

Title: Enrichment presentation on Black holes and the Global Positioning System (General Relativity) Continued

Date: Jul 08, 2006 10:35 AM

URL: <http://pirsa.org/06070018>

Abstract:

GPS and relativity

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$$\Delta t' = \gamma \Delta t_0$$

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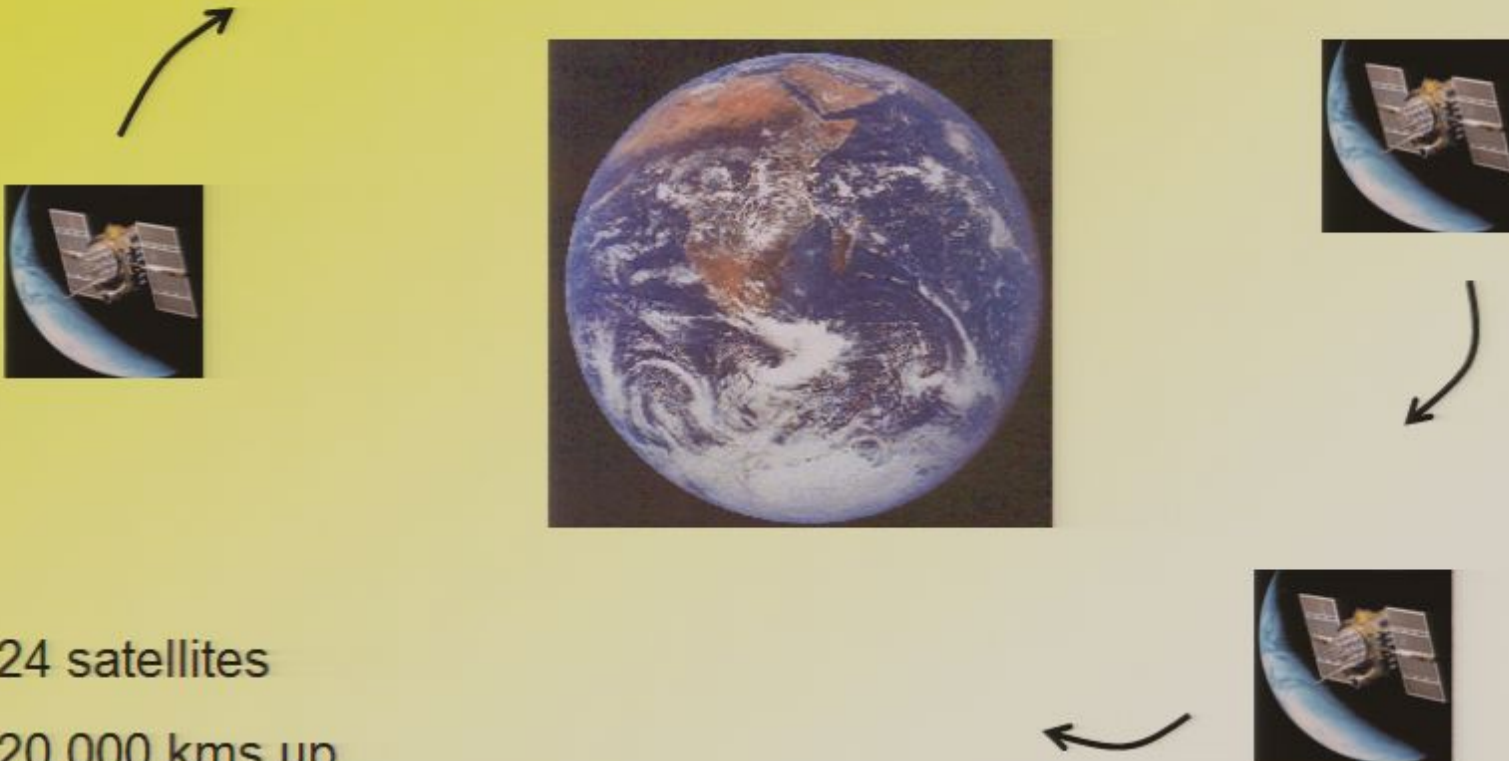
$$\Delta t' = \gamma \Delta t_0$$

Physica Phantastica tour

- Ottawa
- Manitoulin Island
- Sudbury
- Waterloo
- Toronto
- Dryden
- Fort Francis
- Rainy River



Global positioning system (GPS)



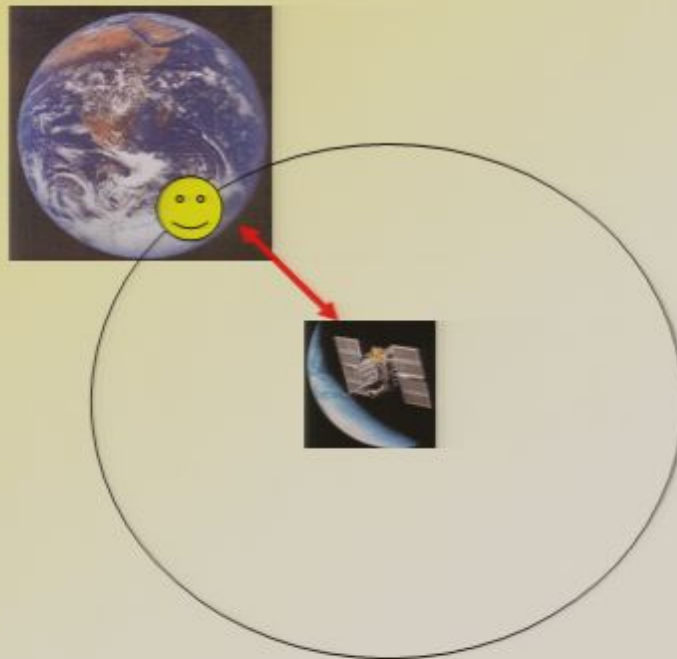
- 24 satellites
- 20,000 kms up
- radio waves

How does it work?

time how long it takes signal to travel from satellite to receiver

speed of radio waves = 300,000 km per second

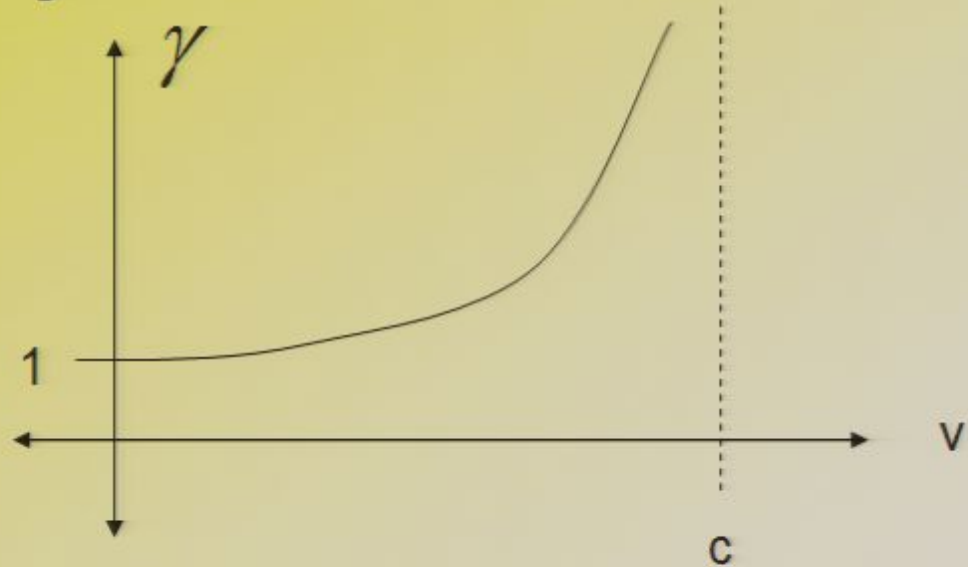
distance = speed x time



Relativity in the GPS

$$t = \gamma t_0$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$



If $v=4\text{km per second}$, what is γ (gamma)?

$$\gamma = 1 + \frac{v^2}{2c^2}$$

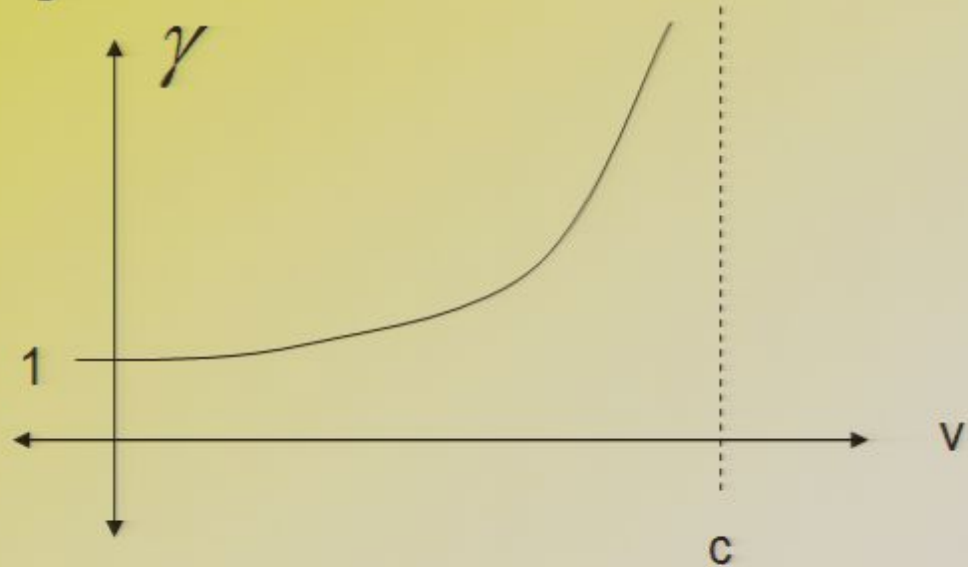
$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2} x^2 + \frac{n(n-1)(n-2)}{3!} x^3 + \dots$$

Calculate $\frac{v^2}{2c^2}$

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$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \left(1 - \frac{v^2}{c^2}\right)^{-\frac{1}{2}}$$

$$n = \frac{c}{v}$$

$$\alpha = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \left(1 - \frac{v^2}{c^2} \right)^{-\frac{1}{2}}$$

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$n = -\frac{1}{2}$
 $x = v$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \left(1 - \frac{v^2}{c^2}\right)^{-\frac{1}{2}}$$

$$n = \dots$$

$$x = v \dots$$

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$$n =$$

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$$n = -\frac{1}{2}$$

$$x = \frac{v^2}{c^2}$$

$$\therefore 1 + nx$$

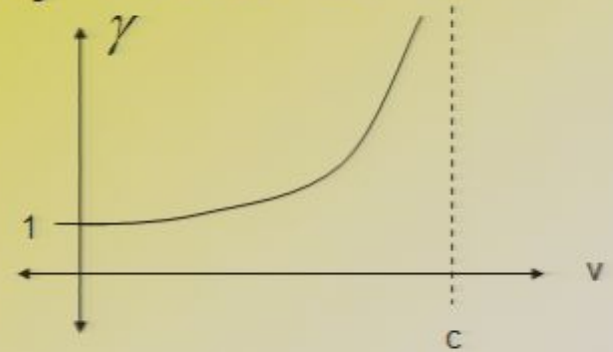
$$= 1 + \left(-\frac{1}{2}\right) \left(\frac{v^2}{c^2}\right)$$

$$= 1 - \frac{v^2}{2c^2}$$

Relativity in the GPS

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Calculate $\frac{v^2}{2c^2}$

$$8.89 \times 10^{-11}$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \left(1 + n \frac{v^2}{c^2}\right)^{-\frac{1}{2}}$$

4 km s^{-1}
 $3 \times 10^8 \text{ ms}^{-1}$
 $\frac{4}{3 \times 10^8}$

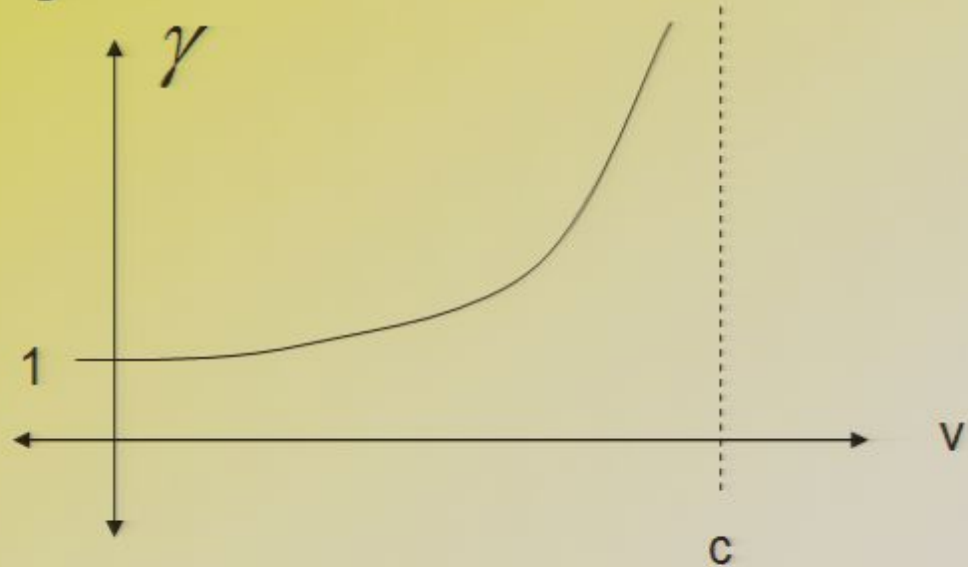
$n = -\frac{1}{2}$
 $x = \frac{v^2}{c^2}$

$$\begin{aligned} \therefore 1 + nx &= 1 + \left(-\frac{1}{2}\right) \left(\frac{v^2}{c^2}\right) \\ &= 1 + \frac{v^2}{2c^2} \end{aligned}$$

Relativity in the GPS

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$$8.89 \times 10^{-11}$$

Satellite clocks slow by around 10^{-10} seconds each second.

- corresponds to what distance error?
 - a) 3 cm
 - b) 3 m
 - c) 3 mm
-
- Errors accumulate.

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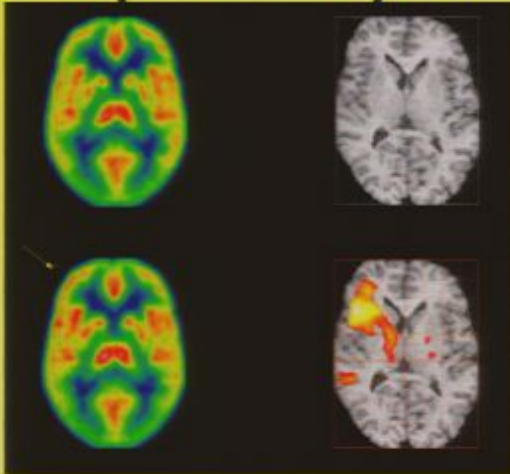
- corresponds to what distance error?
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-
- Errors accumulate.
3cm x 24 hours x 3600 seconds =

Gravity slows down time



Time slightly quicker ---
 10^{-10} sec. per second

Positron Emission Tomography (PET): Einstein in the hospital



cancer detection, brain research

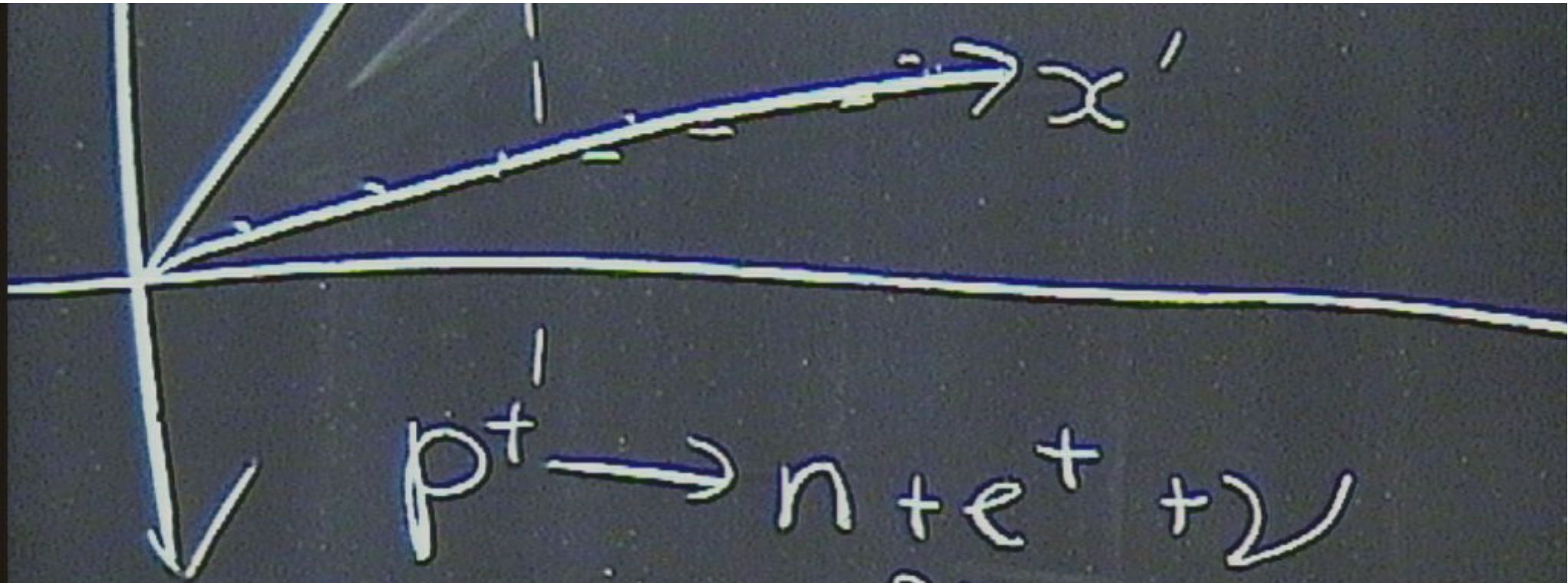
quantum physics & special relativity

antimatter!

$$E=mc^2$$

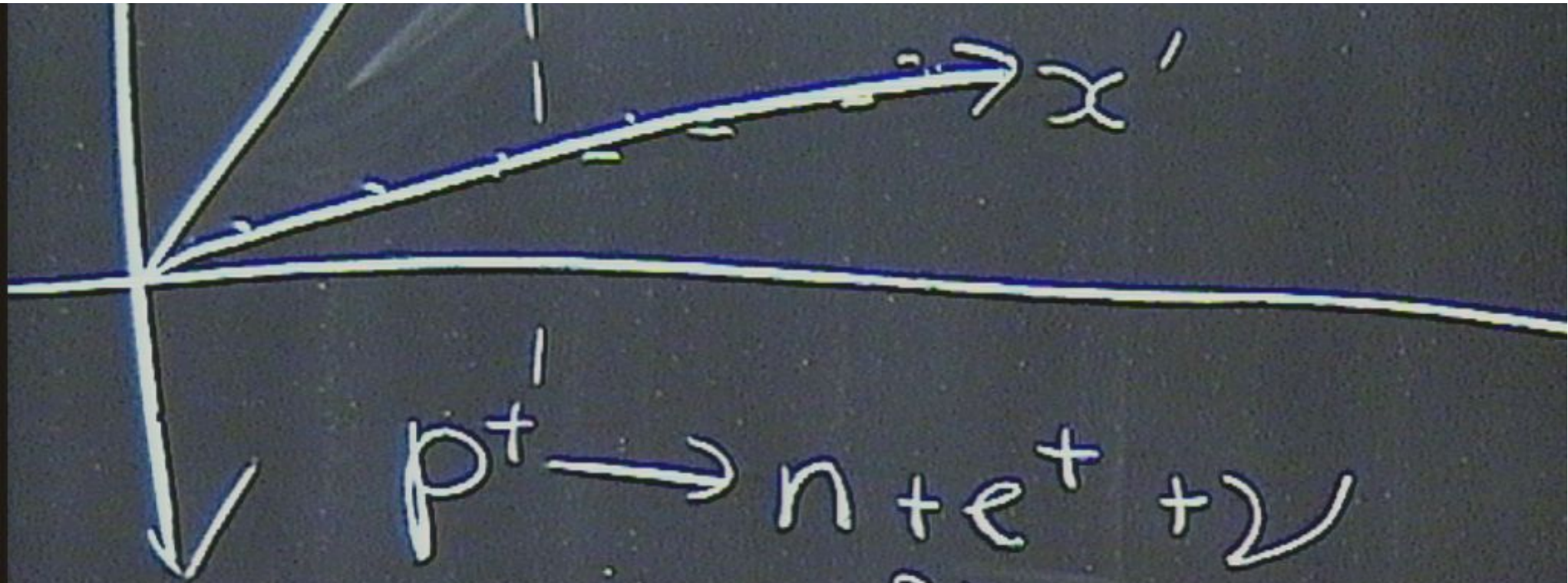
$$m_{\text{electron}} = m_{\text{positron}} = 9.11 \times 10^{-31} \text{ kg}$$

\therefore



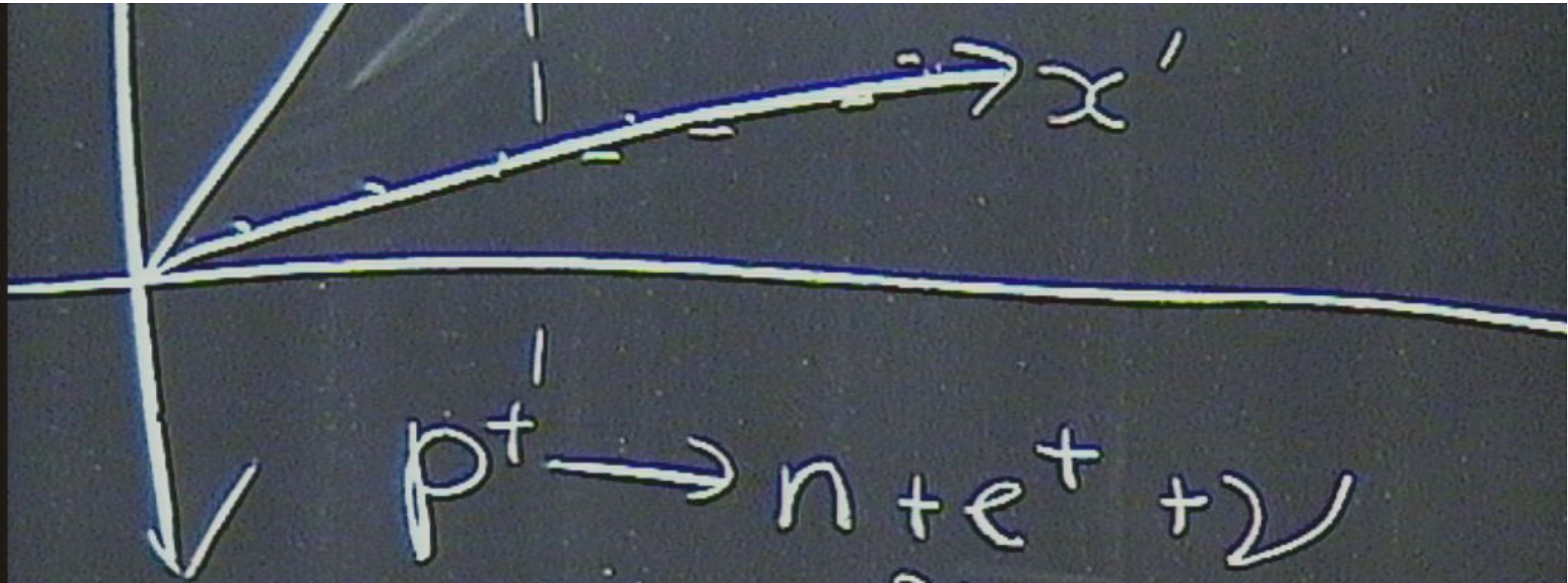
$p^t \rightarrow n + e^t + 2$
 POSITION

$$\left(\frac{x = \sqrt{-1}}{2} \right) = 1 + \left(-\frac{1}{2} \right) \left(\frac{-\sqrt{-1}}{2} \right)$$



$p^+ \rightarrow n + e^+ + 2$
 POSITION

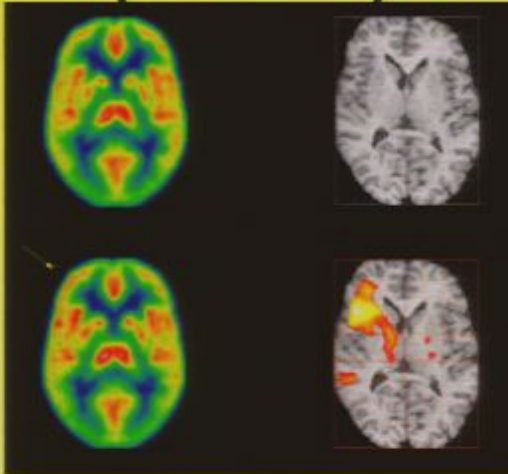
$$\left(\frac{\sqrt{2}}{2} \right) = 1 + \left(-\frac{1}{2} \right) \left(\frac{-\sqrt{2}}{2} \right)$$



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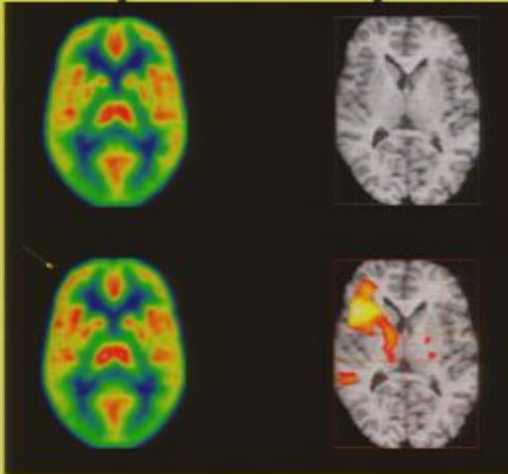
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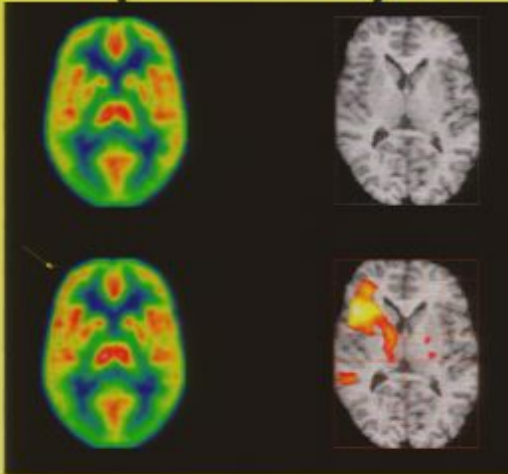
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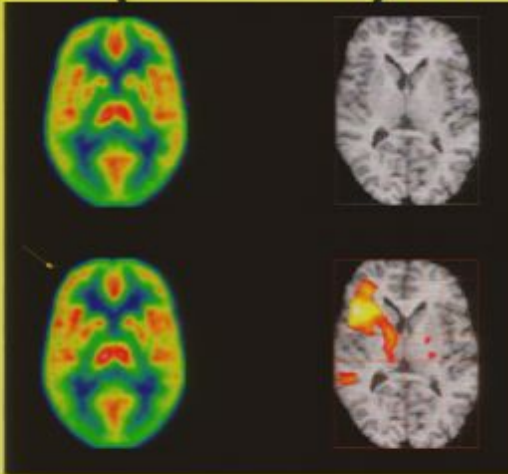
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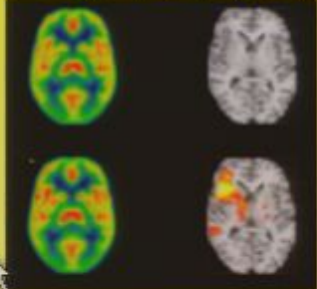
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