Title: Keynote Presentation on A Picture of Quantum Theory

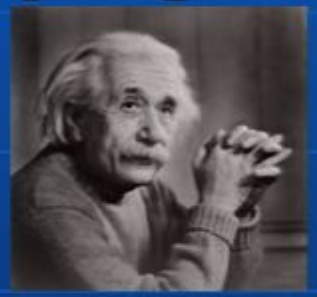
Date: Jul 04, 2006 01:00 PM

URL: http://pirsa.org/06070002

Abstract:



# Cats, Collapses and the Nature of Reality

## What does quantum theory really mean?




# Einstein's reaction to quantum theory

Einstein spring 1927:

i) Quantum theory does not yield the classical behavior of macroscopic objects to a good approximation.
ii) Quantum theory leads to correlations among spatially separated objects that appear to violate action-by-contact principles.

# Outline

- Classical Physics in Configuration Space
- Quantum Physics in Configuration Space
- The Measurement Problem
- Different Interpretations
- Conclusion

*"Never underestimate the pleasure of hearing something you already know!"*

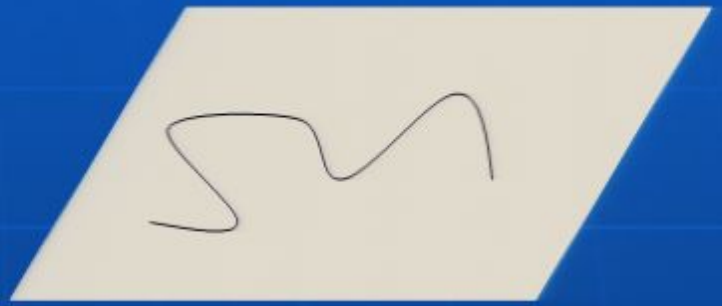
*Enrico Fermi*

# Classical Physics

# Configuration Space

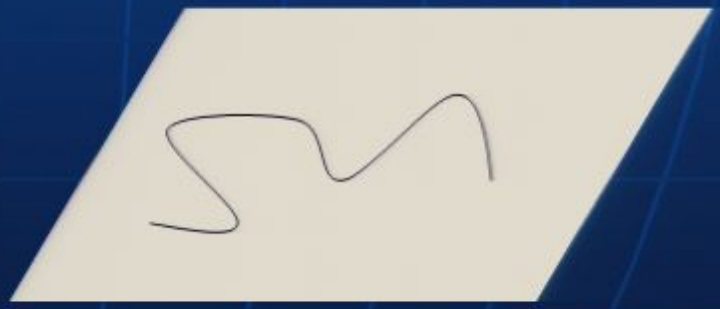
**One Particle:** $X=(x,y,z)$

3D



**Two Particles:** $X=((x_1,y_1,z_1),(x_2,y_2,z_2))$

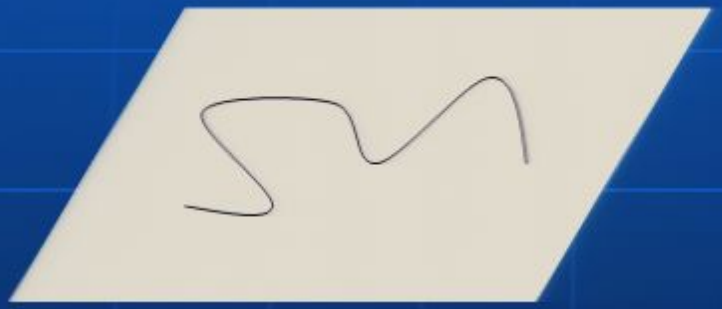
2×3D



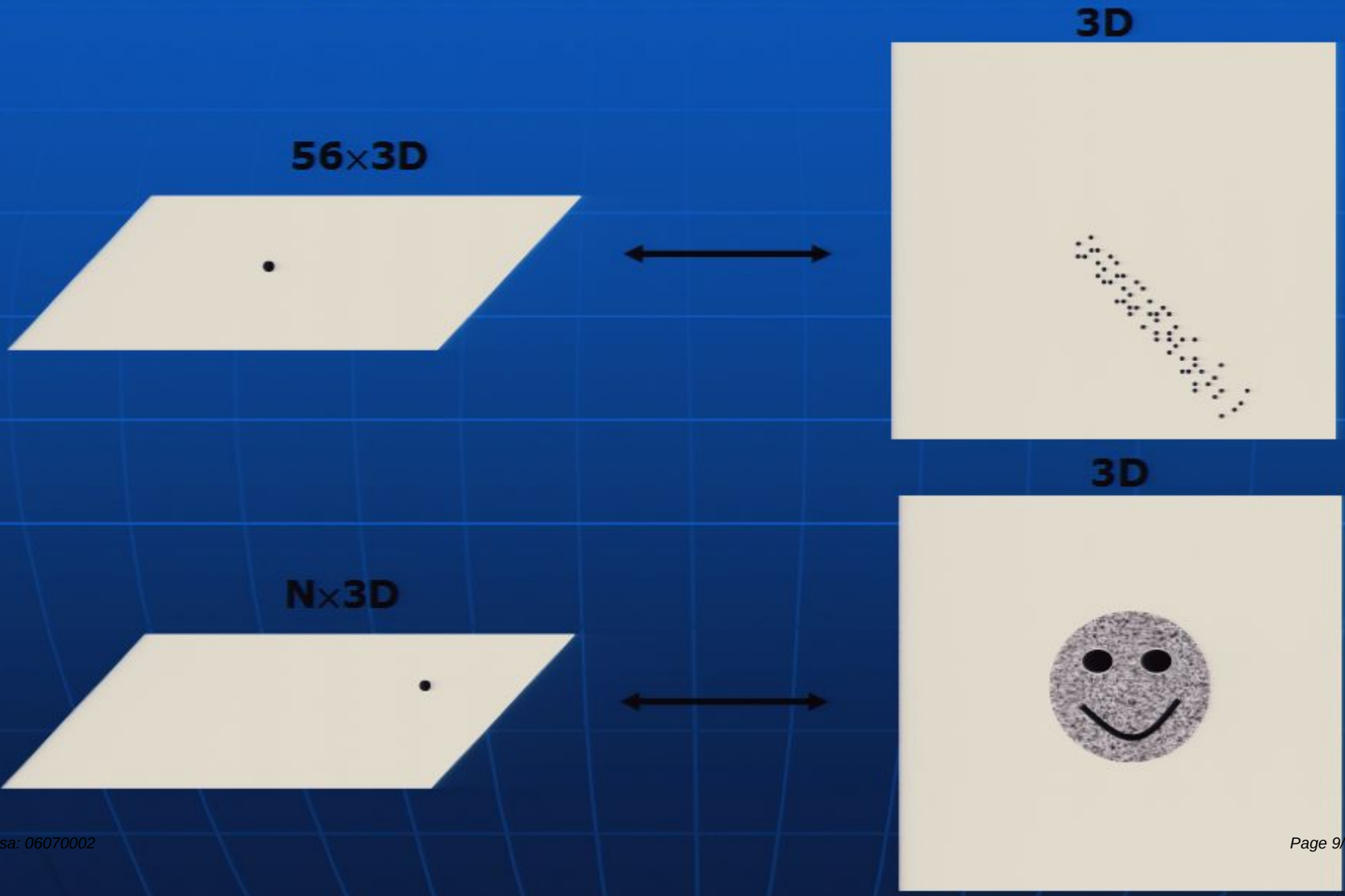
# Configuration Space

**N Particles:** $X=((x_1,y_1,z_1),(x_2,y_2,z_2),\ldots,(x_N,y_N,z_N))$

**N×3D**



# Correspondence to the Real World



# Short-Hand Notation

$$X=((x_1,y_1,z_1),(x_2,y_2,z_2),\cdots,(x_N,y_N,z_N)) \longleftrightarrow |\ \rangle$$

N×3D

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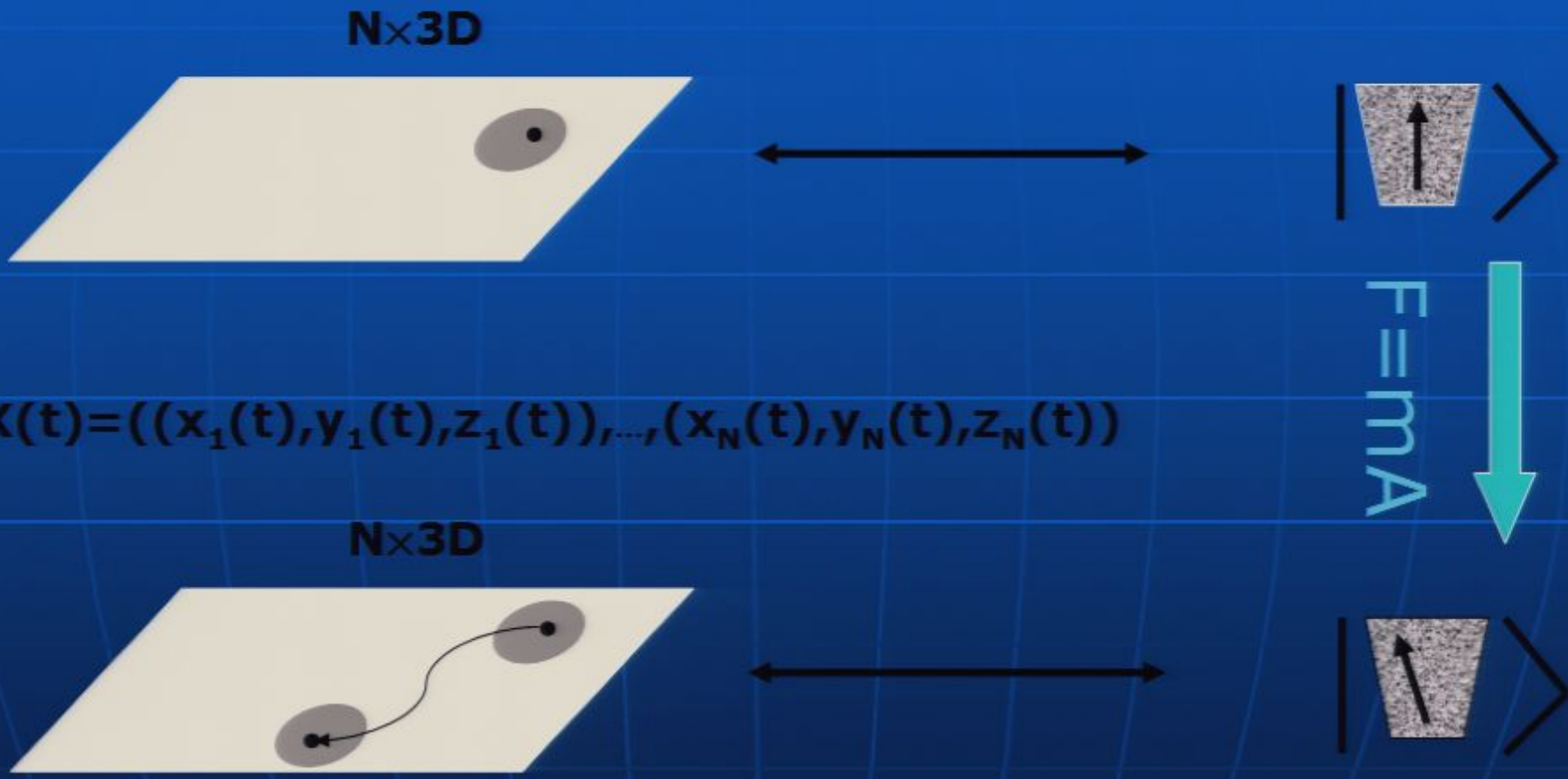


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# Quantum Theory

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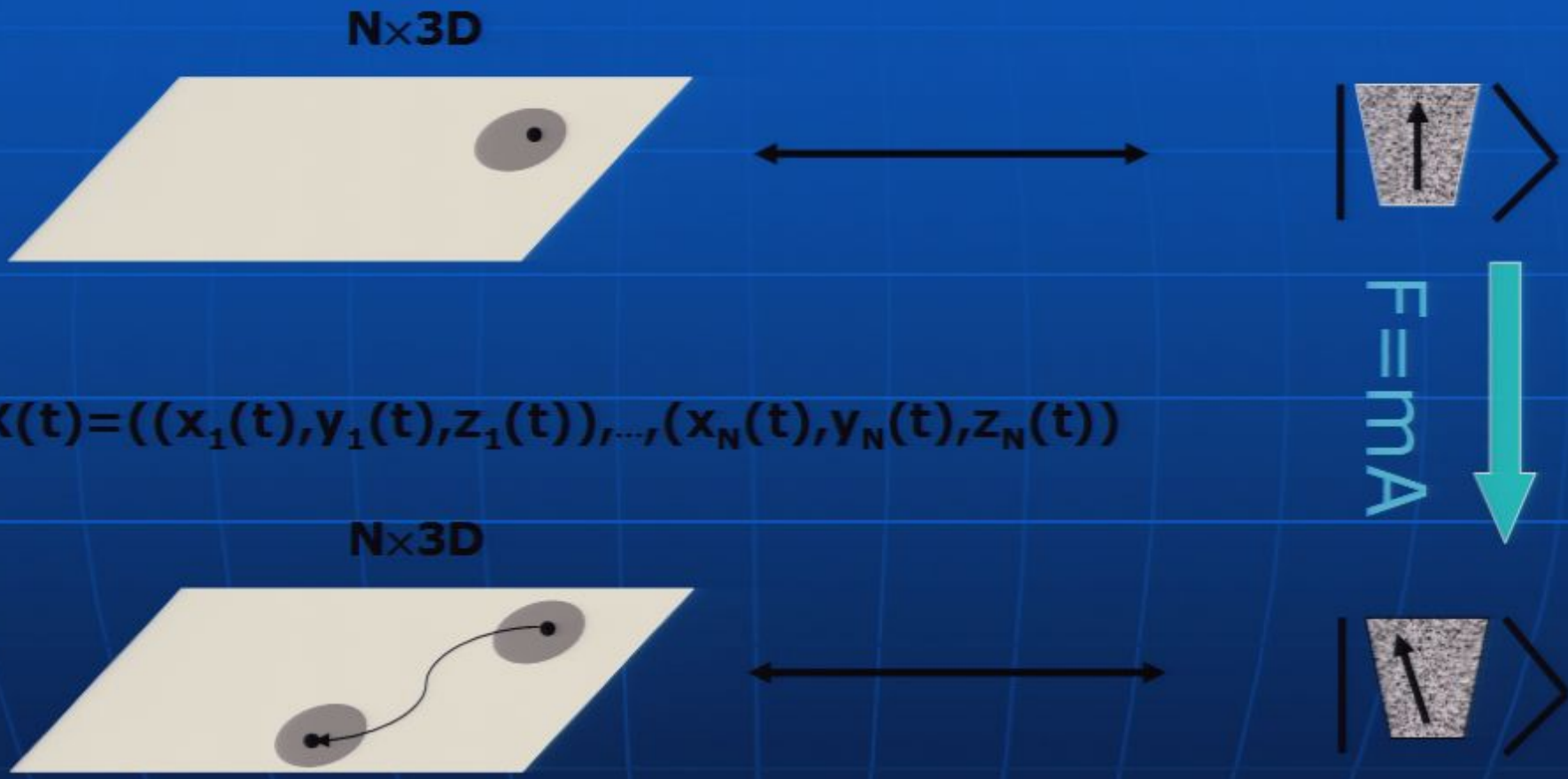


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# Quantum Theory

# Quantum Theory: what's different?

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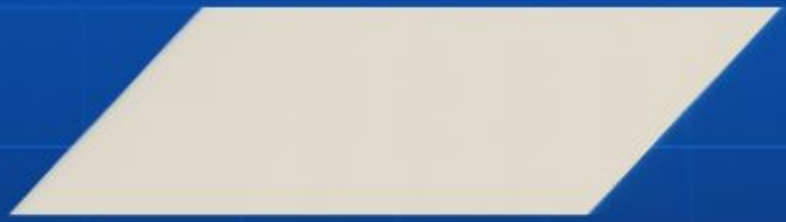


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A state in quantum theory is represented by a complex function $\Psi(X)$ on configuration space, called the wave-function.

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F=mA

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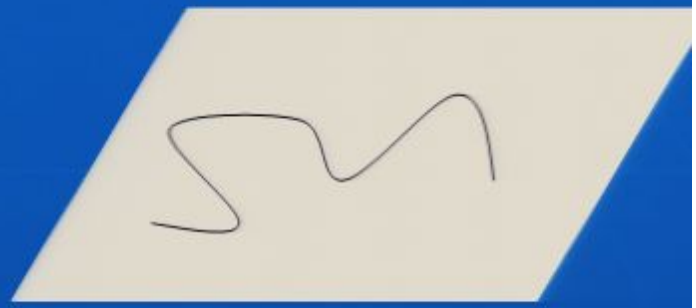
One Particle: $X=(x,y,z)$

$\Psi(x,y,z)$



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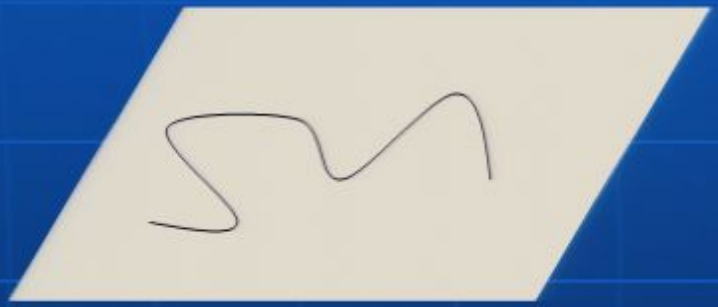

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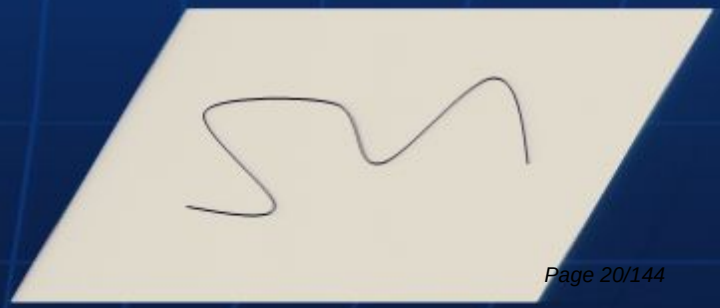
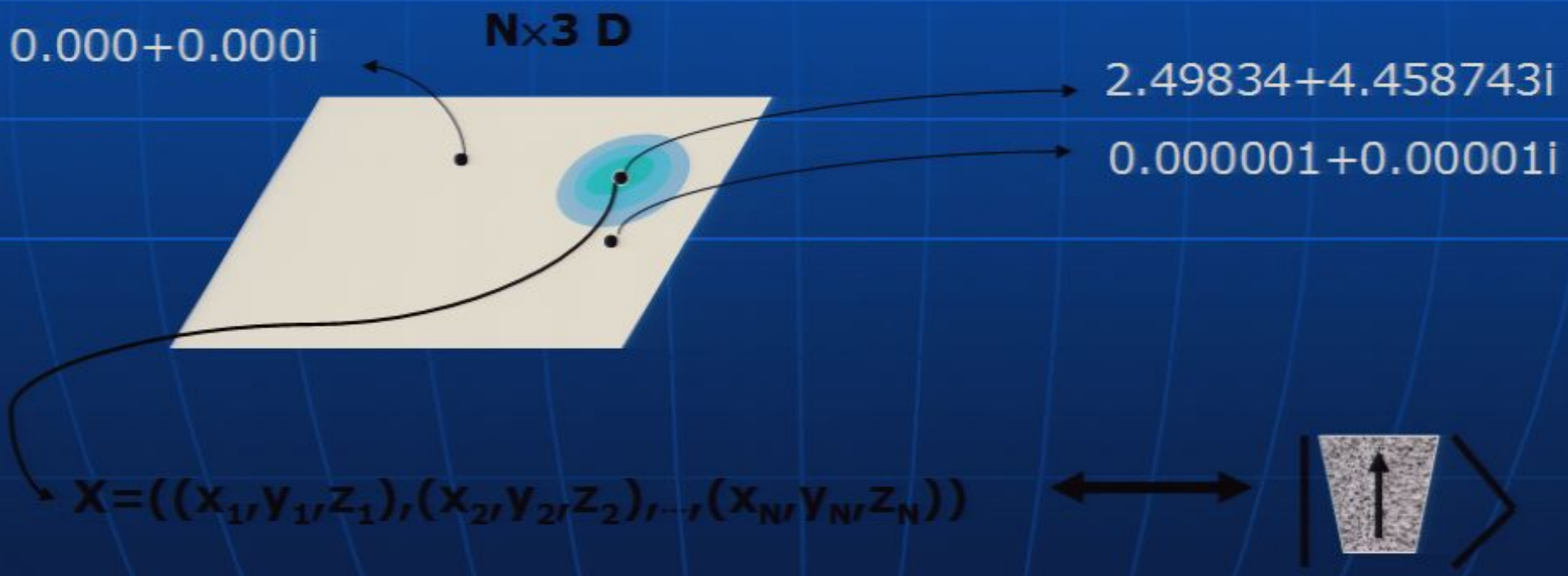
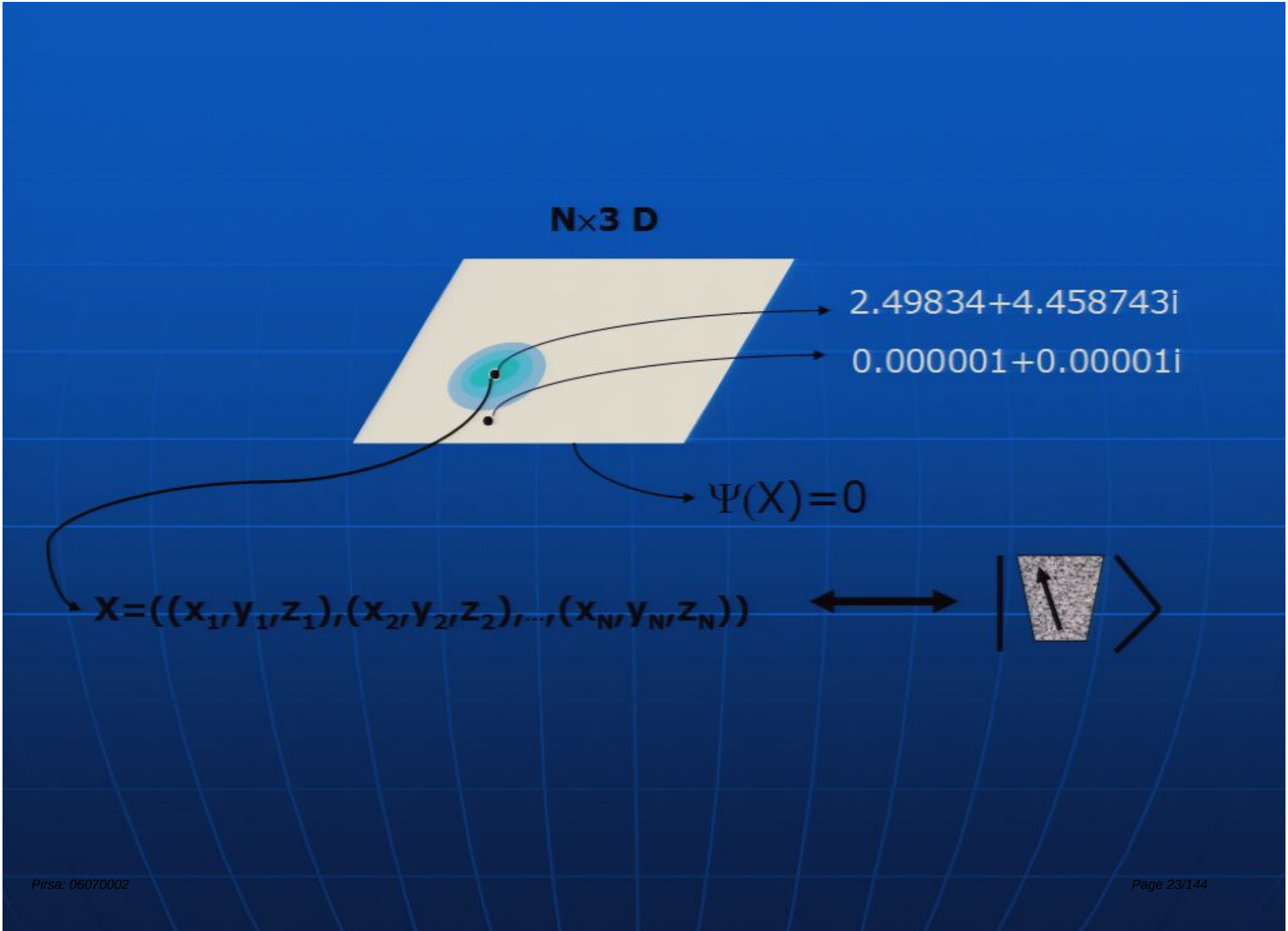


We are going to assume that quantum theory is fundamental and applies to everything, even macroscopic bodies and not just atoms and electrons.

# Correspondence to Reality

Assume that we have a wave-function that is "peaked" around some point X in configuration space.




N×3 D
2.49834+4.458743i
0.000001+0.00001i
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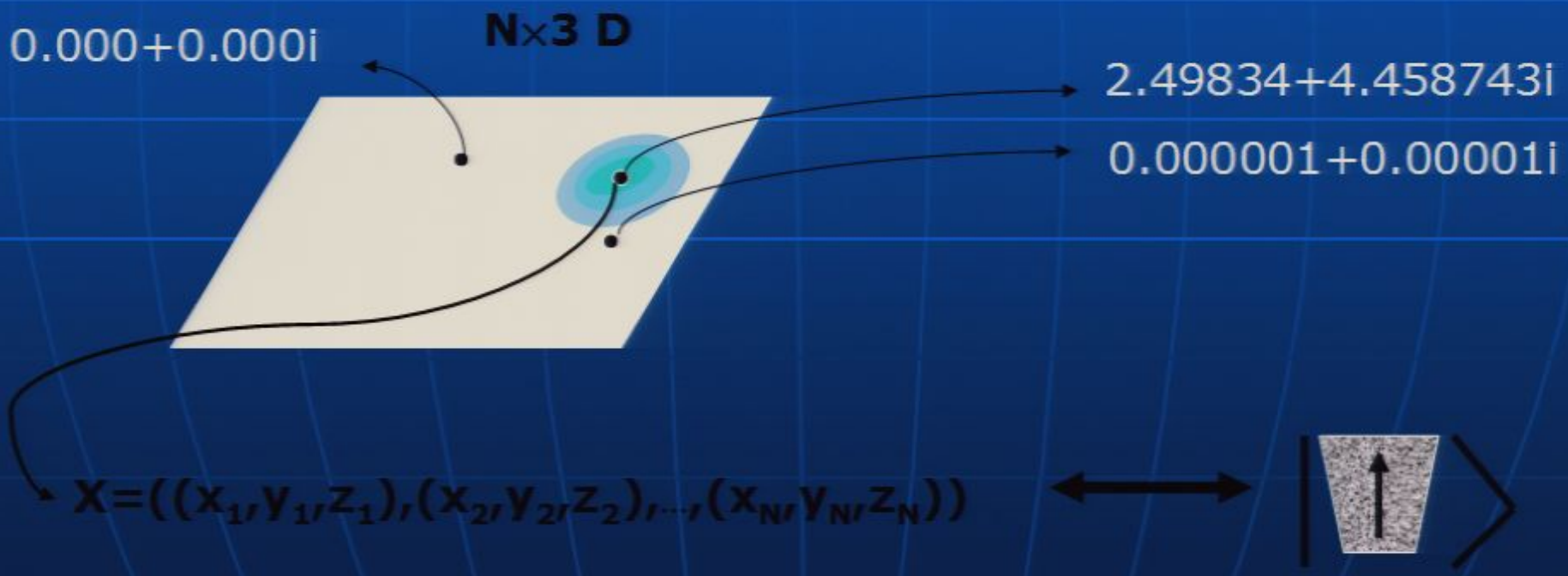

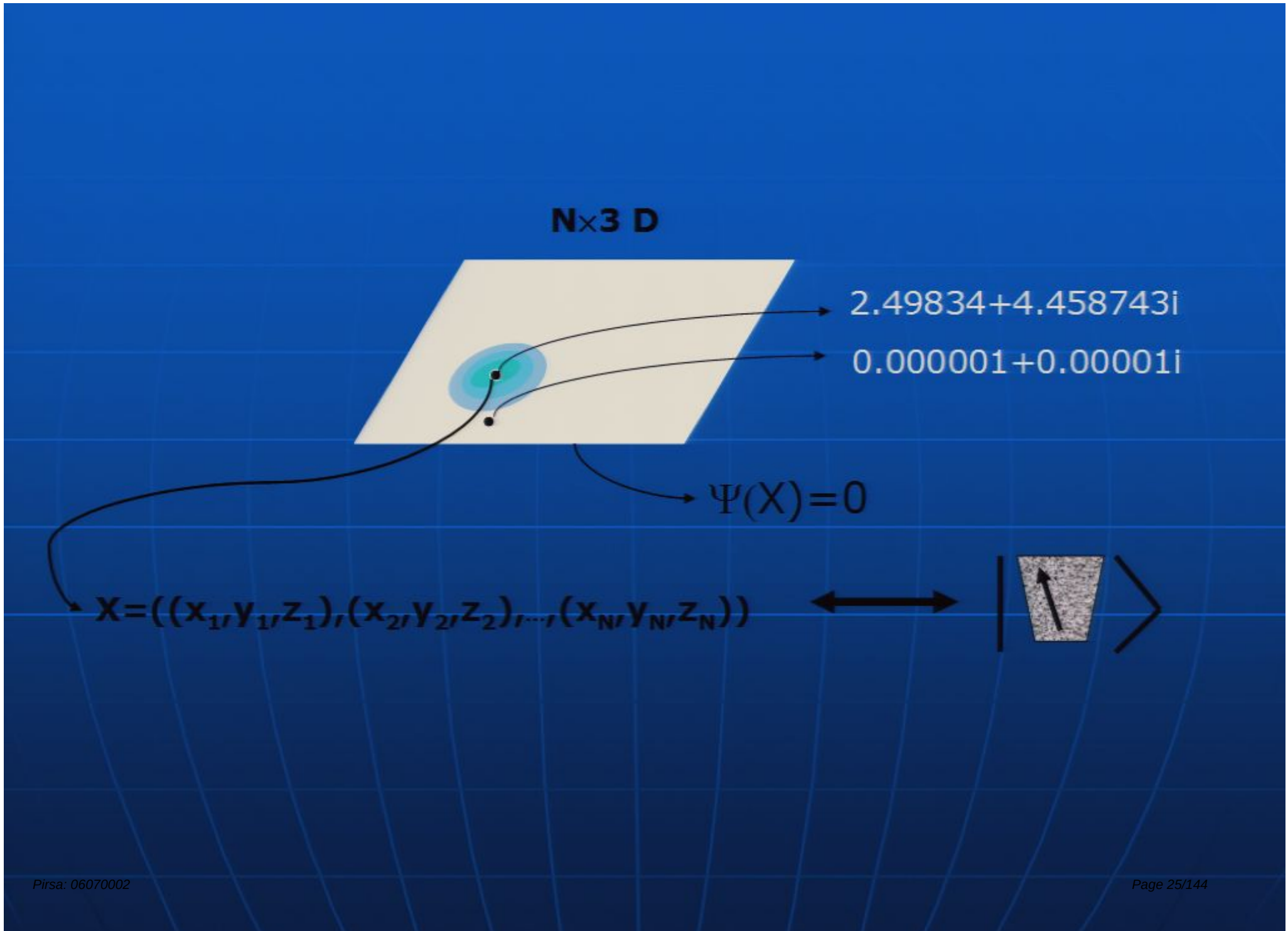
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$$\alpha\Psi_1+\beta\Psi_2$$

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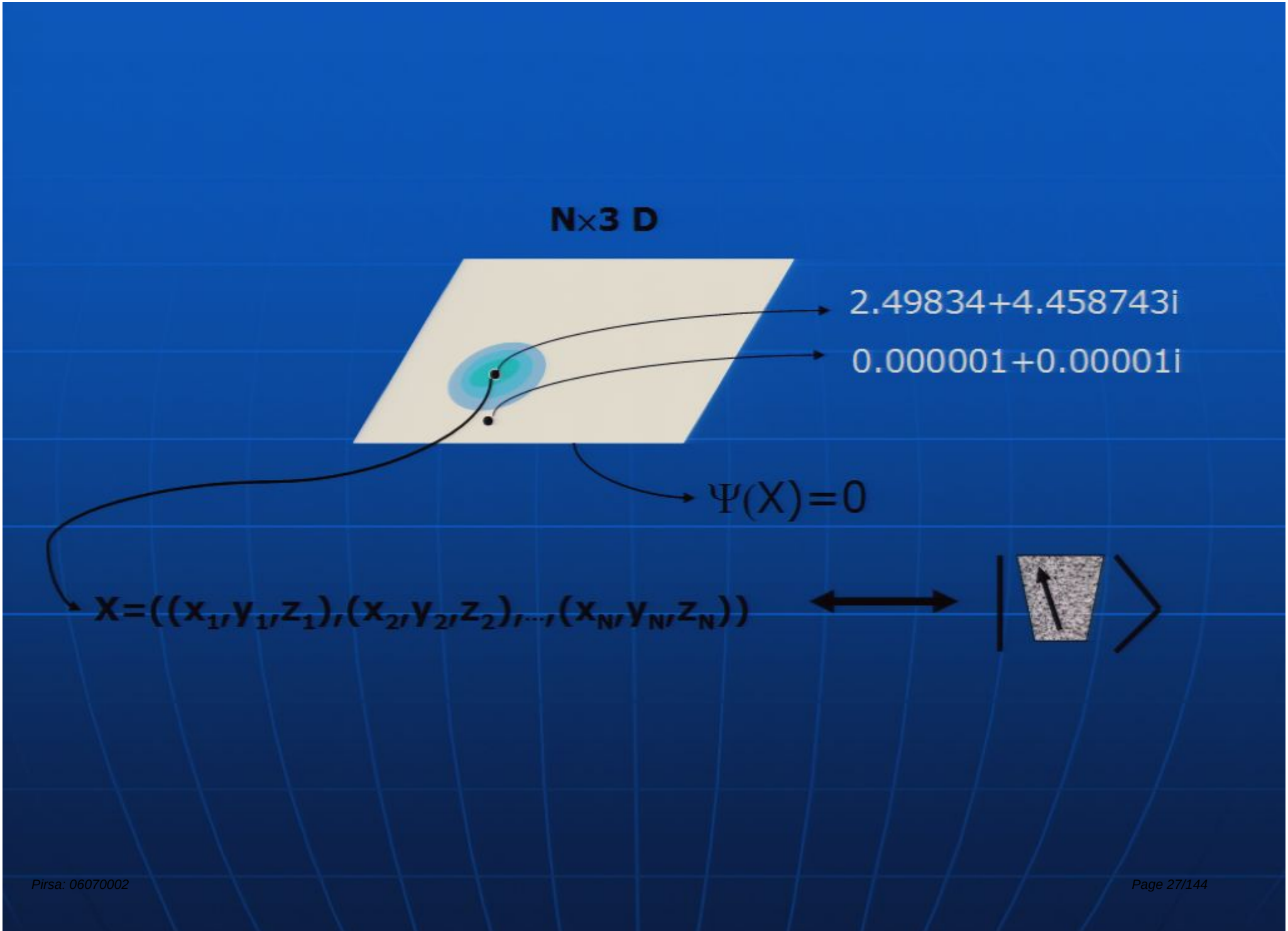
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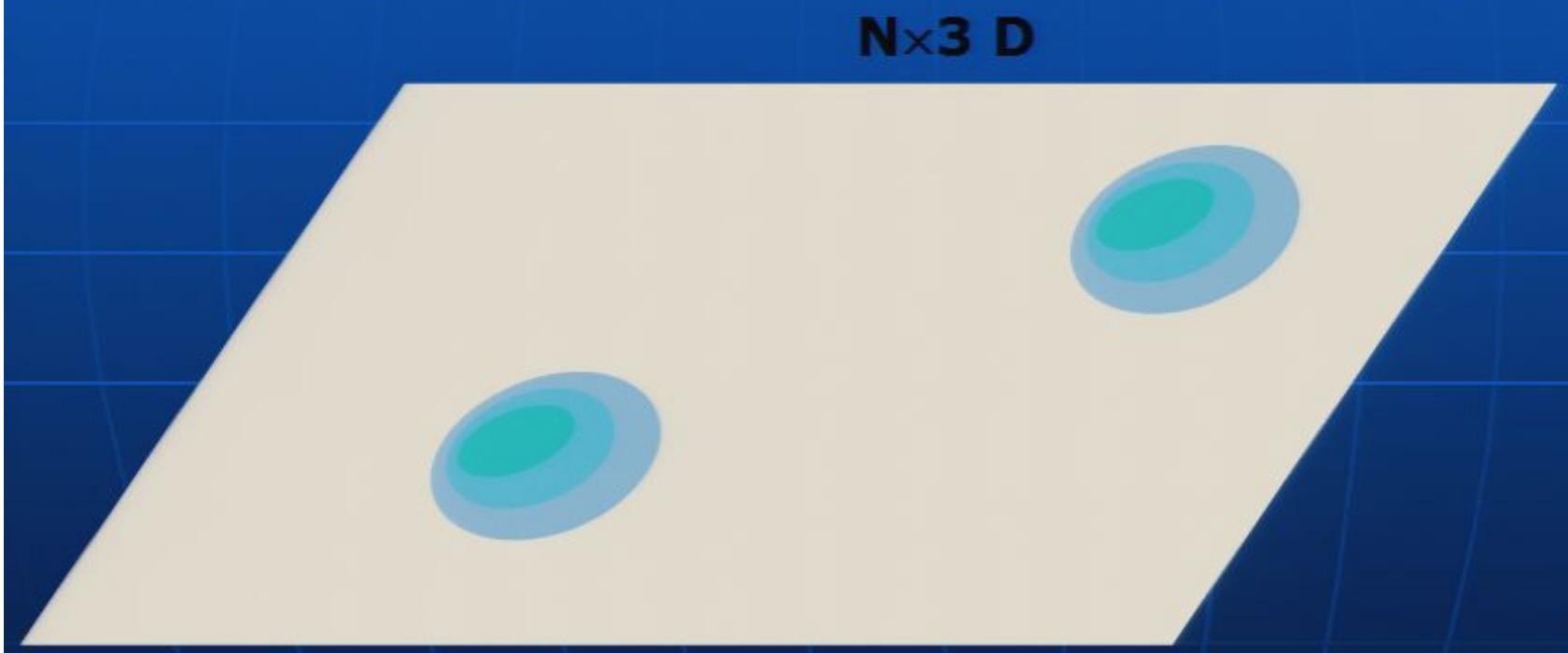

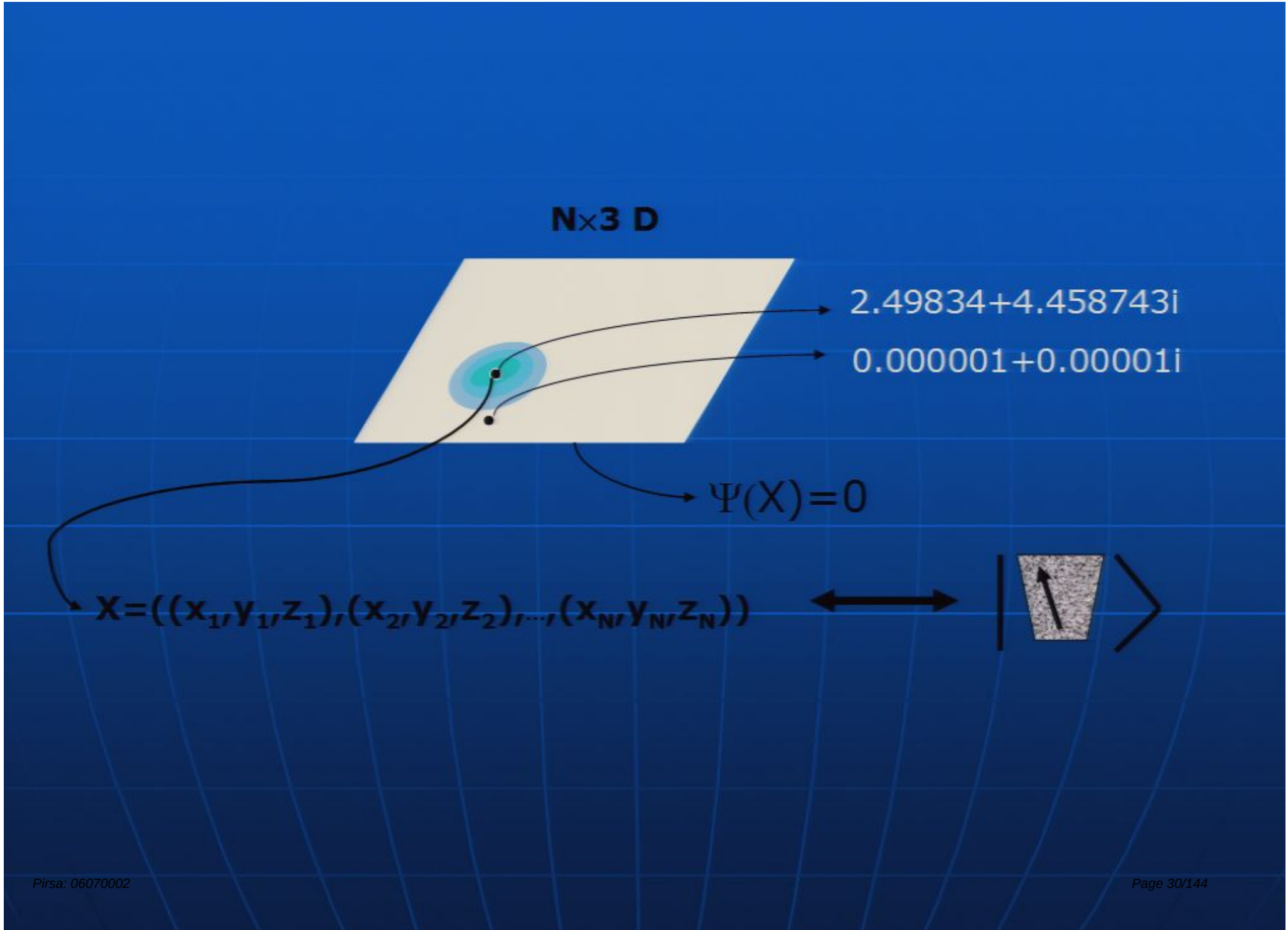
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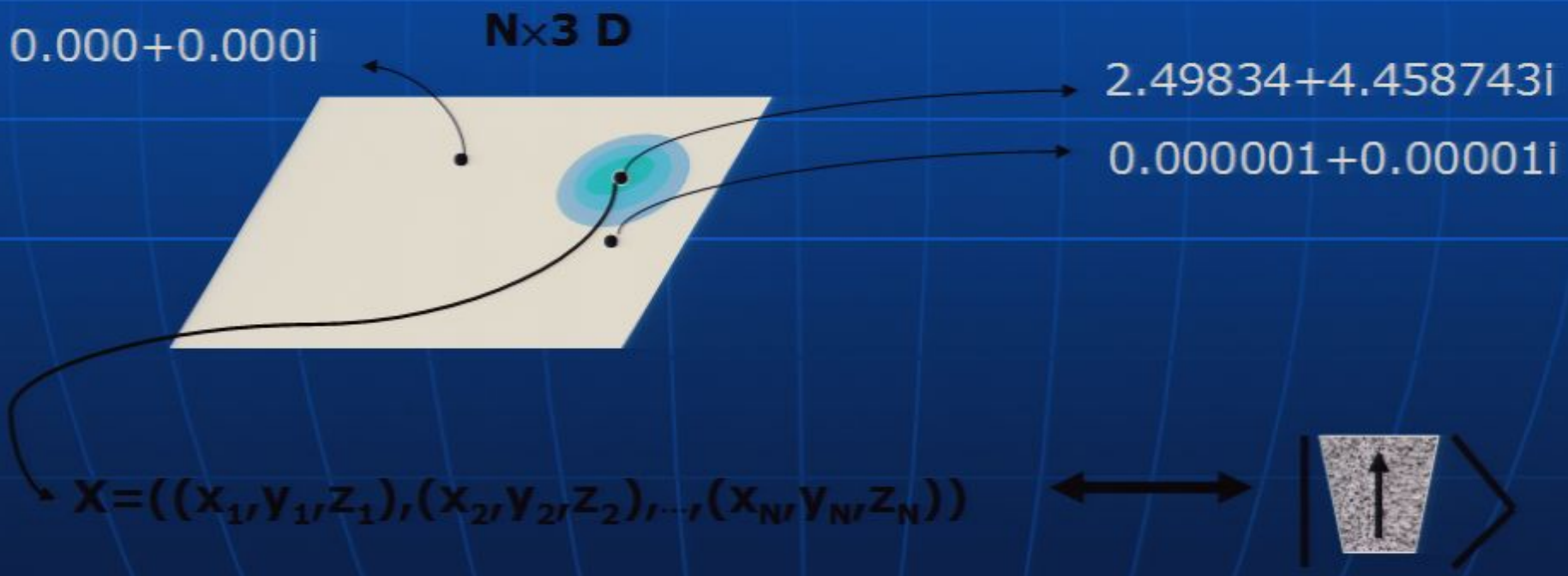

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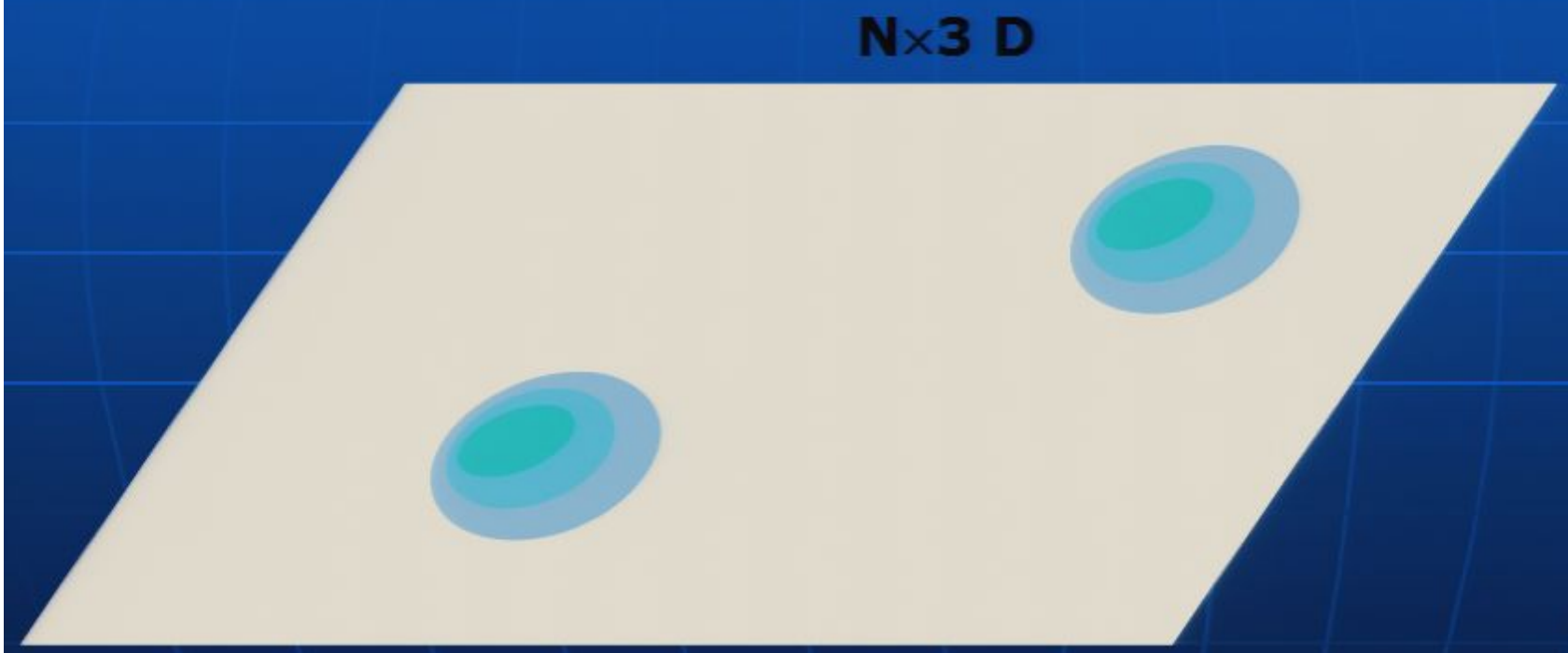

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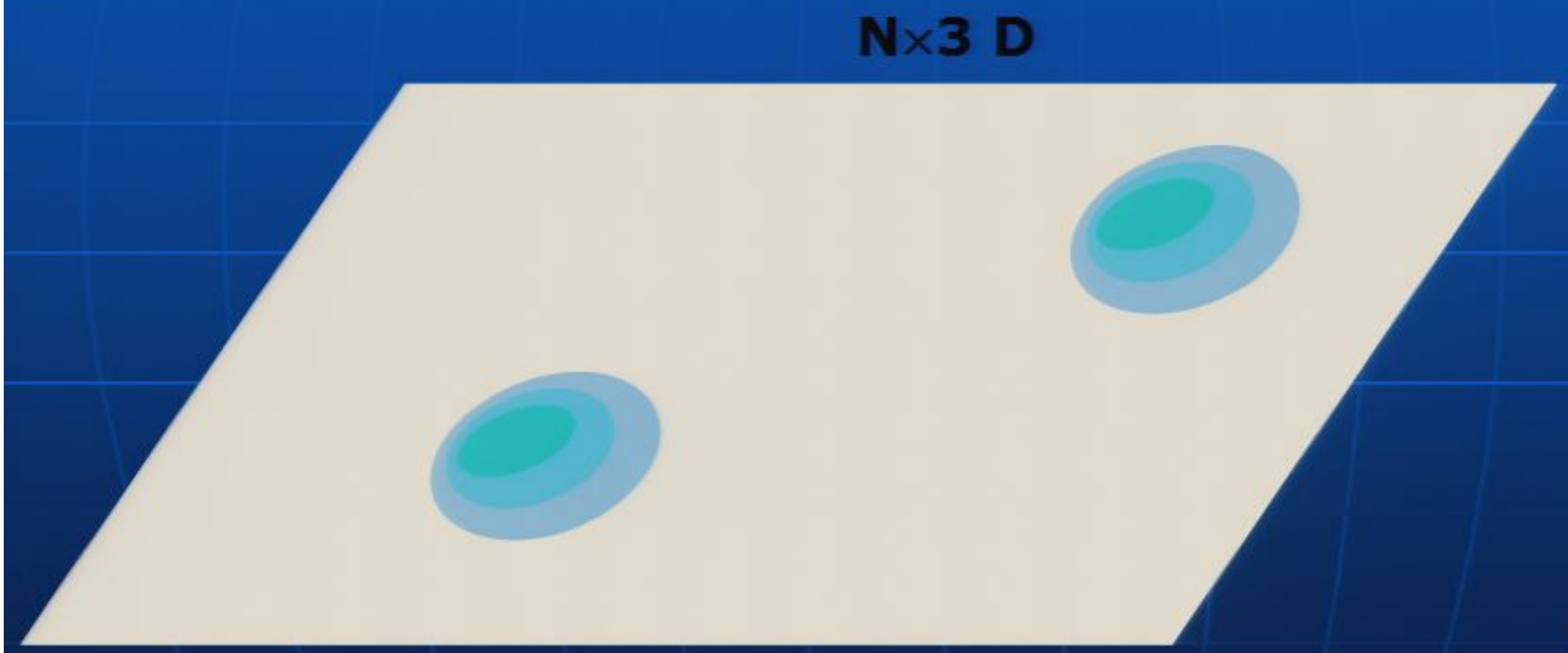

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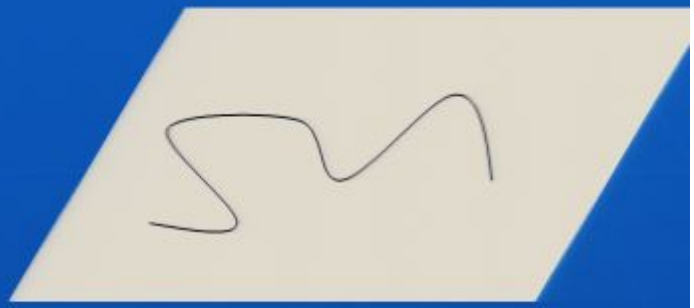

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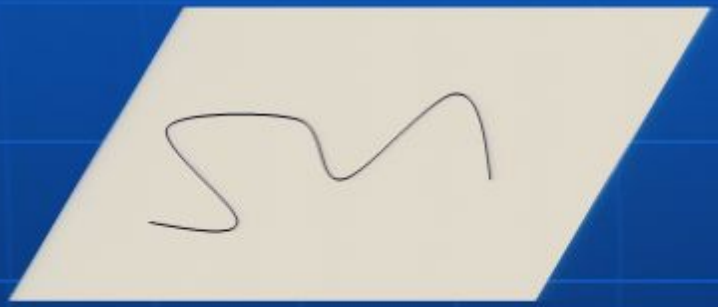

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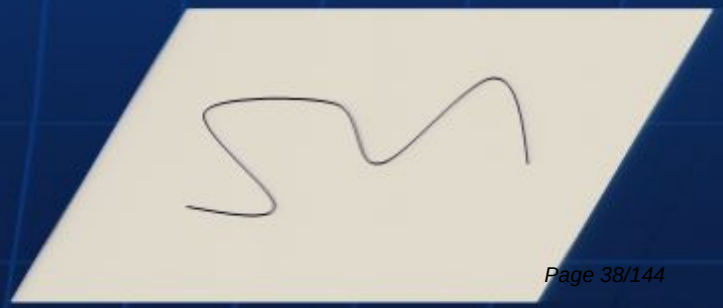

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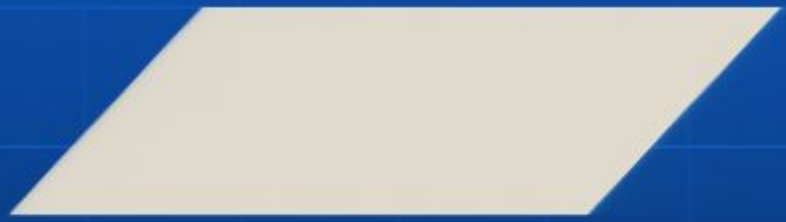


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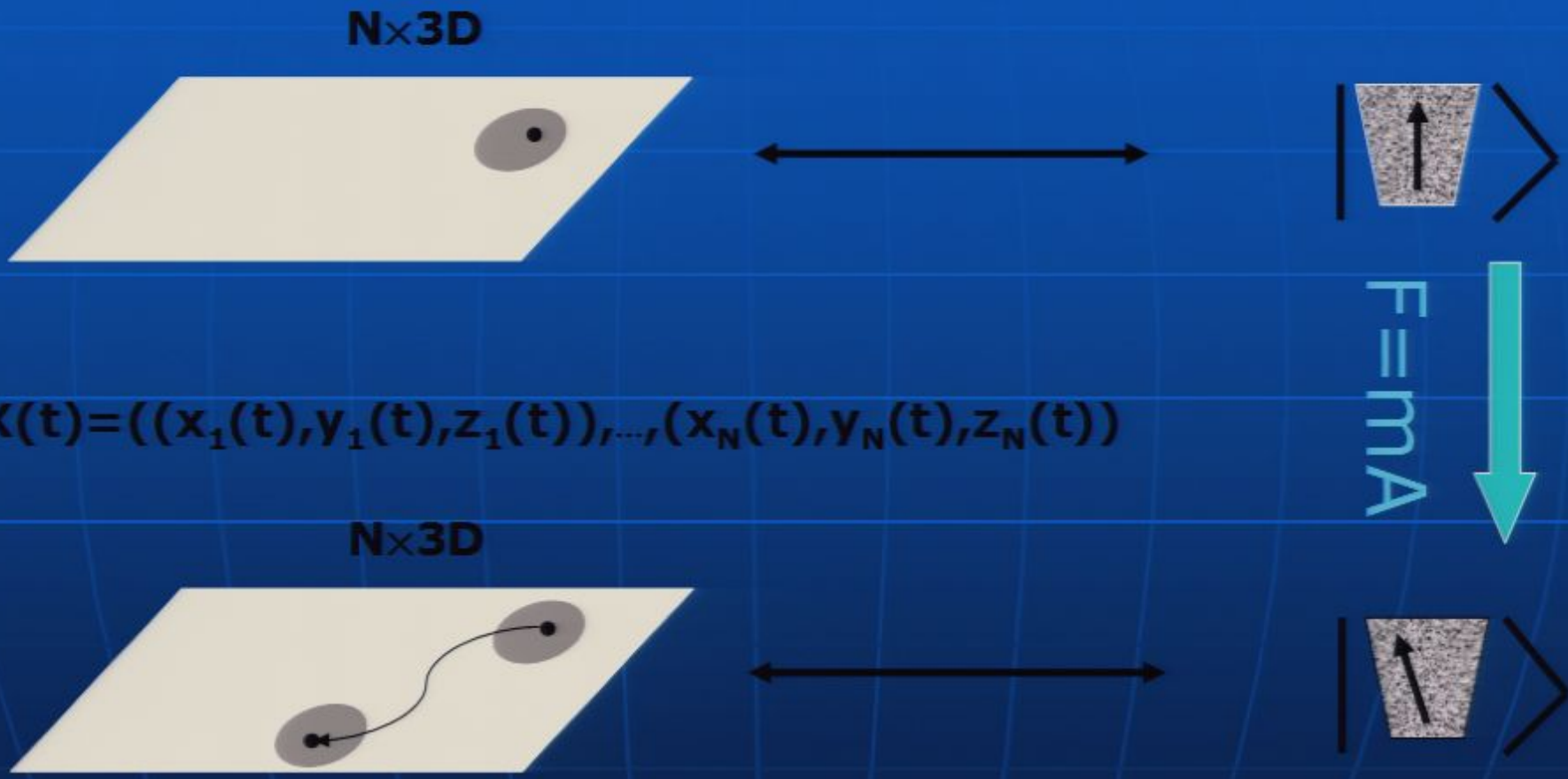


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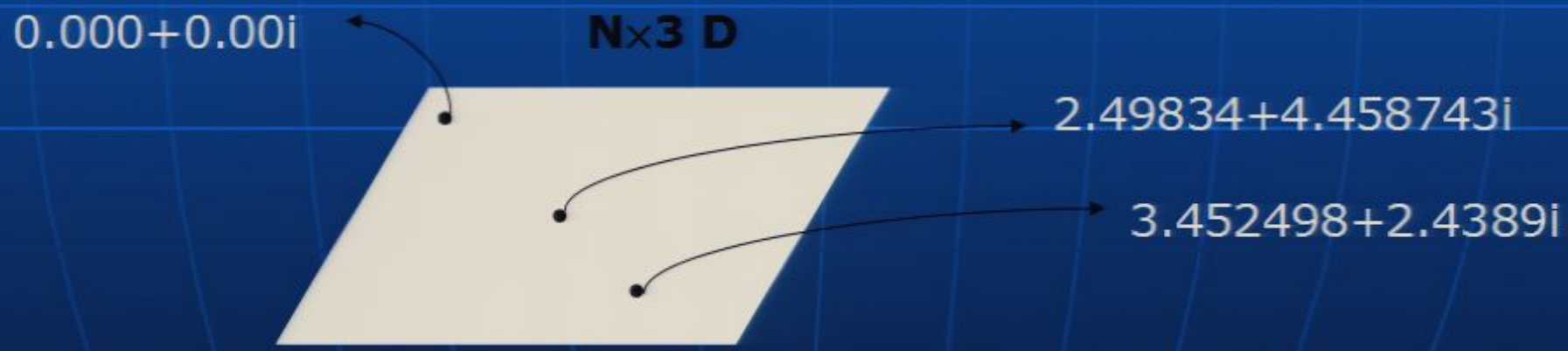

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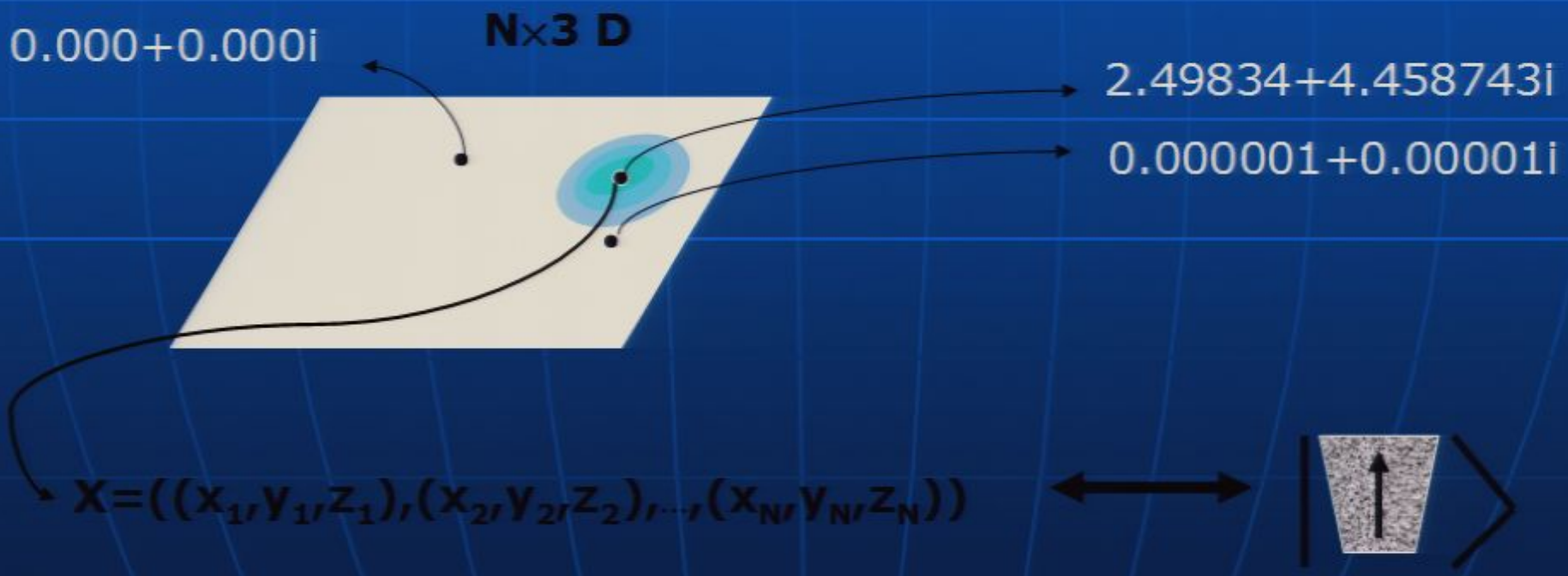

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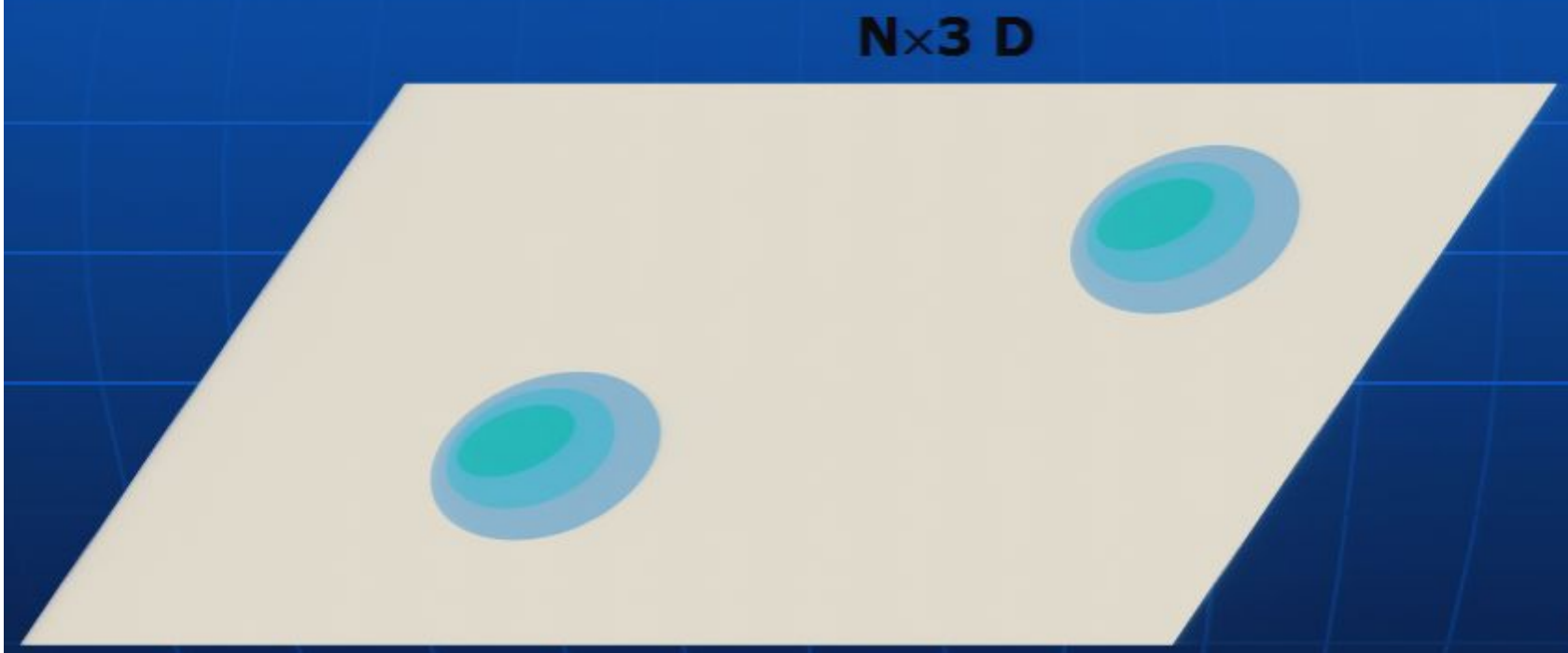

Maybe the laws of quantum theory will make it unlikely for these strange states to occur.
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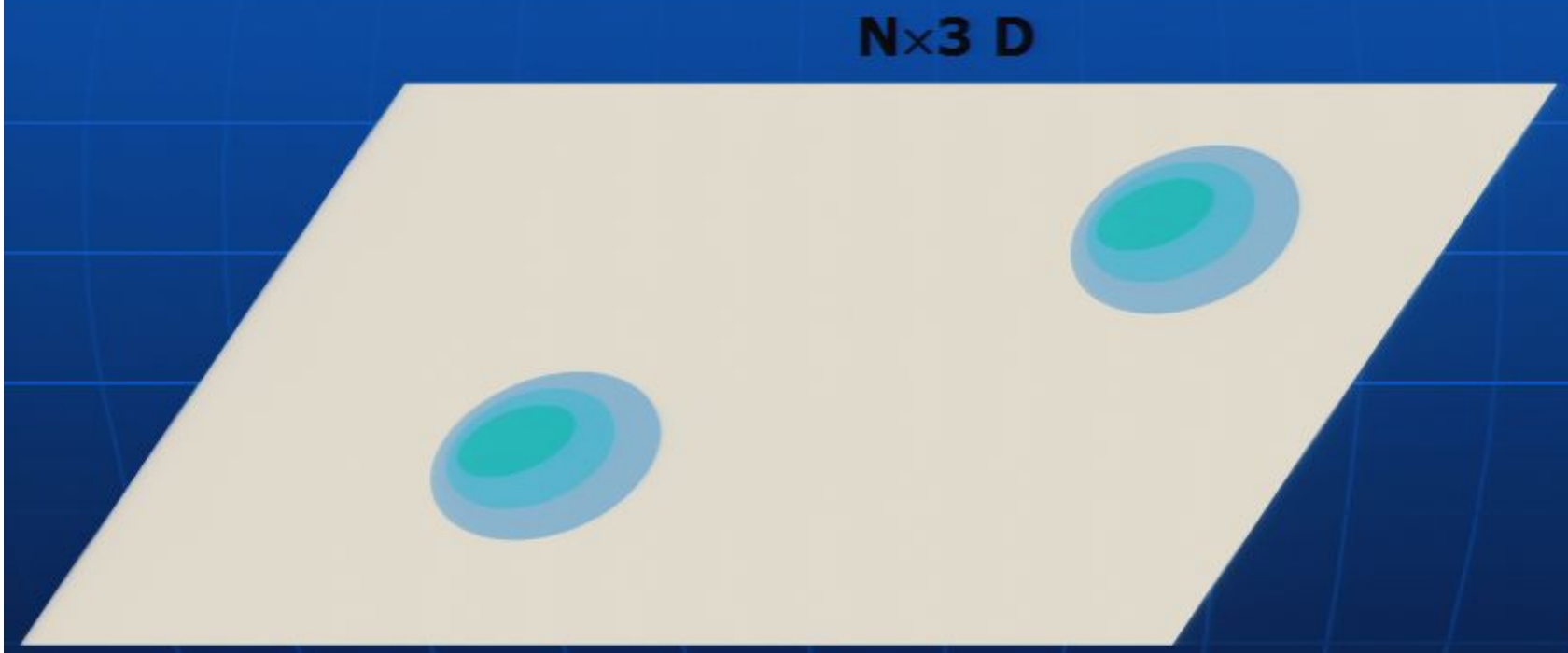

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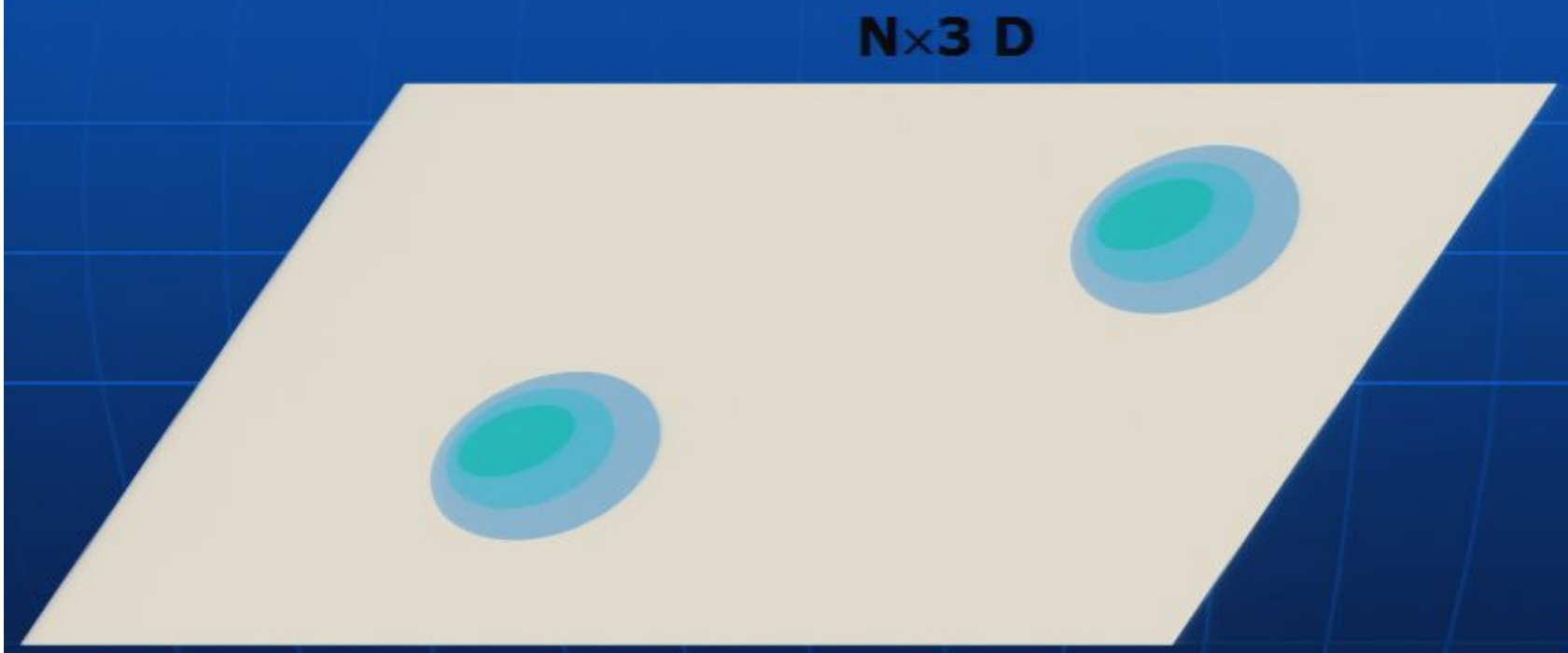

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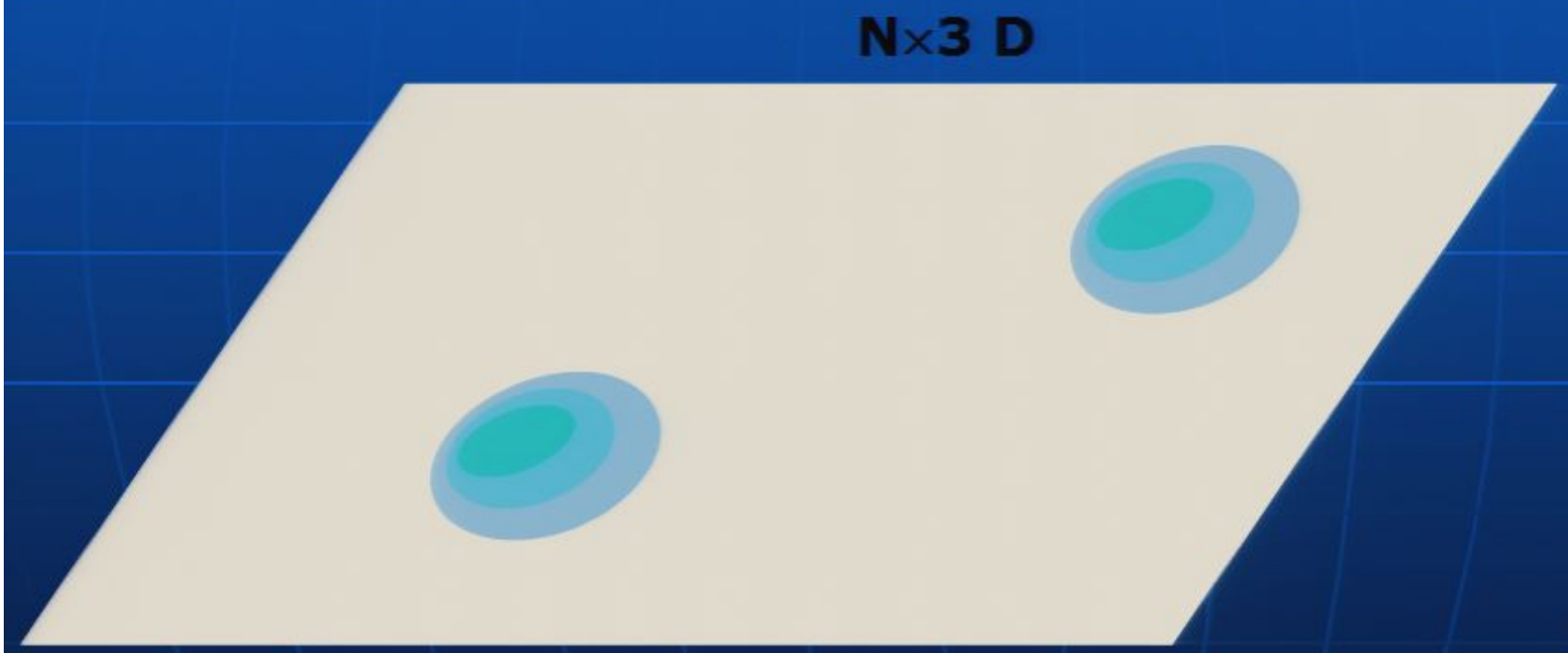

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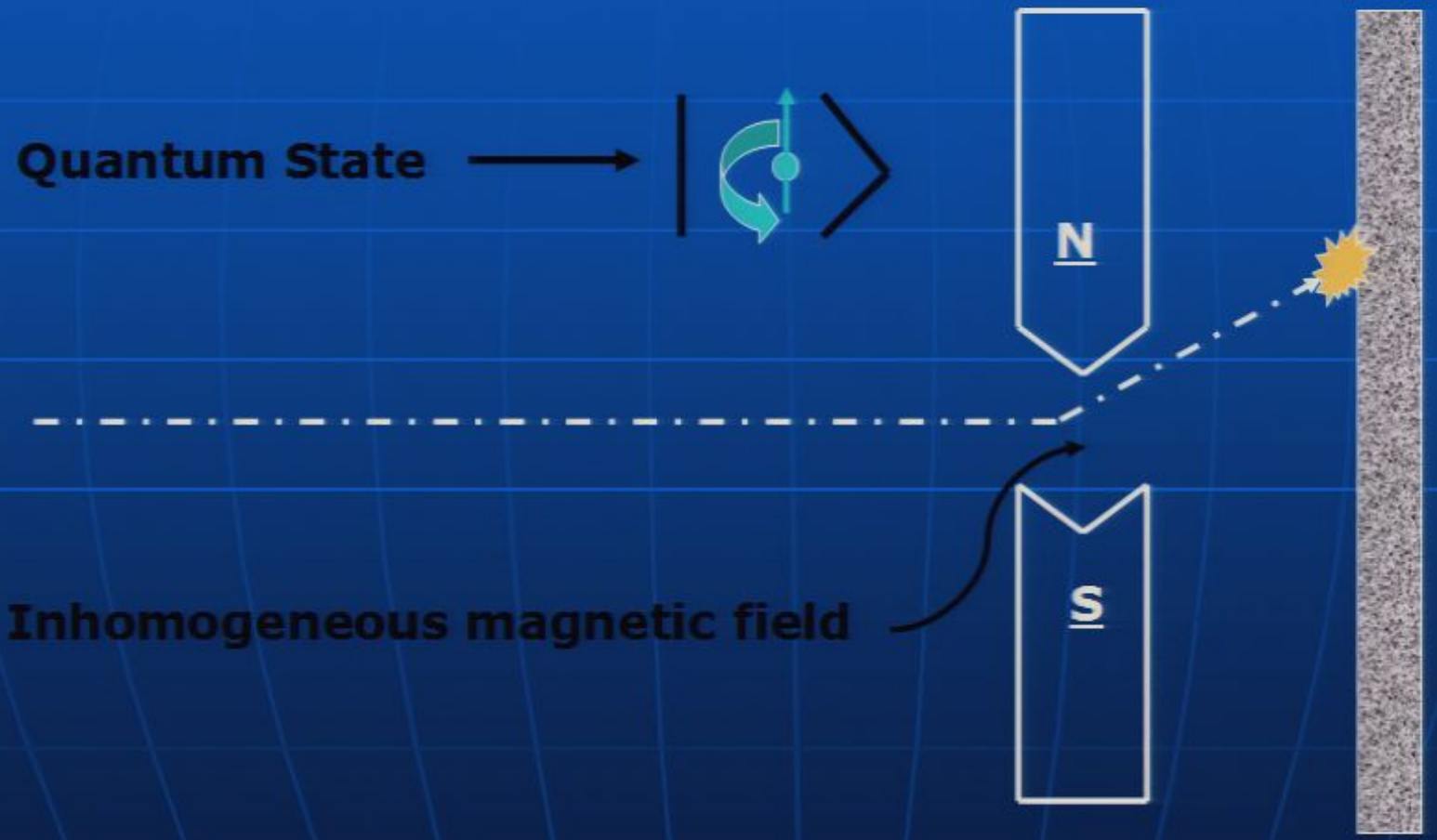
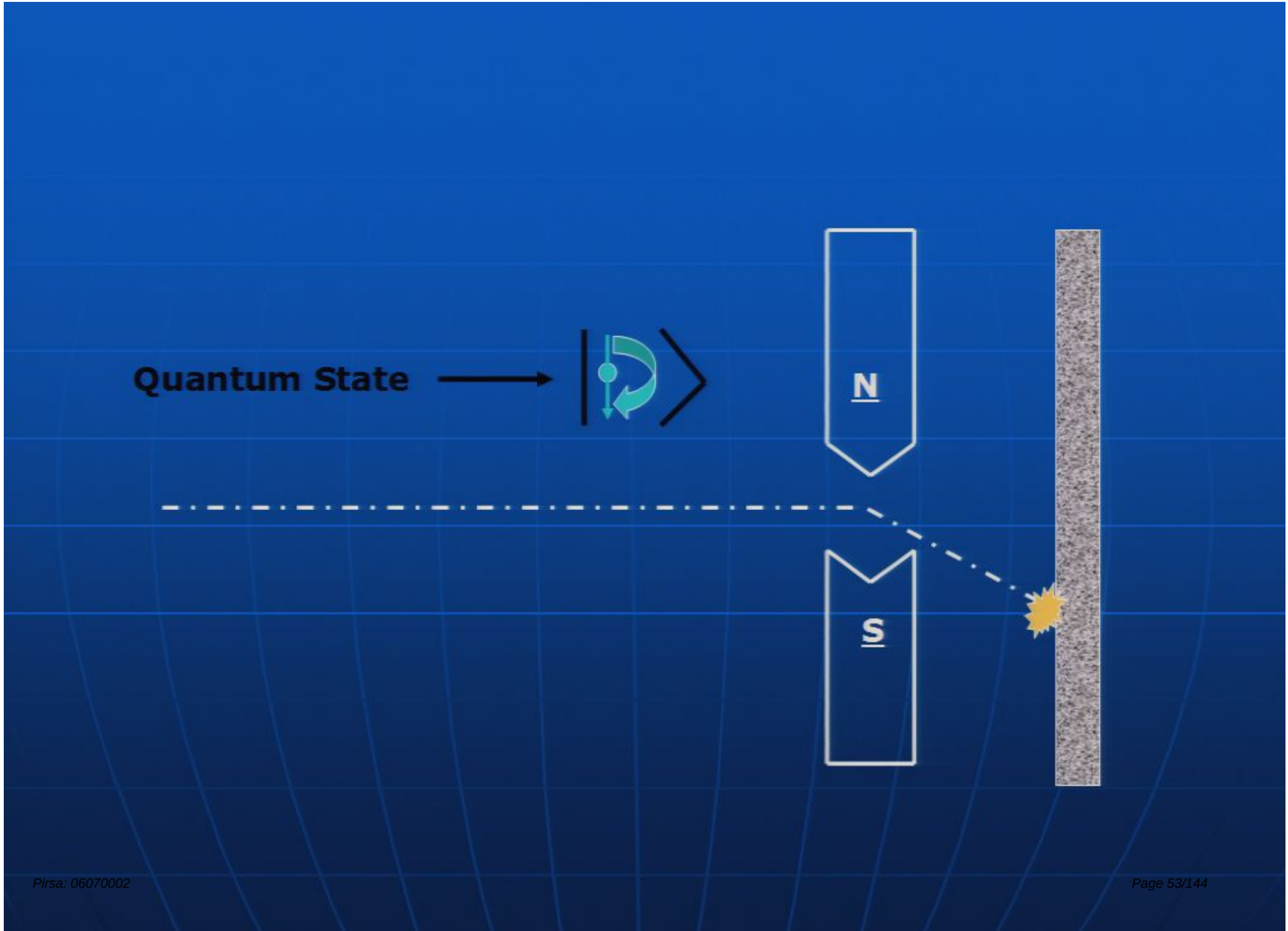
# Quantum Measurement Theory

Example: measurement of spin




Quantum State
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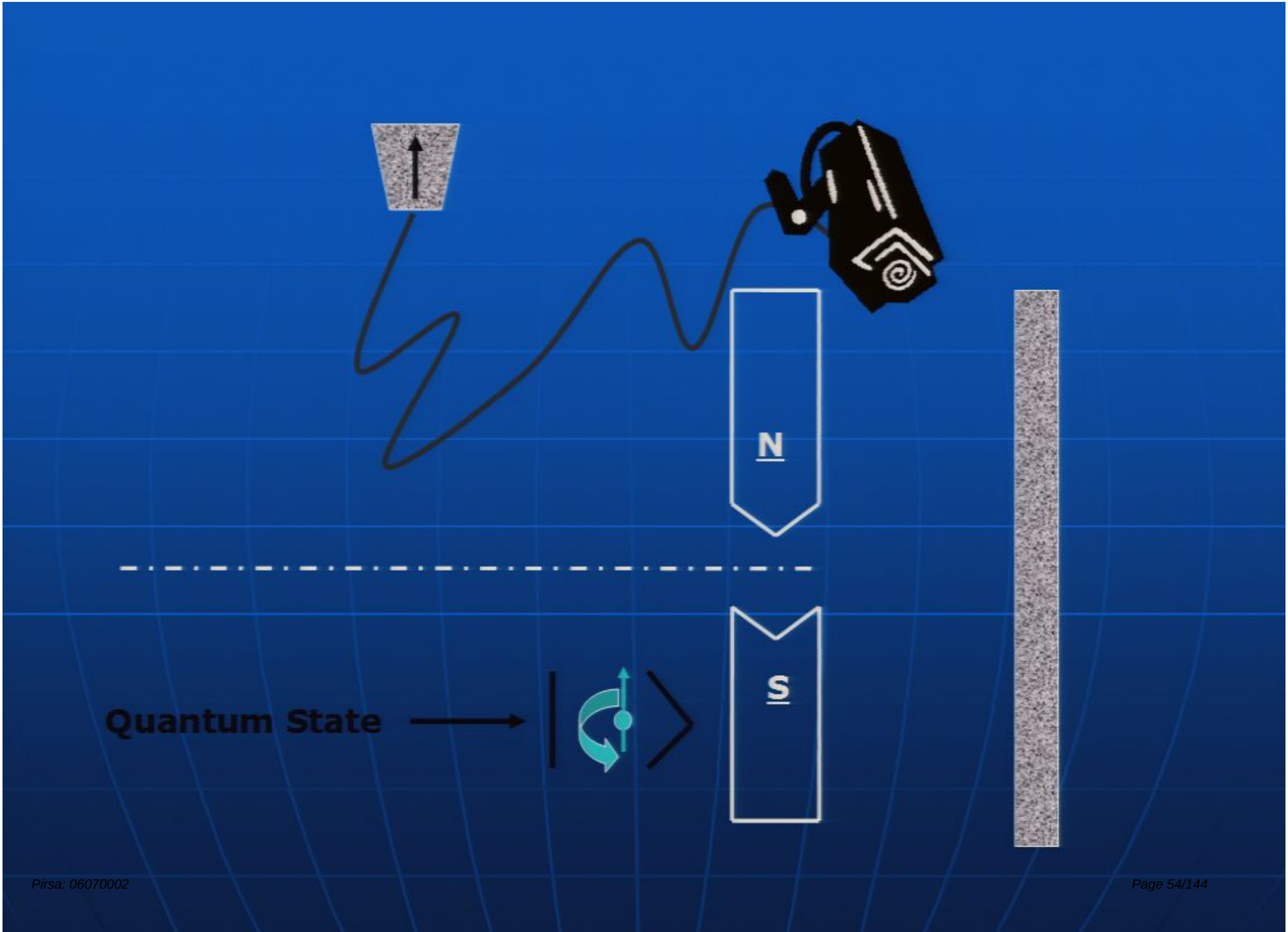
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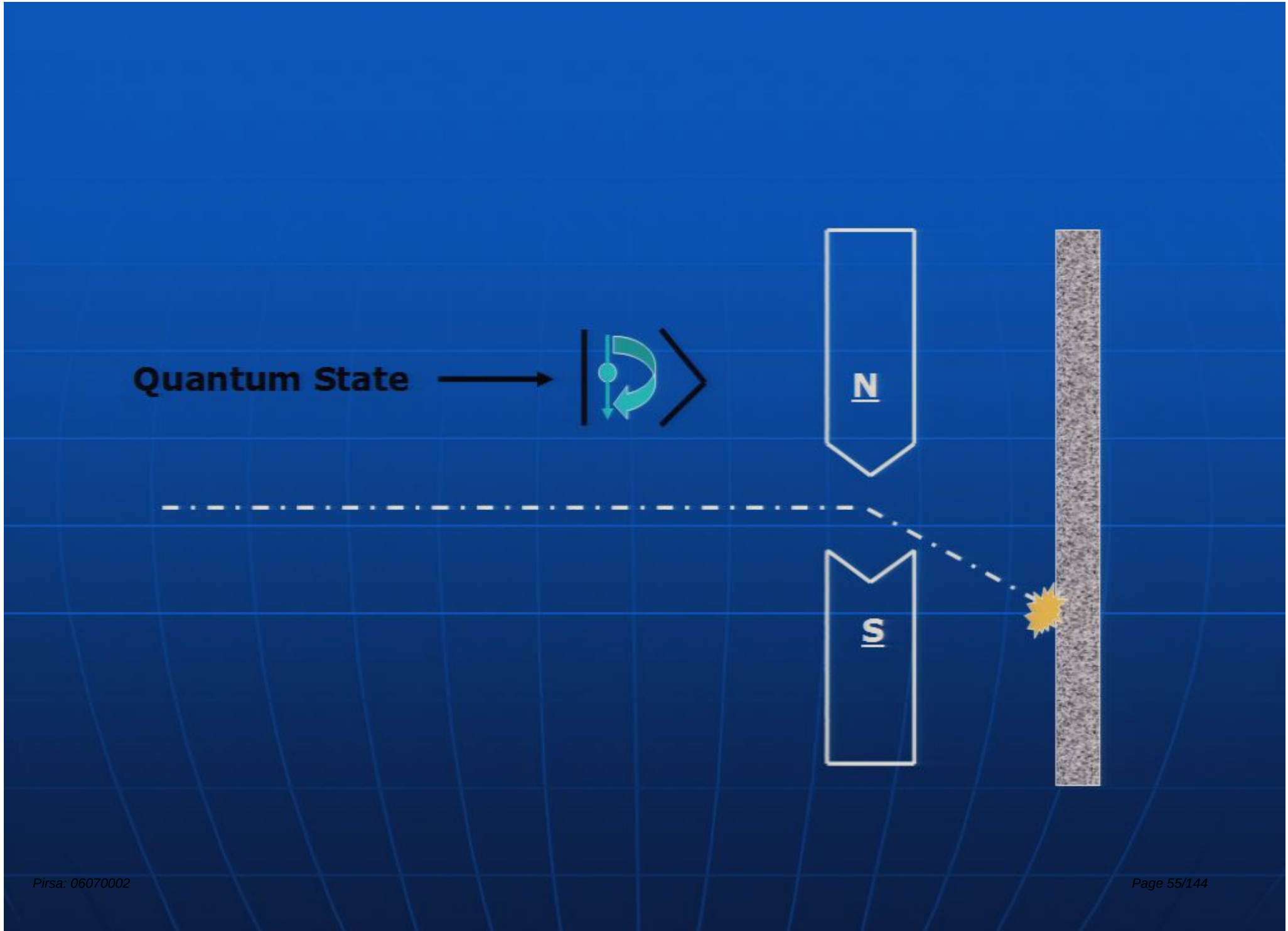
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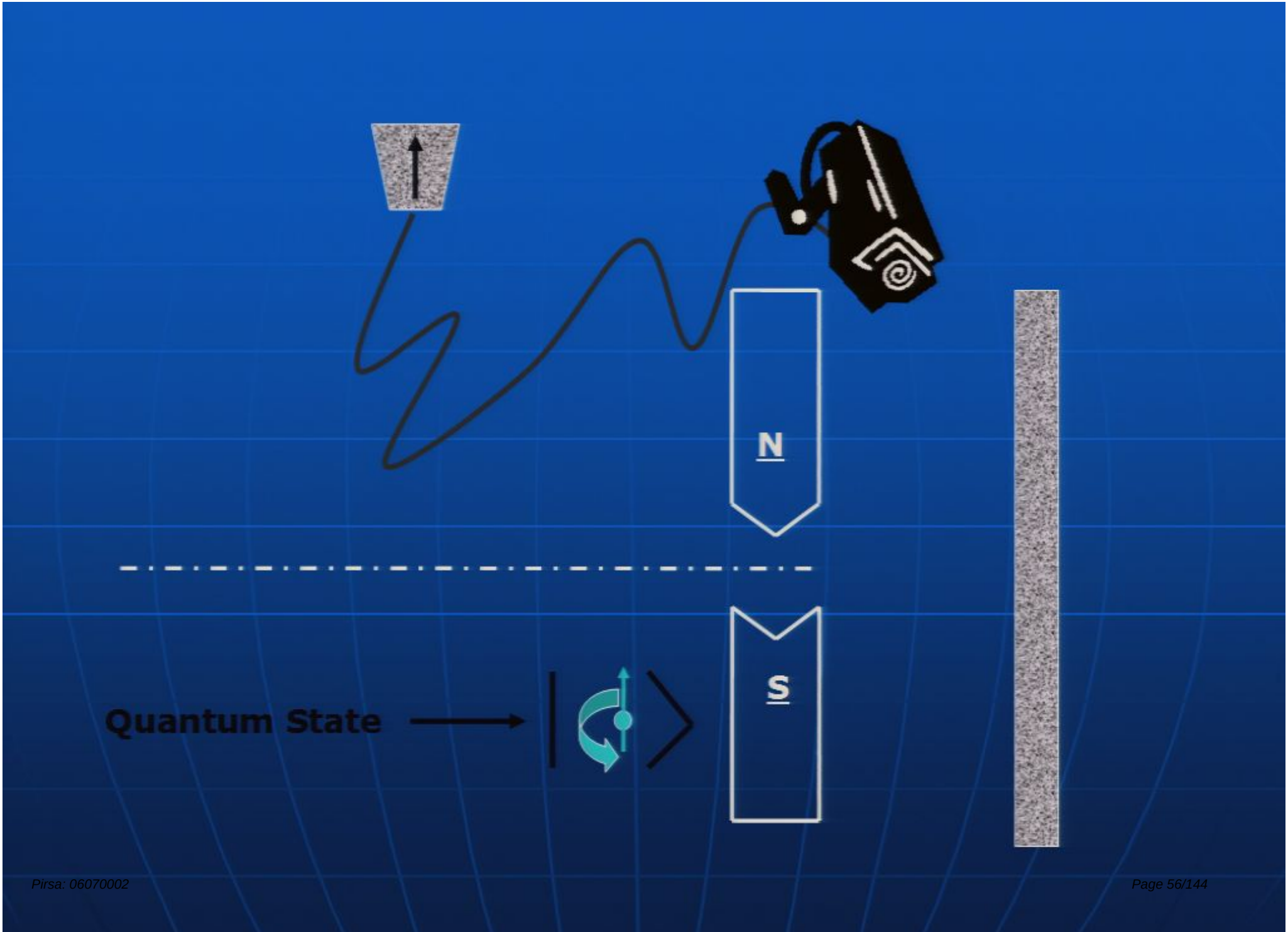
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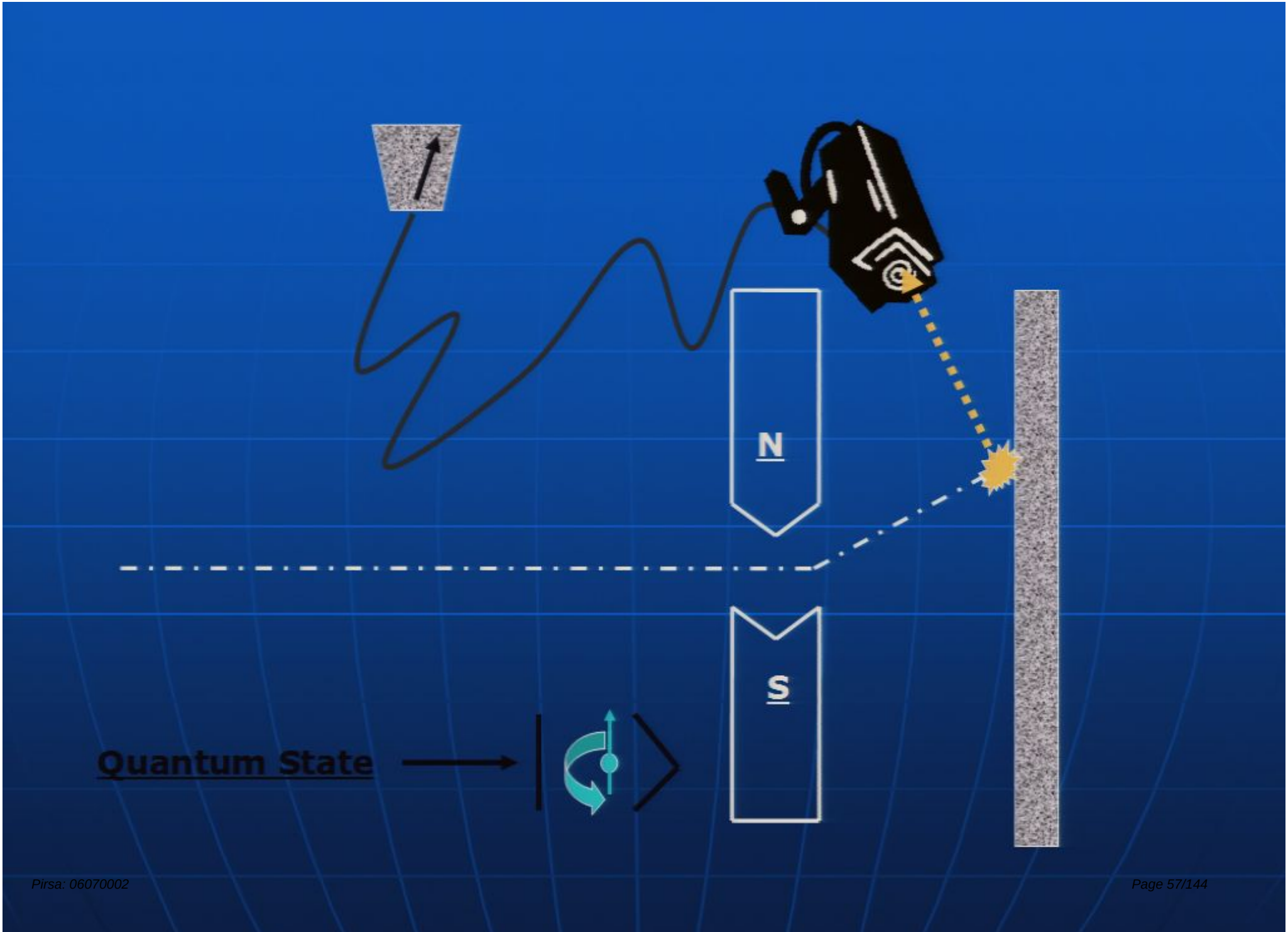
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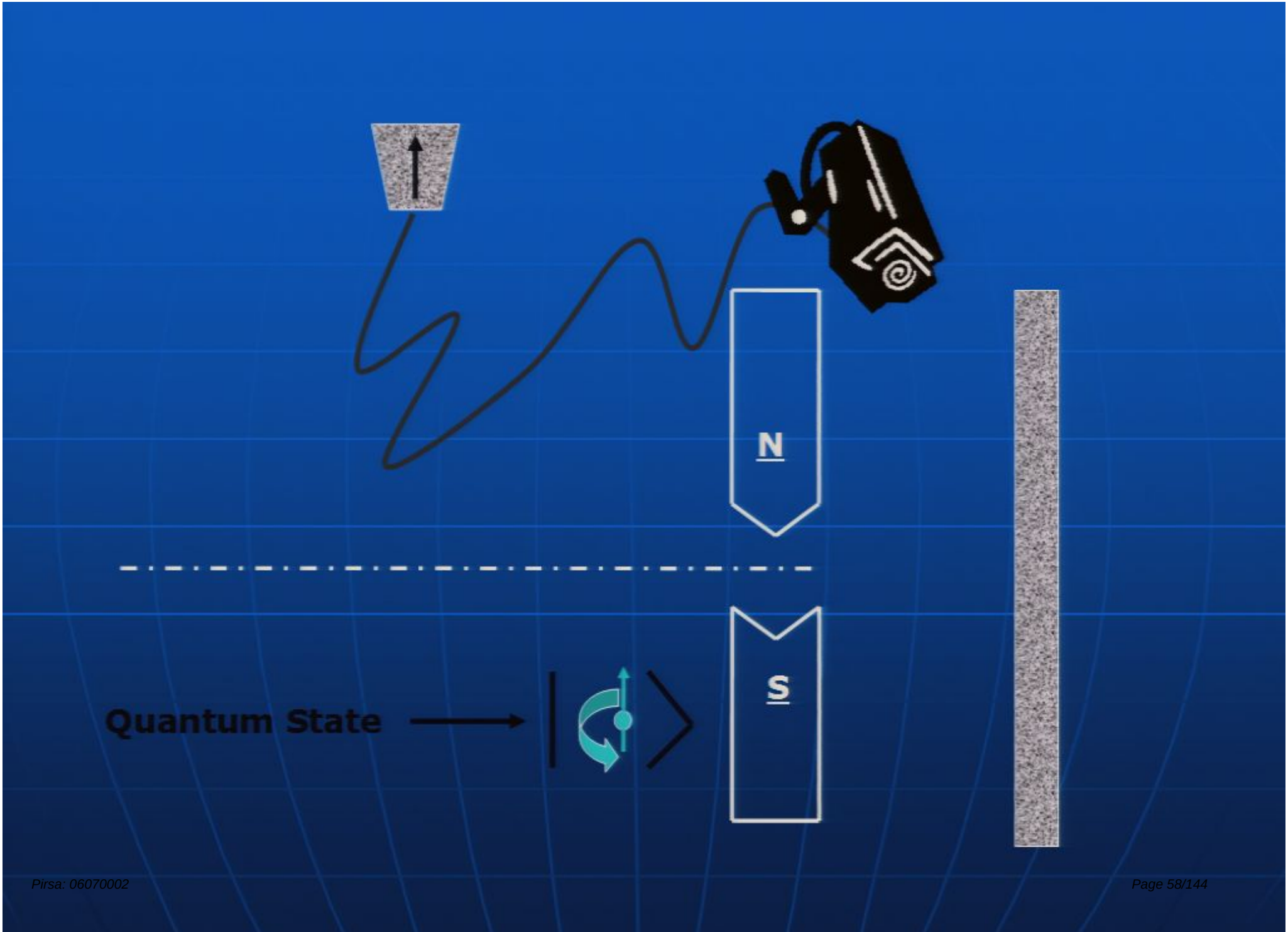
Quantum State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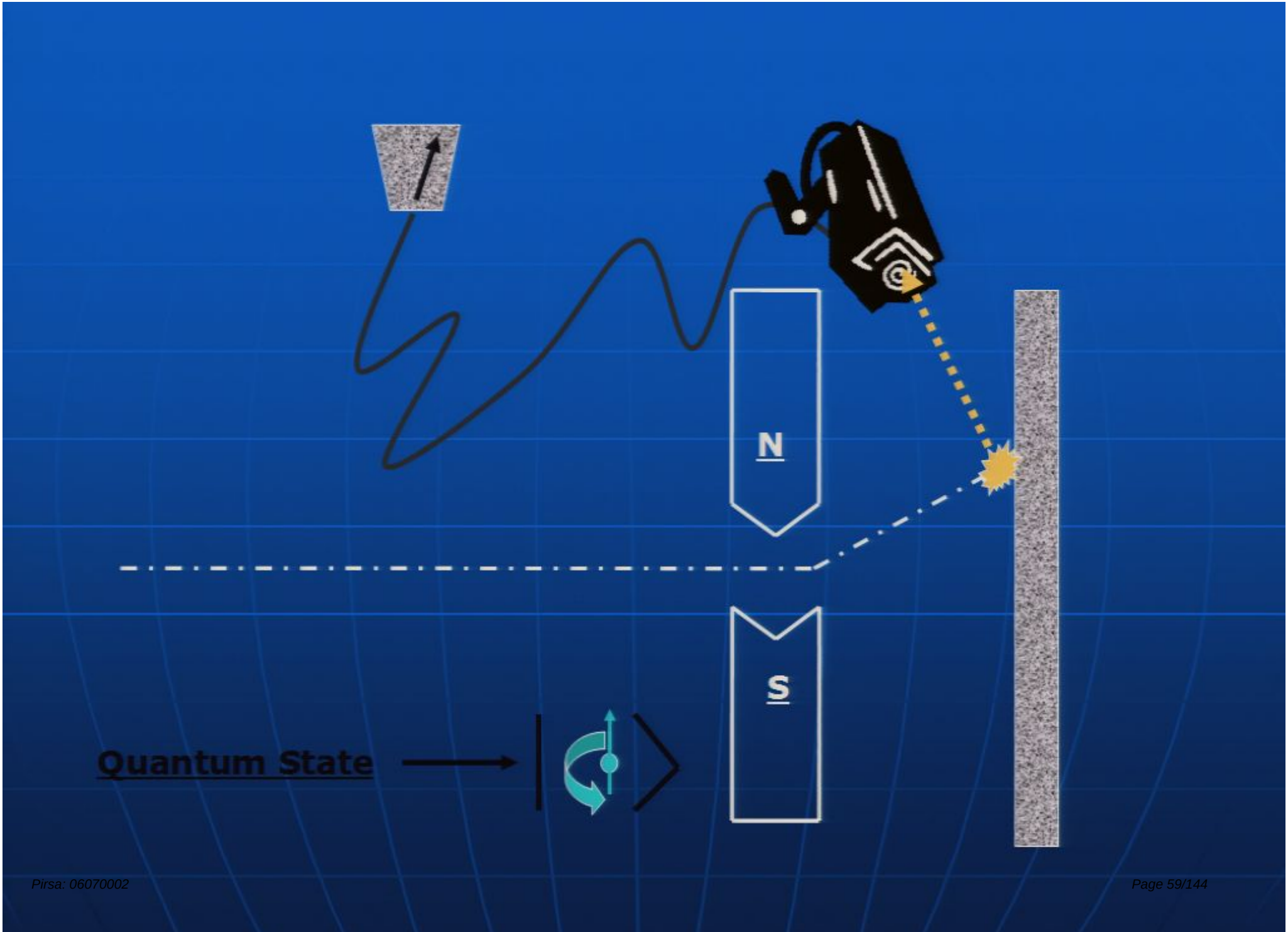
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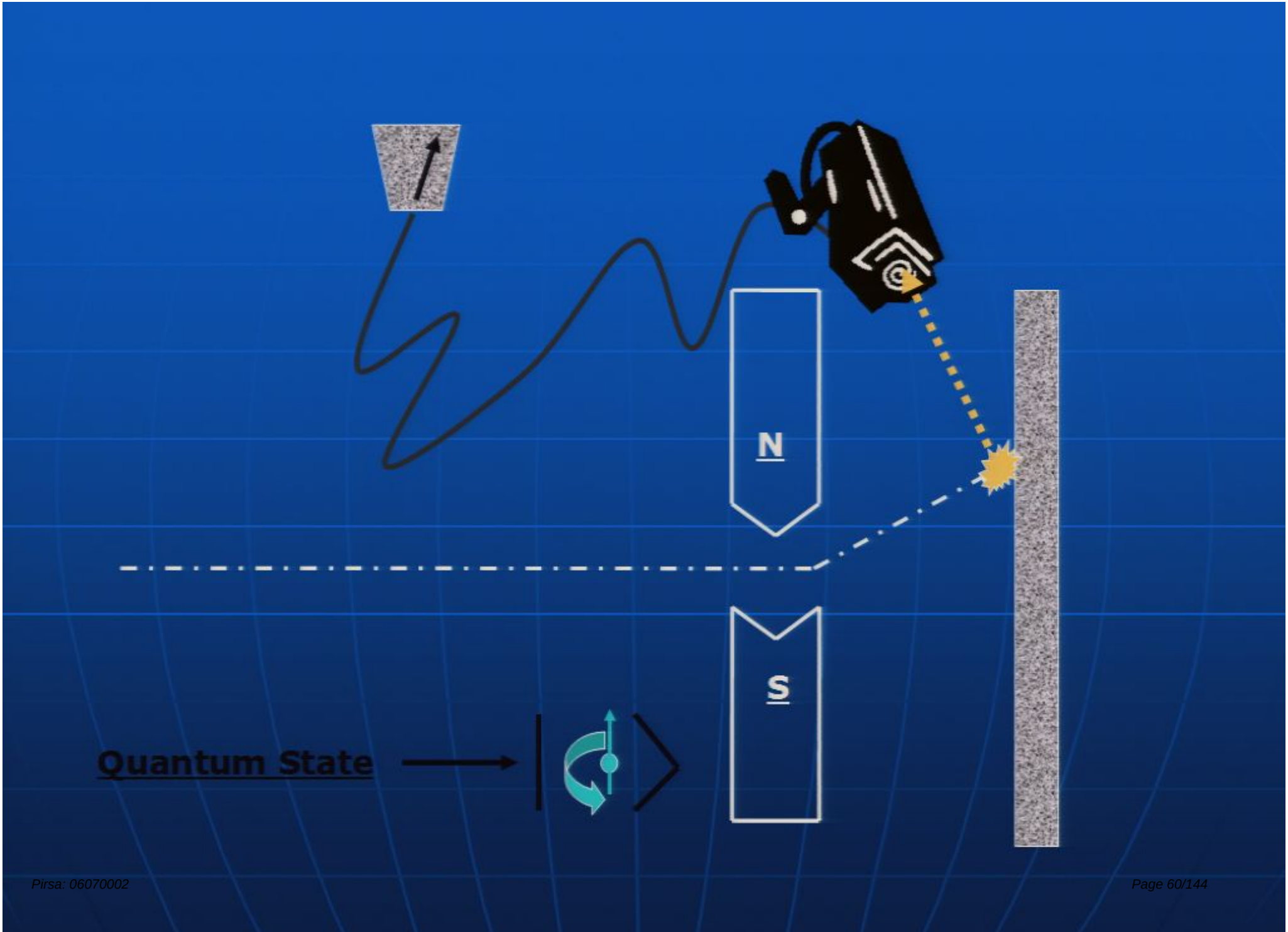
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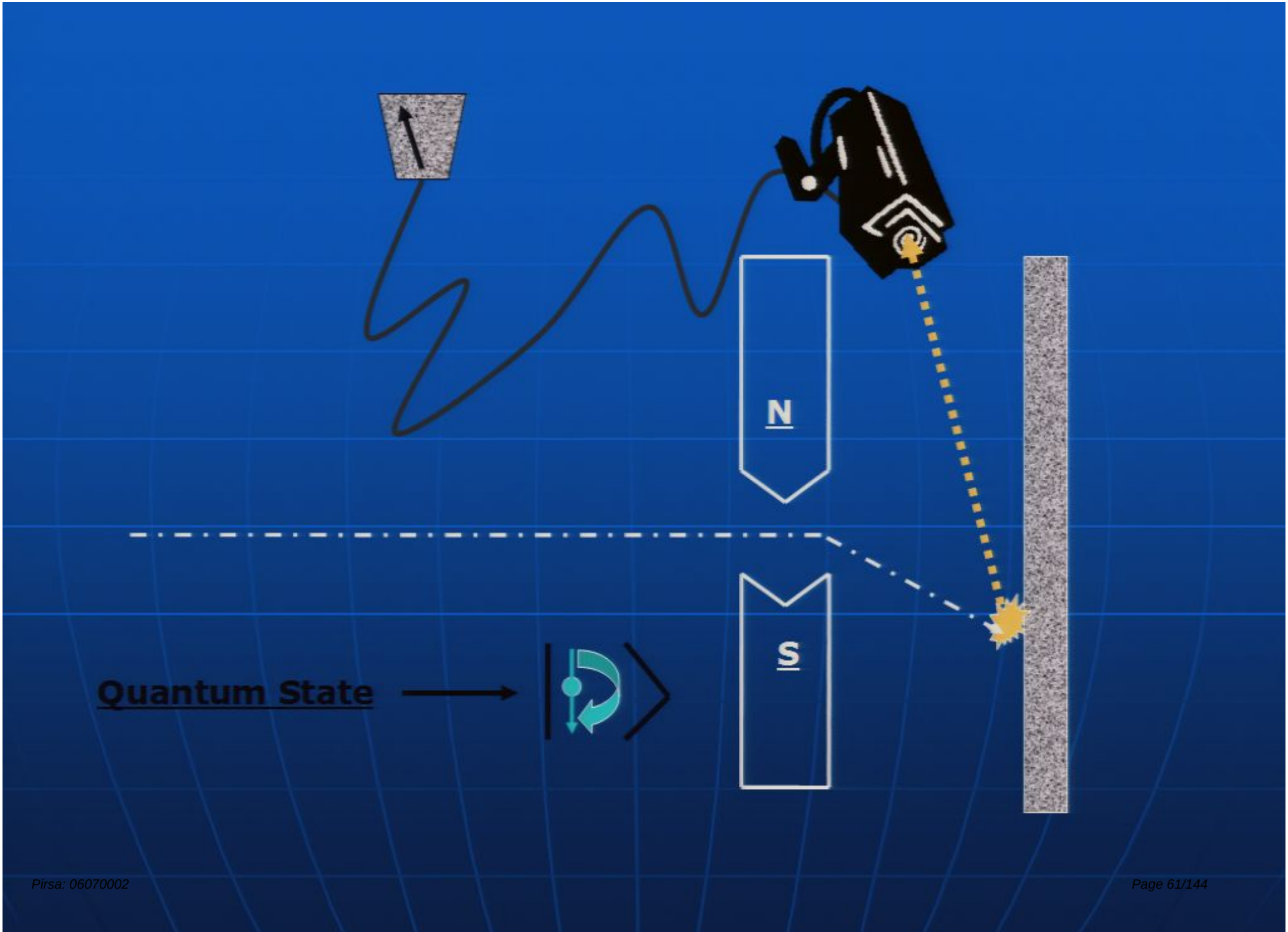
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# Evolution of the quantum state

Ideal Experiment:

# Superposition Principle II

If two quantum states evolve according to:

$$\Psi_1 \longrightarrow \Phi_1$$

$$\Psi_2 \longrightarrow \Phi_2$$

Then the super position $\alpha\Psi_1+\beta\Psi_2$ will evolve according to:

$$\alpha\Psi_1+\beta\Psi_2 \longrightarrow \alpha\Phi_1+\beta\Phi_2$$

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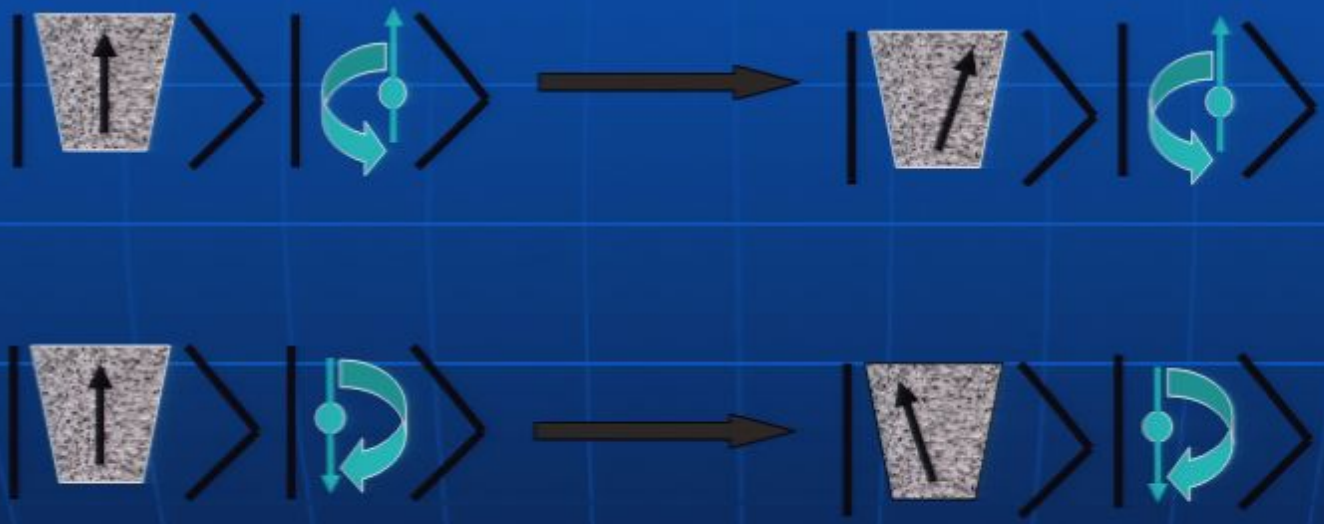

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# The Measurement Problem

According to Superposition Principle I
the state

$$\alpha \left| \uparrow \right\rangle \left| \circlearrowleft \right\rangle + \beta \left| \uparrow \right\rangle \left| \circlearrowright \right\rangle$$

is a possible quantum state.
It is not a "strange" state since it is only the electron which is in a superposition of "spin up" and "spin down".
In fact, this quantum state is routinely created in laboratories.

According to Superposition Principle II
the state has to evolve according to:

# But now we are in trouble!

The state

$$\alpha \left| \text{  } \right\rangle \left| \text{  } \right\rangle + \beta \left| \text{  } \right\rangle \left| \text{  } \right\rangle$$

is a superposition of two macroscopically distinct states!

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# But now we are in trouble!

The state

$$\alpha \; |\uparrow\rangle|\circlearrowleft\rangle + \beta \; |\text{pointer}\rangle|\circlearrowright\rangle$$

is a superposition of two macroscopically distinct states!

In a quantum experiment the state will in general evolve into a strange superposition of two macroscopically distinct states!

*According to quantum theory it is not only electrons that can be here and there at the same time! Also macroscopic objects like the measurement equipment, … and human beings…*

# … or cats…

# Different Reactions

| |
|---|
| "Shut Up! and Calculate" Interpretation |
| Copenhagen Interpretation |
| Von Neumann-Dirac Collapse Interpretation |
| Many Worlds Interpretation |
| Quantum Information Interpretation |
| Hidden Variable Interpretation |

# Copenhagen Interpretation

- The world should be divided into two parts: the quantum system one is measuring, and the classical apparatus that is doing the measuring
- The quantum system should be treated according to quantum theory
- The apparatus should be treated according to classical physics.
- The interaction between a quantum system and a classical system (i.e the measurement process) is regarded as unanalyzable. One cannot give a precise scientic description of what is going on in a measurement process.

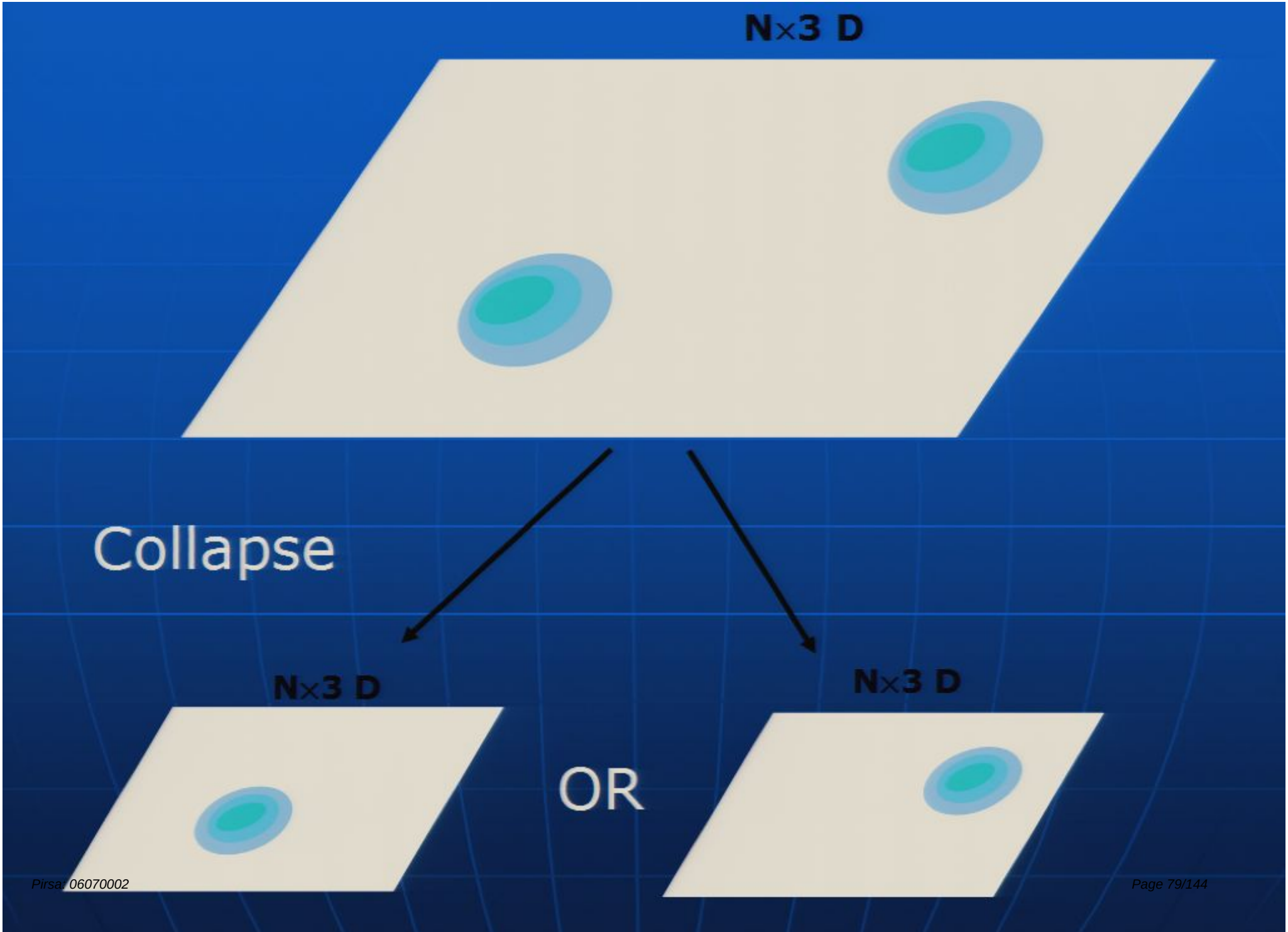
# Problems

- How do I know what is a quantum system and what is a classical apparatus? A classical apparatus is made out of atoms! How many atoms do I need in order to be sure that it is a classical system?
- No satisfactory answer given by Bohr.
- And isn't it non-scientific to claim that it is scientifically impossible to analyze what happens during a measuring process?

# Von Neumann & Dirac

- When macroscopic bodies are involved the wave-function

Collapses into


N×3 D
Collapse
N×3 D
OR
N×3 D

# Problems

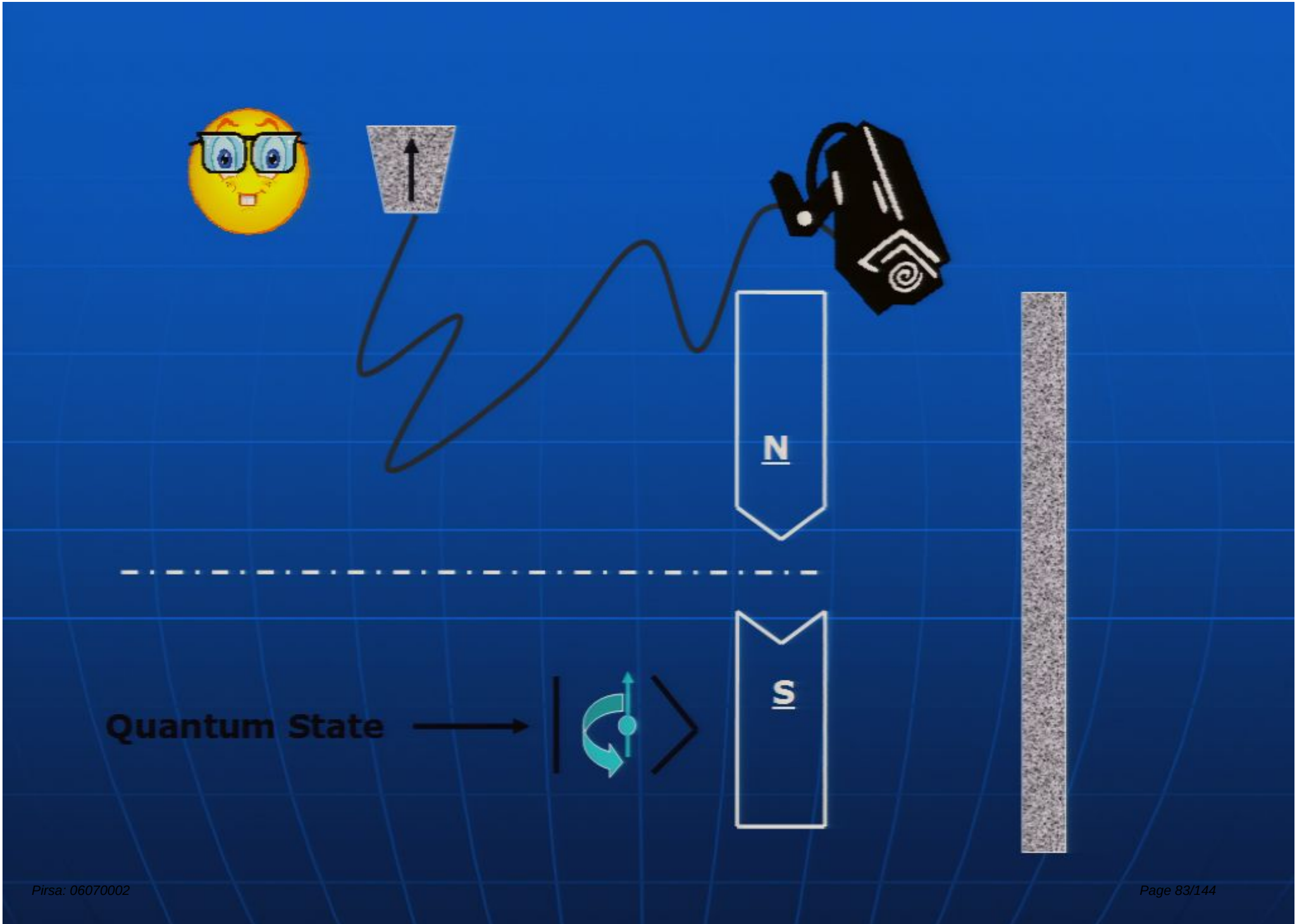
- If the wave-function collapses then when is this supposed to occur? How big must a "classical" apparatus be in order for a collapse to occur?
- And where are the mathematical equations that tell me EXACTLY how and when the wave-function collapses?

# Collapse theories

- Pearle, Ghirardi, Rimini, Weber, modified quantum theory. Collapse is a physical process.
- Energy is not conserved.
- Fully relativistic collapse theories are difficult to make: infinite energy production per unit time!
- "Almost"-relativistic ones are possible to construct (Pearle).

# Many Worlds

- Let's take quantum theory REALLY seriously and fully accept these strange superpositions.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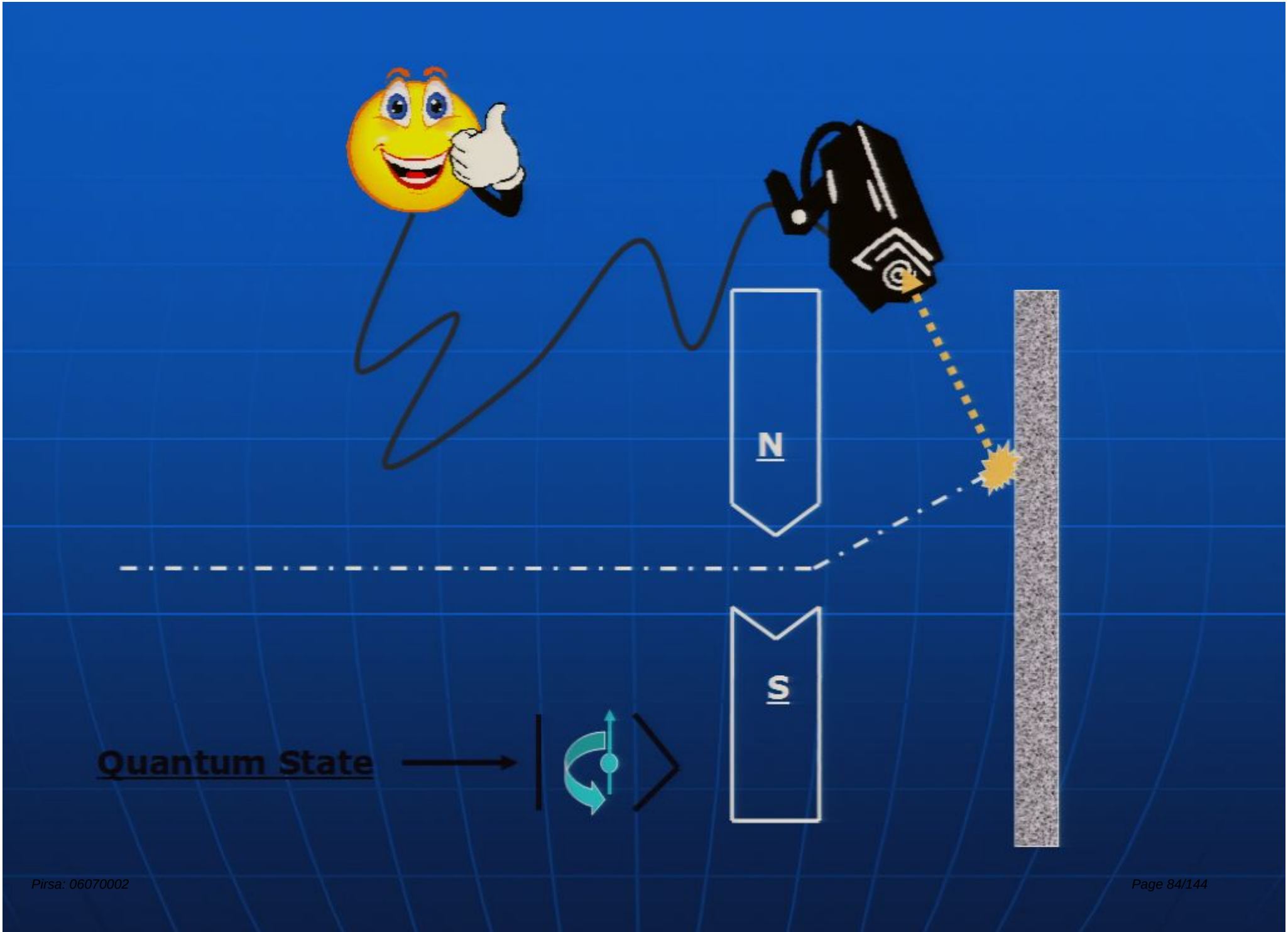
Quantum State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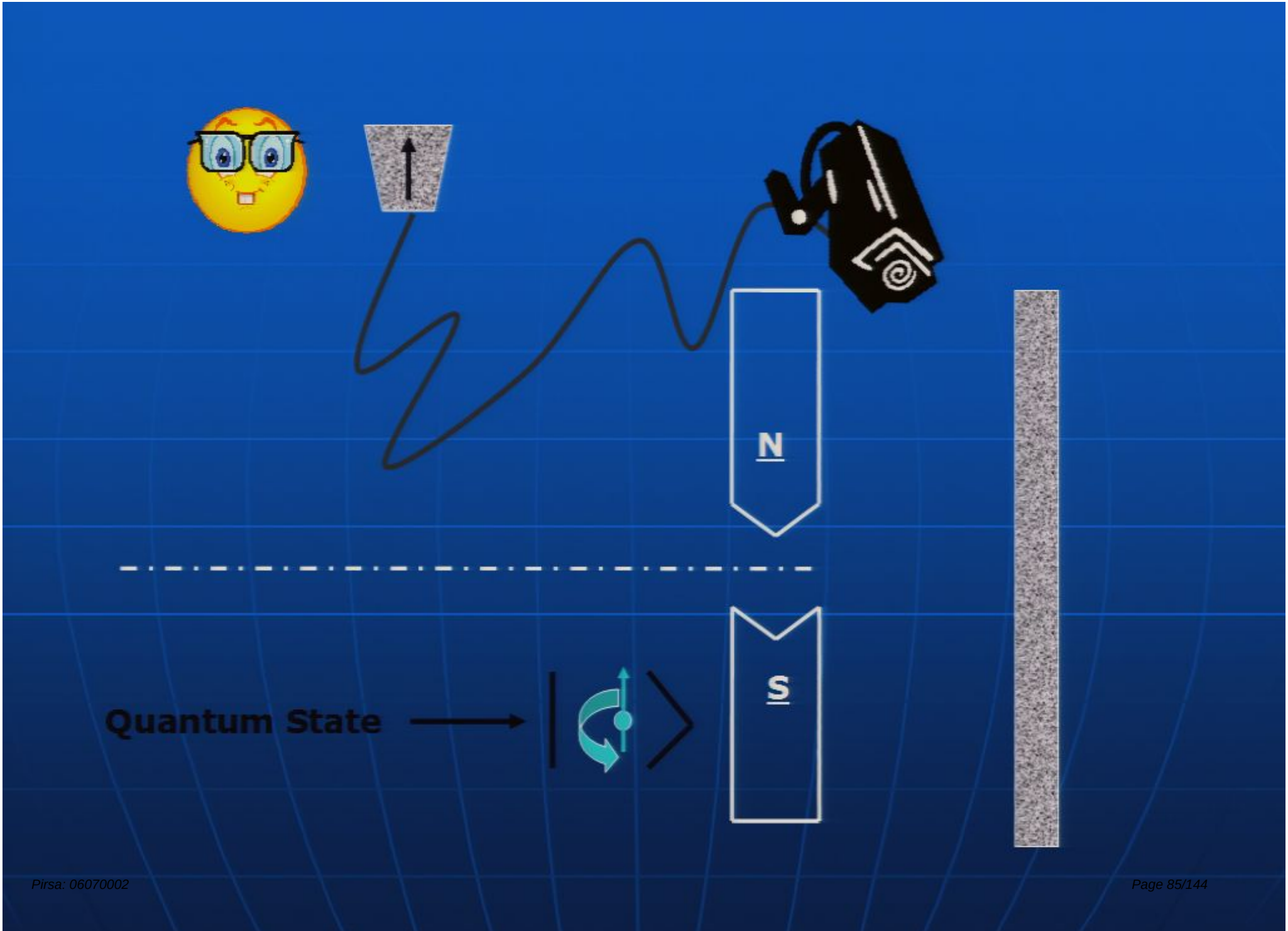
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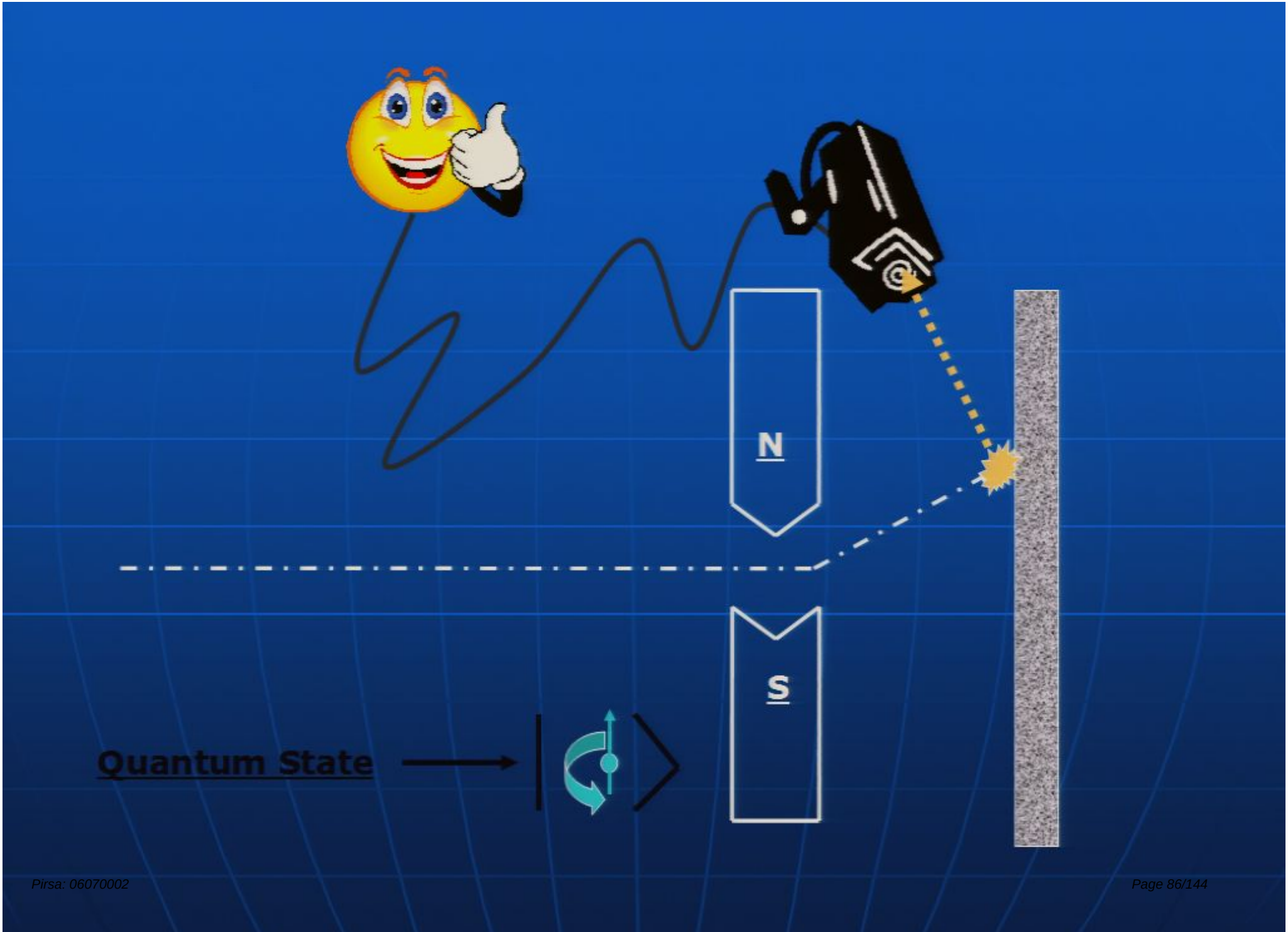
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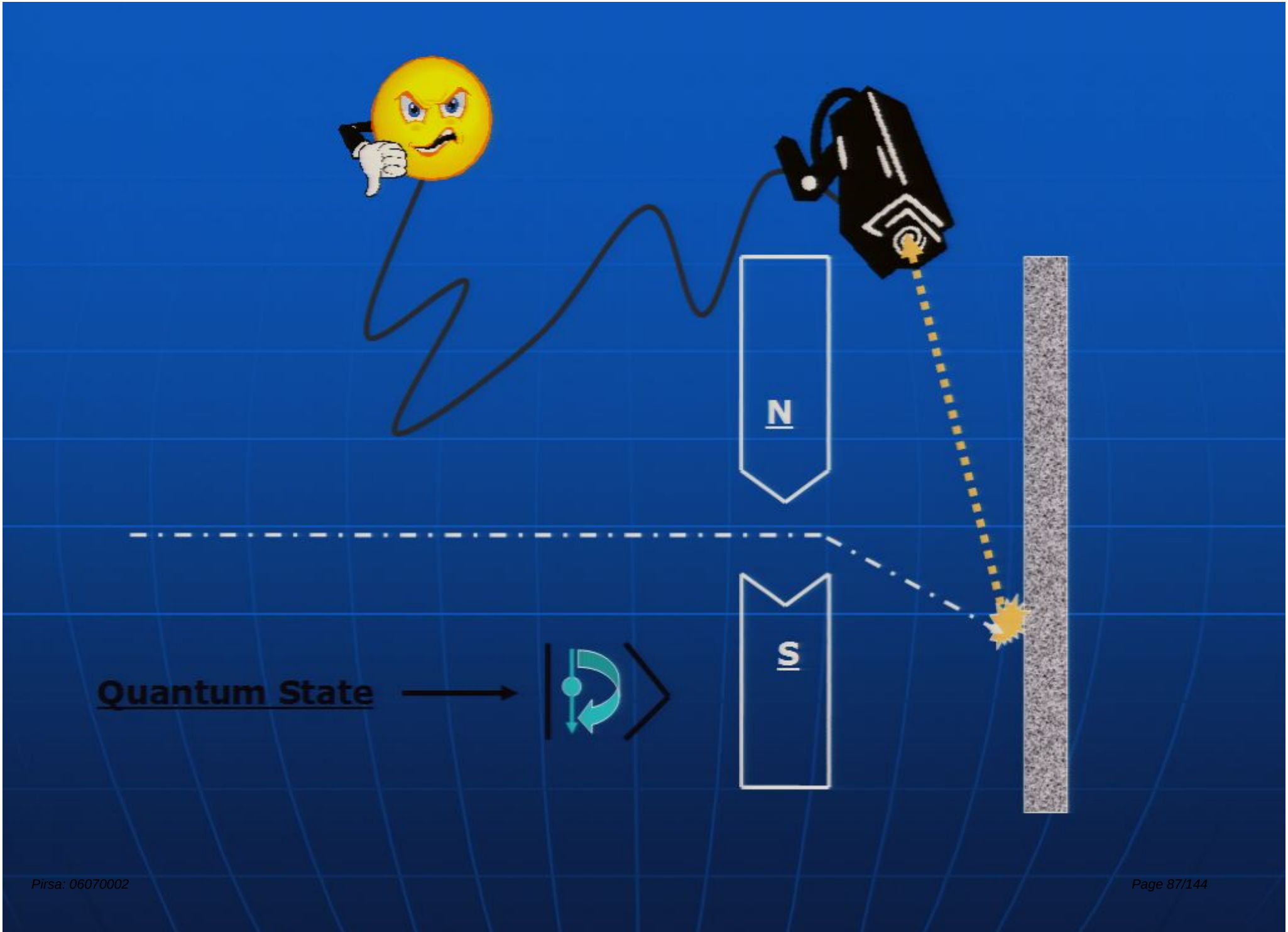
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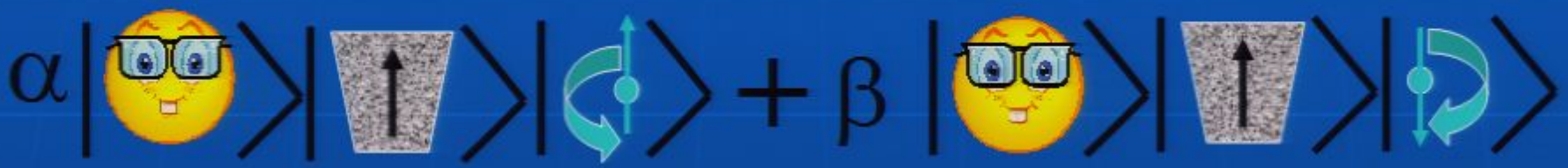

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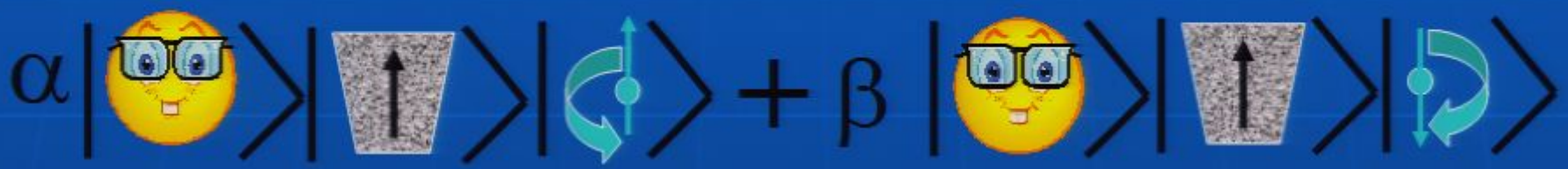

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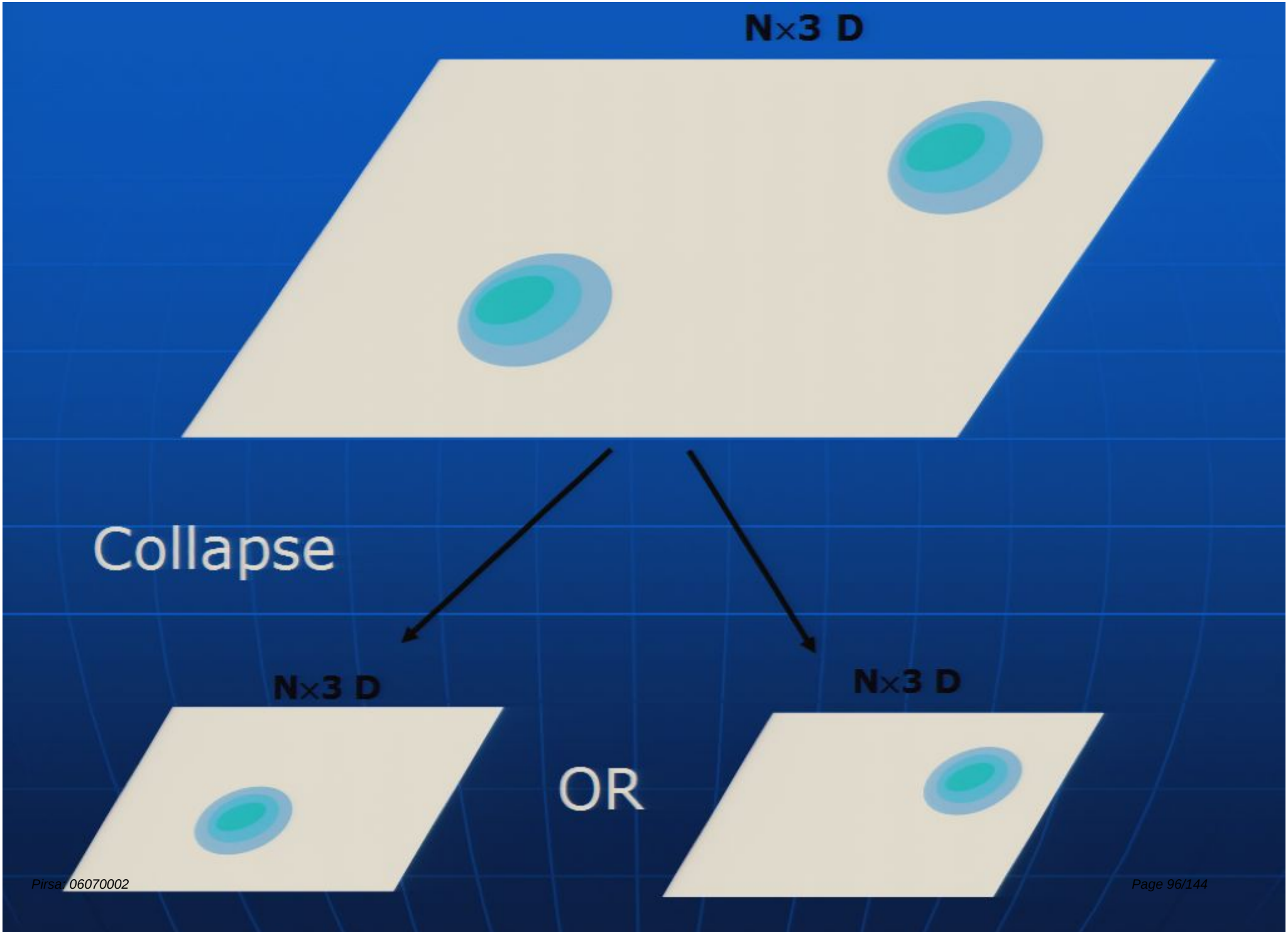
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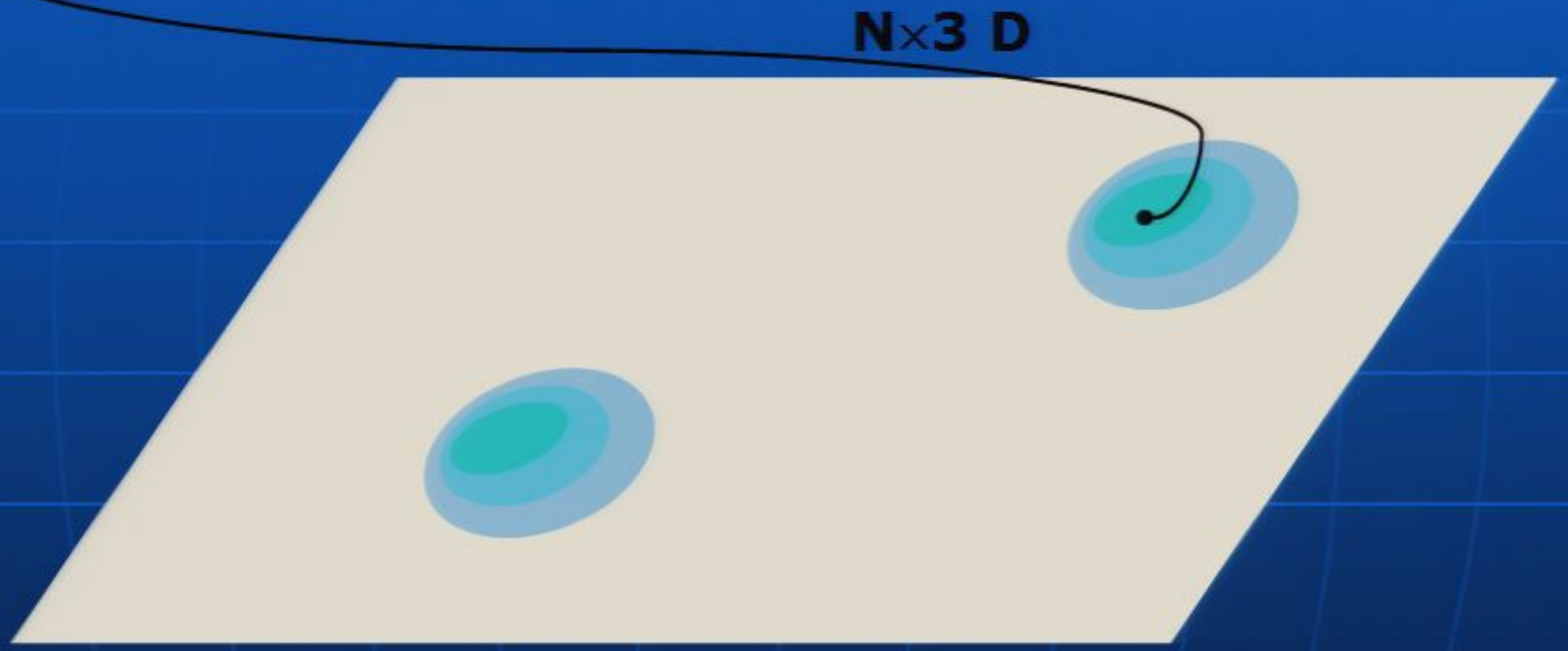
# Problems

- Knowledge about what? Knowledge about the outcome of an experiment?
- Ok, but if you are claiming to say something precise here you better specify exactly what you mean by an "an experiment". Is it perhaps the interaction between a classical apparatus and a quantum system?
- We again run into the same problem we had with the Copenhagen interpretation.

# deBroglie-Bohm theory

$X=((x_1,y_1,z_1),(x_2,y_2,z_2),\cdots,(x_N,y_N,z_N))$ $\longleftrightarrow$ $|\uparrow\rangle$




A system is described by $(\Psi(x),X(t))$.

# Dynamics

In classical theory X evolves according to Newtons laws F=mA.

In deBroglie-Bohm theory X evolves according to the non-classical equations

$$m\frac{dX}{dt} = \mathrm{Im}\left(\frac{\nabla\Psi}{\Psi}\right)$$

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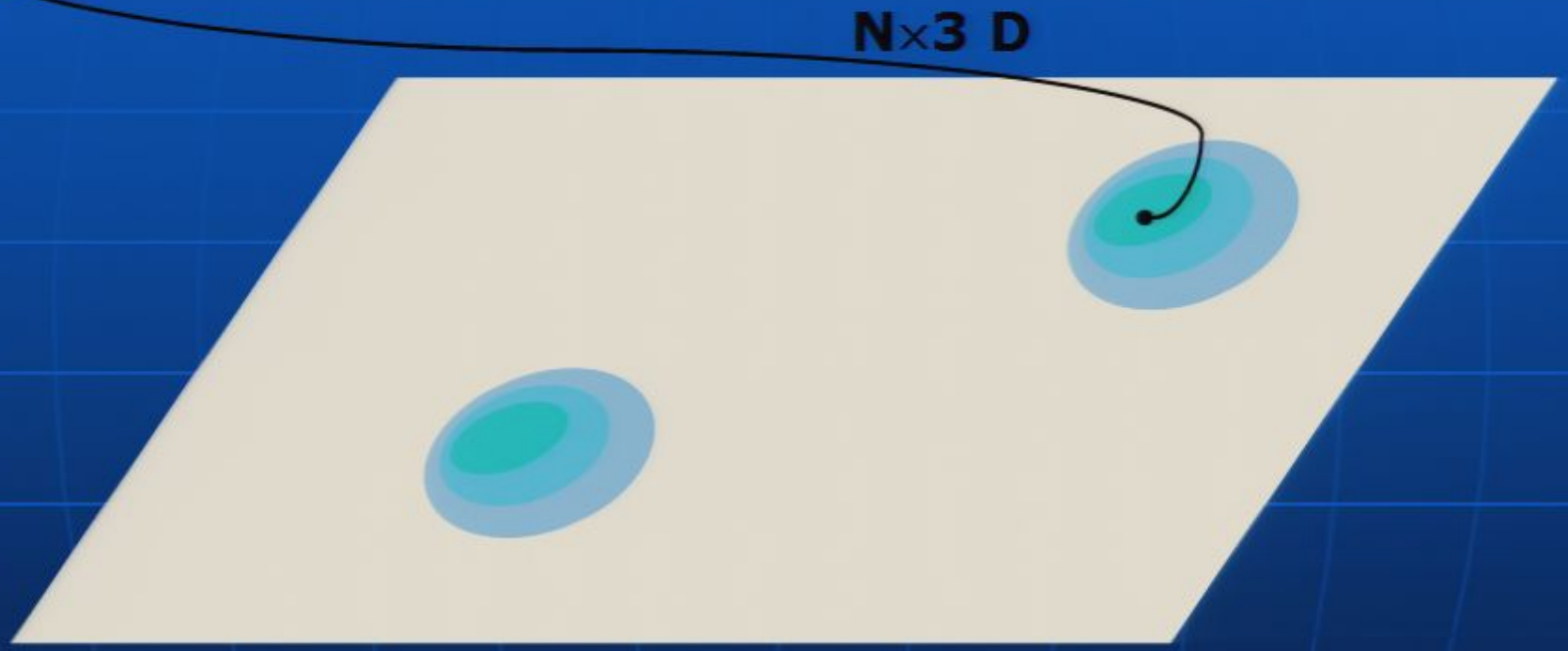


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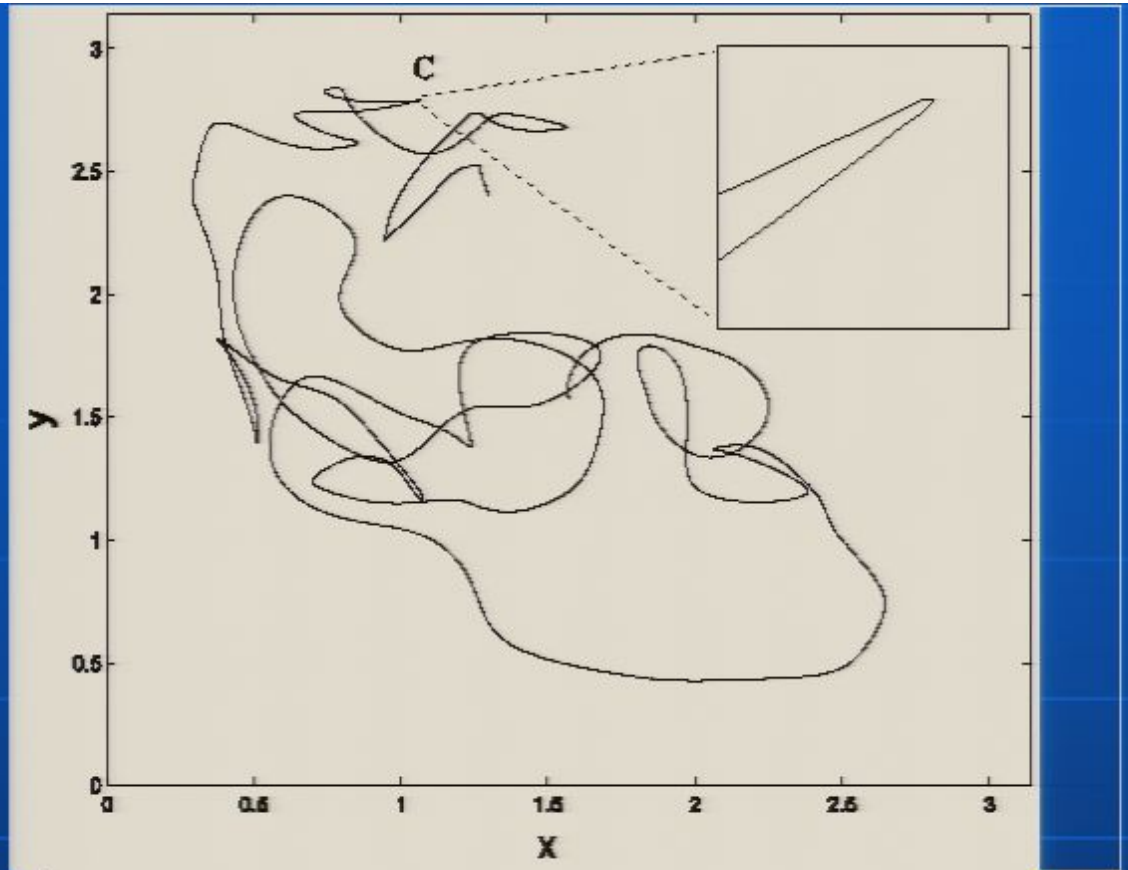
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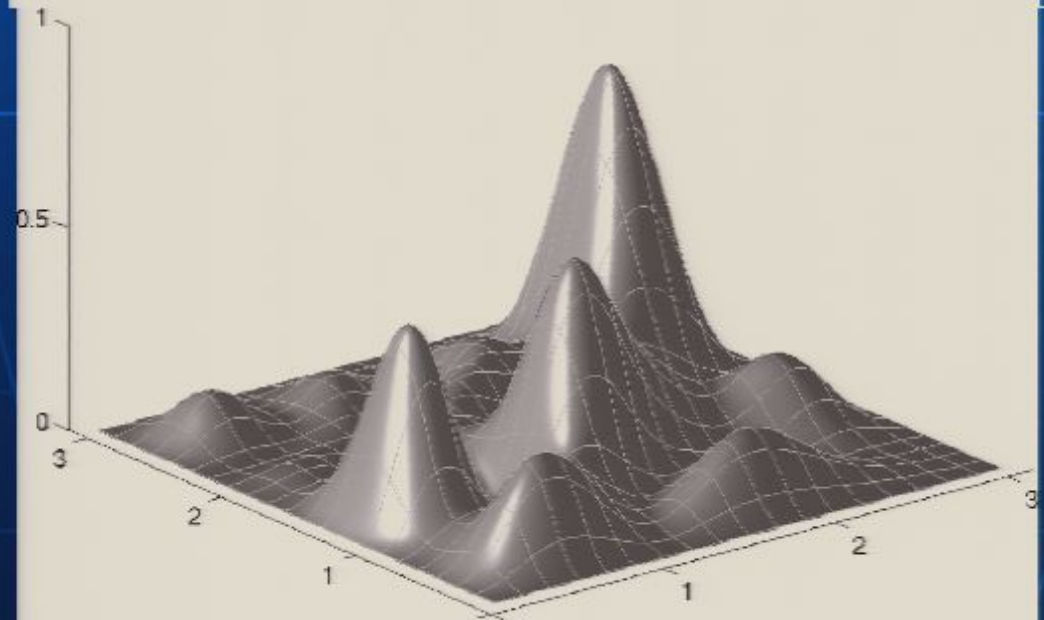
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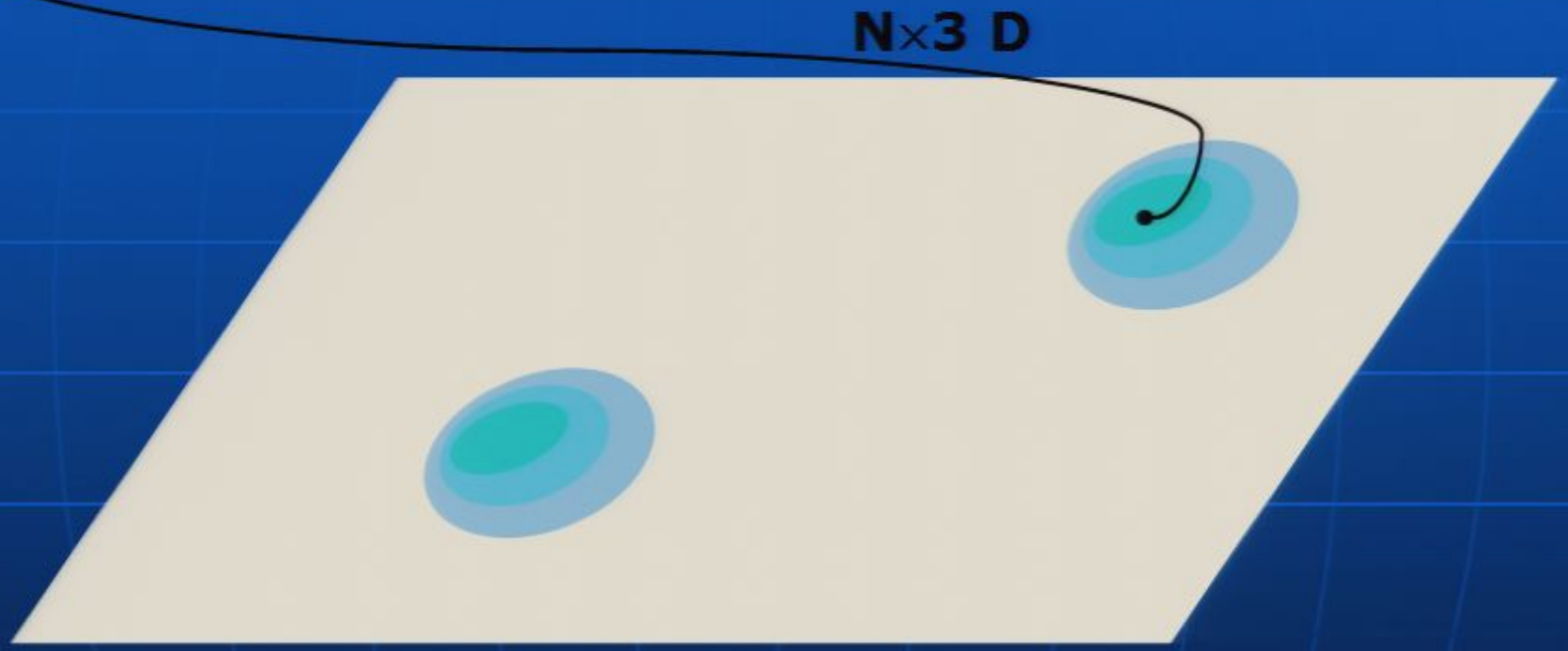


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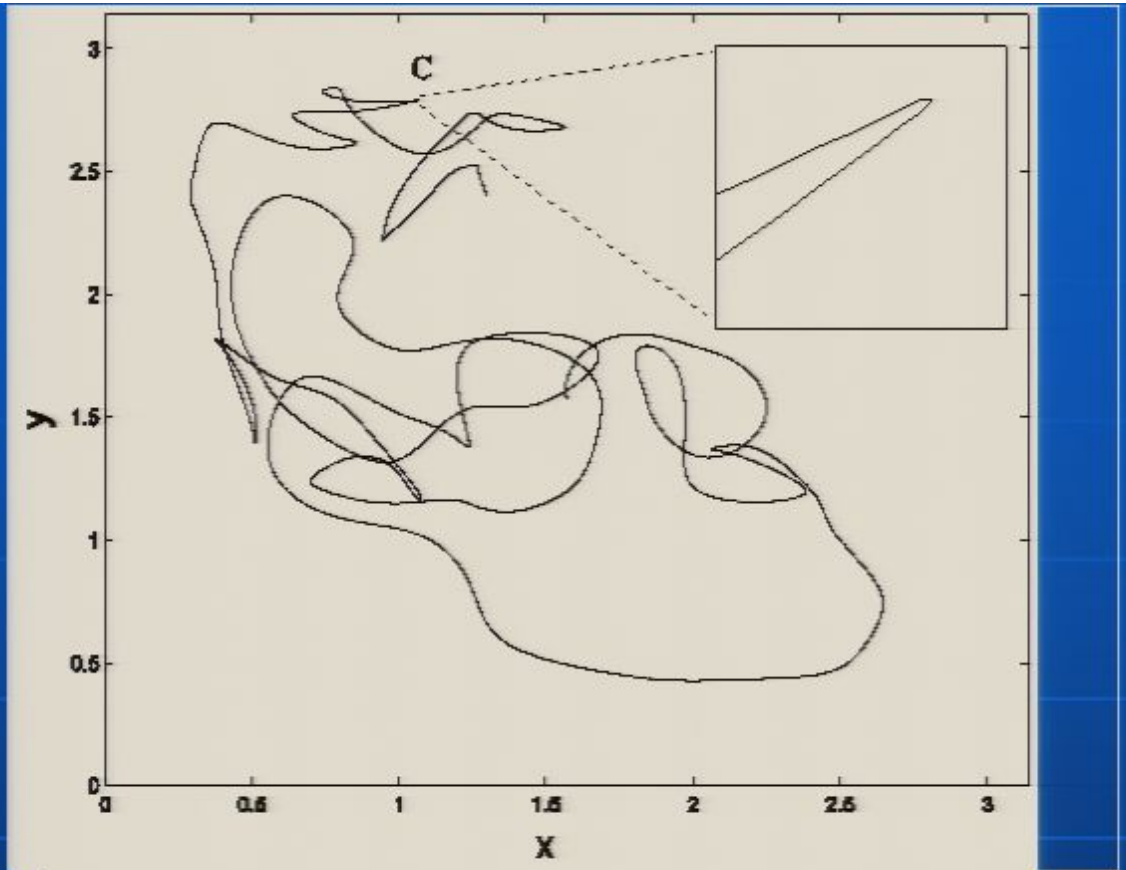
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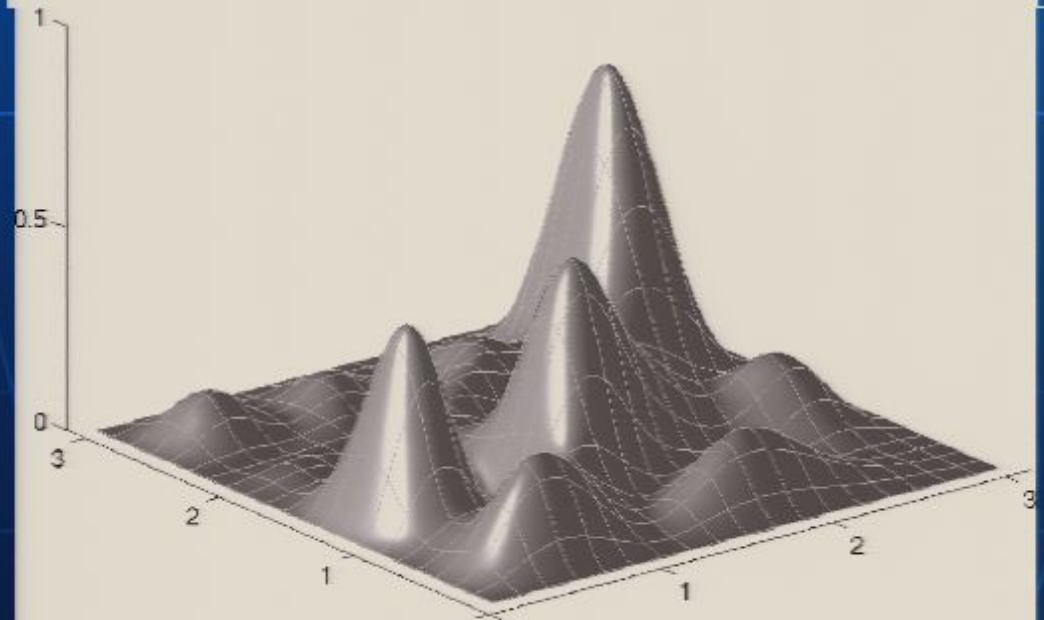
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# Good News

The theory is completely well defined, even deterministic, reproduces all the predictions of quantum theory (also also relativistic quantum theory) and the superposition principle is still valid.

dBB is a much richer theory with quantum theory emerging only in quantum equilibrium.

Explains the quantum statistics as a feature of quantum equilibrium.

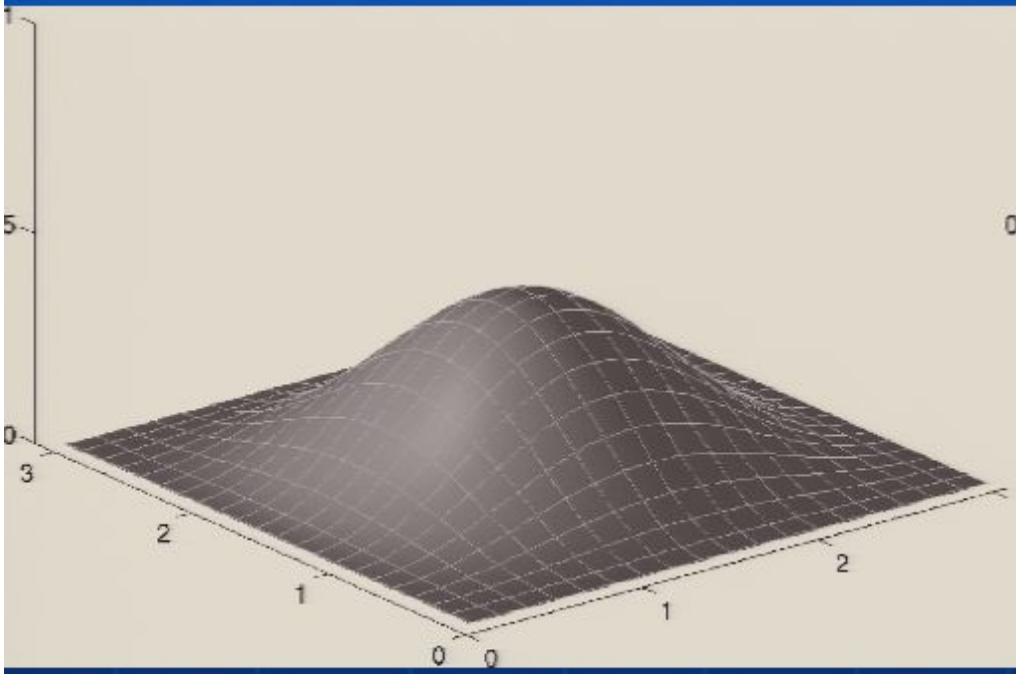
# Problems

- The universe according to this theory seems rather strange. There are two things that make up the world i) the particles in 3D space ii) the wave-function that "lives" in 3N D configuration space.
- The wave-function is fundamentally unobservable. The world we see is represented by the configuration X(t) just as in Newtonian physics.
- Empty wave problem.

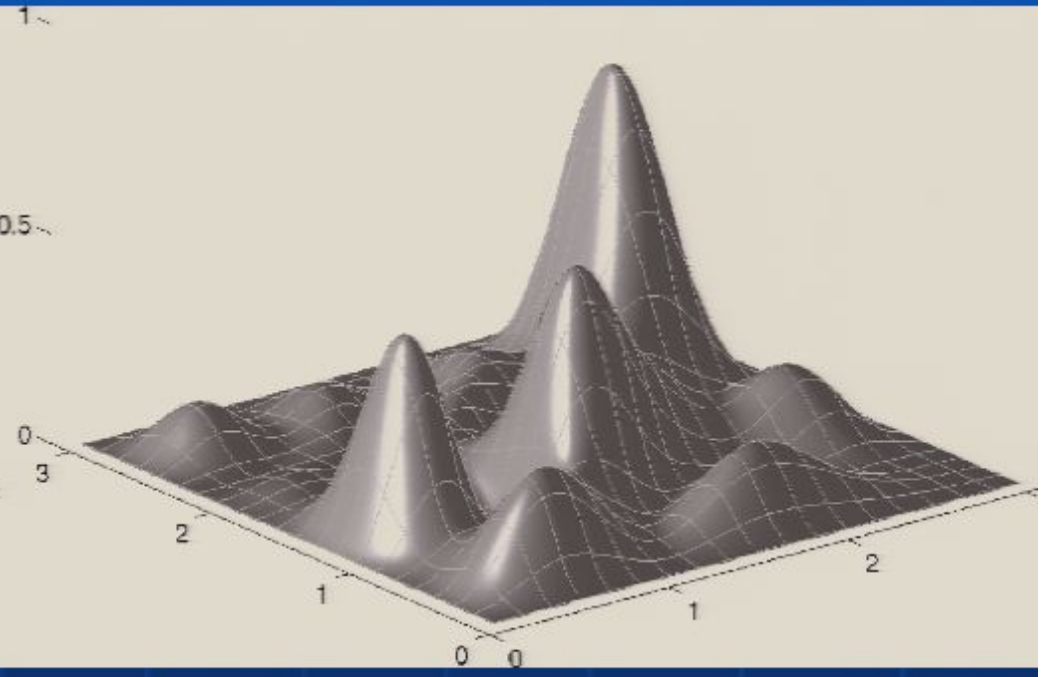
# Conclusion

- Quantum theory is an extremely successful theory. Yet it is hard to see how it really can be a fundamental theory.
- Out of the interpretations only the collapse theories and hidden variable theories are precisely formulated wihtout vague concepts like 'classical', microscopic.
- But both of these are different theories with different predictions than quantum theory.

P(x,y) at t=0




$|\psi(x,y)|^2$ at t=0



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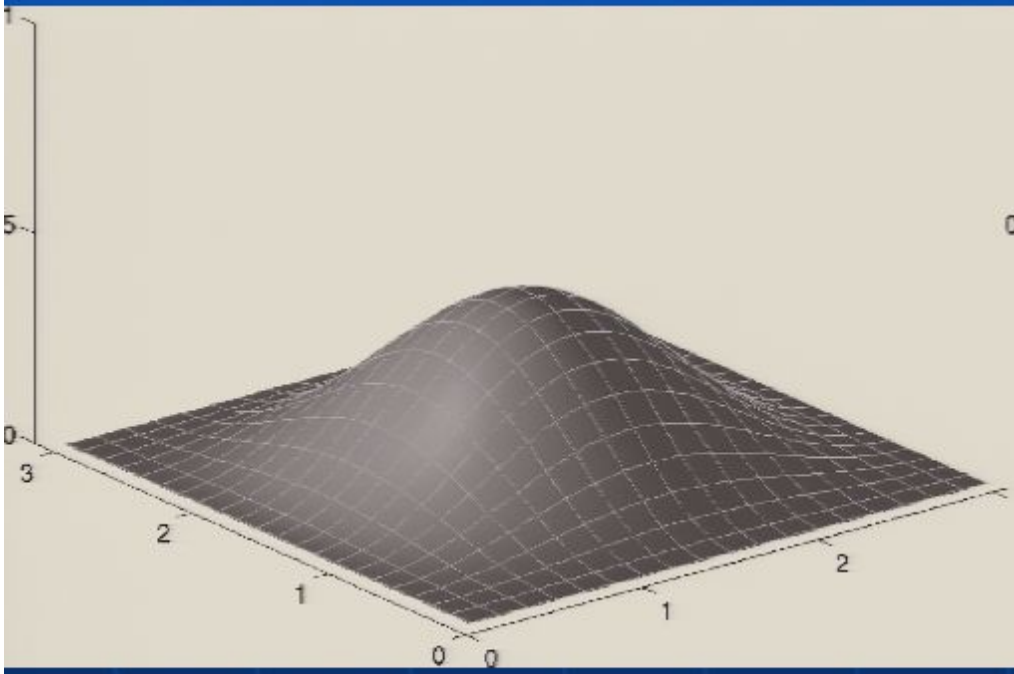


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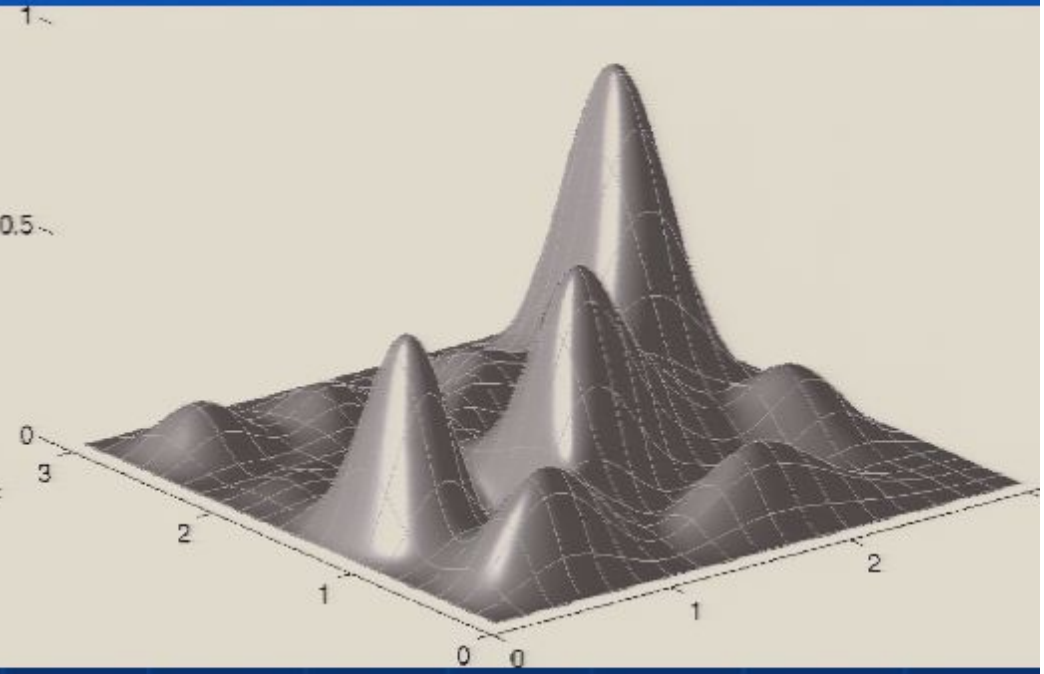
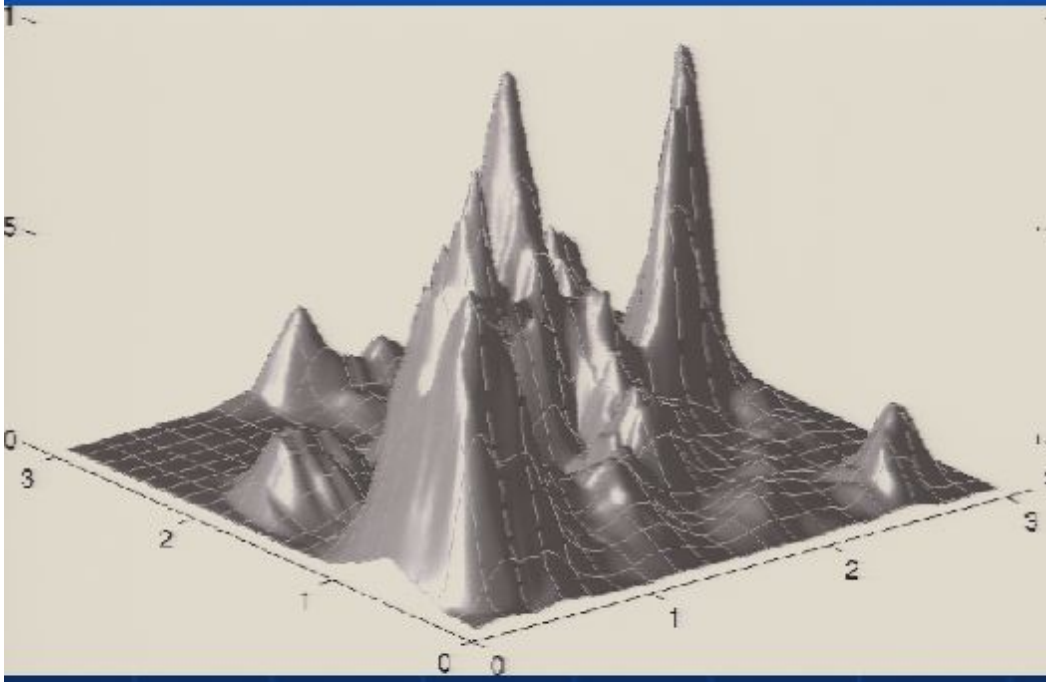


P(x,y) at t=2π

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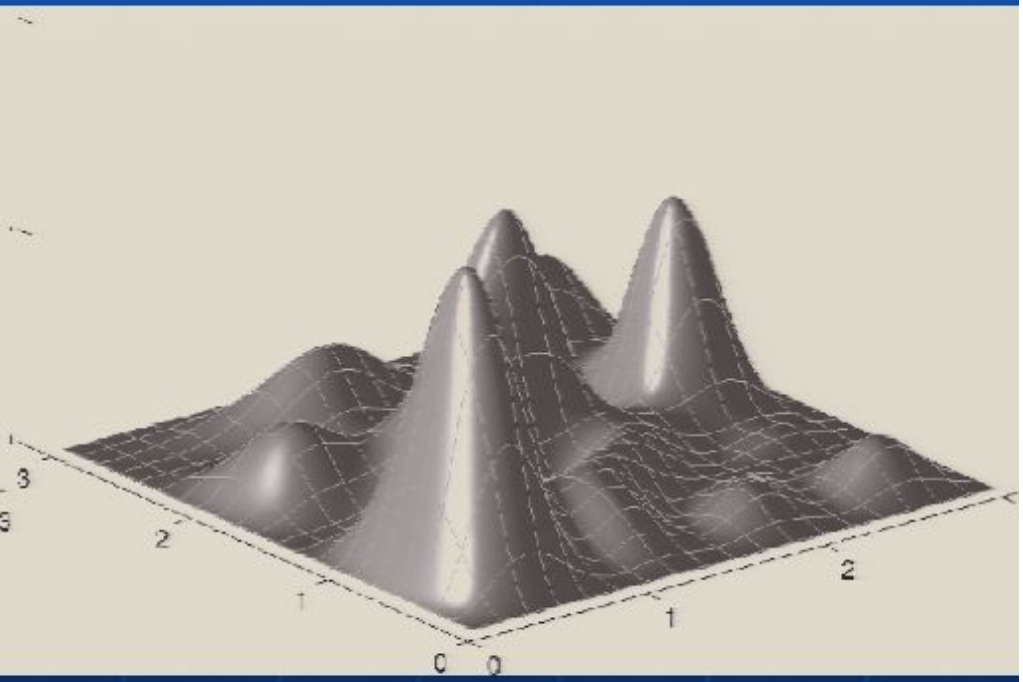

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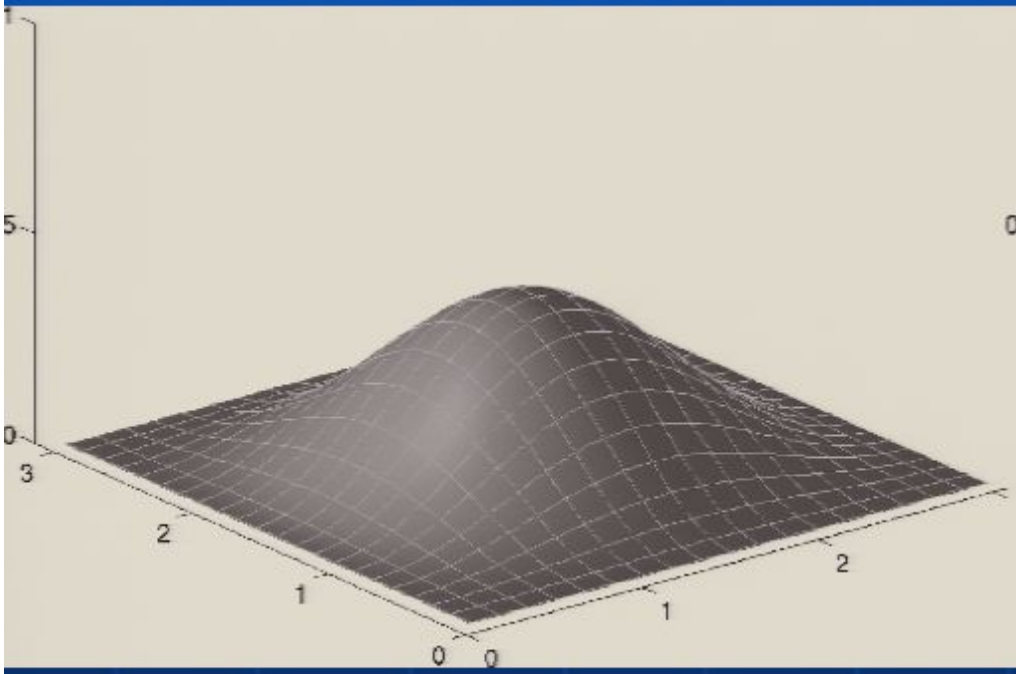
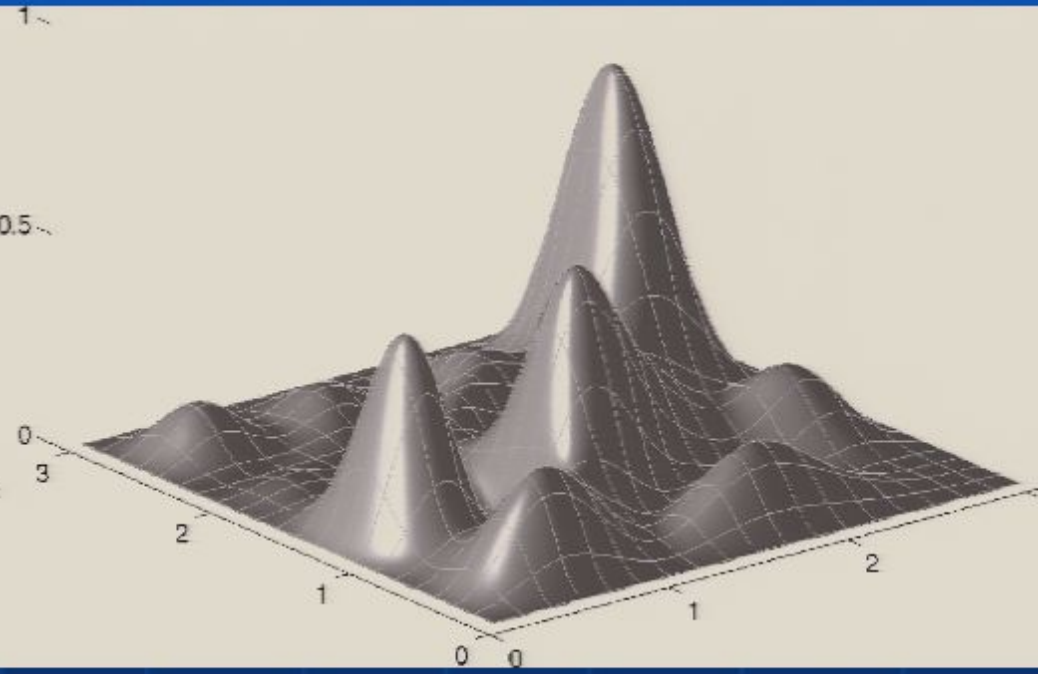



$|\psi(x,y)|^2$ at t=0



P(x,y) at t=4π

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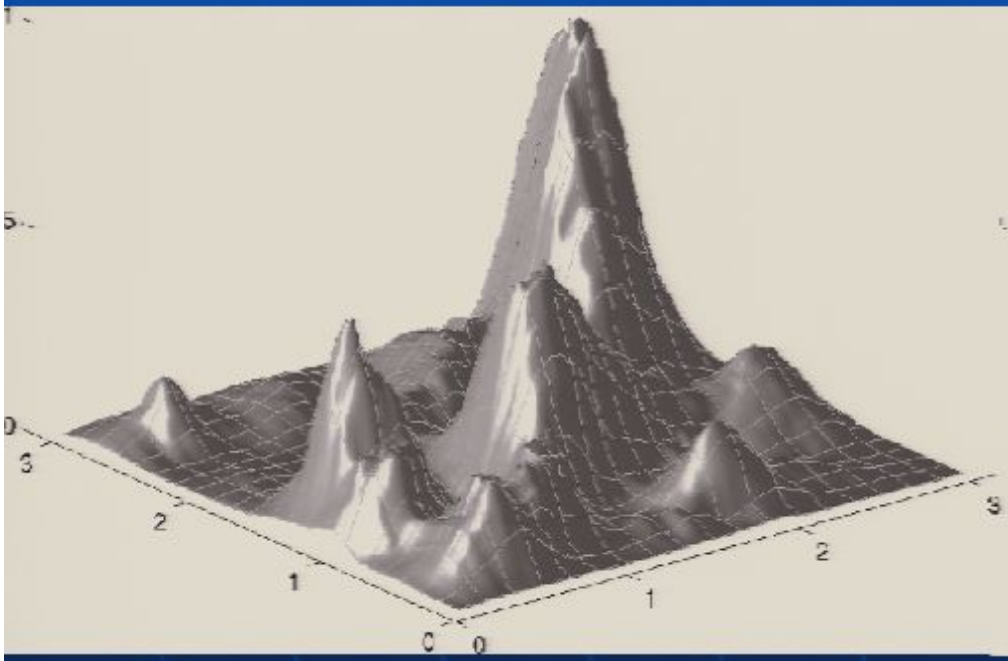


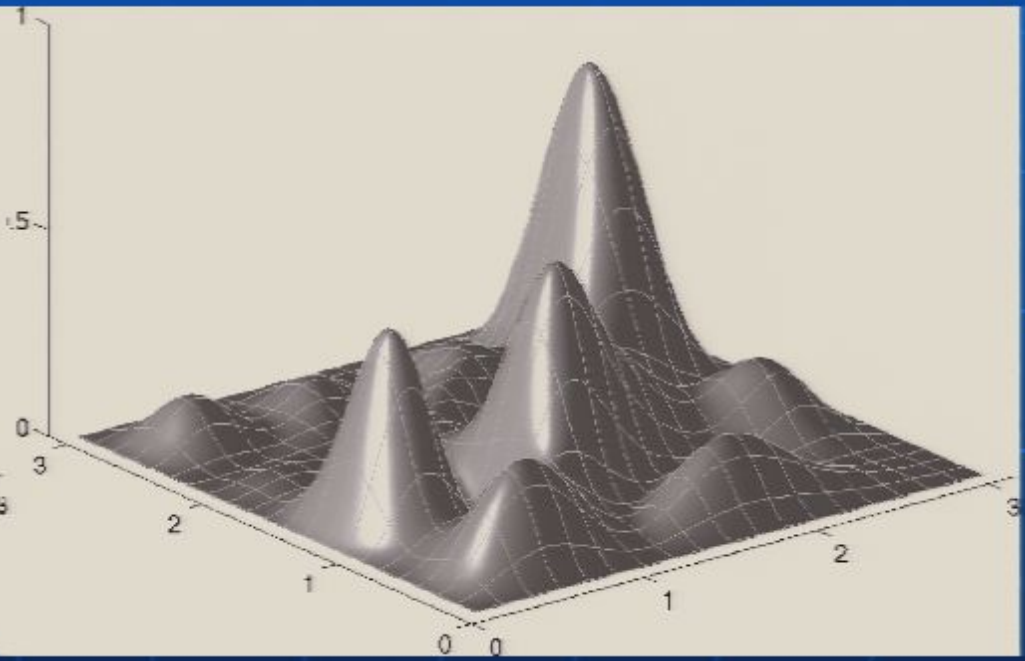

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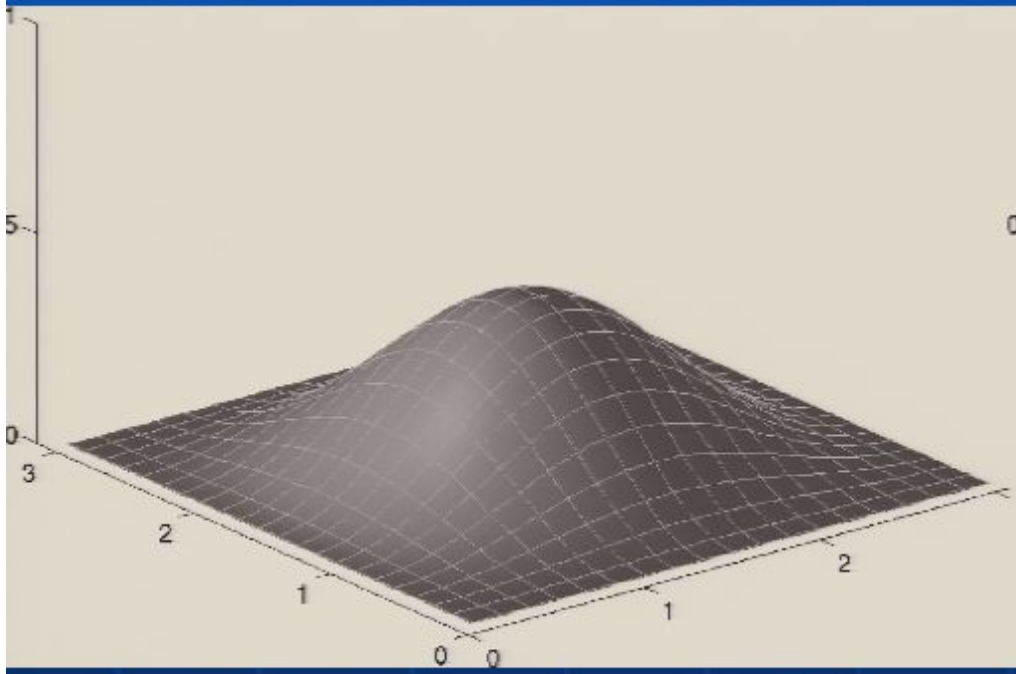


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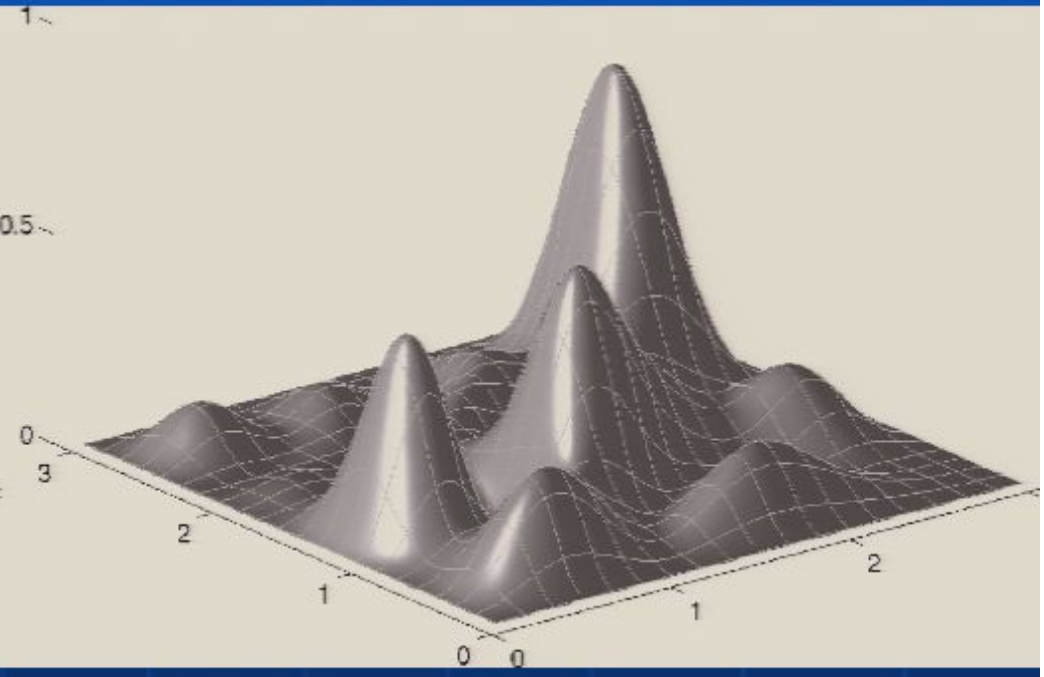

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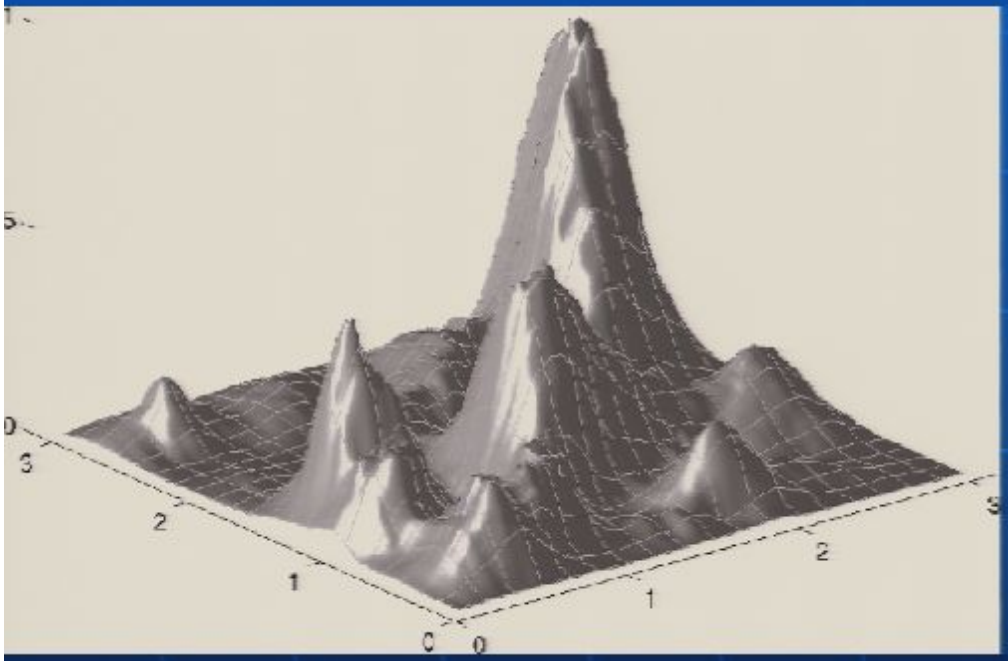

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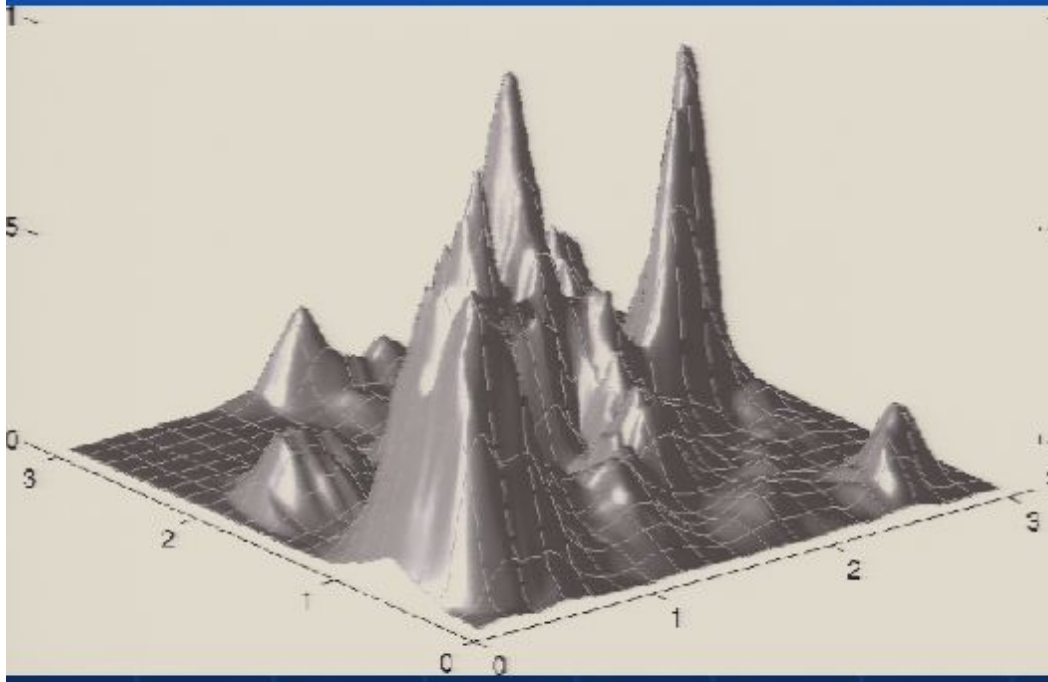


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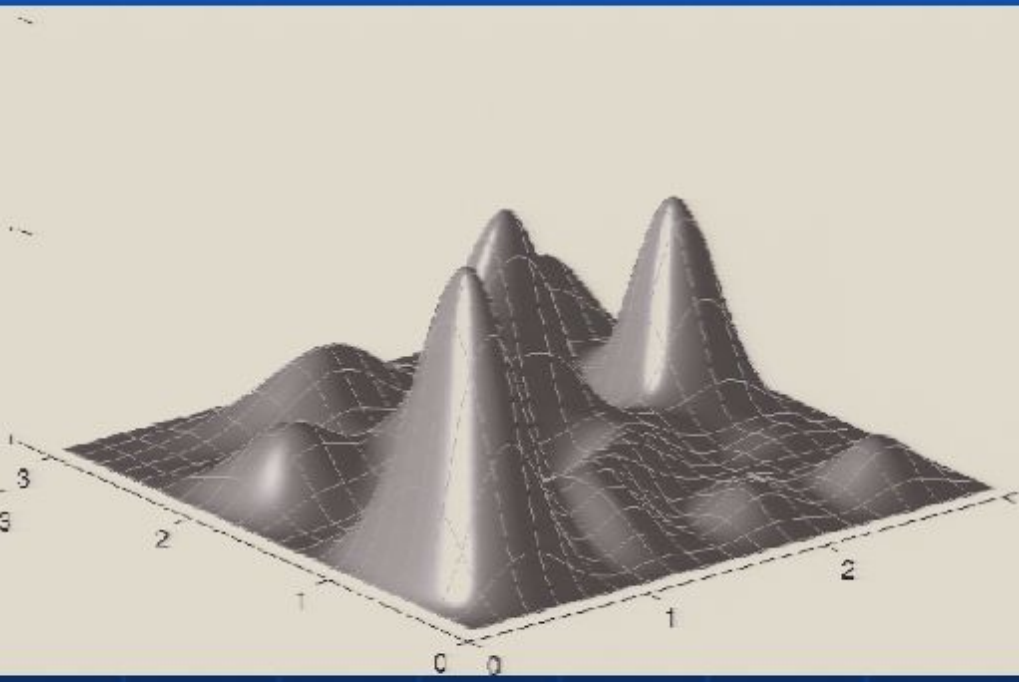

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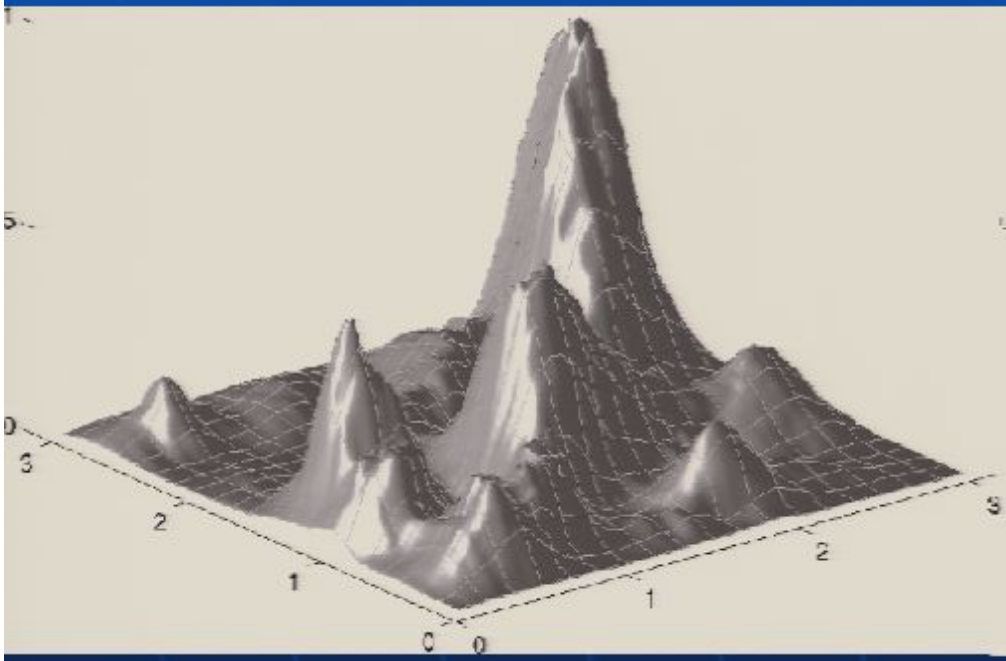


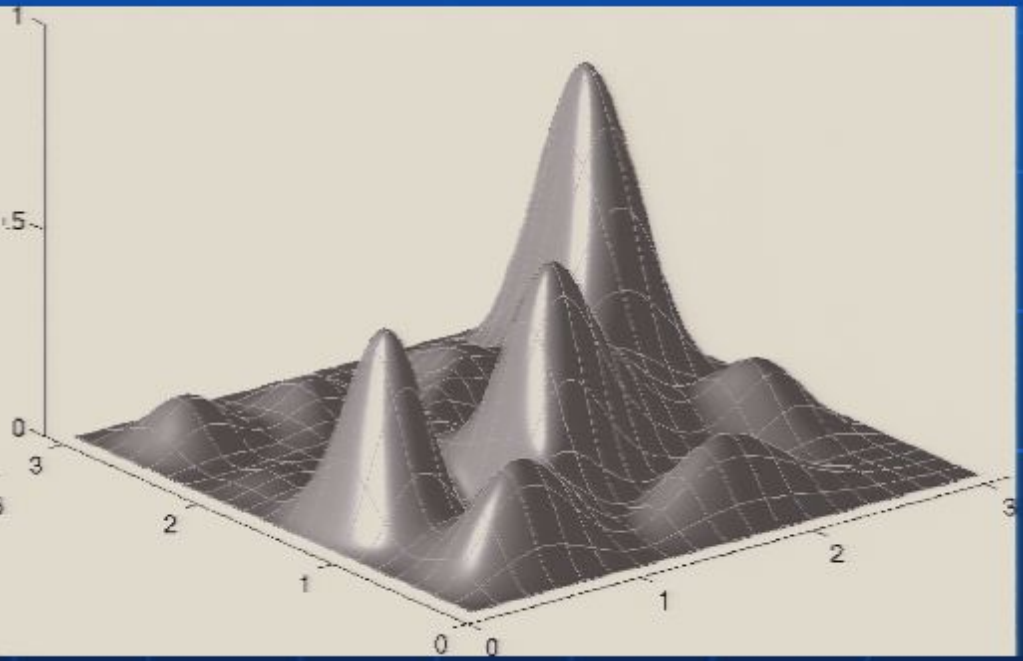

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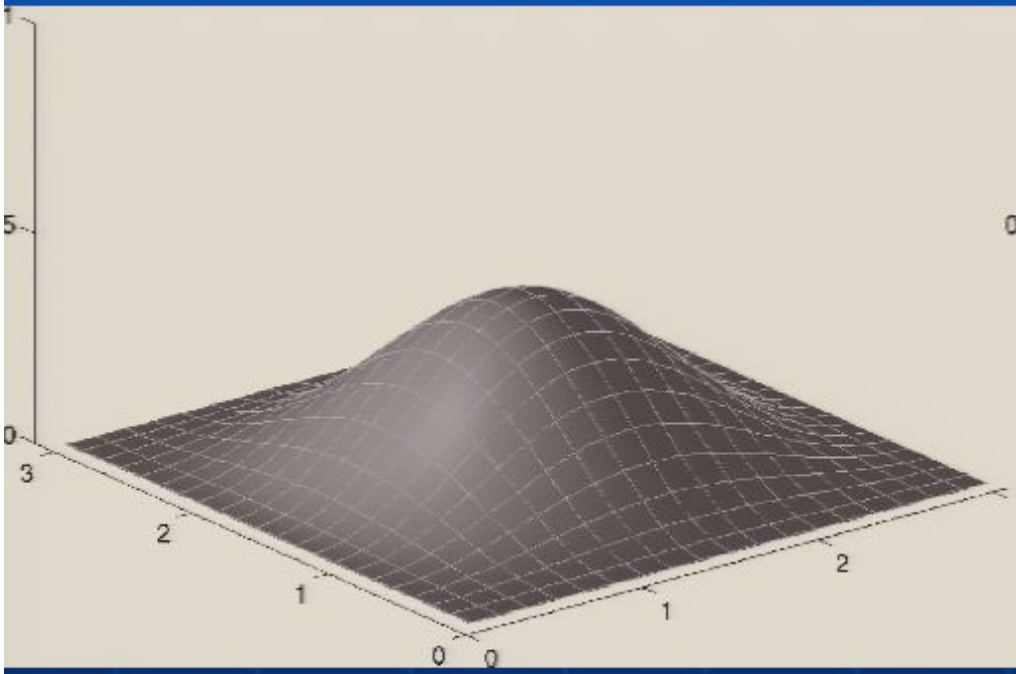
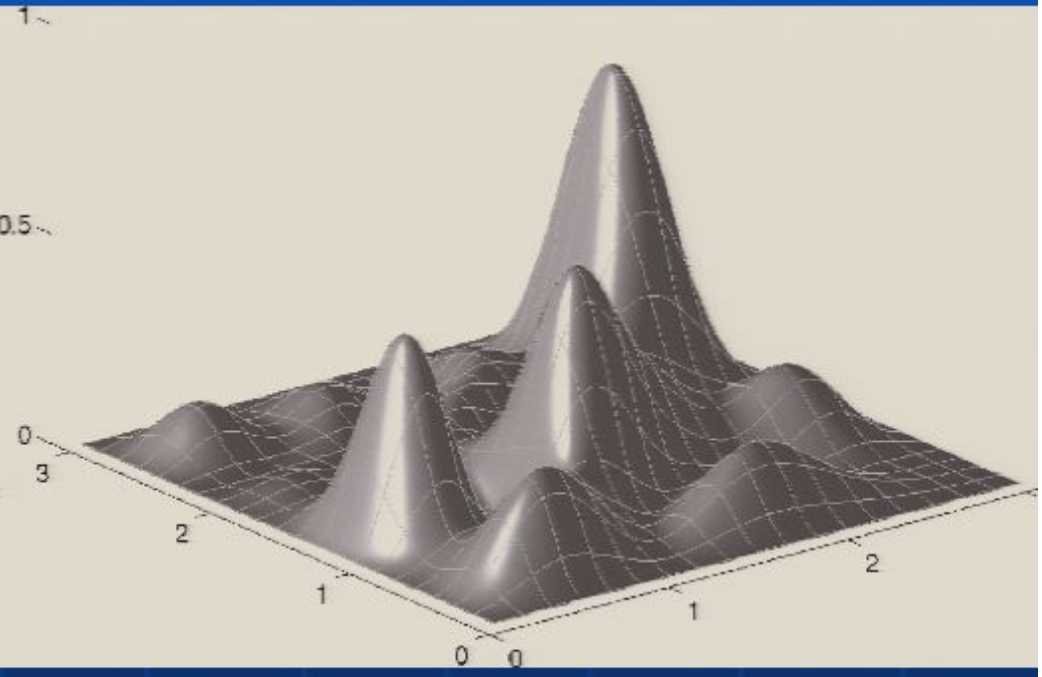
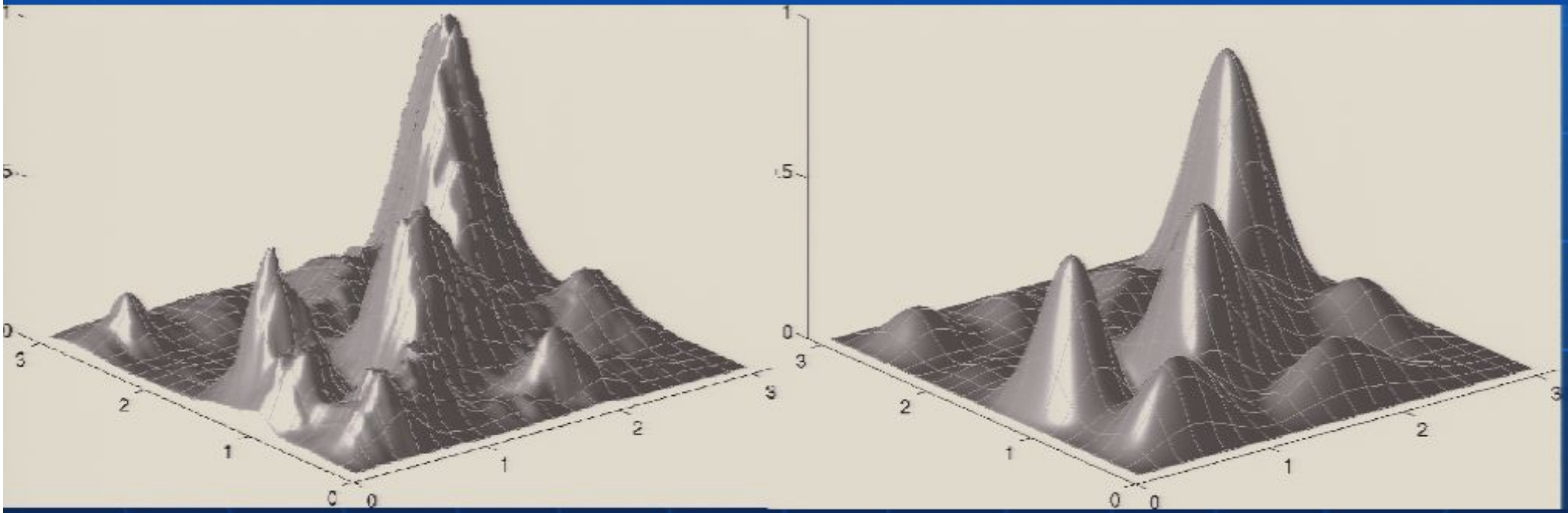



$|\psi(x,y)|^2$ at t=0



P(x,y) at t=4π

$|\psi(x,y)|^2$ at t=4π



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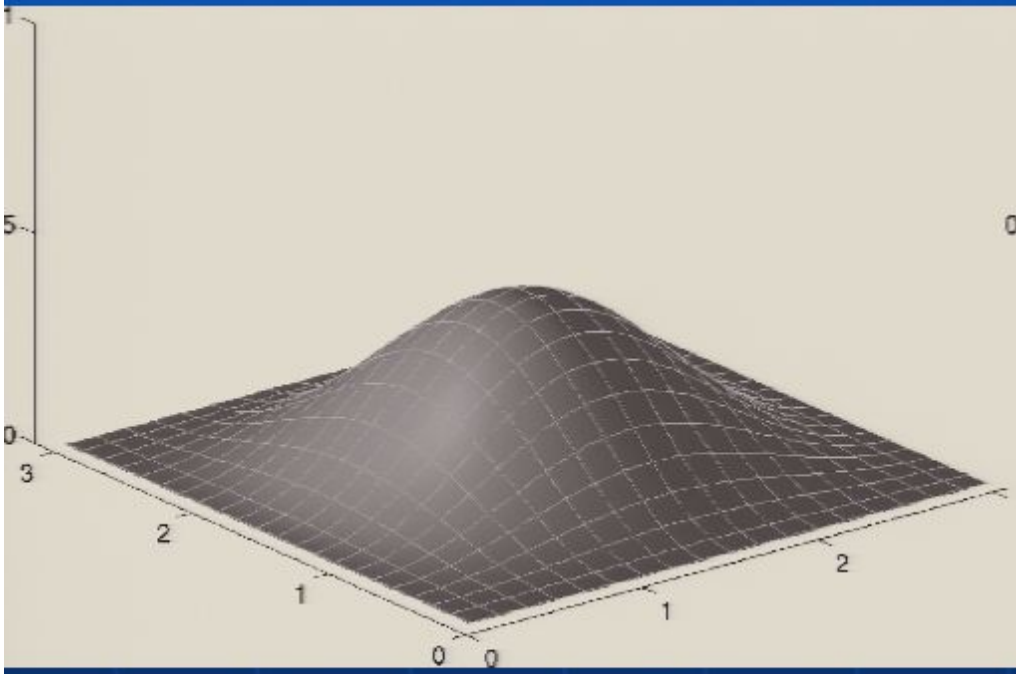


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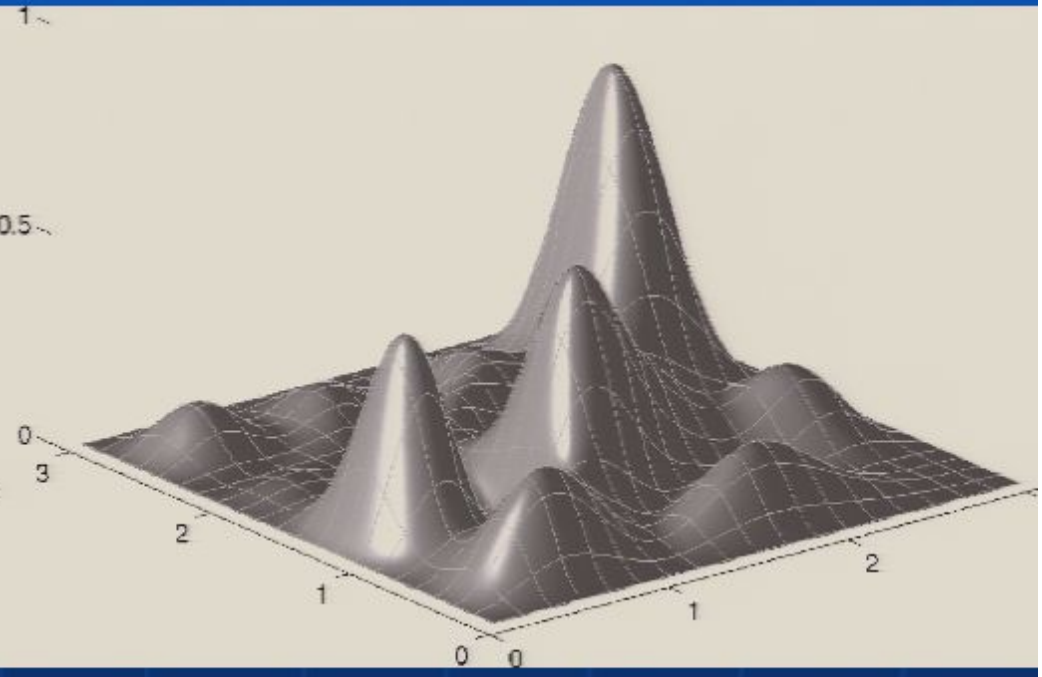
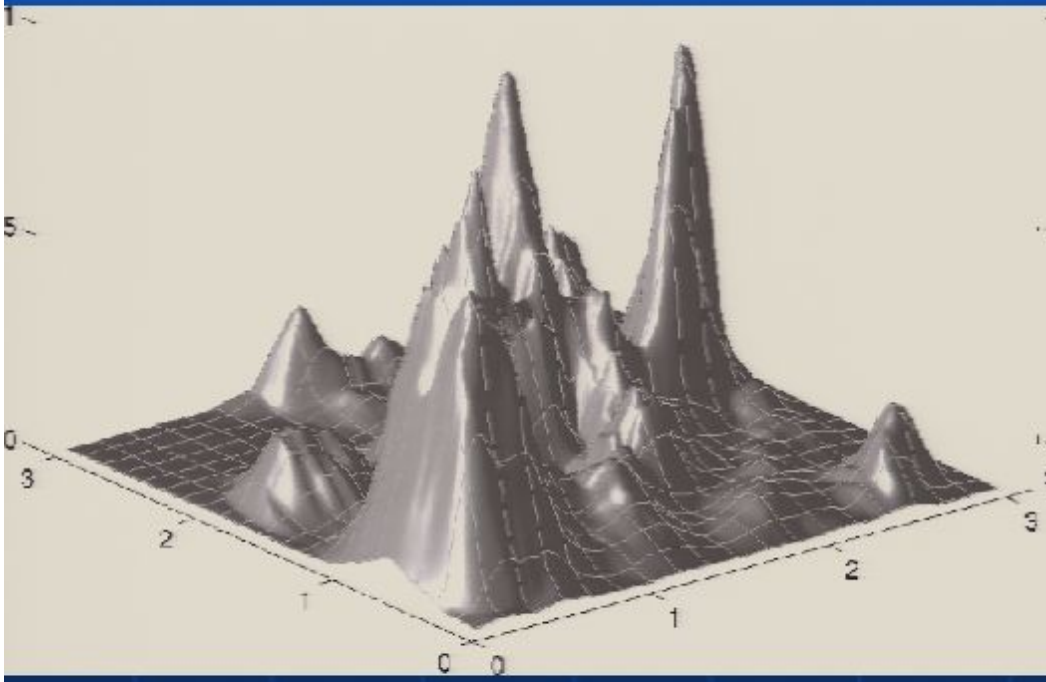
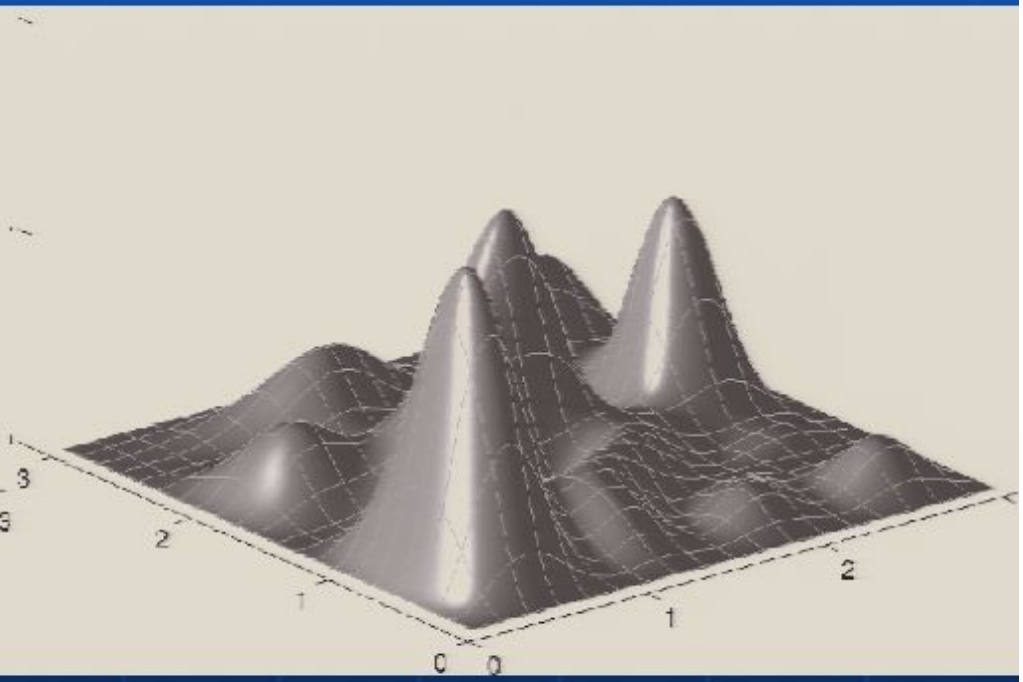


P(x,y) at t=2π

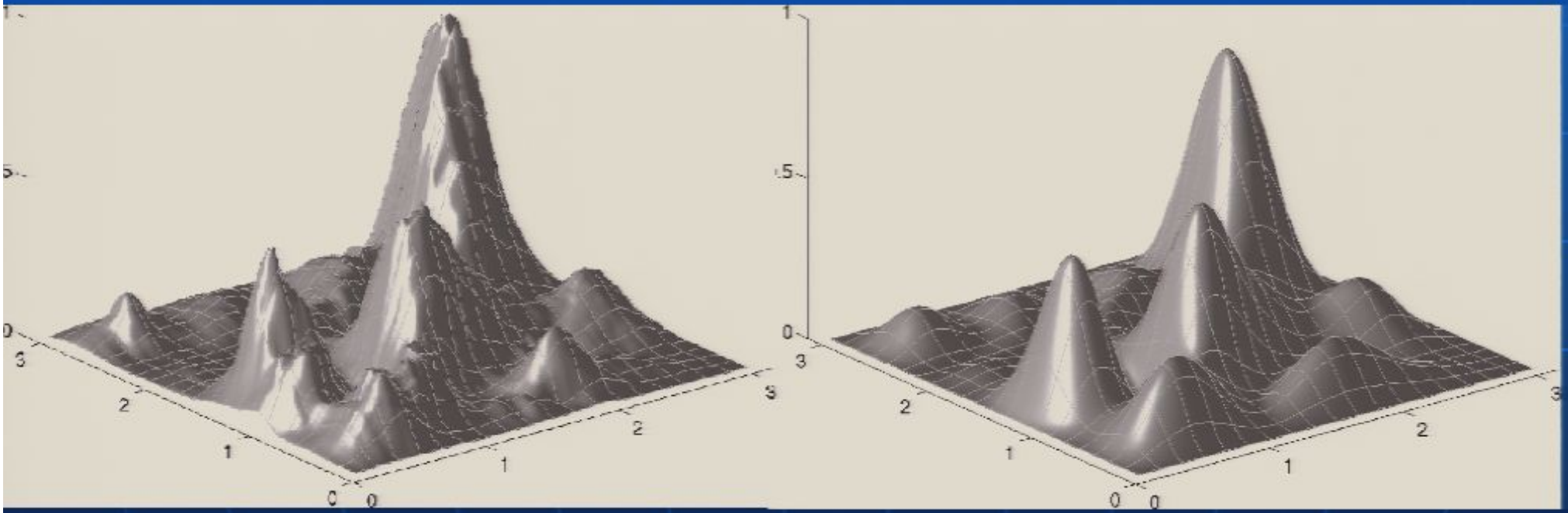


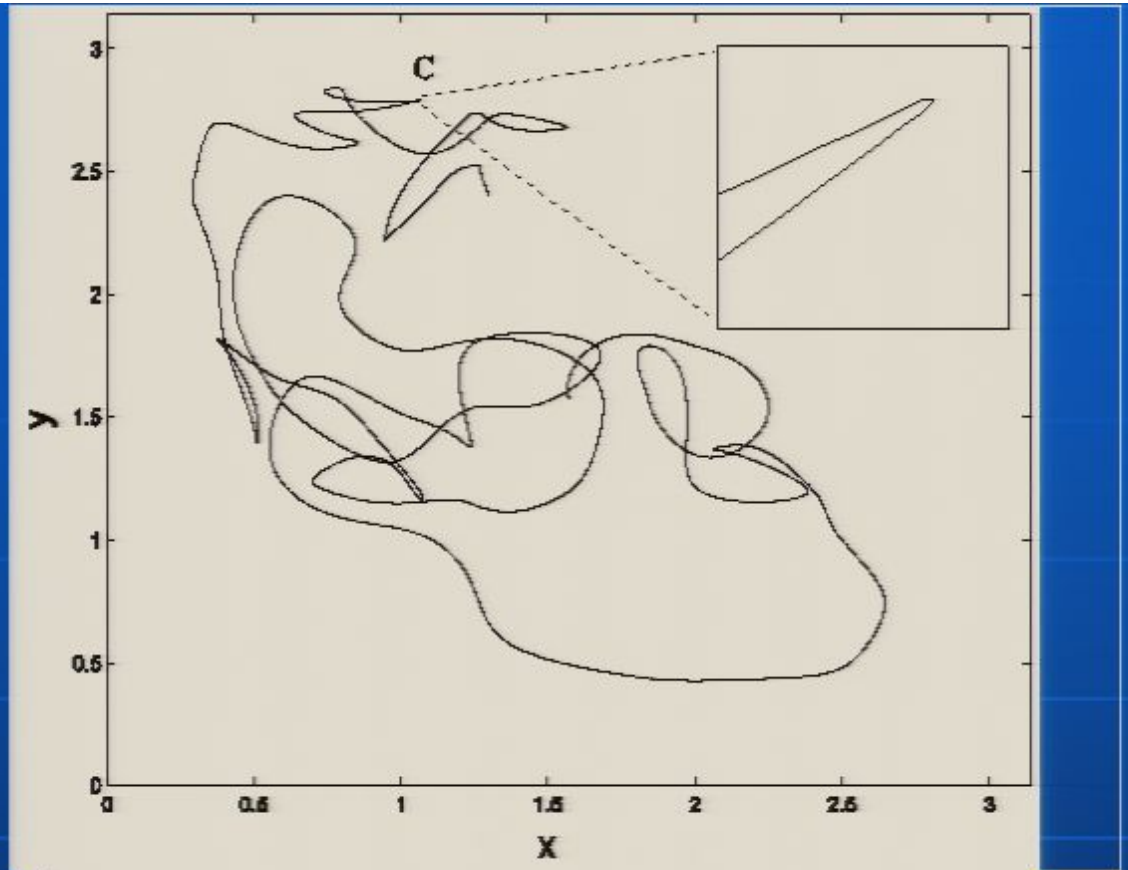

$|\psi(x,y)|^2$ at t=2π



P(x,y) at t=4π

$|\psi(x,y)|^2$ at t=4π

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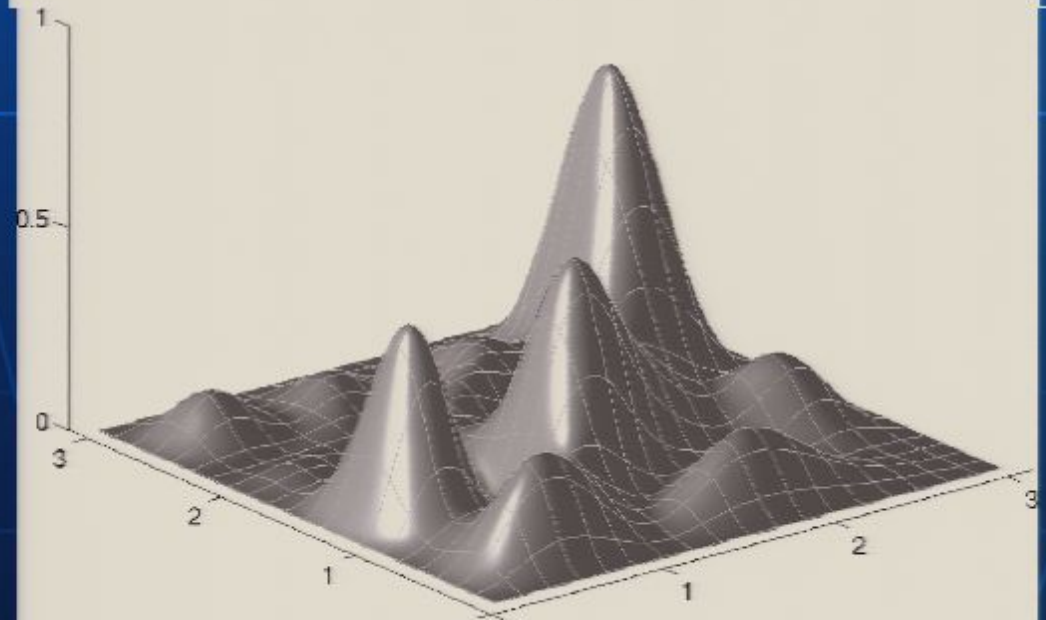
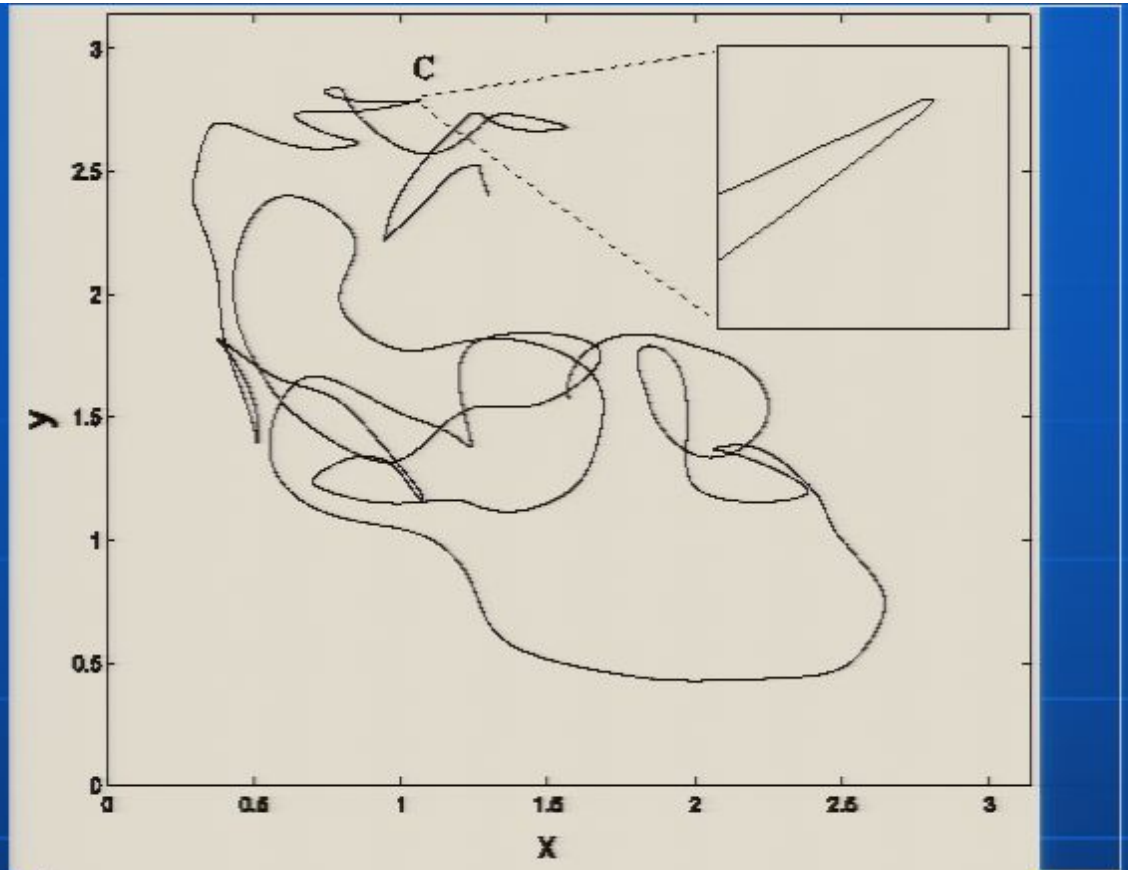

1
0.5
0
3
2
1
1
2
3

# Dynamics

In classical theory X evolves according to Newtons laws F=mA.

In deBroglie-Bohm theory X evolves according to the non-classical equations

$$m\frac{dX}{dt} = \mathrm{Im}\left(\frac{\nabla\Psi}{\Psi}\right)$$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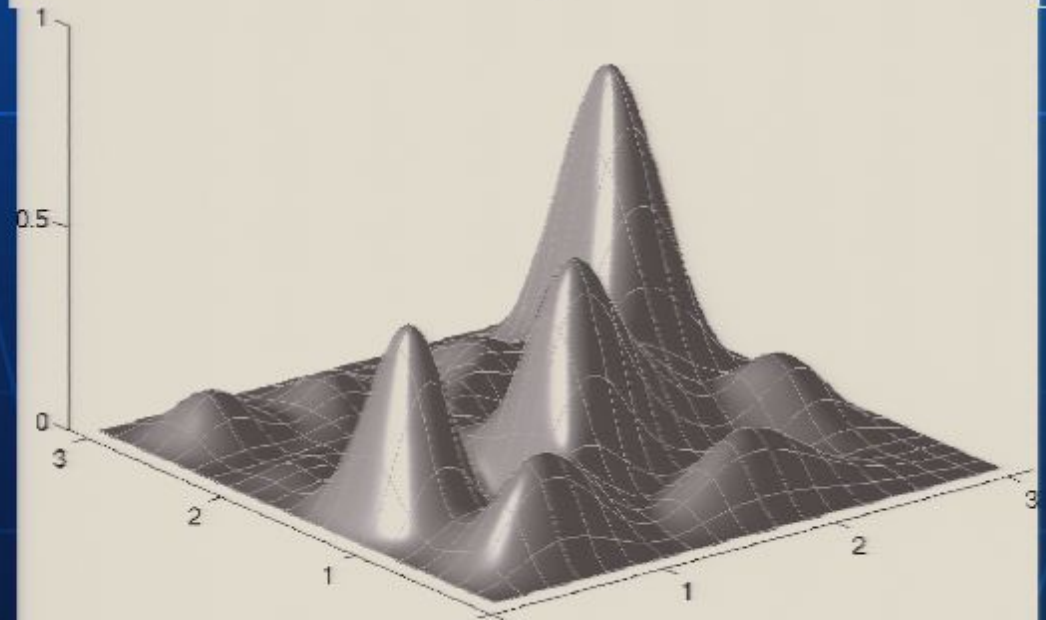
1
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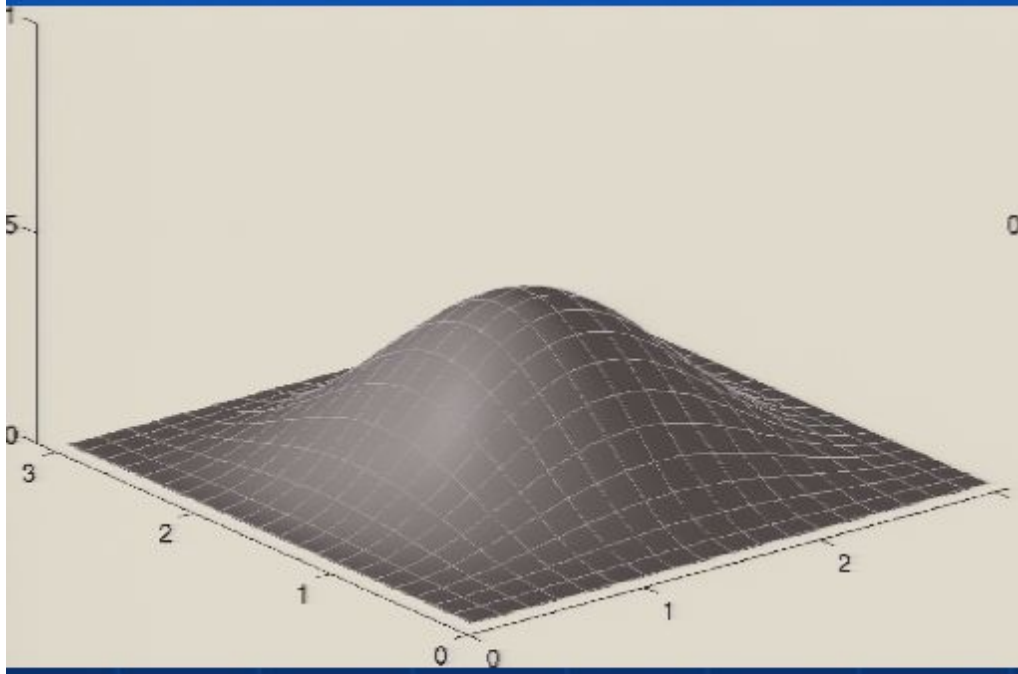
# Good News

The theory is completely well defined, even deterministic, reproduces all the predictions of quantum theory (also also relativistic quantum theory) and the superposition principle is still valid.

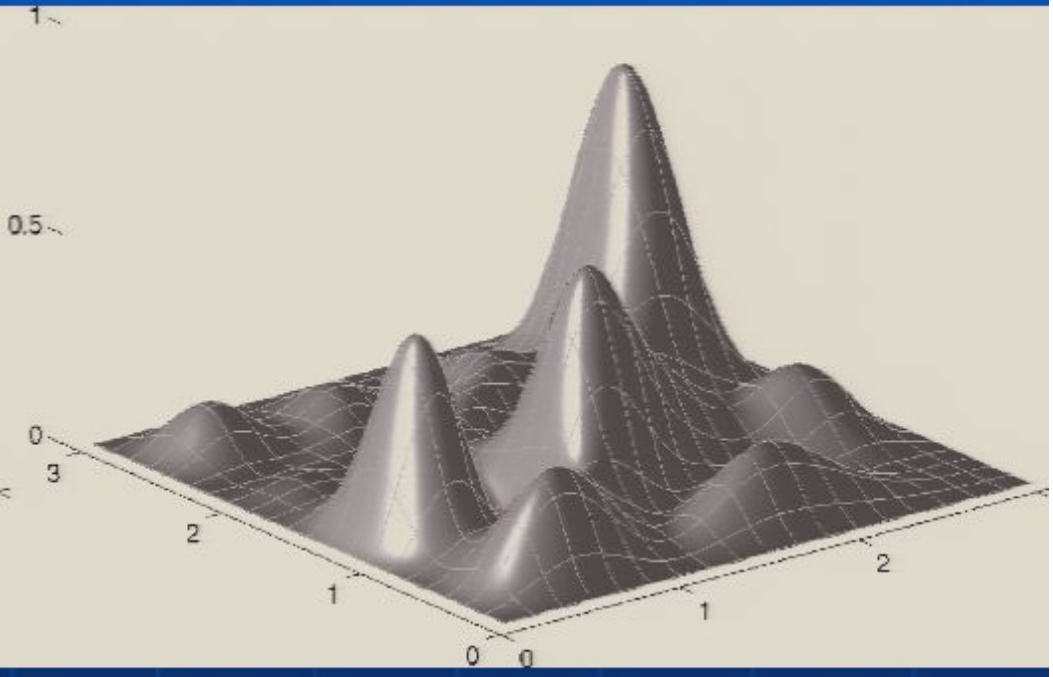
dBB is a much richer theory with quantum theory emerging only in quantum equilibrium.

Explains the quantum statistics as a feature of quantum equilibrium.

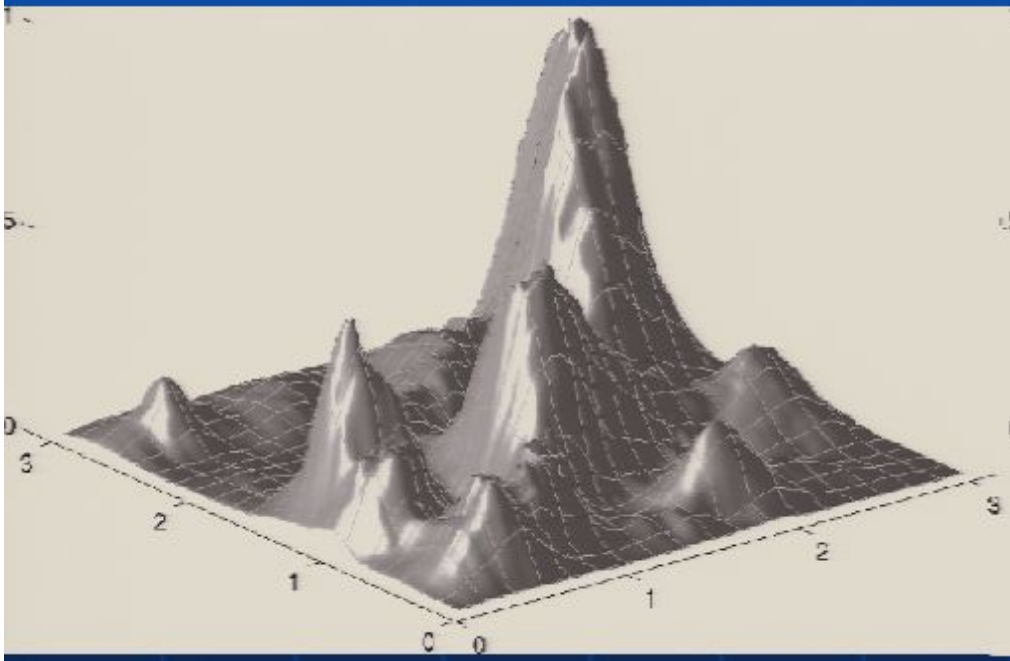
P(x,y) at t=0



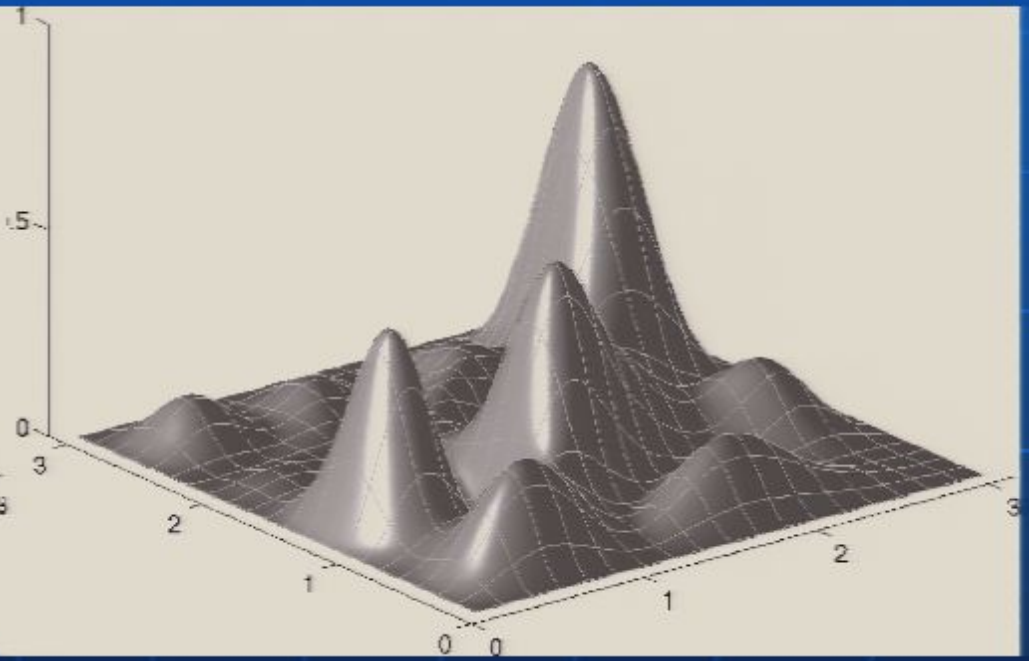

$|\psi(x,y)|^2$ at t=0



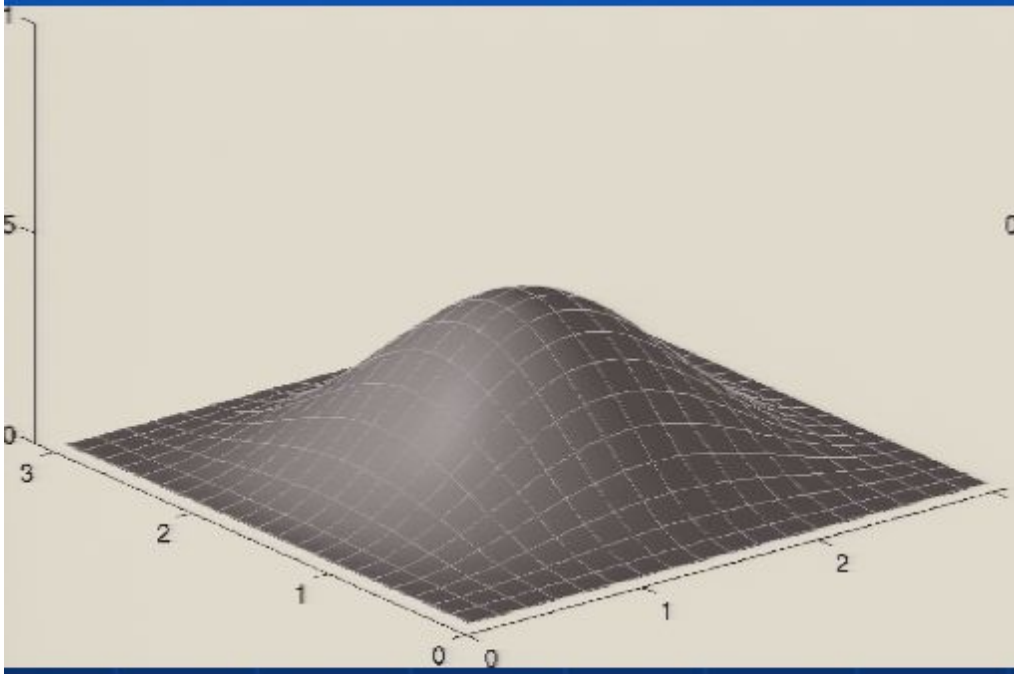
P(x,y) at t=4π



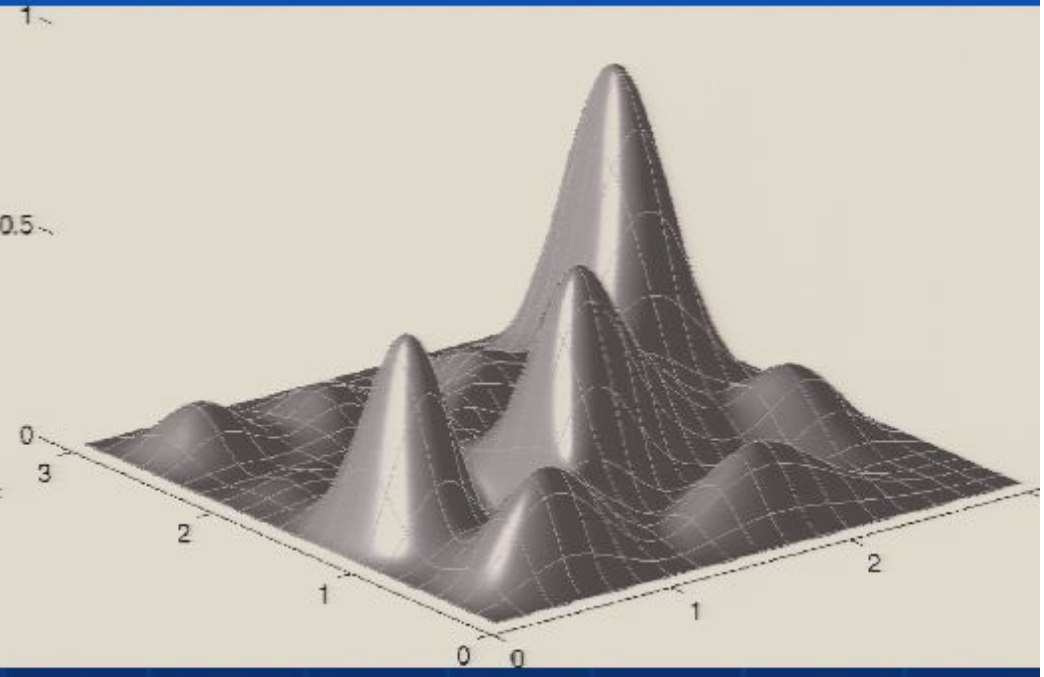

$|\psi(x,y)|^2$ at t=4π



P(x,y) at t=0

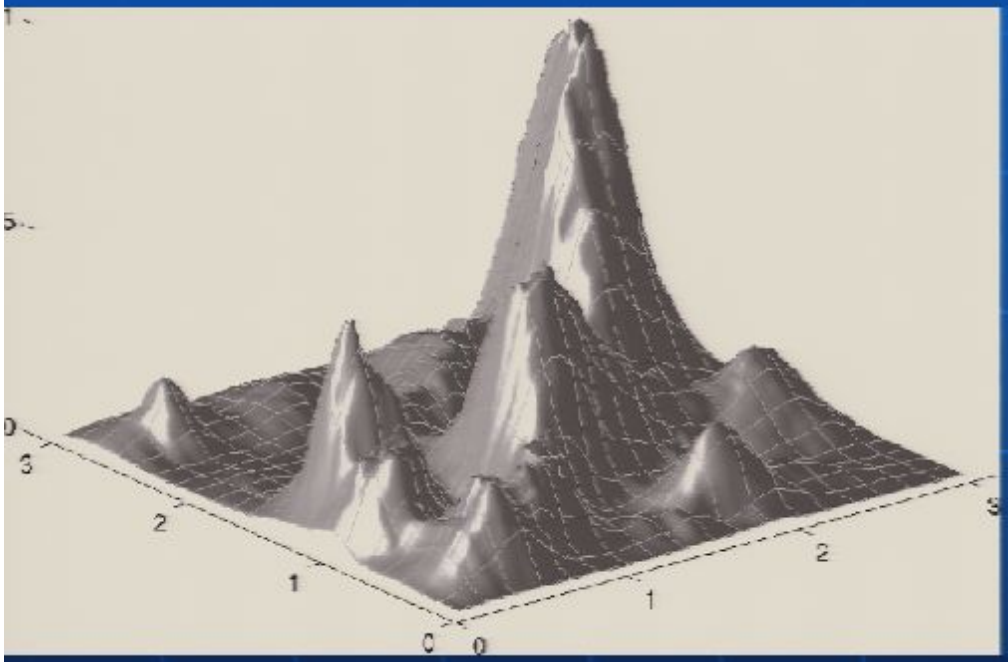



$|\psi(x,y)|^2$ at t=0

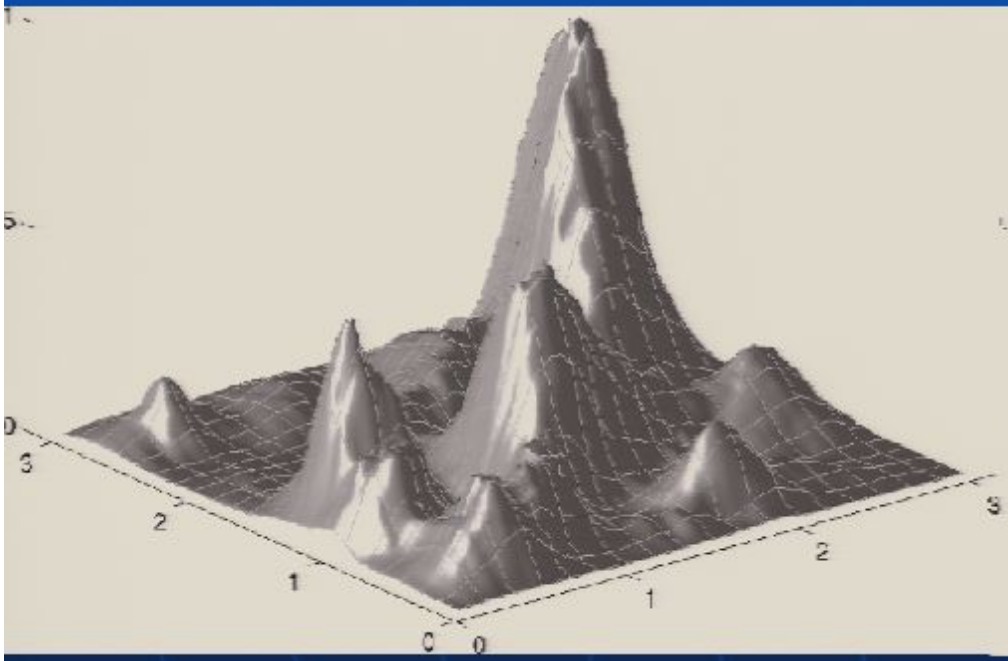


P(x,y) at t=4π

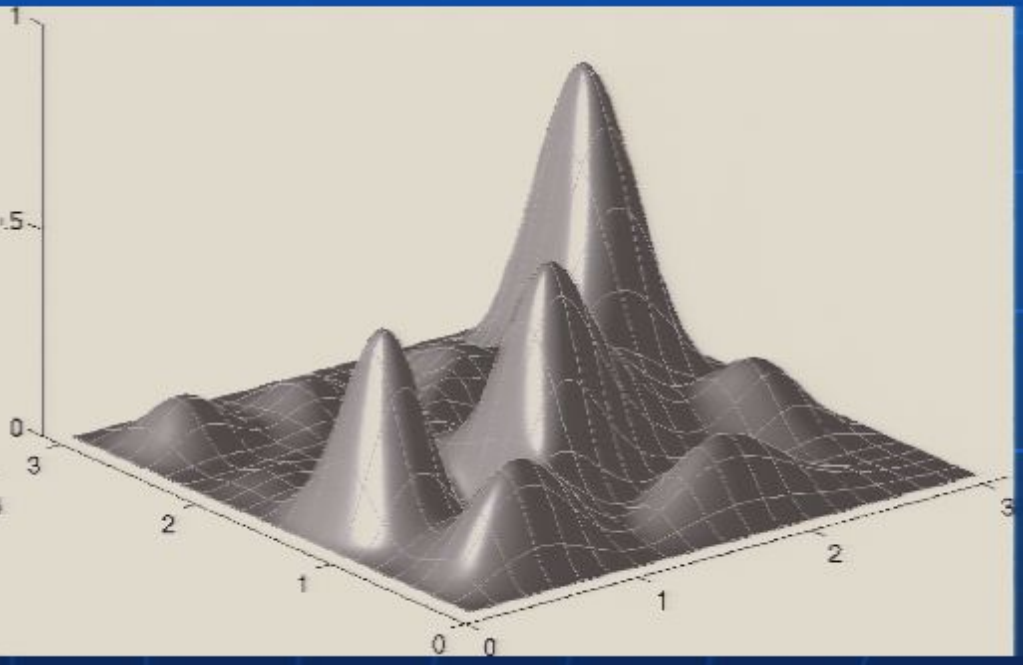
$|\psi(x,y)|^2$ at t=4π

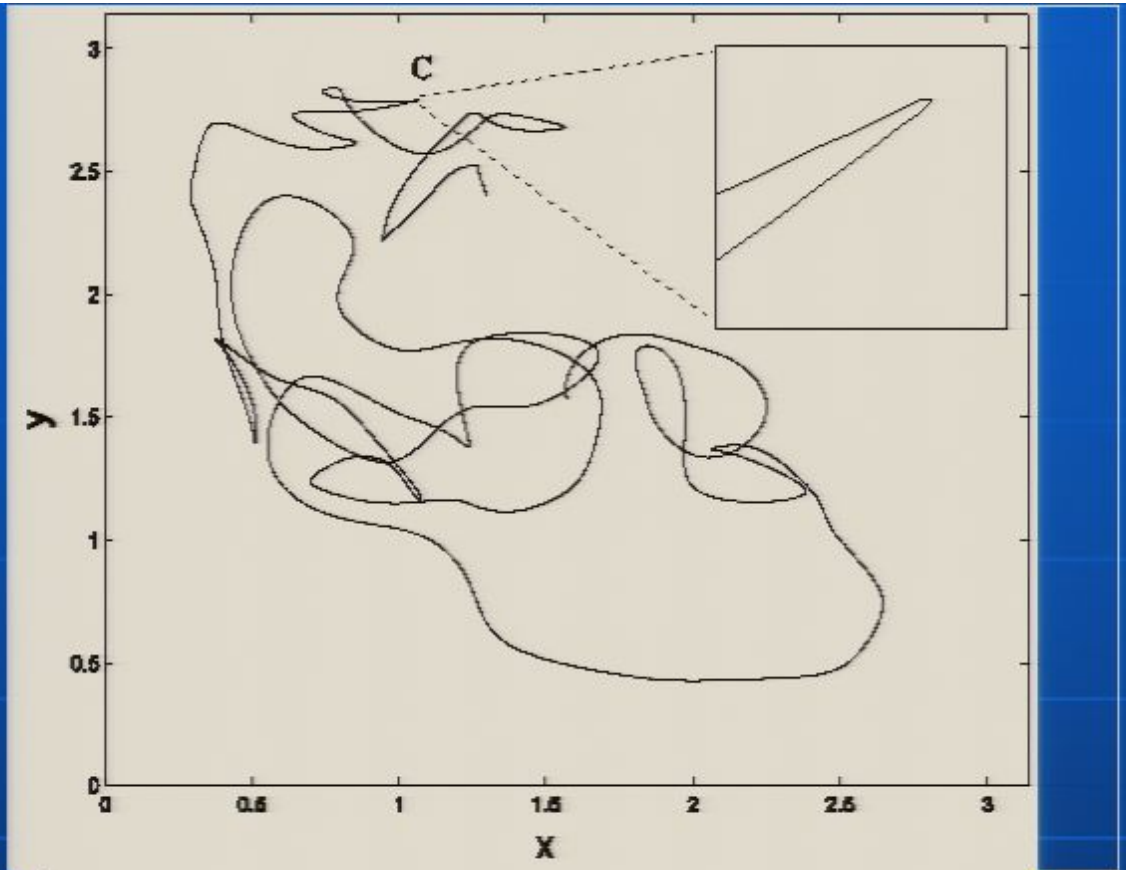


P(x,y) at t=4π



$|\psi(x,y)|^2$ at t=4π

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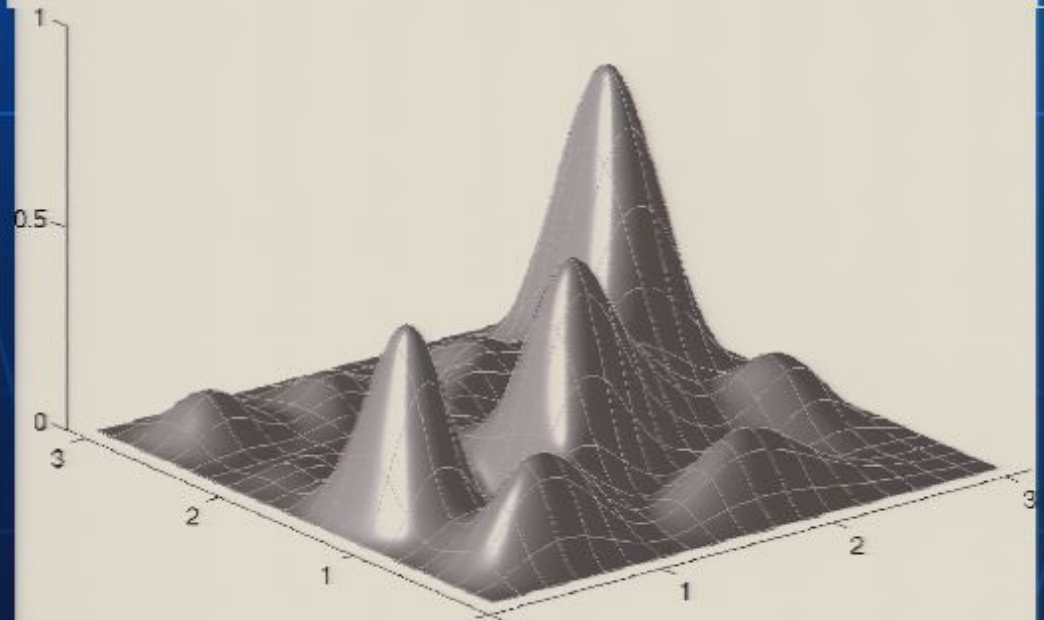
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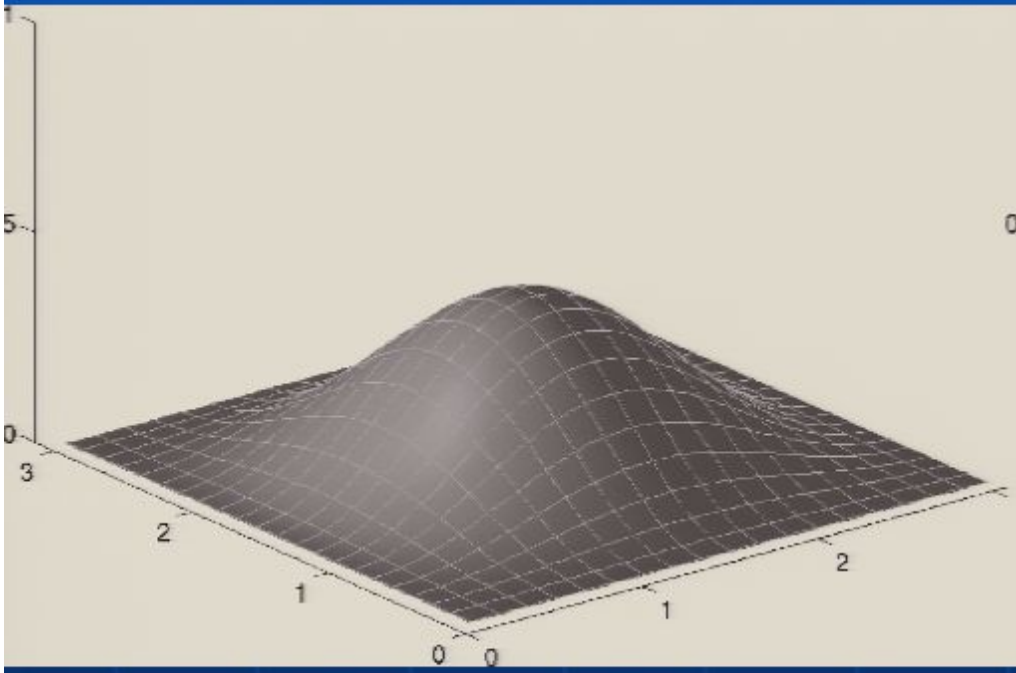
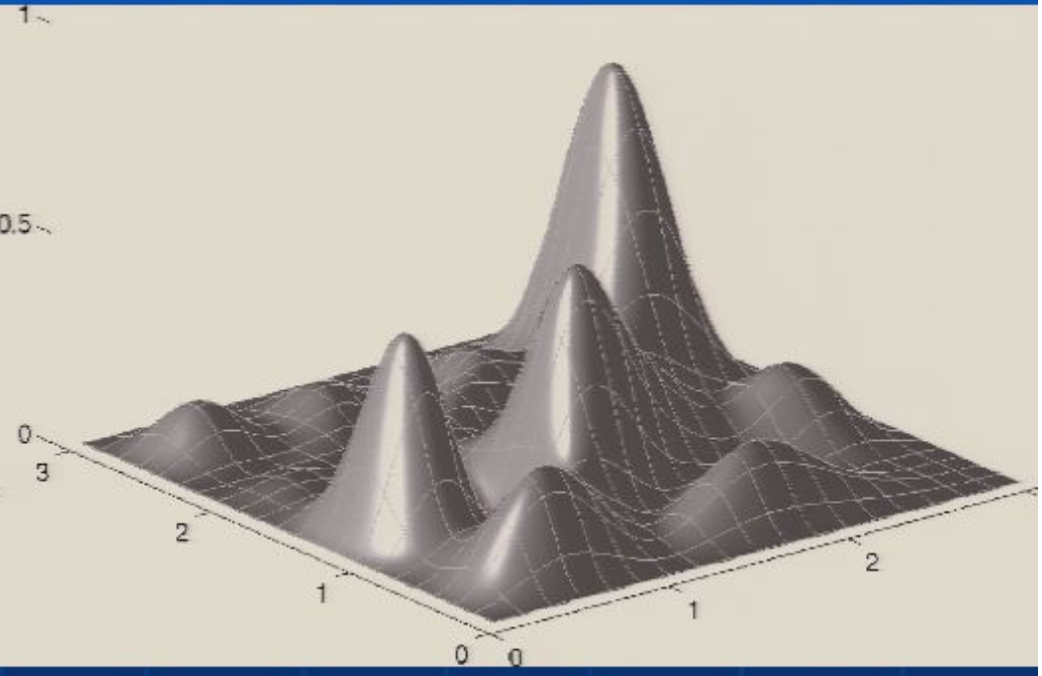
P(x,y) at t=0

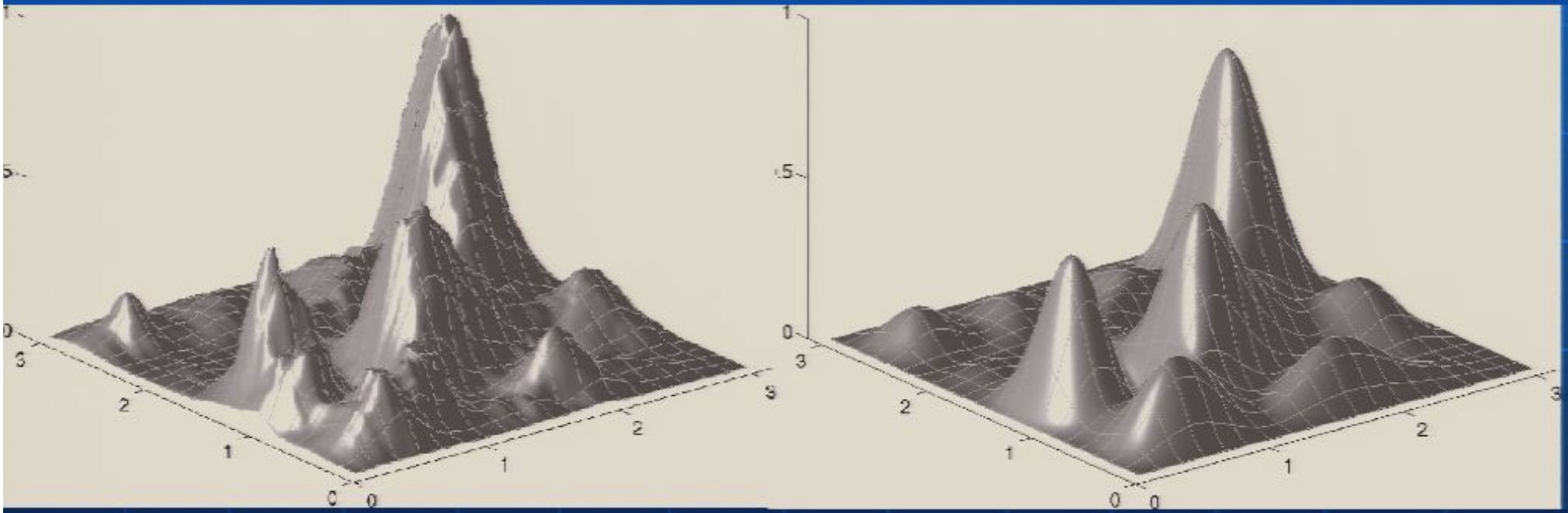



$|\psi(x,y)|^2$ at t=0



P(x,y) at t=4π

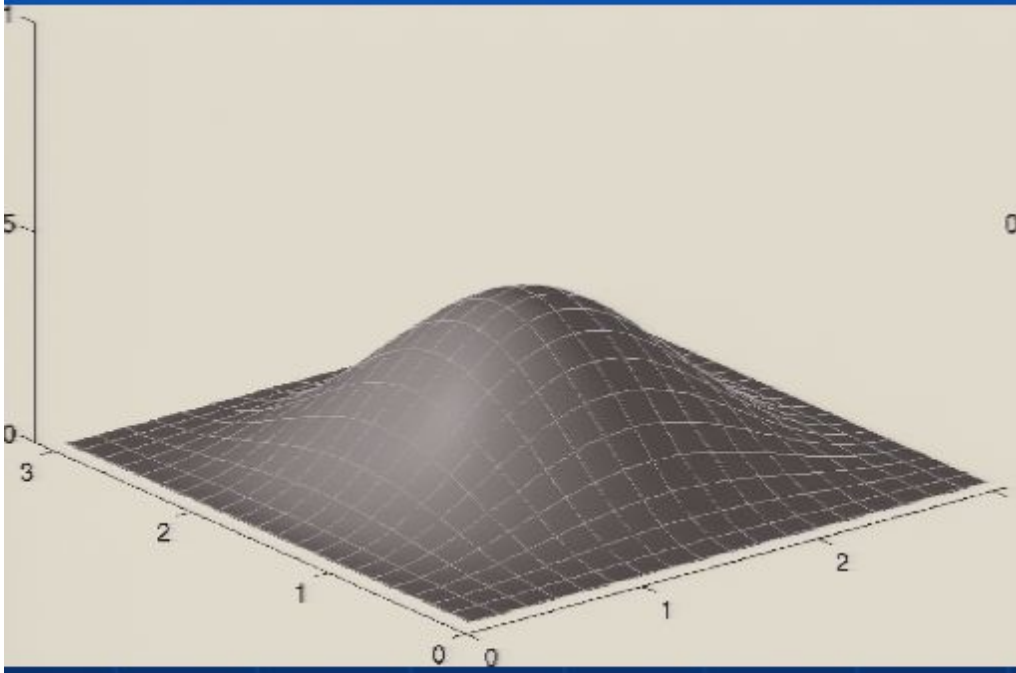
$|\psi(x,y)|^2$ at t=4π



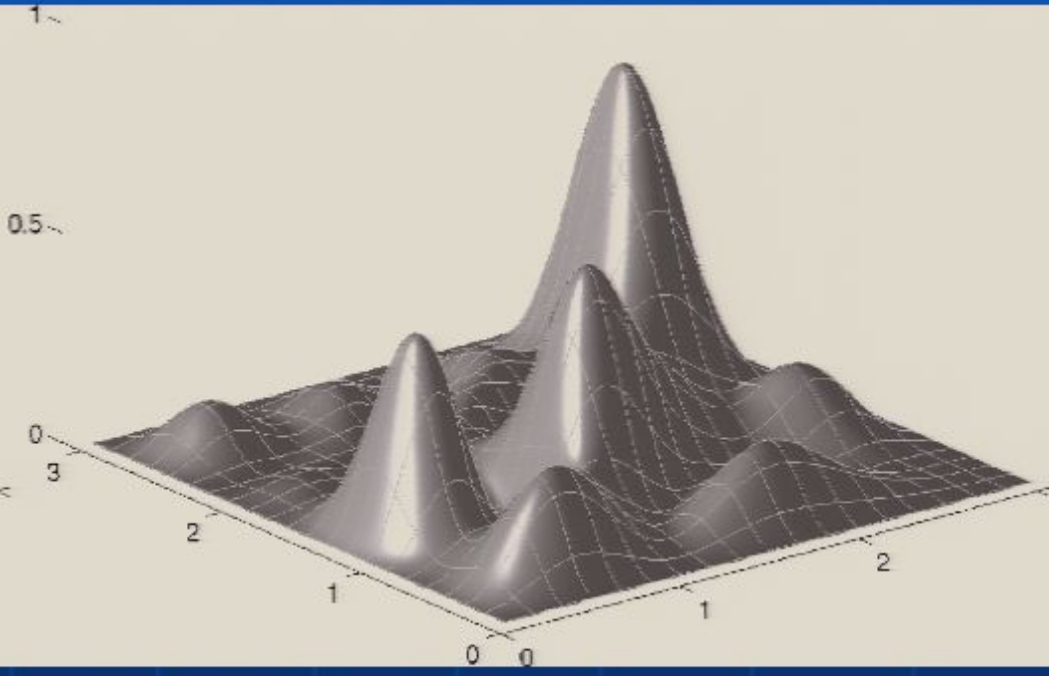
# Conclusion

- Quantum theory is an extremely successful theory. Yet it is hard to see how it really can be a fundamental theory.
- Out of the interpretations only the collapse theories and hidden variable theories are precisely formulated wihtout vague concepts like 'classical', microscopic.
- But both of these are different theories with different predictions than quantum theory.

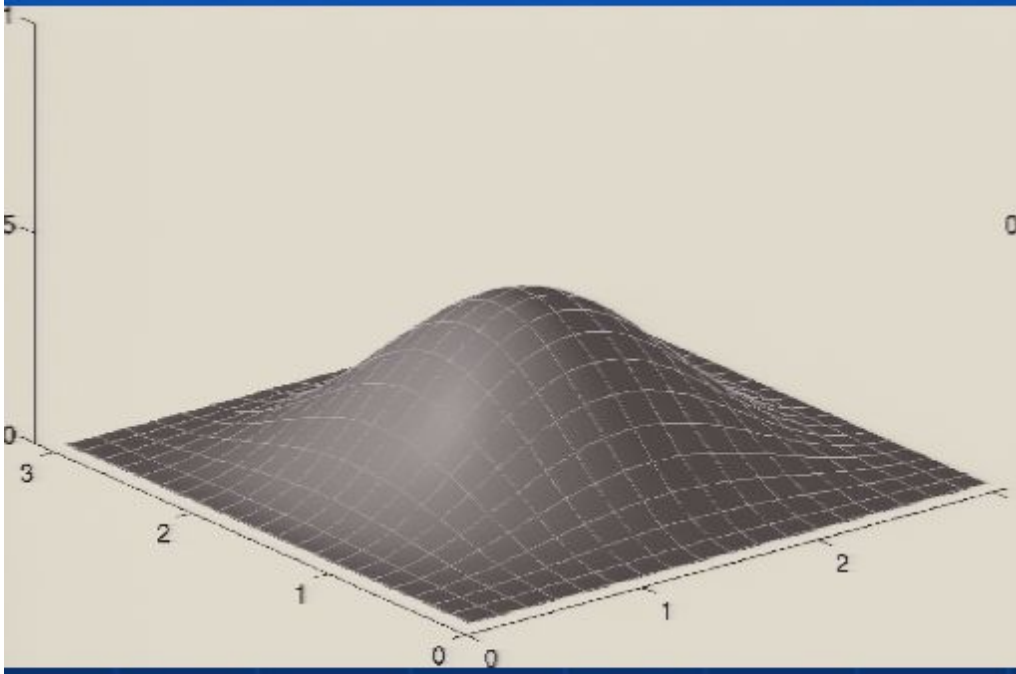
P(x,y) at t=0



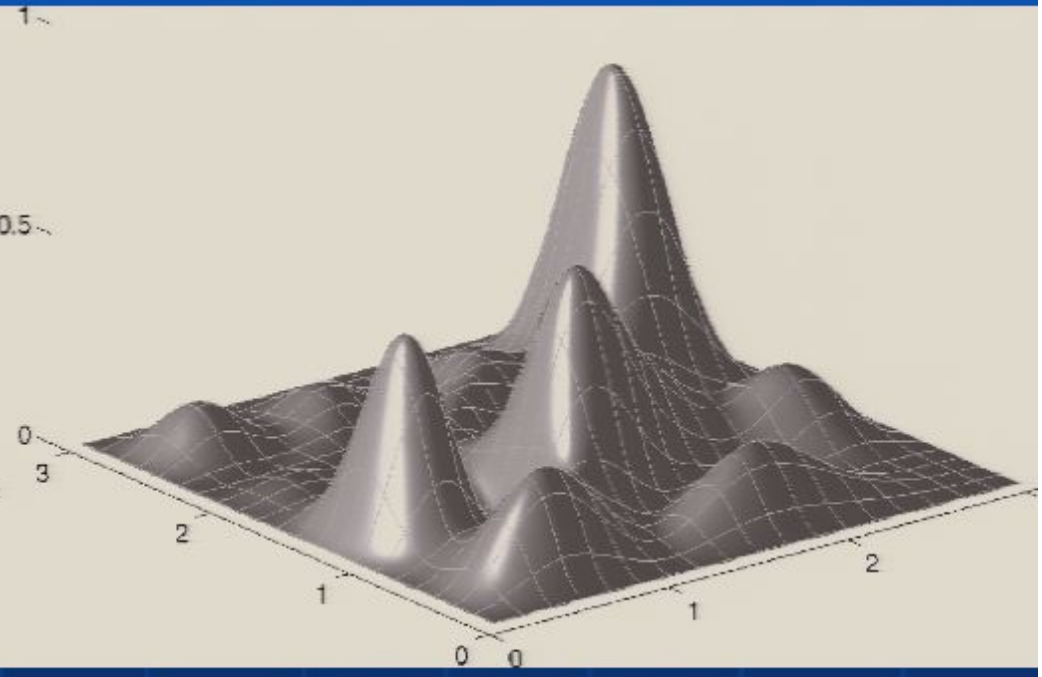

$|\psi(x,y)|^2$ at t=0



P(x,y) at t=0




$|\psi(x,y)|^2$ at t=0



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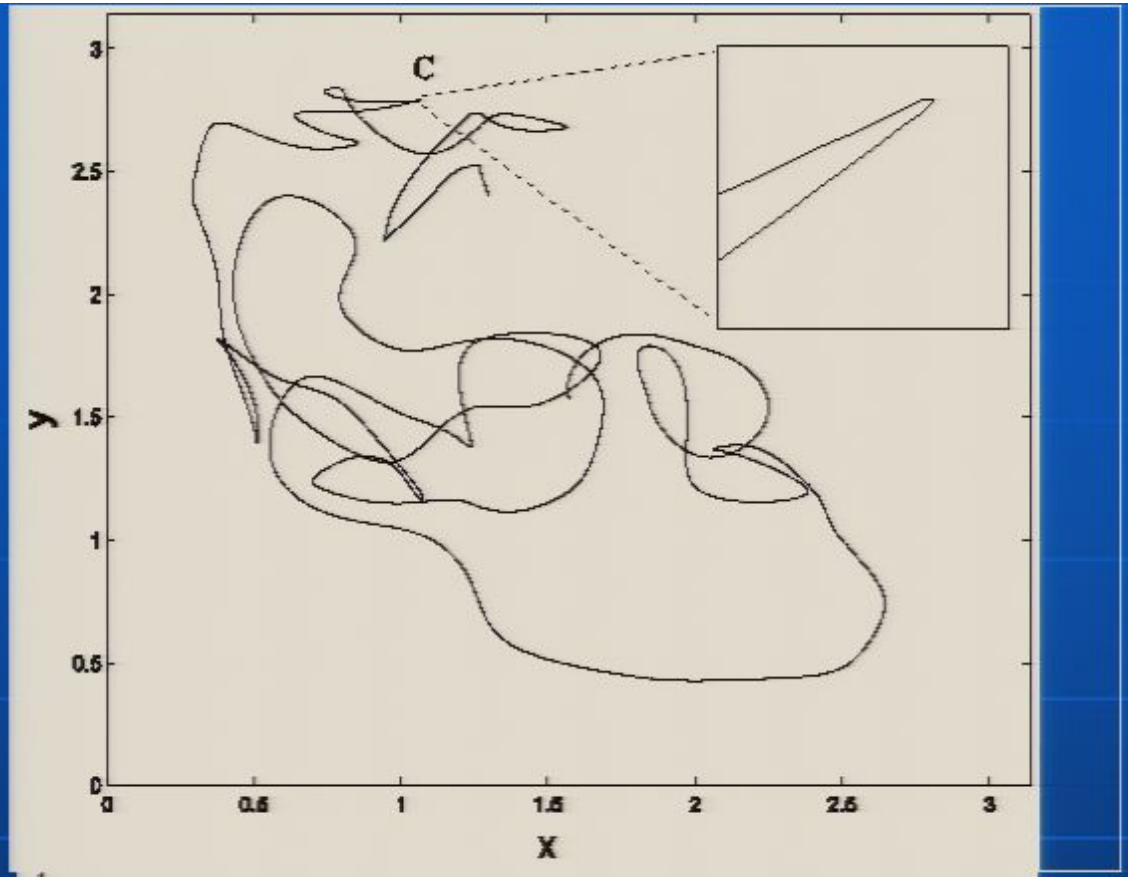
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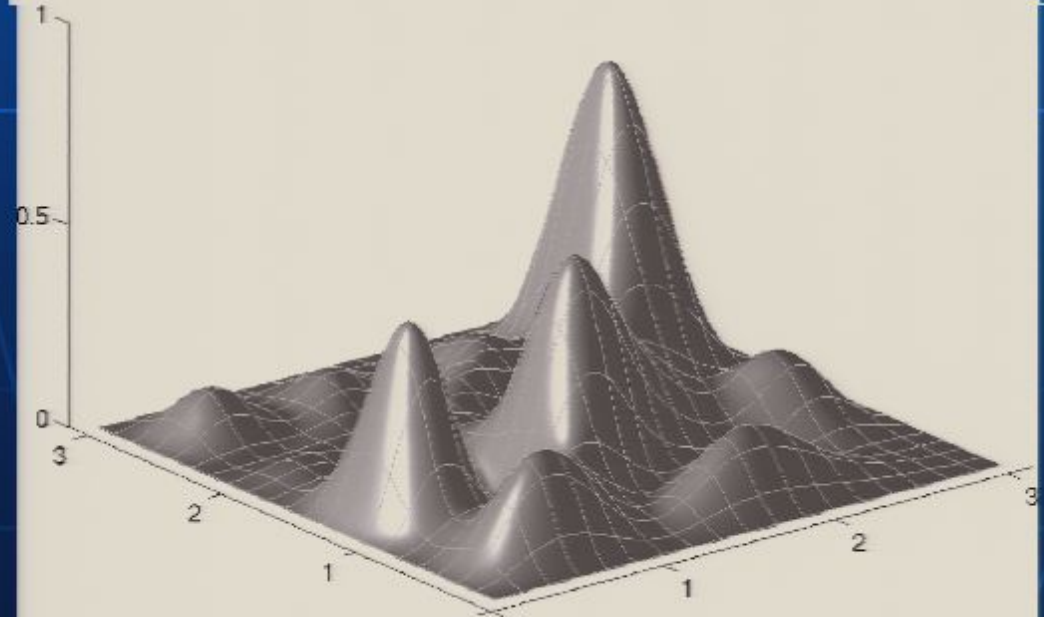
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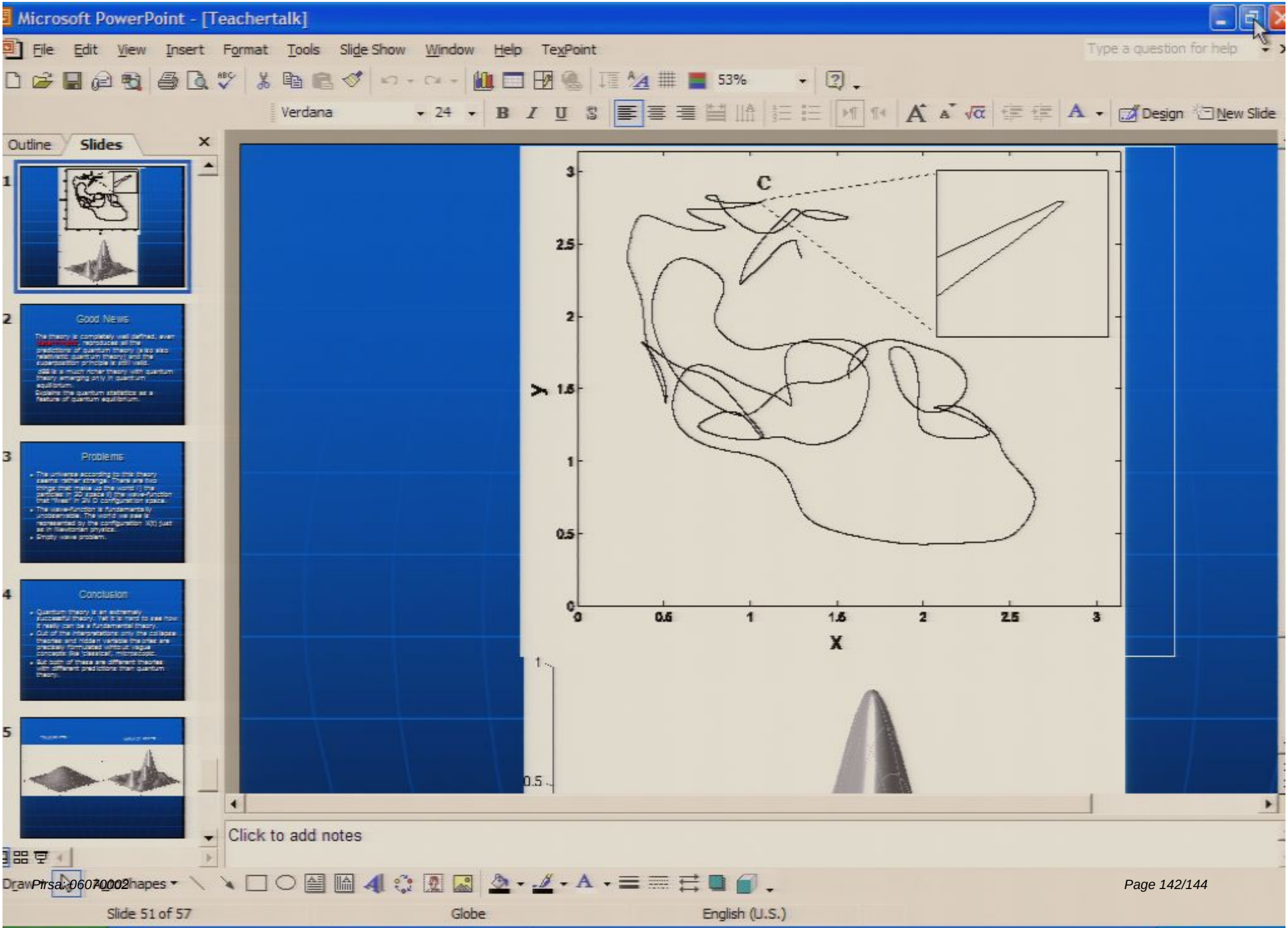
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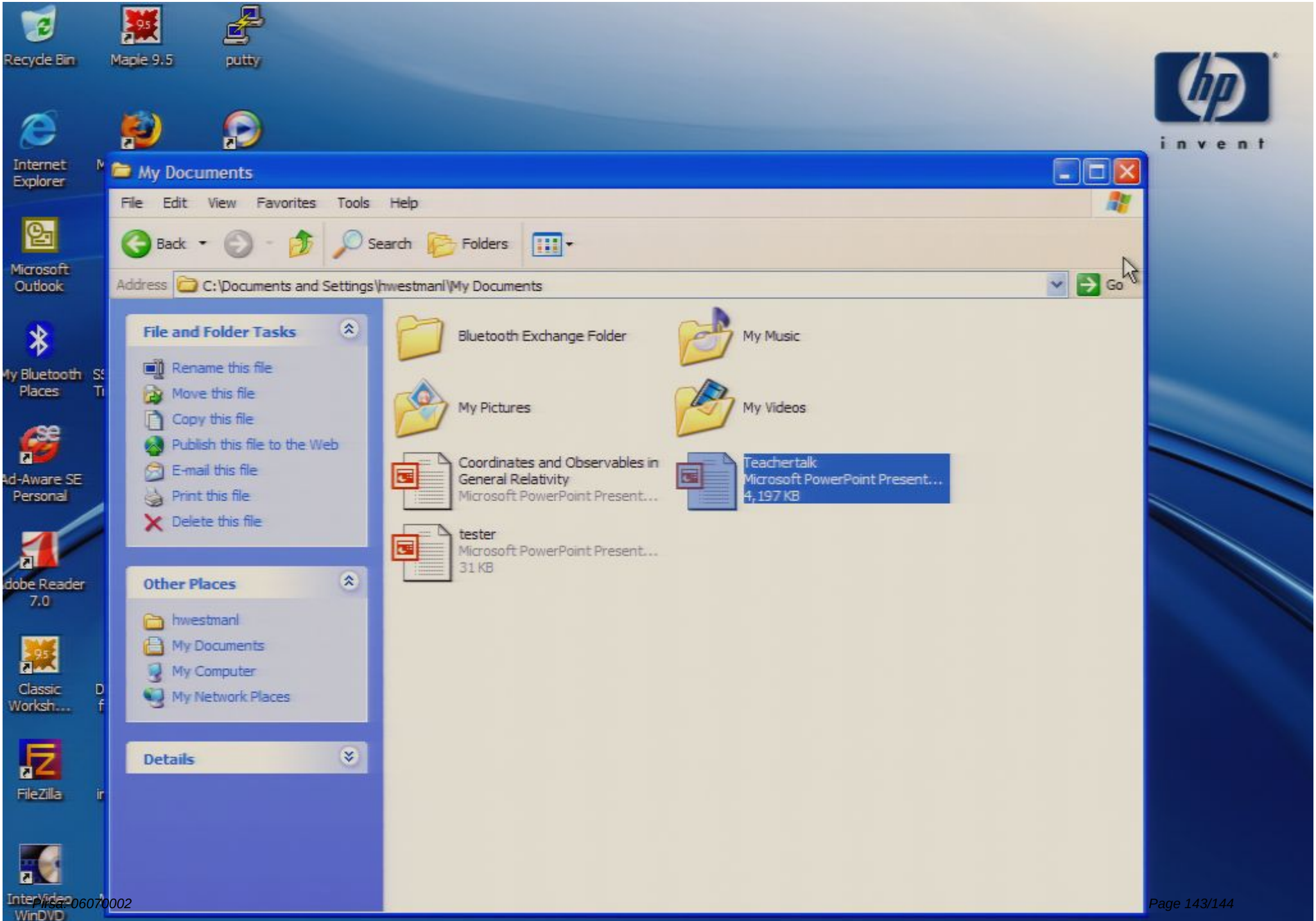
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invent
My Documents
File Edit View Favorites Tools Help
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Move this file
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Publish this file to the Web
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Print this file
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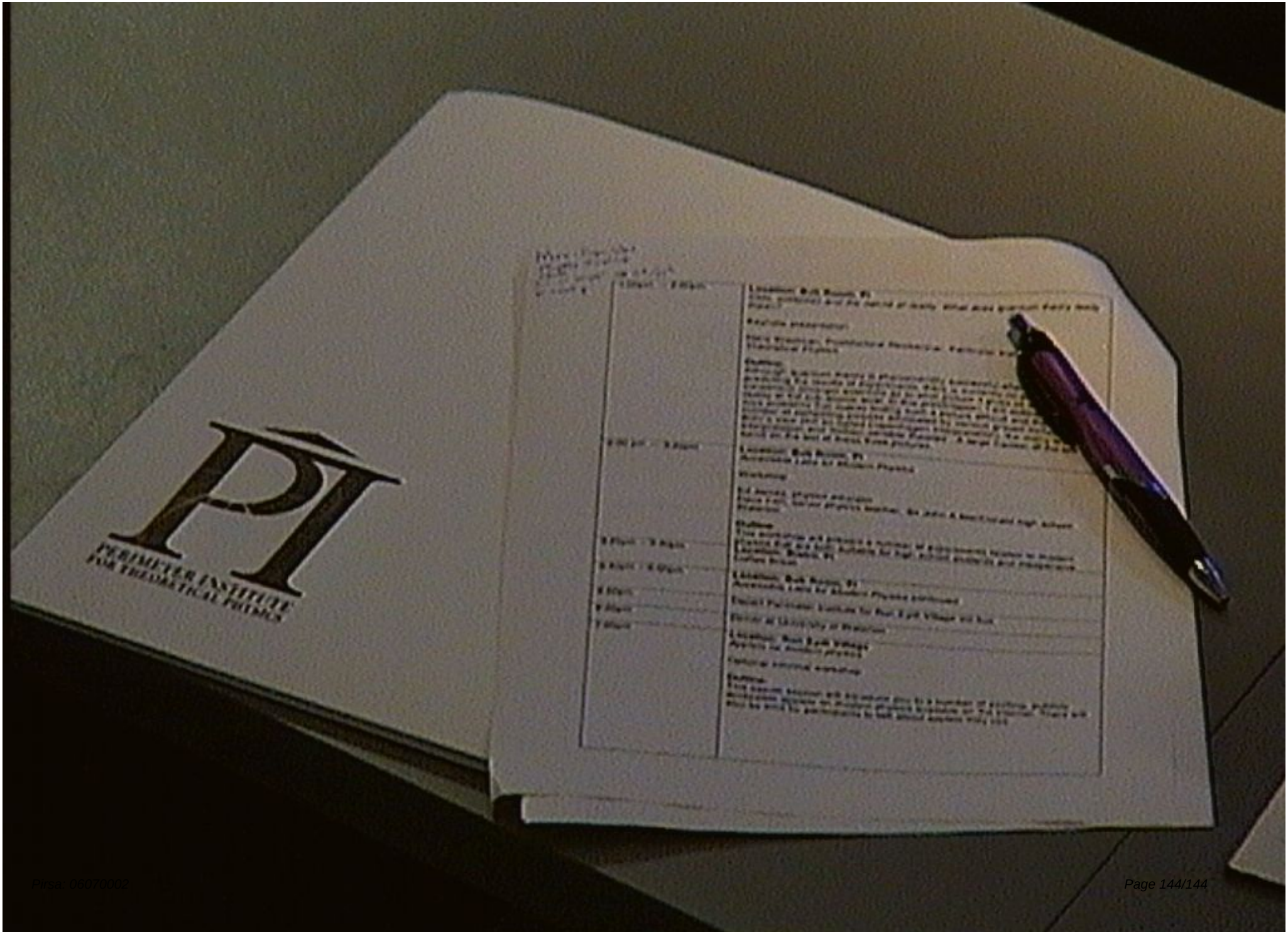
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