

Title: Testing the equivalence principle in the dark sector

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Abstract:

PROBING THE DARK SECTOR WITH THE EQUIVALENCE PRINCIPLE

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(with Paul Steinhardt)

The dark energy problem: is dark energy dynamical or due to a cosmological constant?

- Why is the cosmological constant so small?
(Anthropic explanation? A dynamical explanation?)
- Dynamical dark energy can solve the cosmic coincidence problem (quintessence trackers, k -essence)

Measuring the equation of state

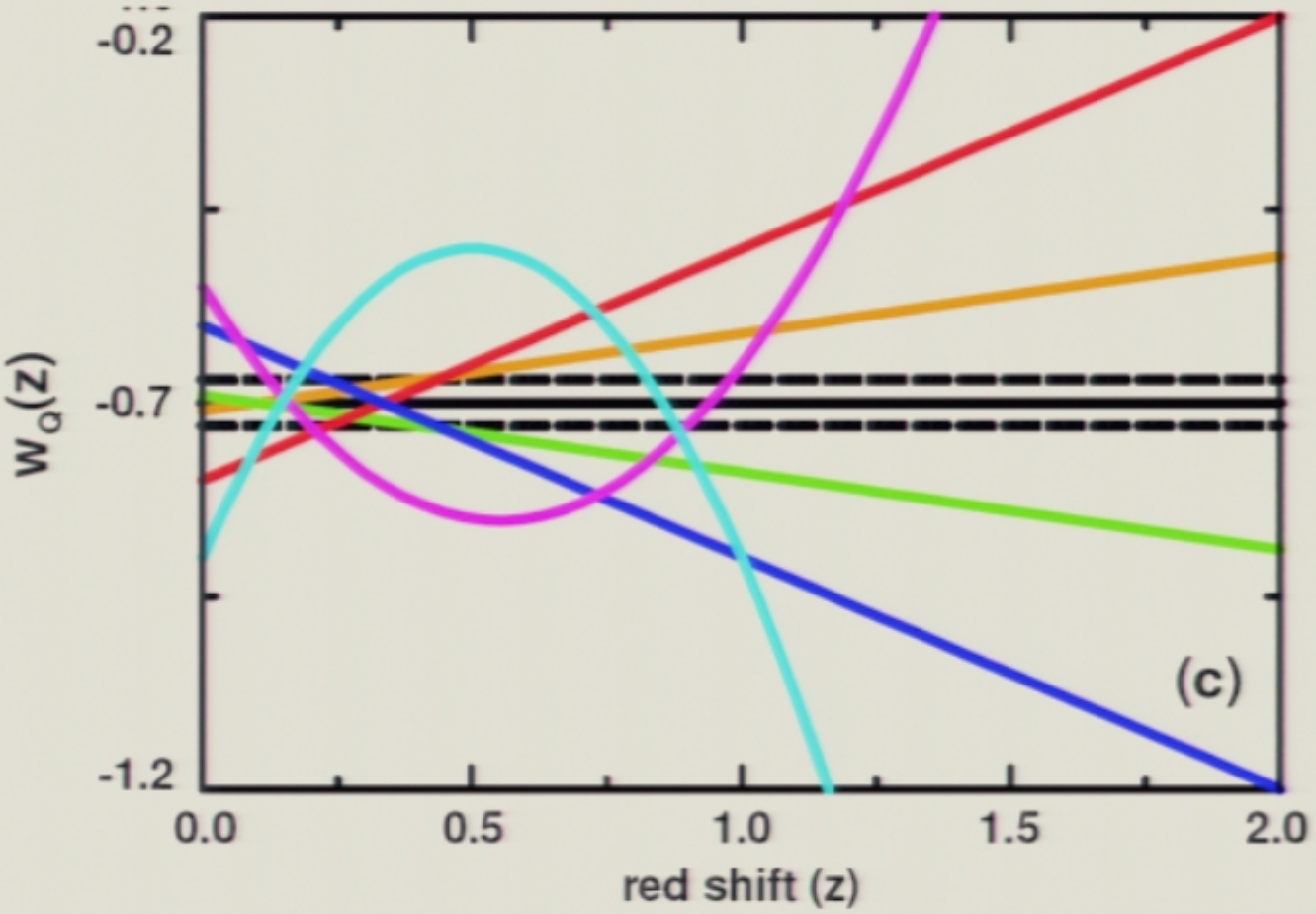
- A detection of $w + 1$ is unambiguous evidence of dynamical dark energy, however
- $w + 1$ is constrained indirectly by supernovae

$$d_L = \frac{1+z}{H_0} (1 + \Omega_m / \Omega_Q)^{1/2} \int_1^{1+z} \frac{dx}{x^{3/2}} \left[\frac{\Omega_m}{\Omega_Q} + \exp\left(3 \int_1^x \frac{dy}{y} w_Q(y)\right) \right]^{-1/2}$$

and there may be limits to how well it can be measured

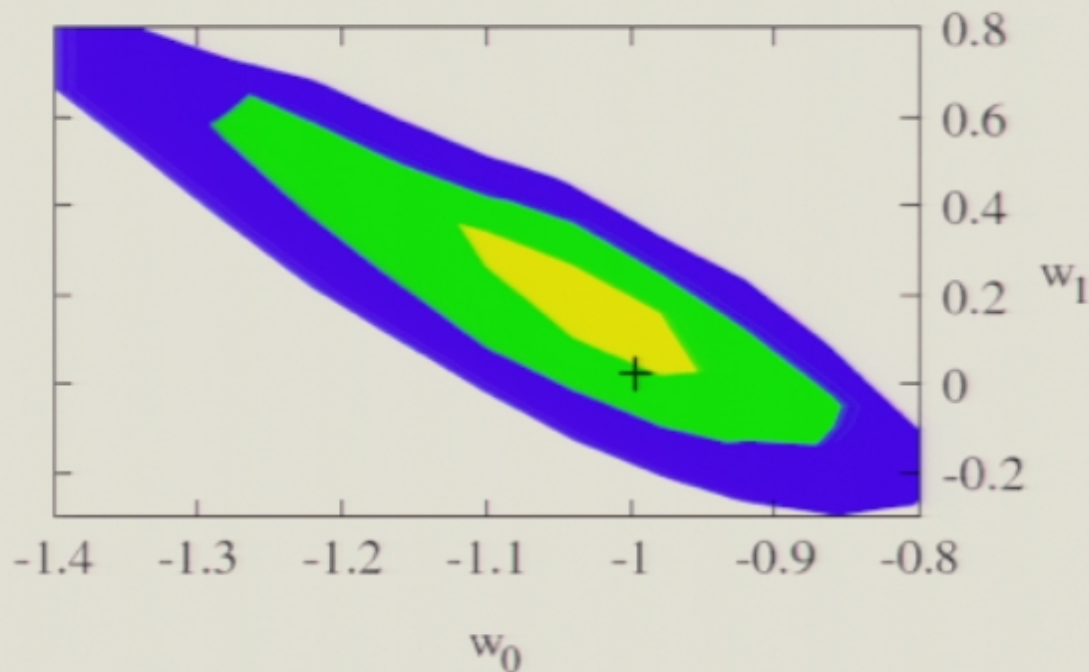
- Some models (e.g. quintessence trackers) predict w approaching -1 in the late universe

d_L agrees to 1%



It may not be possible to *directly* rule out quintessence

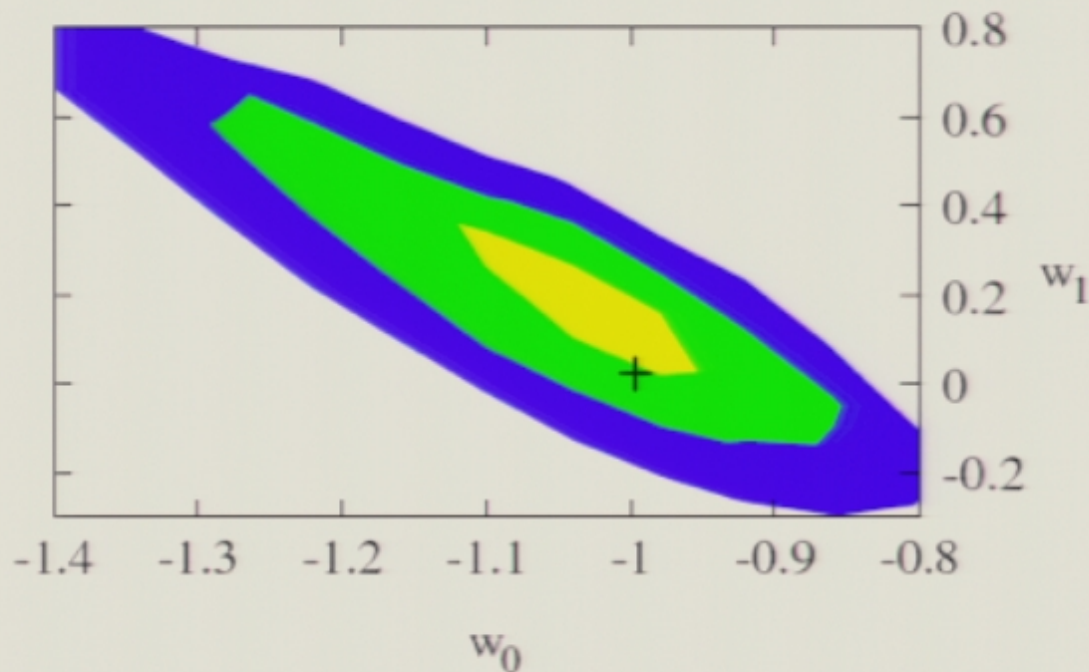
- 8 years of WMAP, 2,000+ supernovae, large-scale structure and weak lensing may only give $\Delta w < 0.10$
and $\Delta dw/dz < 0.18$ (at 1σ).



(Upadhye *et al.*, 2004)

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Alternative: look for model-dependent signatures of dark energy

1. Dark energy perturbations
2. In this talk: look for equivalence principle violating interactions
 - The minimally coupled quintessence model of dark energy is an idealization
 - Equivalence principle violations are predicted by compactification, string/M theory moduli etc...

What kinds of effects arise?

Violations of:

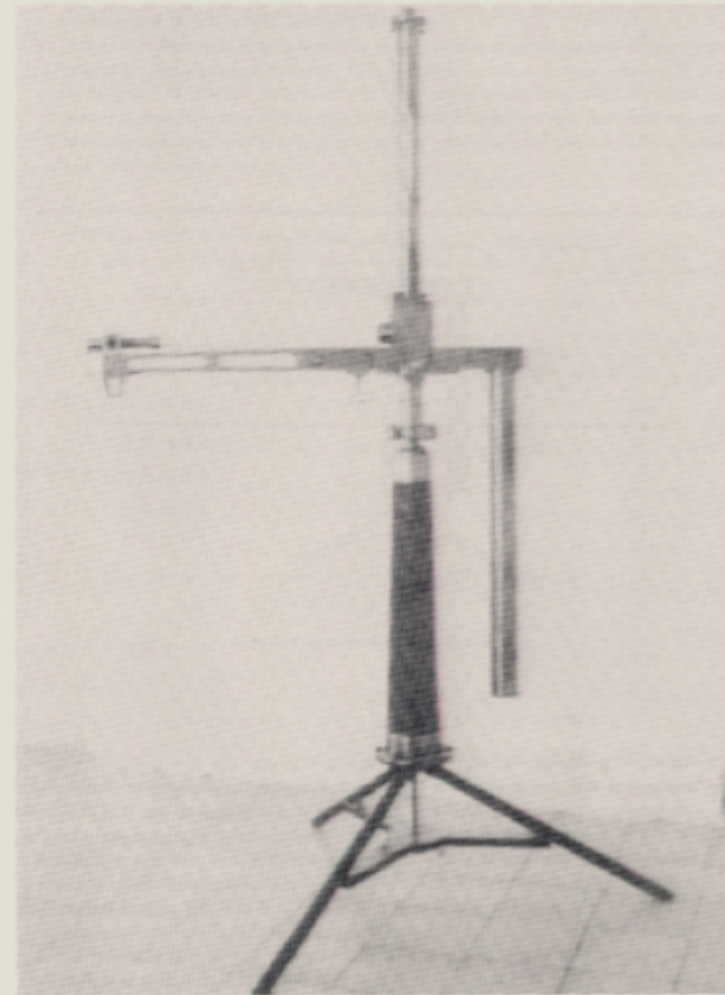
- the universality of free fall
- variation of fundamental constants
- deviations from general relativity

Universality of free-fall

- Test of differential acceleration

$$\eta = 2 \frac{|a_1 - a_2|}{|a_1 + a_2|}$$

- Eötvös torsion-balance experiment
 $\eta < 10^{-12}$ (Braginsky & Panov, '72)
 $\eta < 2 \times 10^{-13}$ (Eöt-Wash)



Eötvös's experiment

Variation of fundamental constants

Fine-structure constant

$$\Delta\alpha/\alpha < 10^{-7} \quad d \log \alpha/dz < 8 \times 10^{-7} \quad (\text{Oklo, } z=0.15)$$

$$d \log \alpha/dz = 9 \times 10^{-6} \quad (\text{Keck/HIRES QSO, } z < 4, 5\sigma)$$

$$d \log \alpha/dz < 3 \times 10^{-6} \quad (\text{VLT/UVES, } z < 2, 3\sigma)$$

Constraints on Newton's constant:

- High-redshift

$\Delta G/G$ no more than 40% since nucleosynthesis (Accetta, 1990)

- low-redshift

$d \log G/dz < 10^{-2}$ (stellar physics, pulsars, ranging etc...)



Metric tests of gravity



Precision tests of general relativity

- Lunar laser ranging
- Deflection of distant radio sources by the sun
- Time-delay experiments

Constrains Eddington (or PPN) parameter $\gamma - 1 < 5 \times 10^{-5}$
(related to Brans-Dicke parameter $\omega > 40,000$)

$$\gamma = \frac{1+\omega}{2+\omega}$$

The problem: equivalence principle violations are tightly constrained

- Couplings should generically be gravitational strength (*i.e.* suppressed by the Planck constant).
- The generic “prediction” is that $\Delta\alpha/\alpha$, $\Delta G/G$, γ , ω , η are of order unity, which is in conflict with observation.
- Gravity is hard to modify.

Dynamical compactifications violate the EP (at some level)

- Kaluza-Klein theory is a mess (Fierz, 1956)
 - includes variation of the coupling constant of the Kaluza-Klein one-form

$$\frac{1}{2} \int d^4x \sqrt{-h} (R_4[h] - (\partial\phi)^2 + \frac{1}{4} e^{\sqrt{6}\phi} F^2)$$

- couplings of the radion and one-form all throughout the matter sector

Dynamical compactifications violate the EP (at some level)

- The simplest S^1/Z_2 compactification (*i.e.* compactification on an interval) is better.

$$\int d^5x \sqrt{-h} \left(\frac{1}{2} R_4[h] - \frac{1}{2} (\partial\phi)^2 + e^{-\sqrt{8/3}\phi} \mathcal{L}_0[\Phi_{i,0}; e^{-\sqrt{2/3}\phi} h_{\mu\nu}] \right. \\ \left. + e^{-\sqrt{8/3}\phi} \mathcal{L}_1[\Phi_{i,1}; e^{-\sqrt{2/3}\phi} h_{\mu\nu}] \right),$$

Matter fields on orbifold planes all couple to the same conformally rescaled metric (this is a *universal* coupling). This is Brans-Dicke theory (but with $\gamma = 1/2$).

Universal couplings generate deviations from general relativity

$$S = \int d^4x \sqrt{-g} \left\{ \frac{1}{2} R[g] - \frac{1}{2} (\partial\phi)^2 - V(\phi) + e^{4\beta\phi} \mathcal{L}_{\text{NG}}[\Psi_i; e^{2\beta\phi} g_{\mu\nu}] \right\}$$

Weyl transformation of Brans-Dicke theory with a potential

$$S = \int d^4x \sqrt{-h} \left\{ \psi R - \omega \psi^{-1} (\partial\psi)^2 + 2\psi\lambda(\psi) + \mathcal{L}_{\text{NG}}[\Psi_i; h_{\mu\nu}] \right\}$$

$$\omega = \frac{1 - 6\beta^2}{4\beta^2} \approx \frac{1}{1 - \gamma}$$

$$\psi = e^{2\beta\phi}$$

$$G_{\text{eff}} = e^{-2\beta\phi} (1 + 2\beta^2)$$

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Warped models

- A *warped* extra dimension

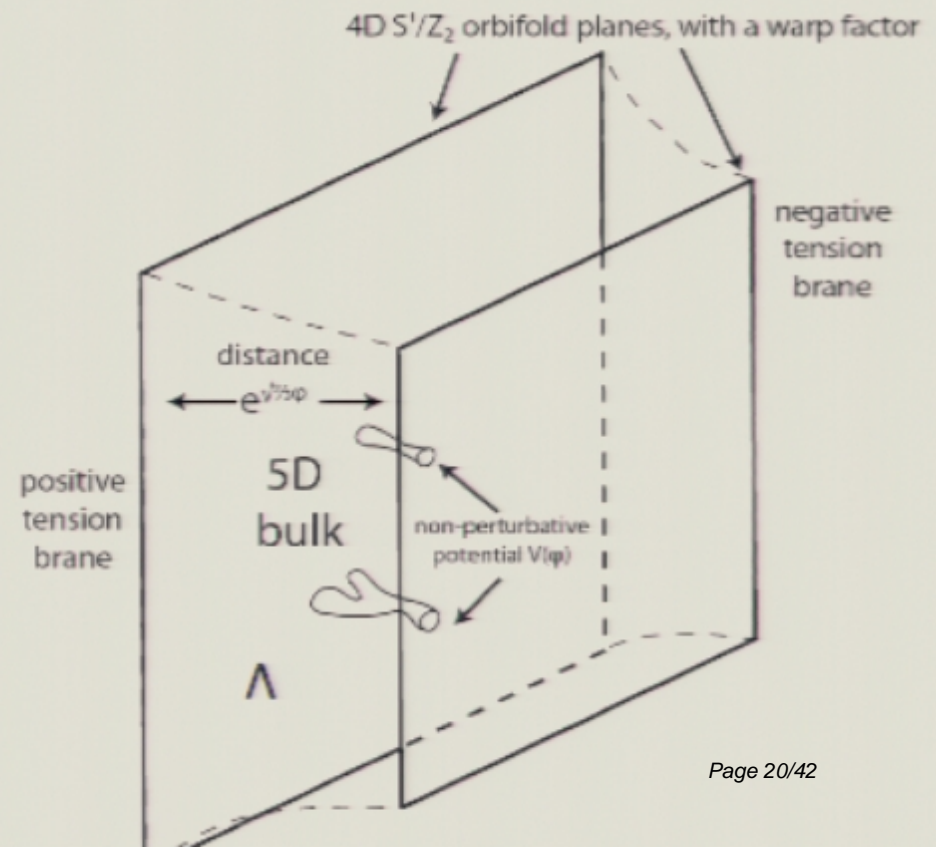
$$ds^2 = \Omega(y)^2 a(t)^2 \eta_{\mu\nu} dx^\mu dx^\nu + (dy)^2$$

where $\Omega(y)$ is the warp factor can improve (or exacerbate) the situation as in the Randall-Sundrum models, heterotic M-theory, etc...

The warp factor

e.g. in RS1 $\gamma = \begin{cases} 1 - \frac{8}{3} \Omega^2 k & \text{+ve tension} \\ -1 + \frac{4}{3} \Omega^2 k & \text{-ve tension} \end{cases}$

(Verlinde 2000, Giddings, Kachru & Polchinski 2002)



4D low-energy effective action of heterotic M-theory (in Brans-Dicke frame)

$$\begin{aligned}
 S = \frac{\pi\rho V}{\kappa^2} \int_{\mathcal{M}^4} \sqrt{-h} d^4x & \left[e^c R - 0 \times e^c (\partial c)^2 - 3 \left(1 + \frac{1}{3} \xi \alpha_0 e^c \right) \partial_\mu C \partial^\mu \bar{C} \right. \\
 & \left. - \frac{3}{8} e^{-c} C C \bar{C} \bar{C} - \frac{3k^2}{4} \left(1 - \frac{1}{3} \xi \alpha_0 e^c \right) C C \bar{C} \bar{C} \right. \\
 & \left. - \frac{V}{8\pi\kappa^2} \left(\frac{\kappa}{4\pi} \right)^{2/3} \int_{\mathcal{M}^4} \sqrt{-g} d^4x \left((1 + \xi \alpha_0 e^c) \text{tr}(F^{(1)})^2 + (1 - \xi \alpha_0 e^c) \text{tr}(F^{(2)})^2 \right) \right]
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(Lukas, Ovrut and Waldram, 1997)

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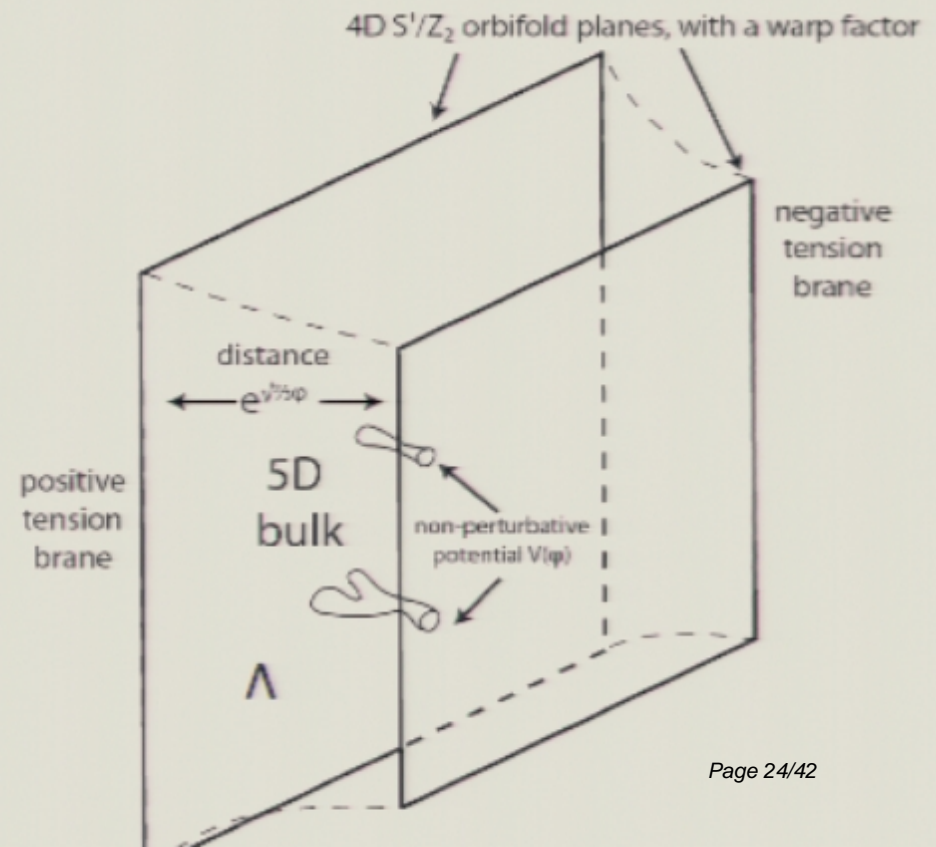
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- Violations of the weak equivalence principle and variation of α are naturally suppressed at higher order (at observational thresholds, depending on the Calabi-Yau manifold)

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- Brans-Dicke parameter is zero, as in the S^1/Z_2 case (e.g. $\gamma = 1/2$)

Other models

- Runaway dilaton (Gasperini, Piazza & Veneziano, 2002)
 - Predicts a specific relation between η and ω , and $d \log \alpha / d \log a$ and η .
- Chameleon cosmology (Khoury & Weltman 2003, Brax *et al.* 2002)
 - EP violations heavily suppressed in dense regions

The equivalence principle effects can be related in the context of dark energy

Local and cosmological tests of the EP

- Local tests
 - universality of free fall
 - solar system tests of gravity
 - gravitational redshift experiments

These tests *directly* measure couplings

- Cosmological tests
 - variation of fundamental constants

Cosmological tests measure the *combined*
couplings and rate of variation of the field

Universal couplings generate deviations from general relativity

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Local and global effects can be related in a dark energy model

$$w + 1 = \frac{\dot{\phi}^2}{\frac{1}{2}\dot{\phi}^2 + V(\phi)} = \dot{\phi}^2 / 3H^2 \Omega_Q$$

$$= \frac{1}{3\Omega_Q} \left(\frac{d\phi}{d \log a} \right)^2$$

$$= \frac{1}{3\Omega_Q} \frac{1}{1-\gamma} \left(\frac{d \log G}{d \log a} \right)^2$$

since

$$\frac{d \log G}{d \log a} = \sqrt{1-\gamma} \frac{d\phi}{d \log a}$$

$$w + 1 = \frac{1}{3\Omega_Q} \frac{1}{1-\gamma} \left(\frac{d \log G}{d \log a} \right)^2$$

This is a generic relation between three observable parameters. (For a cosmological constant, they are all zero.)

Limits $w + 1$ and γ constrain the evolution of G

$$|H_0^{-1} \dot{G}/G| < 4 \times 10^{-3}$$

Could the equivalence principle be strongly violated for dark matter?

- If dark matter couples to $e^{2\beta\varphi}g_{\mu\nu}$ then there is a φ mediated fifth-force, such that

$$G_{\text{eff}} = G(1 + 2\beta^2).$$

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Coupling to dark matter affects homogeneous evolution

$$\rho_{DM} \propto e^{-\beta\phi} a^{-3}$$

$$\frac{d\rho_x}{d\log a} = -3(1+w_x)$$

$$\beta^2 (\Omega_{DE} (1+w_{DE}) + \Omega_{DM} w_{DM}) = 3w_{DM}^2$$

- Amendola and Quercellini (2003) investigated the effect on CMB and found

$\beta < 0.09$ (1σ). (But this depends strongly on the fact that they used the power-law potential for quintessence.)

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Likewise,

$$w + 1 = \frac{1}{3\Omega_Q} \frac{C}{\eta} \left(\frac{d \log \alpha}{d \log a} \right)^2 \sim \frac{10^{-3}}{\eta} \left(\frac{\Delta \alpha}{\alpha} \right)^2$$

holds generally for dark energy models. It implies

$$|H_0^{-1} \dot{\alpha} / \alpha| < 5 \times 10^{-5},$$

which is consistent with but does not improve on other constraints.

Model-dependent couplings to other constants (electron-to-proton mass ratio, QCD scale) are constrained to roughly the same level.

Variation of α

$$\mathcal{L}_{EM} = \frac{1}{16\pi\alpha_0} e^{\lambda\phi} F^2,$$

$$\frac{\dot{\alpha}}{\alpha} = \lambda \dot{\phi} \quad \frac{\Delta\alpha}{\alpha} = \lambda \Delta\phi$$

generates a composition-dependent fifth force

$$\eta \approx 10^{-1} \times 10^{-2} \times \lambda^2$$

difference between two nuclei \nearrow
nuclear fraction \uparrow
relative strength \uparrow

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Conclusions

- It is important to look for dynamical dark energy (equivalently a cosmological scalar field) using other approaches than the equation of state
- Dynamical dark energy is likely to lead to violations of the equivalence principle
- General relations between different kinds of EP violation are satisfied by these models
- Some of the tools of compactification – orbifolds and warped extra dimensions – can be used to suppress deviations from the equivalence principle

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