

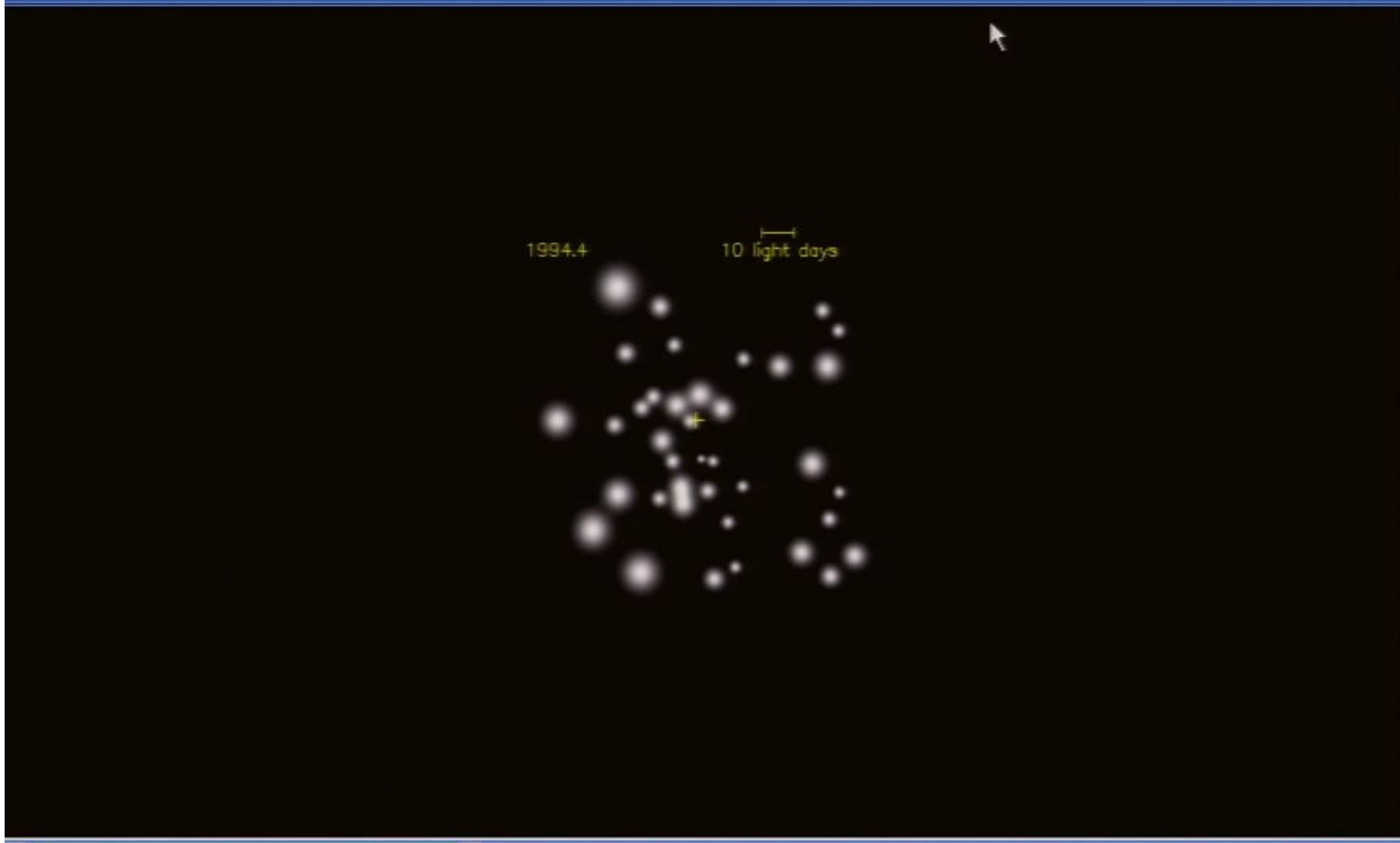
Title: Enrichment Presentation on Special Relativity

Date: Jul 07, 2006 09:00 AM

URL: <http://pirsa.org/06070011>

Abstract:

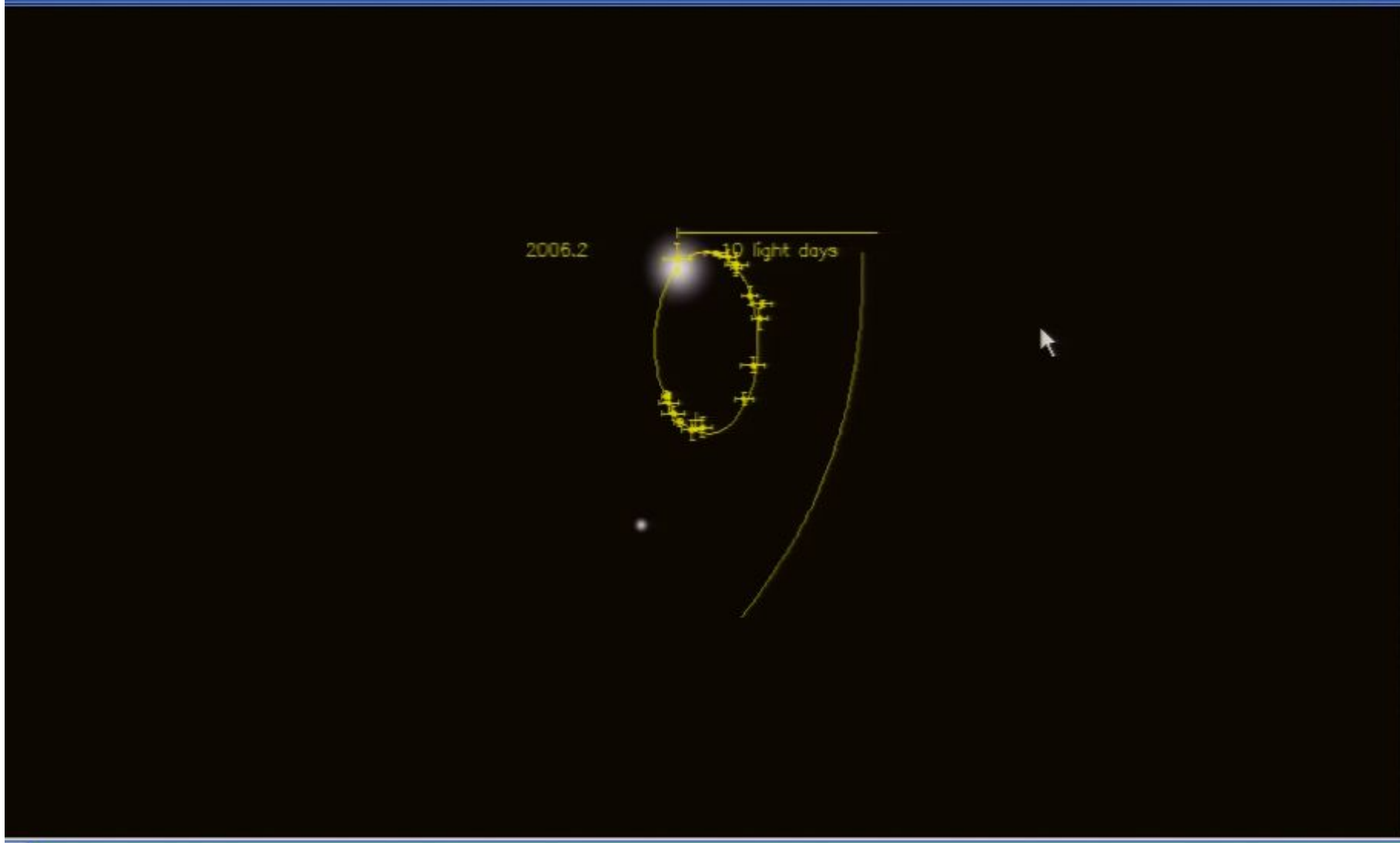




Total Time: 0:19



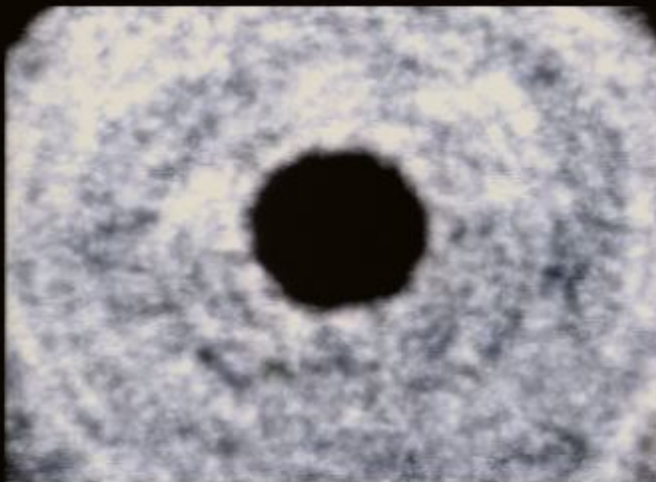
orbit around black ...



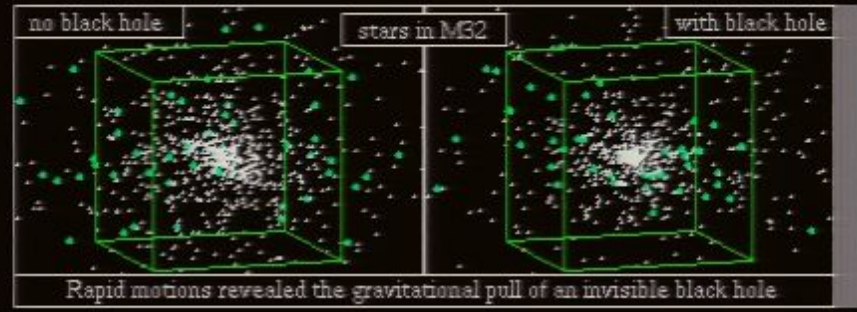
Total Time: 0:19



orbit around black ...



death spiral

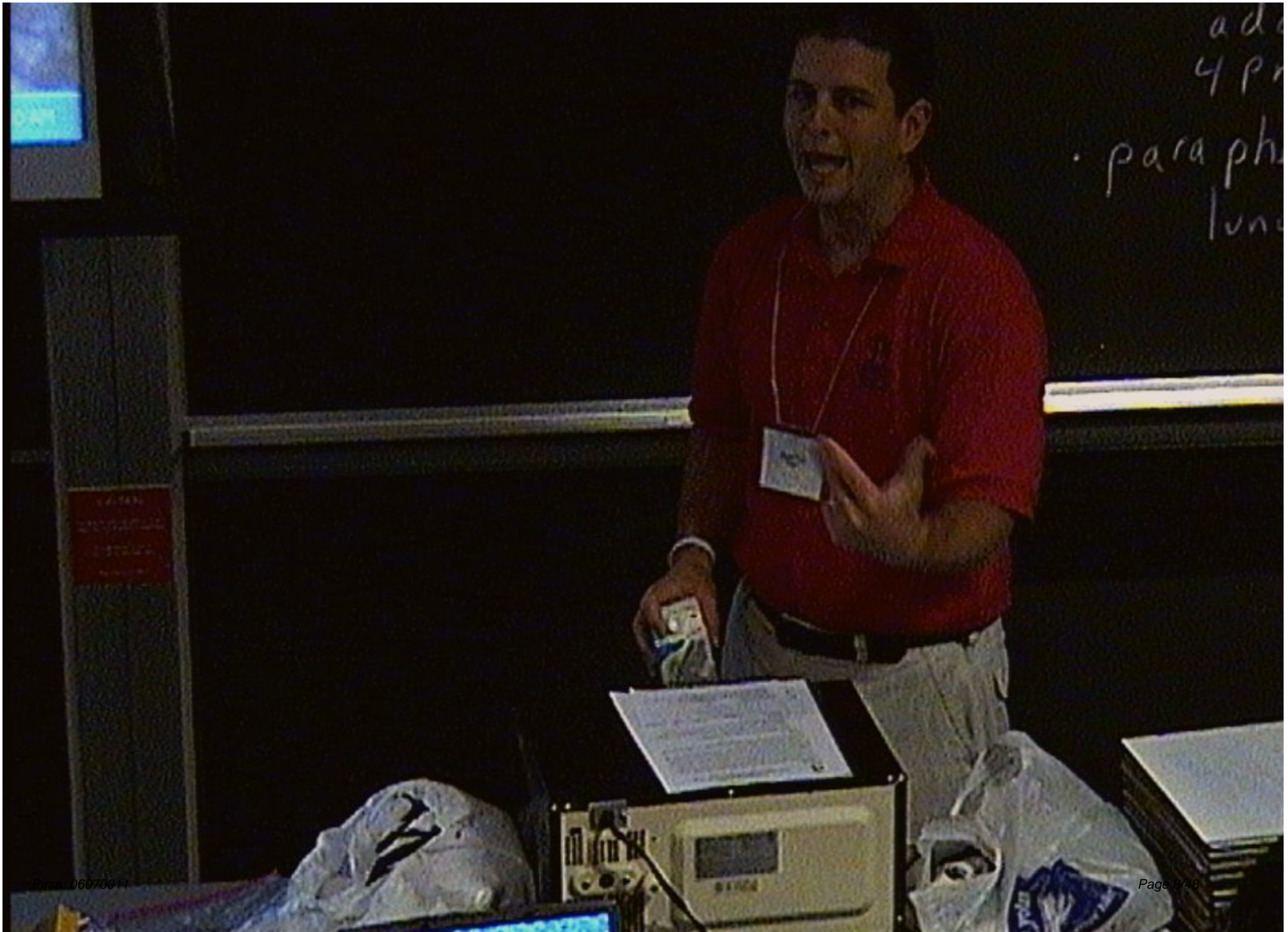




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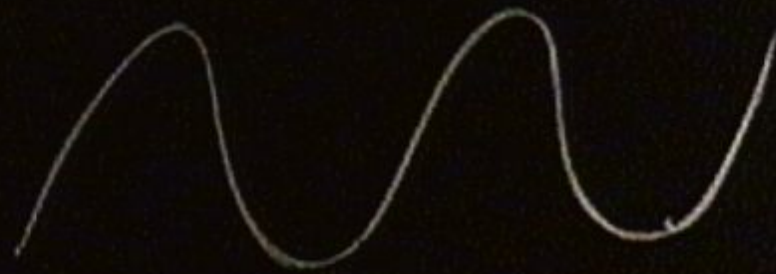


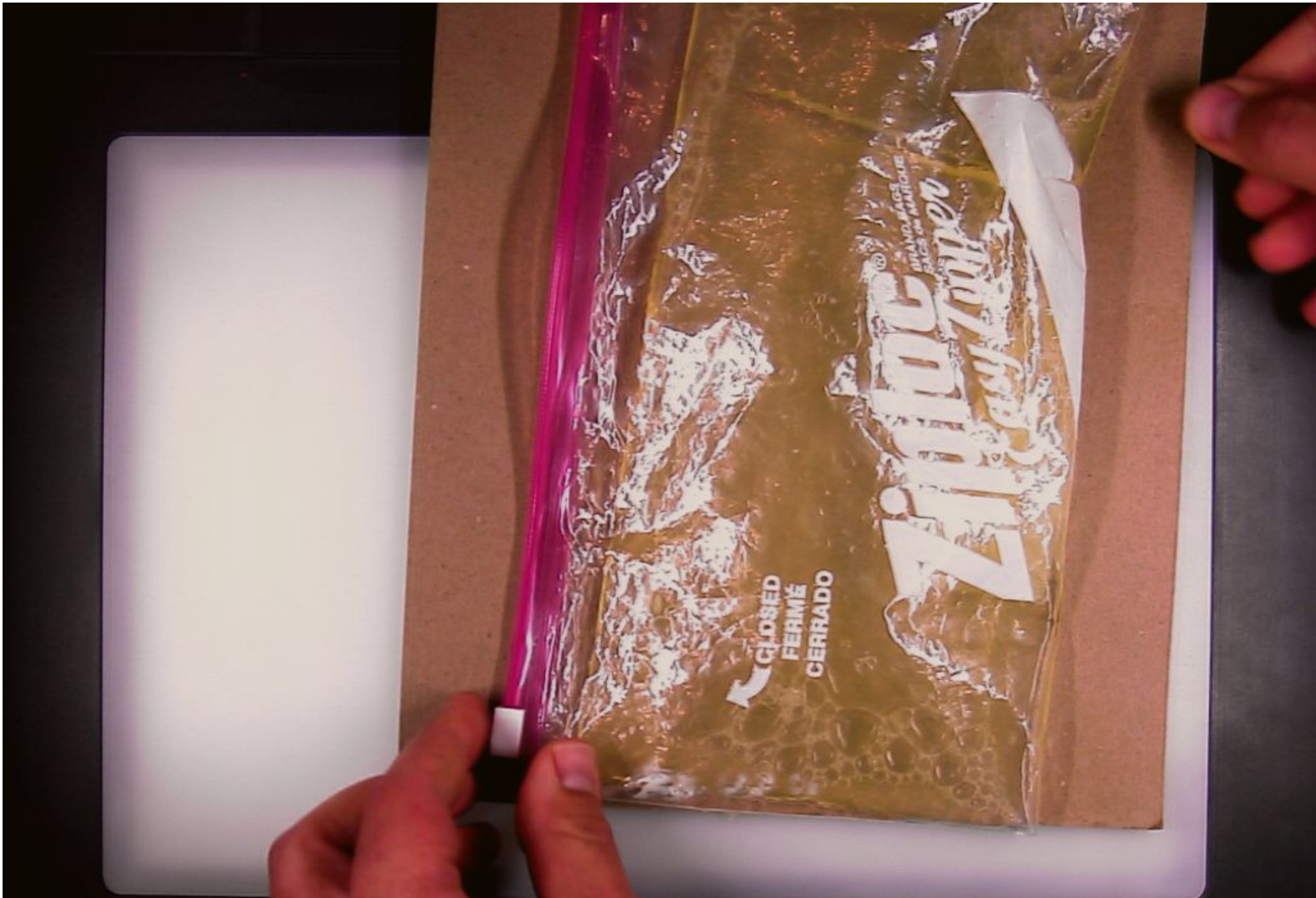
Dr. Quantum Doubl...



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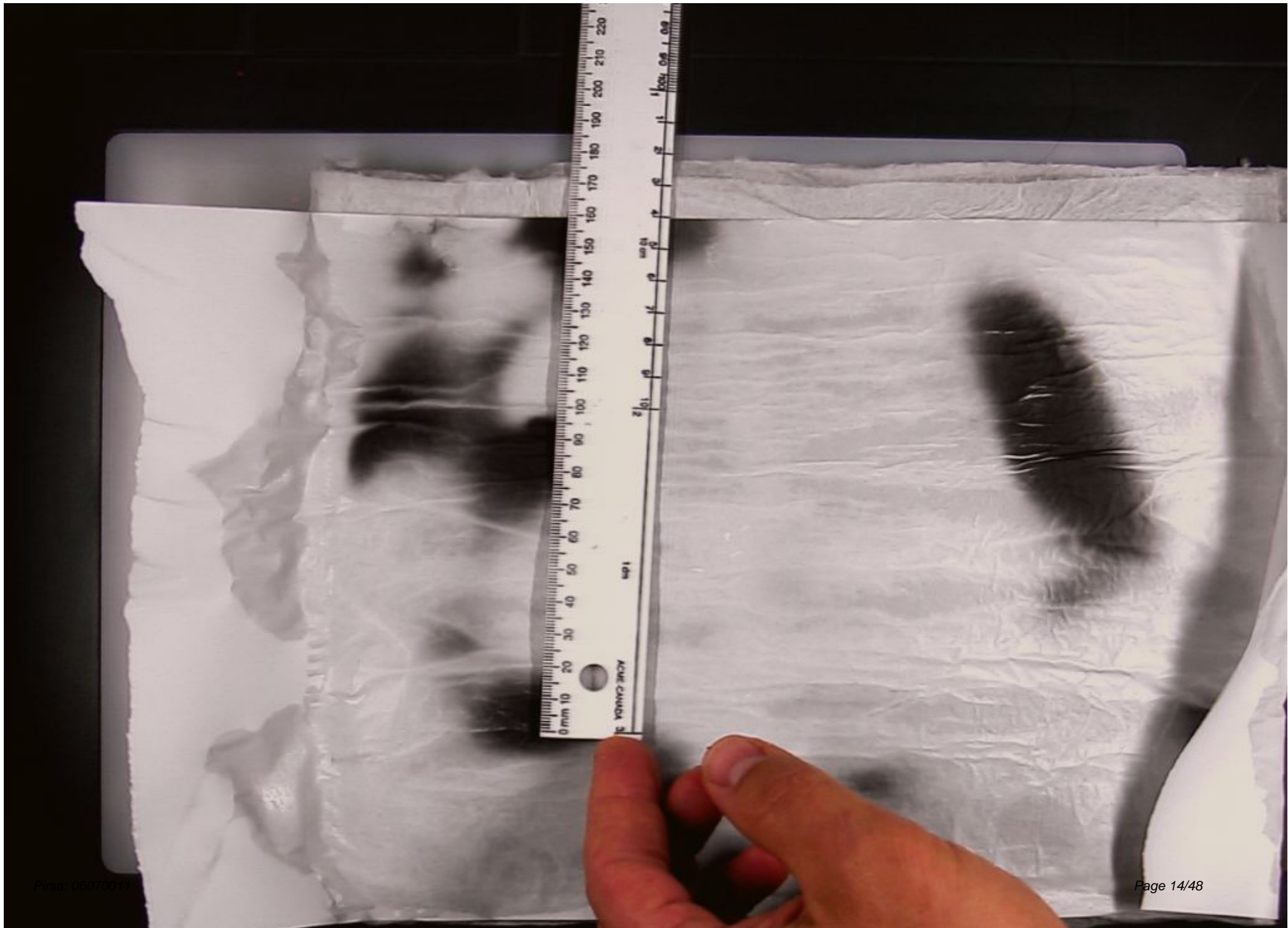


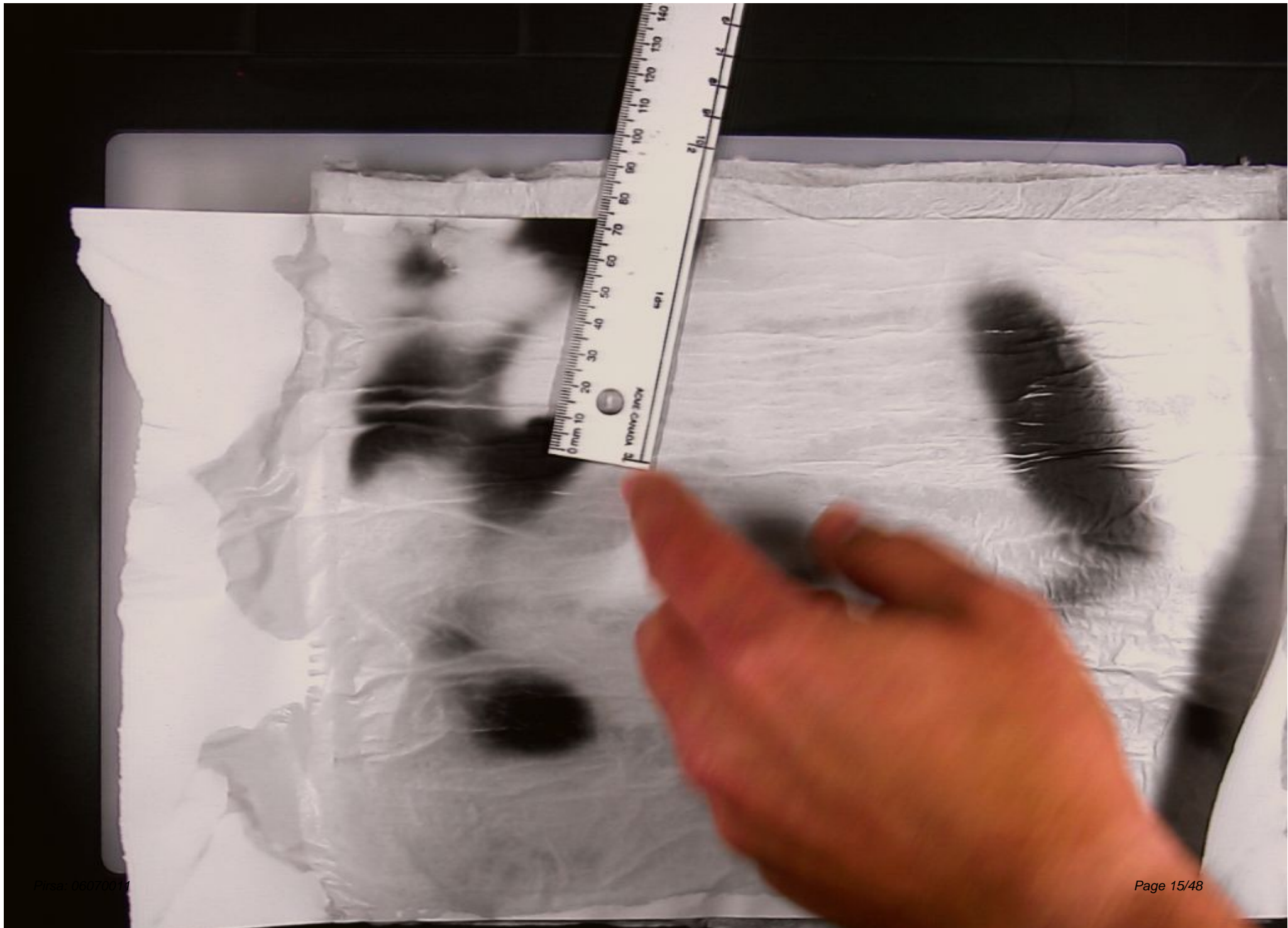


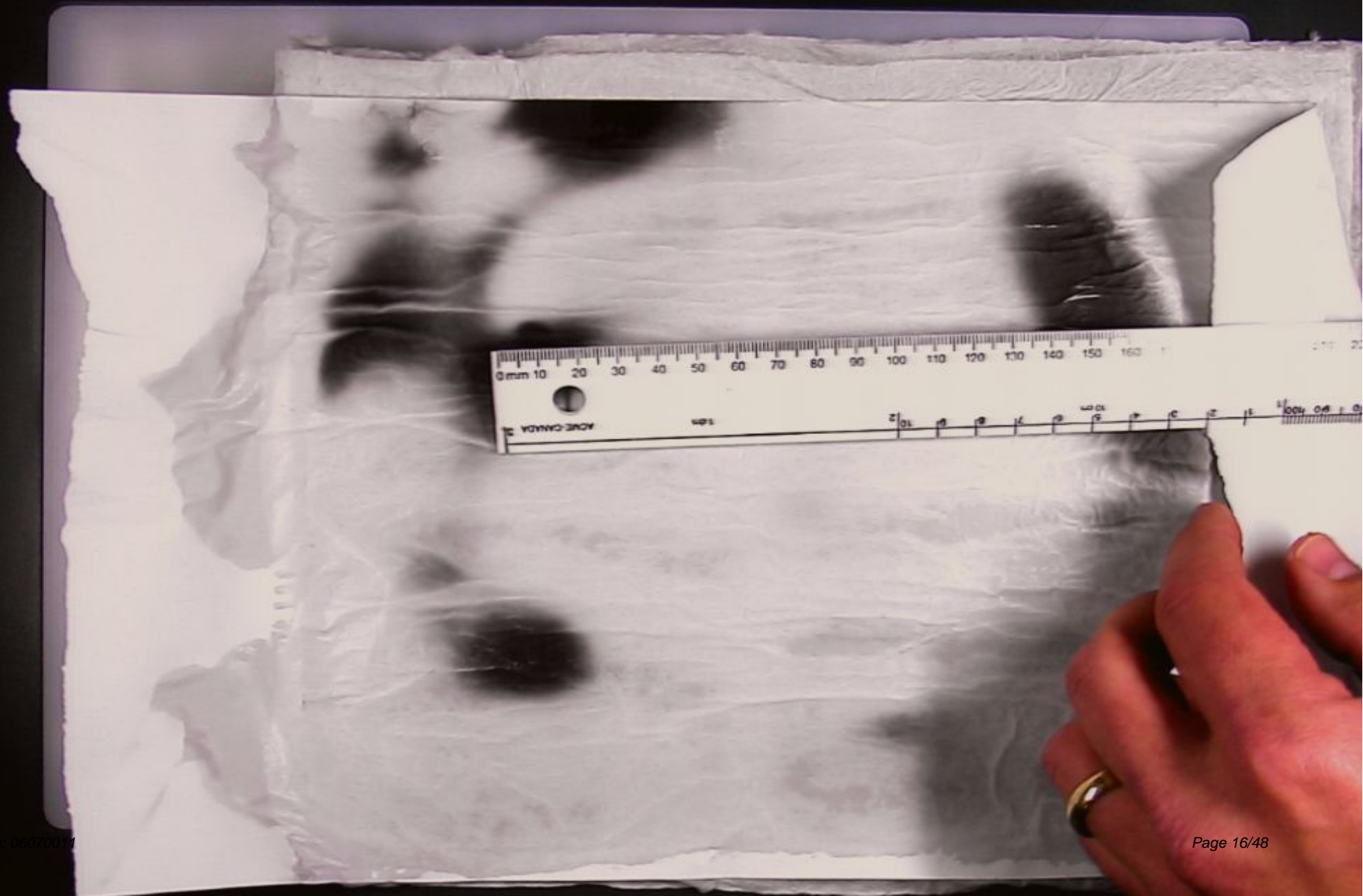


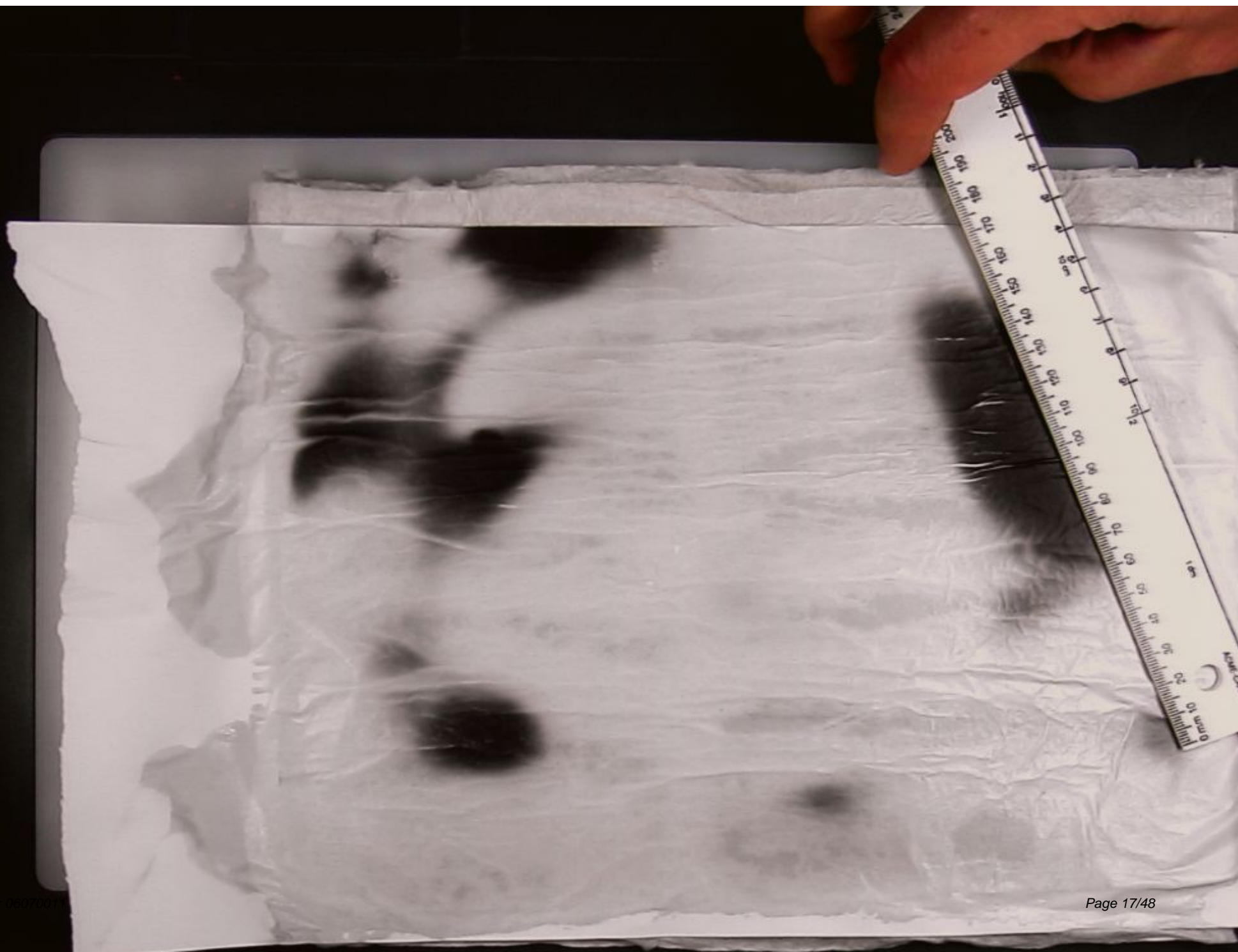


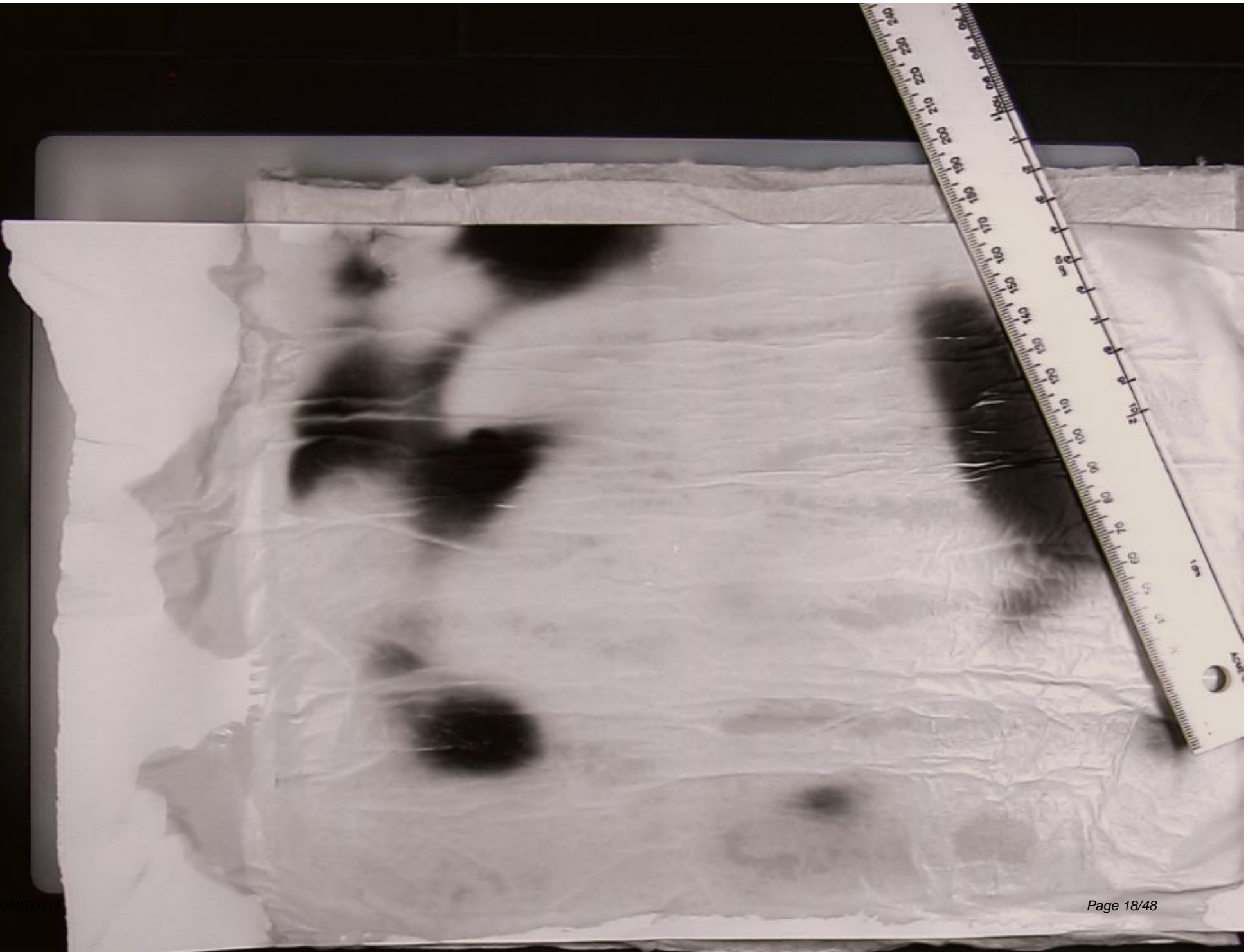












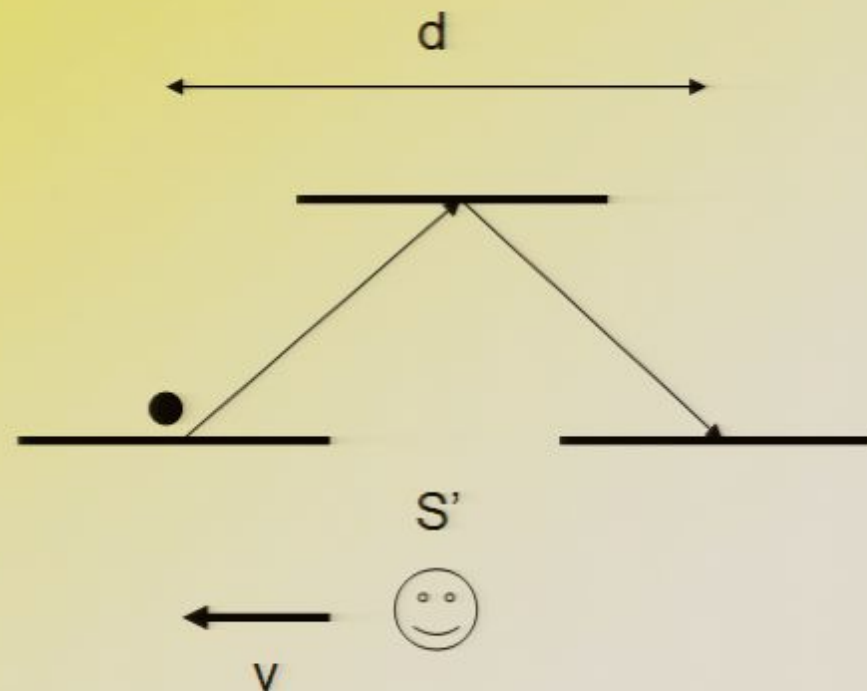
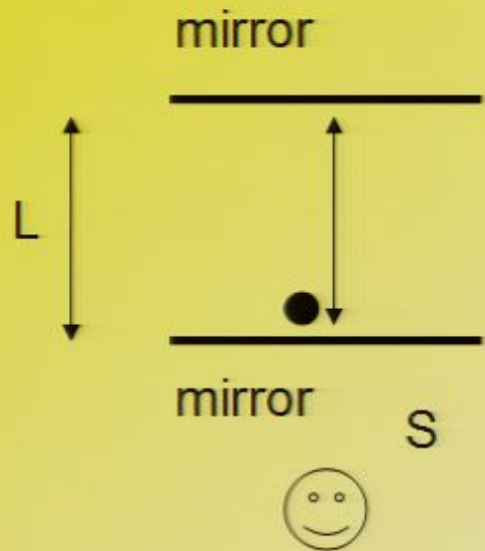
Core concepts of special relativity, Part 2



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Time dilation

- Light clock

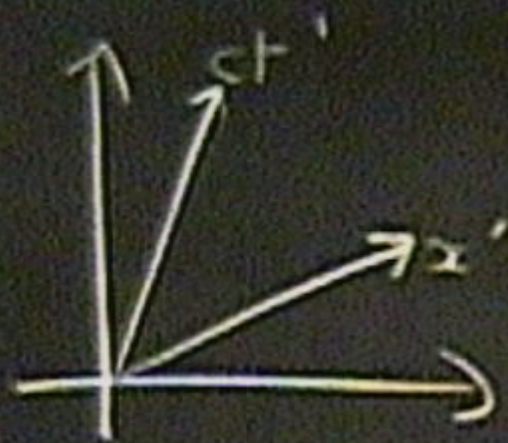


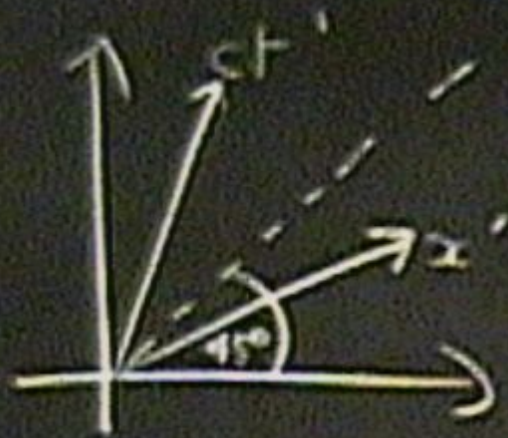
- A and B are the events corresponding to a photon hitting the bottom mirror on two successive occasions.

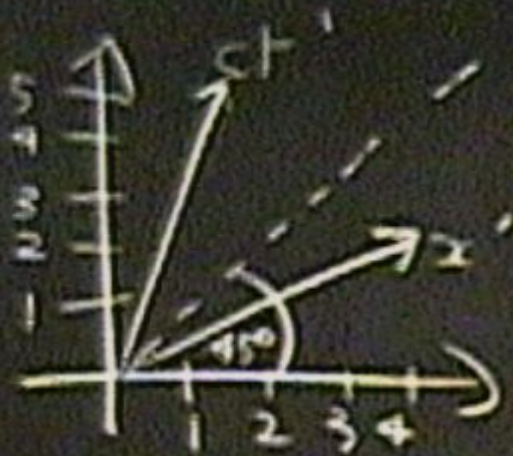
$$\Delta t = 2L / c$$

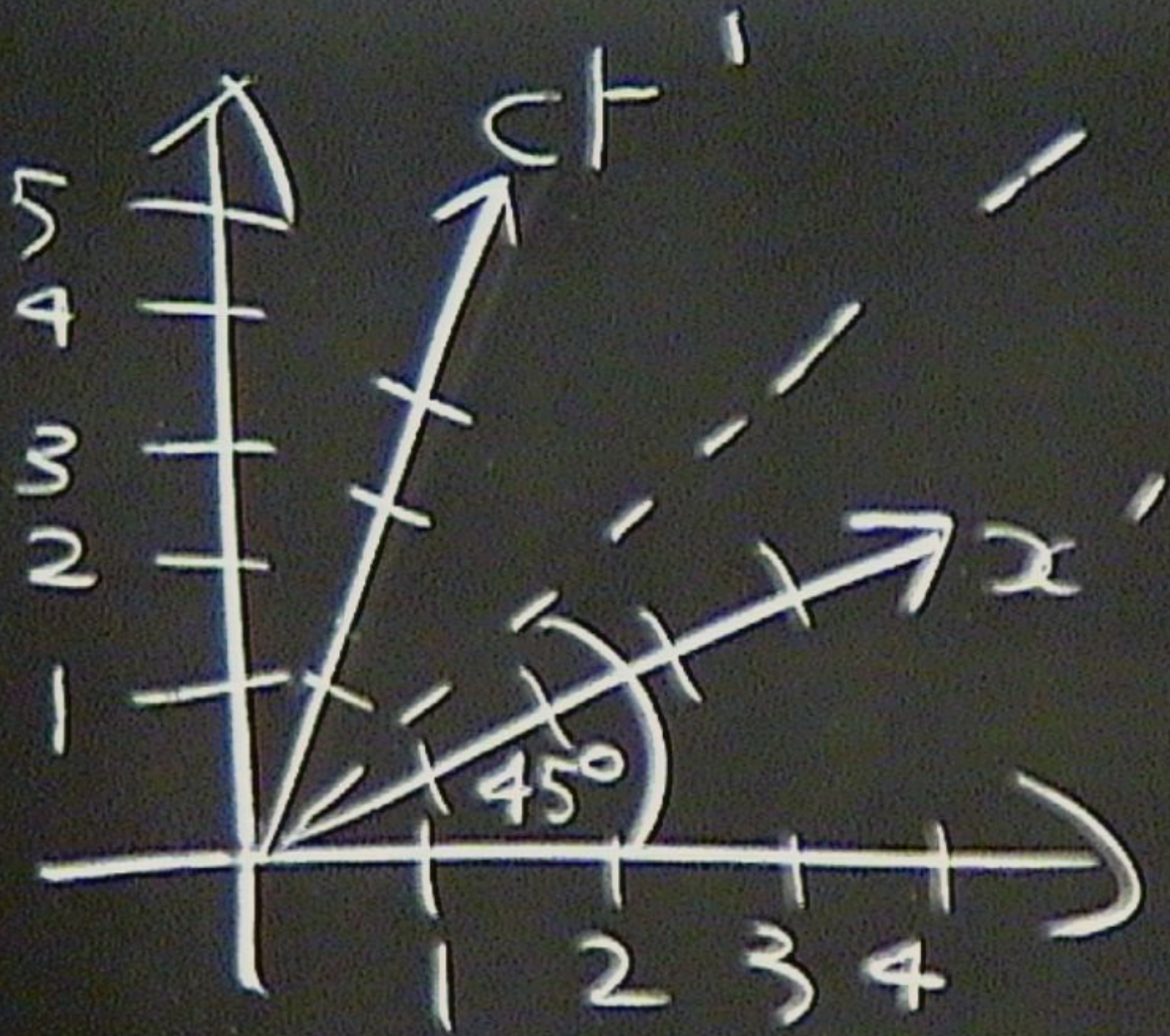
$$\Delta t' = \frac{\text{distance}}{\text{speed}} = \frac{2\sqrt{L^2 + \left(\frac{d}{2}\right)^2}}{c}$$

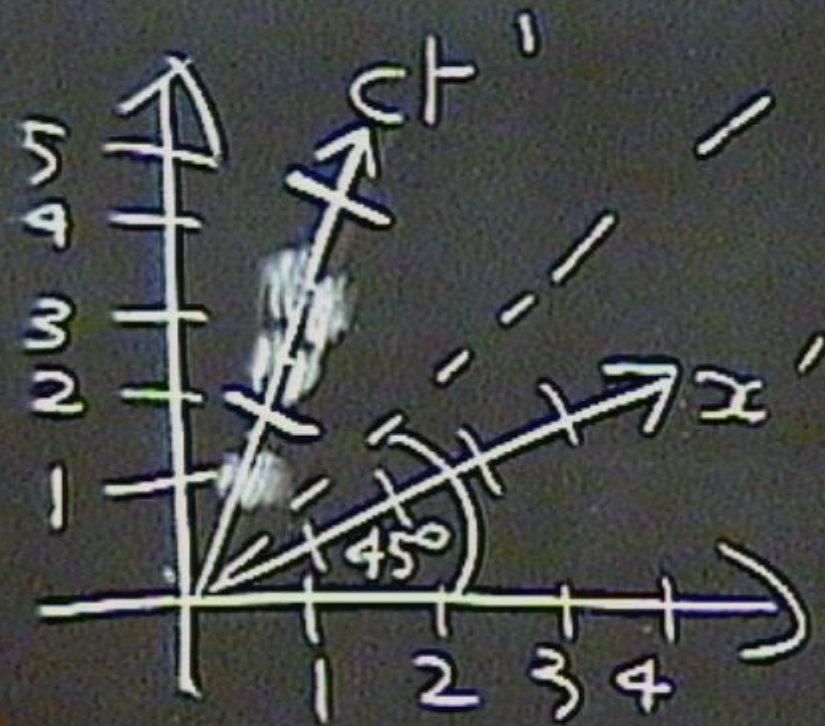
$$d = vt'$$

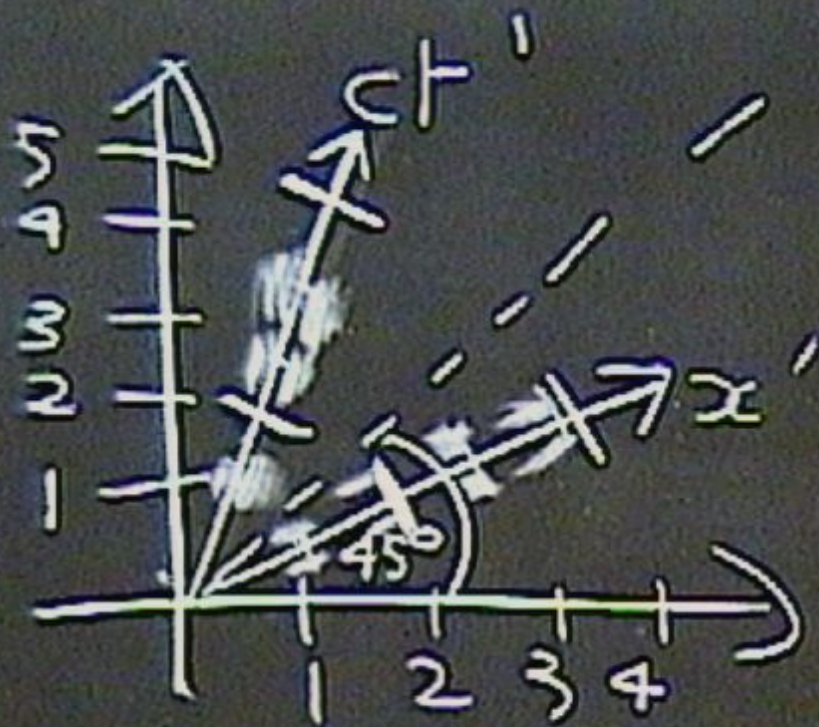


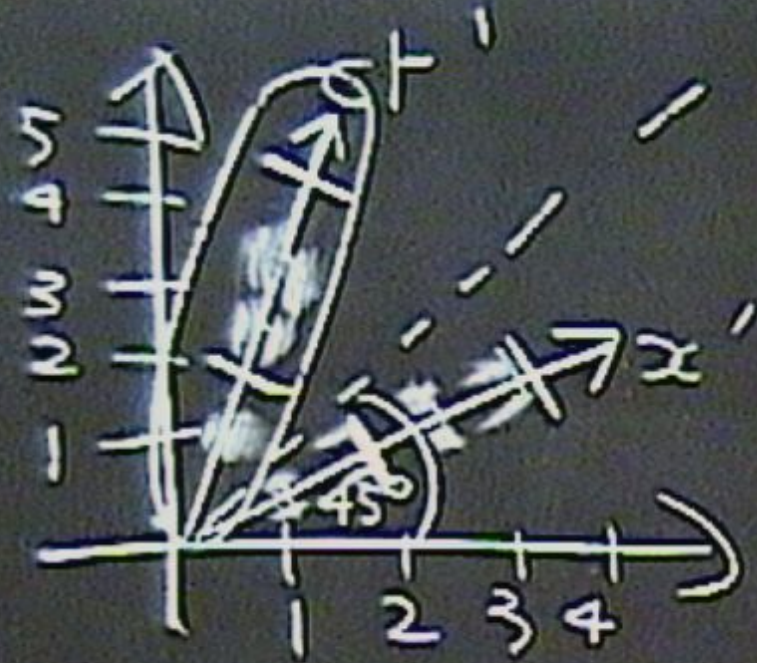






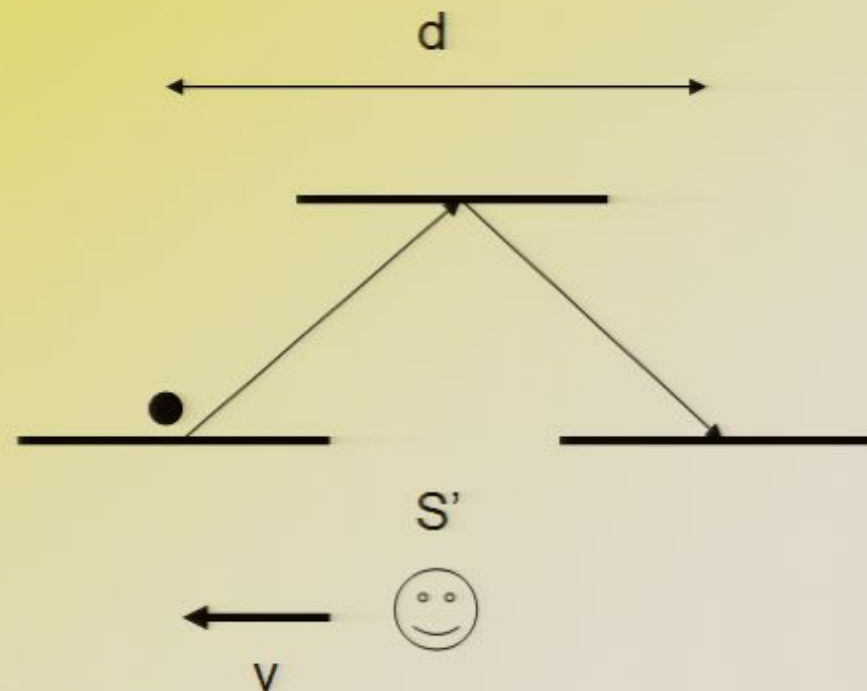
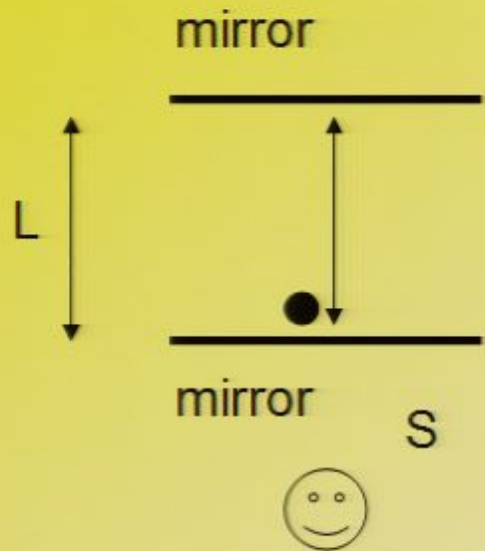






Time dilation

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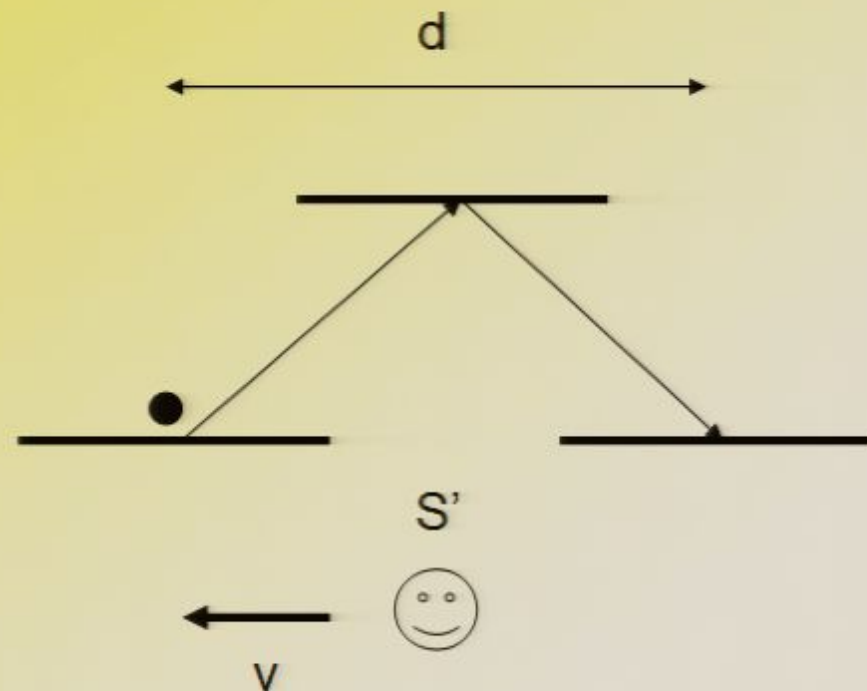
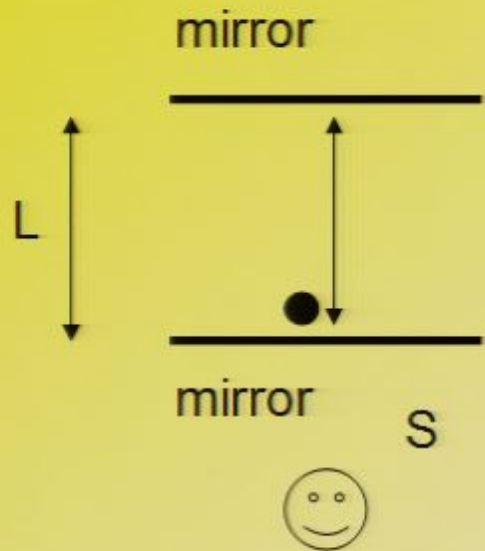
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time dilation

$$(c\Delta t')^2 = 4(L^2 + ((v\Delta t')^2 / 4))$$

$$\therefore 4L^2 = \Delta t'^2 (c^2 - v^2)$$

But $(c\Delta t)^2 = 4L^2$

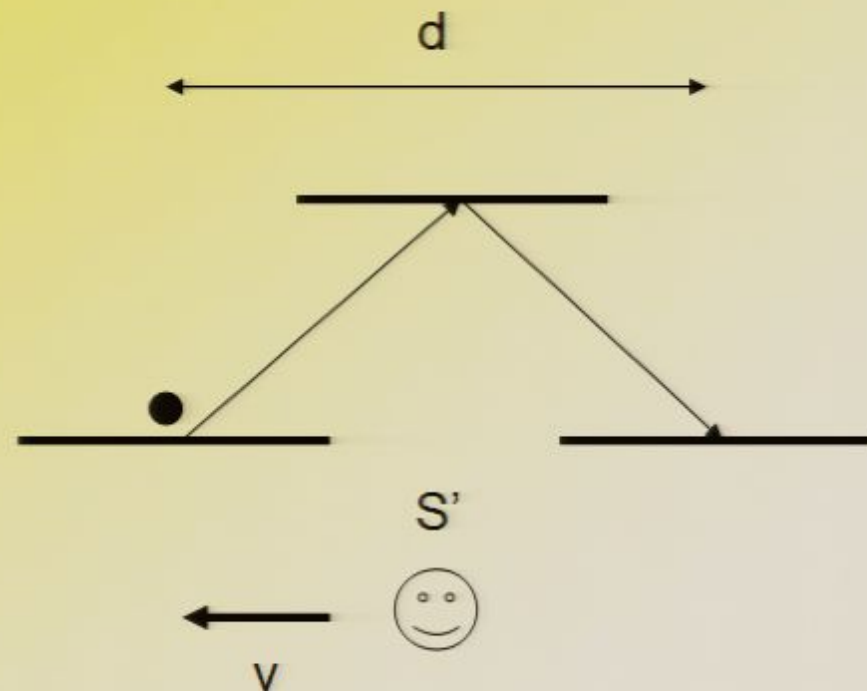
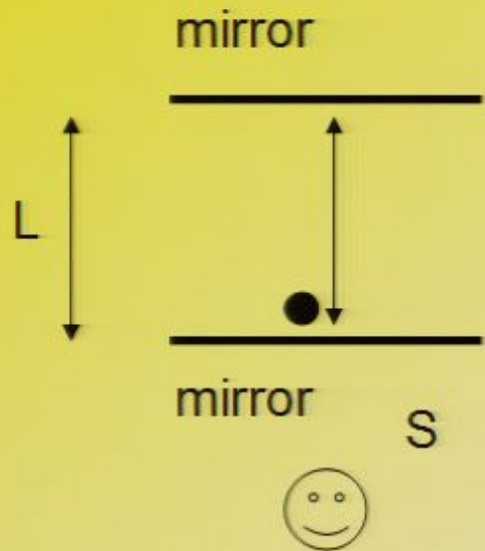
gives $(\Delta t' / \Delta t)^2 = c^2 / (c^2 - v^2)$

$$\therefore \Delta t' / \Delta t = 1 / \sqrt{1 - (v/c)^2}$$

$$\therefore \Delta t' = \gamma \Delta t$$

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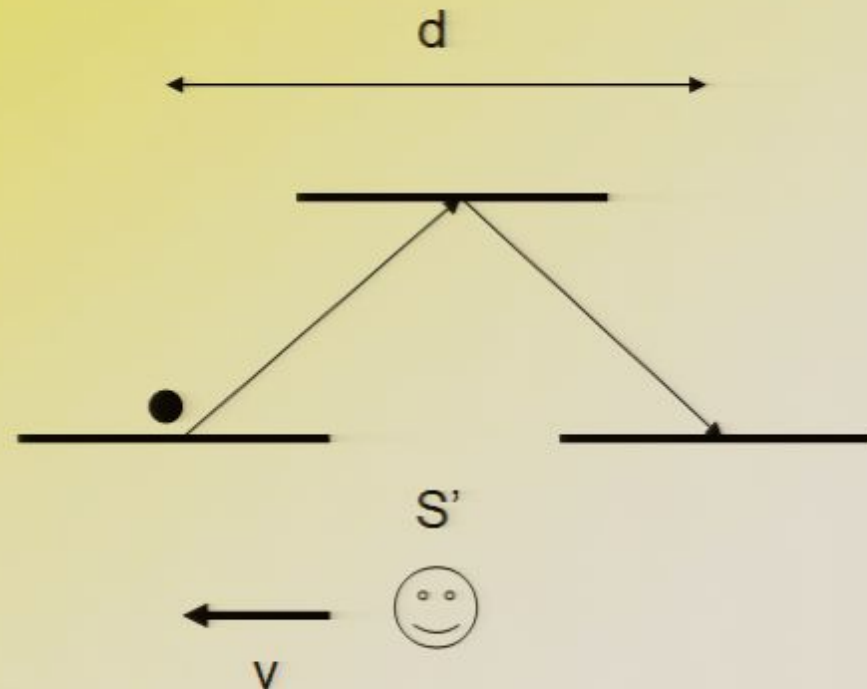
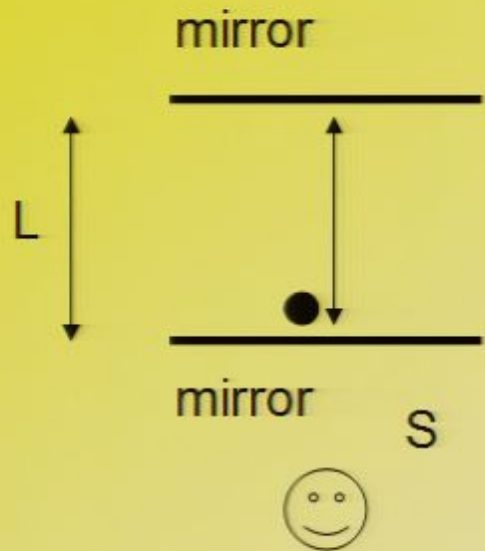
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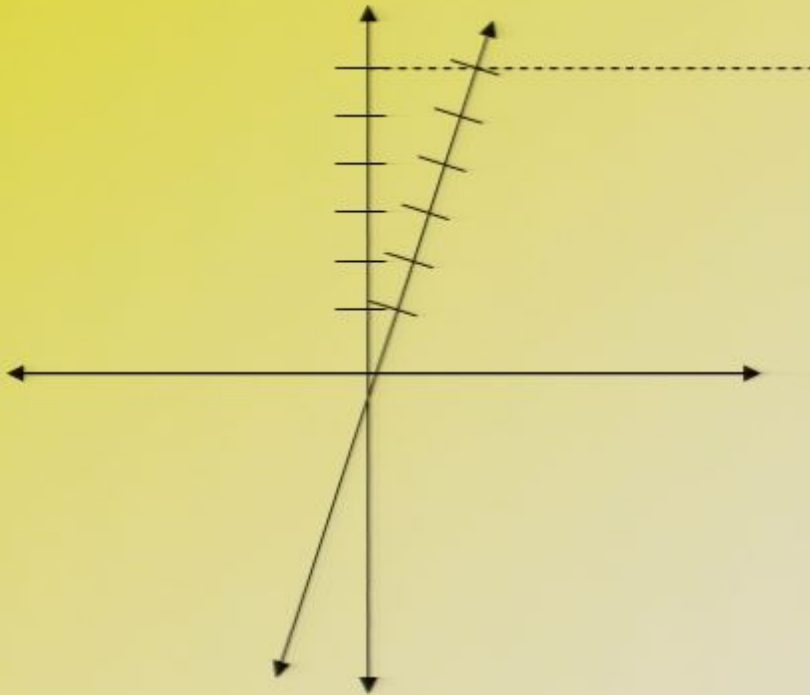
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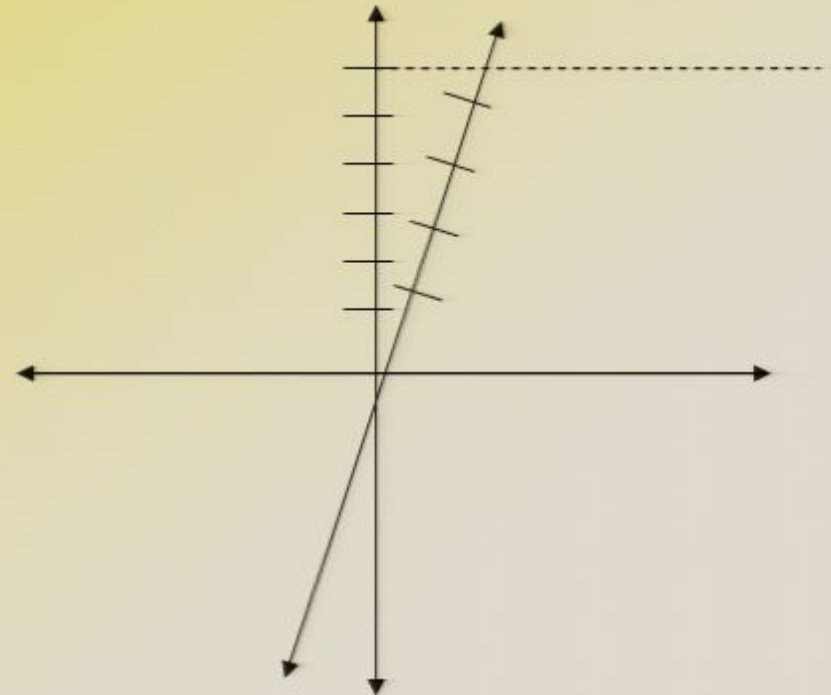
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Scales on time and x axes

- ct' axis: Due to time dilation, it must be stretched out.



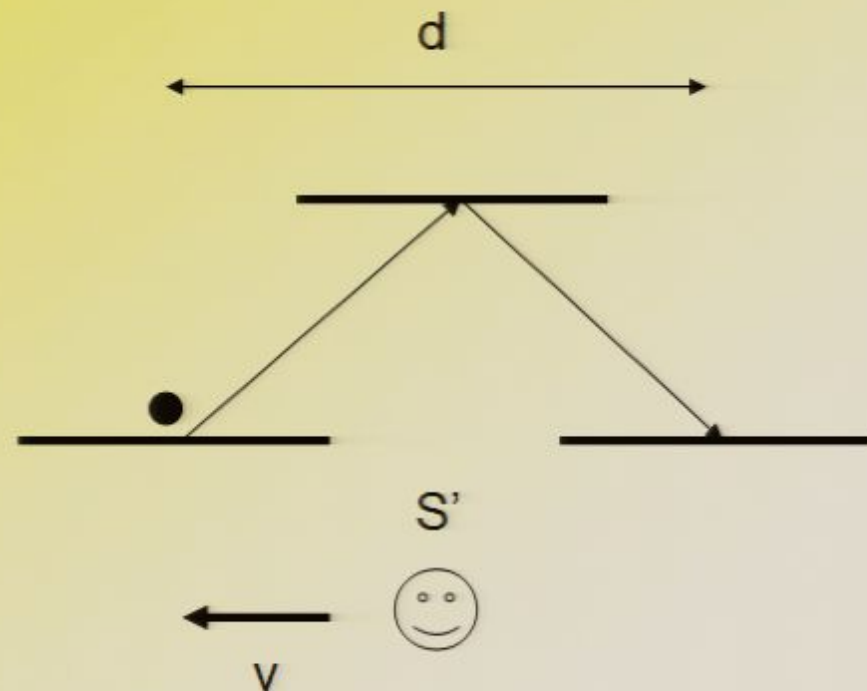
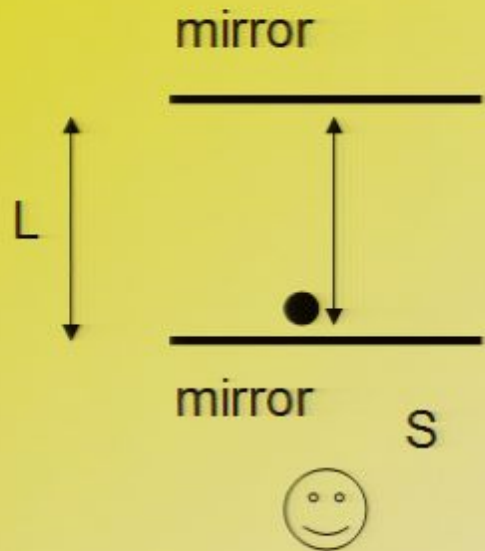
wrong



right

Time dilation

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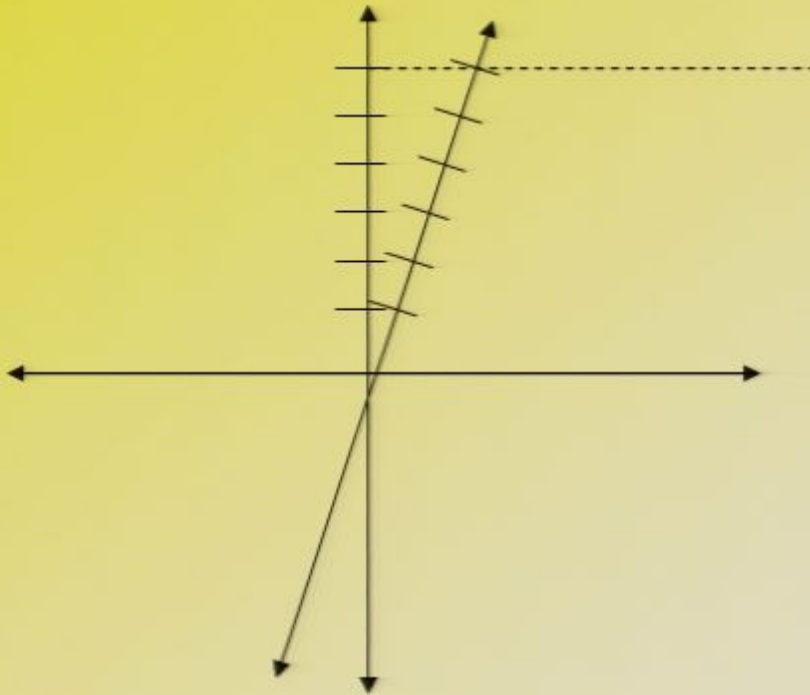
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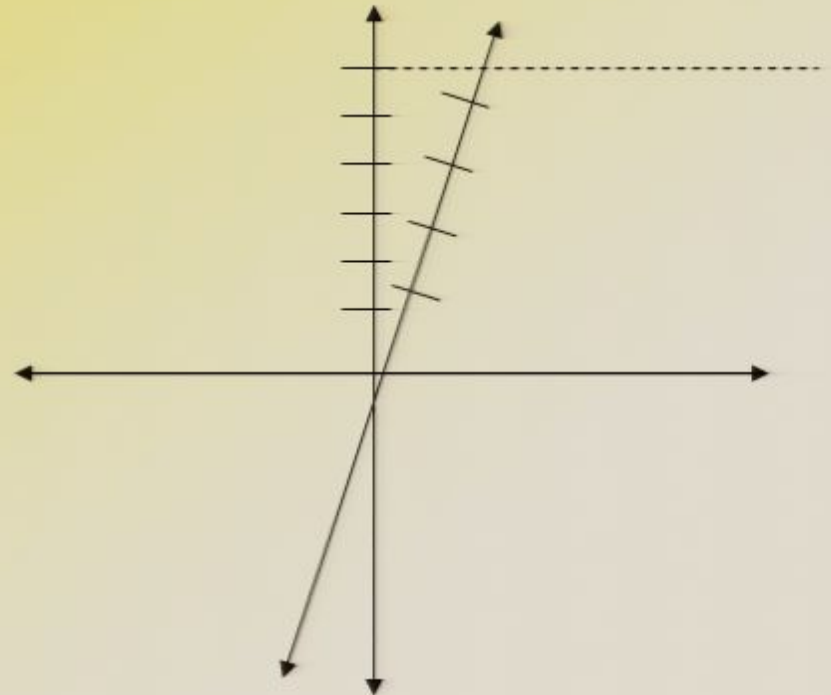
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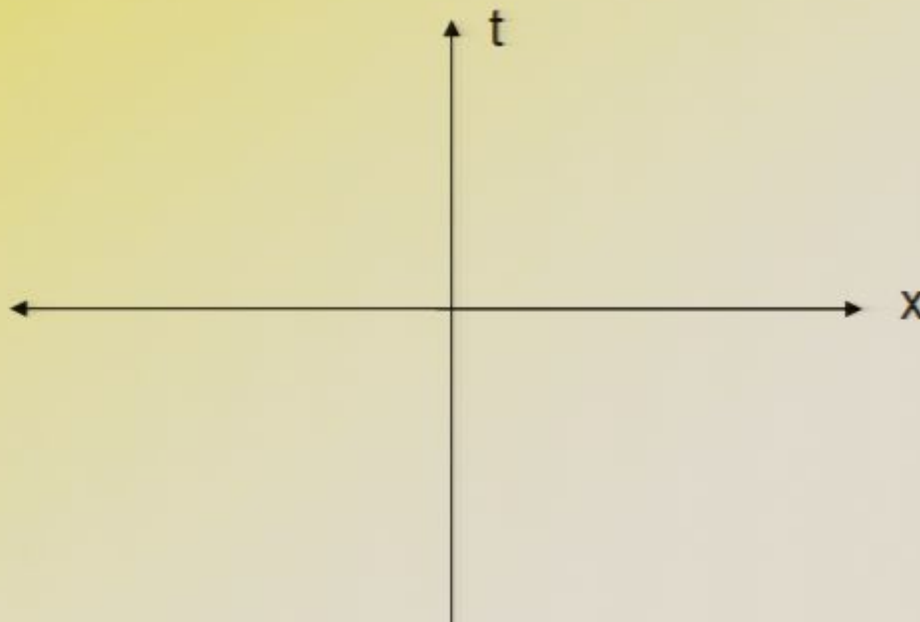
wrong



right

Time dilation

- Consider a black spaceship travelling at $0.5c$ past the earth. At one point, the Klingon on it starts typing into her computer (event A). Some time later, she is finished (event B).
- Assuming A happens in the spaceship's frame time $t=0$ and $x=0$ and B at $t=T$, plot A and B on the spacetime diagram below:



time dilation

$$(c\Delta t')^2 = 4(L^2 + ((v\Delta t')^2 / 4))$$

$$\therefore 4L^2 = \Delta t'^2 (c^2 - v^2)$$

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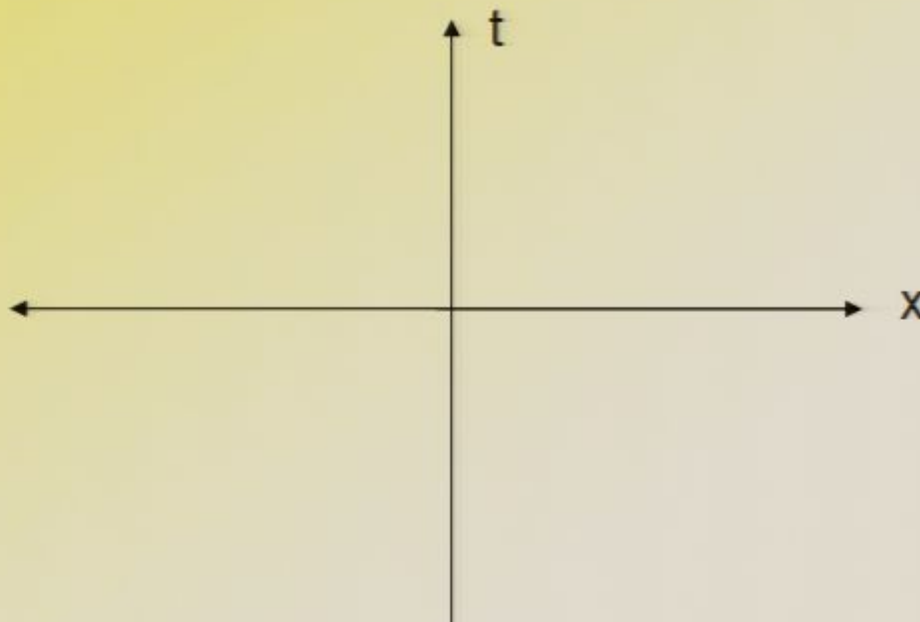
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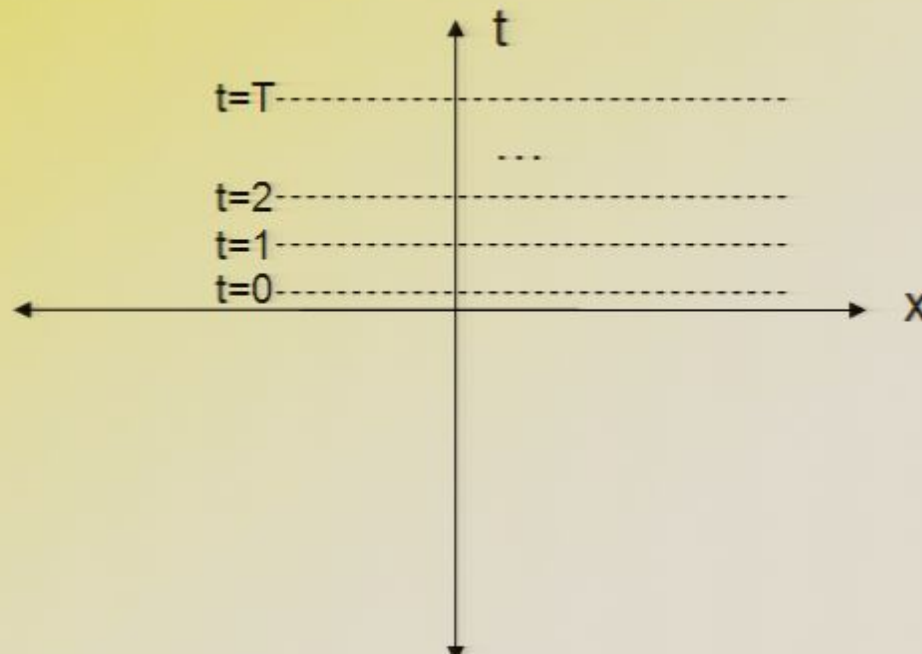
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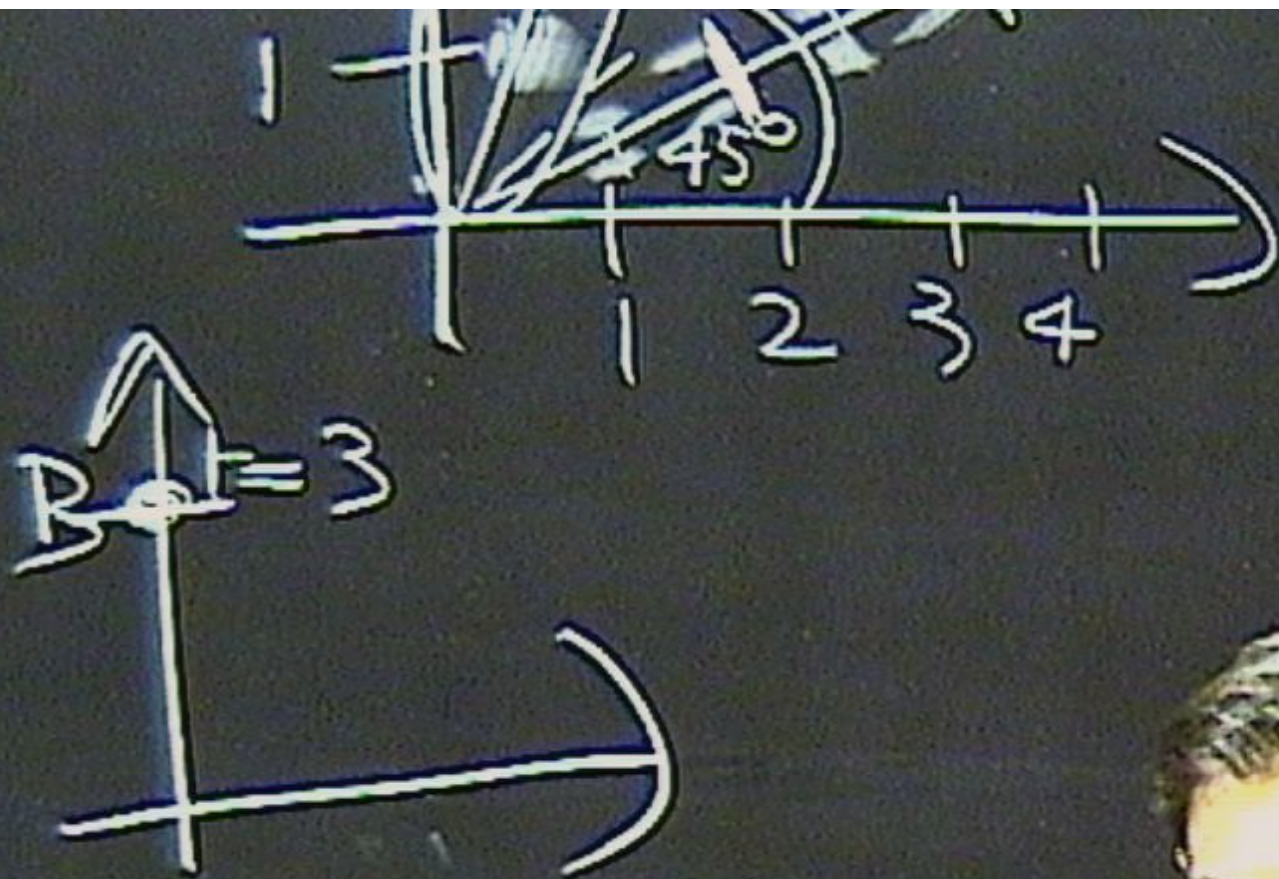
Time dilation

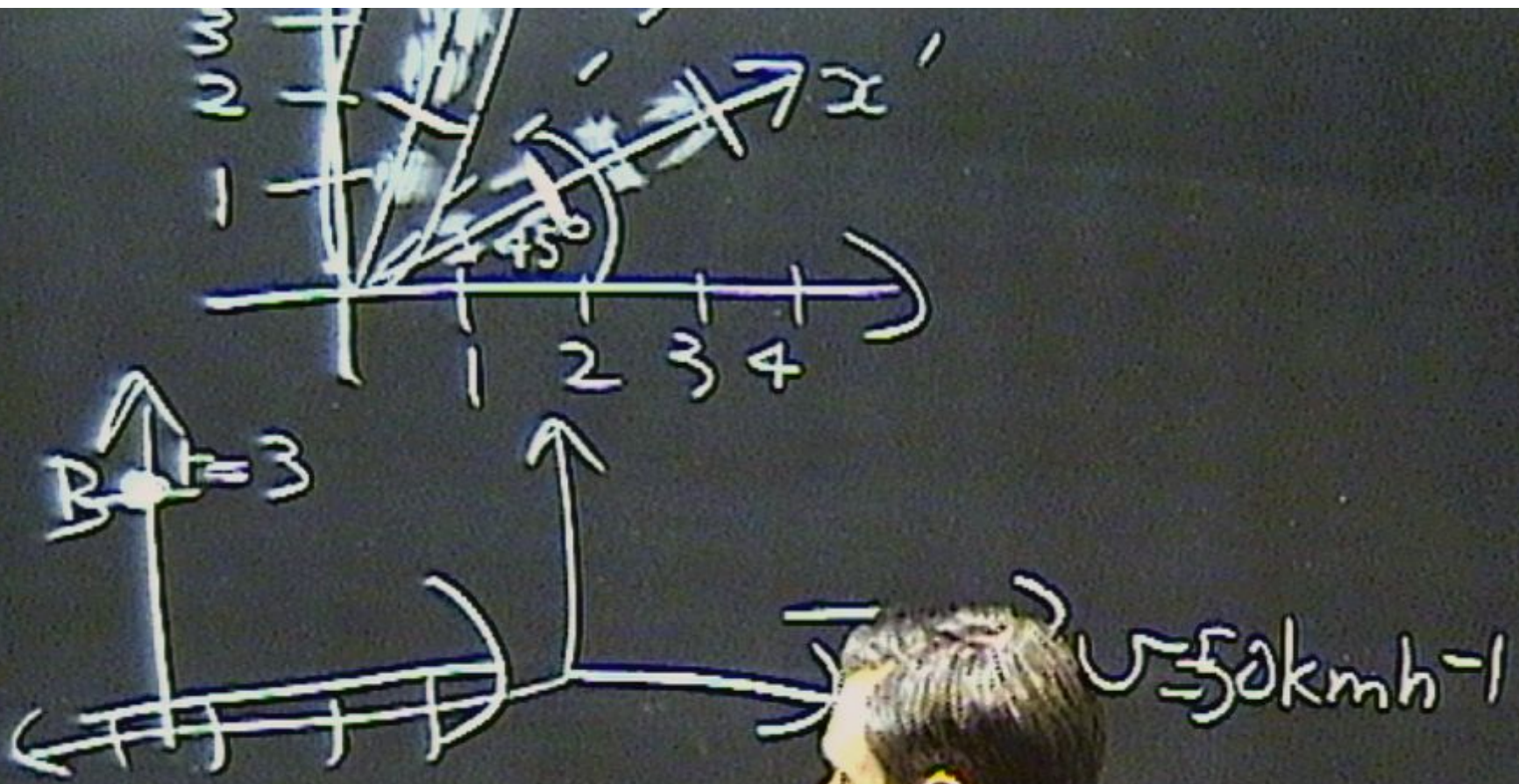
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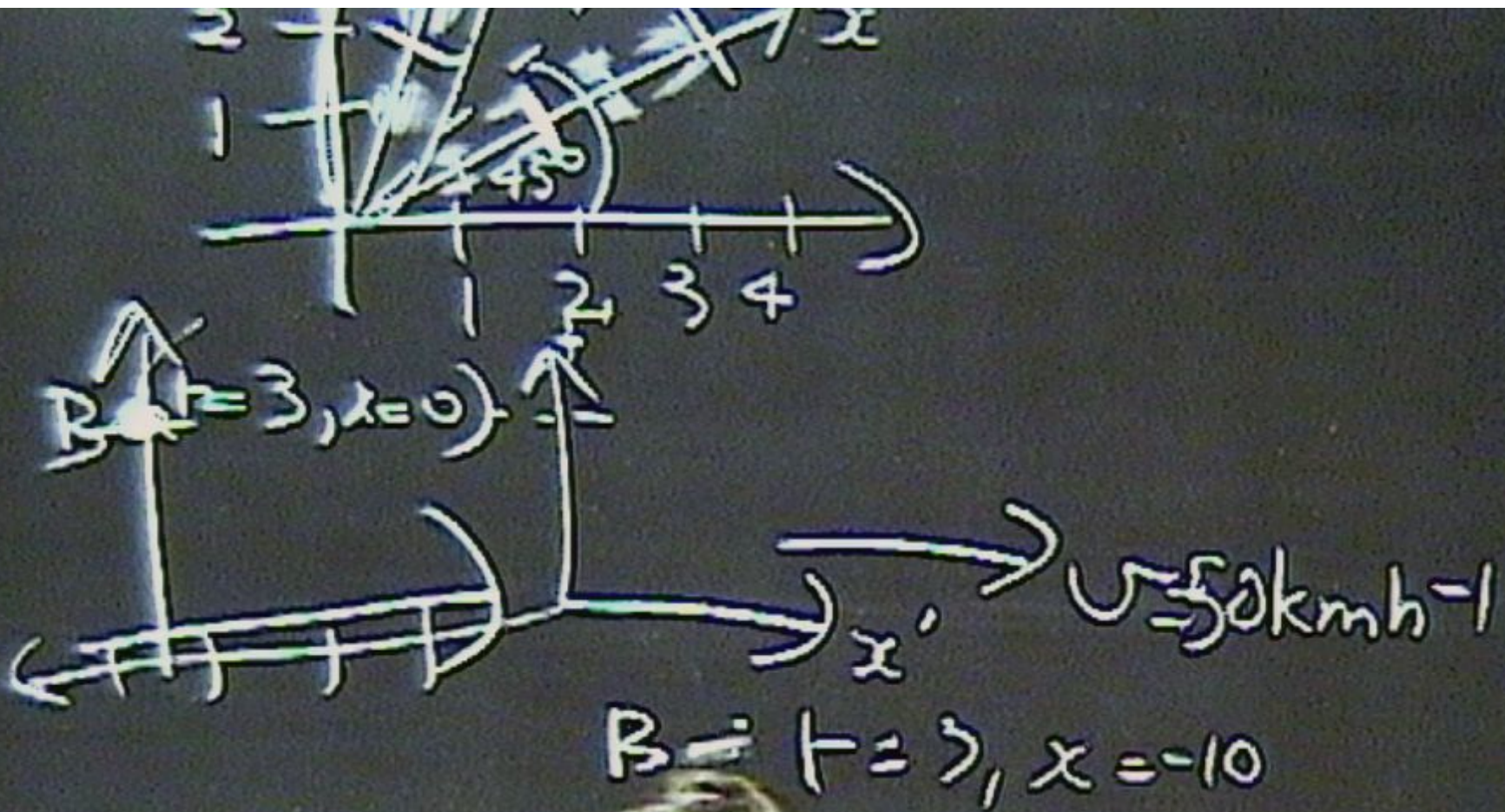


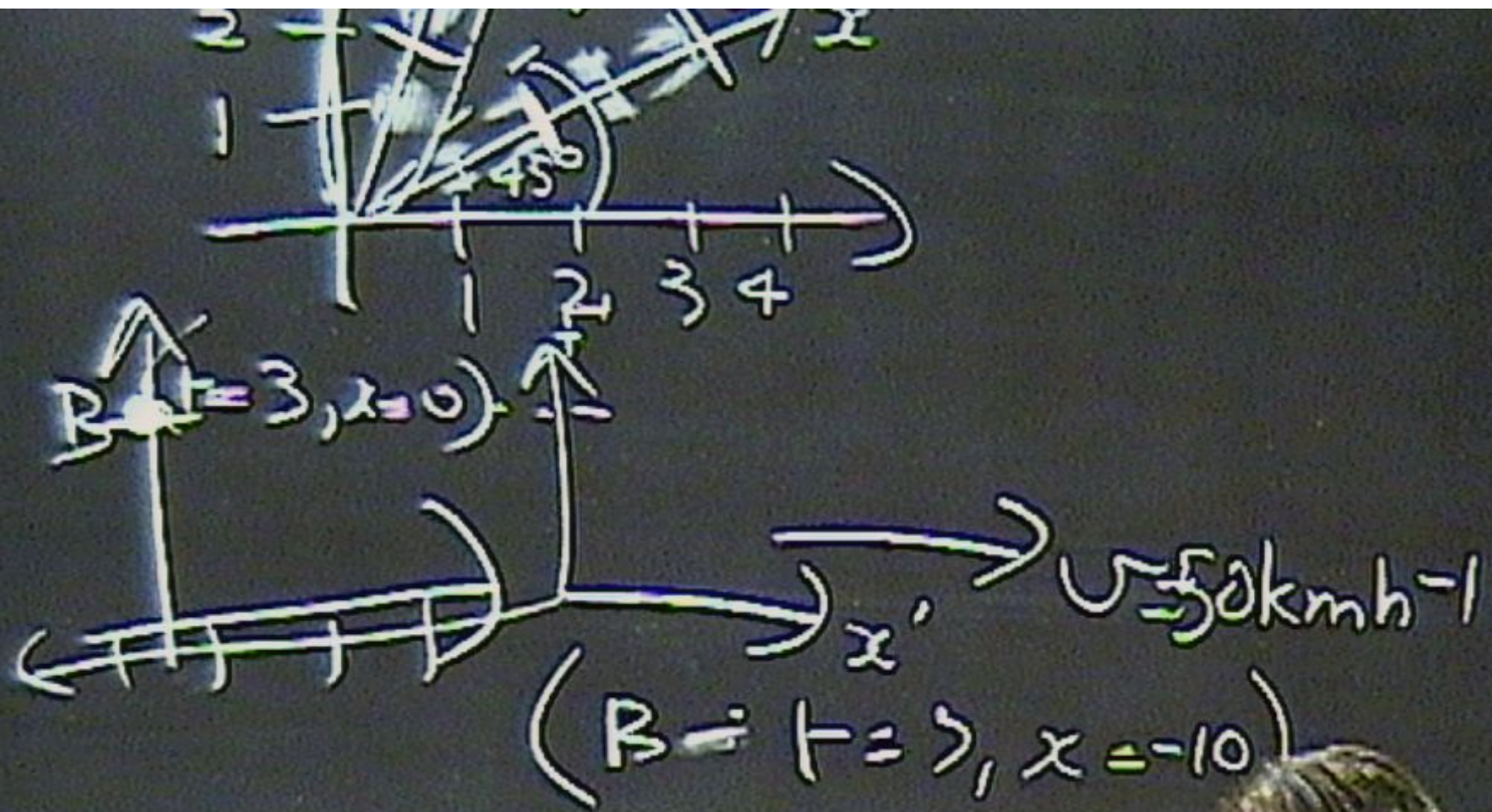
- If we did not know that $\Delta t_s = T$, then we could determine it from the graph through the following procedure:
- Start at A and draw a line of constant time ($t=0$). Continue to draw lines of constant time ($t=1, 2, 3, \dots$) — these are parallel to the x axis — until we draw one that intersects with B. The time for this line is T.

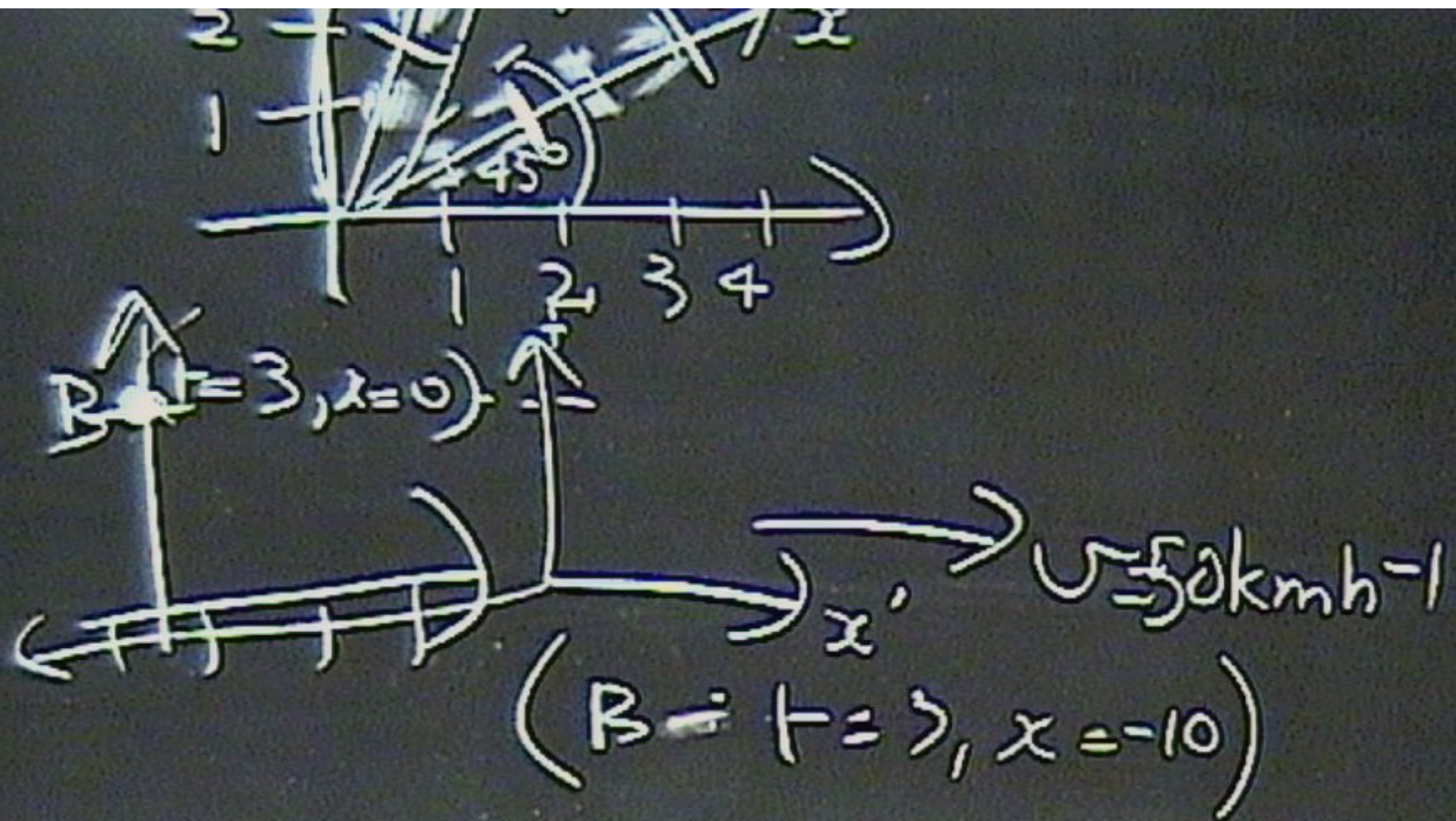




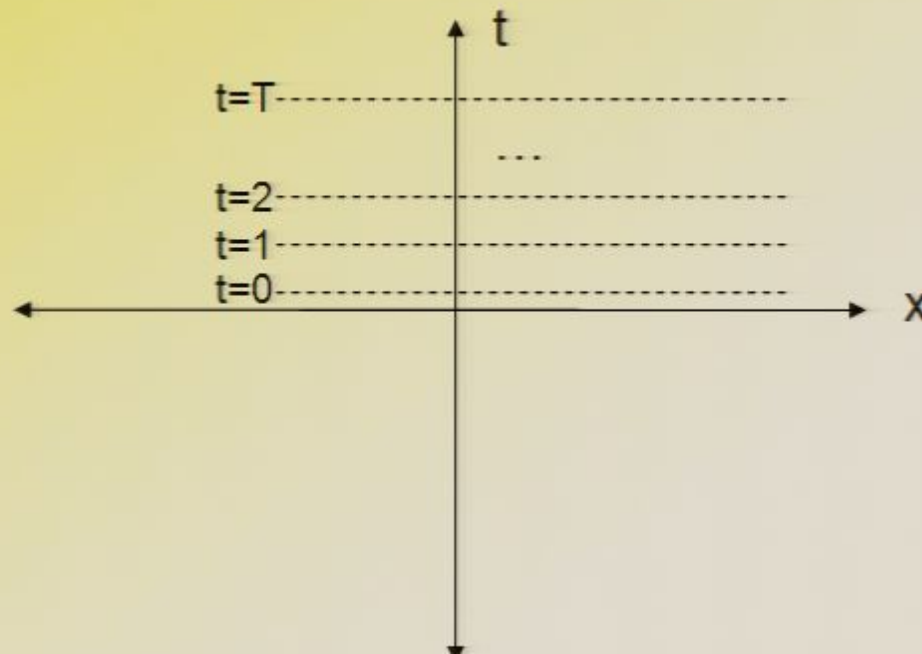








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- To determine the time interval between A and B as measured in Earth's reference frame E. Let us follow an analogous procedure.
- 1. The x' axis corresponds to the line $t'=0$ and so it is the first line.
- 2. Draw another line parallel to the first that corresponds to $t'=1$. i.e. one unit of time upwards.
- 3. Continue this procedure until you draw a line that intersects B.