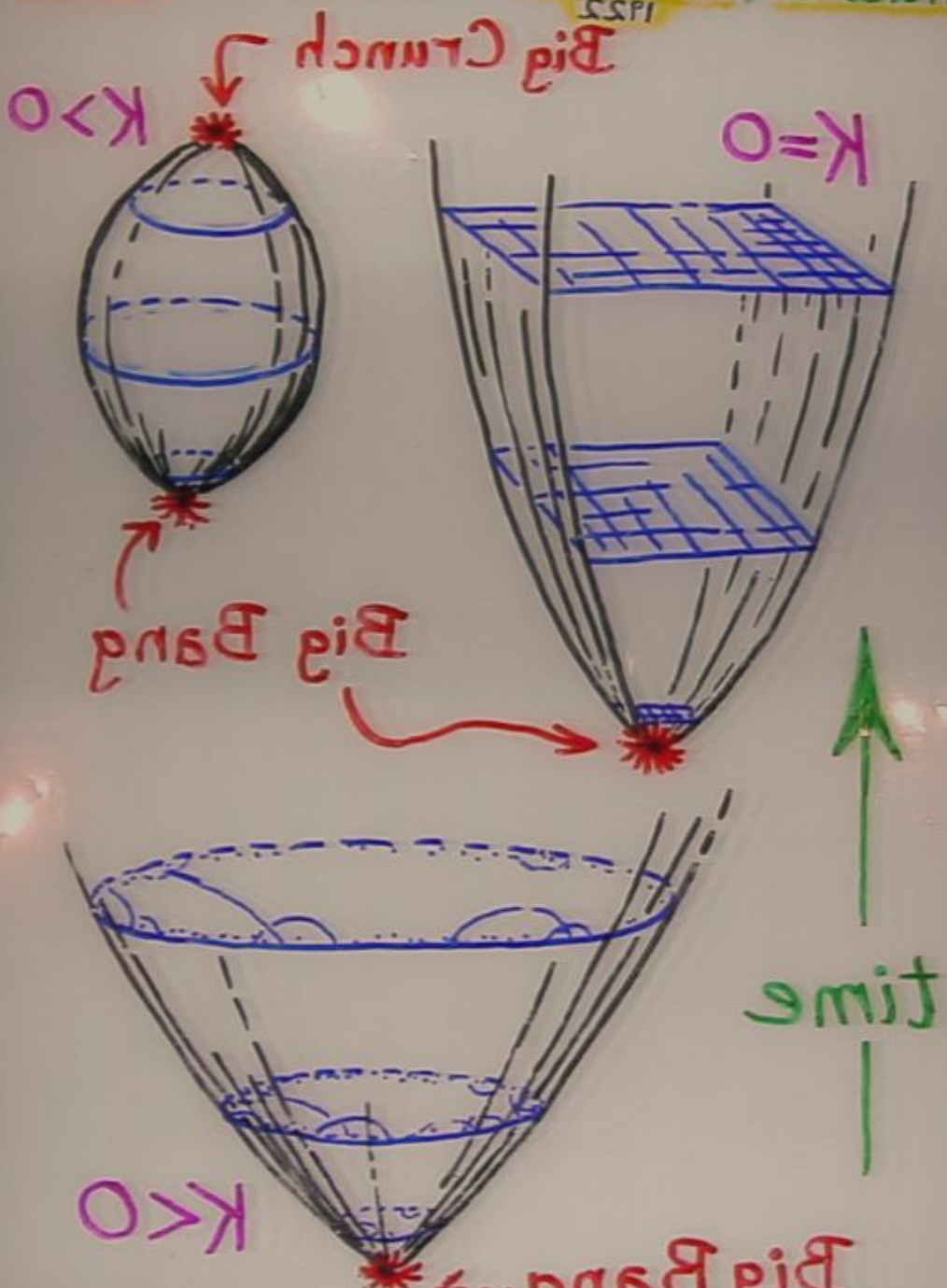
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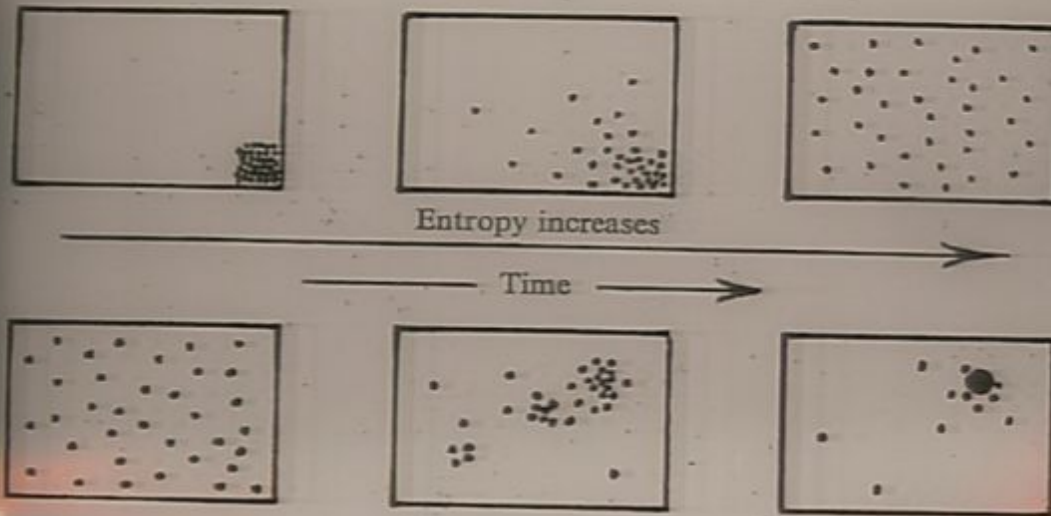


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Standard (Friedmann) cosmologies $\Lambda = 0$
1925

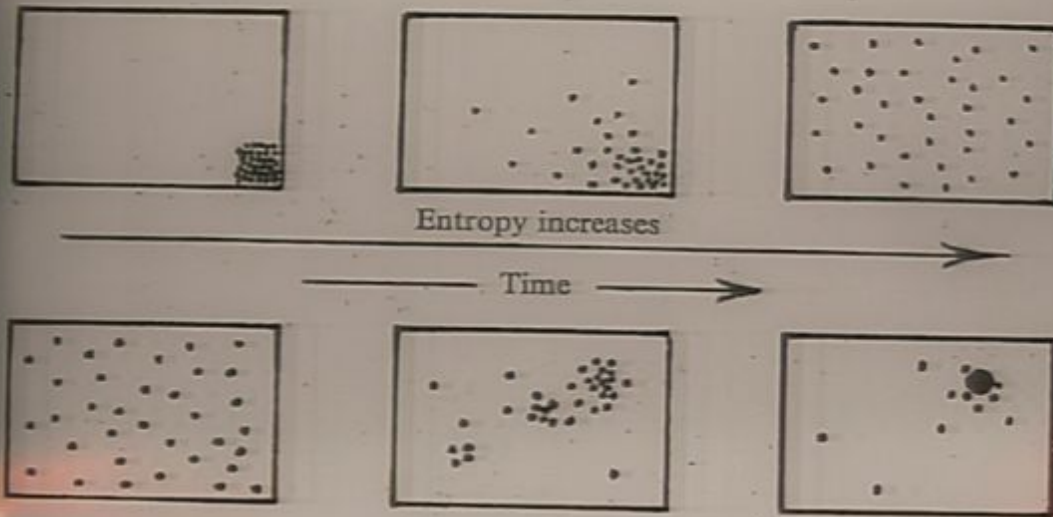


Entropy increase



with gravity!

Entropy increase

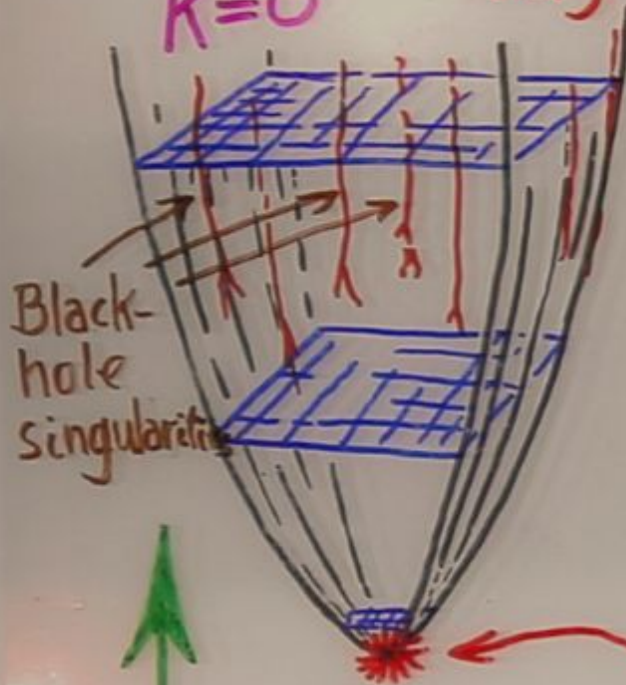


with gravity!

Standard (Friedmann) cosmologies $\Lambda=0$
with perturbations

Big Crunch
very messy!

$K=0$



Big Bang

time

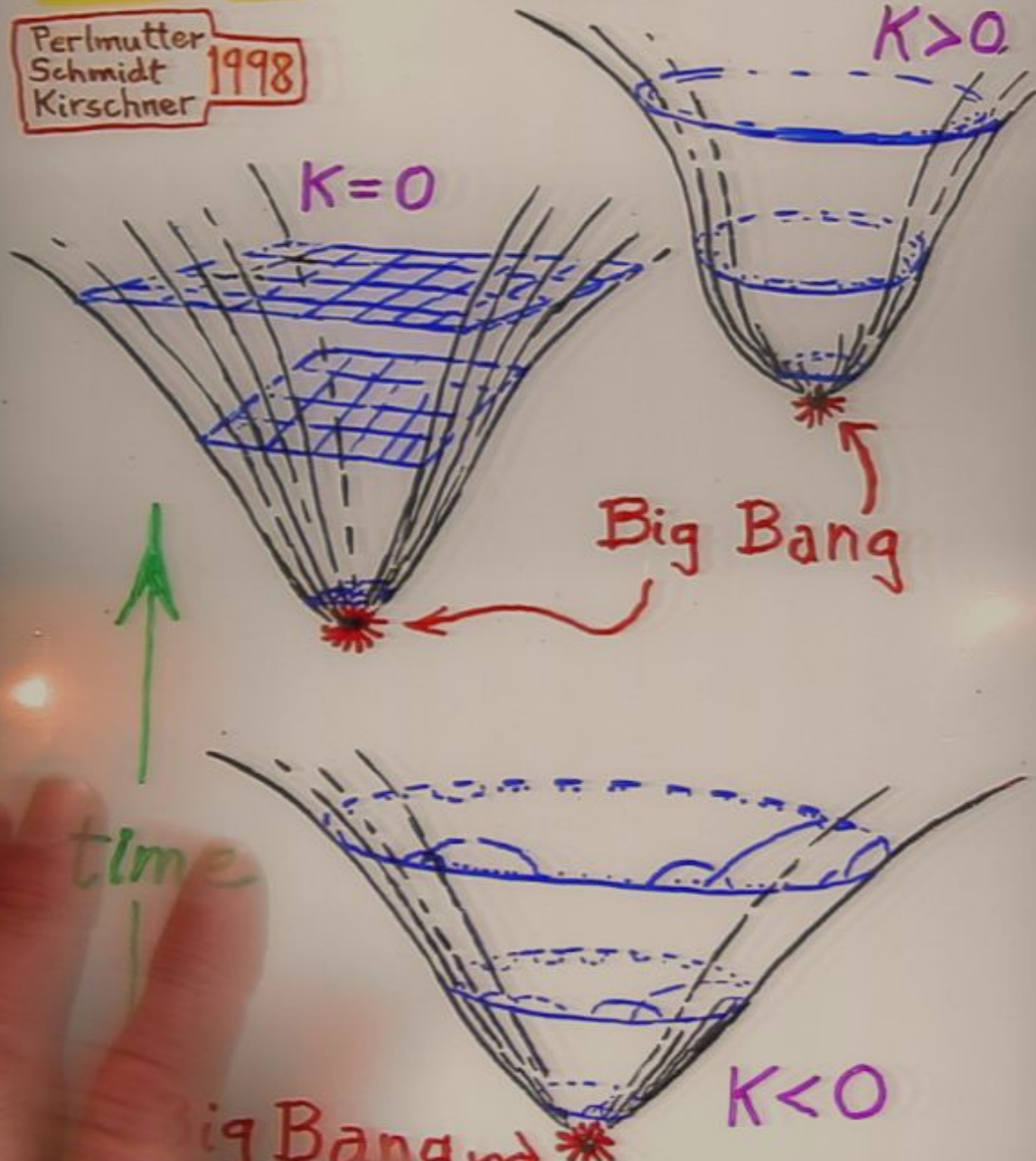
Black-hole singularities

Big Bang

$K<0$

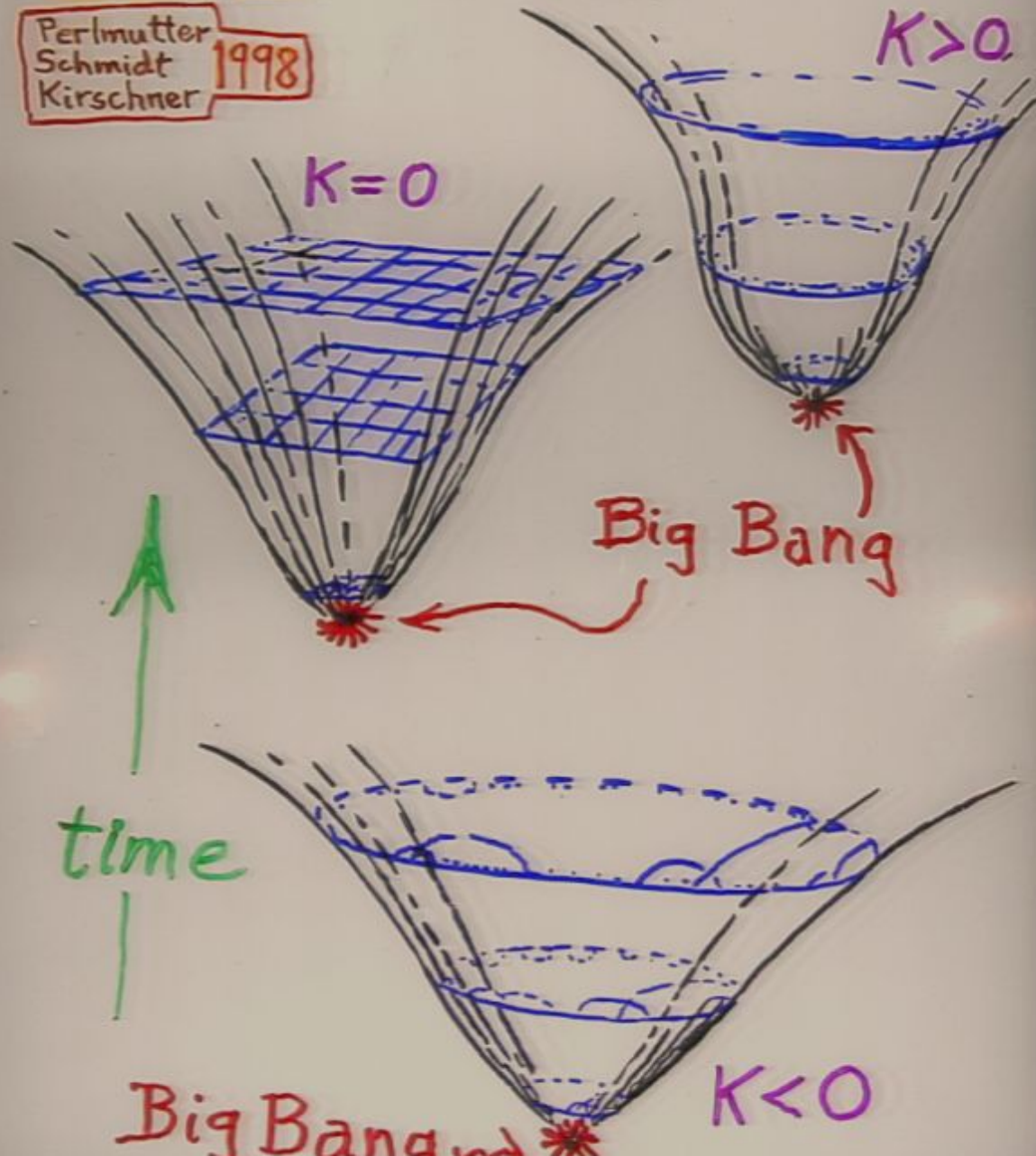
standard cosmologies, with $\Lambda > 0$
positive Cosmological constant
(Einstein 1917) "dark energy"

Perlmutter
Schmidt 1998
Kirschner

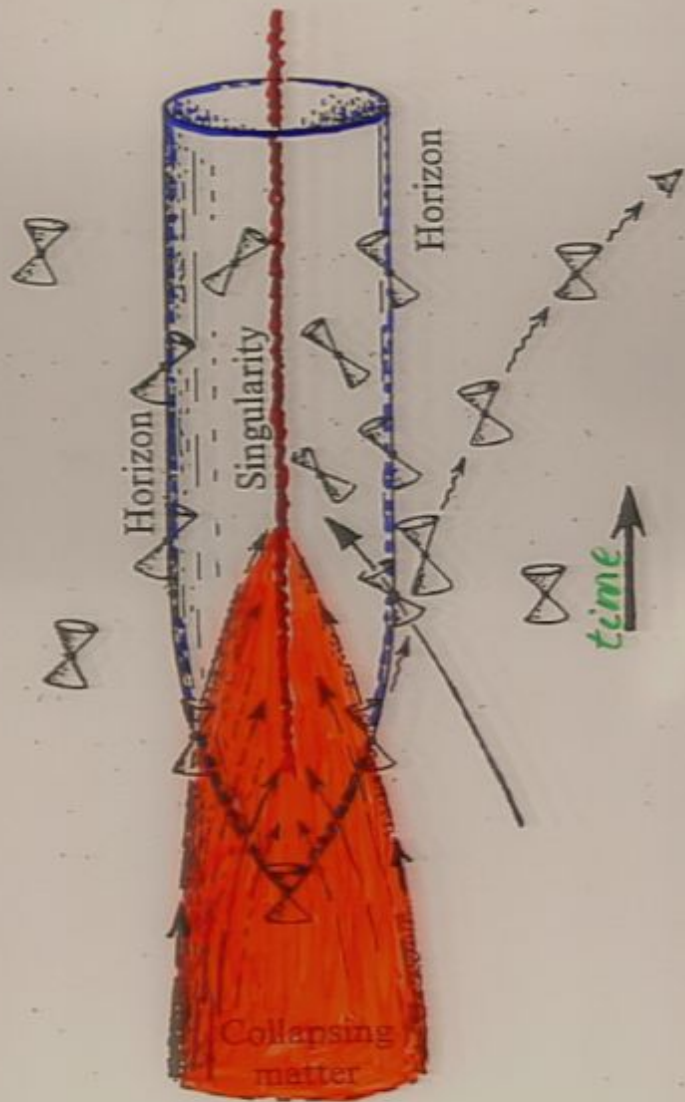


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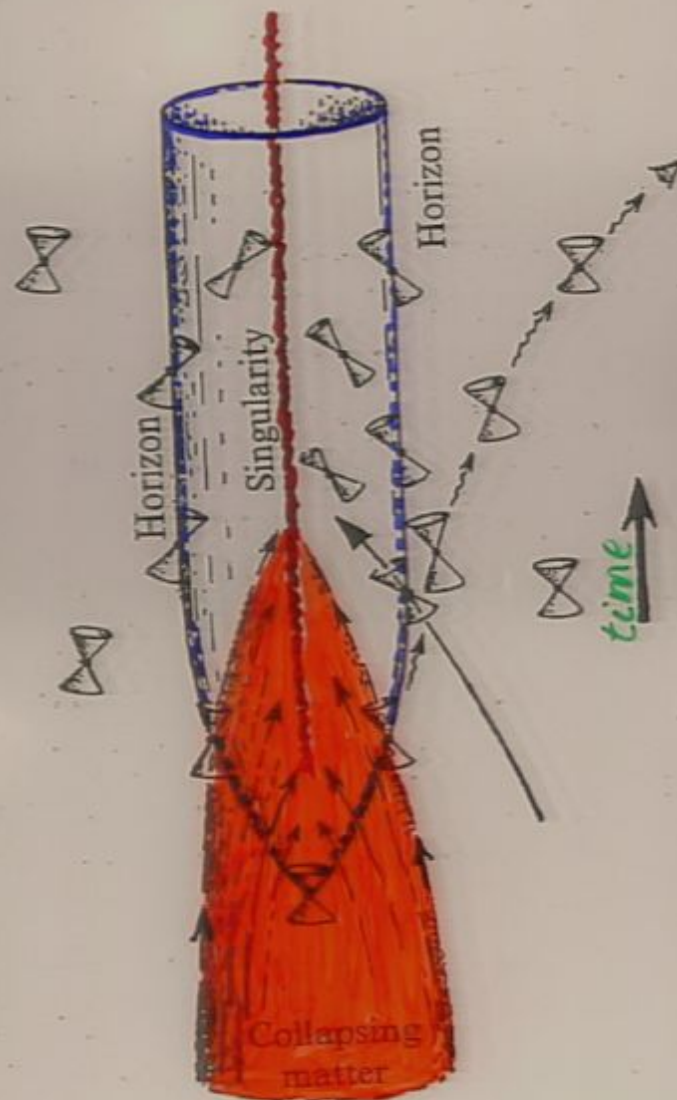
Perlmutter
Schmidt 1998
Kirschner



Collapse to a black hole

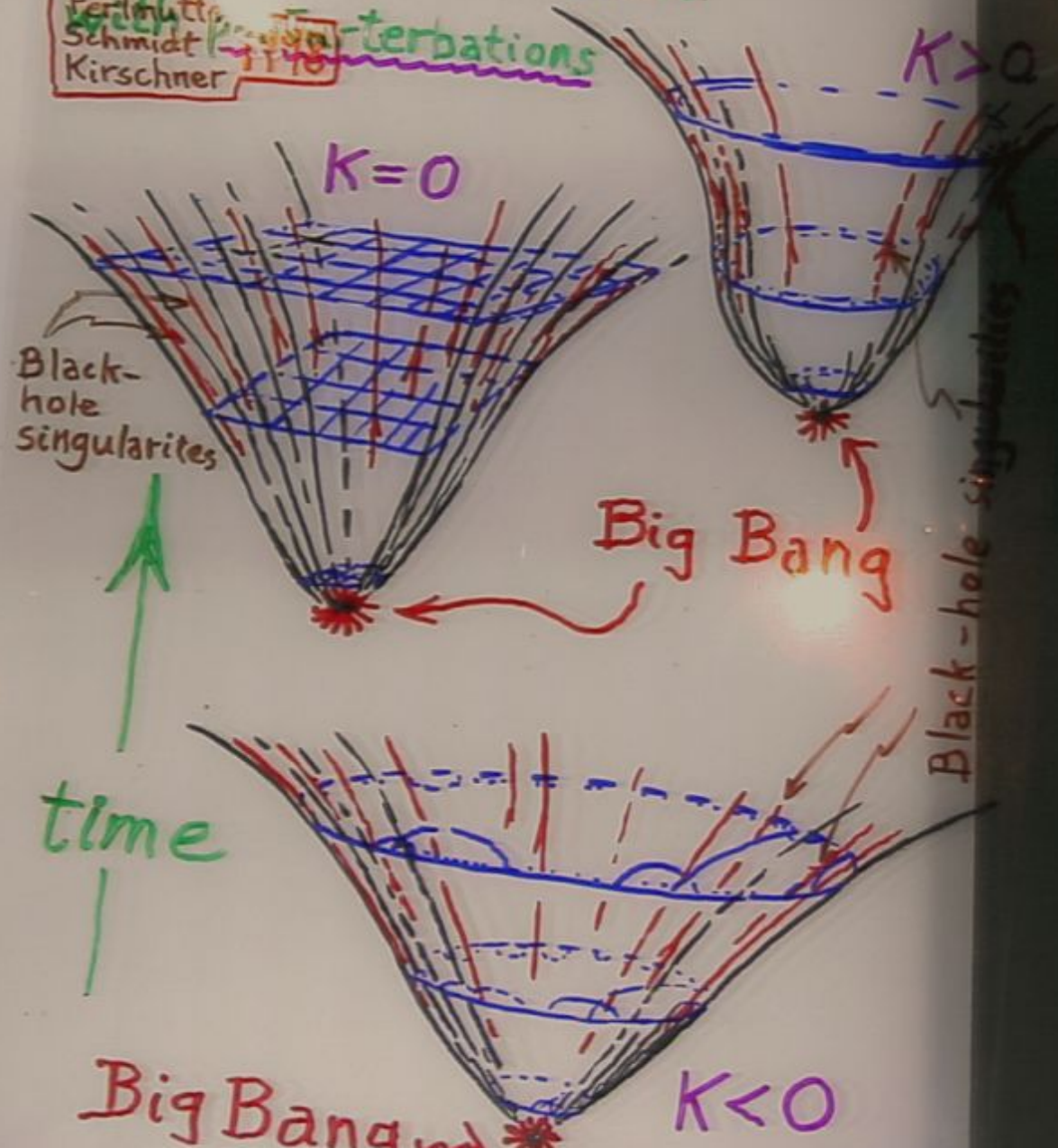


Collapse to a black hole



standard cosmologies, with positive Cosmological constant $\Lambda > 0$
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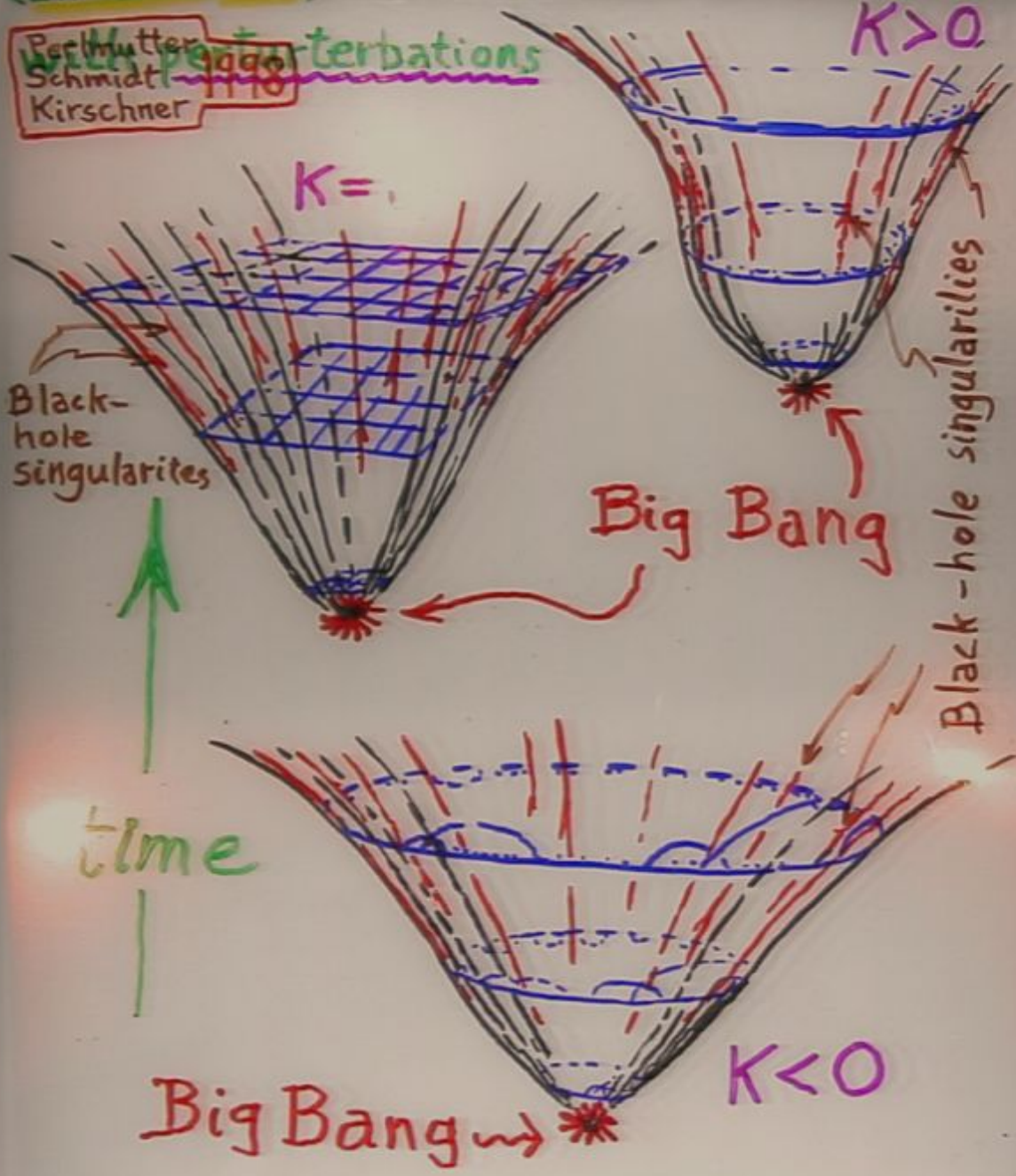
Perlmutter, Schmidt, Kirschner 1998 perturbations

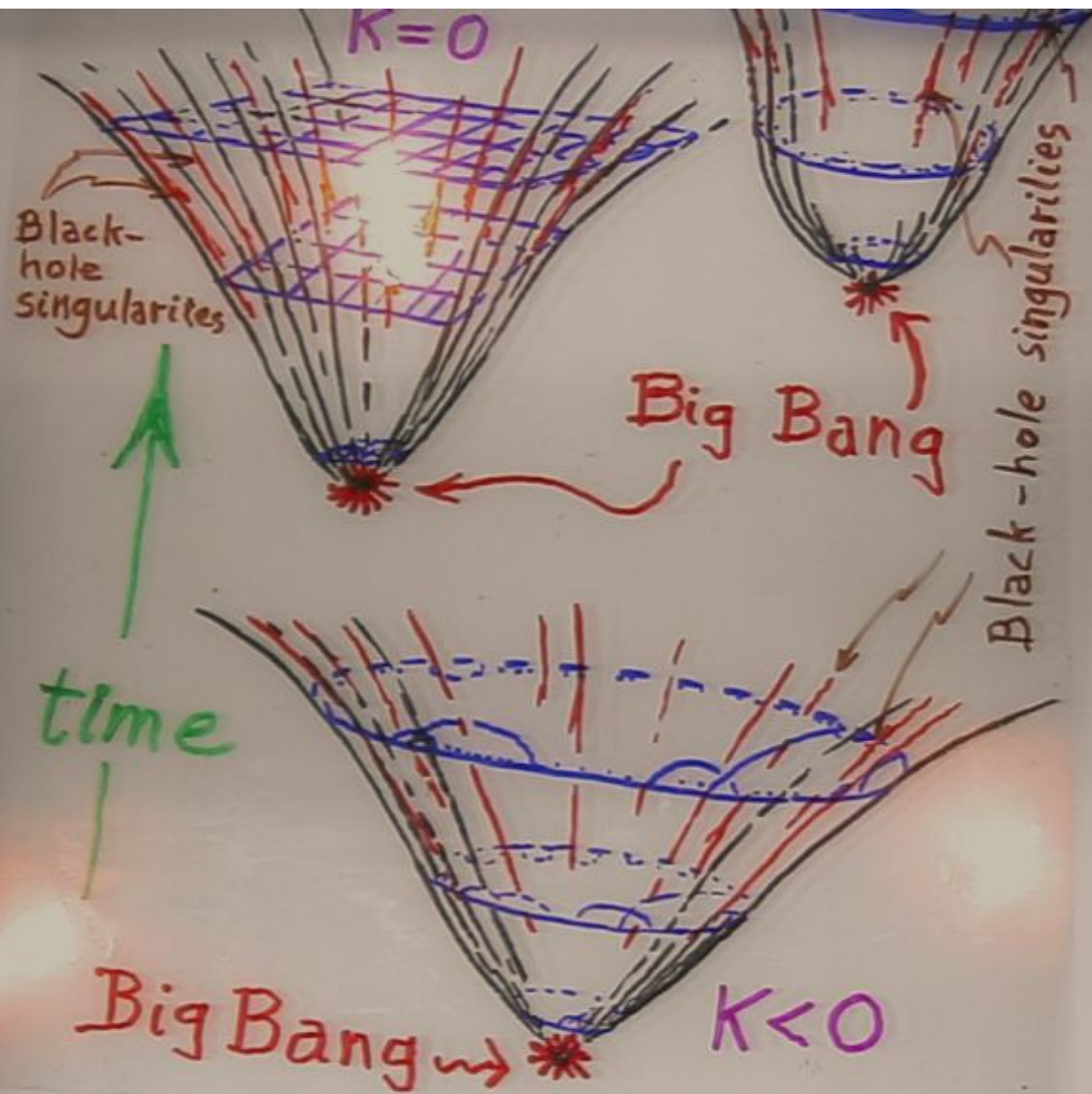


(Einstein 1917) dark energy

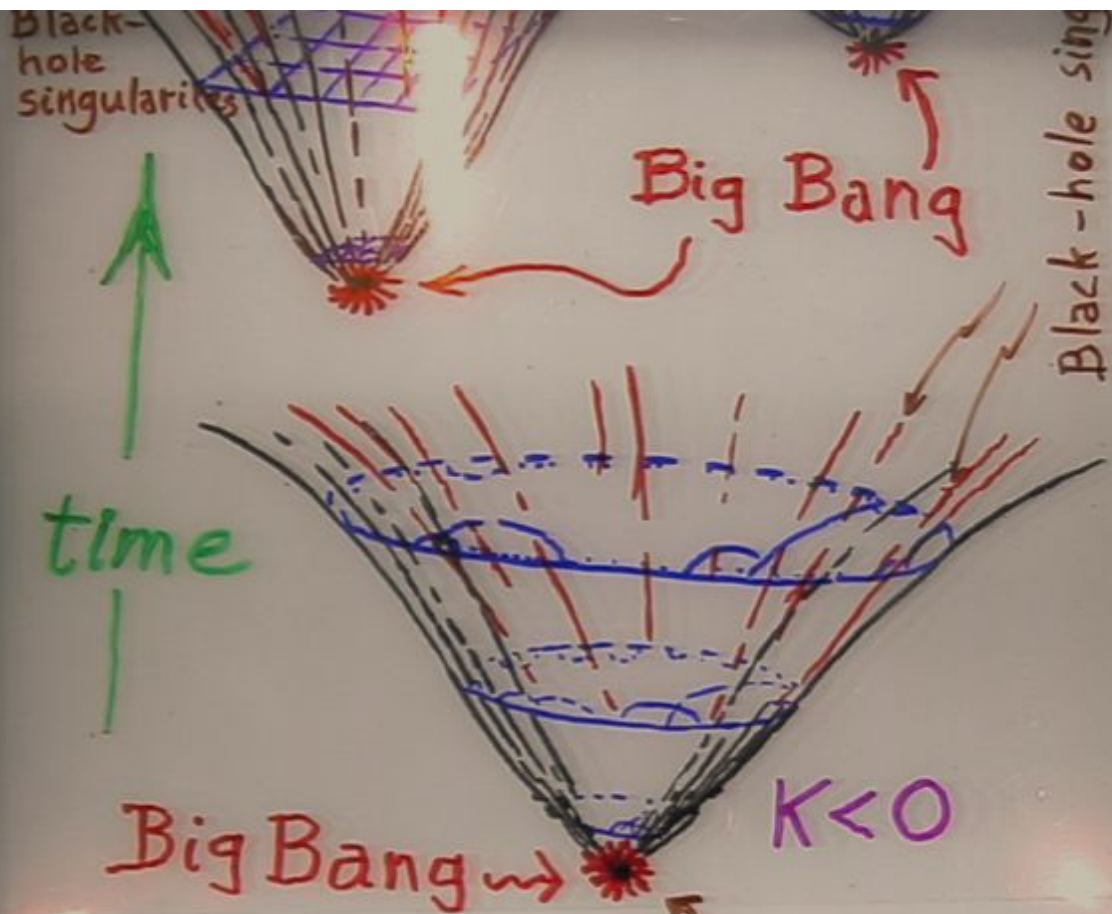
Perlmutter
Schmidt
Kirschner

perturbations





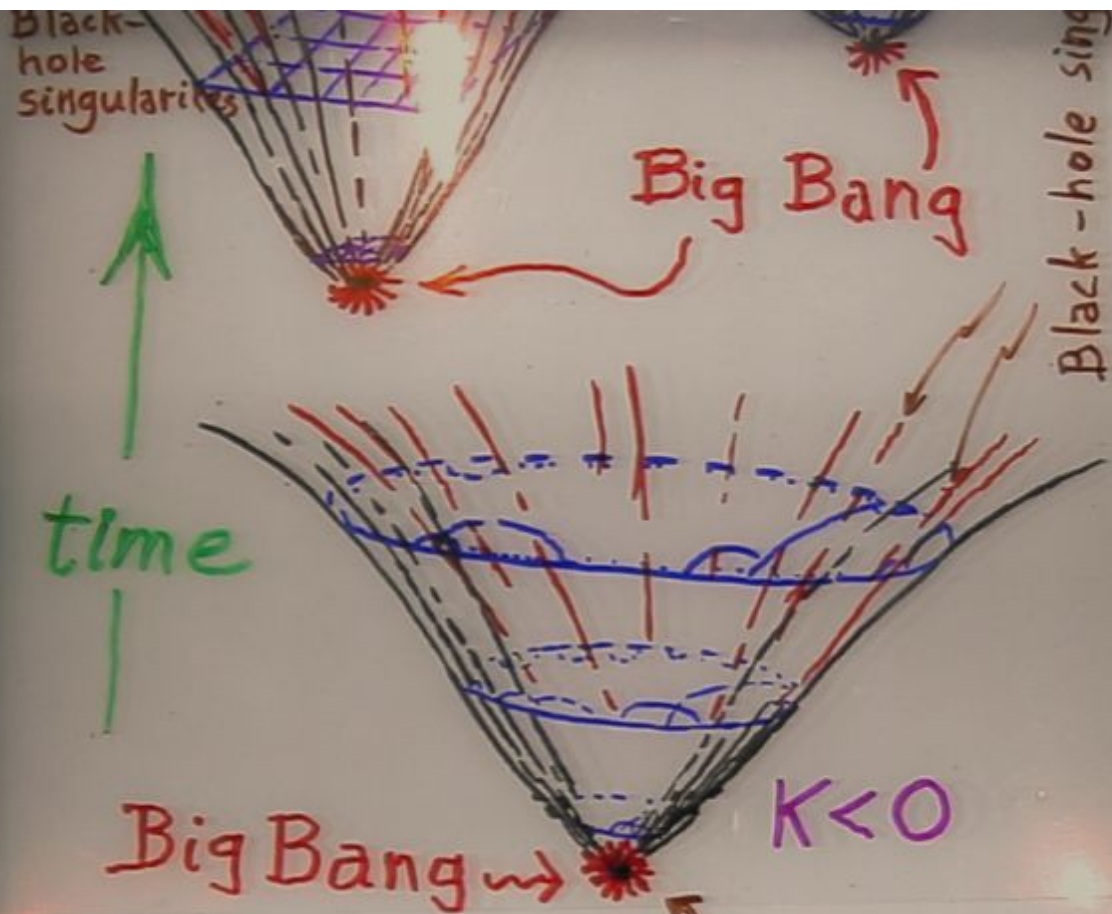
1 chance in $\gg 10^{10^{123}}$



Big Bang singularity was enormously constrained → 10^{10} part
 Gravitational degrees of freedom seem not to have been excited

Weyl curvature hypothesis:

Initial-type singularities (but not final ones) are constrained to have Weyl curv. ≈ 0



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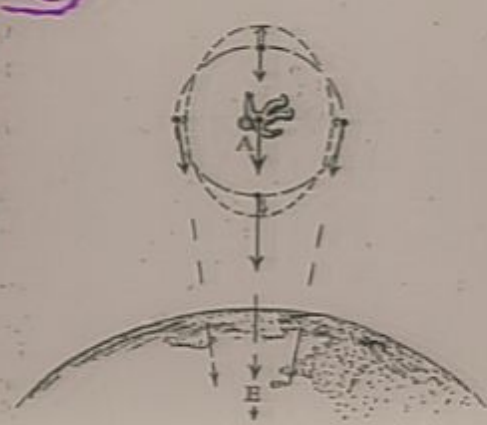
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Space-time curvature: tidal distortion

Full Riemann curvature = Weyl curv. + Ricci curv.

Free gravity



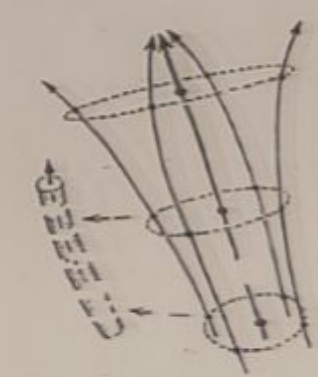
Matter source

spatial picture

(geodesic deviation in space-time)

time ↑

Free gravity



Matter source

Space-time curvature: tidal distortion

Full Riemann curvature

= Weyl curv. + Ricci curv.

Free gravity



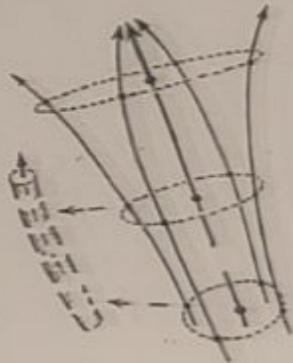
Matter source

spatial picture

(geodesic deviation in space-time)

time ↑

Free gravity



Weyl



Ricci

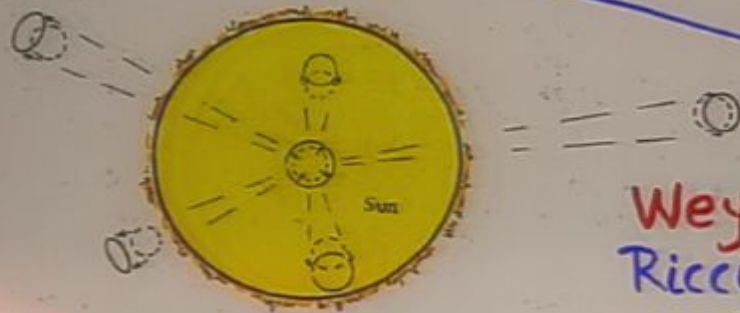
time ↑

Matter source

space-time picture

Effects of Weyl & Ricci (trace-free) space-time curvature on light rays

light bending due to gravitating body



Weyl: distortion
Ricci: magnification

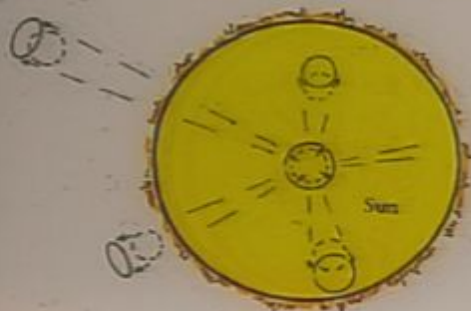
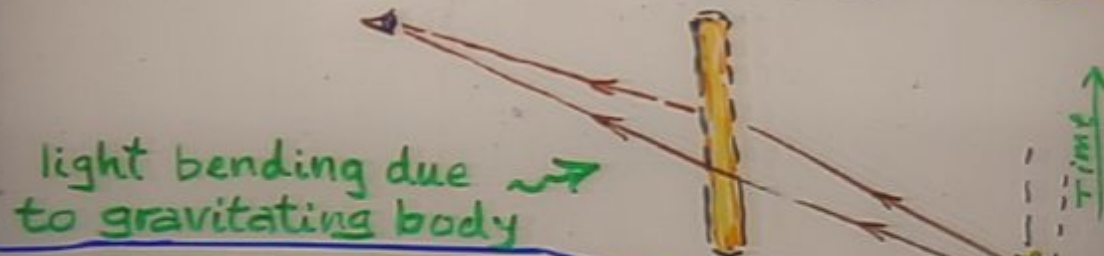
spatial picture



geodesic deviation of light rays

Weyl curvature = conformal curvature

Effects of Weyl & Ricci (trace-free) space-time curvature on light rays



spatial picture

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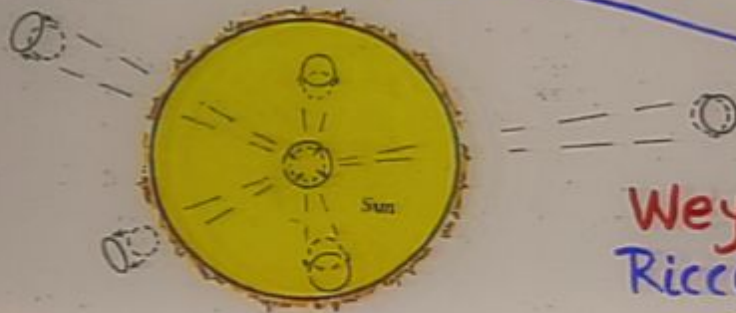


geodesic deviation of light rays

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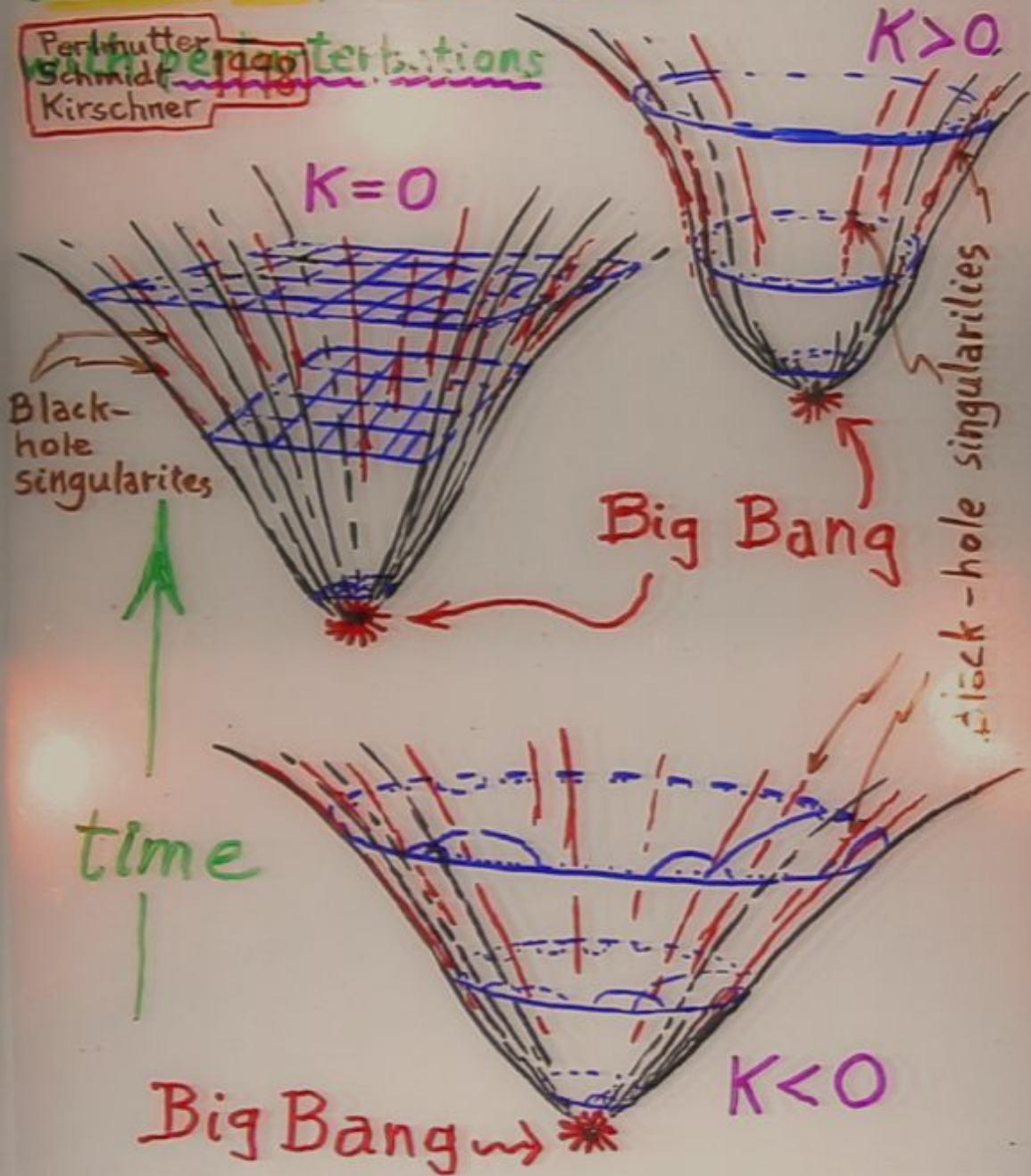
Weyl curvature = conformal curvature

GRAVITATIONAL LENSES IN ABELL 2218

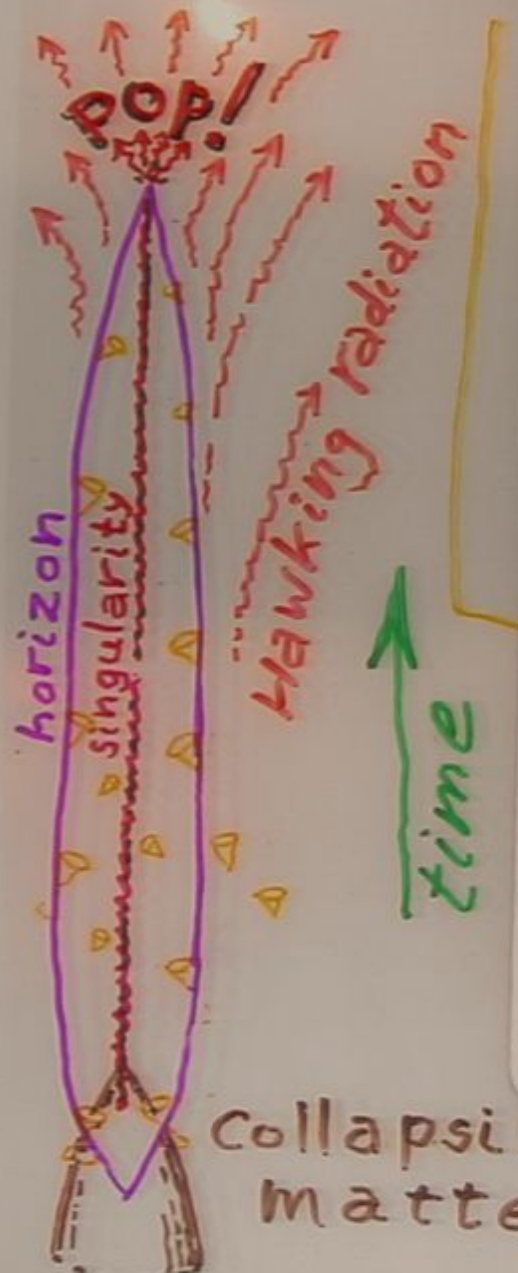


positive Cosmological constant
(Einstein 1917) "dark energy"

Perlmutter
Schmidt
Kirschner



Hawking Black

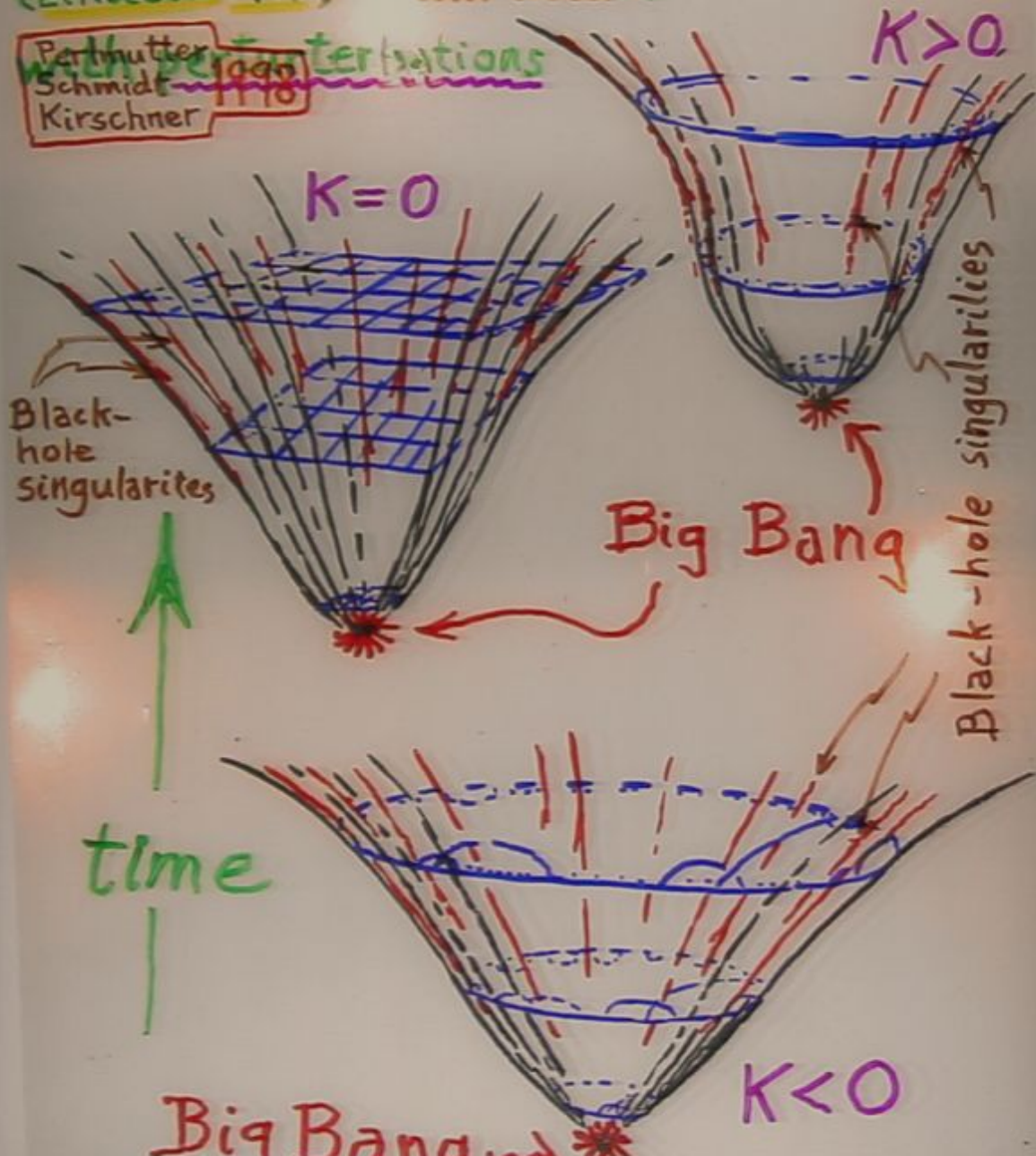


collapsing matter

of singular
TIPs

standard cosmologies, with $\Lambda > 0$
positive Cosmological constant
(Einstein 1917) "dark energy"

Perlmutter
Schmidt 1998
Kirschner 1998
with perturbations



Conformal geometry

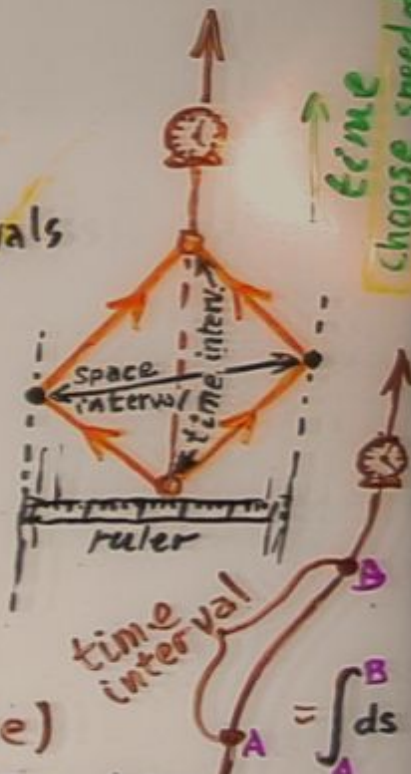
Metric up to local scale changes

Angles and small shapes, not length

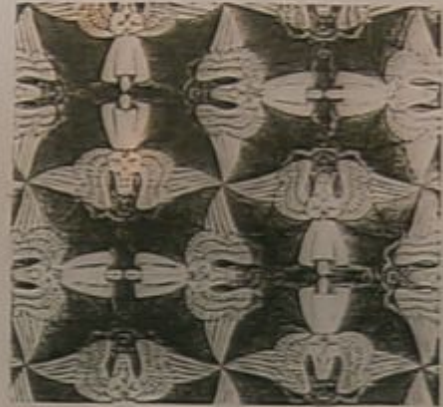
E.g. in Escher's circle limits, the hyperbolic geometry agrees with the Euclidean background

Beltrami
Poincaré

Space-time conformal geom.
= light-cone structure

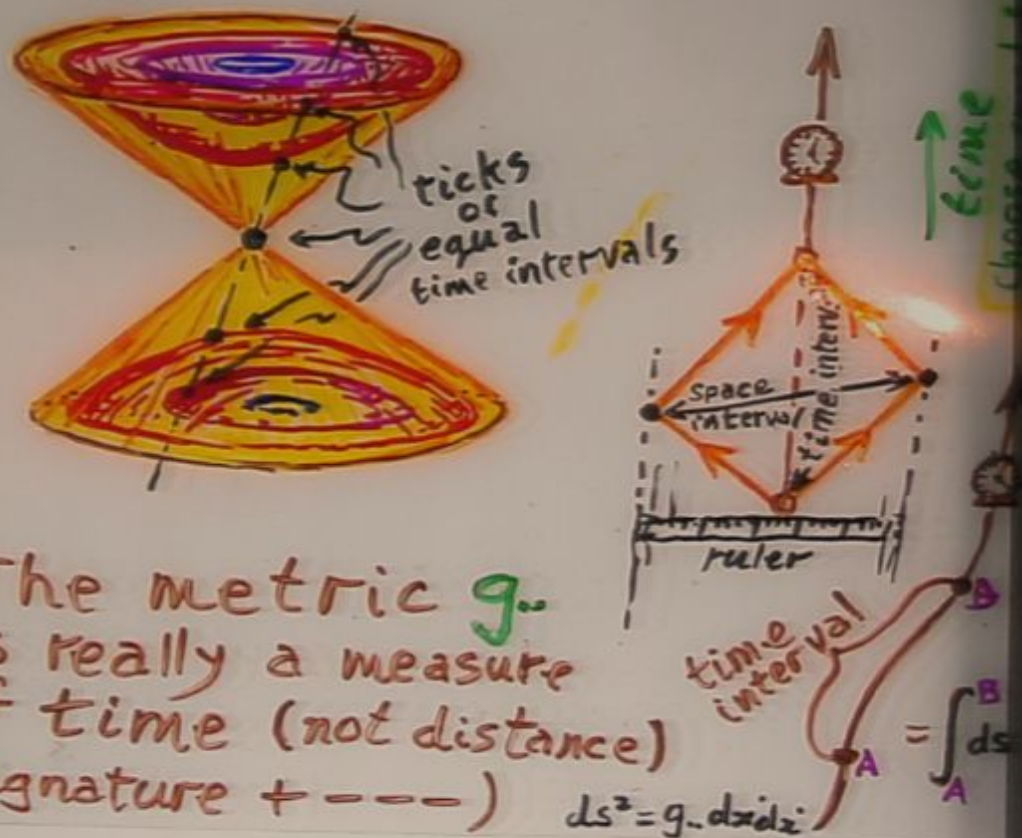


The metric $g_{\mu\nu}$ is really a measure of time (not distance) (signature $(-+++)$)



Metric up to local scale changes
 Angles and small shapes, not lengths
 E.g. in Poincaré's circle limits, the
 hyperbolic geometry agrees with
 the Euclidean background Beltrami
Poincaré

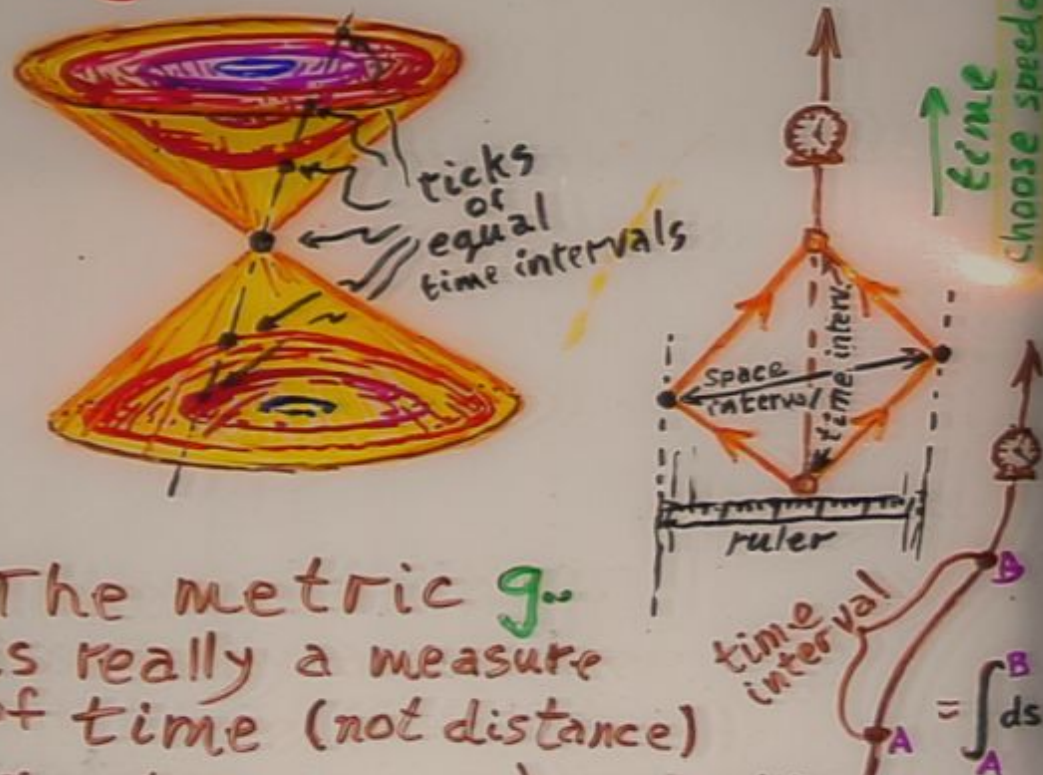
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The metric g_{ij}
 is really a measure
 of time (not distance)
 (signature + ---) $ds^2 = g_{ij} dx^i dx^j$

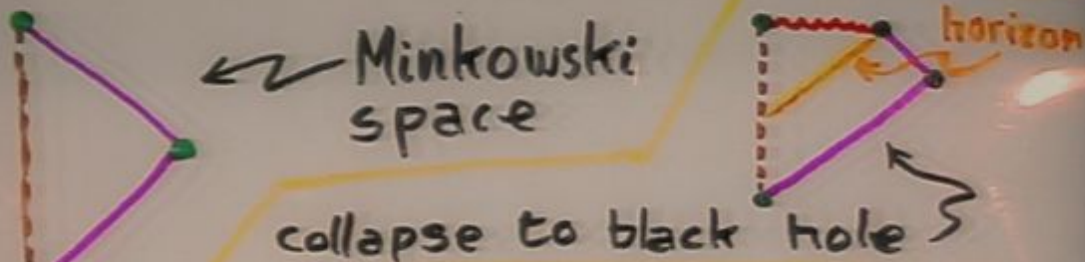
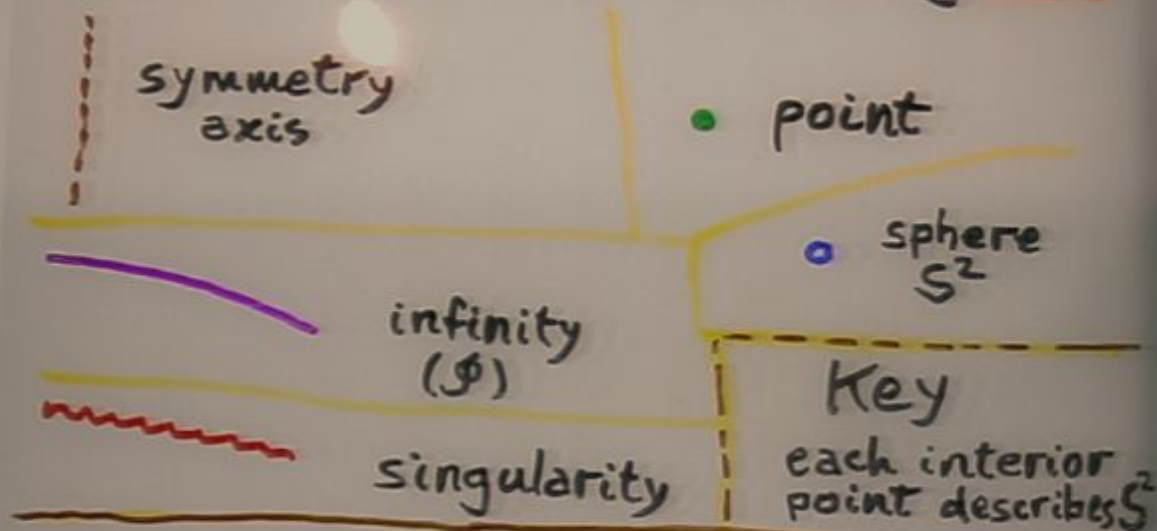
Conformal geometry
 Metric up to local scale changes
 Angles and small shapes, not length
 E.g. in Escher's circle limits, the hyperbolic geometry agrees with the Euclidean background Beltrami Poincaré

Space-time conformal geom.
 = light-cone structure

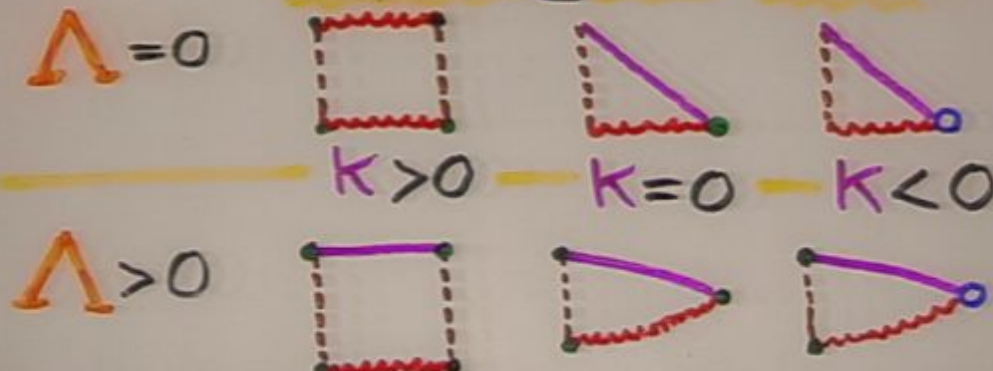


The metric g_{\dots} is really a measure of time (not distance)
 (signature + ---) $ds^2 = g_{\dots} dx^i dx^j$

Strict conformal diagrams



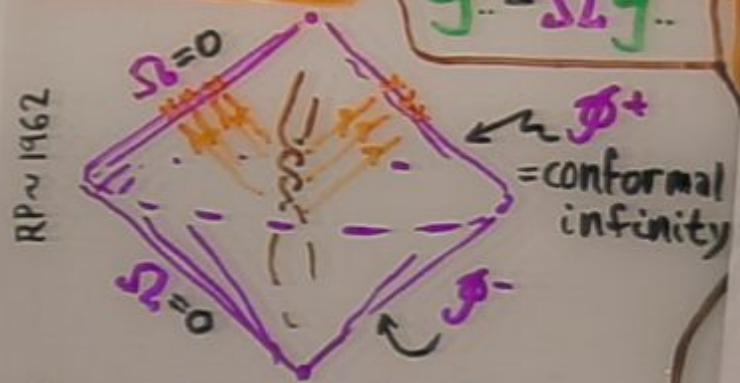
Cosmological models



2 Conformal "Mathematical Tricks"

Gravitational radiation

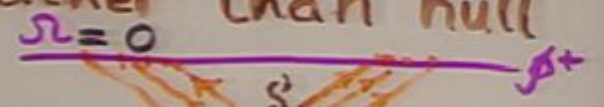
$$\hat{g} = \Omega g$$



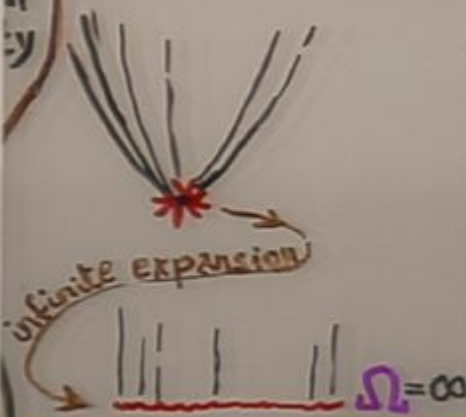
Asymptotically flat space-time $\Lambda = 0$

Trick: shrink ∞ to a finite place by taking $\Omega = 0$ there

When $\Lambda > 0$, this still works (in some sense better (RP Friedrich) - easier) but then \mathcal{I}^+ is spacelike rather than null



Cosmological singularities

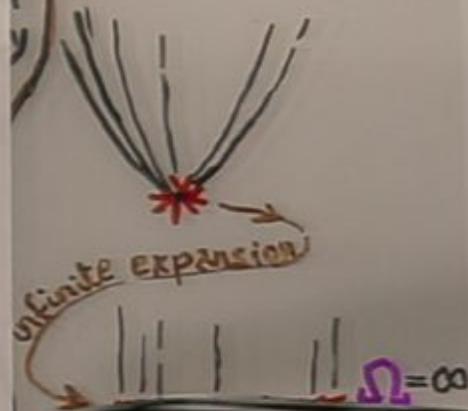


Trick: expand out singularity to obtain a conformally smooth initial hypersurface

Tod's form of Weyl curvature hypothesis:
this works!

physical metric

Cosmological singularities

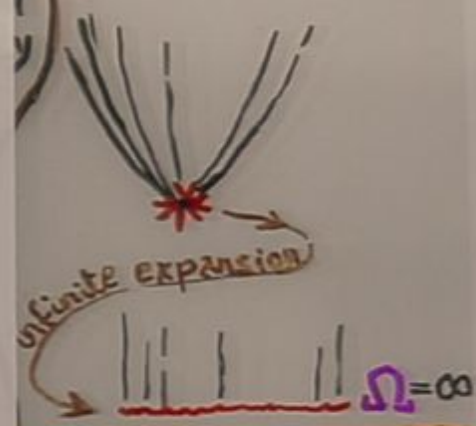


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2 Conformal Mathematical Tricks

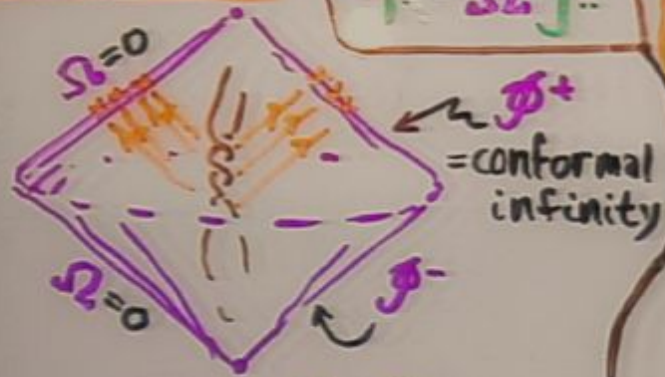
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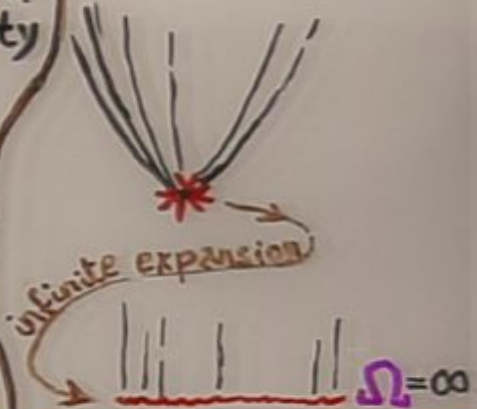
$$\hat{g} = \Omega^2 g$$

Cosmological singularities

RP ~ 1962



Asymptotically flat space-time $\Lambda = 0$

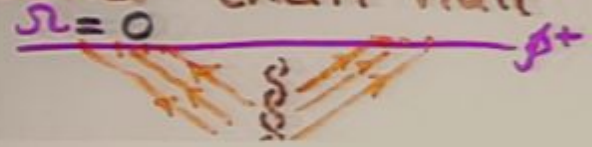


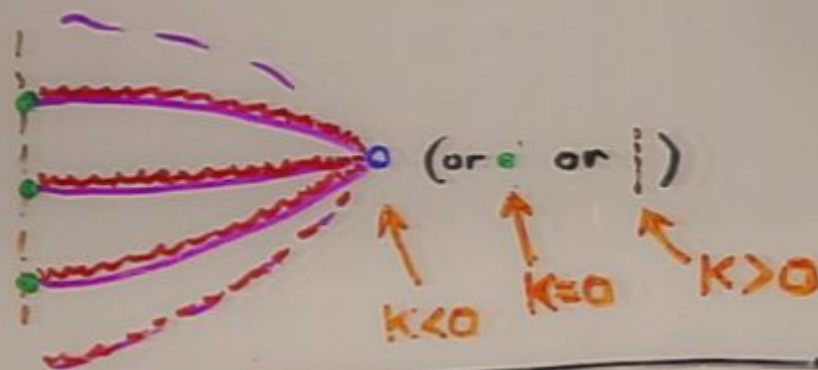
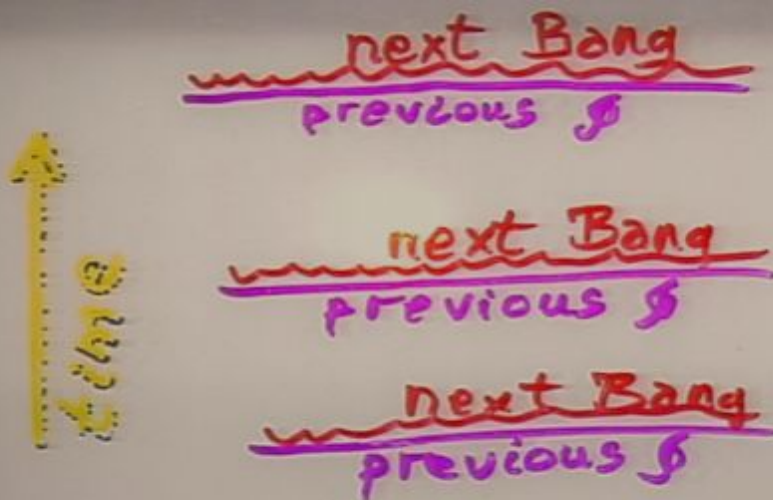
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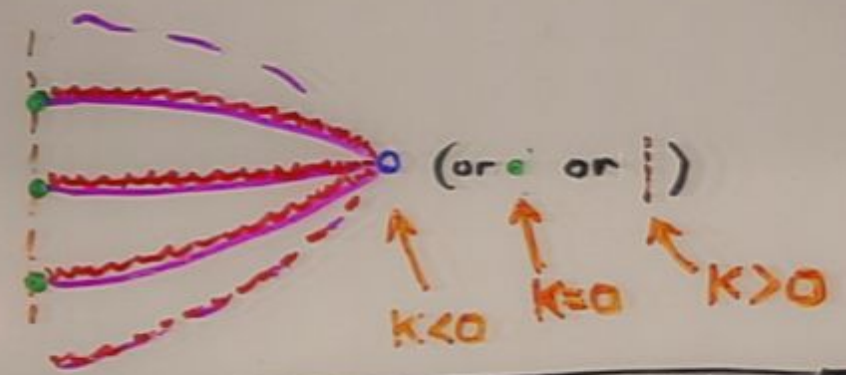
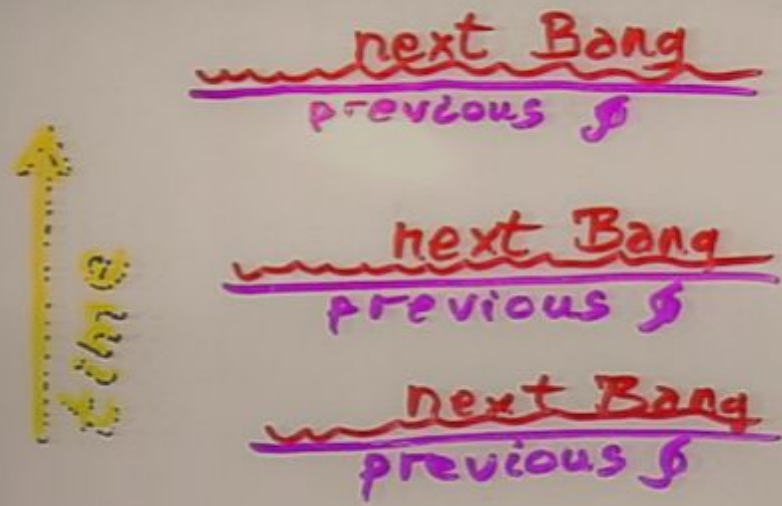
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Requirements / predictions

- Good → • Tod form of Weyl curvature hypothesis :: 2nd Law in form observed
- Questionable → • Need electrons to lose their mass, ultimately (or some other possibility)
- ↳ • Proton decay (or ultimately lose mass)
 - ↳ • All black holes ultimately decay away.
 - ↳ • Quantum aspects of fields eventually go.
 - ↳ • Conformal invariance at very high energies.
- ("K" renorm.)
- Observational? • Primordial grav. waves, density fluct.



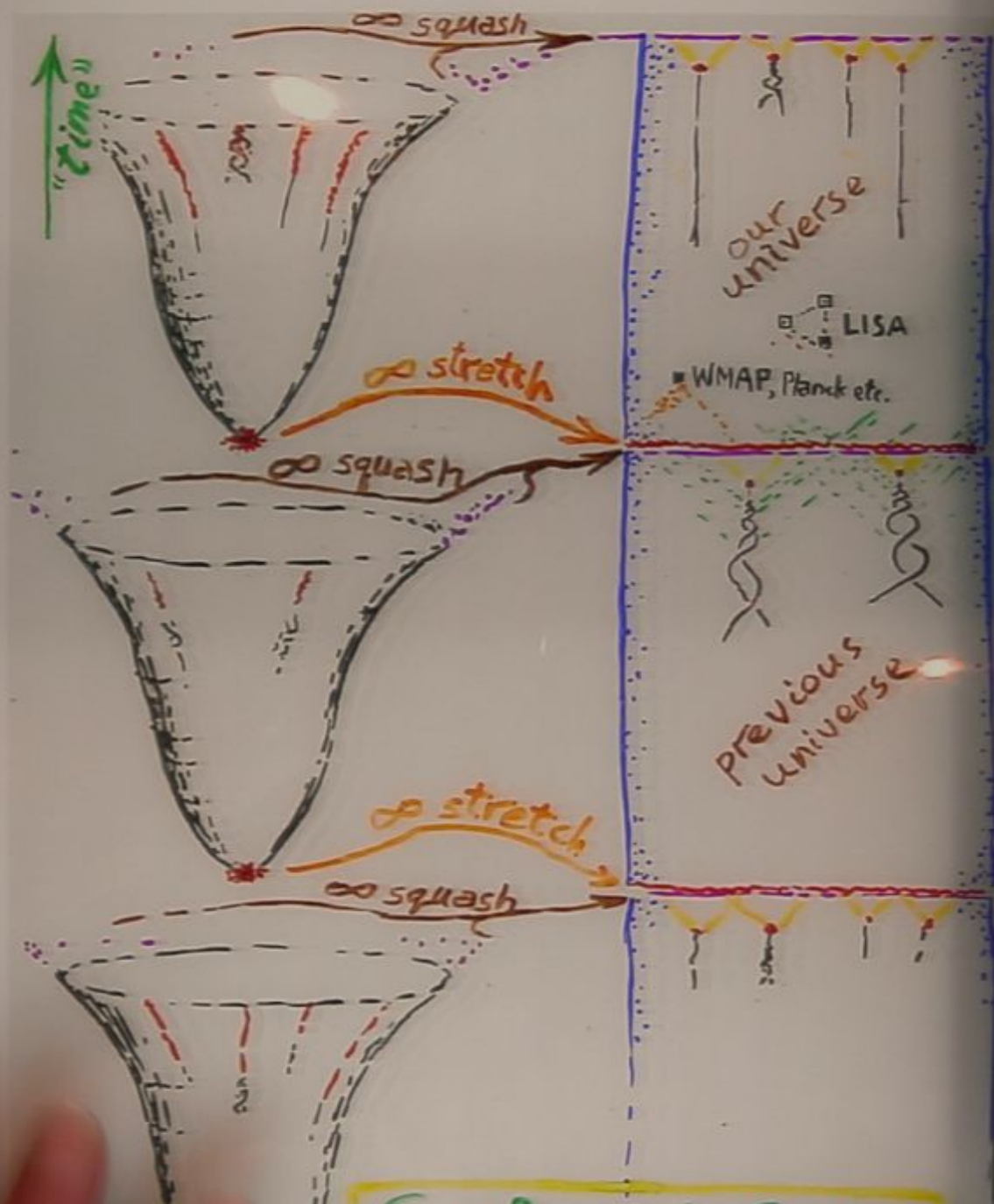
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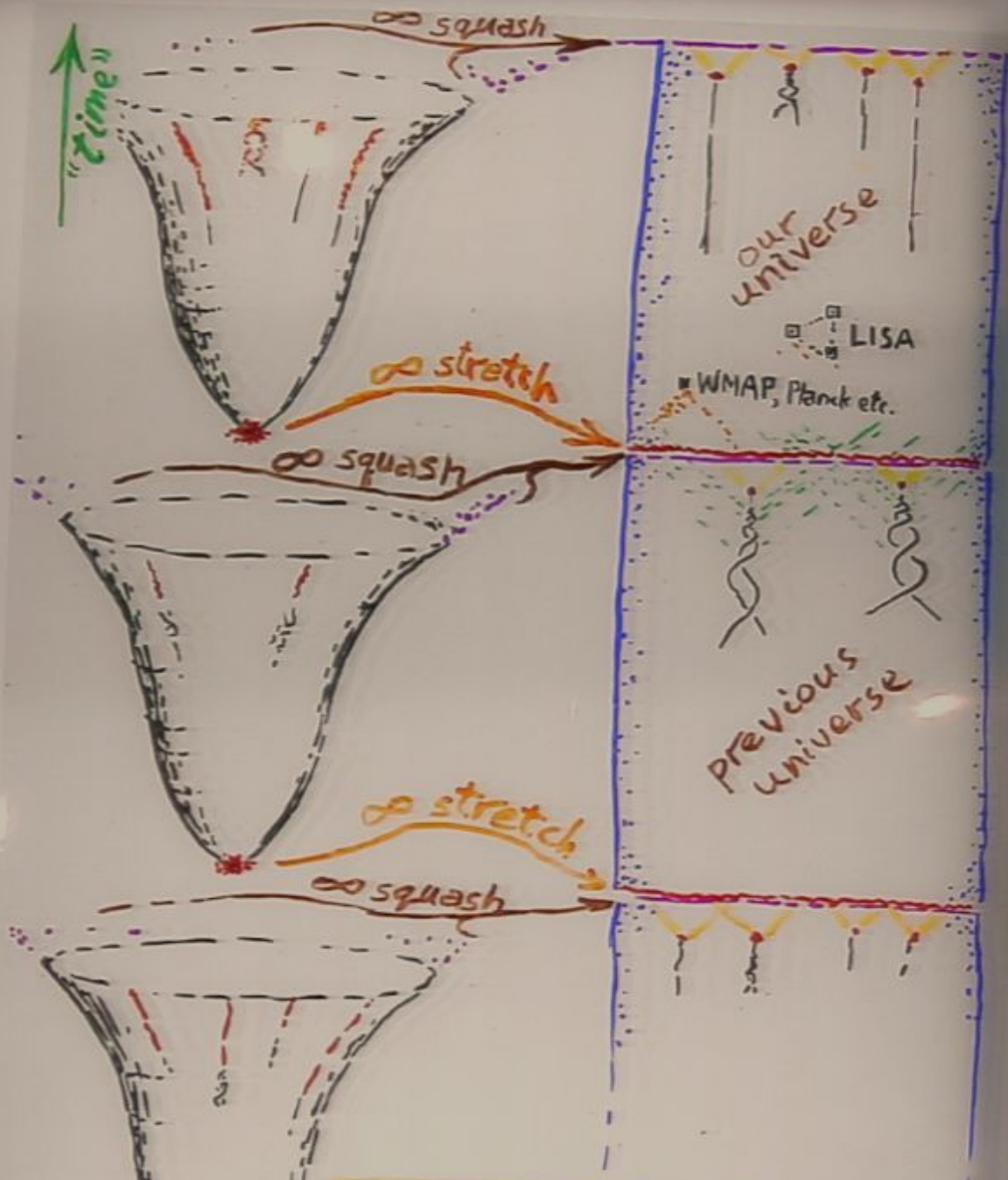
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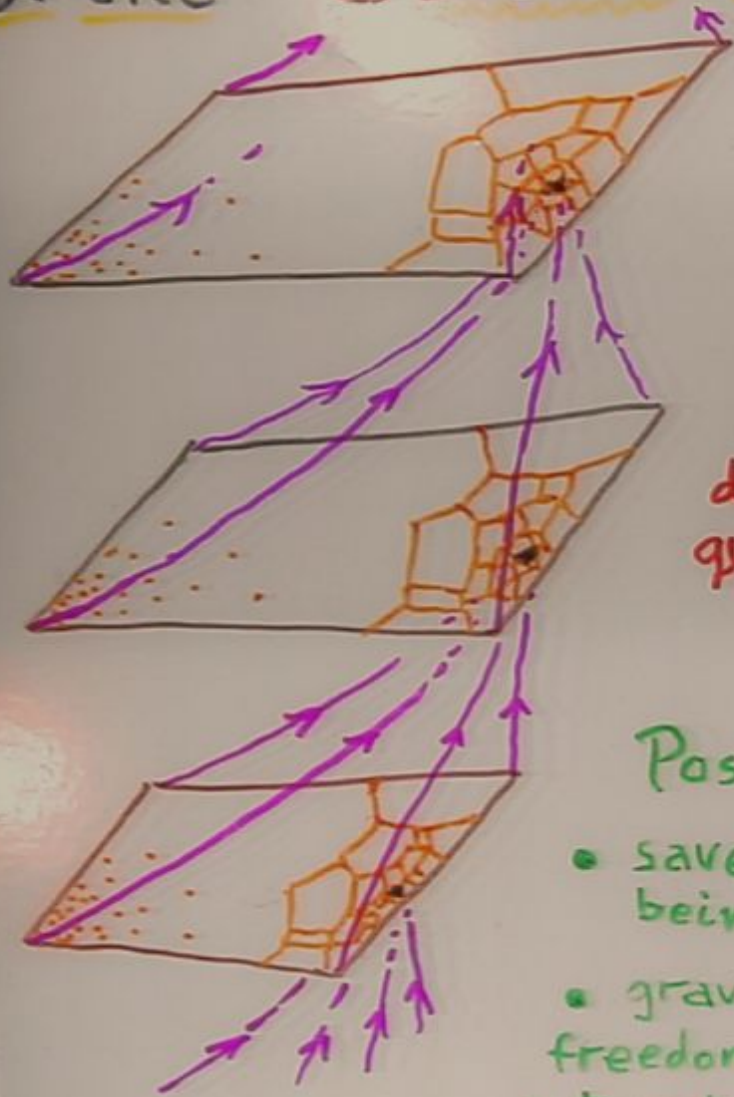
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Conformal Cyclic

Phase-space Volume Loss & the Second Law



N.B. phase space has a natural volume measure determined by quantum theory

$$\left(\frac{dp_n dq_n}{\hbar}\right)^n$$

Possibilities:

- saved by volumes being infinite?
- grav. degrees of freedom "scale away"?
- \hbar gets "renormalized"?
- balanced by "information loss paradox" in Hawking black-hole evaporation. **Best bet**

