

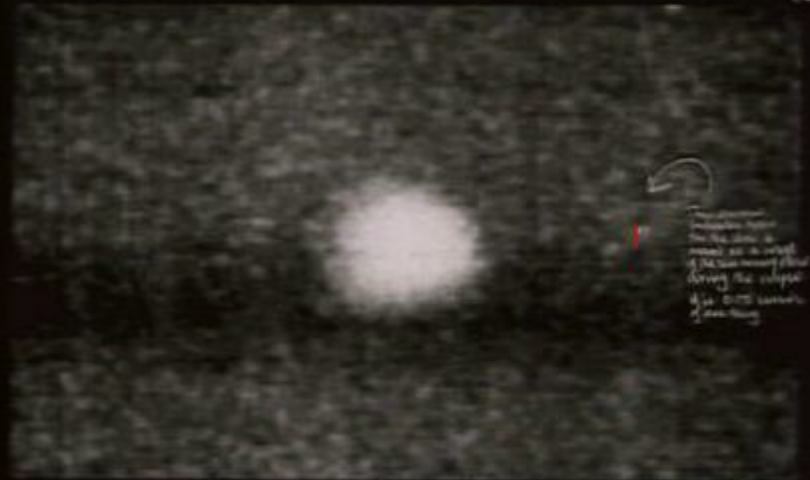
Title: General Relativity - Part 2

Date: Aug 01, 2006 10:45 AM

URL: <http://pirsa.org/06080001>

Abstract:

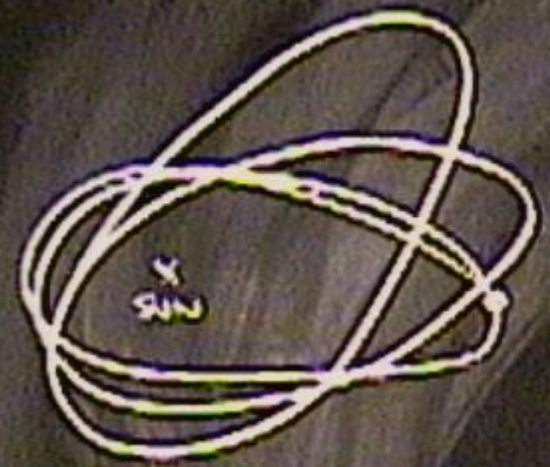
1919 Verification



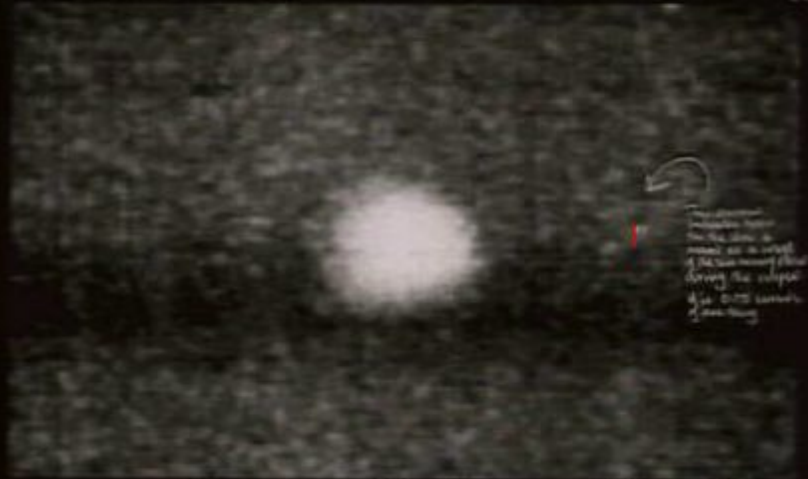
This image is magnified 251 times, compared with glass plate.



The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.



1919 Verification

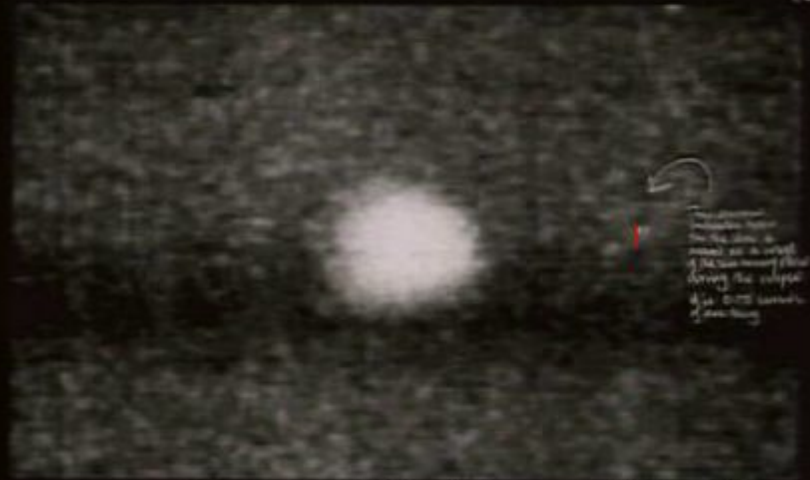


This image is magnified 251 times, compared with glass plate.



The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

1919 Verification



This image is magnified 251 times, compared with glass plate.



The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

General Relativity Test (1976)

65
Excess Time Delay,
Microseconds



Distance > 37 km



General Relativity Test (1976)

79
Excess Time Delay,
Microseconds



Sun

Earth

Mars

Distance > 37 km



General Relativity Test (1976)

96
Excess Time Delay,
Microseconds



Distance > 37 km

General Relativity Test (1976)

124
Excess Time Delay,
Microseconds



Distance > 37 km

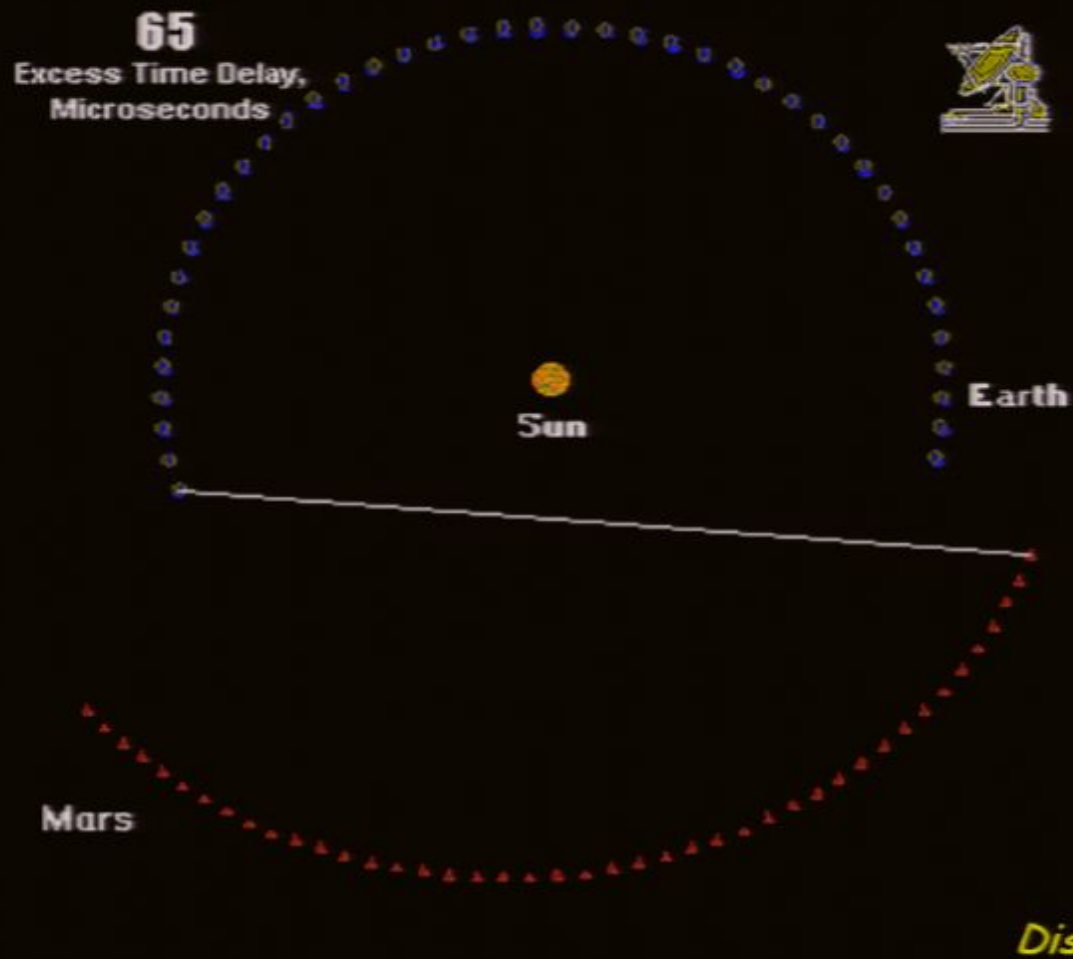
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Microseconds



Distance > 37 km

General Relativity Test (1976)

74
Excess Time Delay,
Microseconds



Distance > 37 km

General Relativity Test (1976)

124
Excess Time Delay,
Microseconds



Distance > 37 km

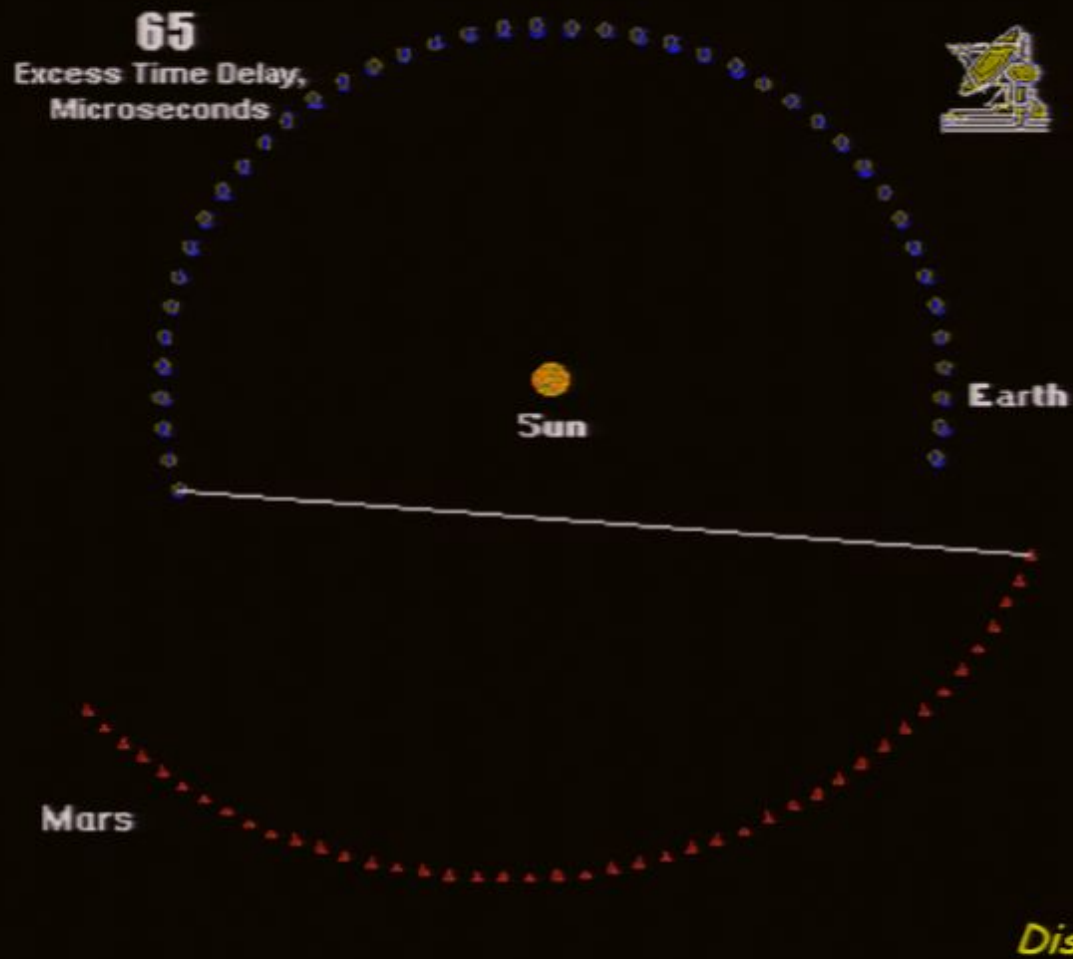
General Relativity Test (1976)



General Relativity Test (1976)



General Relativity Test (1976)



General Relativity Test (1976)

60
Excess Time Delay,
Microseconds



Distance > 37 km

General Relativity Test (1976)

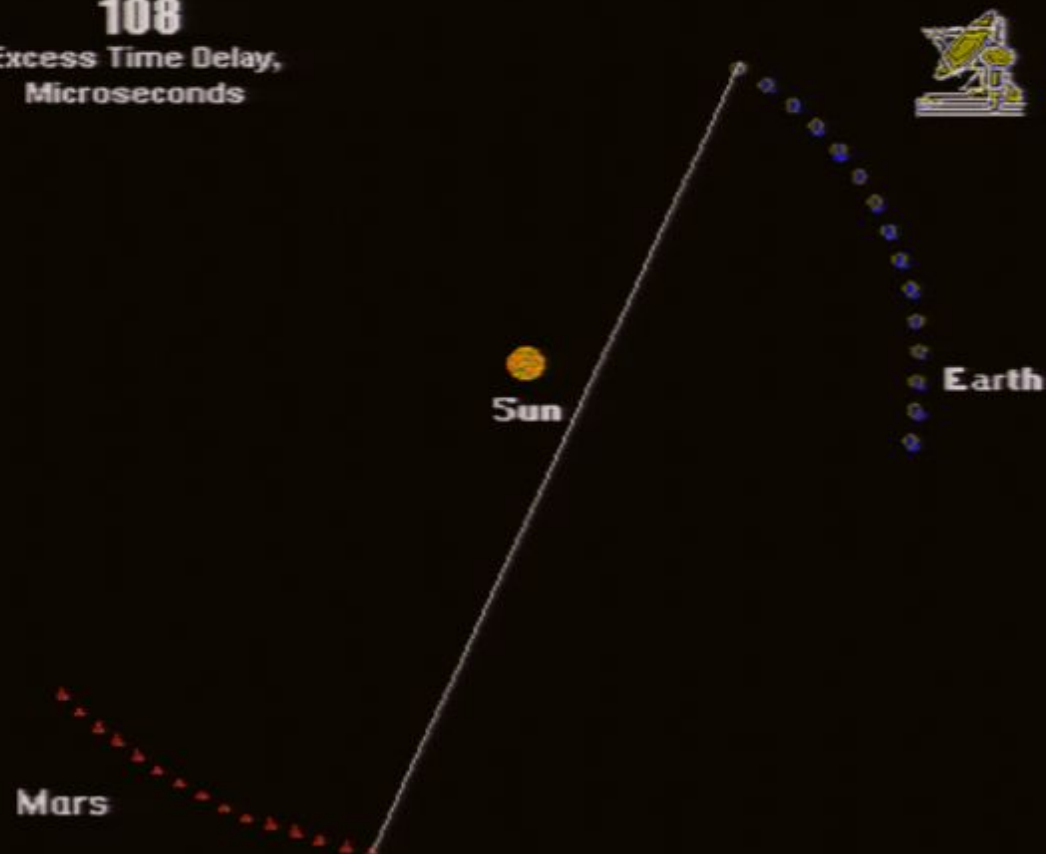
74
Excess Time Delay,
Microseconds



Distance > 37 km

General Relativity Test (1976)

108
Excess Time Delay,
Microseconds



Distance > 37 km

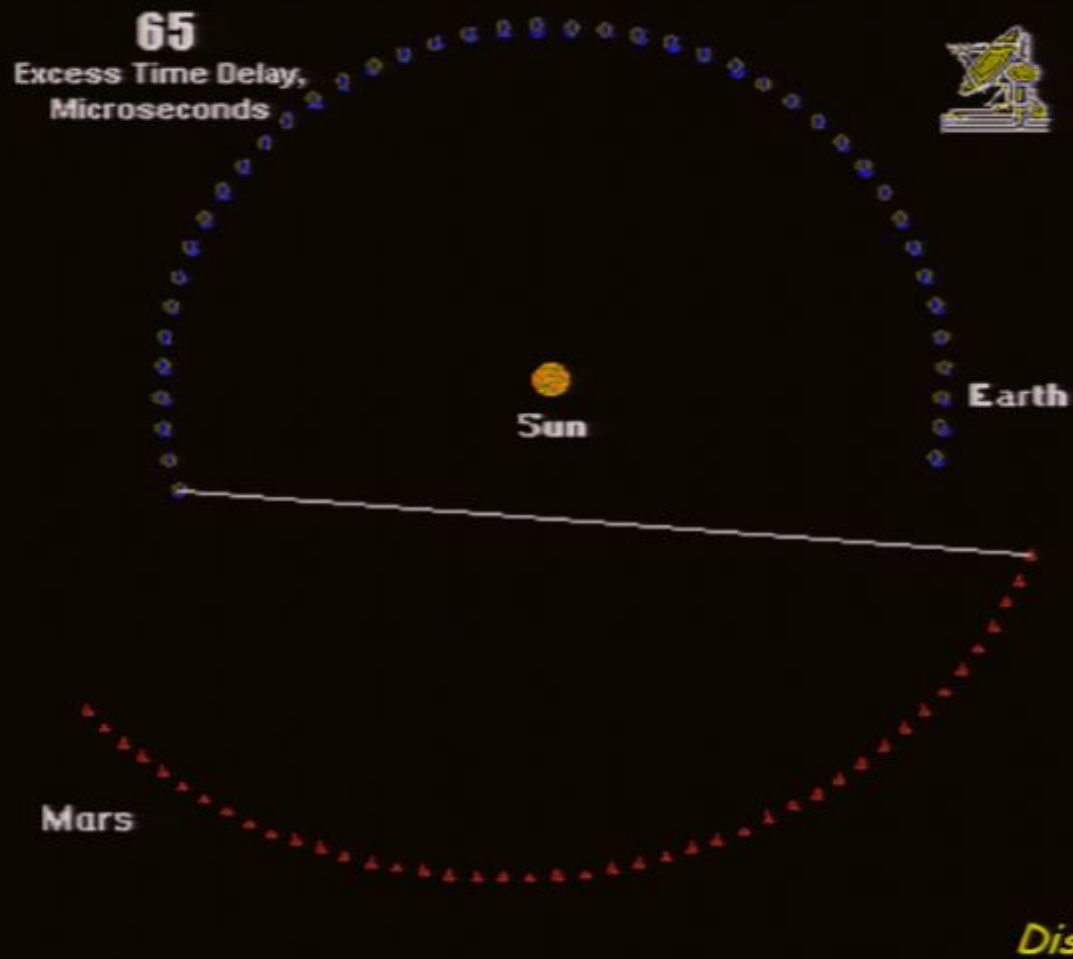
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Distance > 37 km



Karl Schwarzschild (1876-1916)

Calculation of Schwarzschild radius

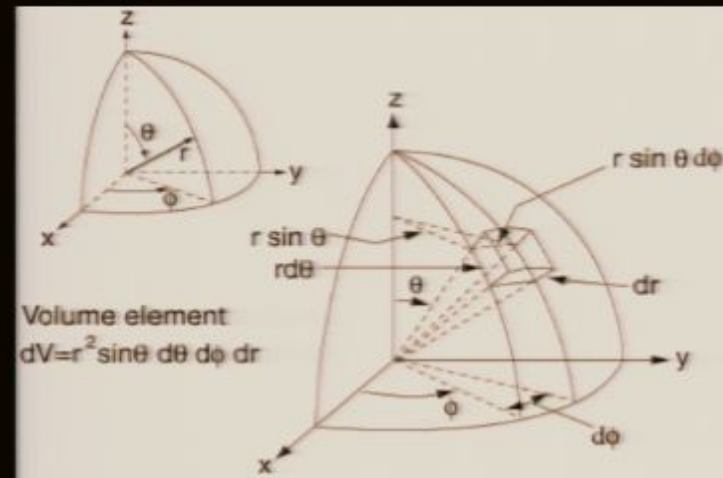
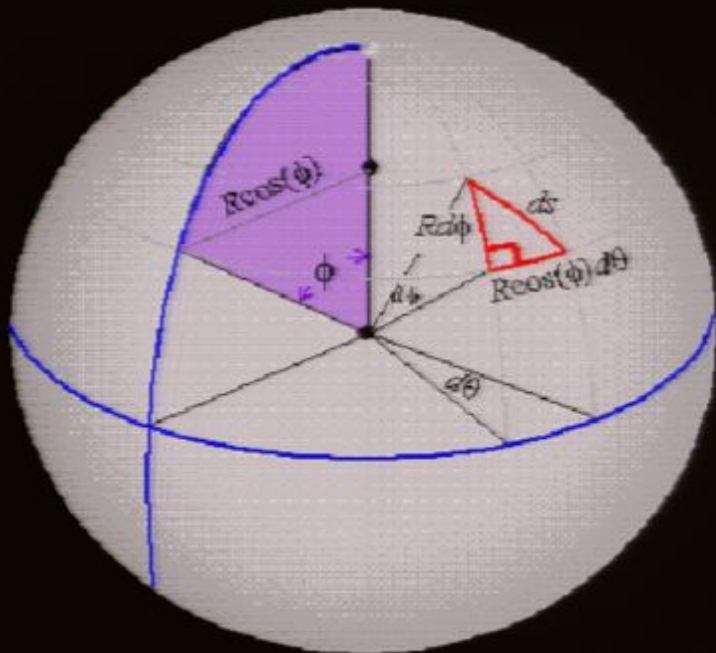
- ***In 1916 Karl Schwarzschild discovers a solution of the Einstein field equation, which describes a nonspinning, uncharged spherical body.***
- ***Did this when serving in the German Army on the Russian front of World War I***
- ***Only required a few days to solve equation and describe spacetime curvature.***
- ***Einstein presented solution on behalf of Shwarzschild to the Academy of Sciences.***
- ***Schwarzchild was killed 4 months later.***

The Schwarzschild Radius

$$ds^2 = -\left(1 - \frac{r_s}{r}\right) c^2 dt^2 + \frac{dr^2}{\left(1 - \frac{r_s}{r}\right)} + r^2 (d\theta^2 + \sin^2(\theta) d\phi^2)$$

$$r_s = \frac{2GM}{c^2}$$

r, θ, ϕ are the polar coordinates



Schwarzschild Metric



Schwarzschild Metric

$$\tau^2 = t^2 - s^2 \quad \leftarrow \text{Timelike Spacetime Metric}$$

Schwarzschild Metric

$$d\tau^2 = dt^2 - dx^2 - dy^2 \leftarrow \text{2D flat Spacetime in Cartesian}$$

Is the square of the wristwatch time between two events as marked by x, y, t



Schwarzschild Metric

$$(d\tau)^2 = (dt)^2 - (dr)^2 - (rd\phi)^2 \iff 2D \text{ flat Spacetime in Polar}$$

Schwarzschild Metric

$$d\tau^2 = \left(1 - \frac{r_s}{r}\right) c^2 dt^2 - \frac{dr^2}{\left(1 - \frac{r_s}{r}\right)} - r^2 d\phi^2$$



*Curvature added, now
Schwarzschild timelike
Spacetime Metric*

$$r_s = \frac{2GM}{c^2}$$

Schwarzschild Metric

$$d\sigma^2 = -\left(1 - \frac{2M}{r}\right) dt^2 + \frac{dr^2}{\left(1 - \frac{2M}{r}\right)} + r^2 d\phi^2$$

The metric describes the shape of spacetime outside of matter. Once you hit matter, be it some gas, a star, a planet, or a rock, this metric no longer applies.

You can see that, if $r = 2M$, dt term would be zero. That is to say that at the event horizon there would be no change in time. Makes sense; you can look at the event horizon as being the place where time "stops." The dr factor deals with how close to something you are. You'll notice that it "blows up" when $r = 2M$.

Schwarzschild Metric

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Spacelike Fo^{\wedge}

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$$d\tau^2 = \left(1 - \frac{2M}{r}\right) dt^2 - \frac{dr^2}{\left(1 - \frac{2M}{r}\right)} - r^2 d\phi^2$$

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Schwarzschild radii for different objects

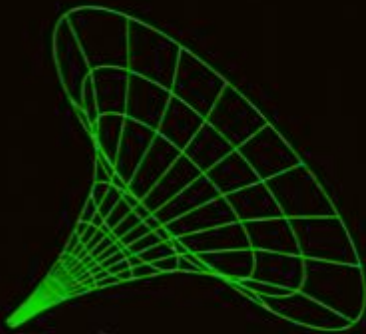
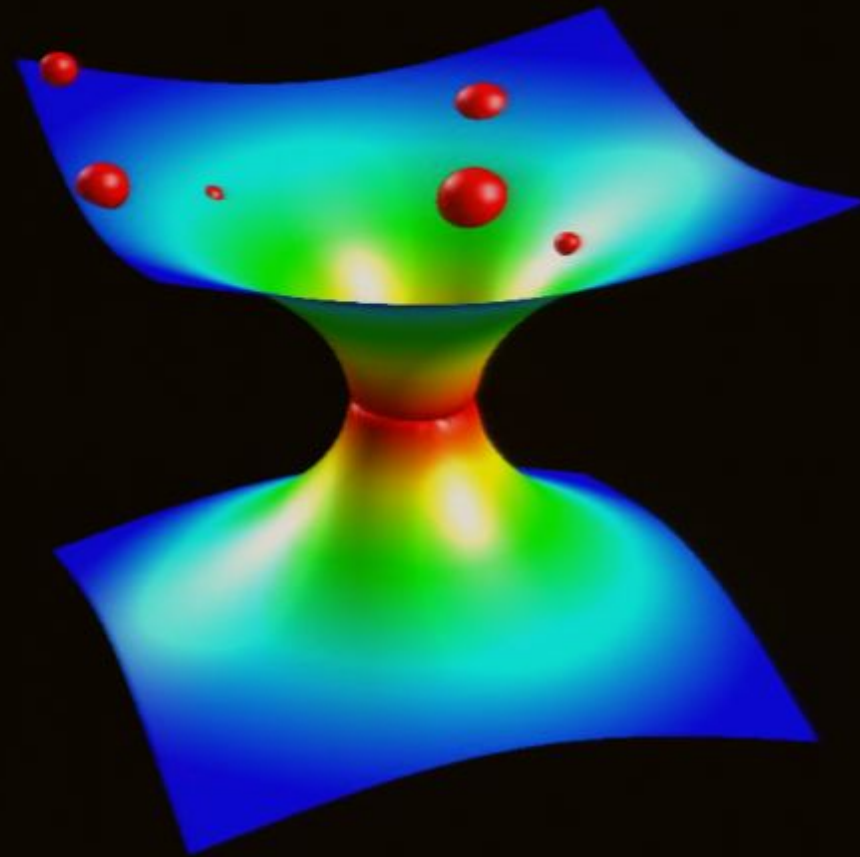
Object	Mass	R_S
Atom	10^{-26} kg	10^{-51} cm
Human Being	70 kg	10^{-23} cm
Earth	6.0×10^{24} kg	0.89 cm
Sun	2.0×10^{30} kg	3.0 km
Galaxy	$10^{11} M_S$	10^{-2} l.y.
Universe (if closed)	$10^{23} M_S$	10^{10} l.y.

$$r_s = \frac{2GM}{c^2}$$



Embedding Diagram

*Emphasis on
Spatial rather
than temporal
interpretations*

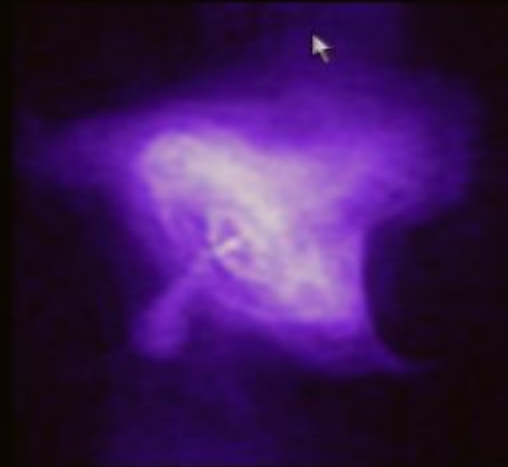


Sir Arthur Eddington



- *1926 Book - The internal constitution of the Stars*
- *Early proponent of Einstein's Theory of General Relativity (next to Einstein best expert on General Relativity)*
- *Poses the mystery of white dwarfs and attacks the reality of black holes predicted by Schwarzschild.*
- *Believed White Dwarf was last state in a stars life (rock Star)*
- *Paradox with White Dwarf*

Subrahmanyan Chandrasekhar



- Idolized Eddington, resolved Eddington's paradox*
- In 1930 he showed that there is a maximum mass for White Dwarfs*
- 1935 Eddington attacks his work. "Chandra" left the field of Blackholes until 1970's*
- Nobel Prize in Physics 1983*



Walter Baade and Fritz Zwicky



- *Identifies the process of a supernovae, predicted that this collapse strips the atoms of their electrons, packing the nuclei together as a neutron star.*

- *Neutron stars would not be verified observably until 1968.*

- *Identified the galaxies associated with cosmic radio sources.*

- *Still something was missing that took a star from fusion to supernovae.*



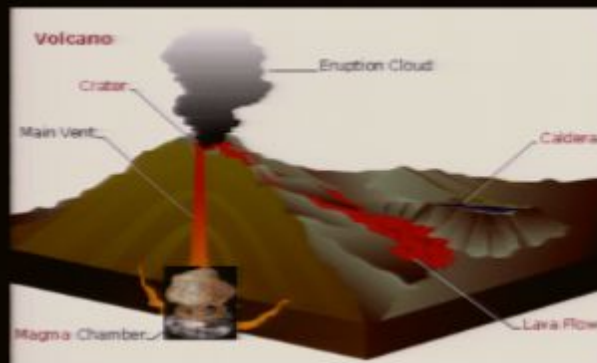
Robert J. Oppenheimer

- *Showed that there is a maximum mass for a neutron star from 1.5 to about 3 solar masses (1938).*
- *In a highly idealized calculation, showed that an imploding star forms a black hole.*
- *Led the American atomic bomb project.*
- *Which provided the opportunity to experimentally verify and test theories (too expensive for the universities) and the development of the atomic bombs which mimic the power source for the sun to come up with the mathematics and understanding of stellar mechanics*
- *Major battle with Wheeler.*



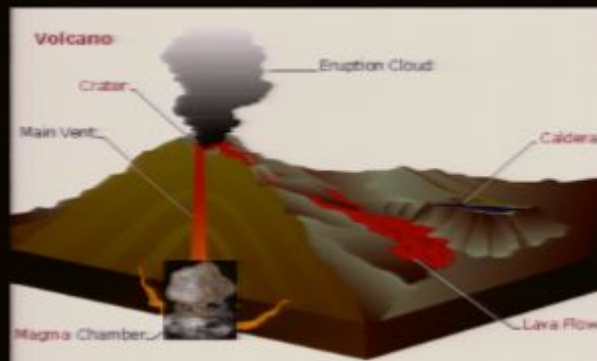
Yakov Zel'dovich

- *Soviet counterpart to Oppenheimer.*
- *Developed the theory of nuclear chain reactions. (1939)*
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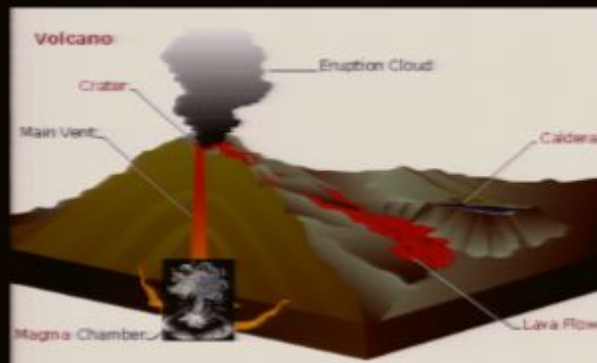
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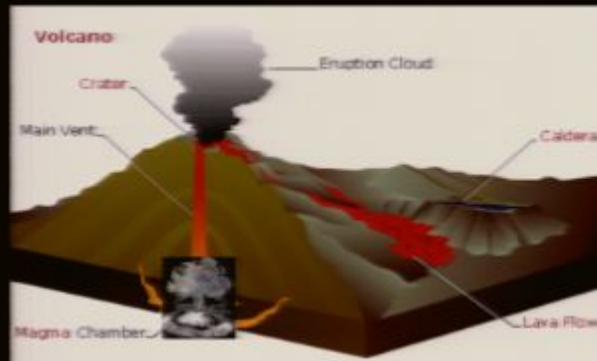
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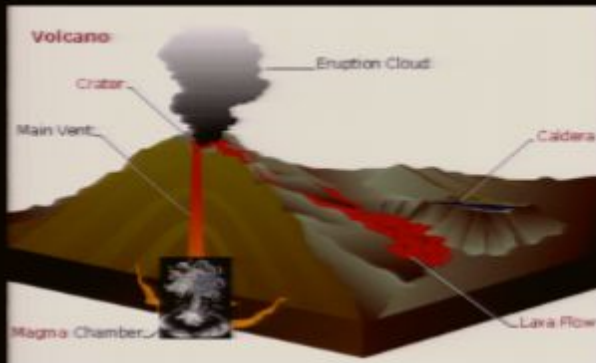
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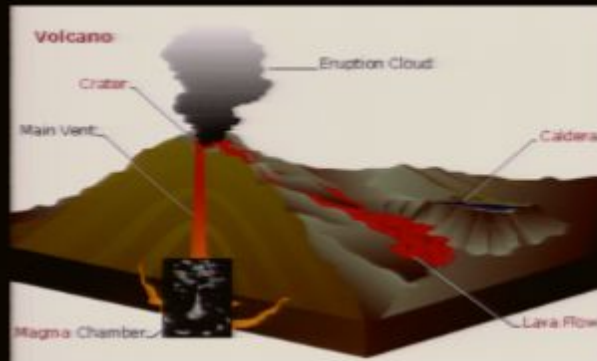
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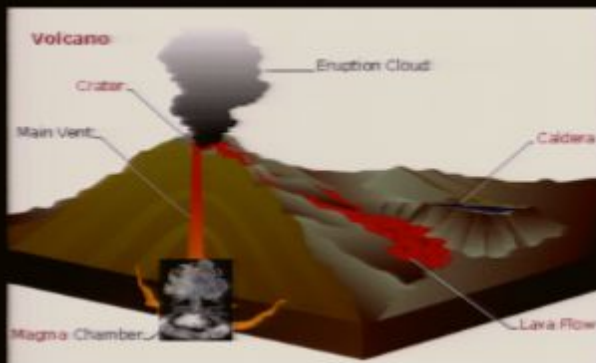
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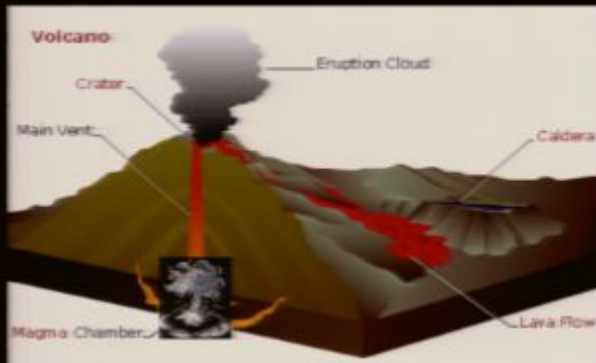
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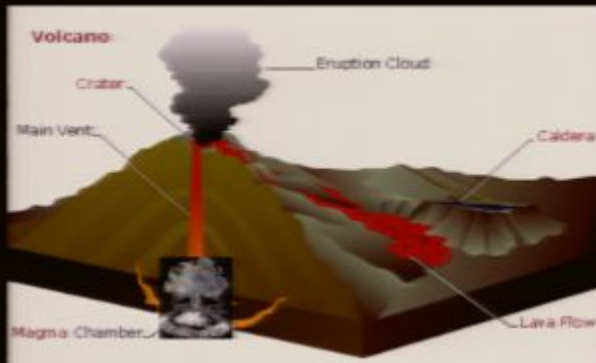
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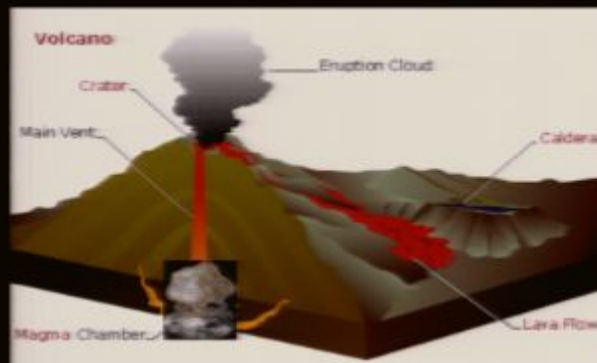
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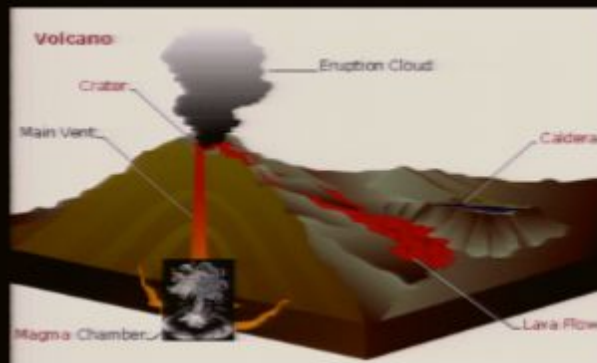
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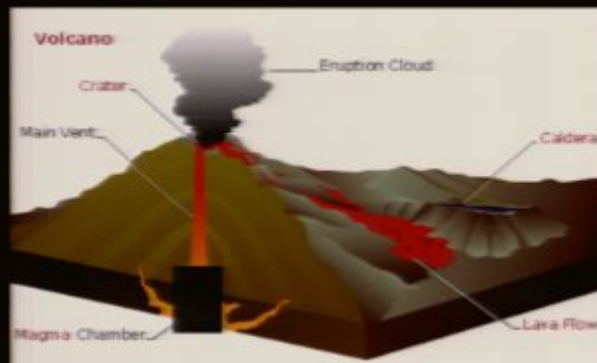
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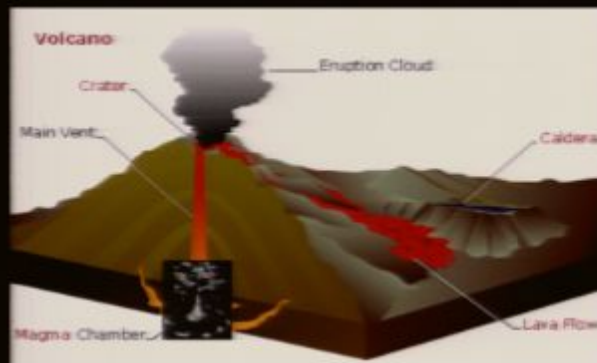
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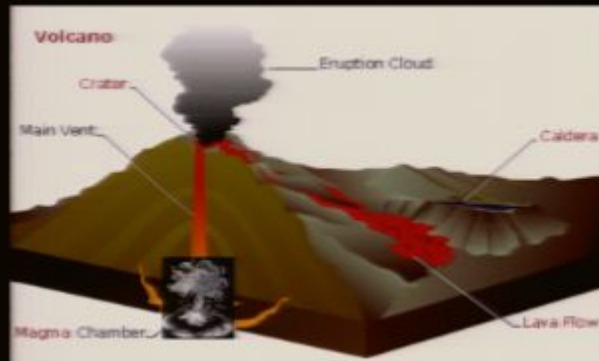
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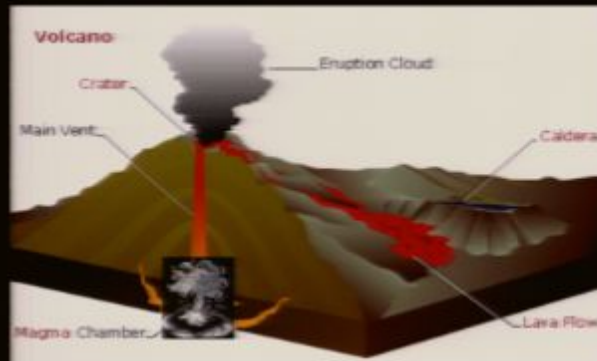
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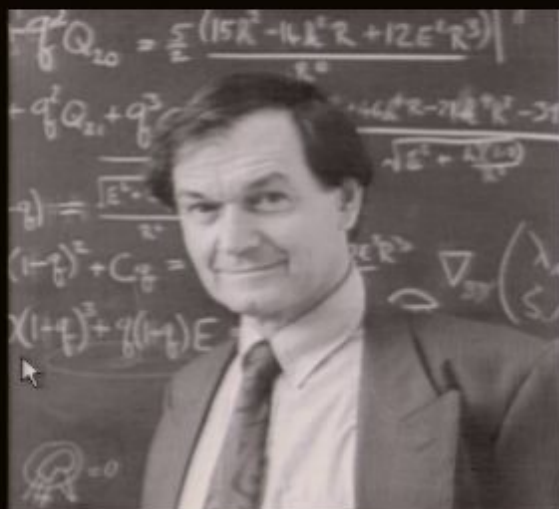


John Wheeler

- *With Bohr develops the theory of nuclear fission.*
- *Completes a catalog cold, dead stars firming up evidence of destiny of dead stars. (1957)*
- *Major battle with Oppenheimer about existence of black holes. (1957)*
- *Retracted argument and became the leading proponent of black hole. (1960)*
- *Coined the phrase "Black Hole" (1967).*
- *Coined the phrase "a Black Hole has no hair" (1968).*

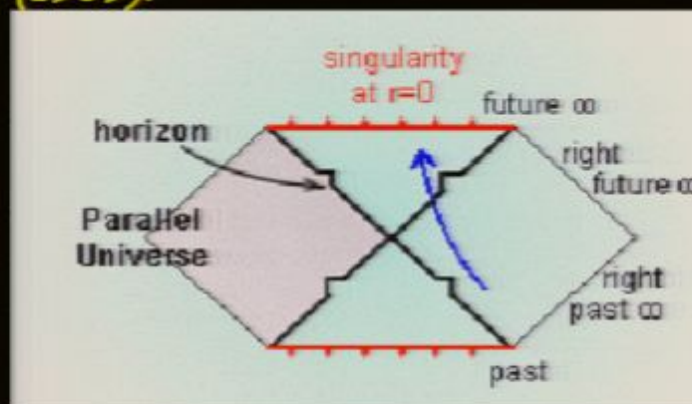


Roger Penrose



- Speculated black holes lose their hair by radiating it away.
- Discovered that spinning black holes store energy in space outside their horizon (1969).
- Discovered surface area of black holes must increase.
- Proved that black holes must have singularities at their core (1964).
- Proposed cosmic censorship conjecture (1969).

Topology



The Blackhole Stars Today



Hawking



Bekenstein



Thorne



Susskind



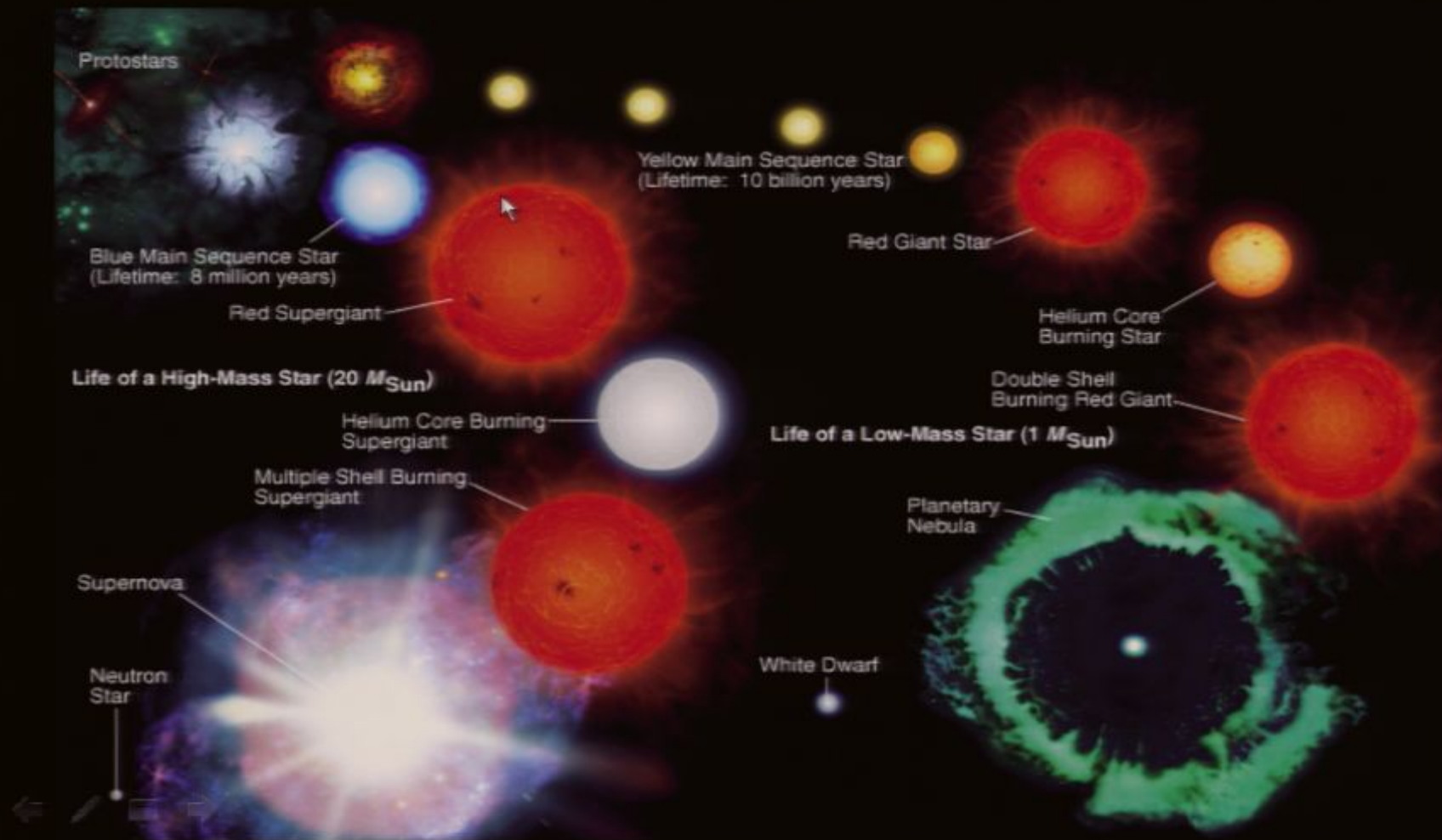
Werner Israel



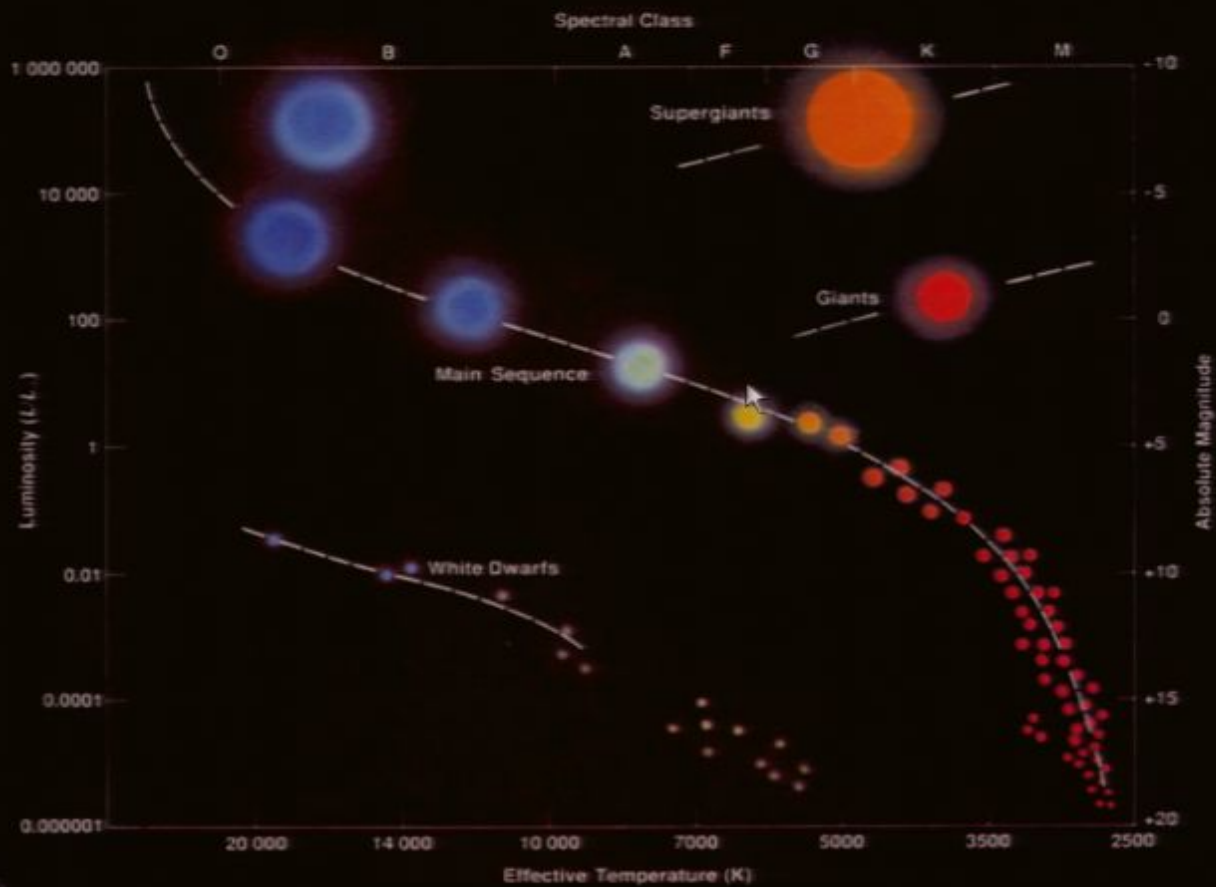
Robert Wald

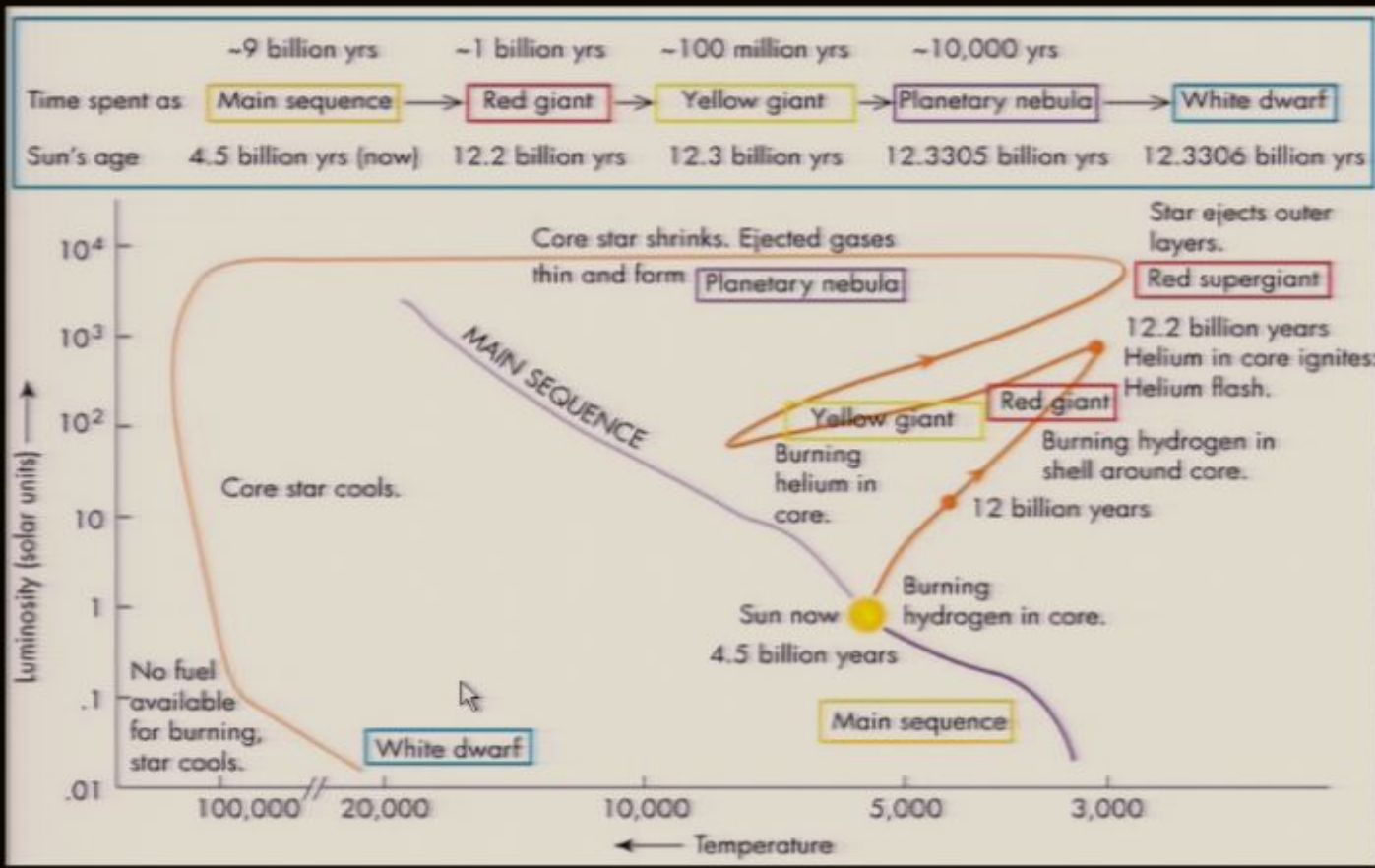


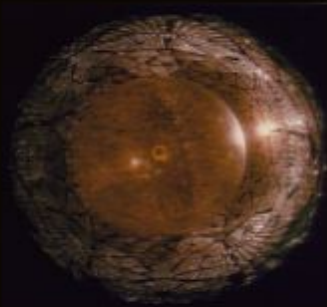
Life Cycle of Stars



Hertzsprung-Russel Diagram







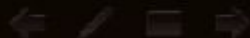
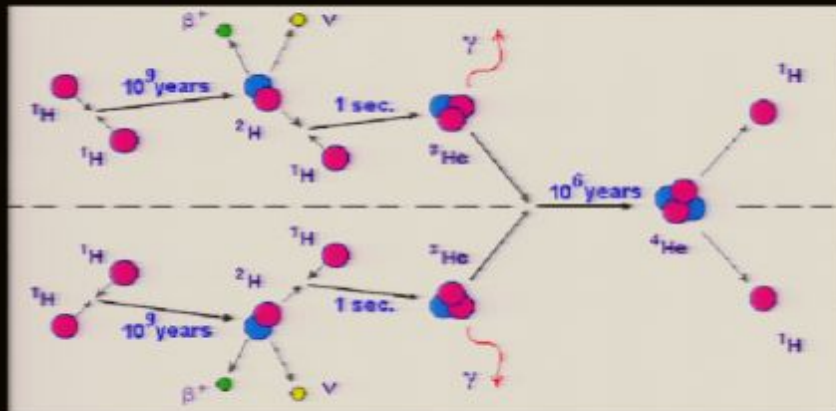
Stellar Energy

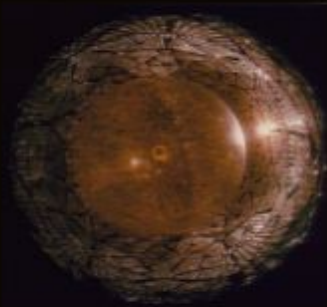
Proton-Proton Chain [4H → He + energy]

Two hydrogen nuclei merge to produce deuterium nucleus, a positron, and a neutrino. Add another hydrogen and you get helium 3 and a gamma photon (energy). Two Helium 3 merge and produce helium 4 and two Hydrogen nuclei.

Two 1H Atoms Combine

● = Neutron
● = Proton





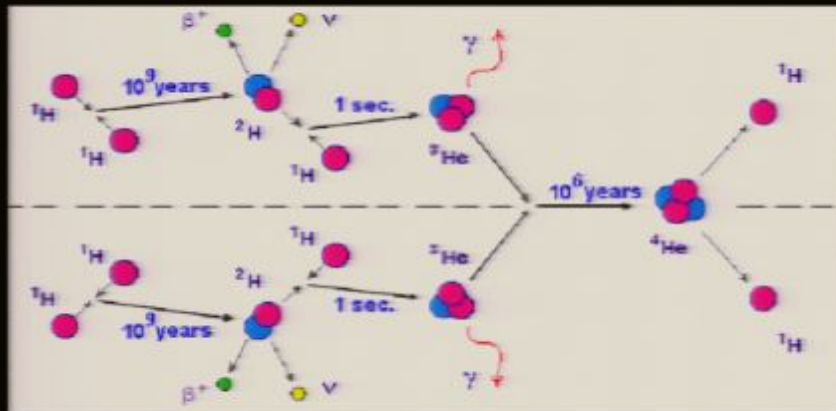
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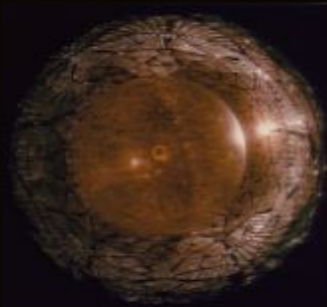
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2He Is Formed

● — Neutron
● — Proton



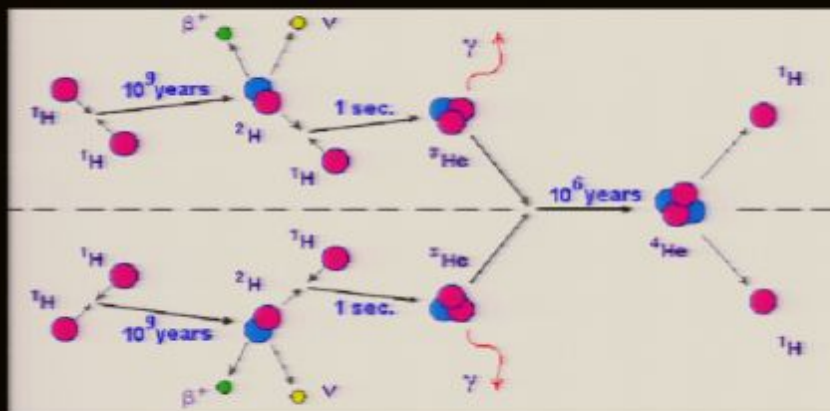
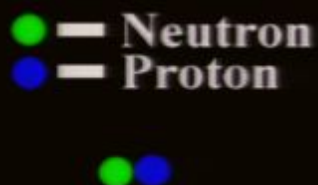


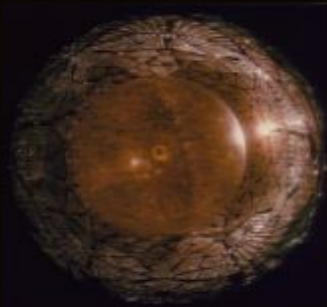
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Proton Decays Into A Neutron





Stellar Energy

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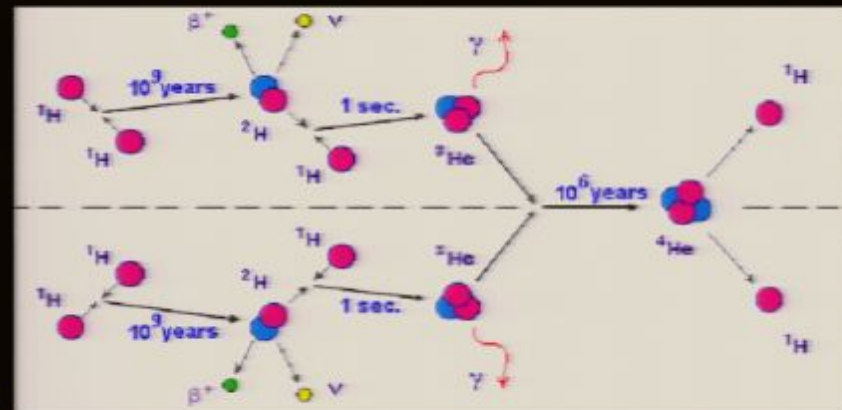
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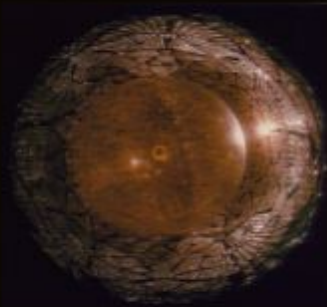
Stray 1H Fuses with 2H

● = Neutron
● = Proton

Positron — ●

Neutrino — ●





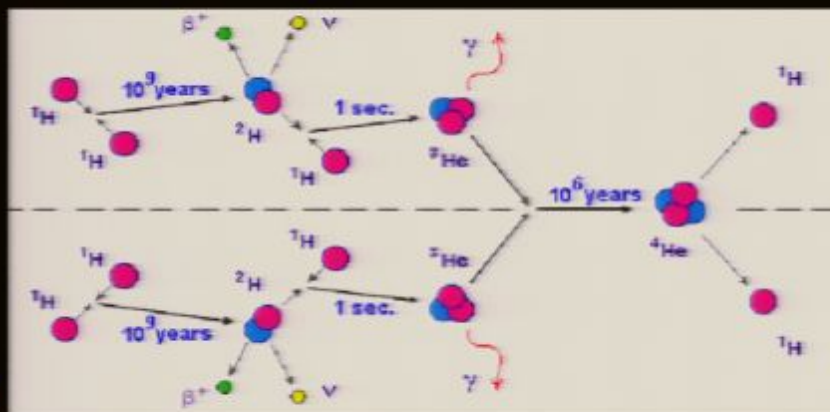
Stellar Energy

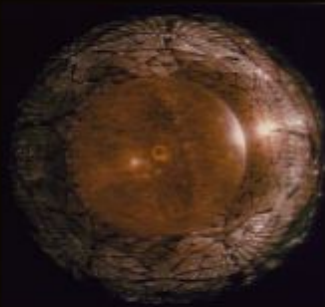
Proton-Proton Chain [4H → He + energy]

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3He Is Created

● = Neutron
● = Proton





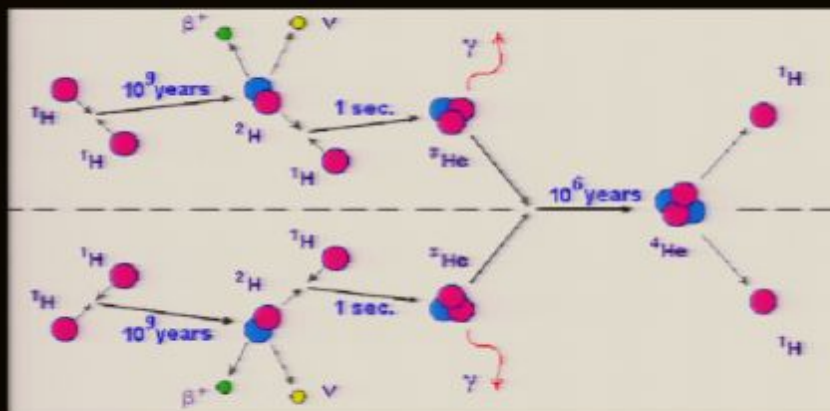
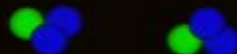
Stellar Energy

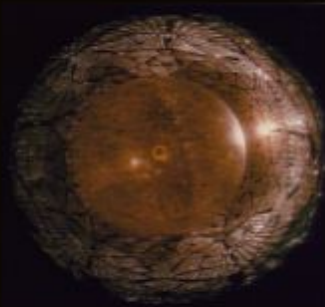
Proton-Proton Chain [4H → He + energy]

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Two 3He Fuse Together

● = Neutron
● = Proton





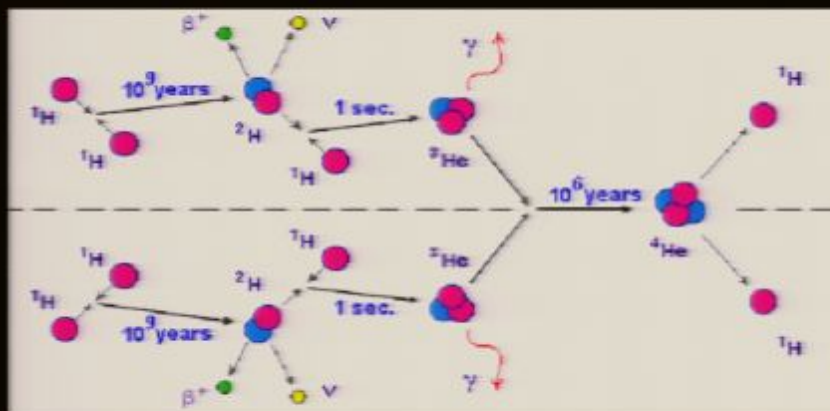
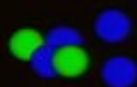
Stellar Energy

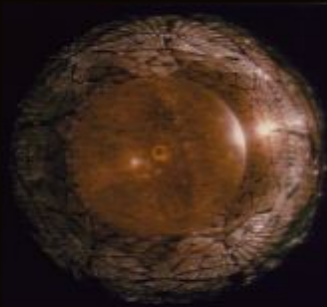
Proton-Proton Chain [4H → He + energy]

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Two 1H Atoms Released

● = Neutron
● = Proton





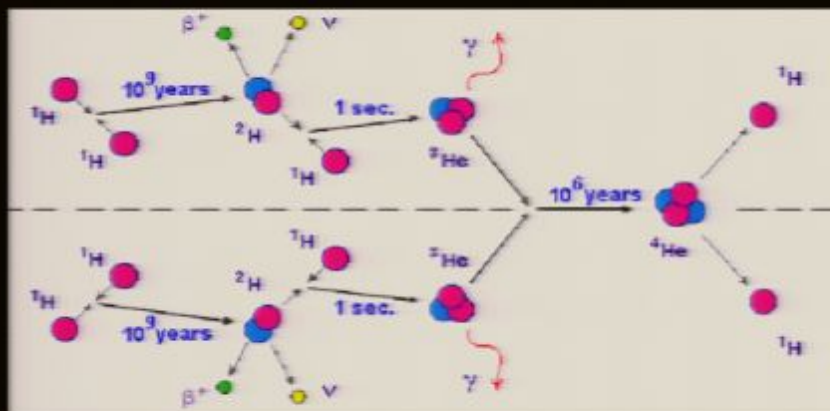
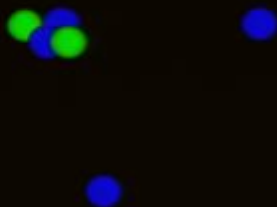
Stellar Energy

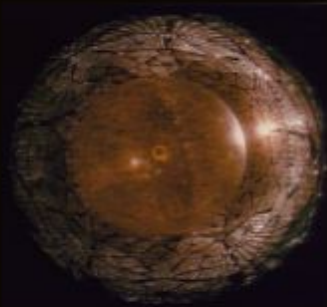
Proton-Proton Chain [4H → He + energy]

Two hydrogen nuclei merge to produce deuterium nucleus, a positron, and a neutrino. Add another hydrogen and you get helium 3 and a gamma photon (energy). Two Helium 3 merge and produce helium 4 and two Hydrogen nuclei.

4He Is Formed

● = Neutron
● = Proton



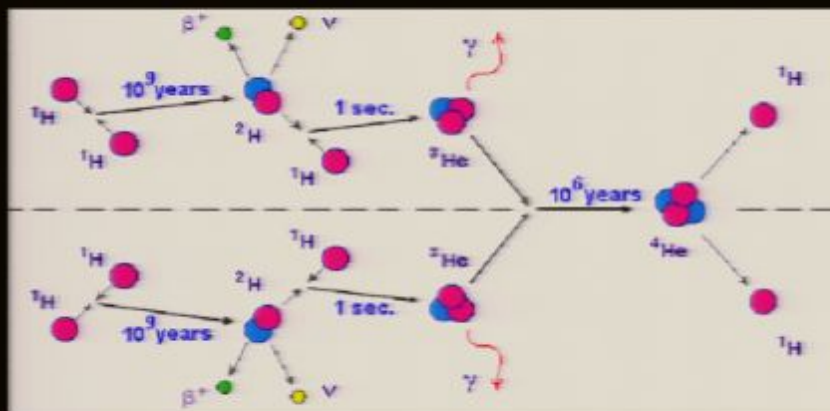
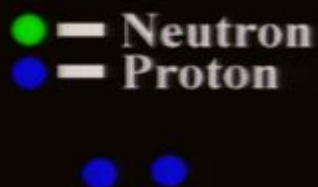


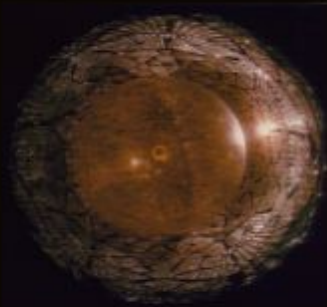
Stellar Energy

Proton-Proton Chain [4H → He + energy]

Two hydrogen nuclei merge to produce deuterium nucleus, a positron, and a neutrino. Add another hydrogen and you get helium 3 and a gamma photon (energy). Two Helium 3 merge and produce helium 4 and two Hydrogen nuclei.

Proton-Proton Reaction





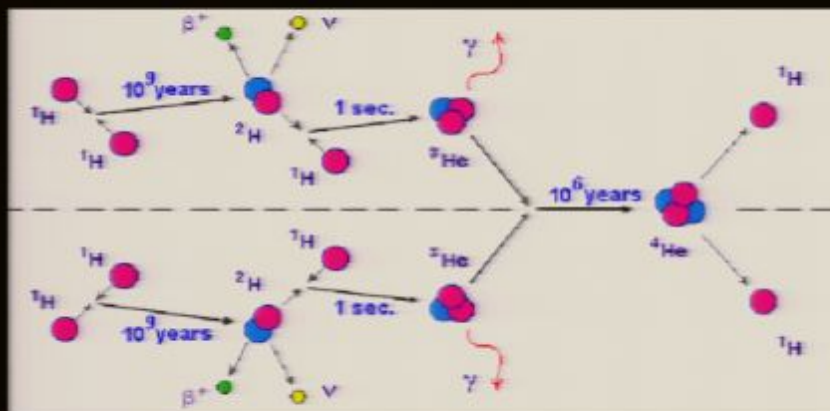
Stellar Energy

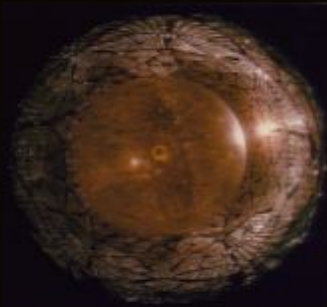
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Two 1H Atoms Combine

● = Neutron
● = Proton





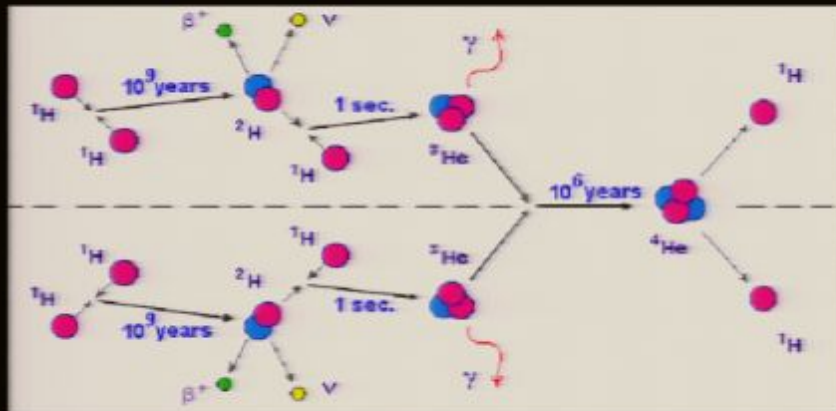
Stellar Energy

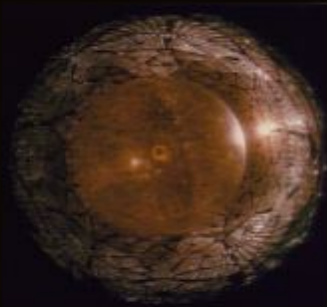
Proton-Proton Chain [4H → He + energy]

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2He Is Formed

● = Neutron
● = Proton



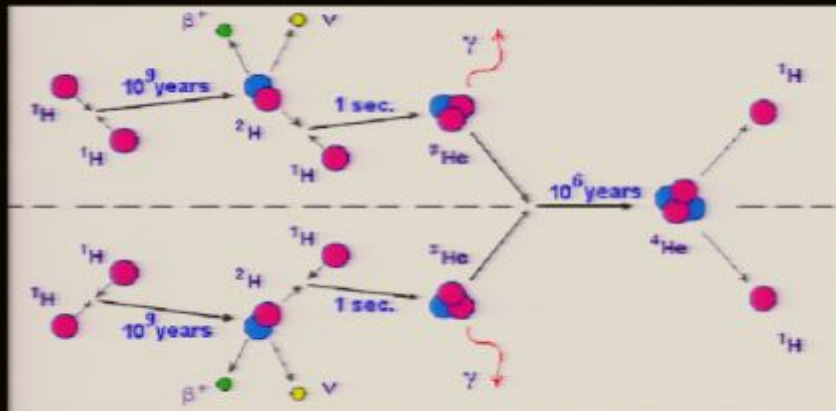


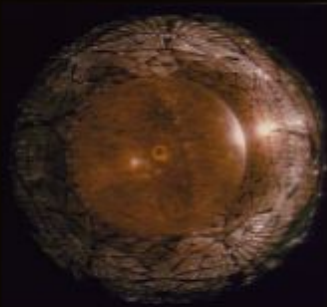
Stellar Energy

Proton-Proton Chain [4H → He + energy]

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Proton Decays Into A Neutron





Stellar Energy

Proton-Proton Chain [4H → He + energy]

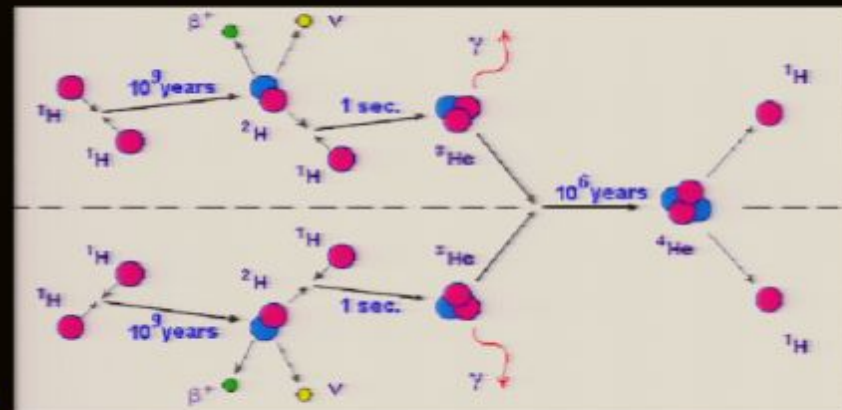
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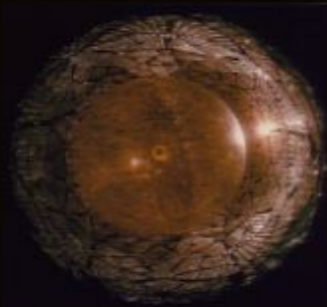
Stray 1H Fuses with 2H

● = Neutron
● = Proton

Positron —●

Neutrino —●





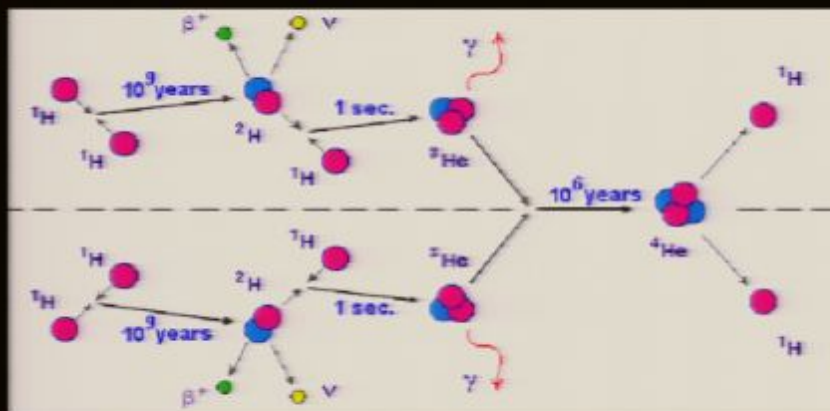
Stellar Energy

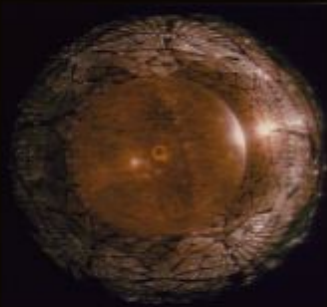
Proton-Proton Chain [4H → He + energy]

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3He Is Created

● = Neutron
● = Proton





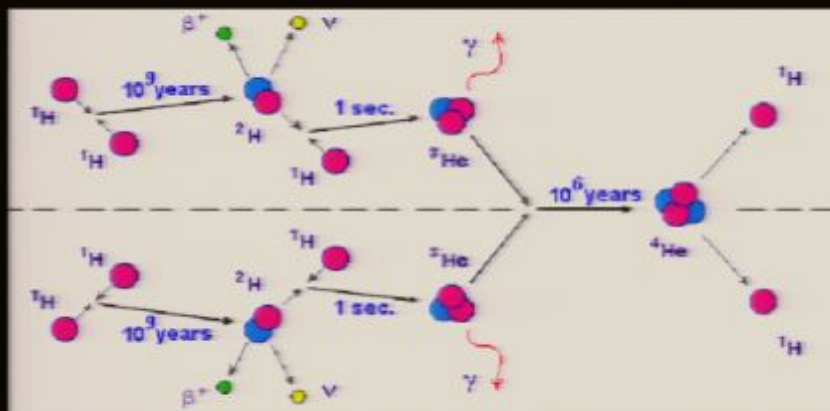
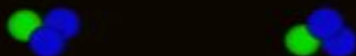
Stellar Energy

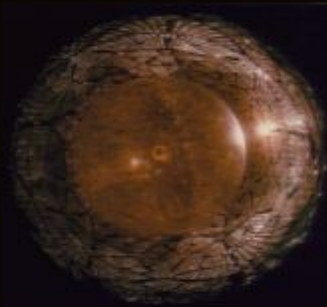
Proton-Proton Chain [4H → He + energy]

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Two 3He Fuse Together

● = Neutron
● = Proton





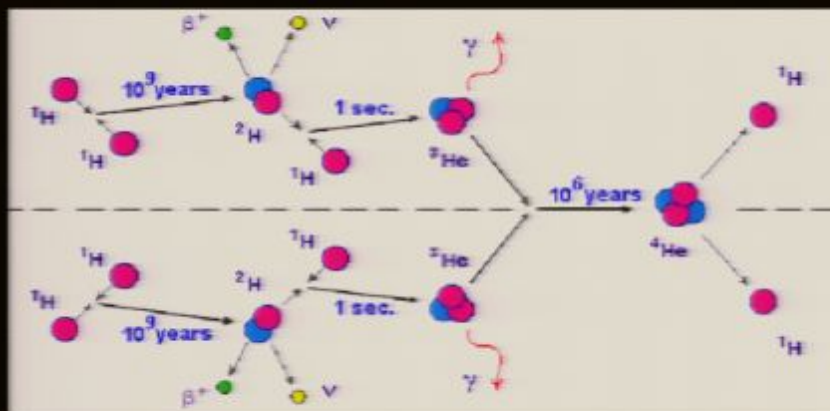
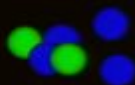
Stellar Energy

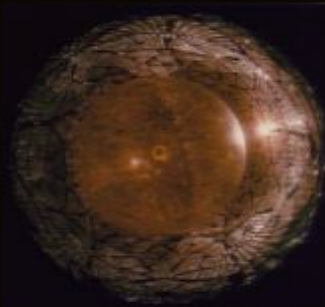
Proton-Proton Chain [4H → He + energy]

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Two 1H Atoms Released

● = Neutron
● = Proton





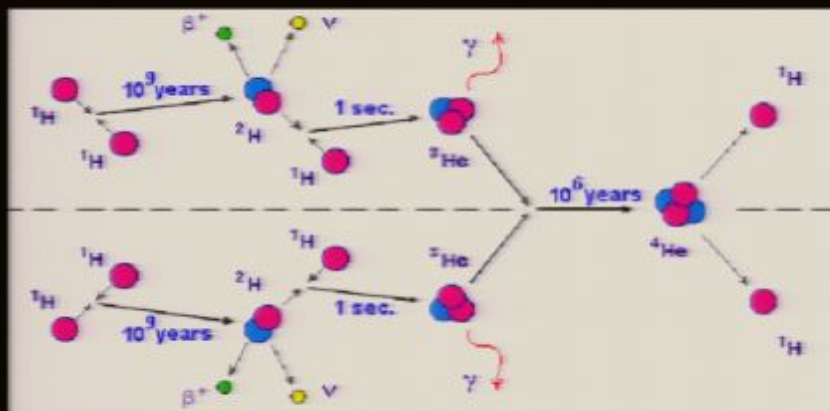
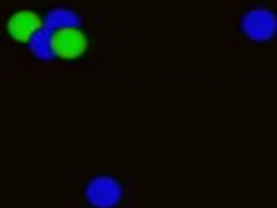
Stellar Energy

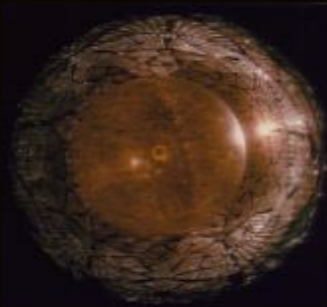
Proton-Proton Chain [4H → He + energy]

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4He Is Formed

● = Neutron
● = Proton



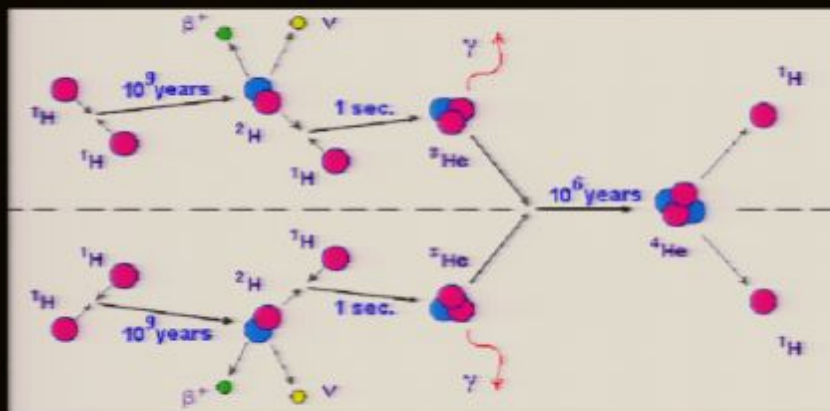
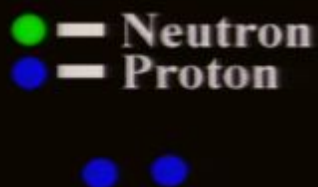


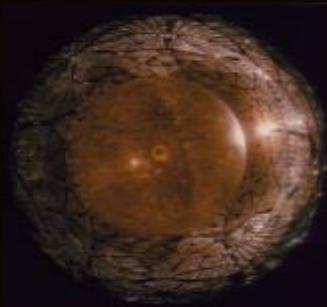
Stellar Energy

Proton-Proton Chain [4H → He + energy]

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Proton-Proton Reaction





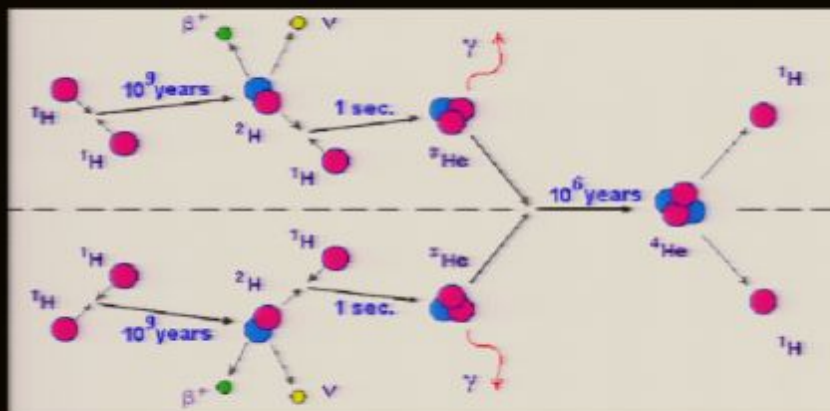
Stellar Energy

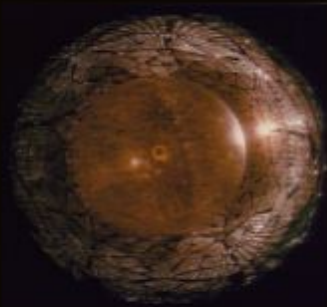
Proton-Proton Chain [4H → He + energy]

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Two 1H Atoms Combine

● = Neutron
● = Proton





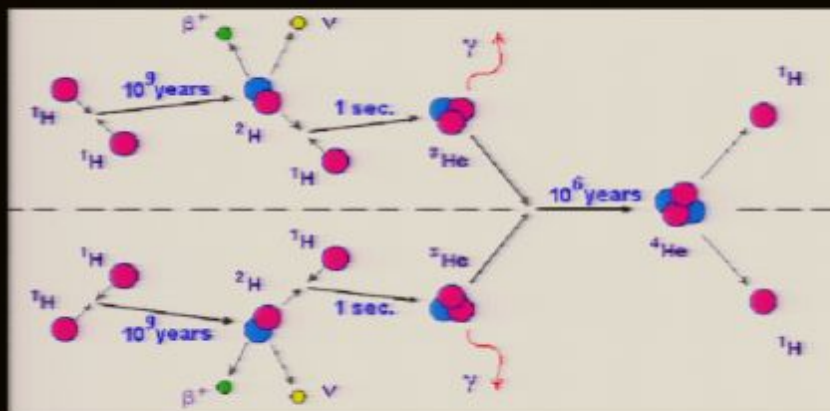
Stellar Energy

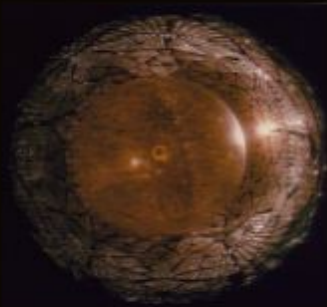
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2He Is Formed

● = Neutron
● = Proton



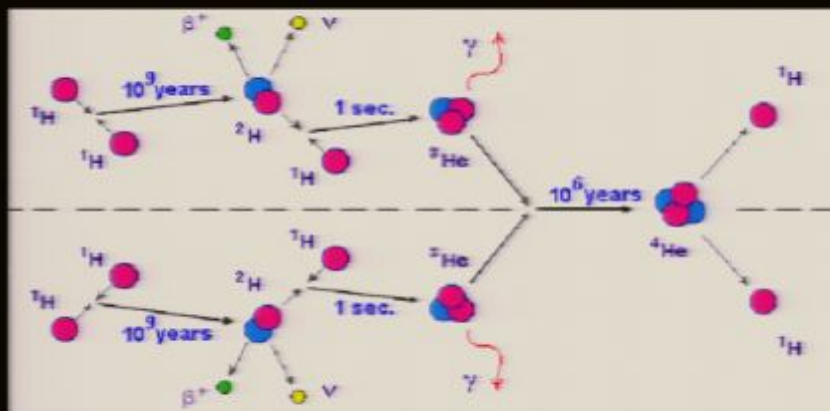
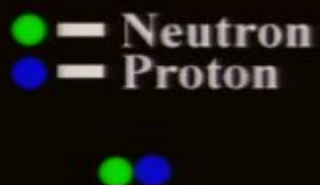


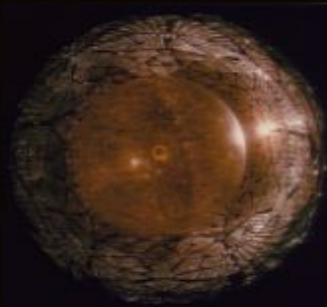
Stellar Energy

Proton-Proton Chain [4H → He + energy]

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Proton Decays Into A Neutron





Stellar Energy

Proton-Proton Chain [$4\text{H} \rightarrow \text{He} + \text{energy}$]

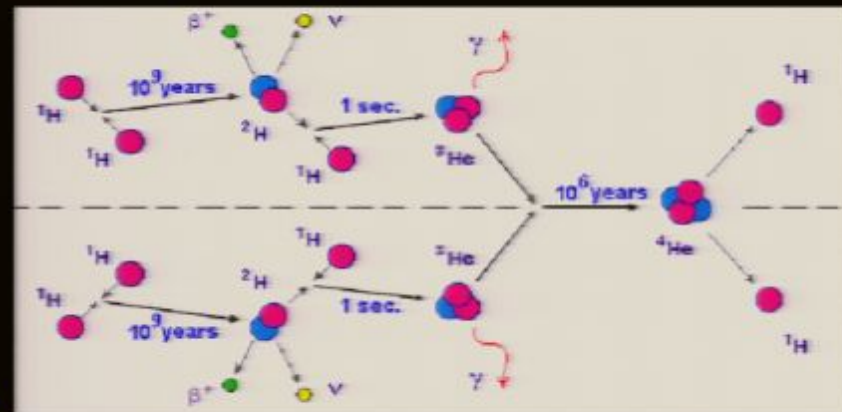
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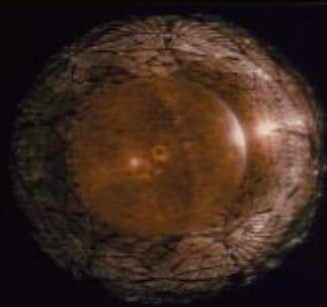
Stray 1H Fuses with 2H

● = Neutron
● = Proton

Positron — ● ●

Neutrino — ●





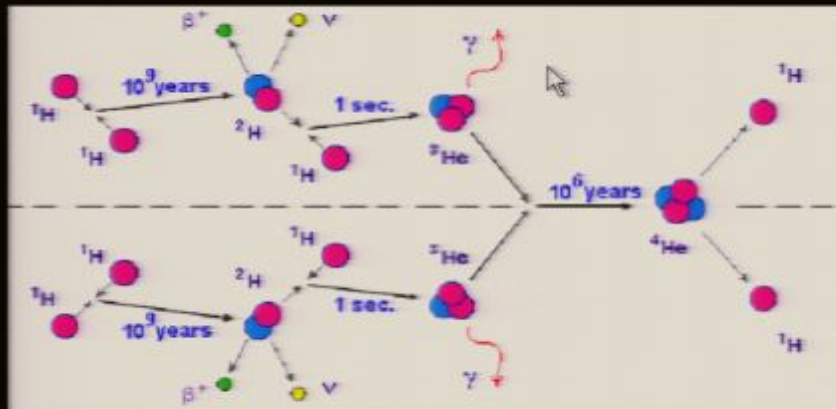
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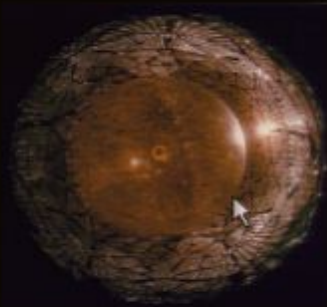
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3He Is Created

● = Neutron
● = Proton





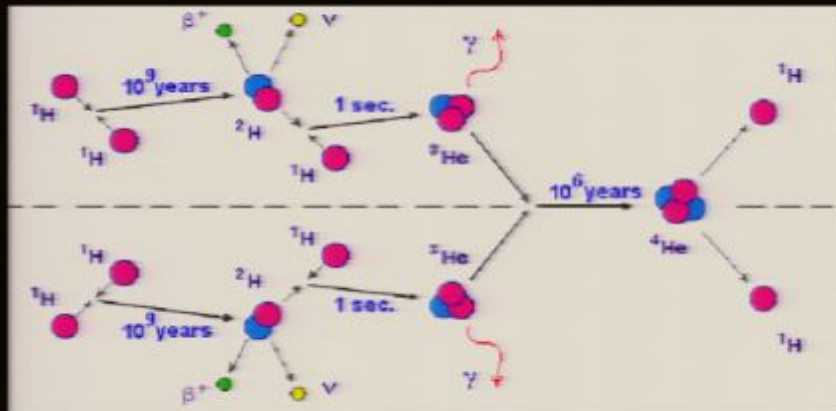
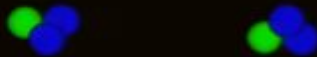
Stellar Energy

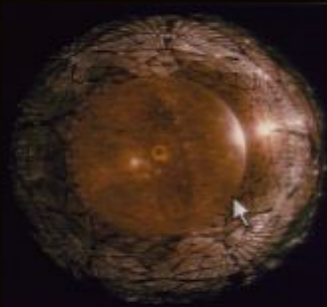
Proton-Proton Chain [4H → He + energy]

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Two 3He Fuse Together

● = Neutron
● = Proton





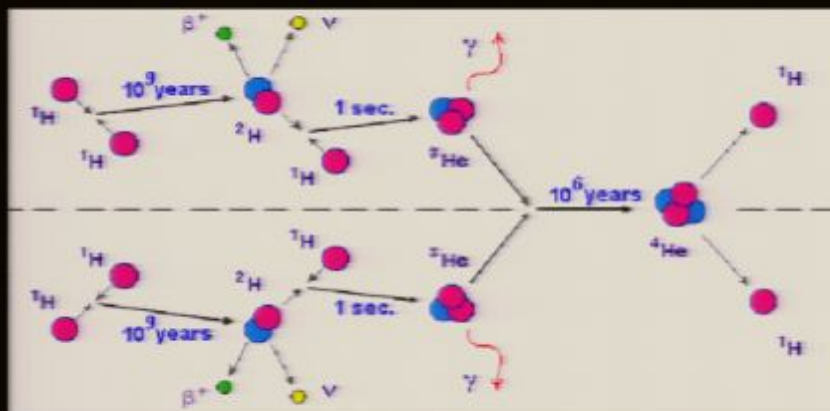
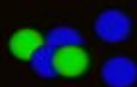
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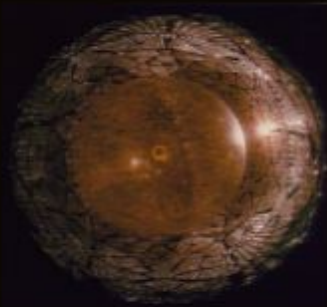
Proton-Proton Chain [4H → He + energy]

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Two 1H Atoms Released

● = Neutron
● = Proton





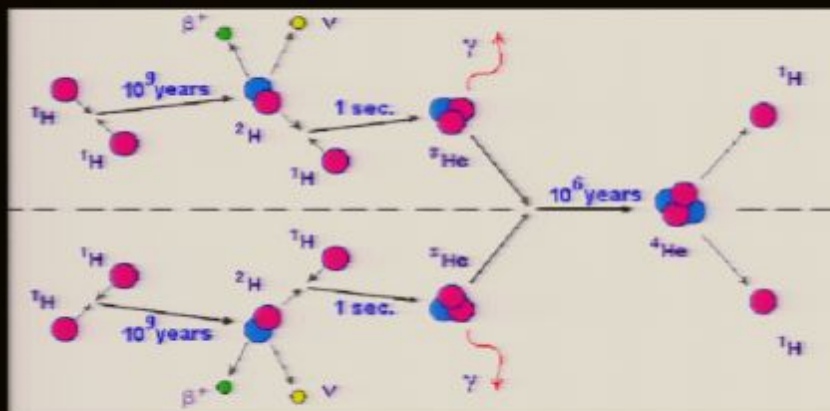
Stellar Energy

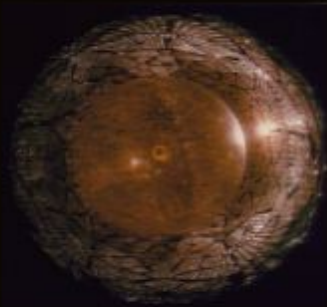
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4He Is Formed

● = Neutron
● = Proton



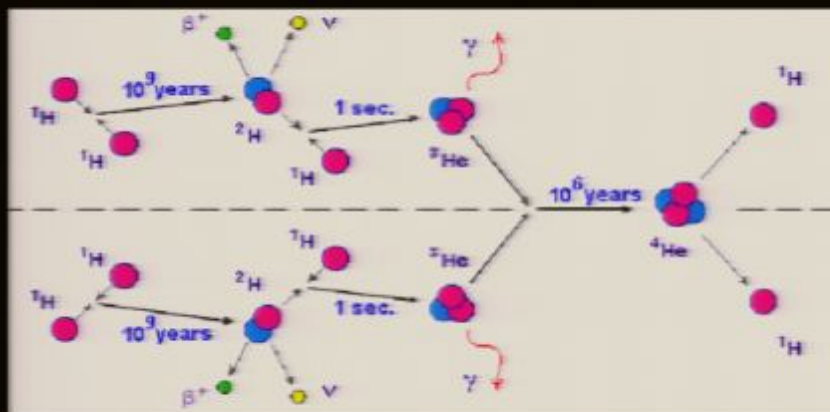
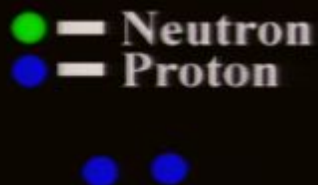


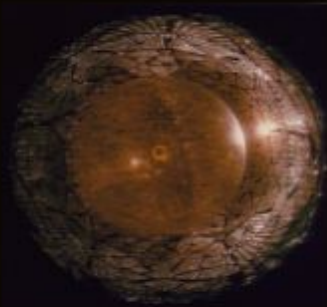
Stellar Energy

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Proton-Proton Reaction





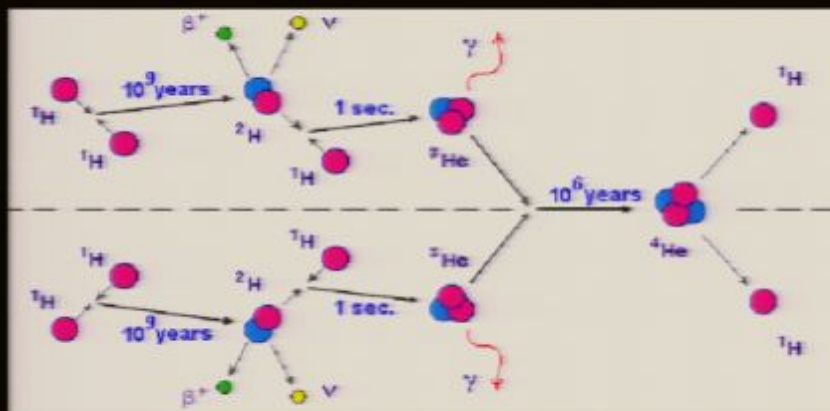
Stellar Energy

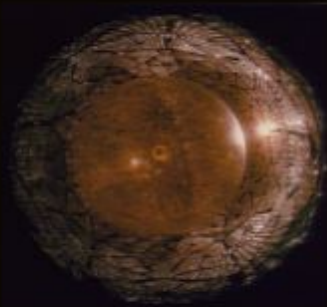
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Two 1H Atoms Combine

● = Neutron
● = Proton





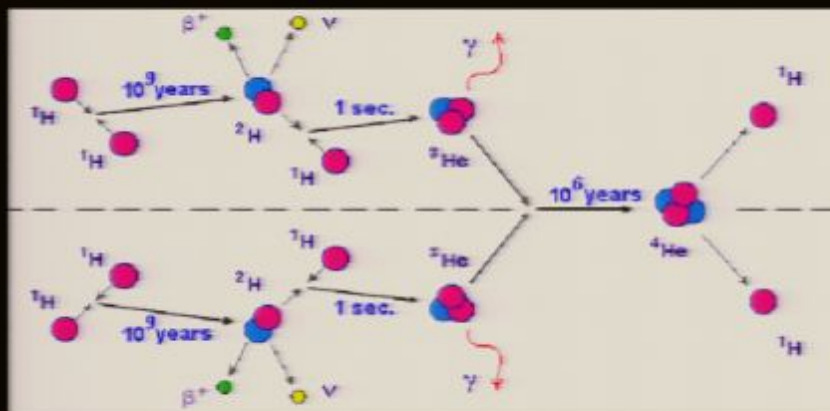
Stellar Energy

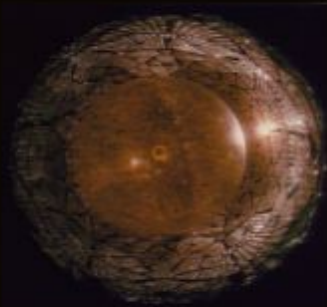
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2He Is Formed

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● = Proton



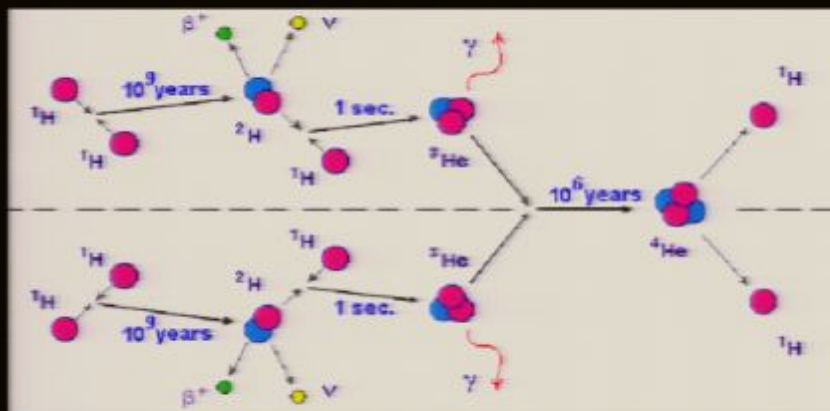
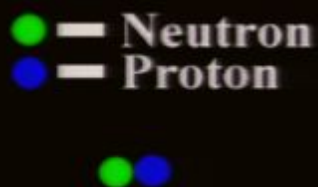


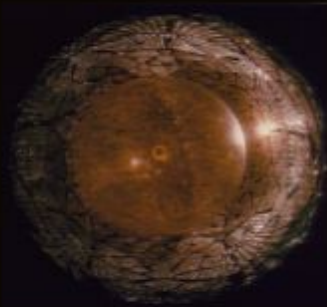
Stellar Energy

Proton-Proton Chain [4H → He + energy]

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Proton Decays Into A Neutron



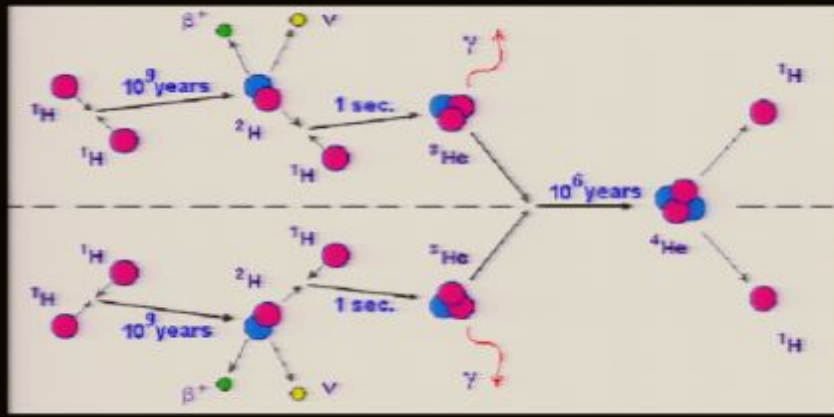
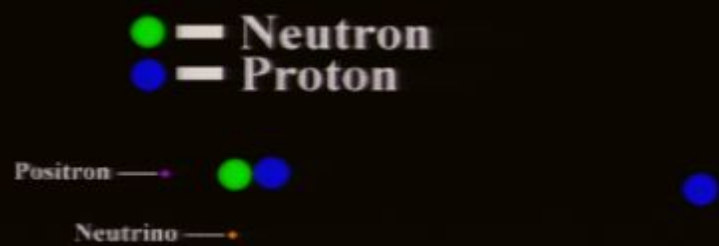


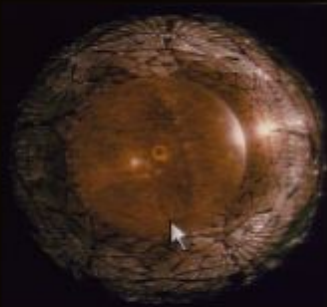
Stellar Energy

Proton-Proton Chain [4H → He + energy]

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Stray 1H Fuses with 2H





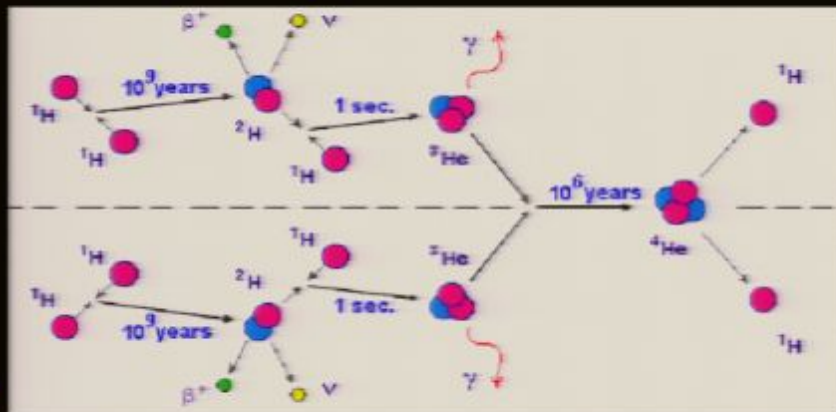
Stellar Energy

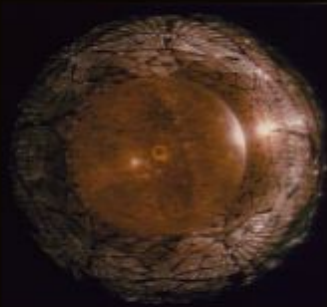
Proton-Proton Chain [4H → He + energy]

Two hydrogen nuclei merge to produce deuterium nucleus, a positron, and a neutrino. Add another hydrogen and you get helium 3 and a gamma photon (energy). Two Helium 3 merge and produce helium 4 and two Hydrogen nuclei.

3He Is Created

● = Neutron
● = Proton





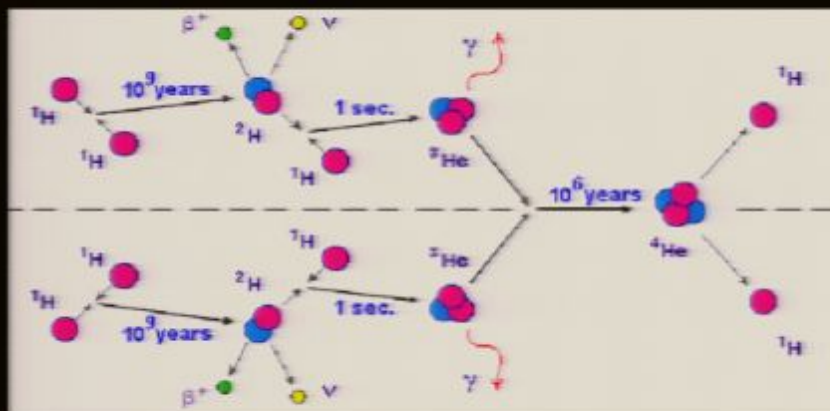
Stellar Energy

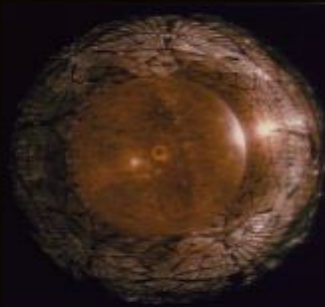
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Two 3He Fuse Together

● = Neutron
● = Proton





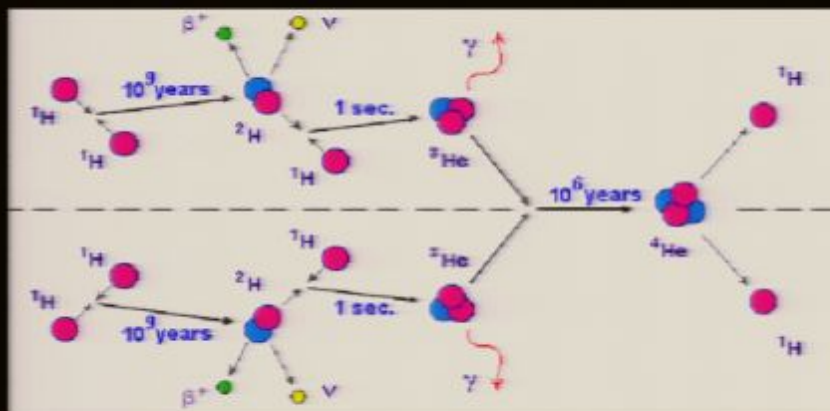
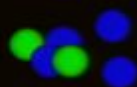
Stellar Energy

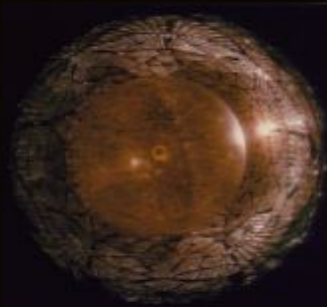
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Two 1H Atoms Released

● = Neutron
● = Proton





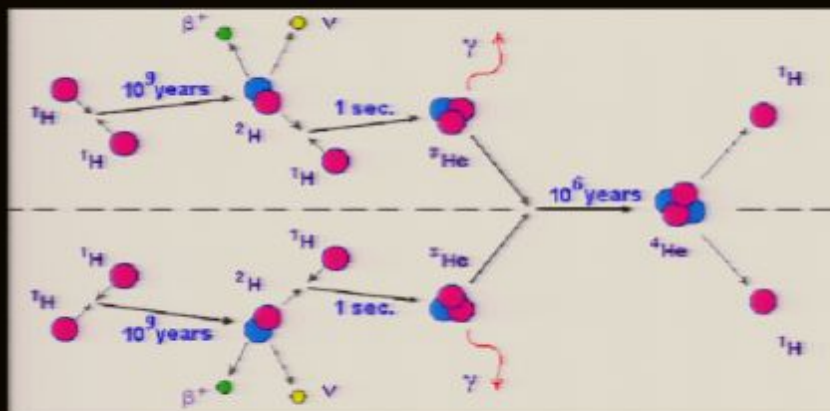
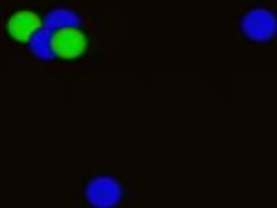
Stellar Energy

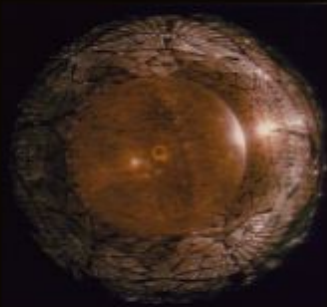
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4He Is Formed

● = Neutron
● = Proton



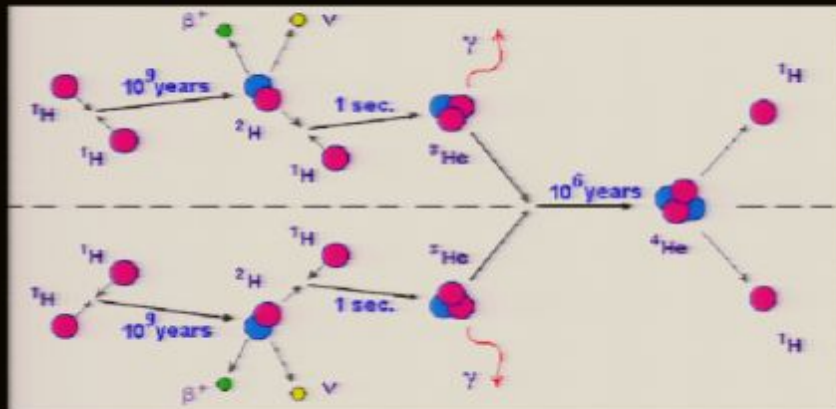
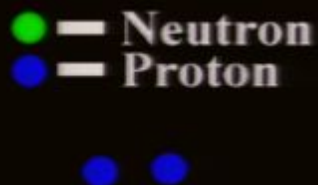


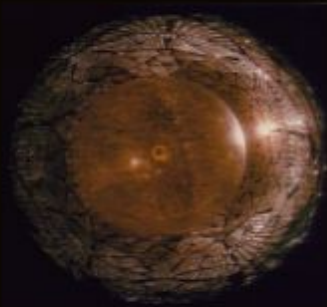
Stellar Energy

Proton-Proton Chain [4H → He + energy]

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Proton-Proton Reaction





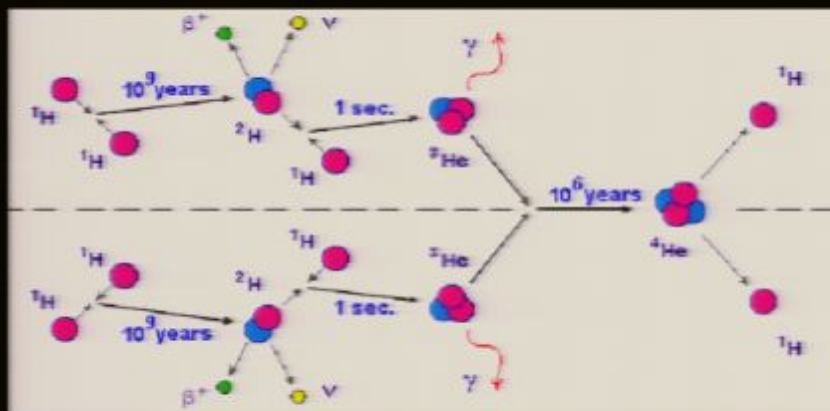
Stellar Energy

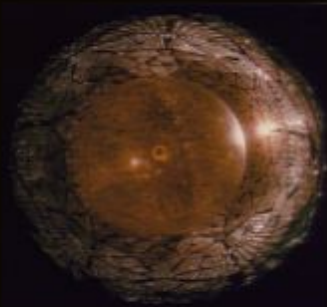
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Two 1H Atoms Combine

● = Neutron
● = Proton





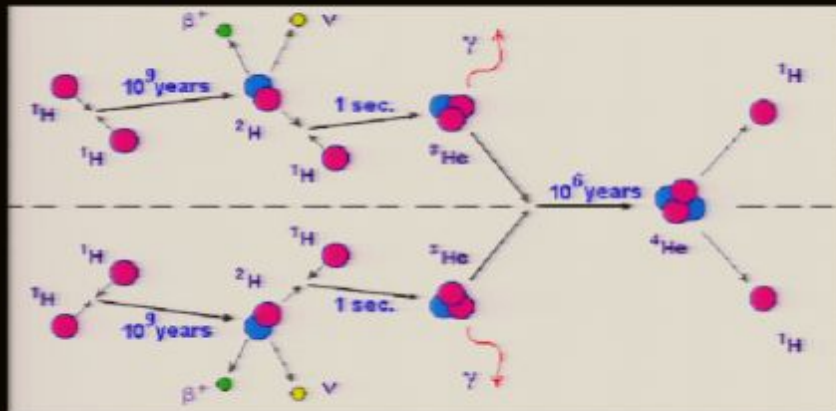
Stellar Energy

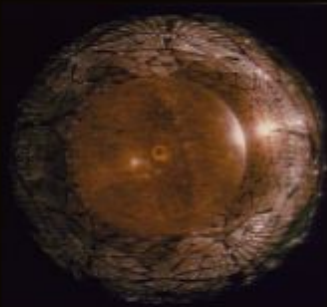
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2He Is Formed

● = Neutron
● = Proton



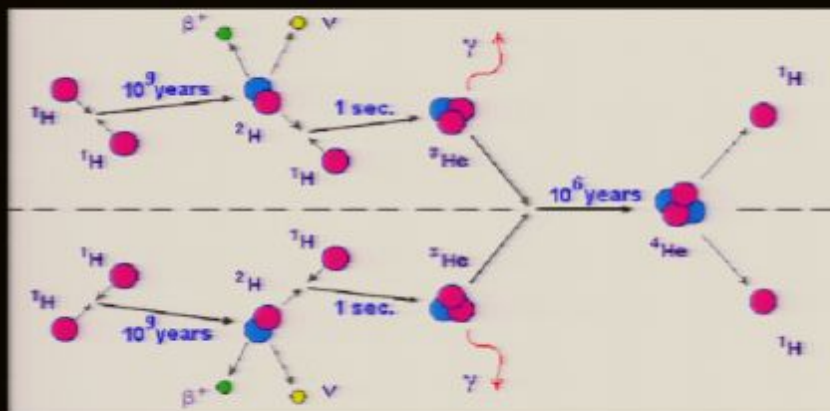


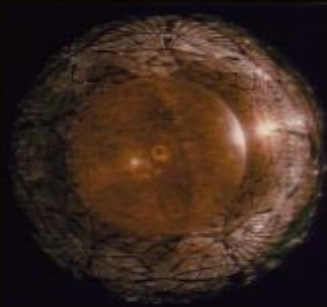
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Proton Decays Into A Neutron





Stellar Energy

Proton-Proton Chain [4H → He + energy]

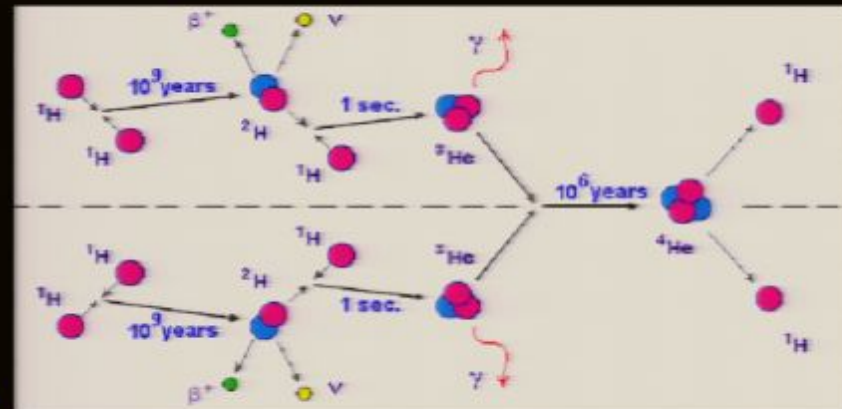
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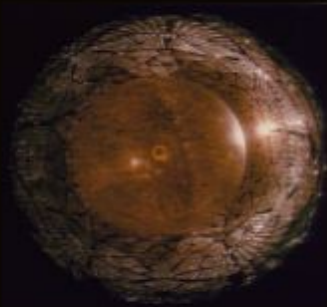
Stray 1H Fuses with 2H

● = Neutron
● = Proton

Positron — ●

Neutrino — ●





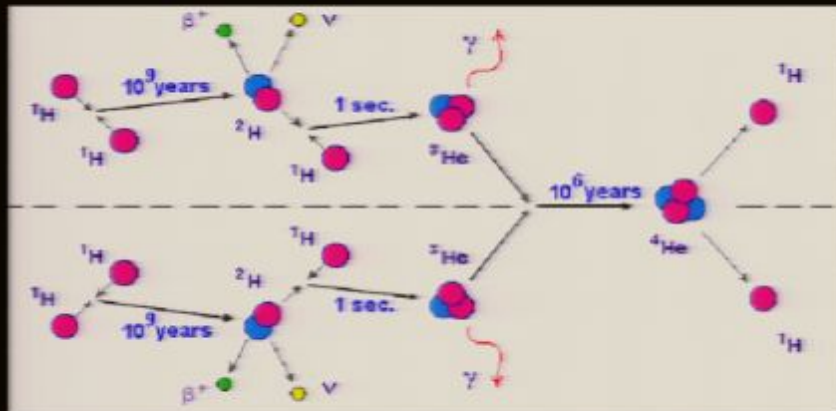
Stellar Energy

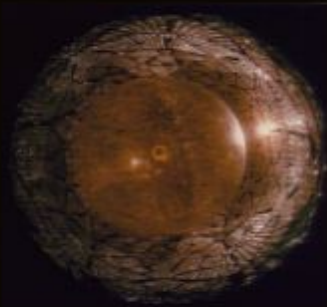
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3He Is Created

● = Neutron
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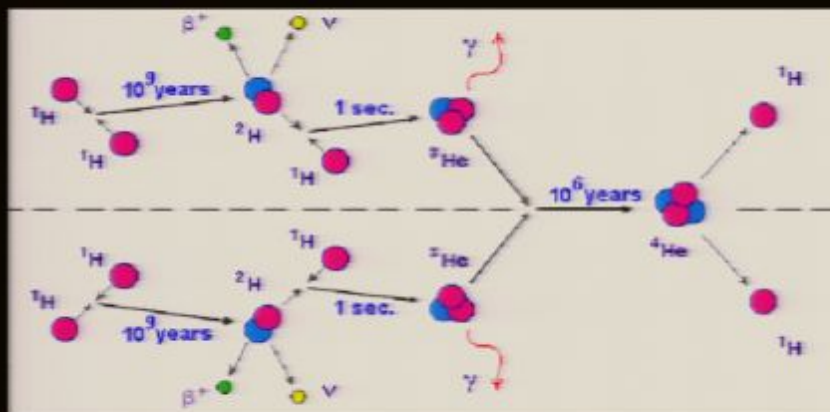
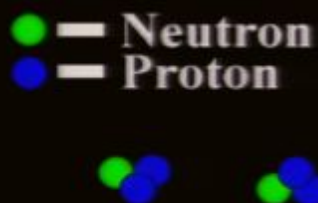


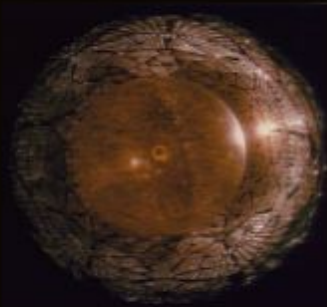
Stellar Energy

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Two 3He Fuse Together





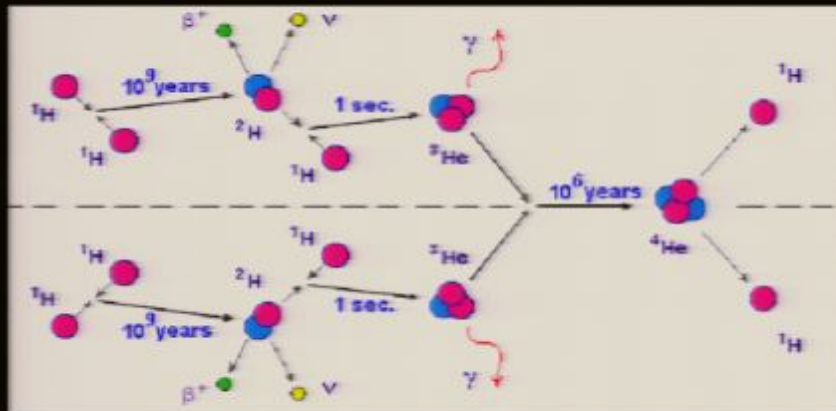
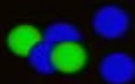
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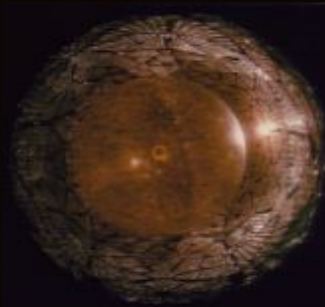
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Two 1H Atoms Released

● = Neutron
● = Proton





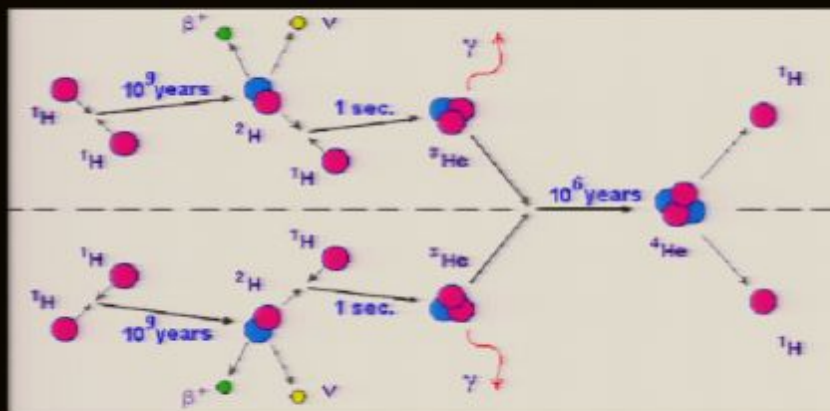
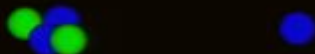
Stellar Energy

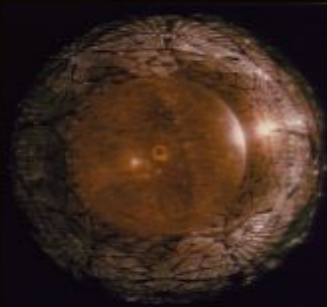
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4He Is Formed

● = Neutron
● = Proton



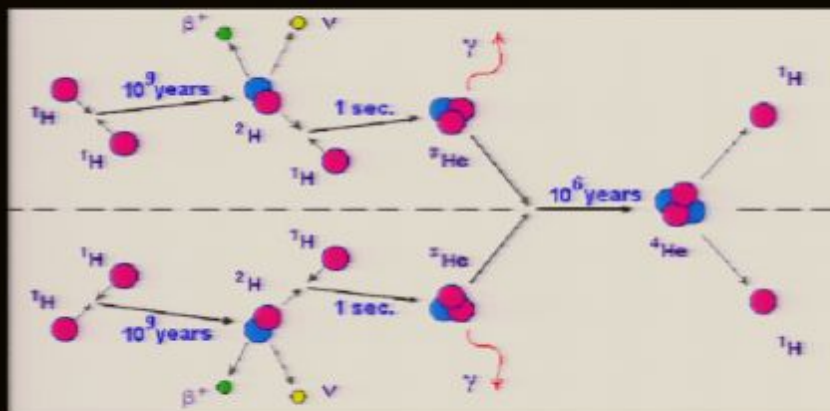
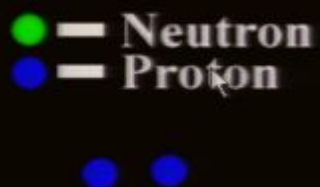


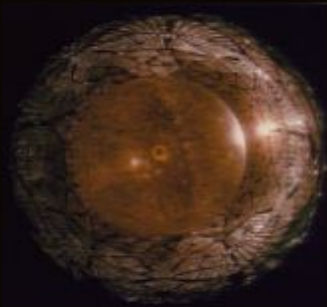
Stellar Energy

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Proton-Proton Reaction





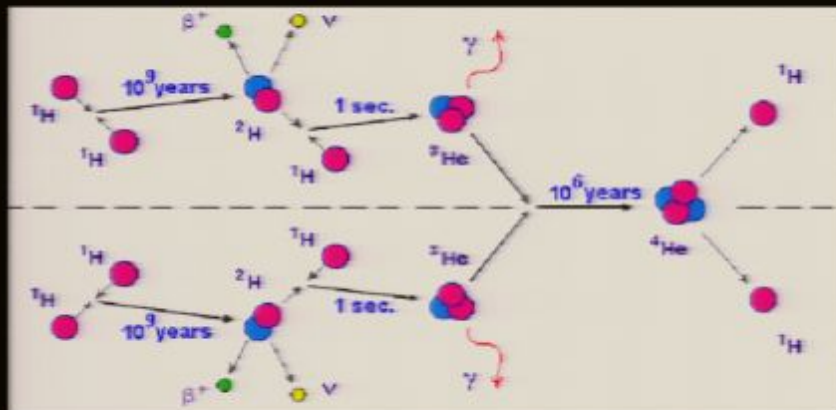
Stellar Energy

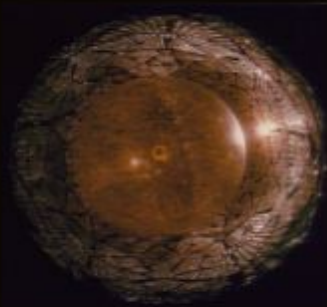
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Two 1H Atoms Combine

● = Neutron
● = Proton





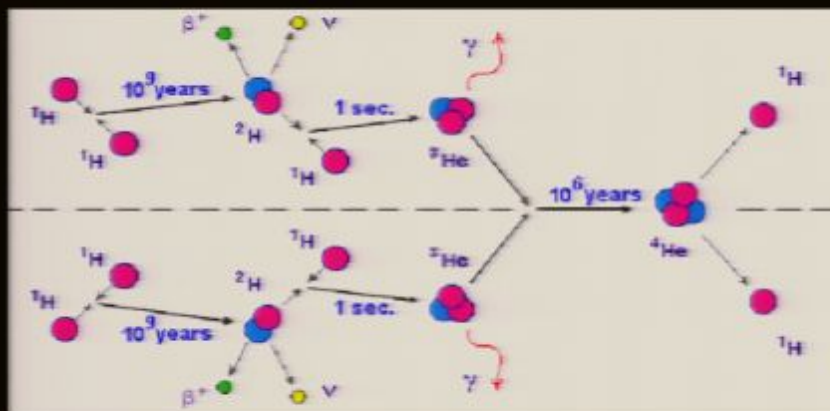
Stellar Energy

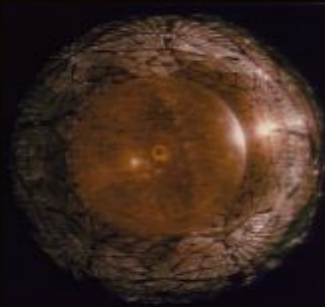
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2He Is Formed

● = Neutron
● = Proton



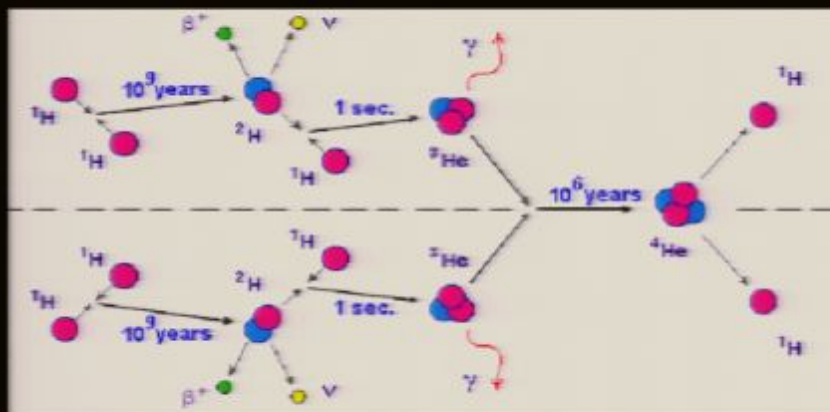
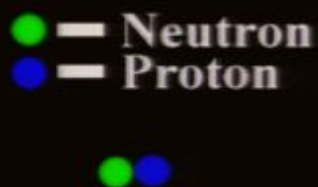


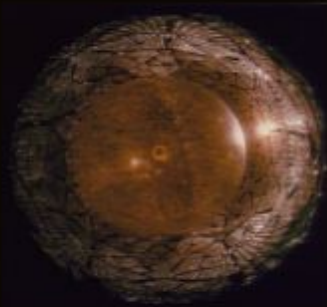
Stellar Energy

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Proton Decays Into A Neutron





Stellar Energy

Proton-Proton Chain [4H → He + energy]

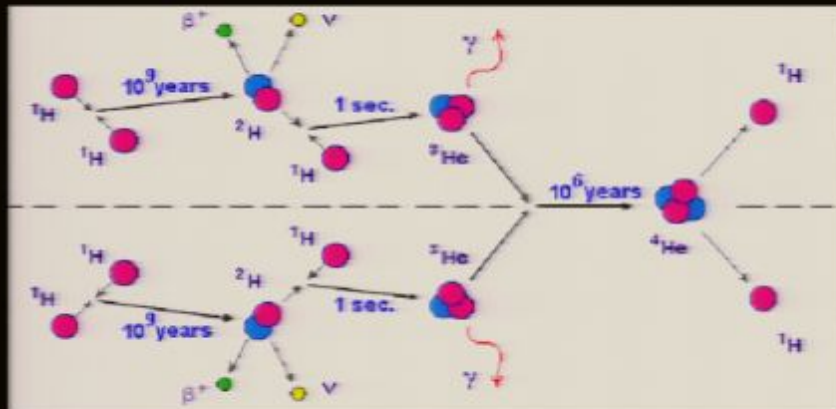
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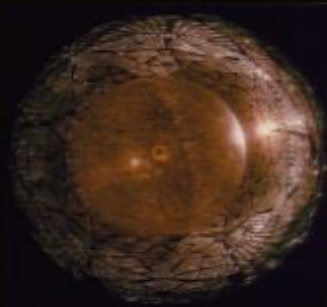
Stray 1H Fuses with 2H

● = Neutron
● = Proton

Positron — ●

Neutrino — ●





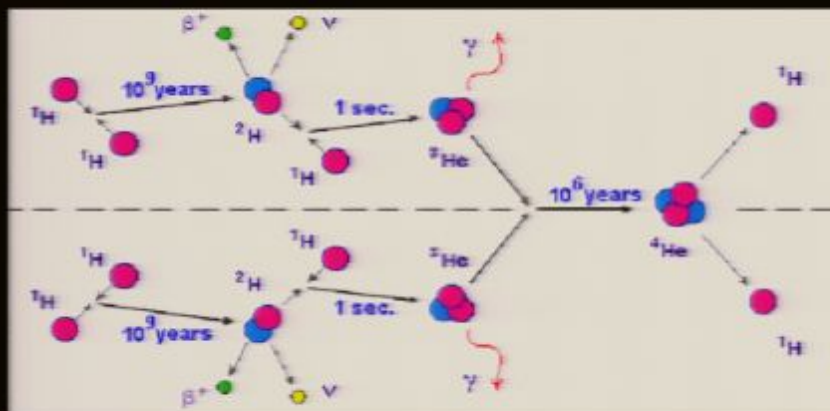
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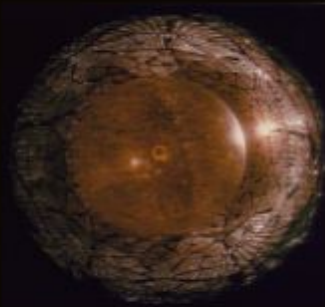
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3He Is Created

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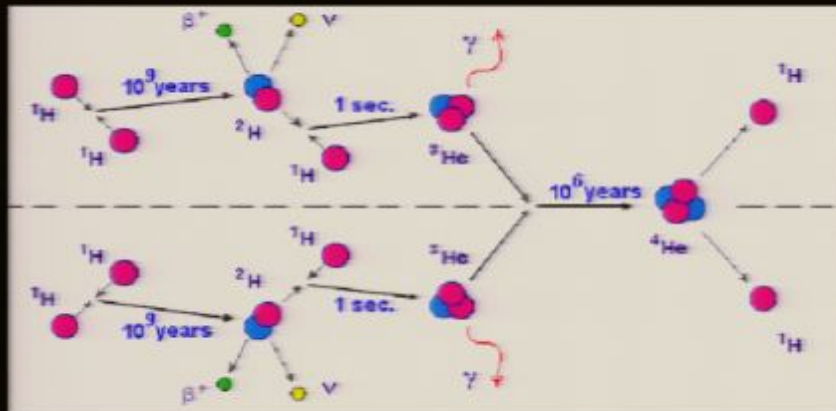
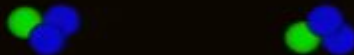
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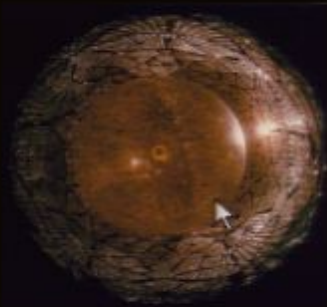
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Two 3He Fuse Together

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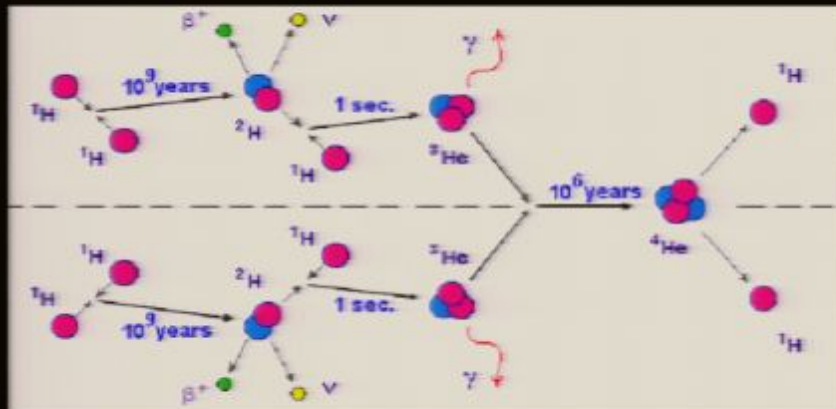
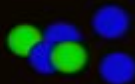
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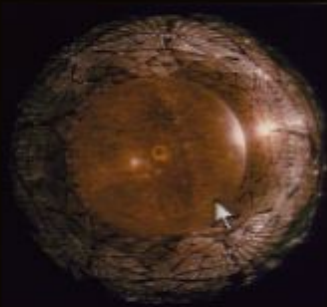
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Two 1H Atoms Released

● = Neutron
● = Proton





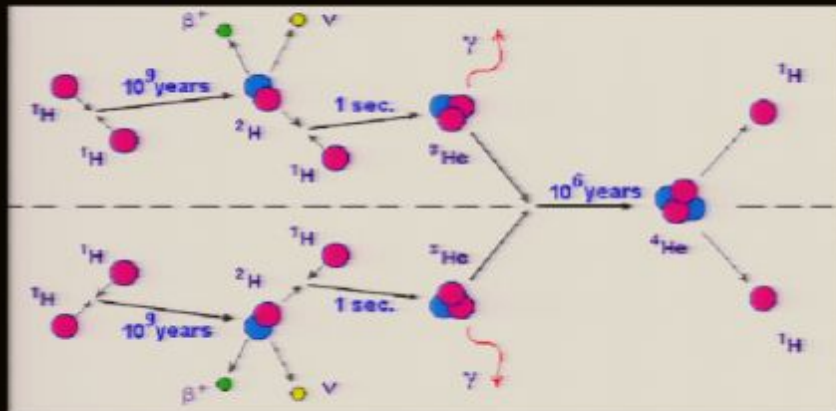
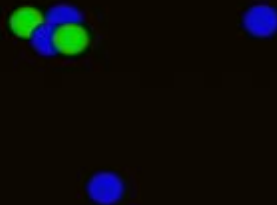
Stellar Energy

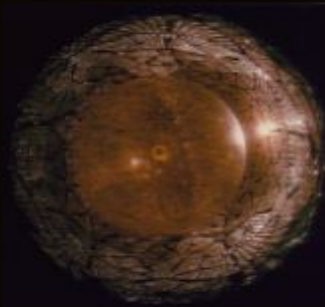
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4He Is Formed

● = Neutron
● = Proton



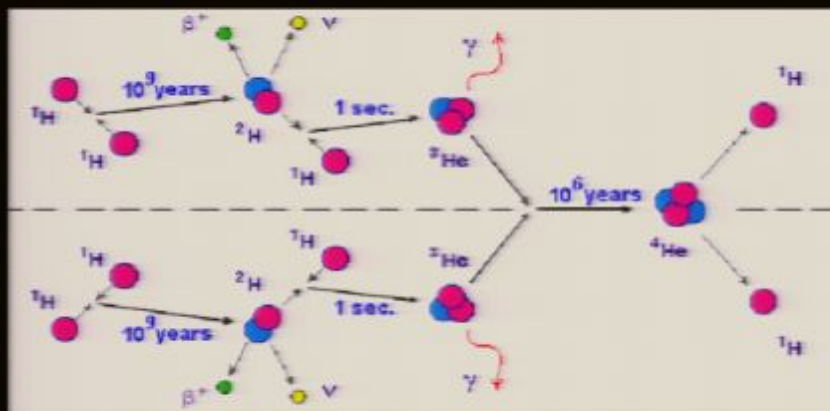
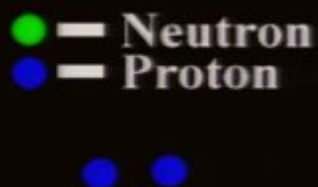


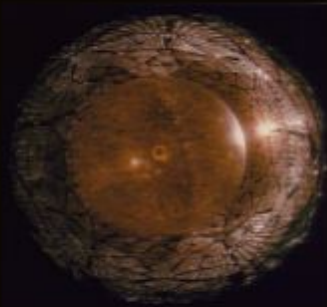
Stellar Energy

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Proton-Proton Reaction





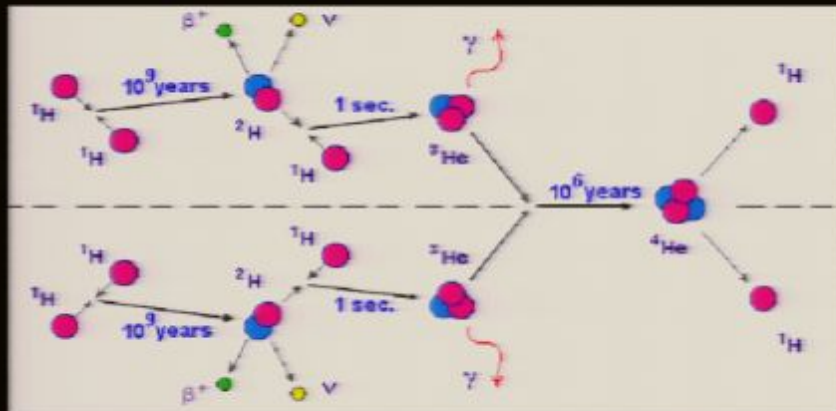
Stellar Energy

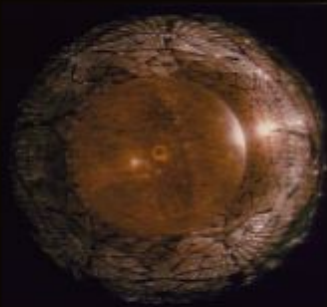
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Two 1H Atoms Combine

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● = Proton





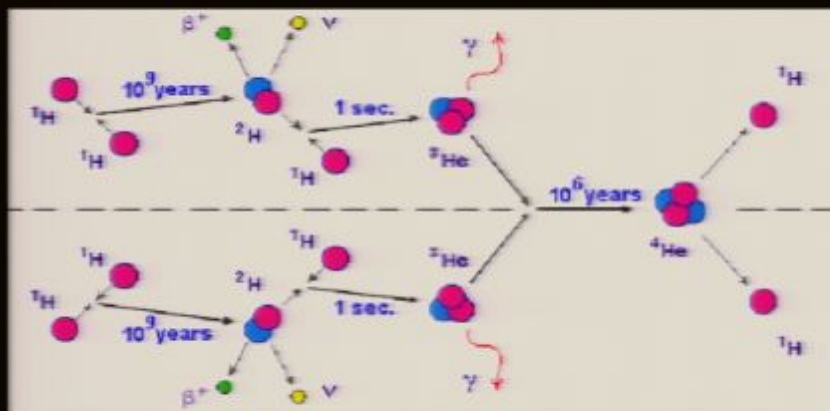
Stellar Energy

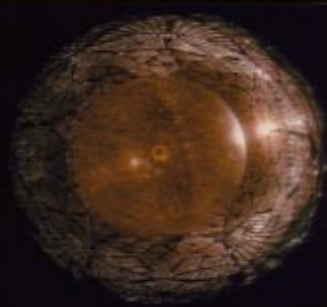
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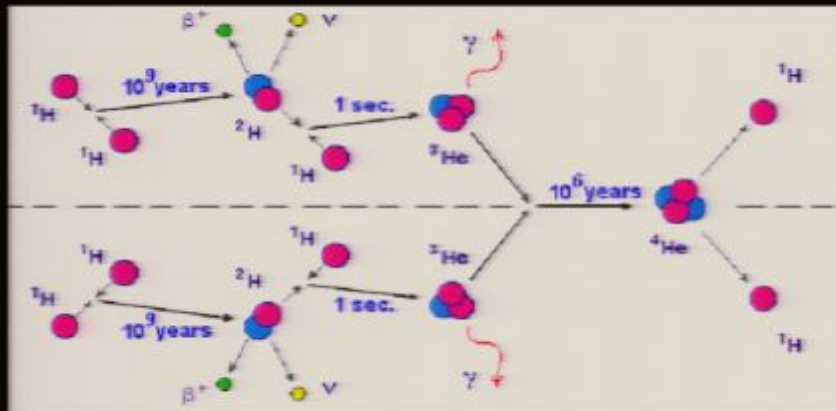


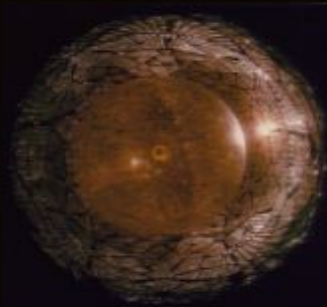
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Proton Decays Into A Neutron





Stellar Energy

Proton-Proton Chain [4H → He + energy]

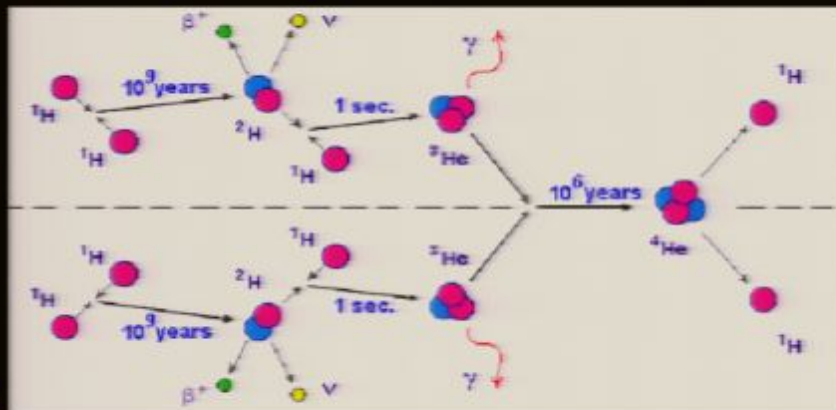
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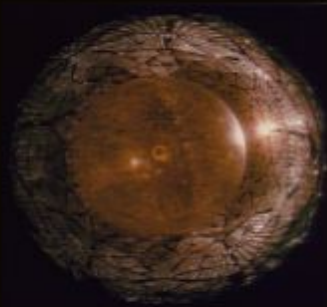
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Positron — ● ●

Neutrino — ●





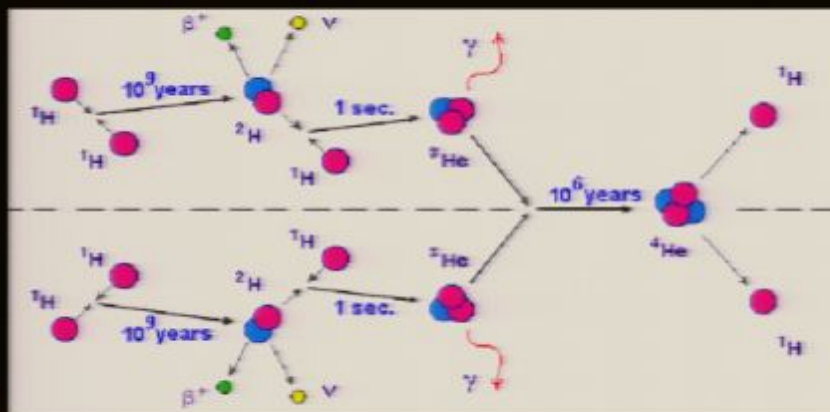
Stellar Energy

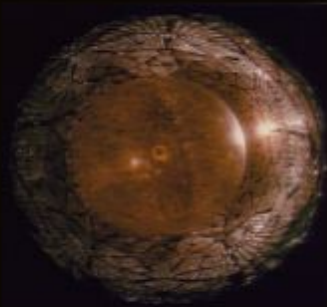
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3He Is Created

● = Neutron
● = Proton





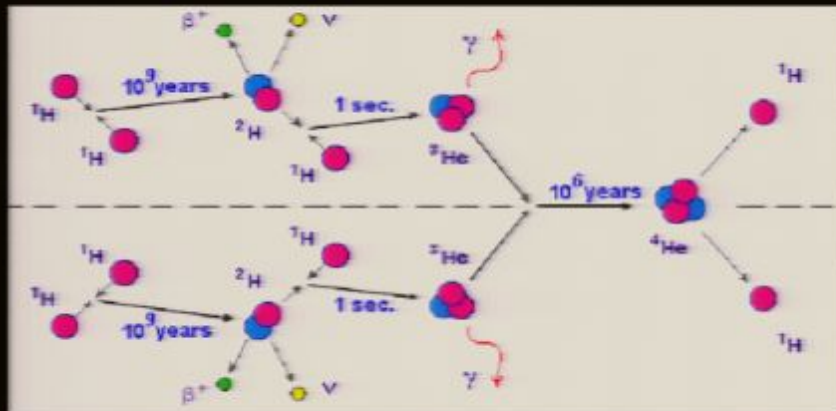
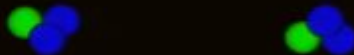
Stellar Energy

Proton-Proton Chain [4H → He + energy]

Two hydrogen nuclei merge to produce deuterium nucleus, a positron, and a neutrino. Add another hydrogen and you get helium 3 and a gamma photon (energy). Two Helium 3 merge and produce helium 4 and two Hydrogen nuclei.

Two 3He Fuse Together

● = Neutron
● = Proton

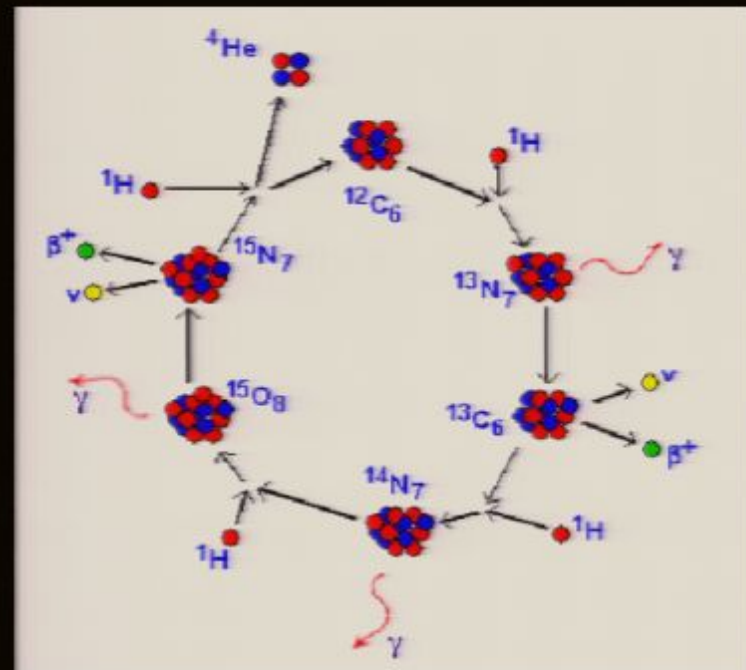
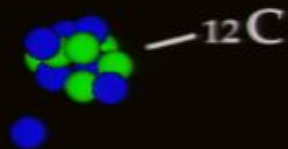


CNO Cycle

- The higher the temperature, the more important the production of energy from the CNO.
- For stars less than 1 solar mass proton-proton cycle dominates.

Stray 1H Absorbed Into
12C, Forming 13N

● — Neutron ● — Proton

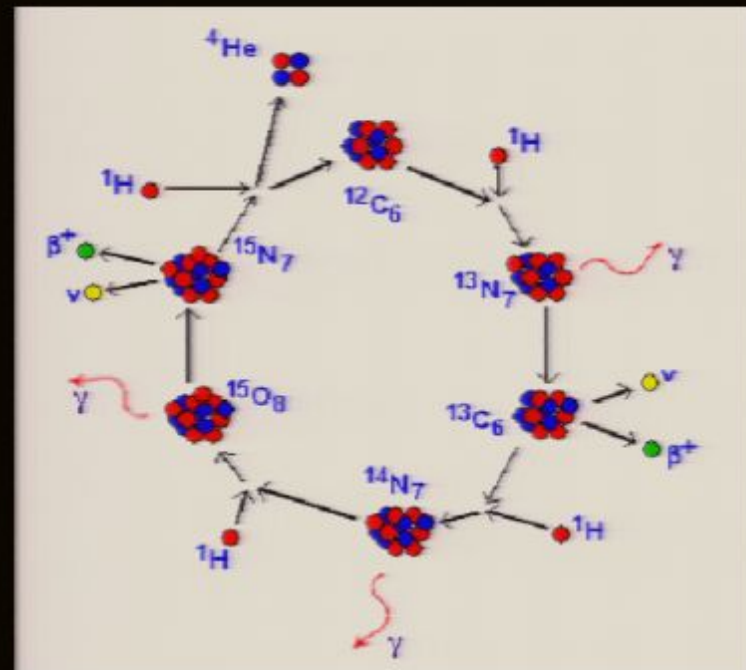
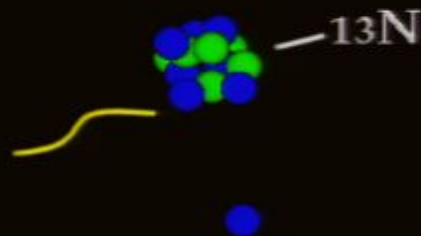


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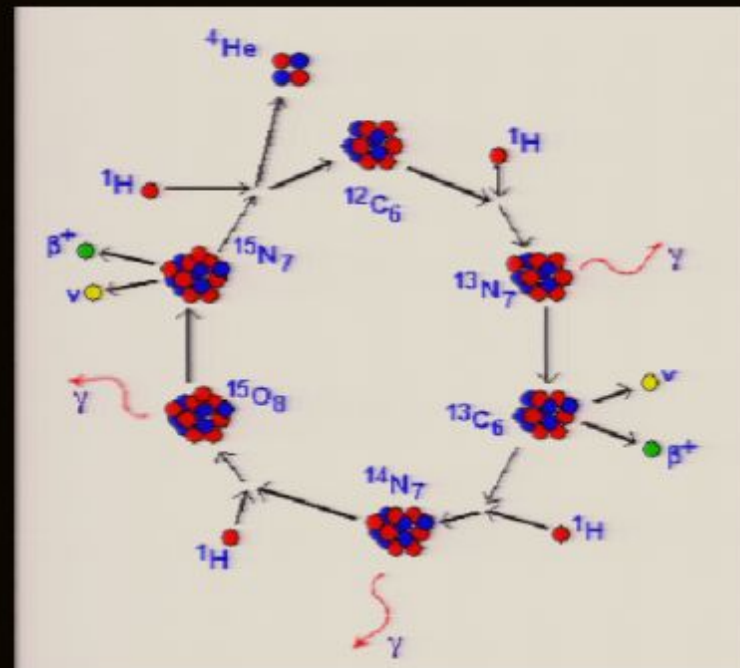
Gamma Ray Released

● — Neutron ● — Proton



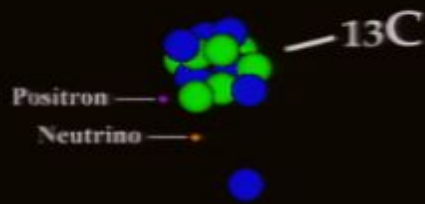
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^{13}N β^+ Decays Into ^{13}C

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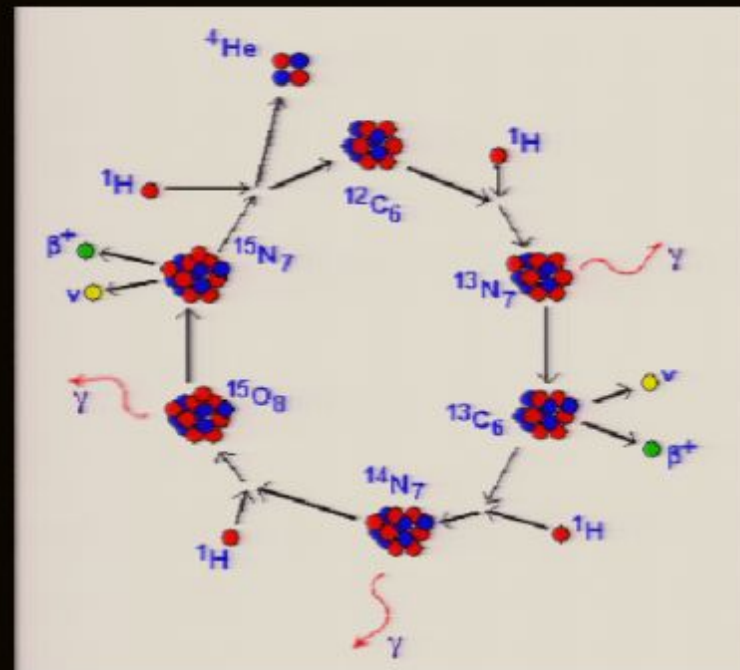
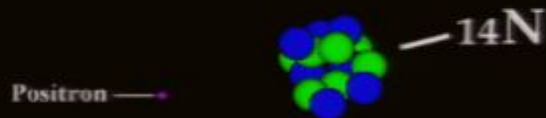


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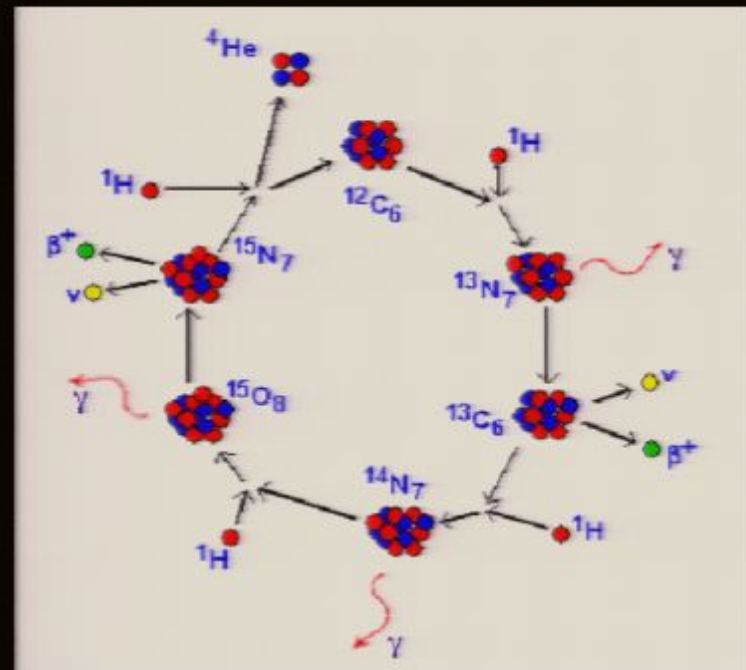
Stray 1H Absorbed Into
12C, Forming 14N

● — Neutron ● — Proton



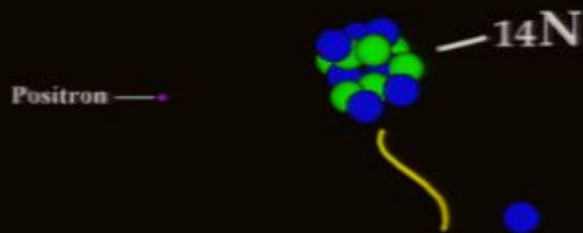
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Gamma Ray Released

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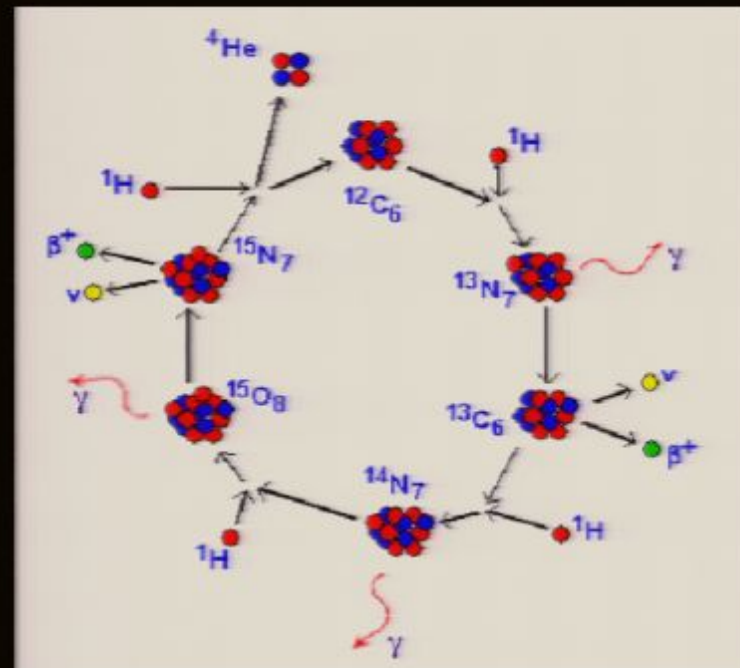
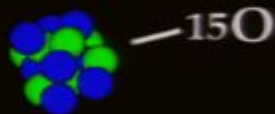


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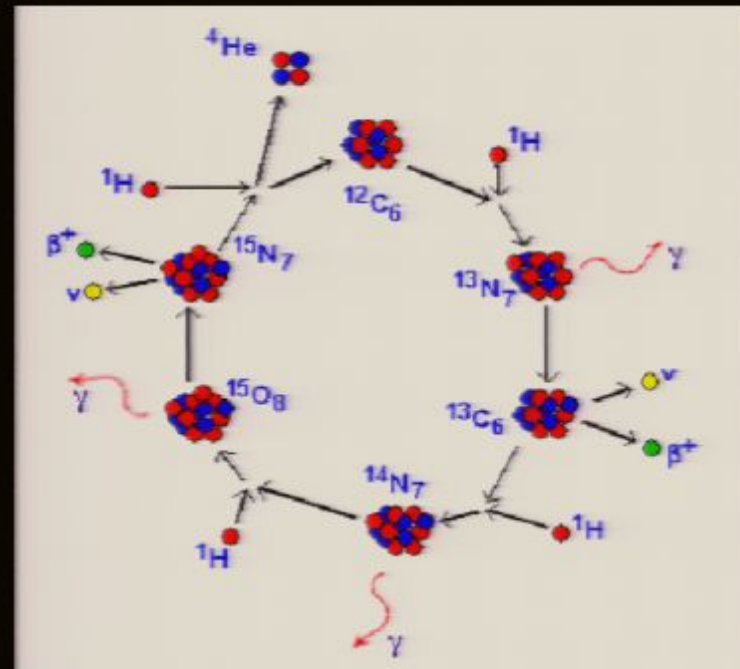
Stray 1H Absorbed Into
14N, Forming 15O

● — Neutron ● — Proton



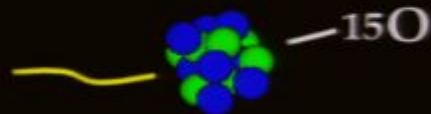
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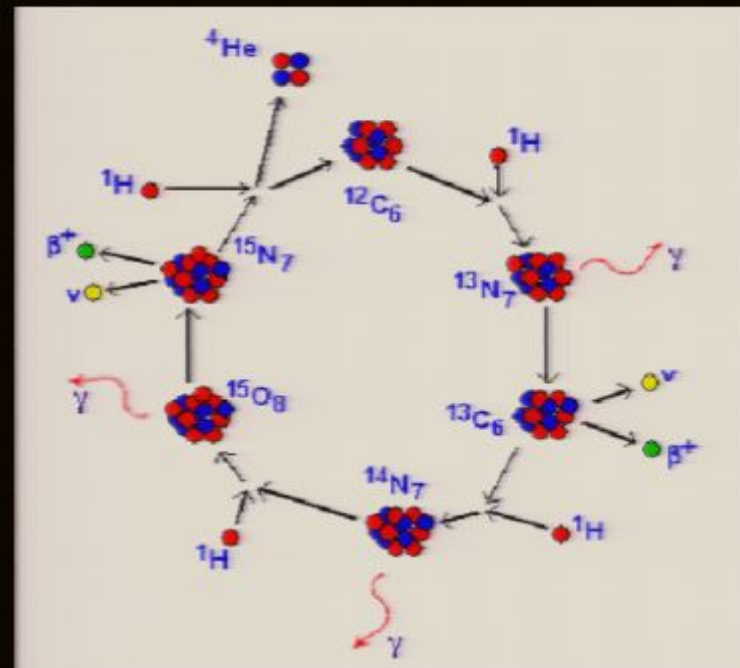
Gamma Ray Released

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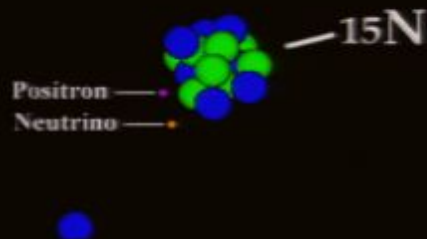
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$^{15}\text{O} \beta^+$ Decays Into ^{15}N

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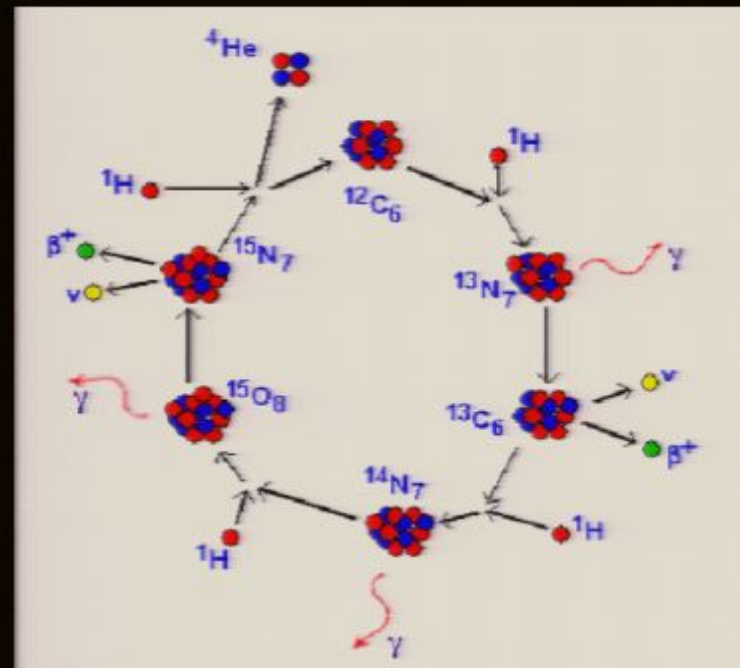
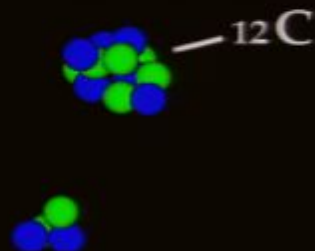


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Alpha Particle Released,
and ^{12}C Remains

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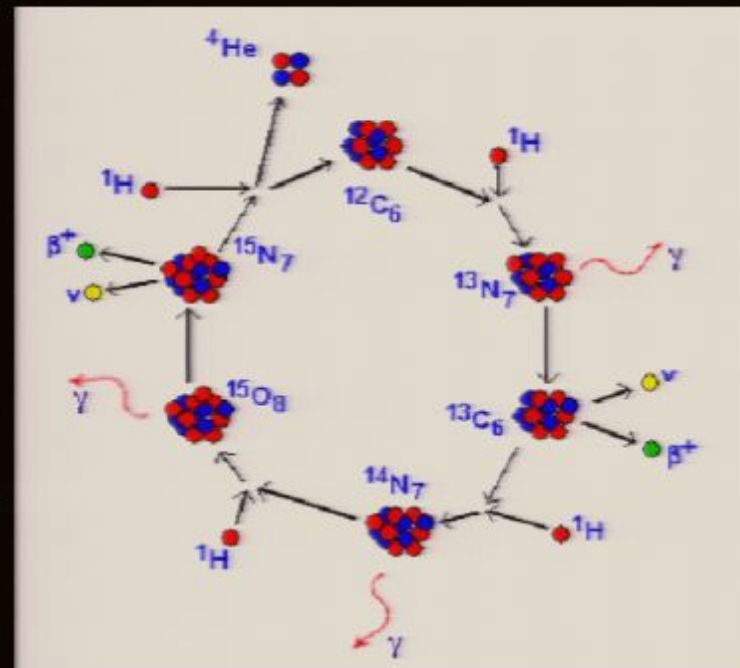
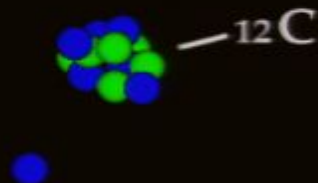


CNO Cycle

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Carbon-Nitrogen-Oxygen (CNO) Cycle

● — Neutron ● — Proton

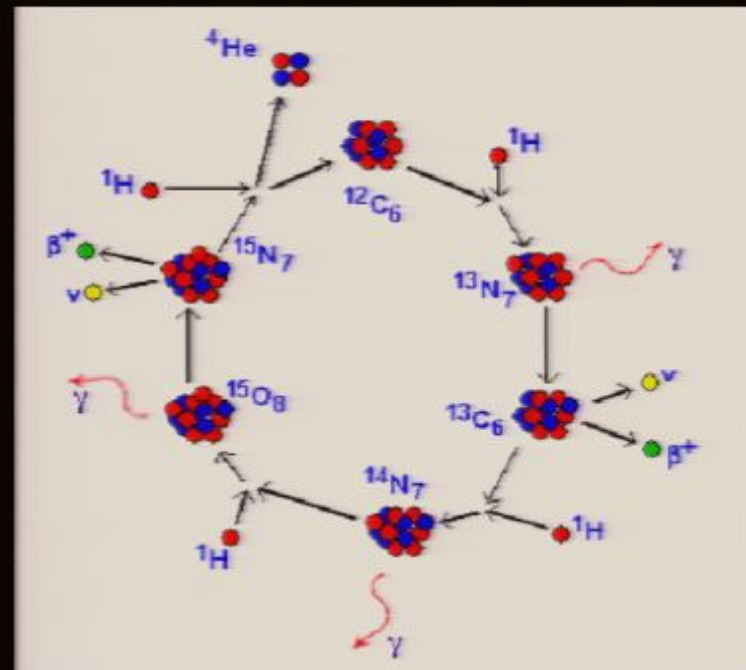
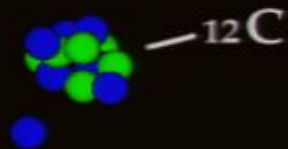


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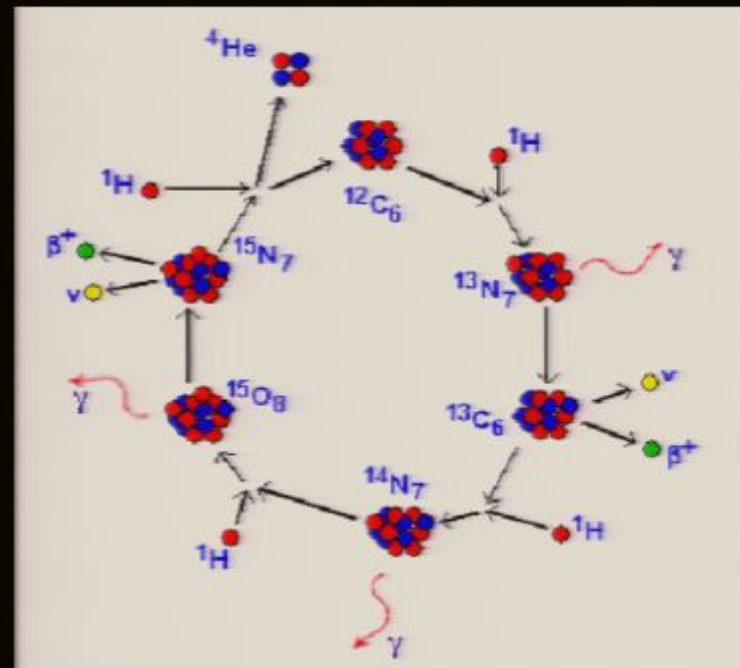
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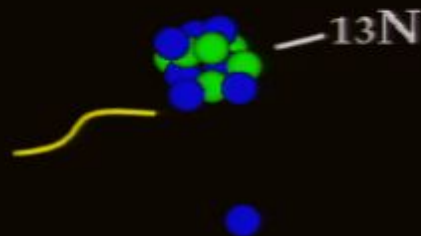
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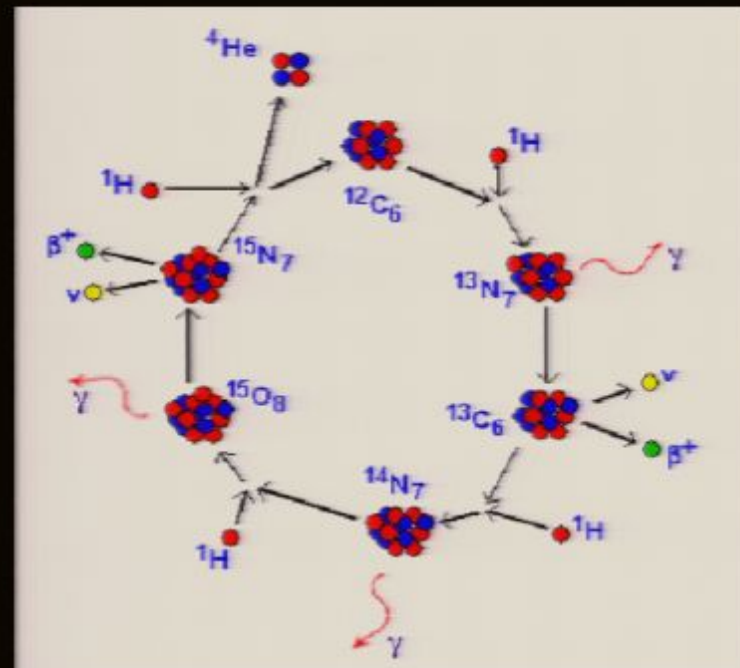
Gamma Ray Released

● — Neutron ● — Proton



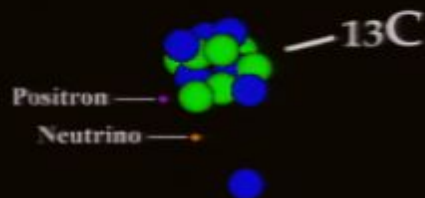
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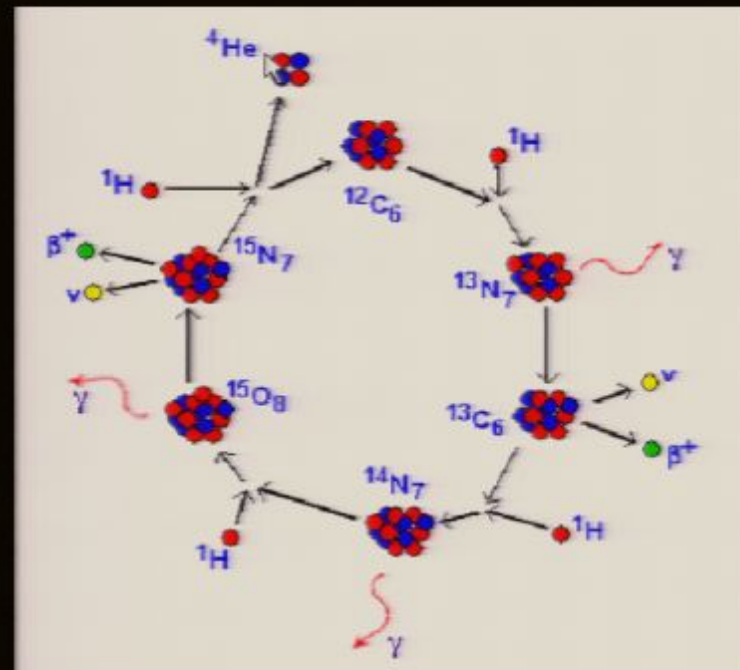
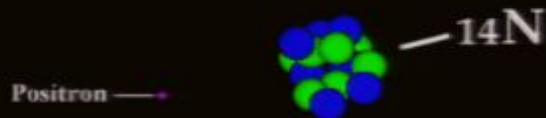


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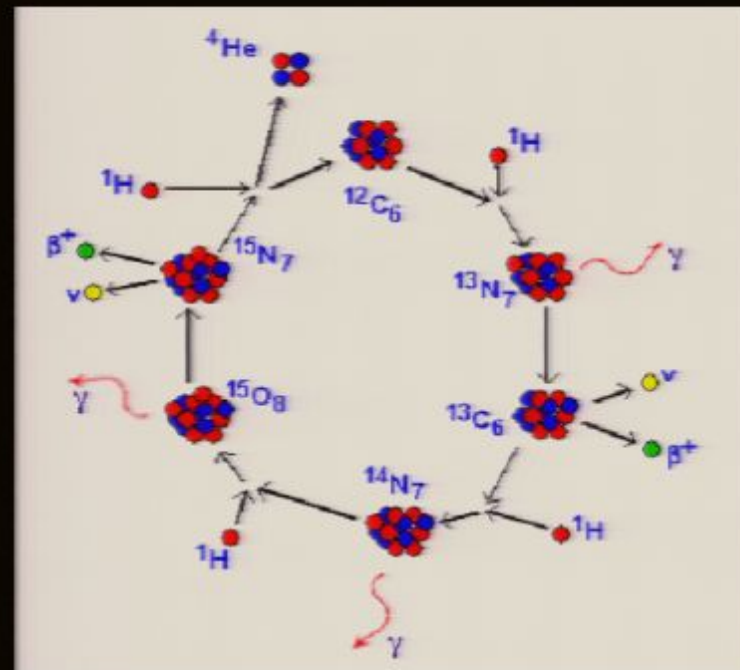
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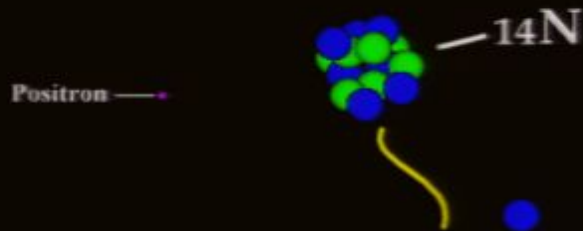
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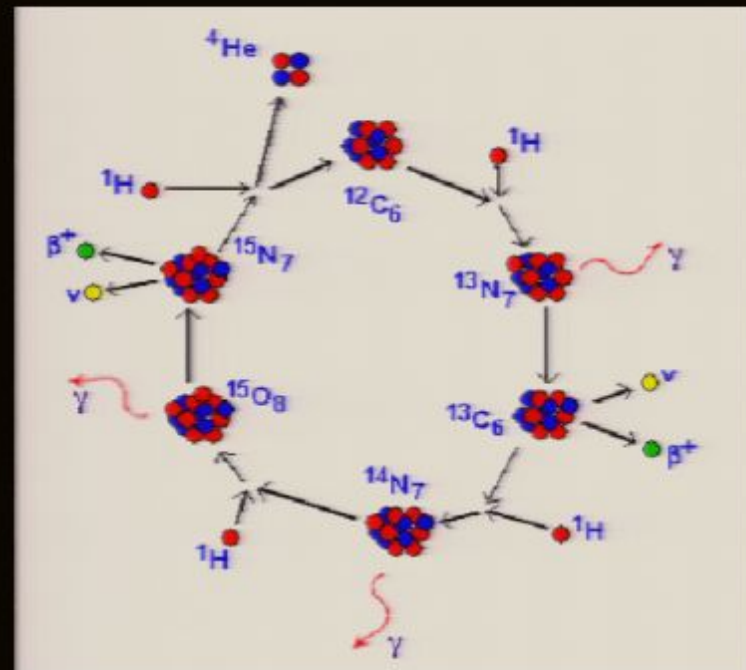
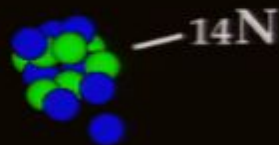


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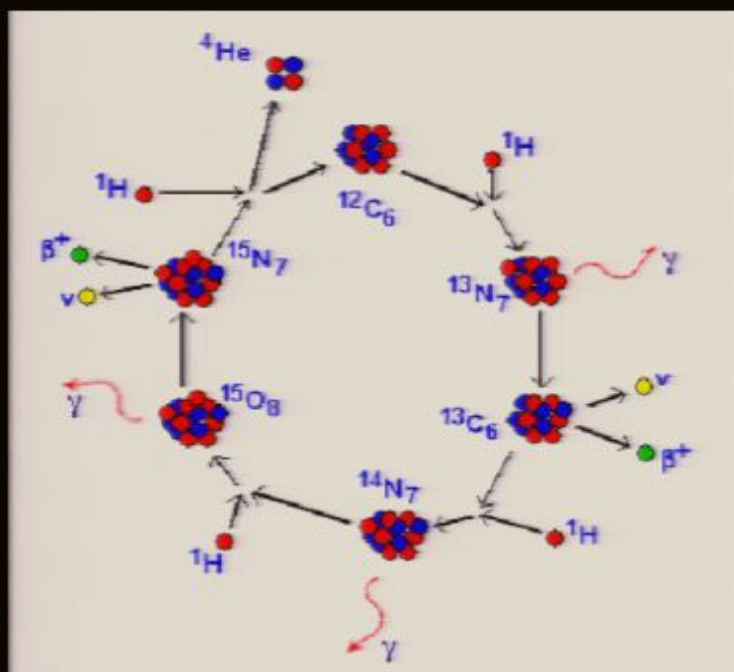
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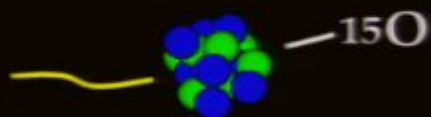
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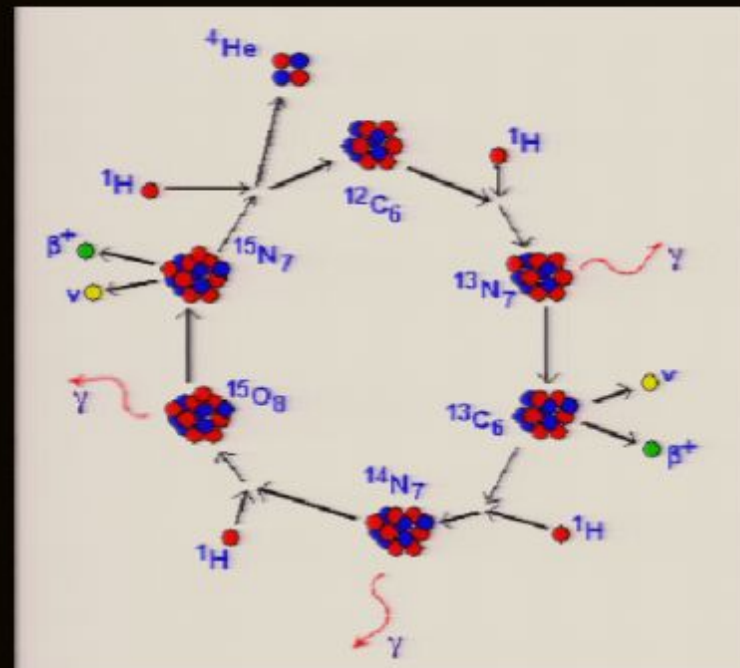
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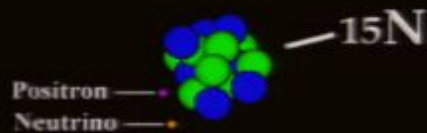
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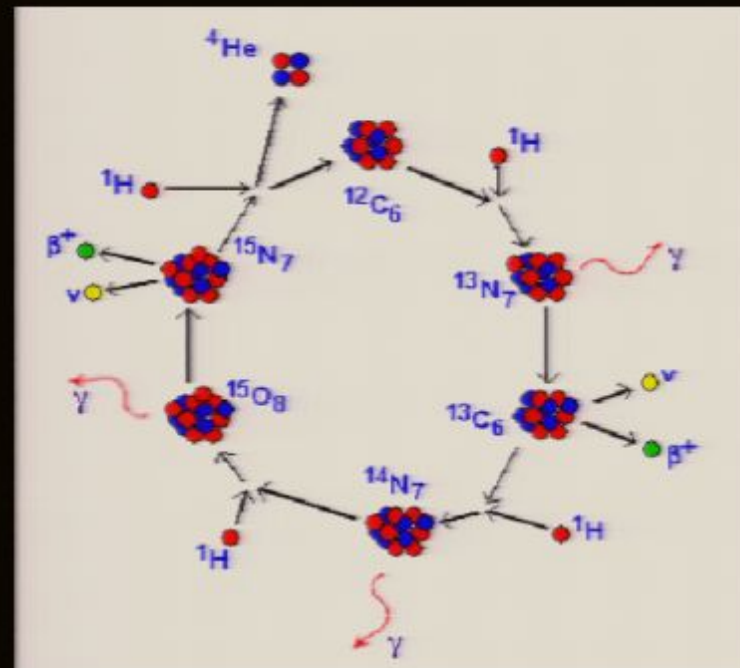
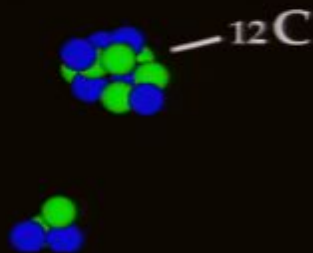


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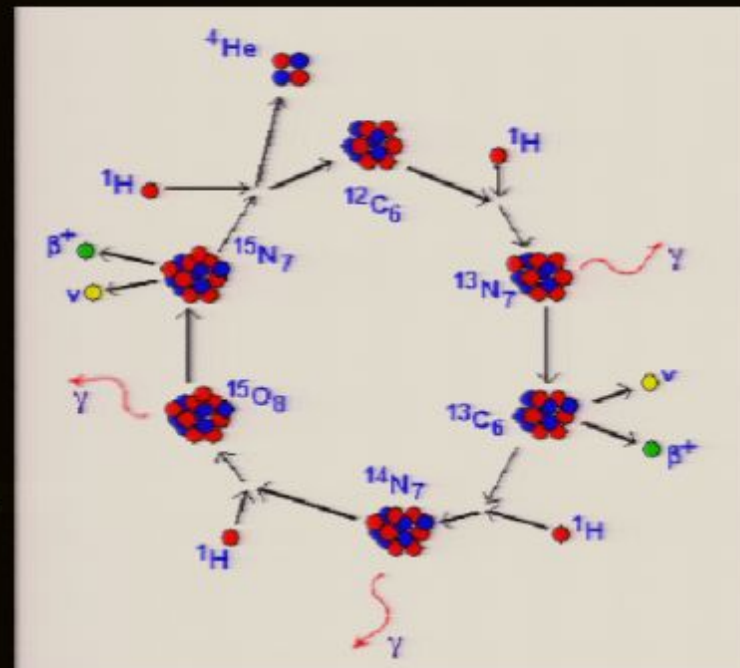
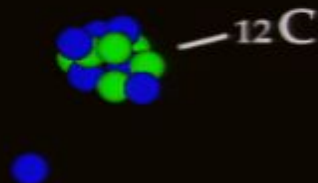


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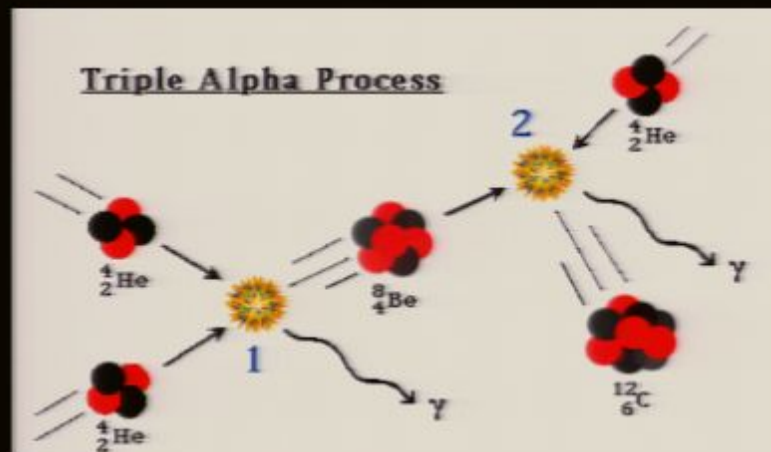
Carbon-Nitrogen-Oxygen (CNO) Cycle

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Beyond Helium

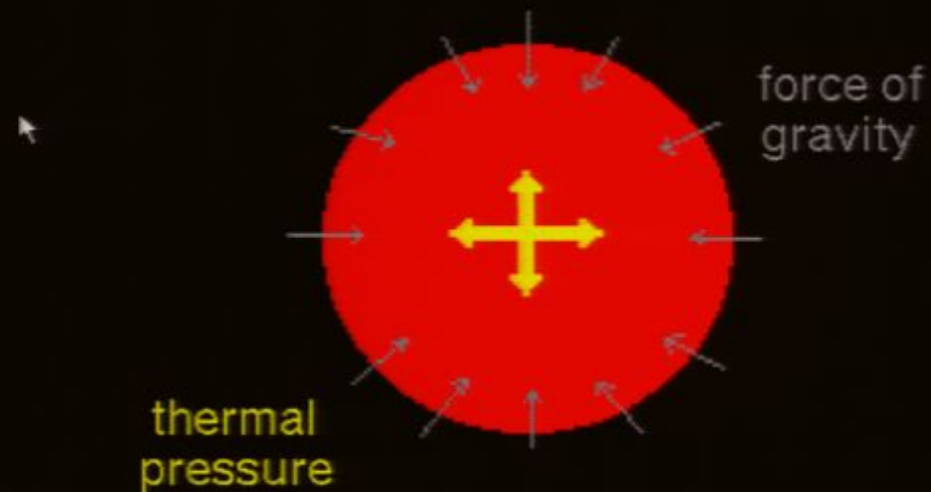
As Hydrogen is exhausted in the core of the star, Helium nuclei merge to create Beryllium with again fuses with another Helium nucleus to give Carbon and then to Oxygen then to Silicon until we finally end up with Iron.



Pressure balance in a star

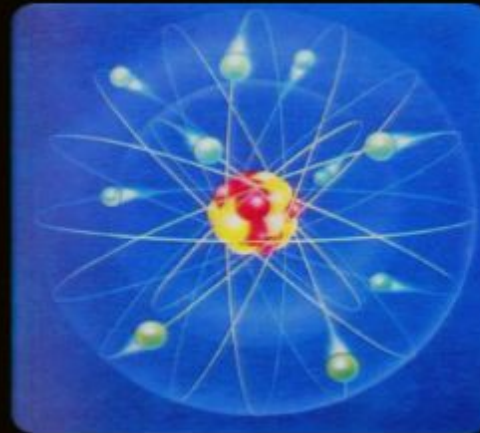
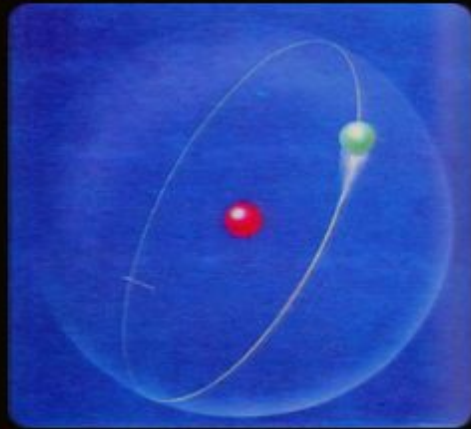


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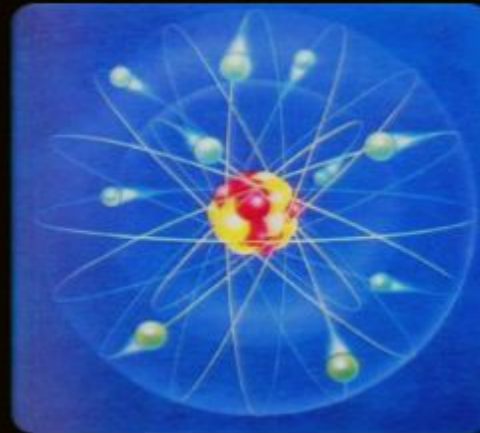
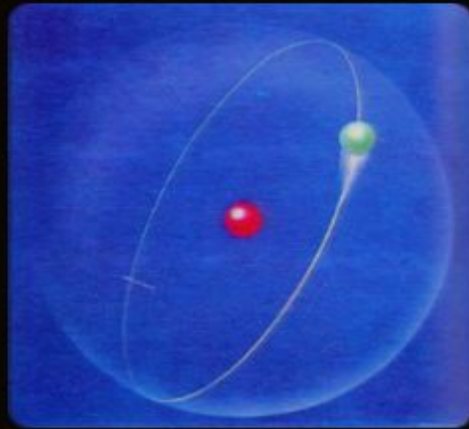


thermal pressure = force of gravity

Model of an Atom



Model of an Atom



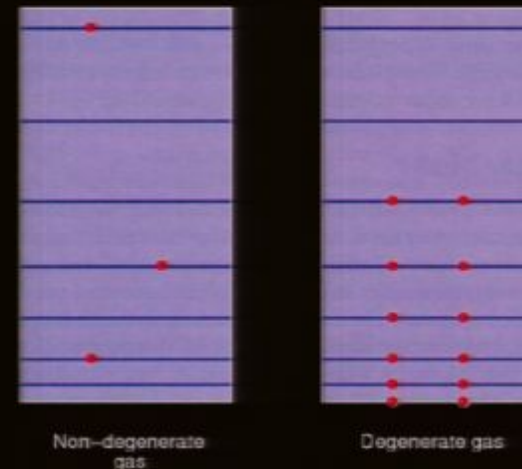
... an atom consists of mainly empty space ...

Electron Degeneracy Pressure

$$R = N_e^{\frac{2}{3}} \frac{h^2}{8Gm_e m_p M}$$

- **Pauli Exclusion Principle:**
No two electrons (fermions) can occupy the same position in space at the same time doing the same thing.
- Electrons are packed side by side in a white dwarf
- This prevents it from collapsing any further

Calculate pressure

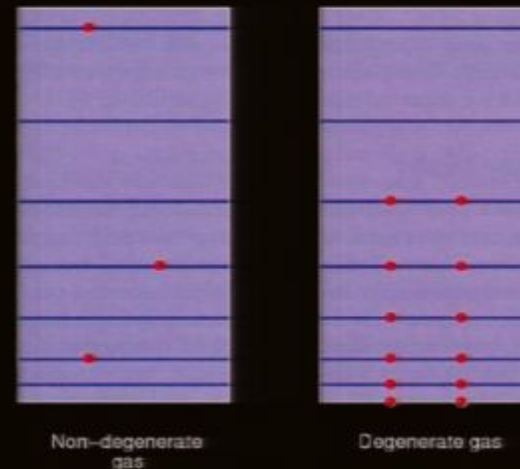


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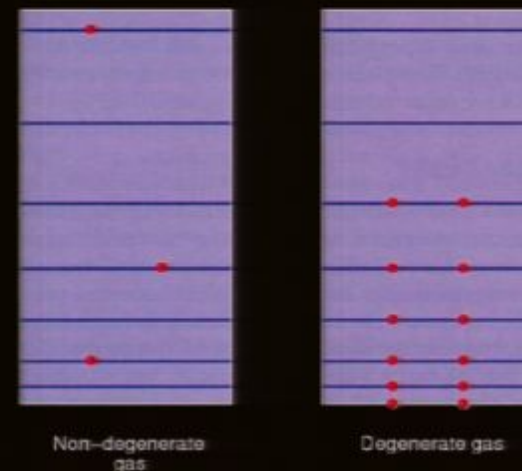


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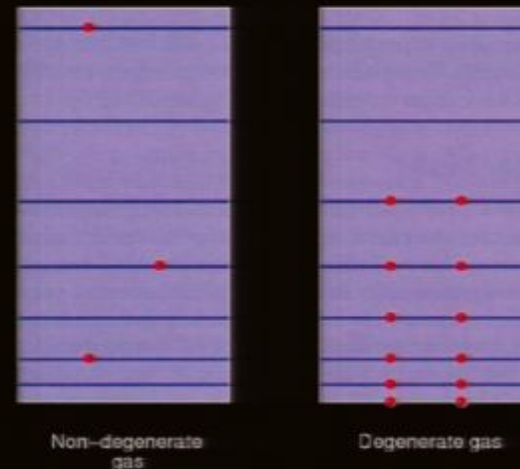


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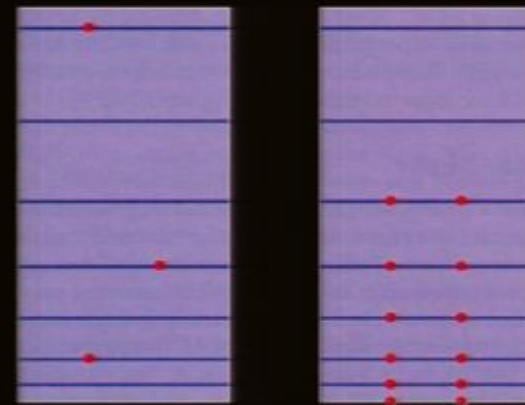
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Electron Degeneracy Pressure

$$R = N_e^{\frac{2}{3}} \frac{h^2}{8Gm_e m_p M}$$

Electron degeneracy pressure is a quantum mechanical effect that arises from the Pauli exclusion principle, which states that no two electrons can occupy the same quantum state. As the density of electrons increases, the available quantum states become more closely spaced, and the electrons are forced into higher energy states, creating a pressure that resists further compression.



Non-degenerate gas

Degenerate gas



Electron Degeneracy Pressure

$$R = N_e^{\frac{2}{3}} \frac{h^2}{8Gm_e m_p M}$$

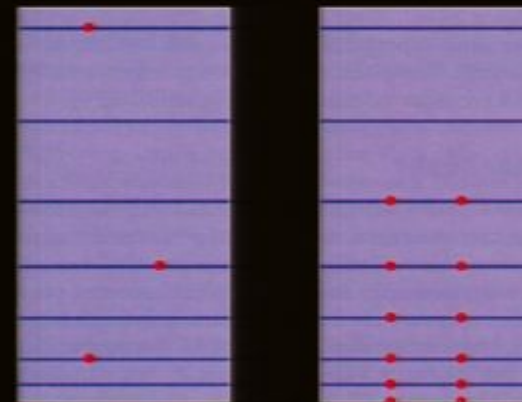
$$h = 6.6261 \times 10^{-34}$$

$$G = 6.6726 \times 10^{-11}$$

$$m_e = 9.1094 \times 10^{-31}$$

$$m_p = 1.6726 \times 10^{-27}$$

$$M = 1.989 \times 10^{30}$$



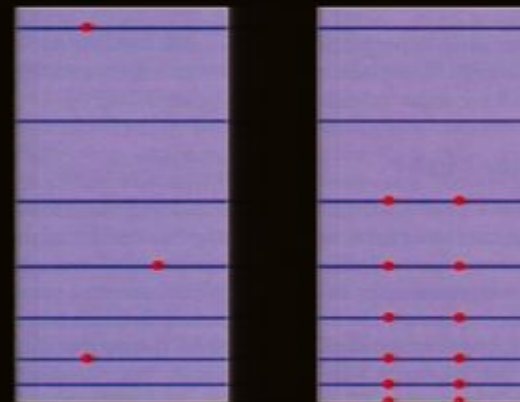
Non-degenerate
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Electron Degeneracy Pressure

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$(5.95 \times 10^{56})^{\frac{2}{3}}$ $2.7 \times 10^{-31} m$



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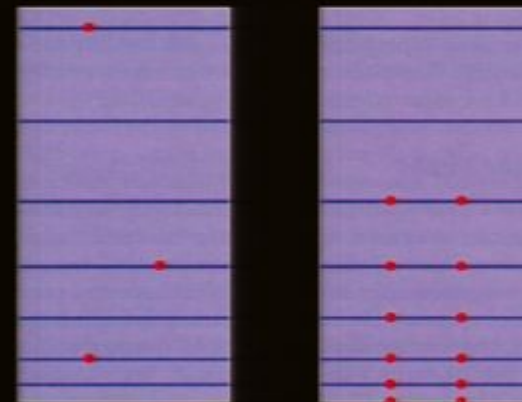


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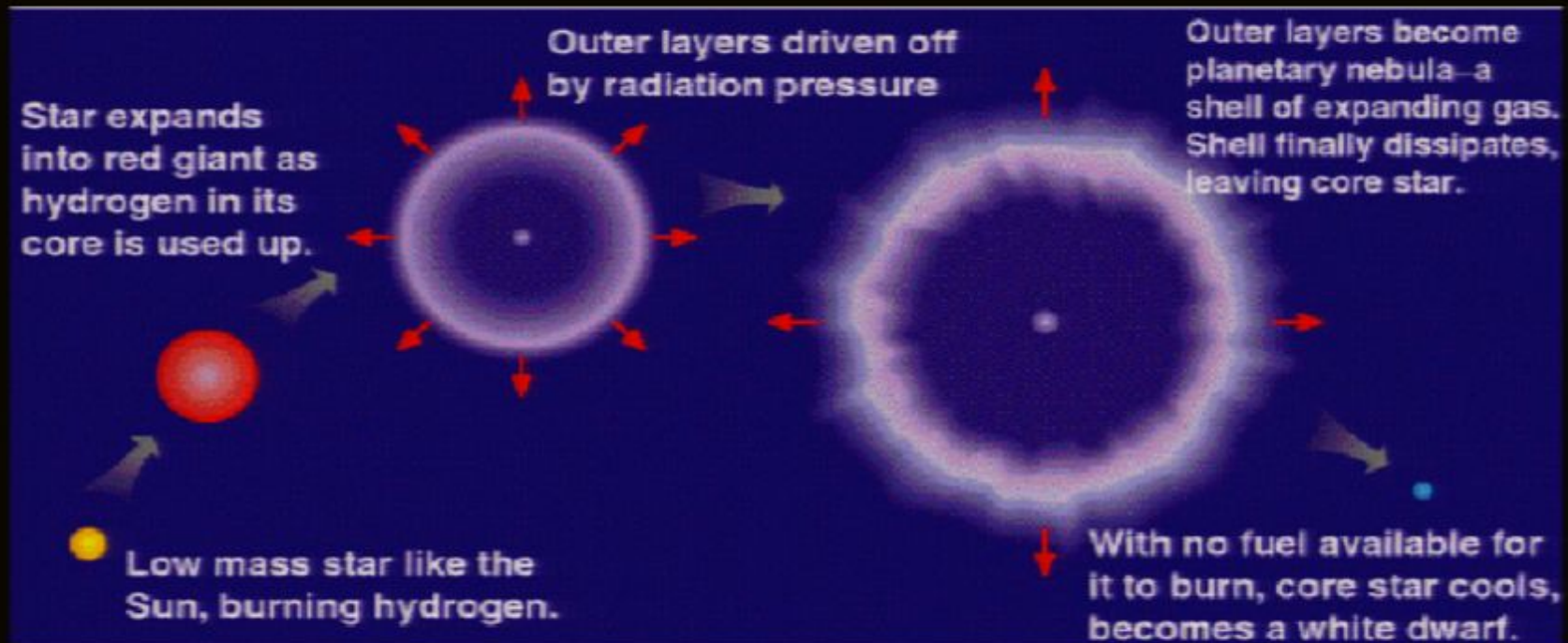
$10^7 m$



Non-degenerate gas

Degenerate gas

Path to being a White Dwarf



7 solar mass star now reduced to about 20% of its original mass

Properties of White Dwarfs

Properties of White Dwarfs

- Helium exhausted, core collapses until density forces electrons to leave their orbits around the atomic nuclei.

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- ...are found in the centers of planetary nebula.

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- ...are found in the centers of planetary nebula.
- ...have masses less than the Chandrasekhar mass (1.4 Solar Masses).

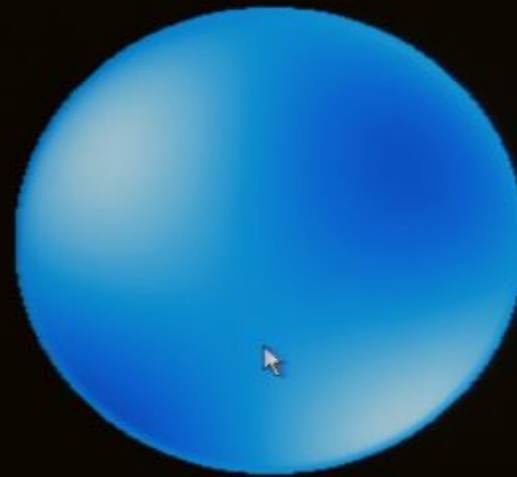
White Dwarf Properties

...have diameters about the same as the Earth's.



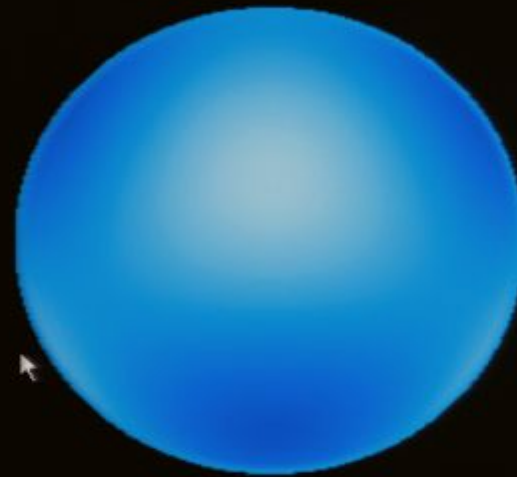
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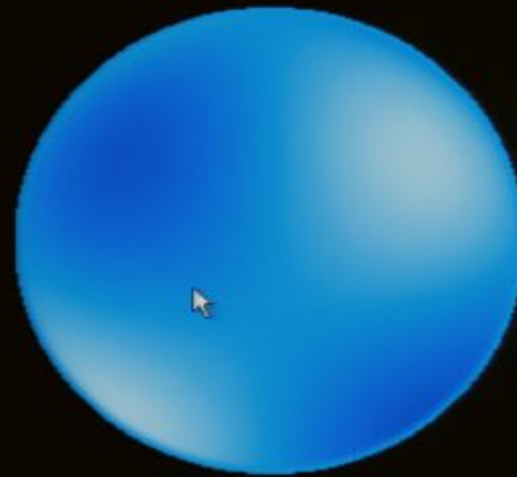
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Ring Nebula



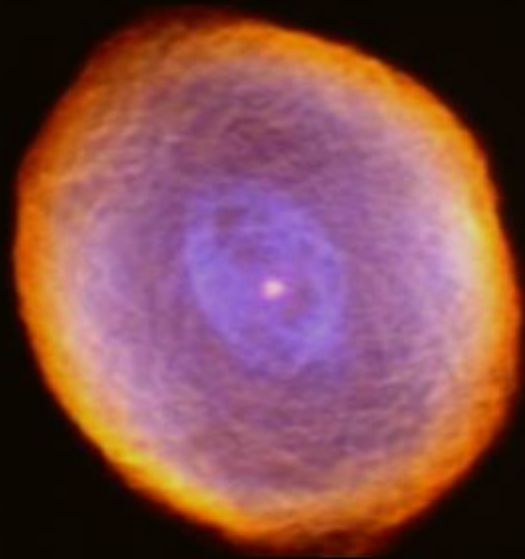
Ring Nebula

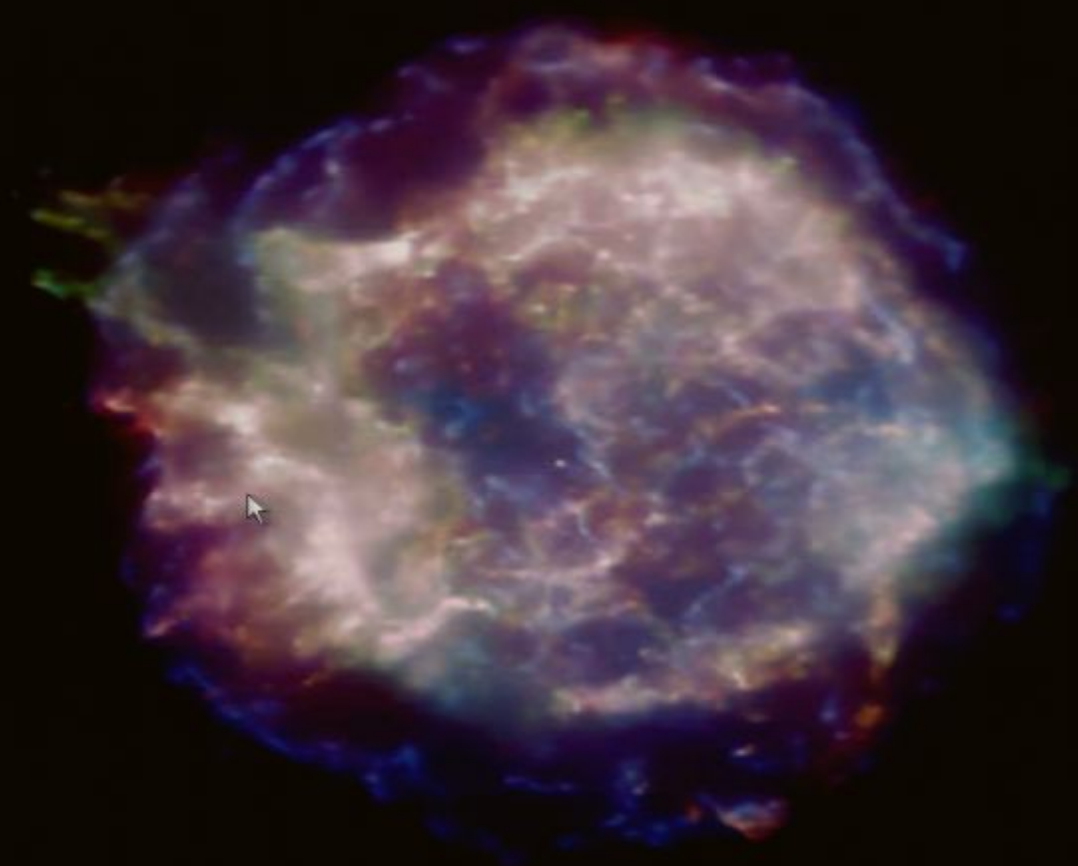


Cat's eye nebula



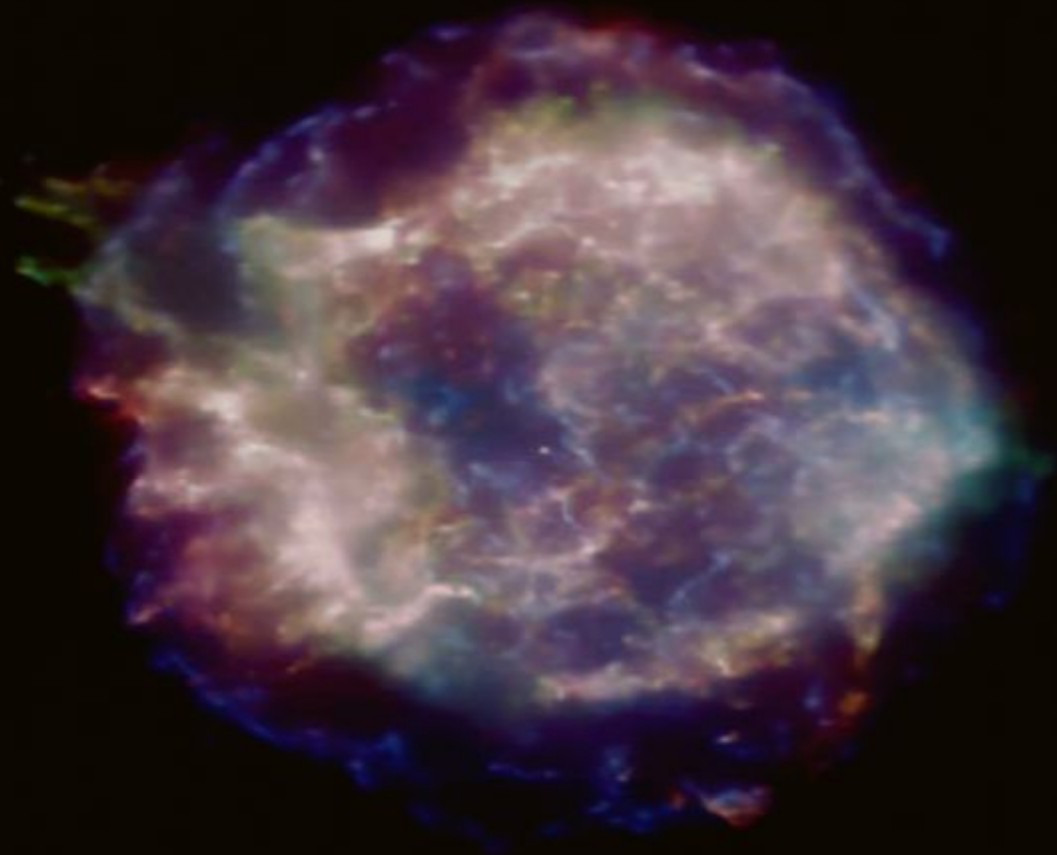
Spirograph Nebula



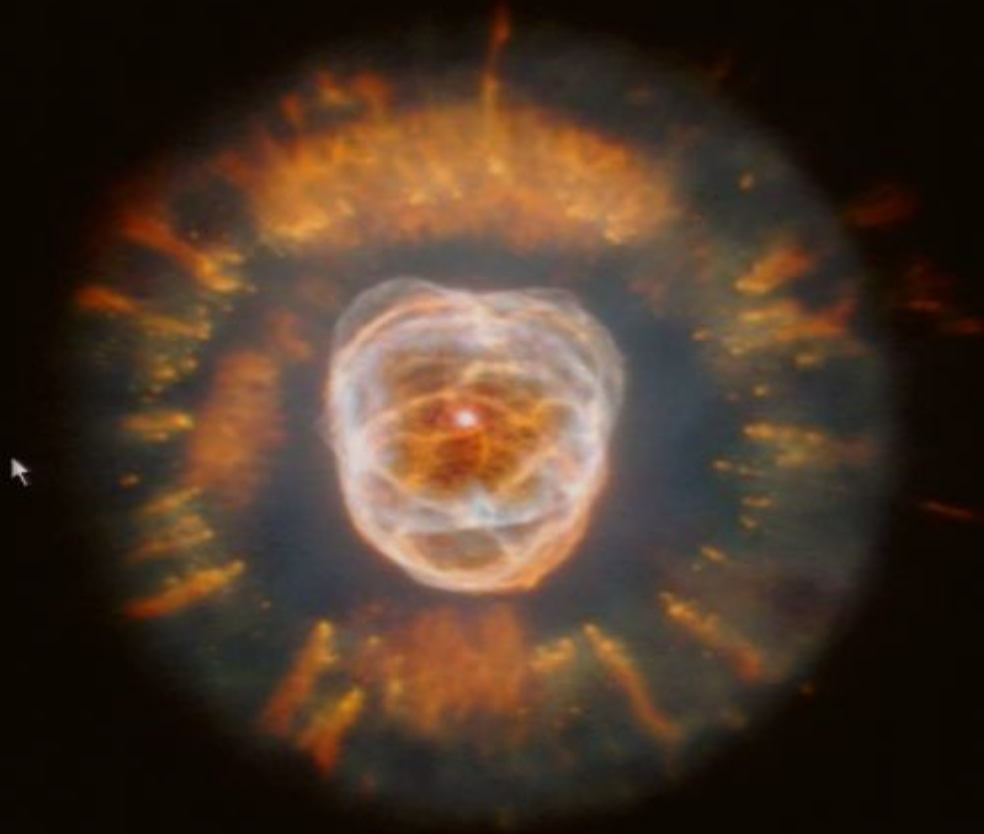


Eskimo Nebula





Eskimo Nebula



Chandrasekhar limit



Chandrasekhar limit

- The maximum mass of a white dwarf is 1.4 solar masses



Chandrasekhar limit

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- Above this, even electron degeneracy pressure cannot counterbalance gravity



Chandrasekhar limit

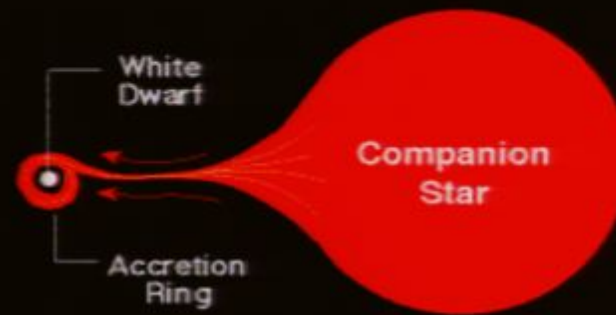
- The maximum mass of a white dwarf is 1.4 solar masses
- Above this, even electron degeneracy pressure cannot counterbalance gravity
- What is the fate of a star more massive than this?



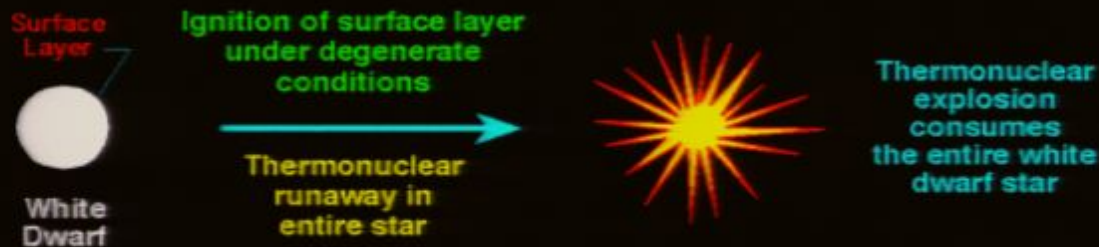
Supernova Remnant

- In the death of a high-mass star (<40 solar mass), the core is converted to neutrons and collapses catastrophically.
- The collapse and rebound creates a supernova.
- But what happens to the neutrons already at the very center of the core?
- The central core is left behind as a small, dense, sphere of neutrons → a neutron star.

Type 1a Super Nova



Thin hydrogen surface layer accumulated on white dwarf through accretion ring

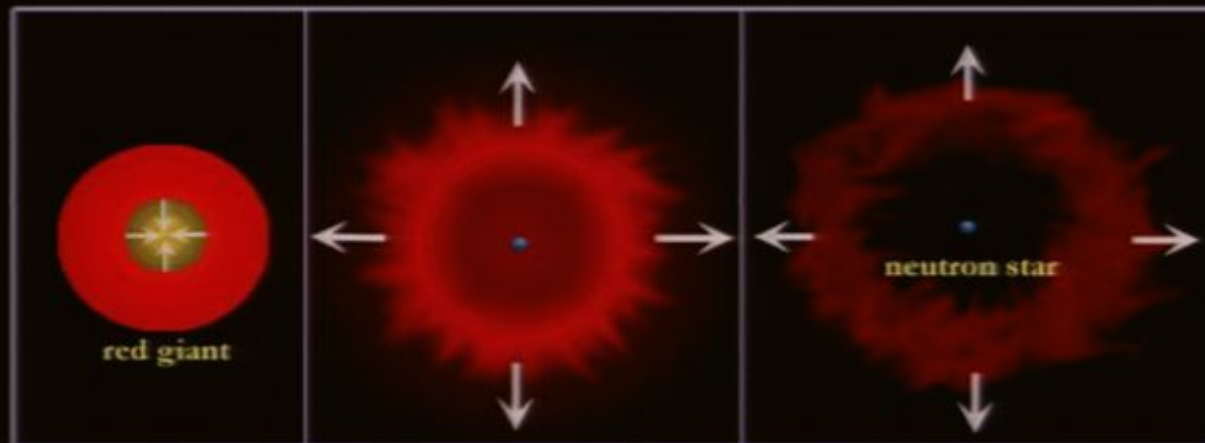


Not of interest to black hole cosmologists, but type 1a's are great yard sticks in determining distances



Type II Supernovae: Birth of a neutron star

- *The core survives and is prevented from collapsing any further by neutron degeneracy pressure*
- *These are what we are interested in.*

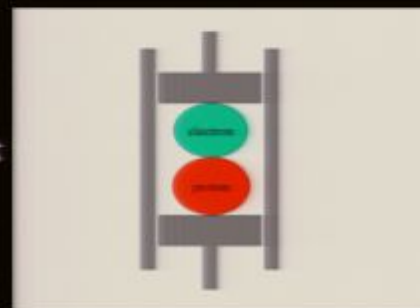
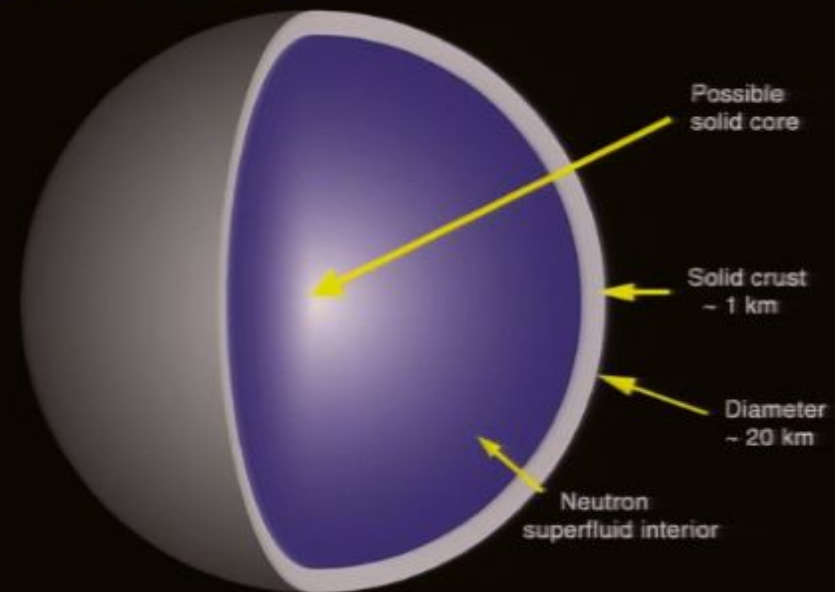


Core Implosion → Supernova Explosion → Supernova Remnant



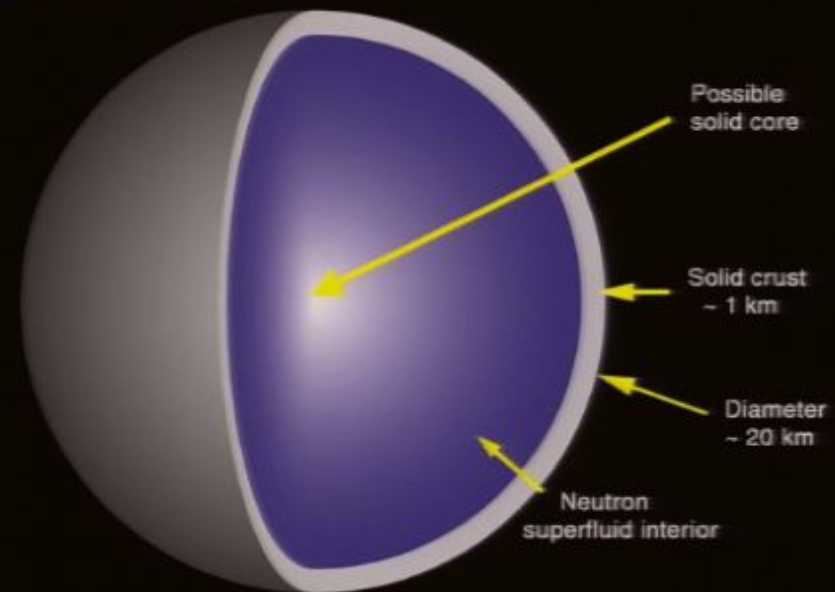
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- A giant ball of neutrons.
- Mass : at least 1.4 x mass of the Sun.
- Temperature 1 million degrees and cooling.
- Diameter: 20 km!
- Density: 10^{18} kg/m³
 - A sugar cube of this matter weighs 400 billion tons
- Day: 1 – 0.001 seconds!
- Magnetic fields as strong as the Sun, but in the space of a city.



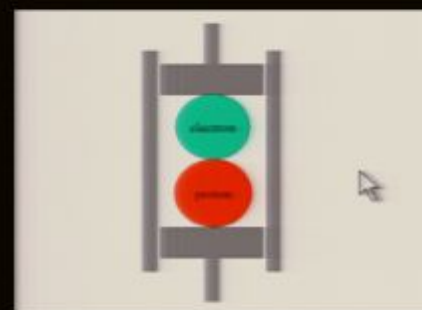
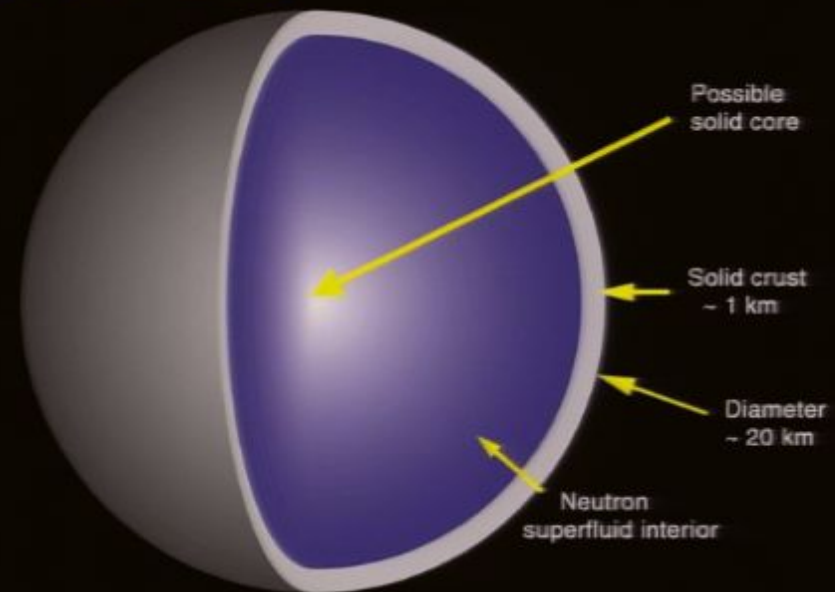
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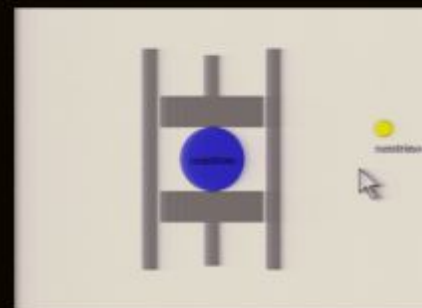
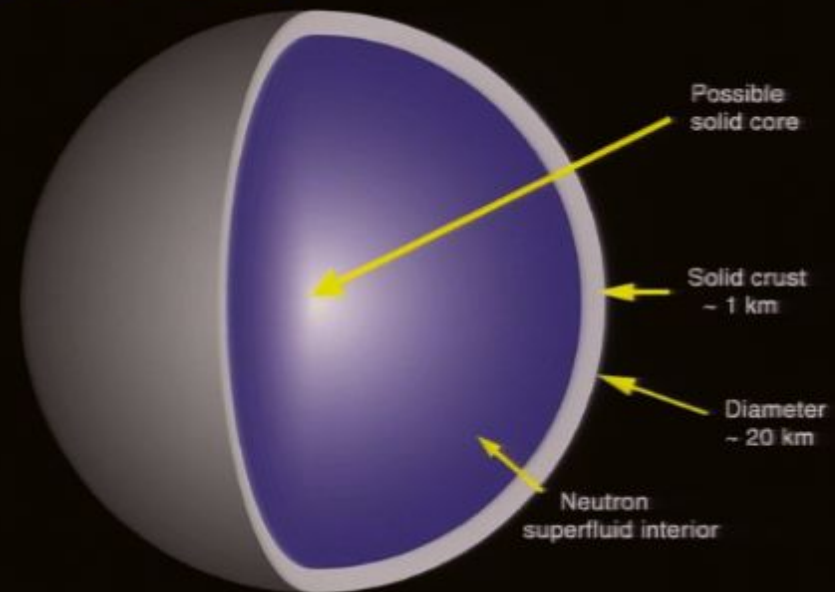
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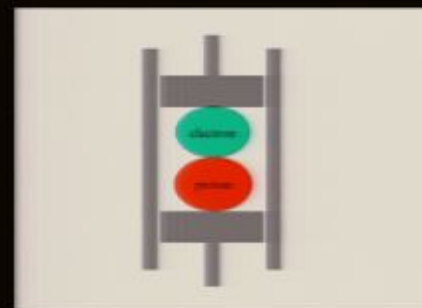
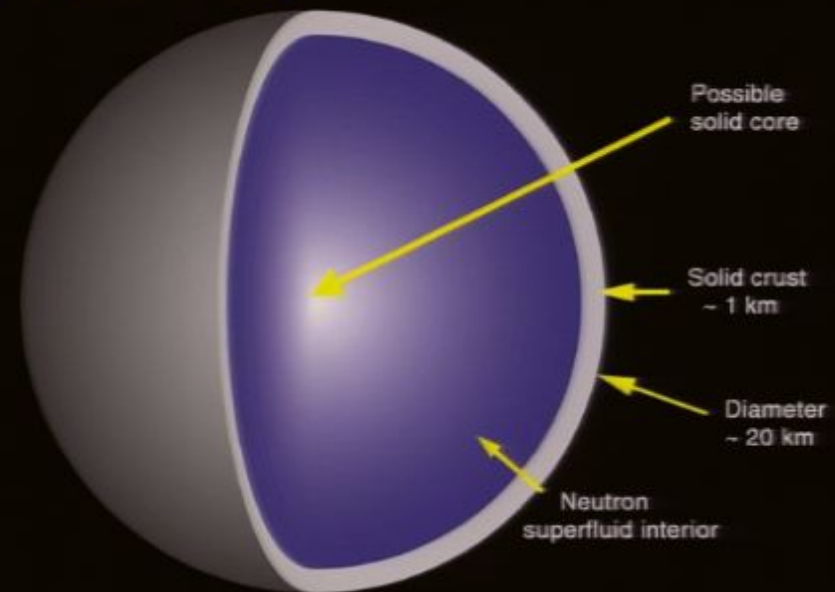
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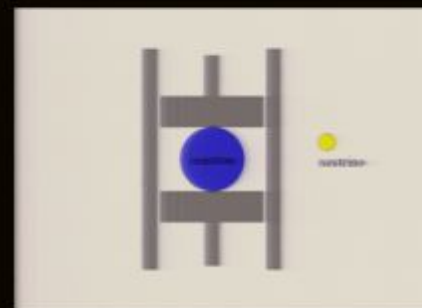
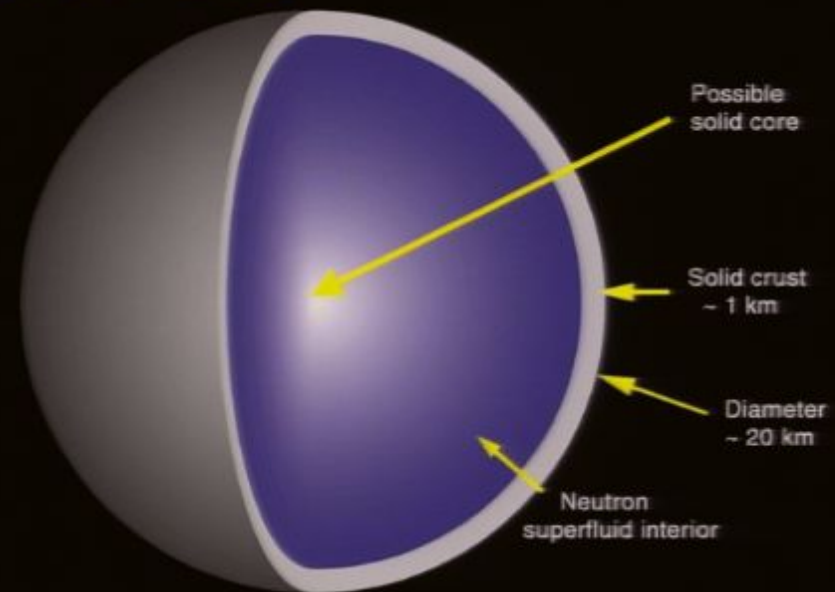
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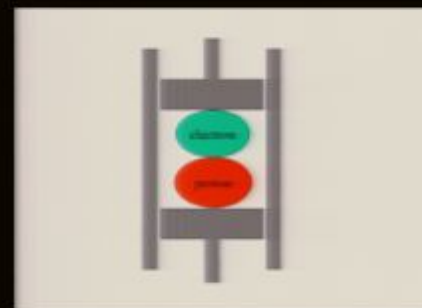
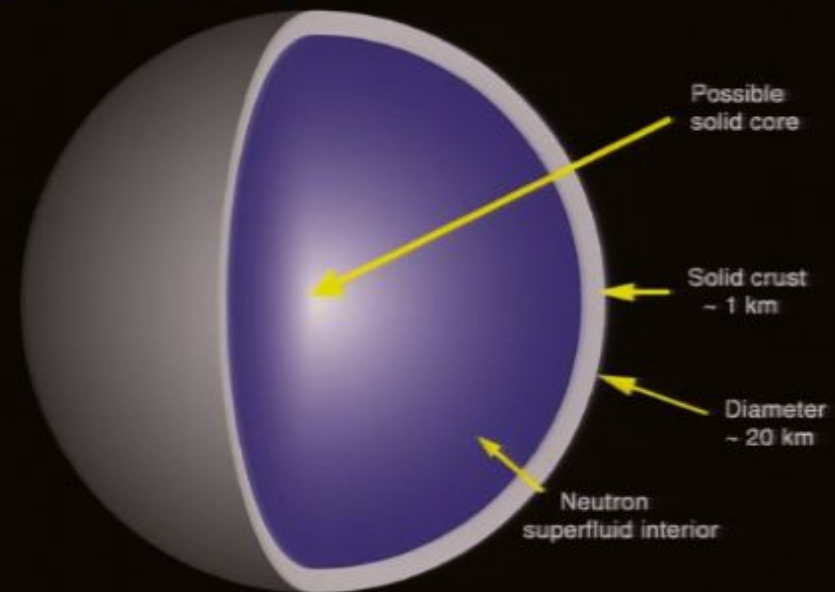
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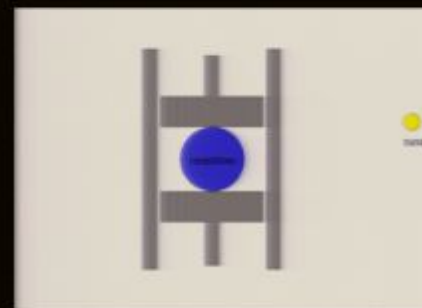
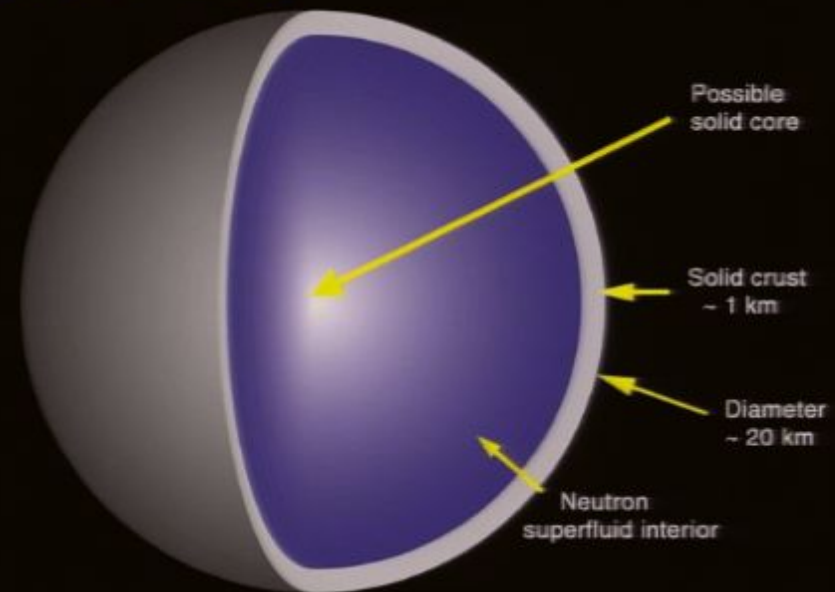
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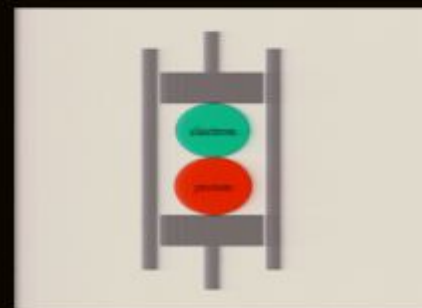
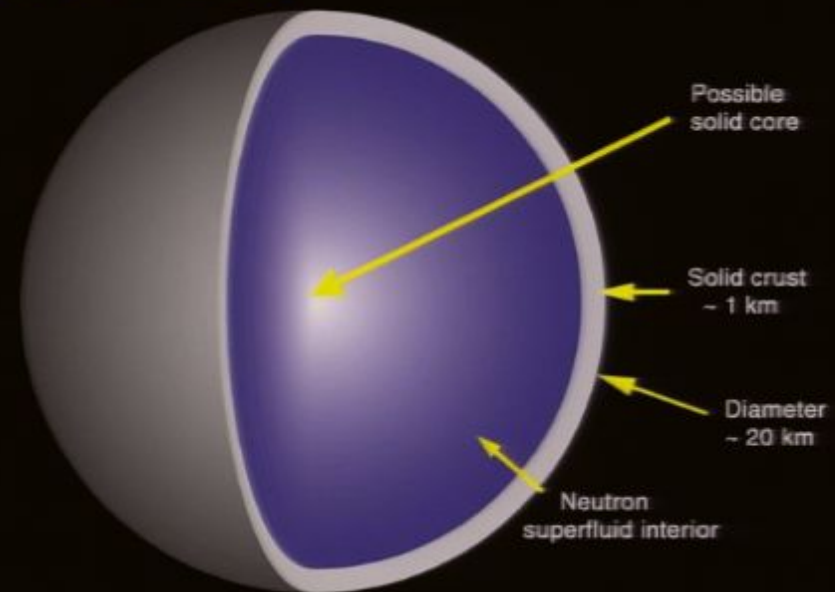
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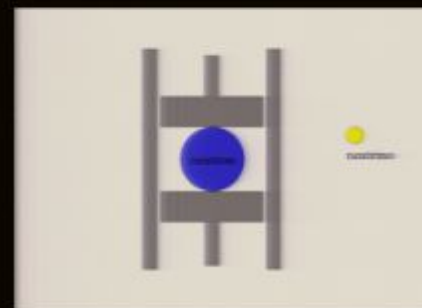
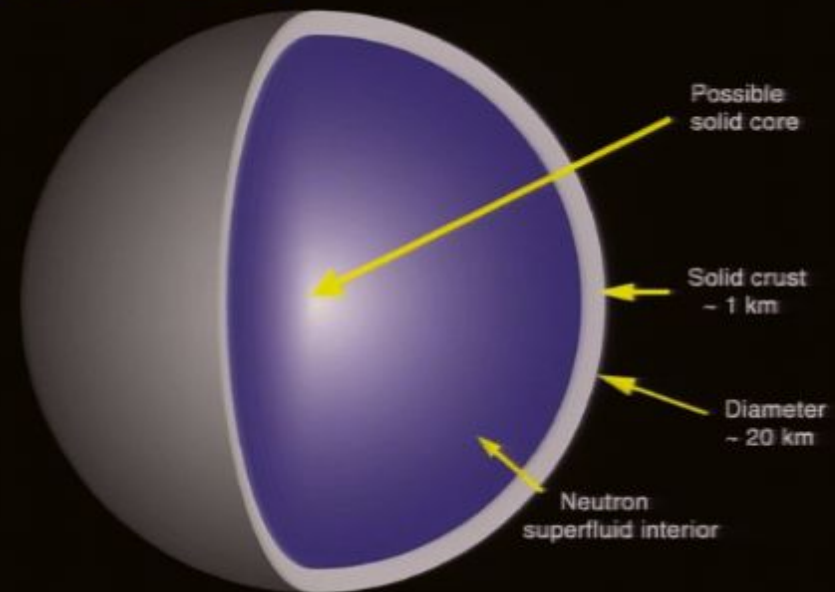
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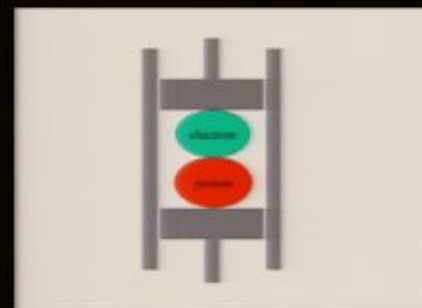
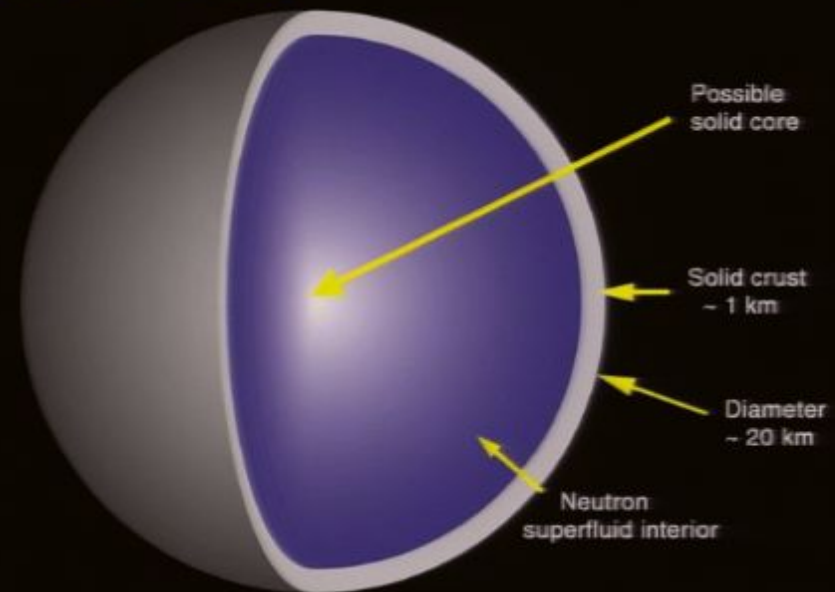
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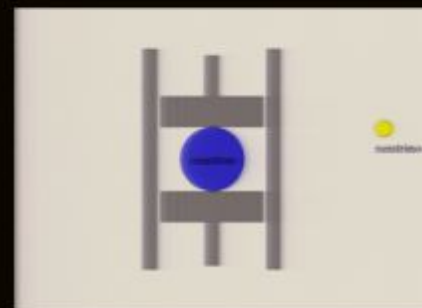
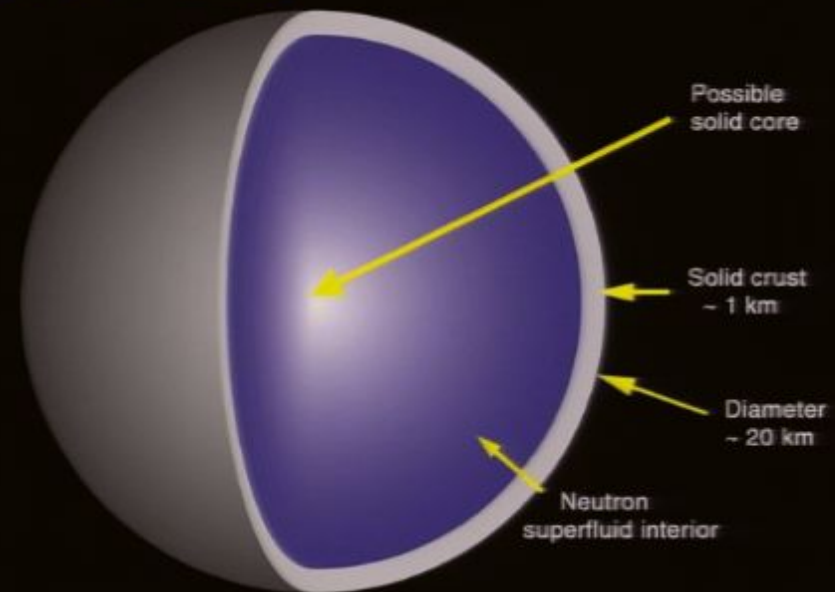
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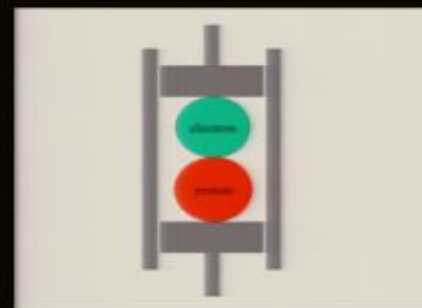
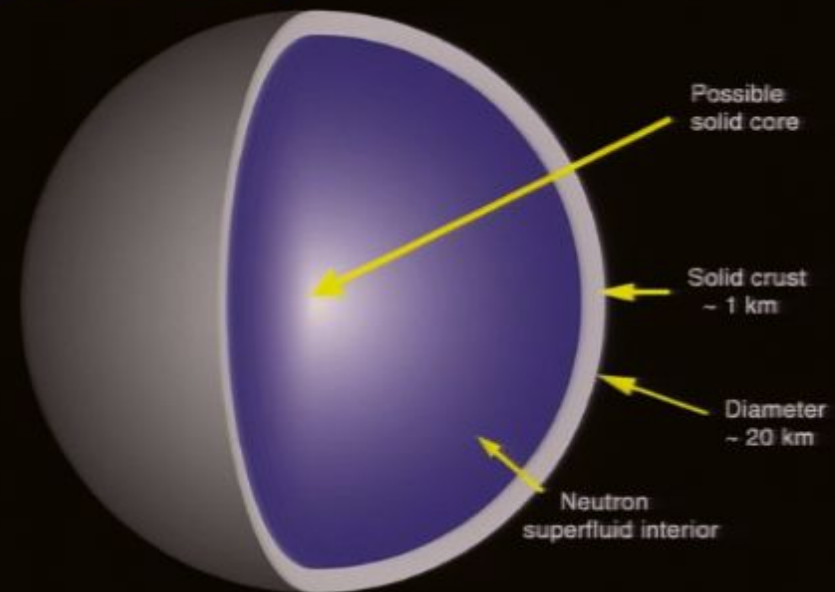
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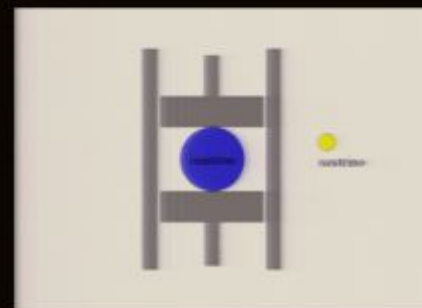
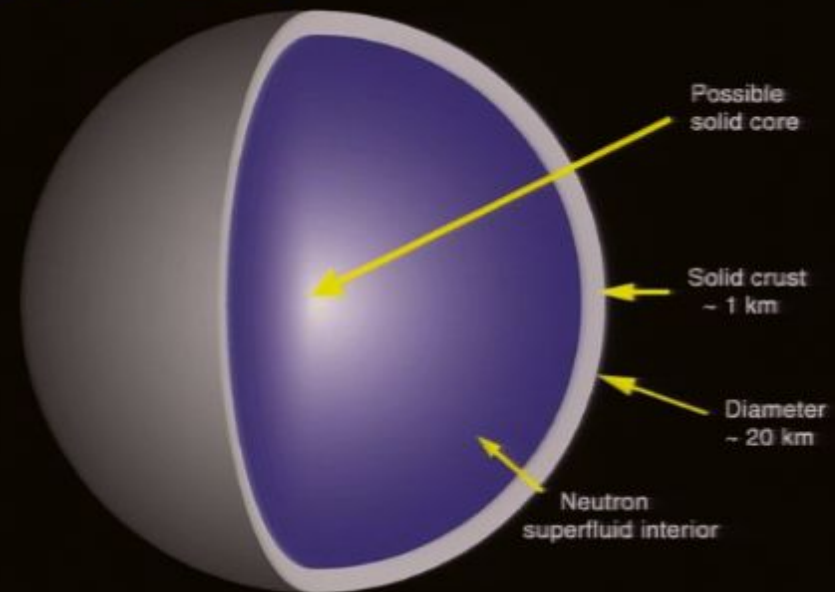
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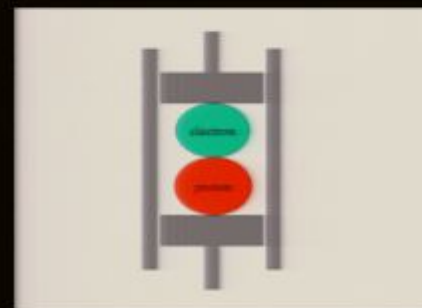
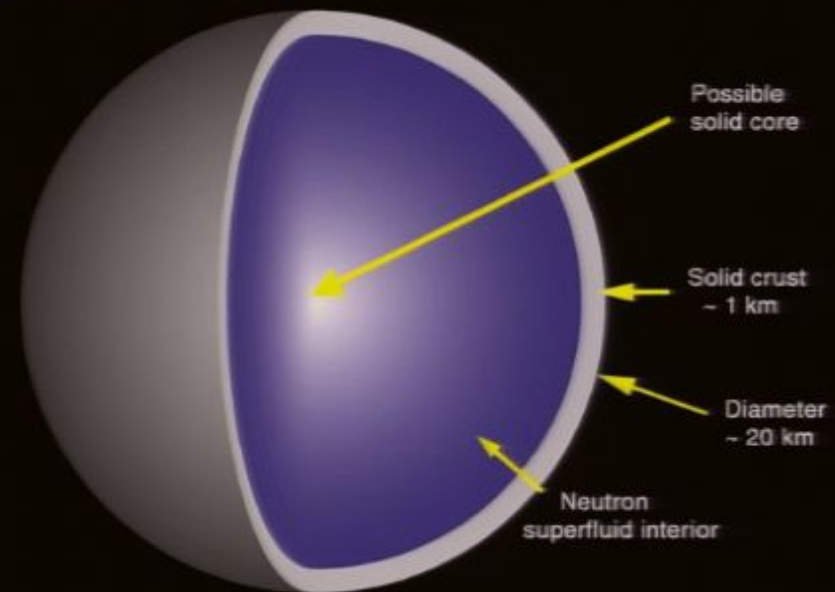
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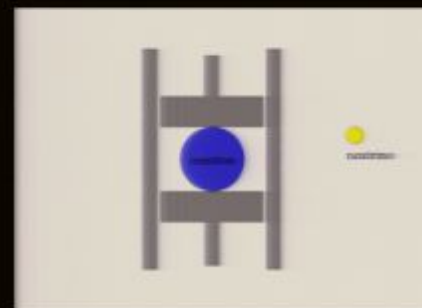
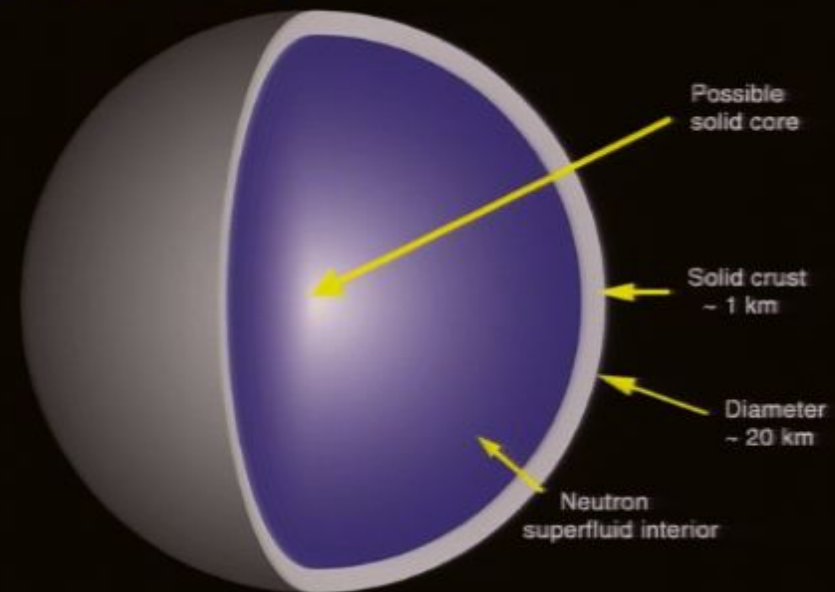
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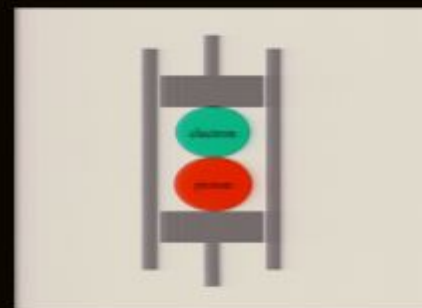
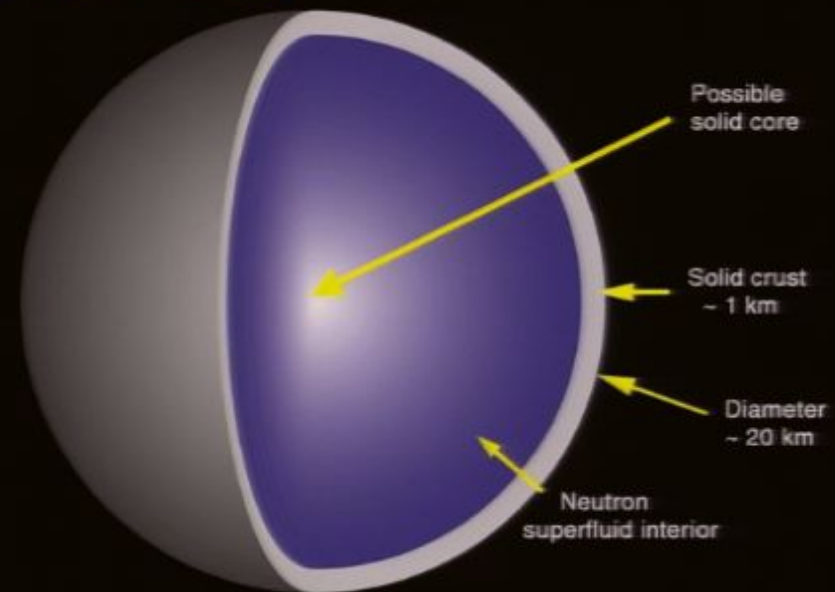
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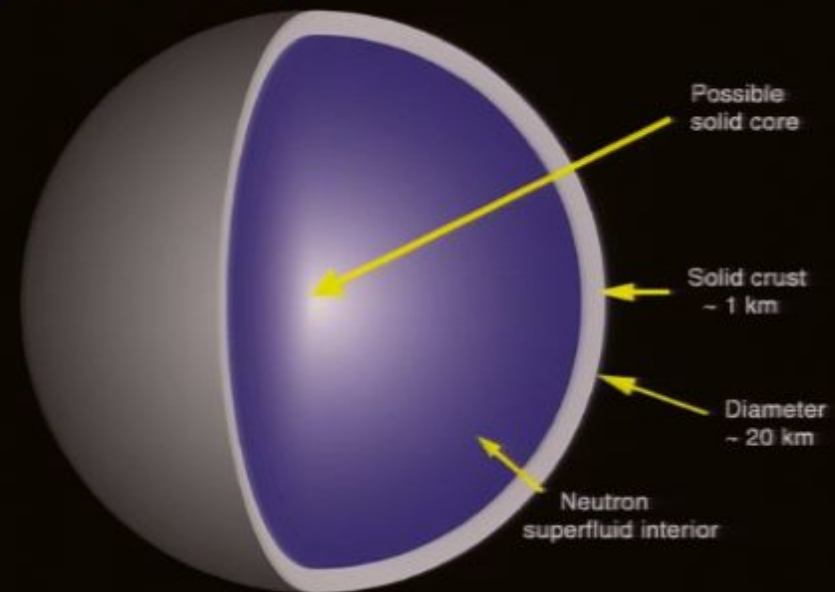
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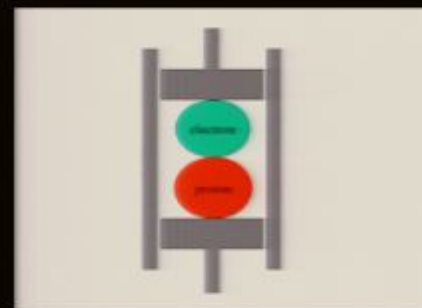
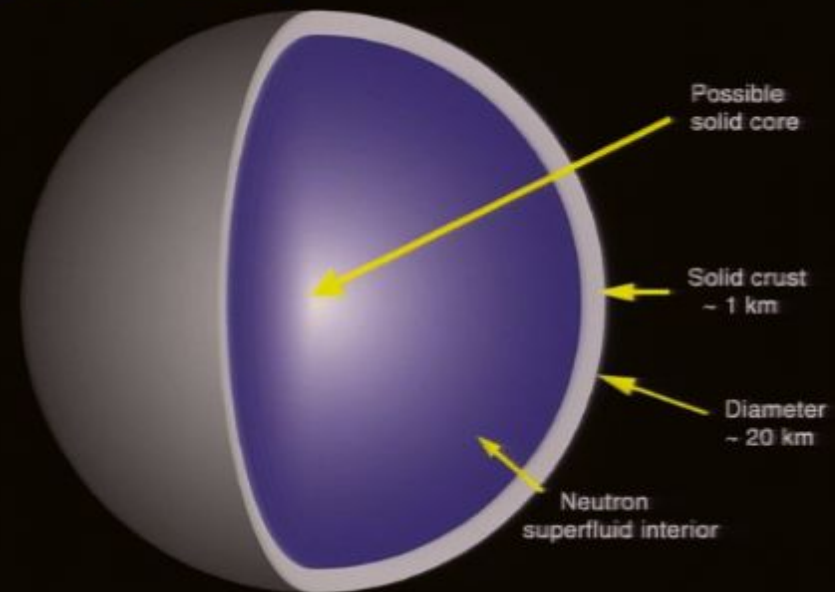
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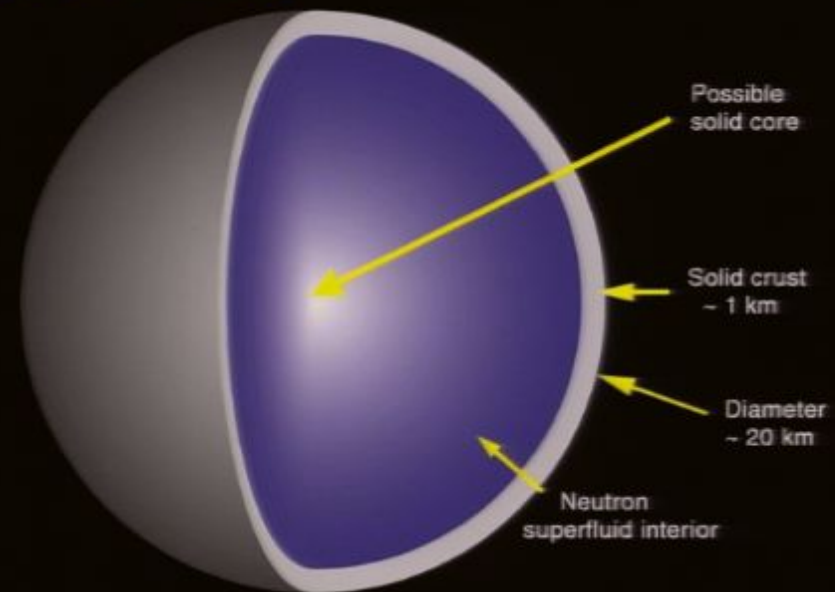
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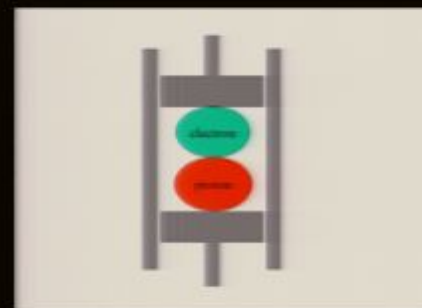
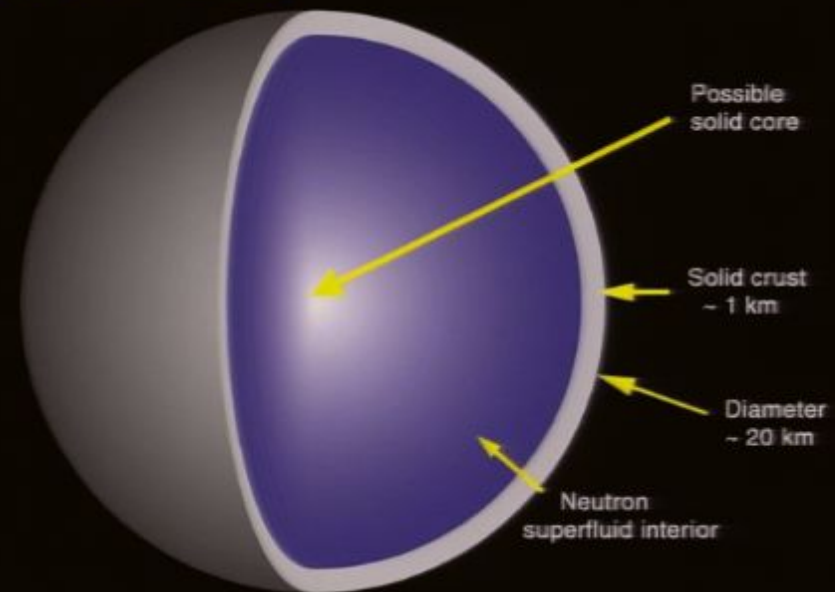
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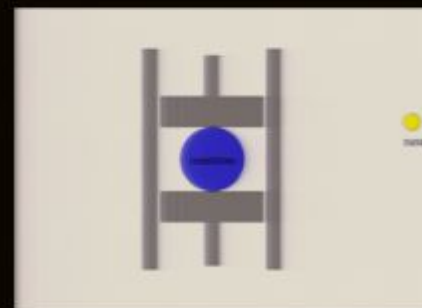
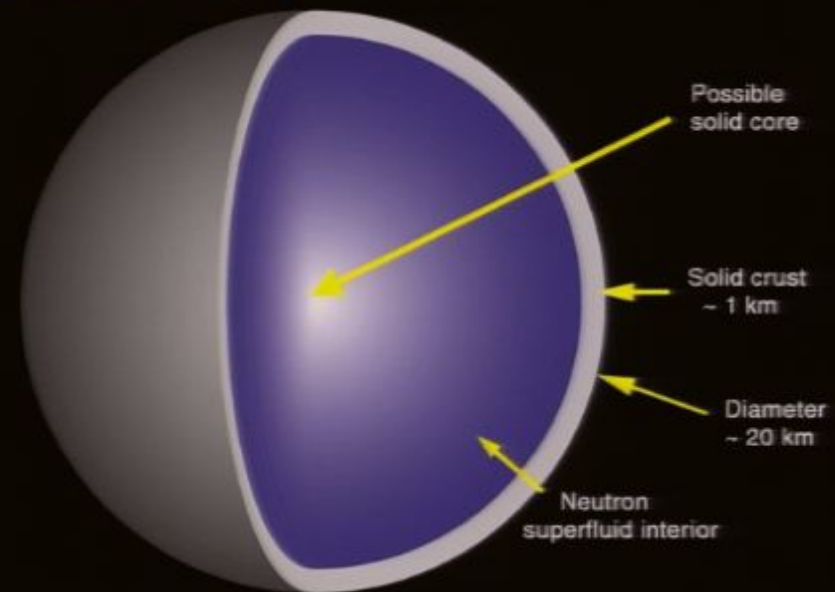
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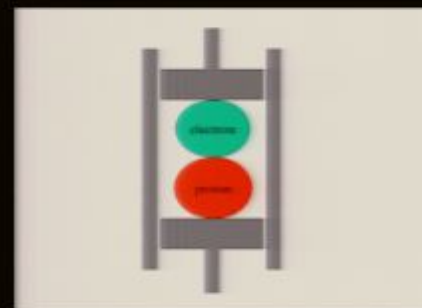
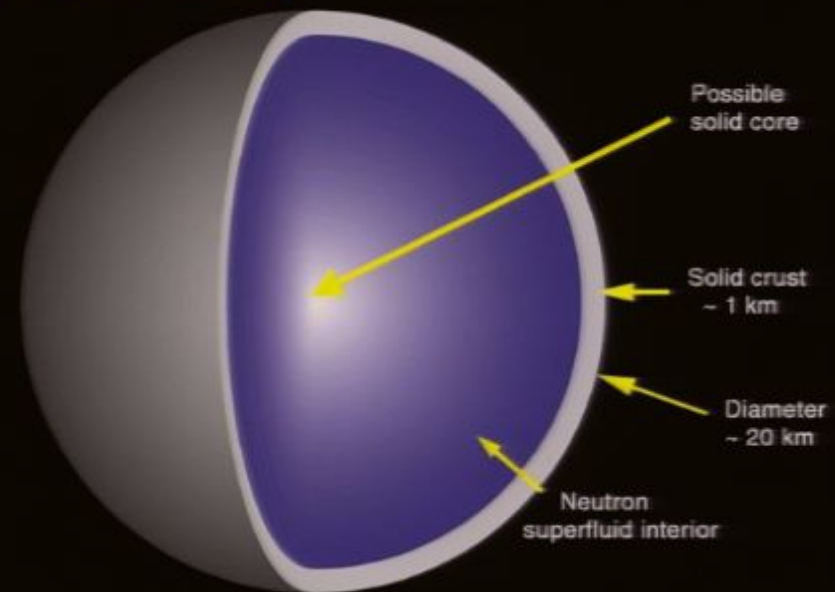
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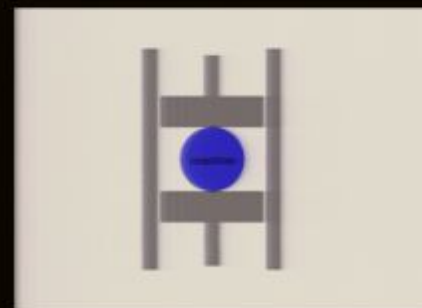
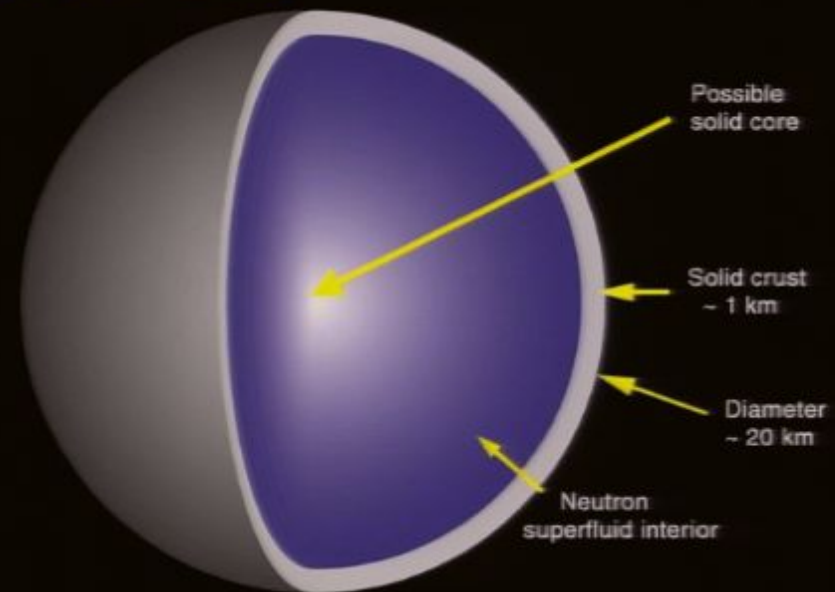
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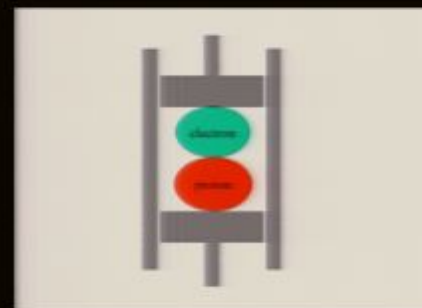
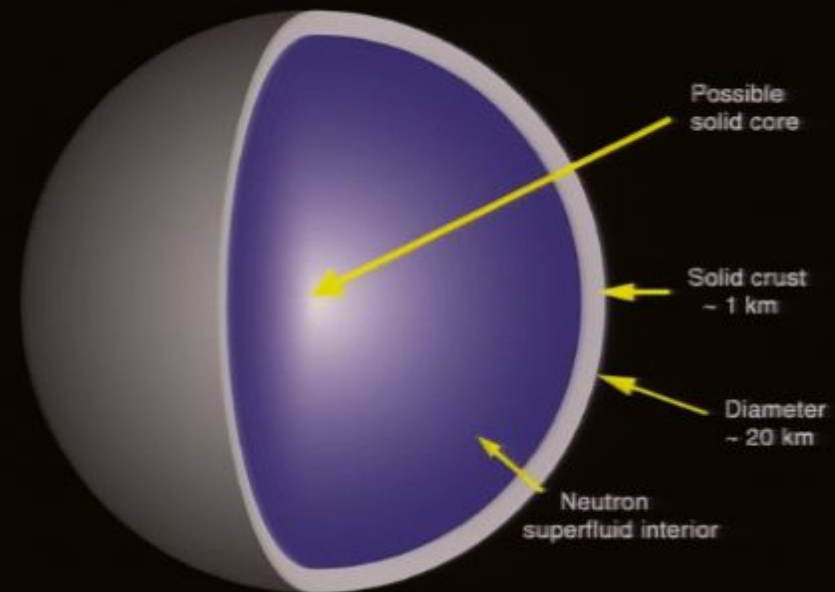
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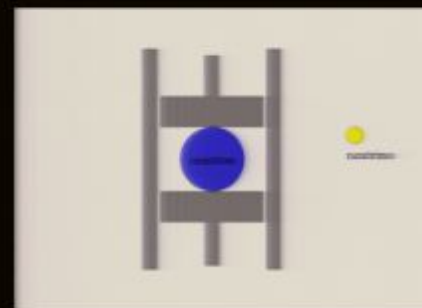
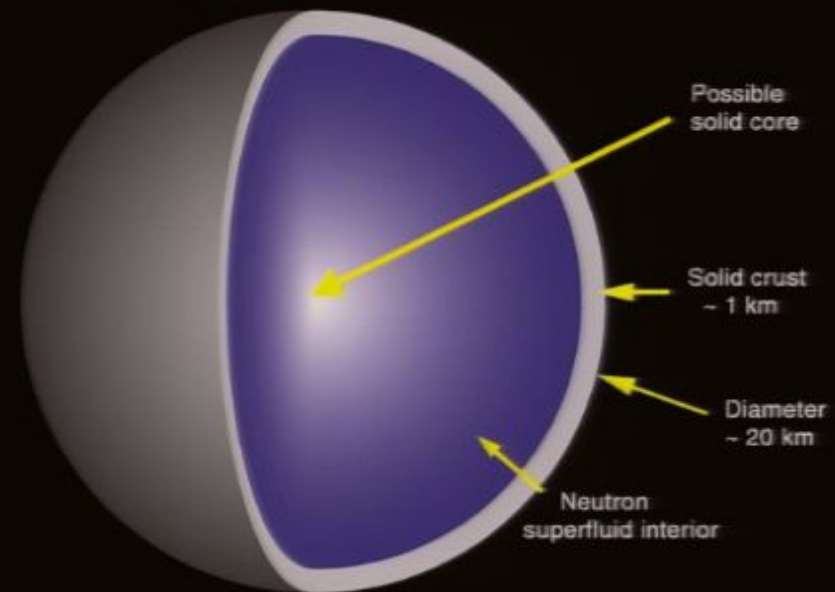
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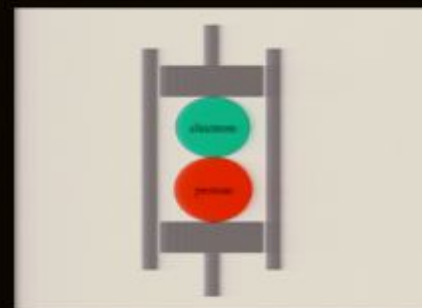
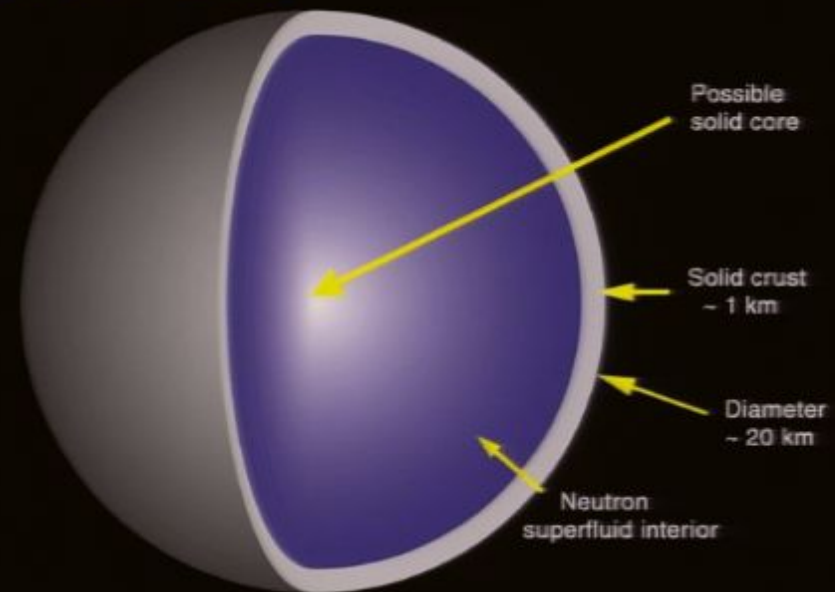
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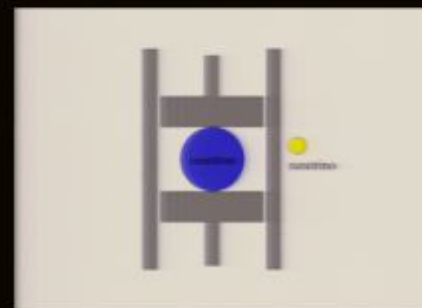
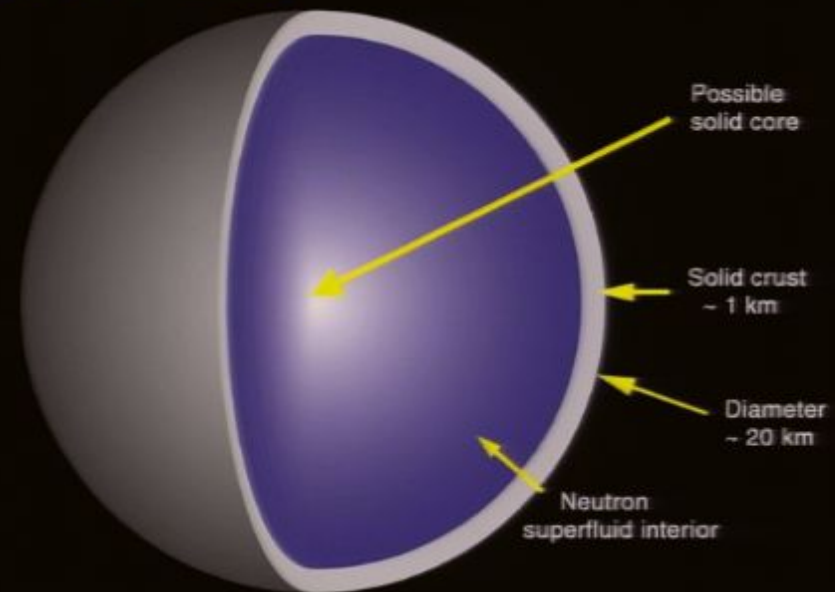
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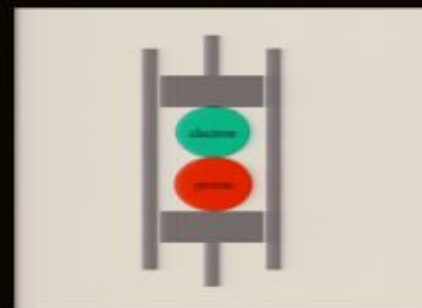
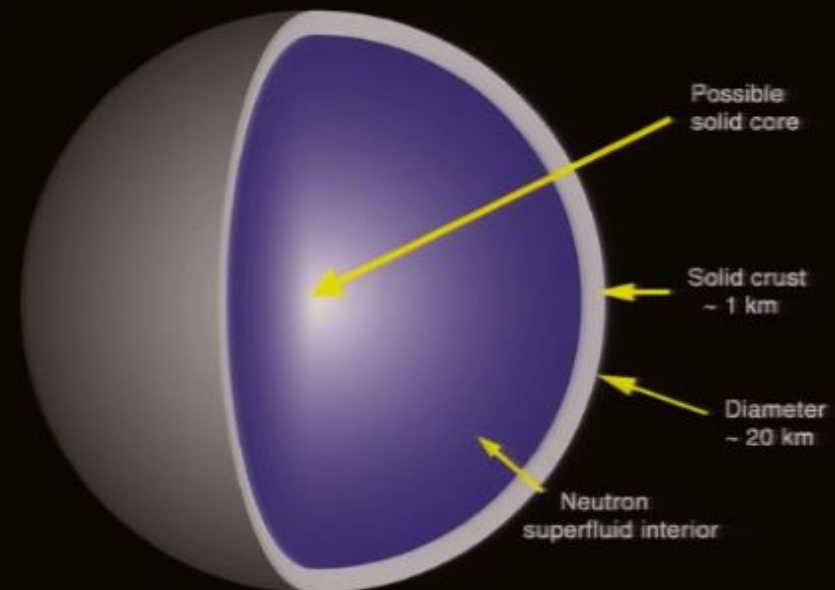
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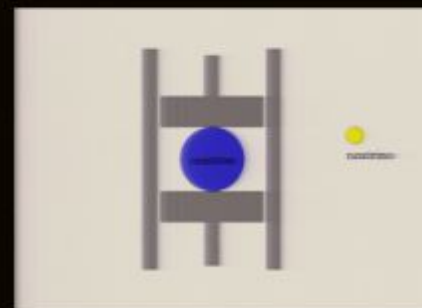
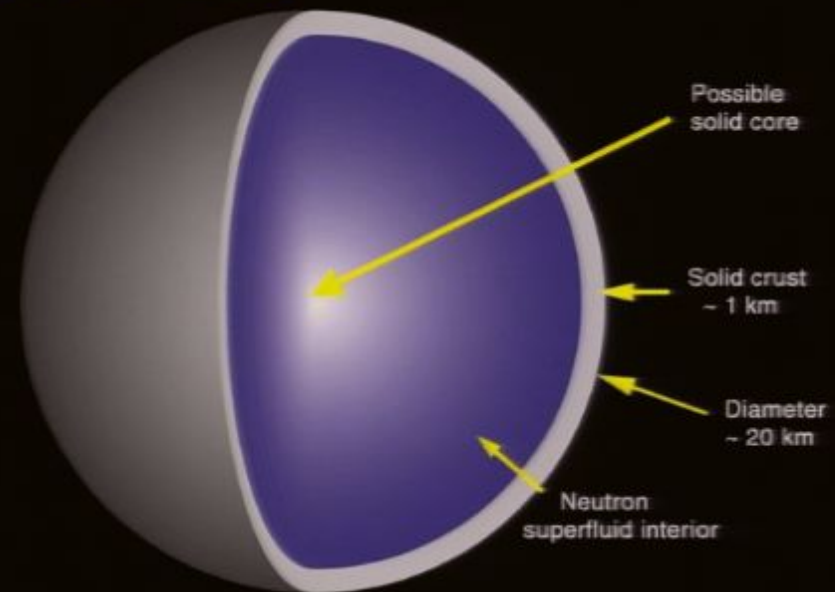
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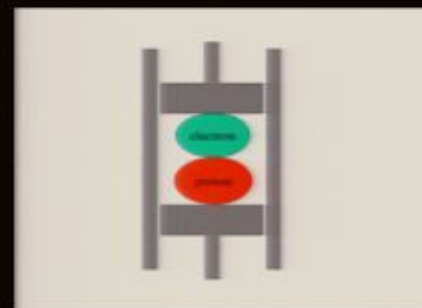
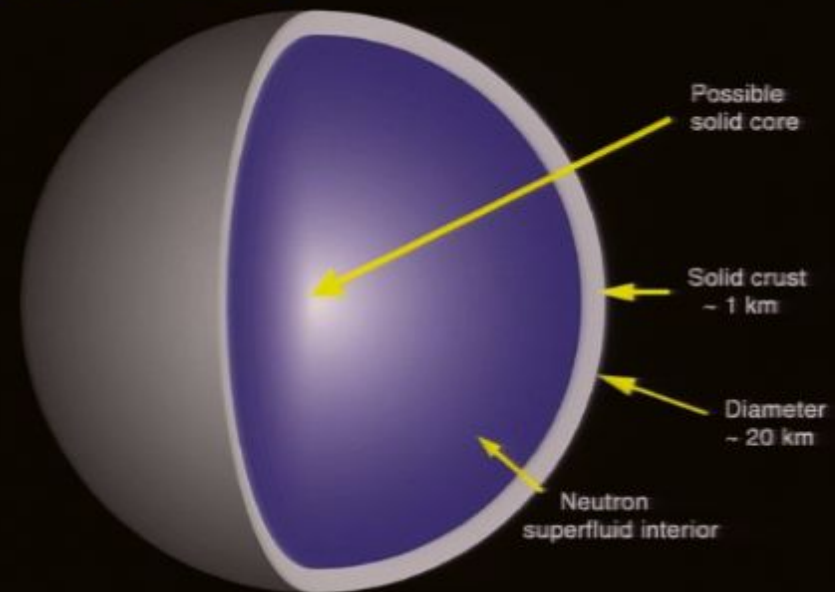
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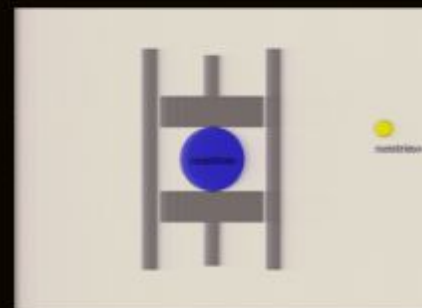
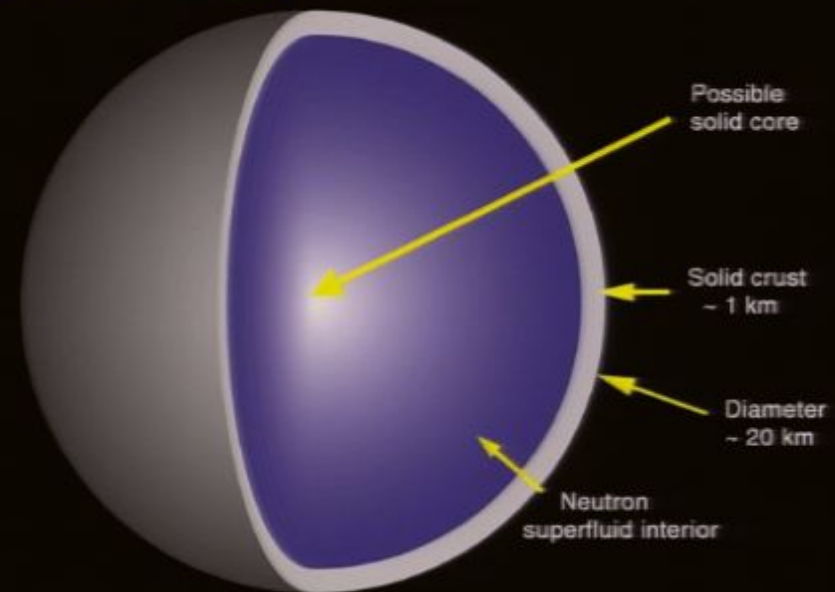
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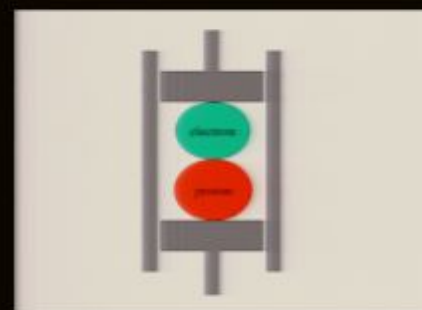
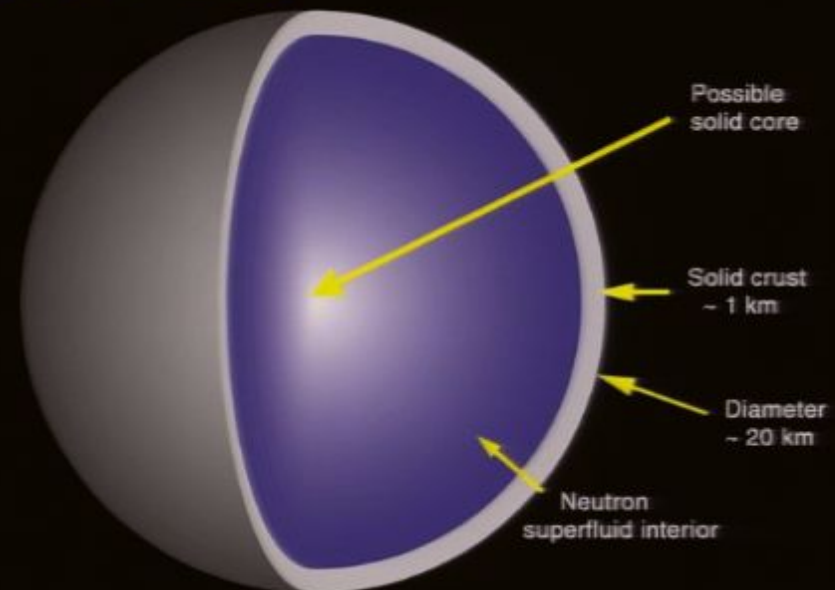
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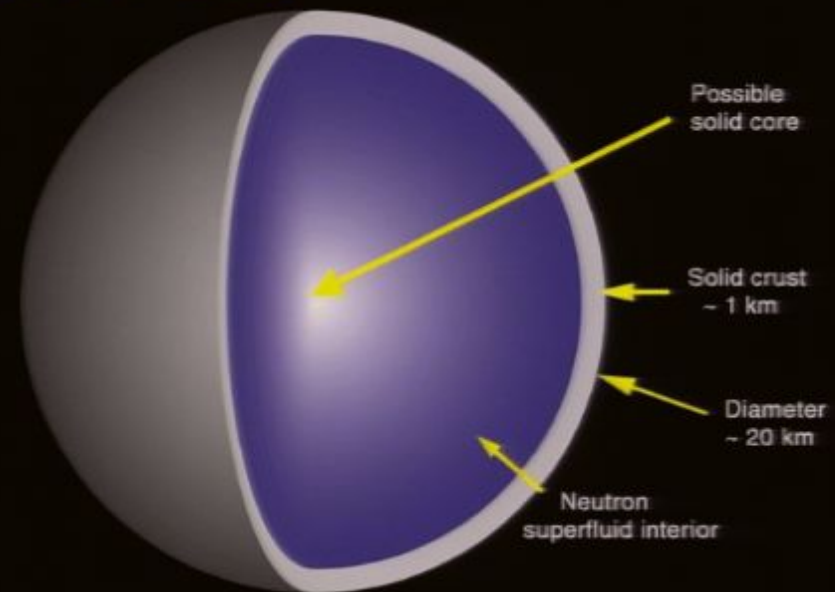
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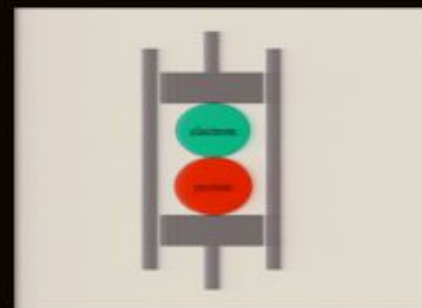
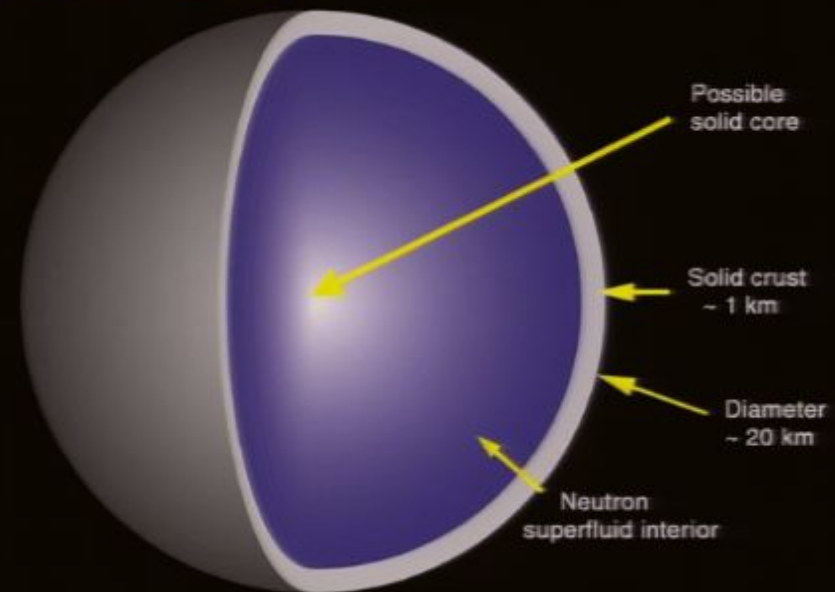
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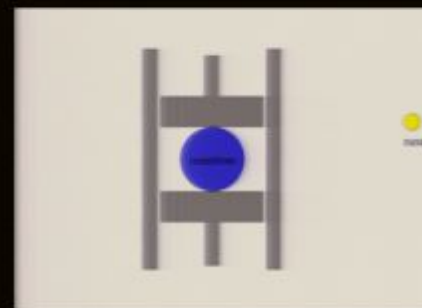
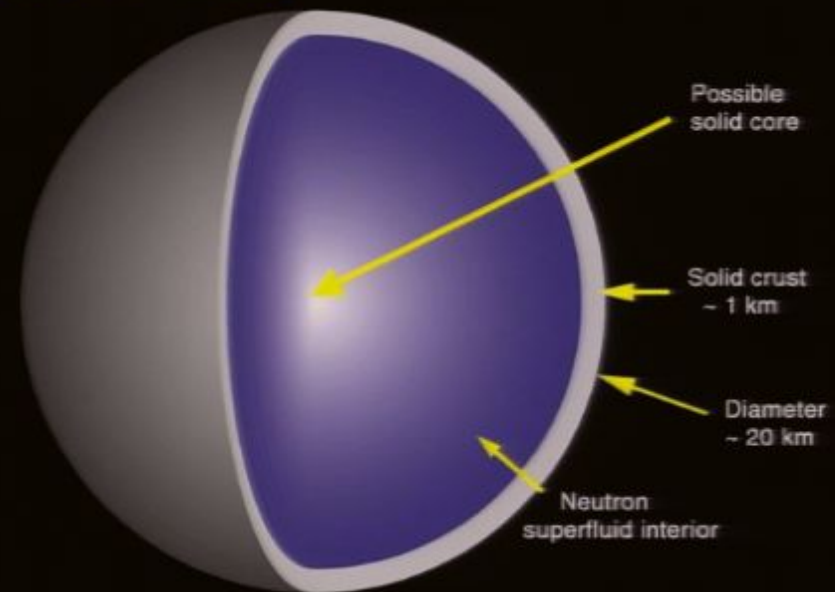
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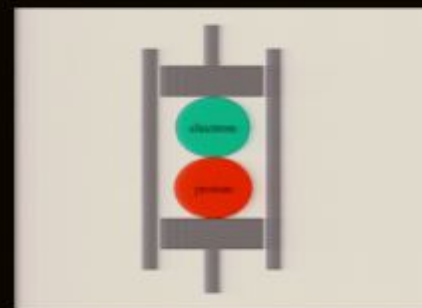
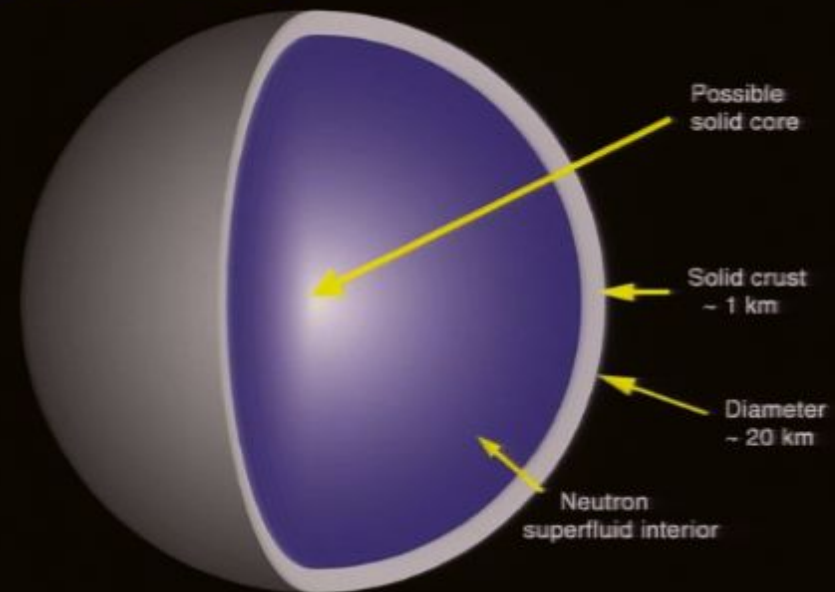
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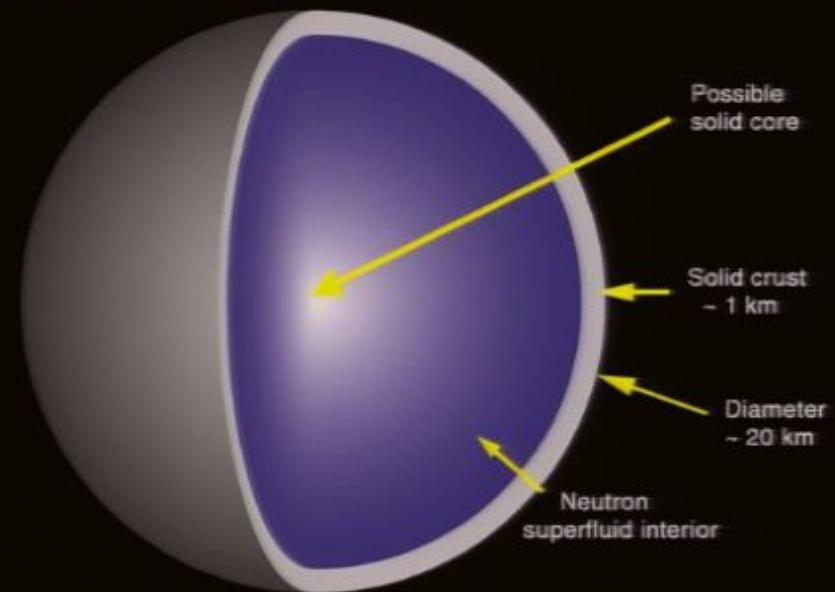
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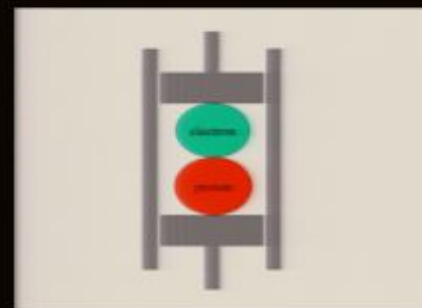
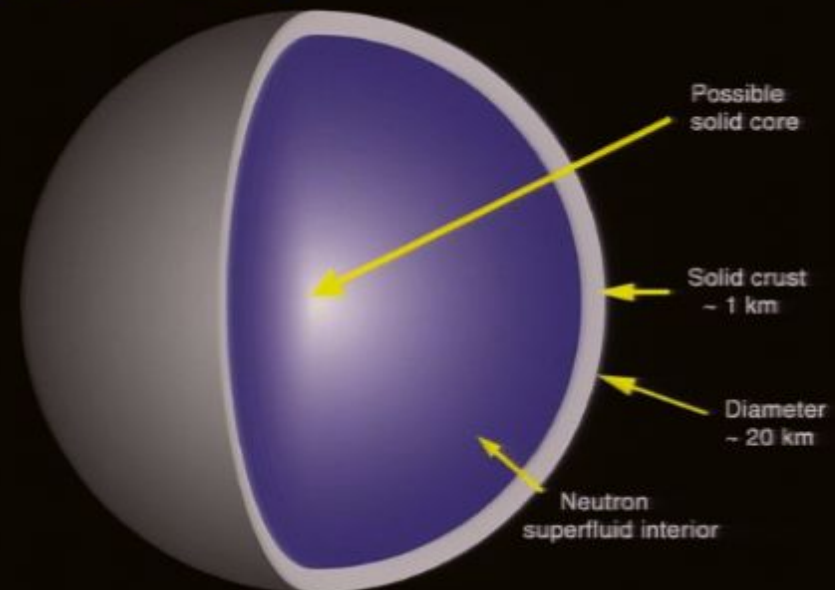
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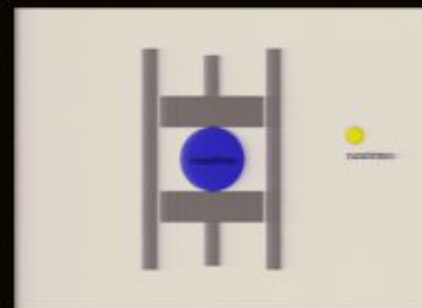
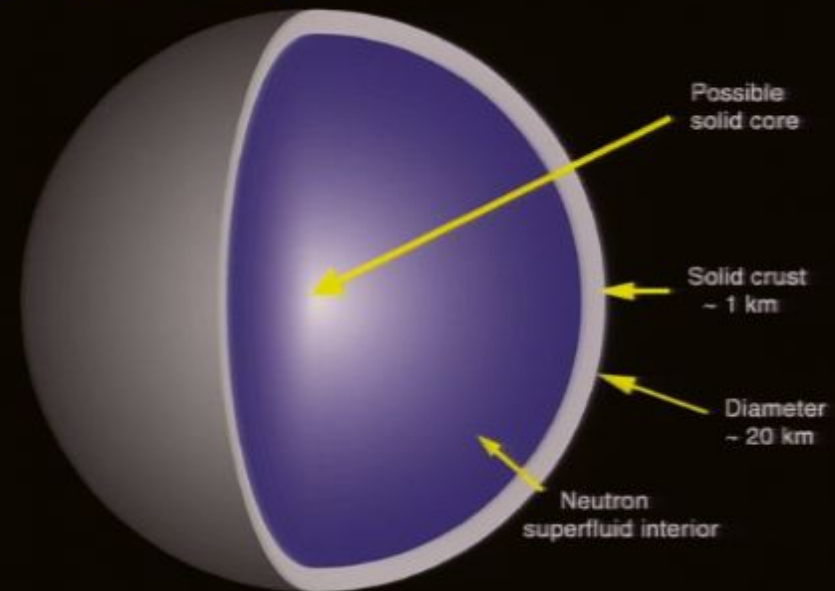
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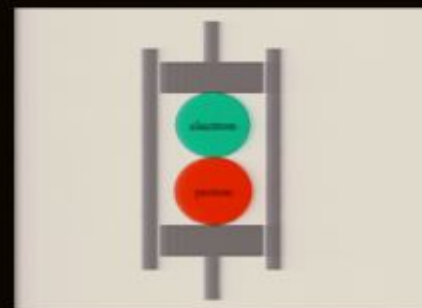
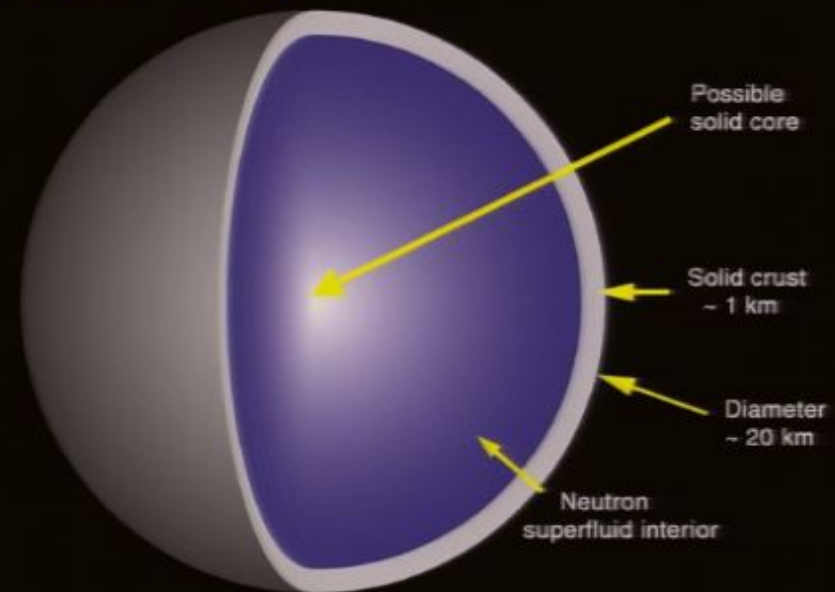
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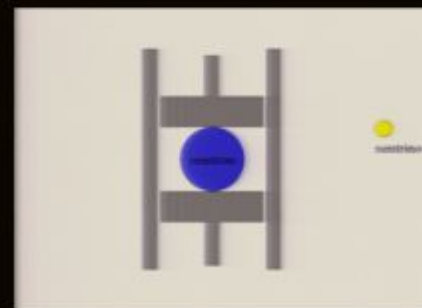
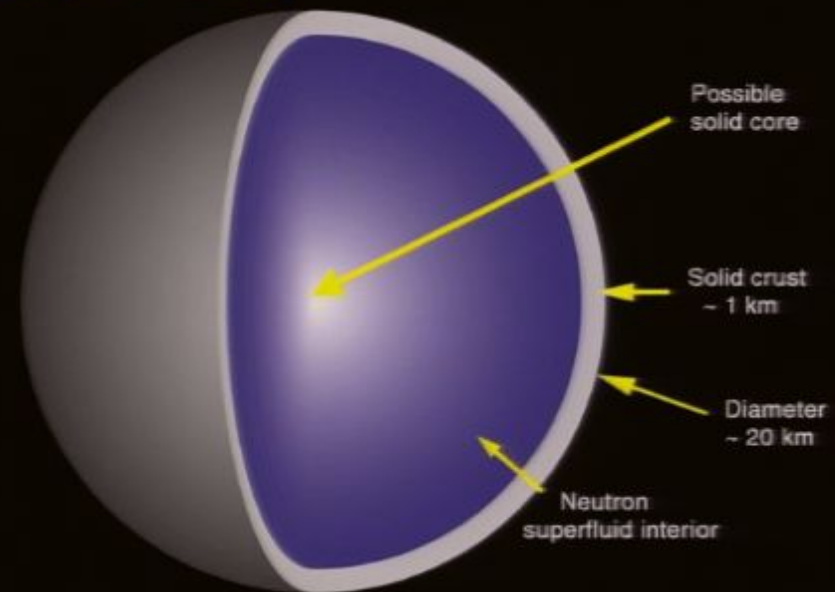
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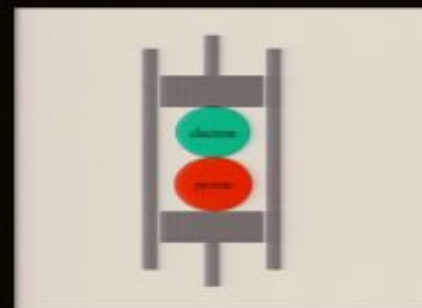
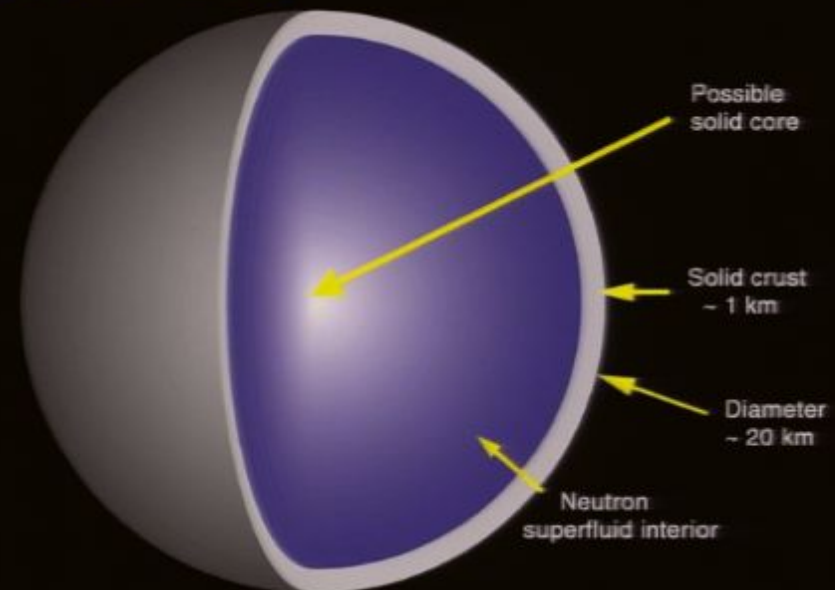
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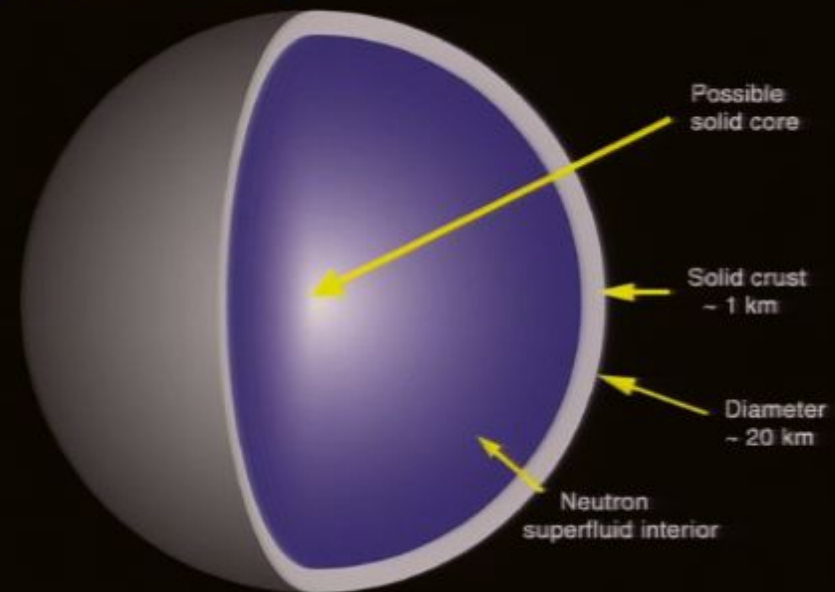
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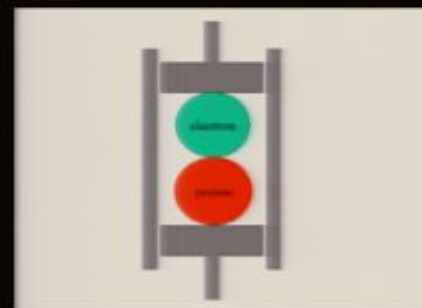
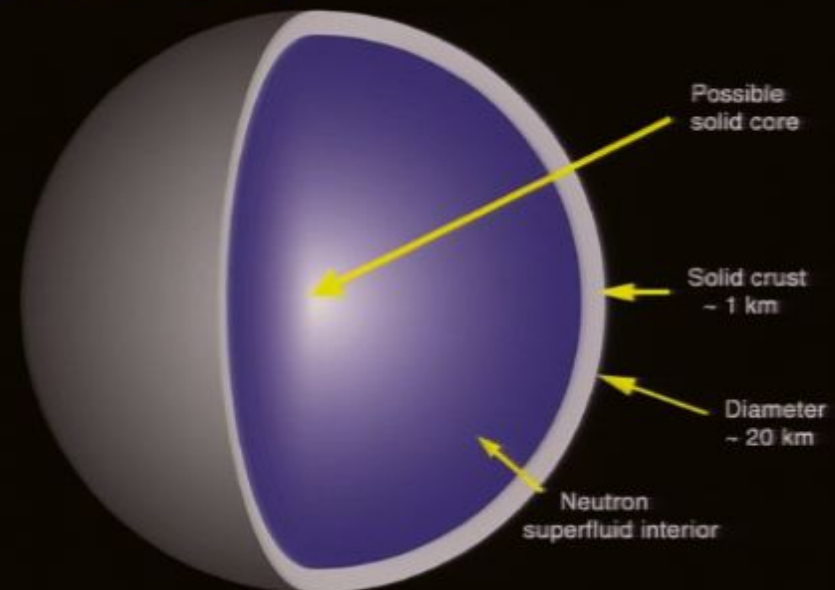
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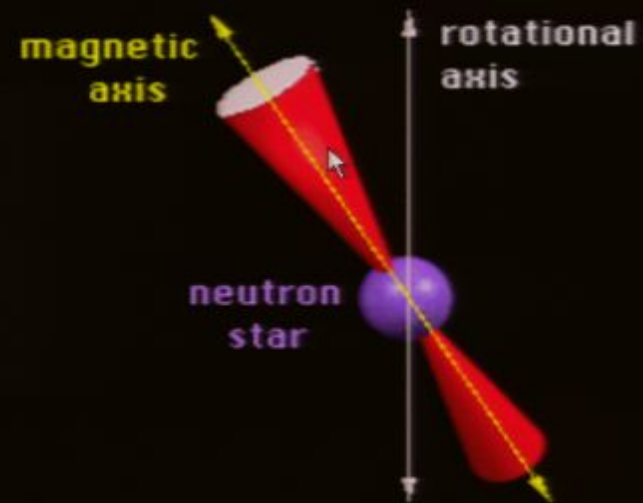
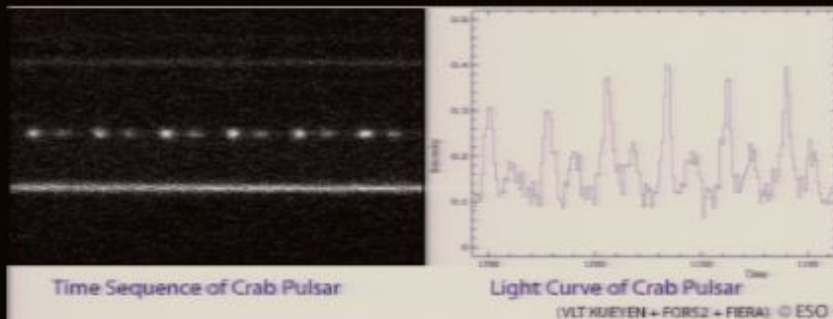


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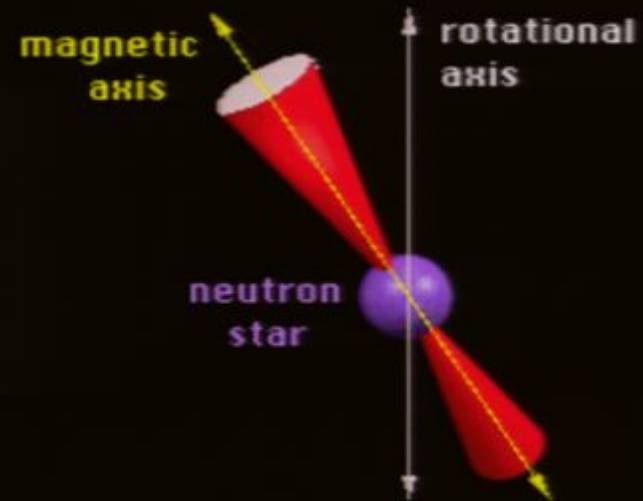
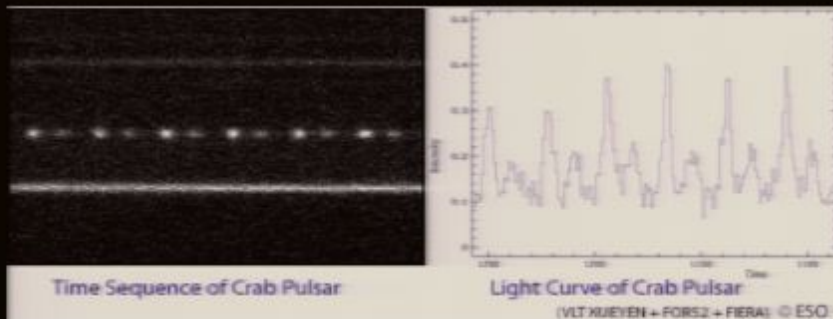


Pulsars



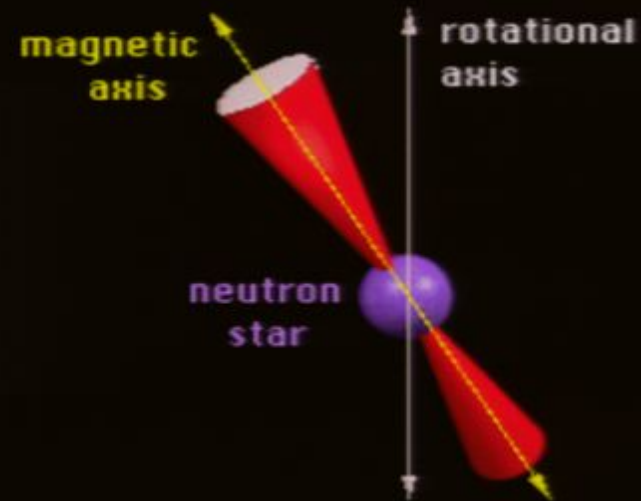
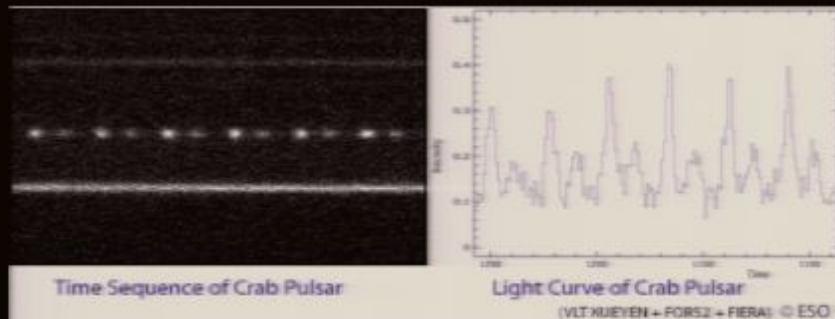
Pulsars

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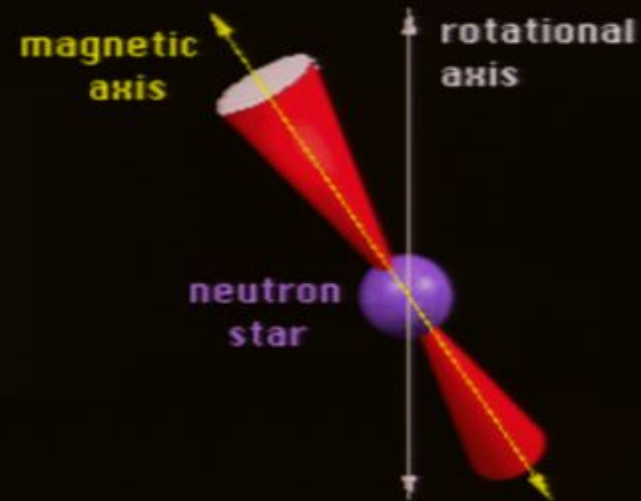
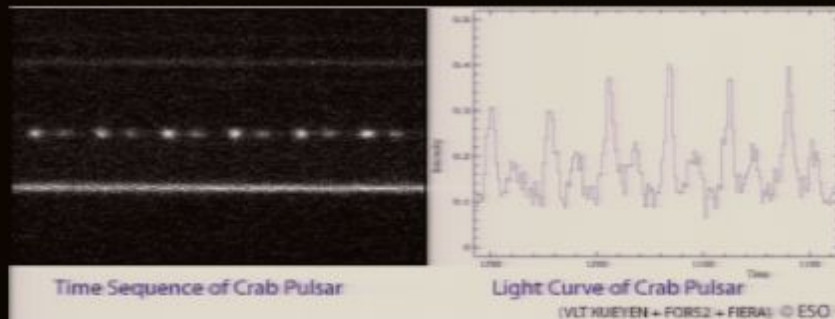
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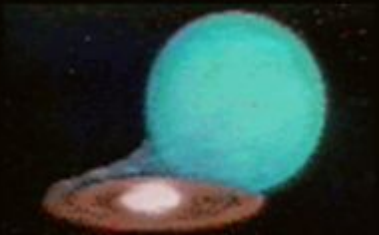
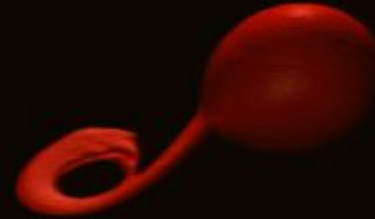
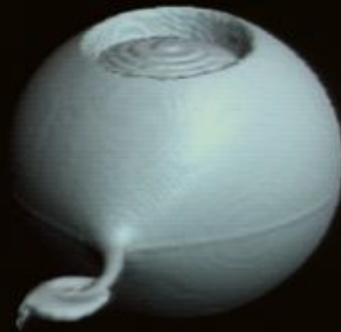
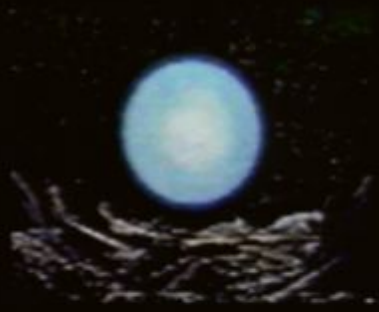


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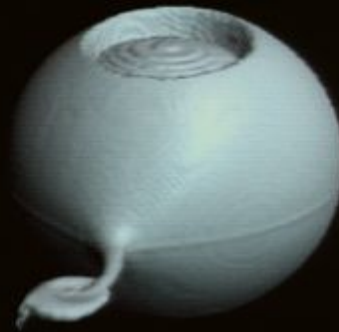
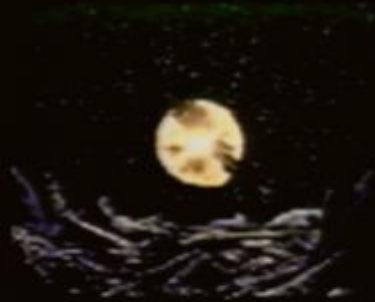
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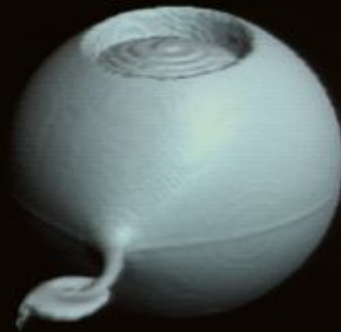
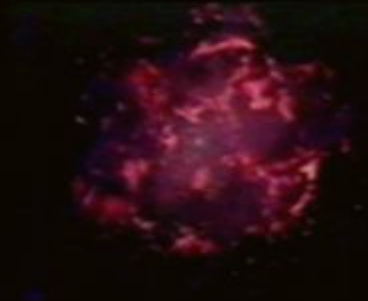
Supernova



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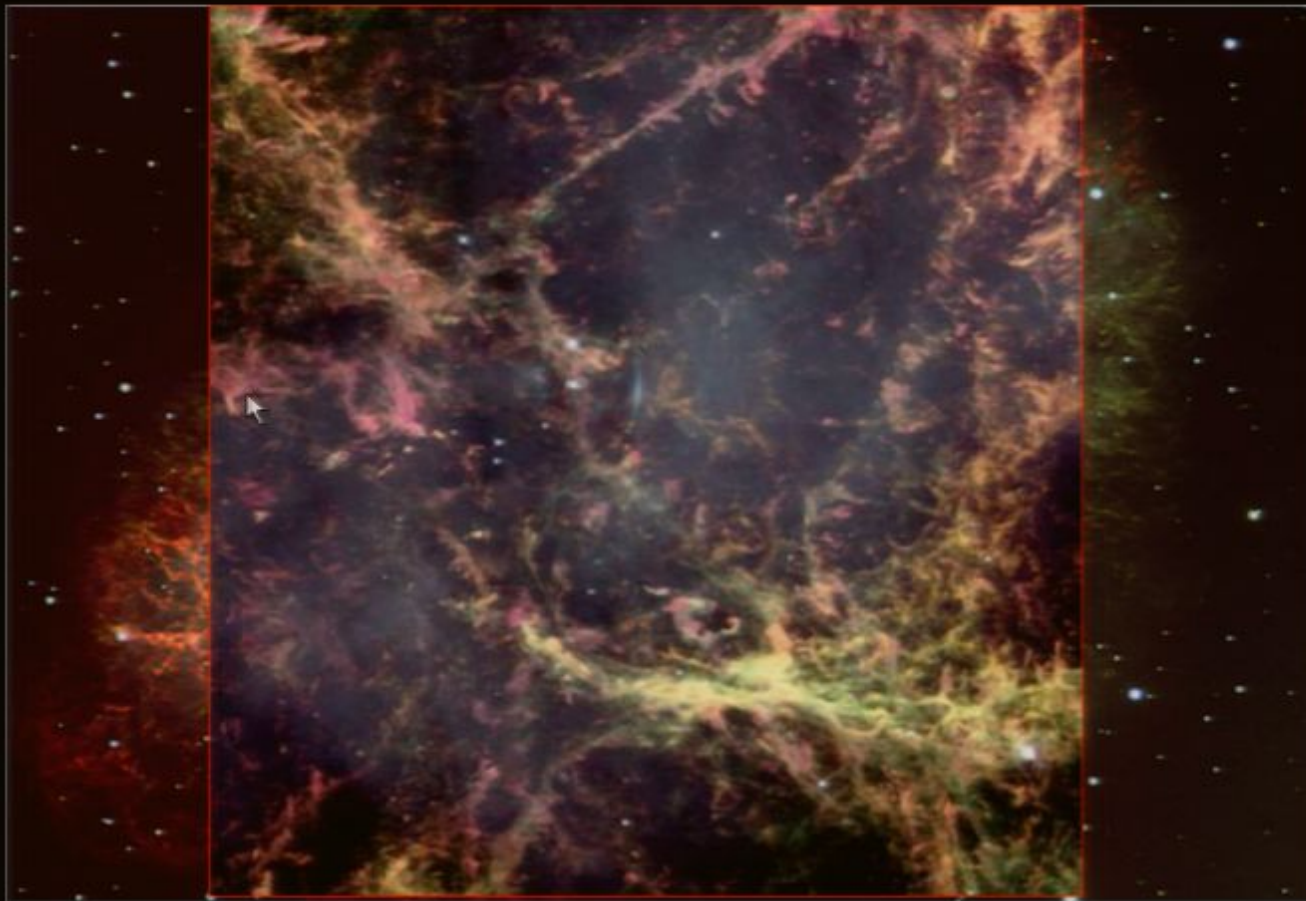
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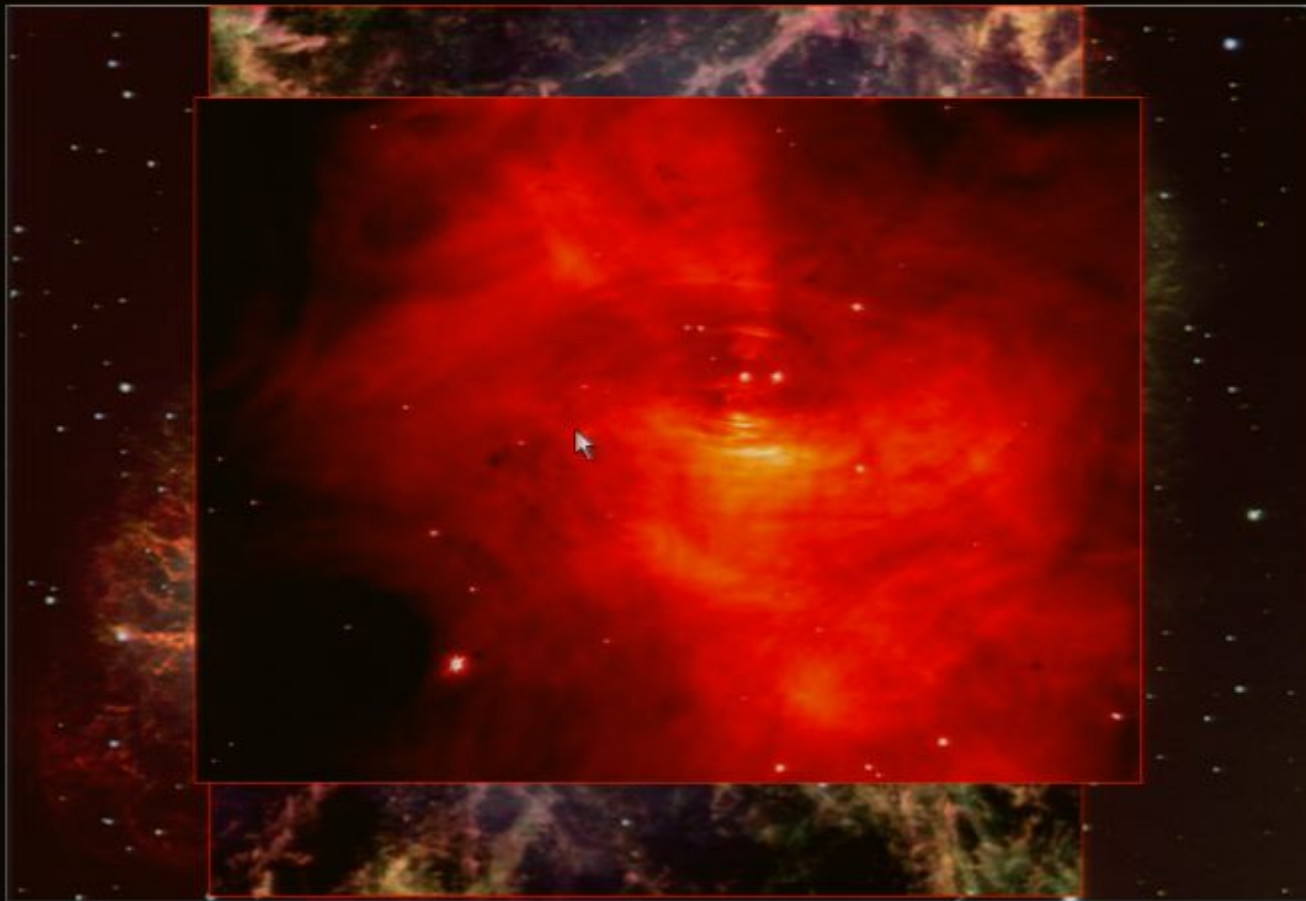
Crab Nebula Pulsar



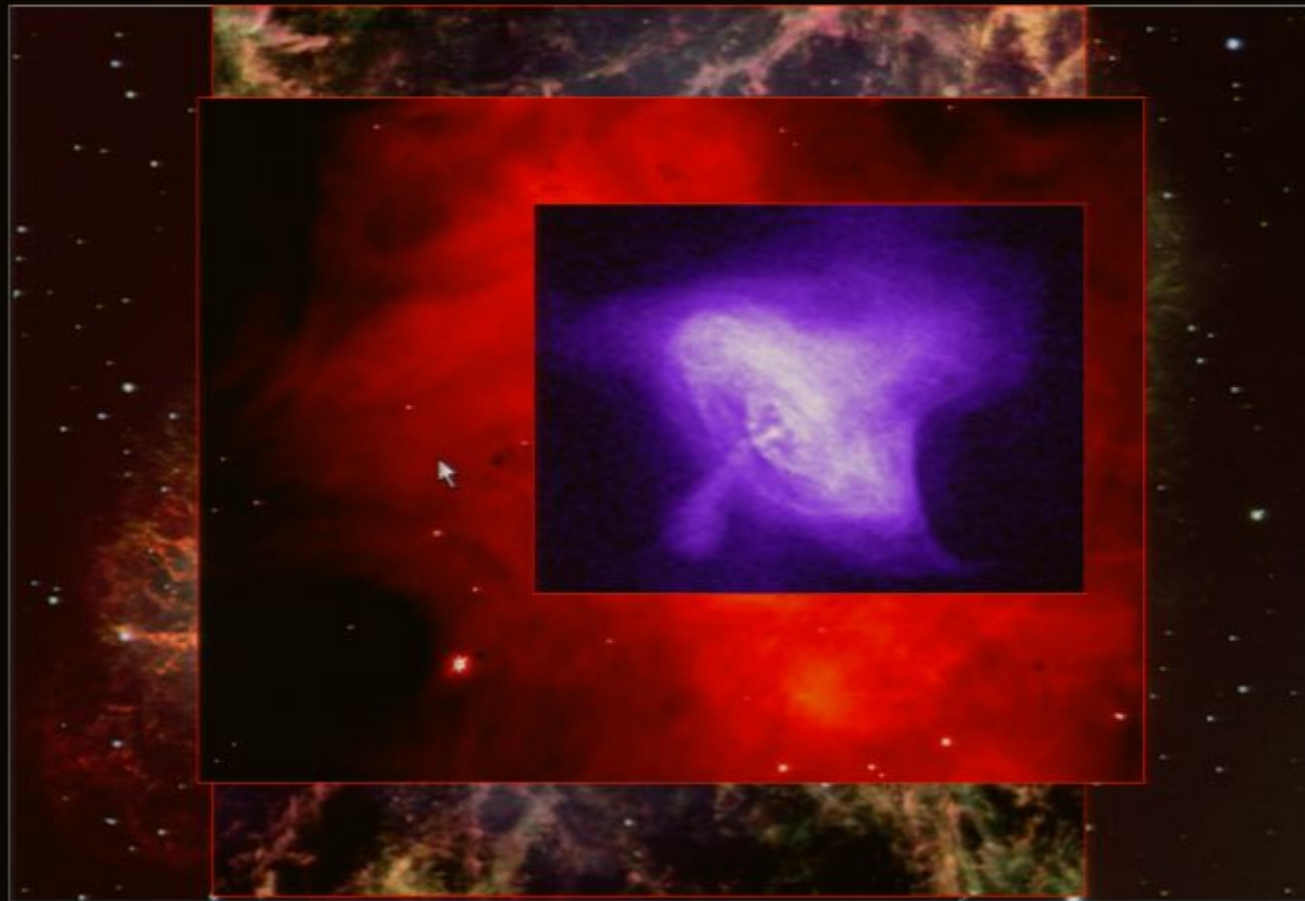
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Mass

- ◆ Low mass stars

- ◆ Less than $8 M_{\odot}$ on Main Sequence

- ◆ Become White Dwarf ($< 1.4 M_{\odot}$)

- ◆ Electron Degeneracy Pressure

- ◆ High Mass Stars

- ◆ Less than $40 M_{\odot}$ on Main Sequence

- ◆ Become Neutron Stars ($1.4 M_{\odot} < M < 3 M_{\odot}$)

- ◆ Neutron Degeneracy

What Next



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- What if the escape velocity is faster than light?

Black Hole

- The star collapses to form a Black Hole.

