

Title: Reheating and Thermalization after inflation

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Abstract:

Reheating and thermalization after inflation

Marco Peloso, Minnesota

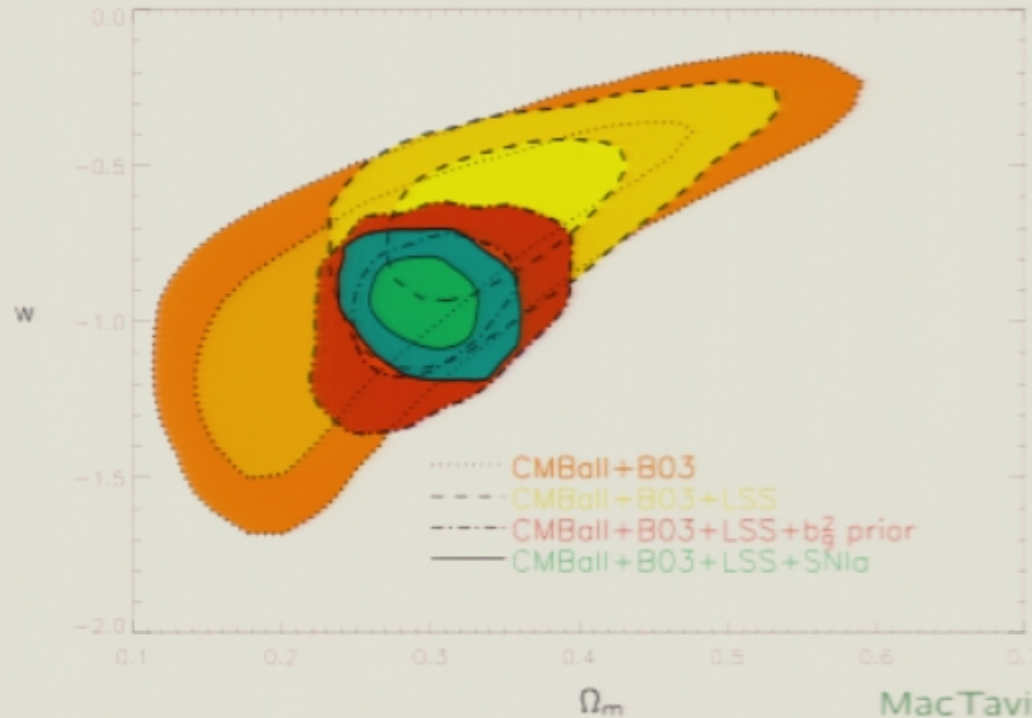
- Overview
- Intermediate equation of state
- Trilinear interactions

Podolsky, Felder, Kofman, M.P., '05

Dufaux, Felder, Kofman, M.P., Podolsky

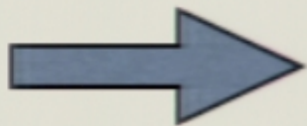
History of the Universe

Clear knowledge
from BBN on



MacTavish et al. '05

$$\Omega_Q \simeq 2/3 \quad , \quad \Omega_m \simeq 1/3 \quad , \quad T_\gamma \simeq 2.7 \text{ K}$$



$$w_Q \lesssim -0.7 \quad z \in [0, 0.25]$$

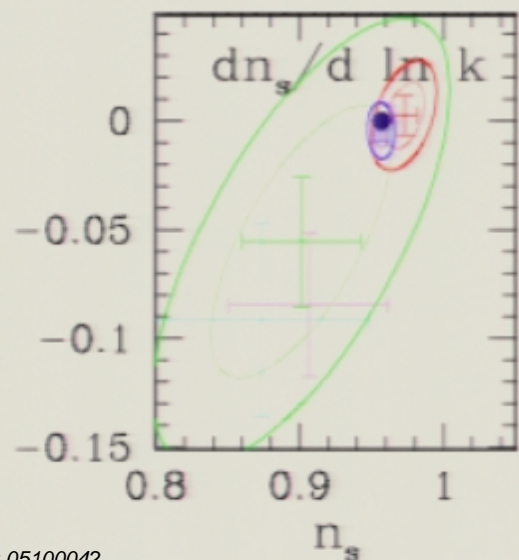
$$w_m = 0 \quad z \in [0.25, 10^4]$$

$$w_r = 1/3 \quad z \in [10^4, ?]$$

Good theoretical control & data for inflation

Slow Roll : $\epsilon = \frac{M_p^2}{16\pi} \left(\frac{V'}{V} \right)^2$, $\eta = \frac{M_p^2}{8\pi} \frac{V''}{V}$, ...

- COBE normalization $\left(\frac{V}{\epsilon} \right)^{1/4} = 6.7 \cdot 10^{16} \text{ GeV}$
- Spectral index $n_s - 1 = -6\epsilon + 2\eta$
- Tensor mode $P_T(k) = \frac{2}{M_p^2} \left(\frac{H_k}{2\pi} \right)^2$

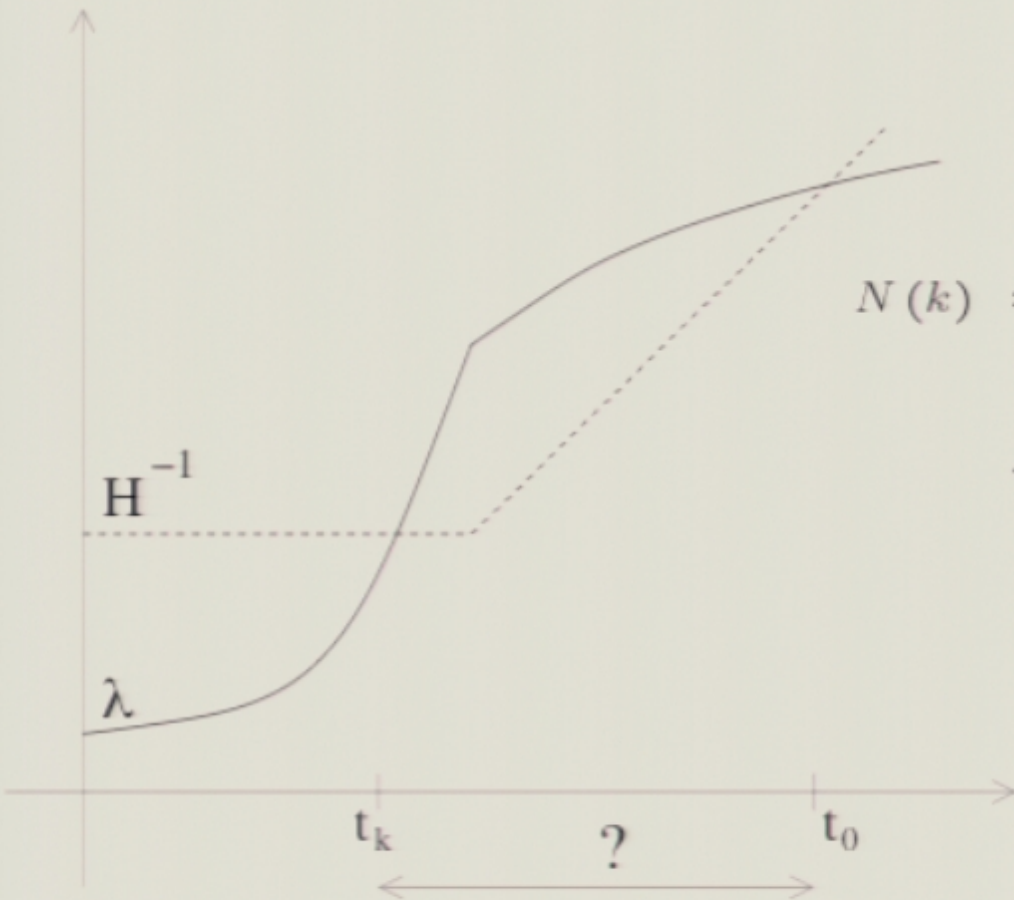


WMAP4

WMAP4 + ground based polarization telescopes

Planck

Present scale \leftrightarrow horizon exit during inflation ?



$$N(k) = 62 - \ln \frac{k}{6.96 \times 10^{-5} \text{ Mpc}^{-1}} - \ln \frac{10^{16} \text{ GeV}}{V_k^{1/4}}$$

$$+ \frac{1}{4} \ln \frac{V_k}{V_{\text{end}}} - \frac{1}{4} \ln \frac{V_{\text{end}}^{1/3}}{\rho_{\text{reh}}^{1/3}} \quad \text{Liddle, Lyth}$$

$$- \frac{1}{4} \ln \frac{a_{\text{reh}}}{a_{\text{end}}} \quad \text{assumption of MD}$$

- MD between $H_{\text{inf}} = 10^{13} \text{ GeV}$ and $T_{\text{rh}} = 10^9 \text{ GeV} \Rightarrow -\frac{1}{4} \ln 10^8 \simeq -4.6$

- Immediate inflaton decay at preheating $\Rightarrow -\frac{1}{4} \ln 20 \simeq -0.75$

Modulated fluctuations

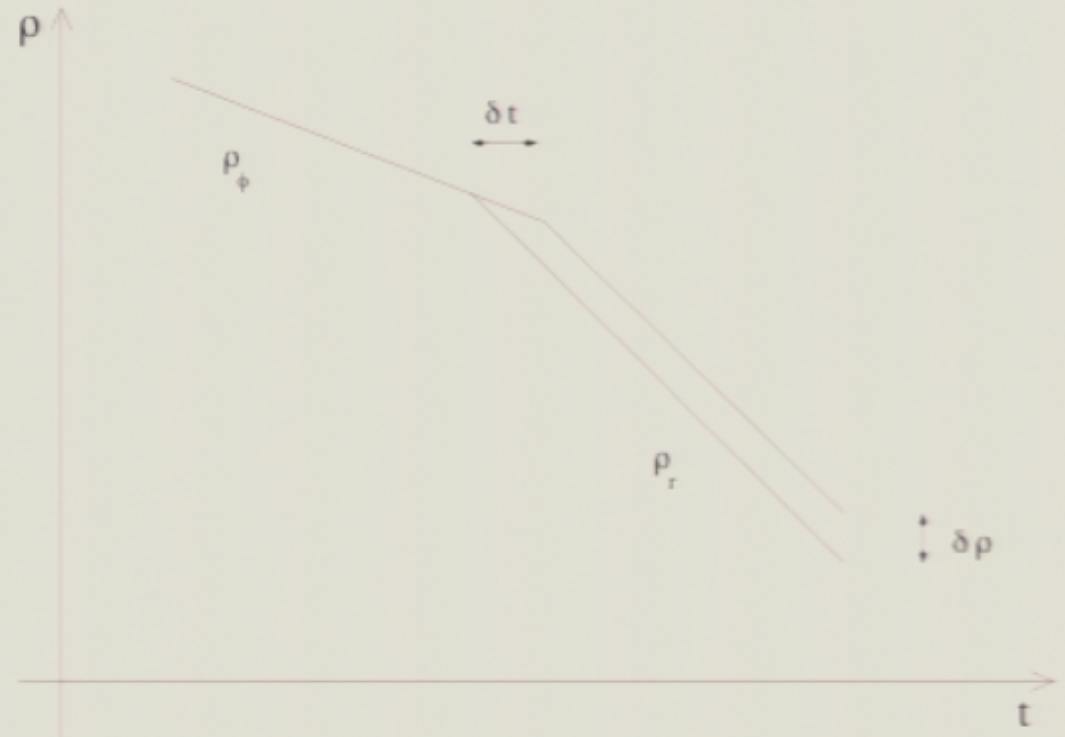
Kofman '03

Dvali, Gruzinov, Zaldarriaga '03

- $V = g^2 \phi^2 \chi^2$. Fluctuations of the coupling give rise to density perturbations

$$g^2 = g^2(z), \quad \delta g^2 = \frac{dg^2}{dz} \delta z$$

$\delta \rho$ due to $\omega_\phi \neq \omega_r$



- To make predictions, need to know details of the transition inflaton \rightarrow radiation

Nonperturbative inflaton decay

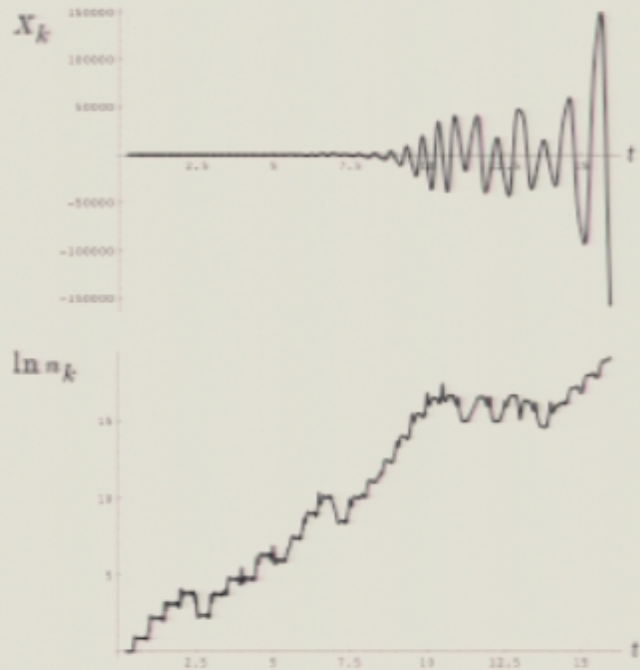
- Traschen, Brandenberger '90; Shtanov, Traschen, Brandenberger '94
- **Preheating:** Kofman, Linde, Starobinsky '94; '97

Resonant particle production due to coherent inflaton oscillations

$$V = \frac{1}{2} m^2 \phi^2 + \frac{g^2}{2} \phi^2 \chi^2 \quad \Rightarrow \quad \omega_\chi^2 = (k/a)^2 + g^2 \phi(t)^2$$

- Excitation when $\dot{\omega}_\chi > \omega_\chi^2$
- Periodic “driving force” \rightarrow resonant instability bands

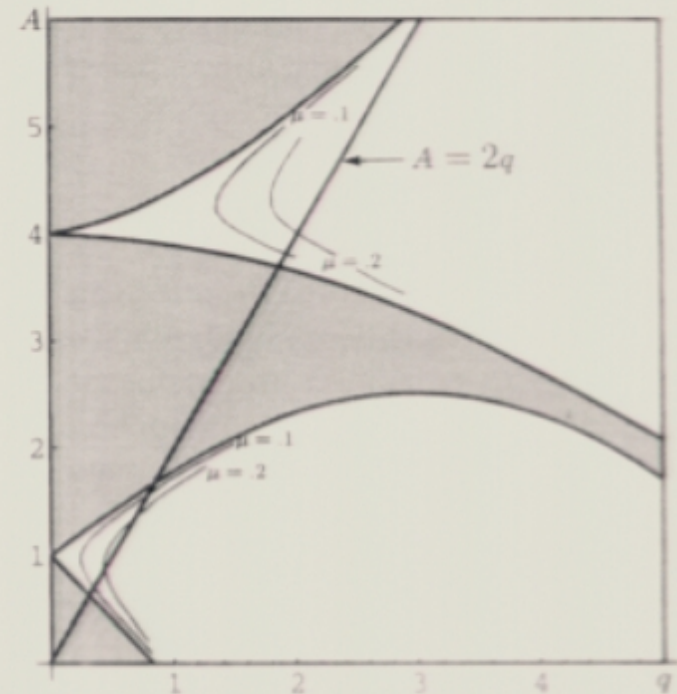
$$\omega^2 \sim m^2 + g^2 \phi^2 \quad \Rightarrow \quad g^2 \gtrsim \frac{m^2}{\phi^2} \sim 10^{-10}$$



- Stimulated particle production
- Redshift of physical momenta:
modes cross stability/instability bands

Stability / Instability chart

$$q \equiv \frac{g^2 \phi^2}{4 m^2} \quad , \quad A \equiv \frac{k^2}{m^2 a^2} + 2q$$

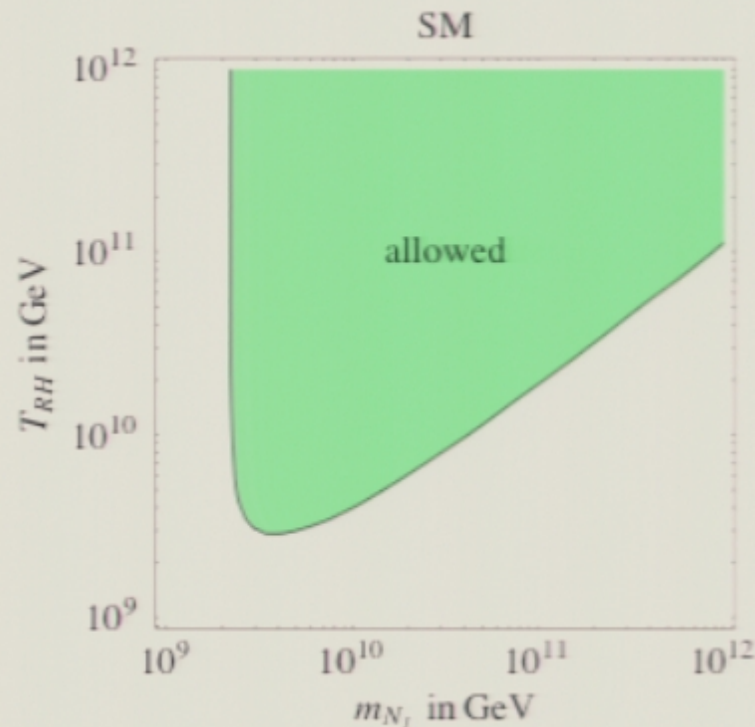


Production of super-heavy particles

- Many models of baryogenesis require heavy masses; thermal production can be in conflict with bounds on T_{rh} from gravitino problem

E.g. Thermal leptogenesis
from r.h. neutrinos

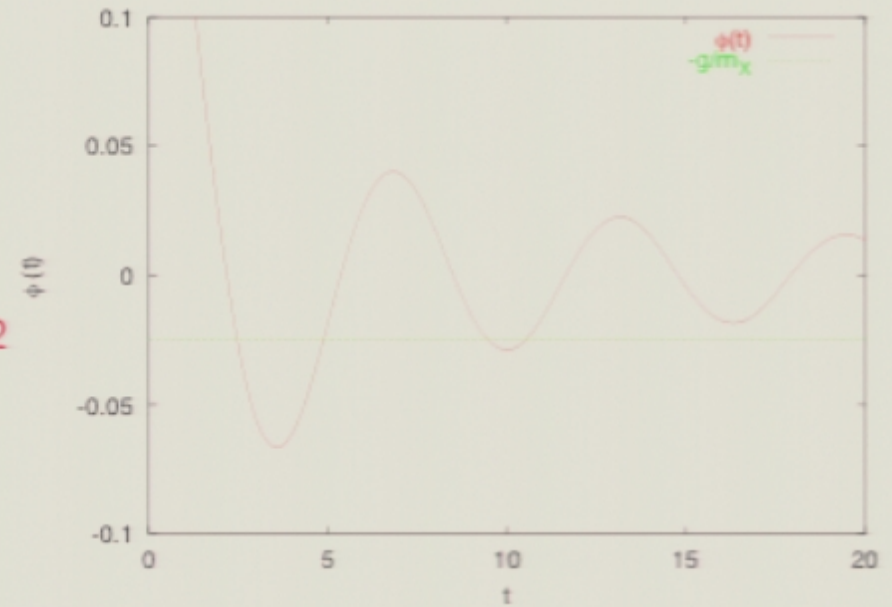
Giudice et al. '04



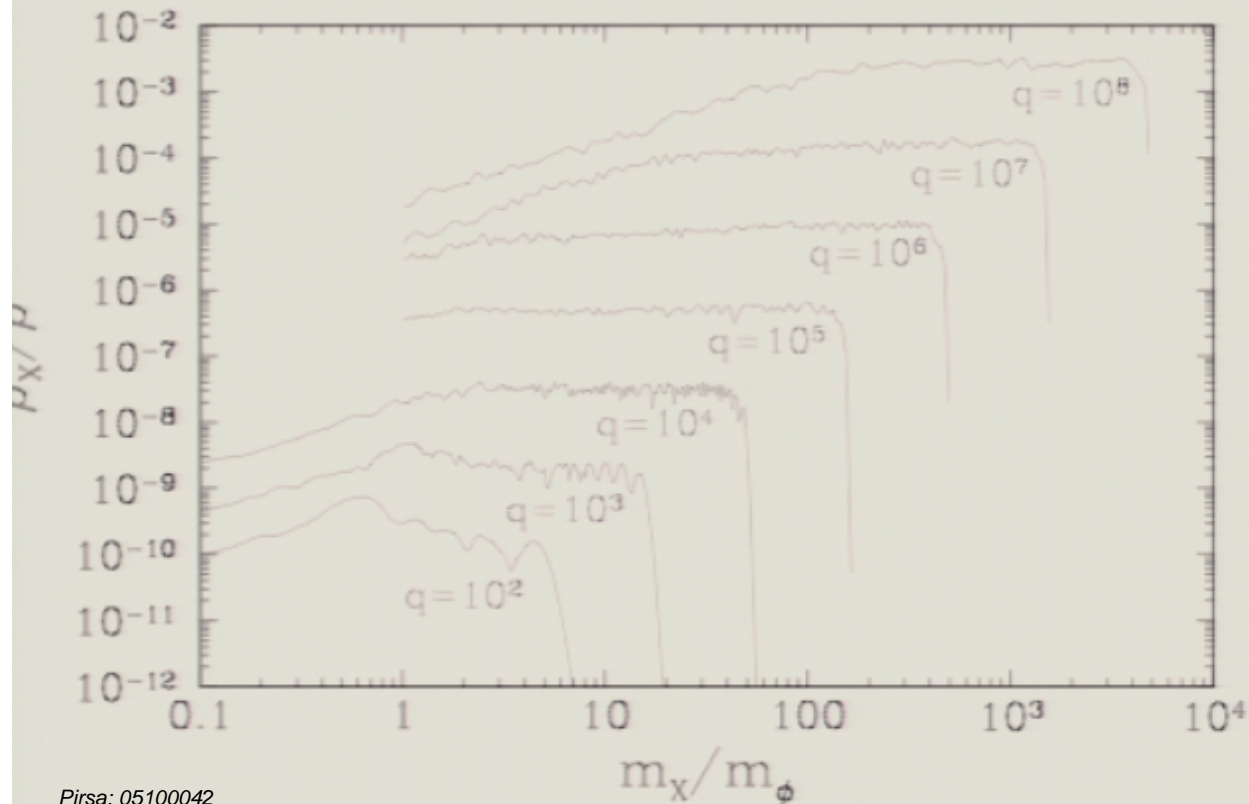
(main reason, $\delta_{CP} \propto m_{N_1}$)

$$\mathcal{L}_{\phi X} = (m_X + g\phi) \bar{X} X$$

$$\text{Preheating} \leftrightarrow \dot{\omega}_k \gtrsim \omega_k^2 \leftrightarrow \dot{m} \gtrsim m^2$$



Giudice, M.P., Riotto, Tkachev, '99



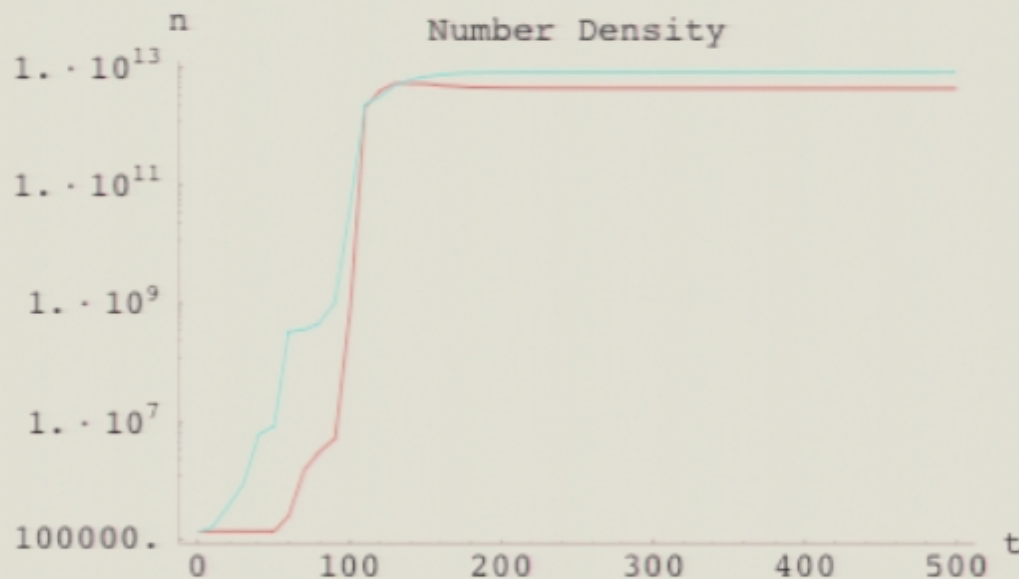
$$(m_X)_{\text{max}} \sim q^2 = g\phi_0/2$$

$$\frac{\rho_X}{\rho_\phi} \propto q m_X^{1/2} \left[\log \frac{q^{1/2}}{m_X} \right]^{3/2}$$

M.P., Sorbo '00

Rescattering

- Parametric resonance ends at $t \sim 100/m$, when the decay products scatter off the zero mode of ϕ , destroying its coherence
- System cannot be studied analytically; perturbative approaches fail, due to the extremely high occupation numbers



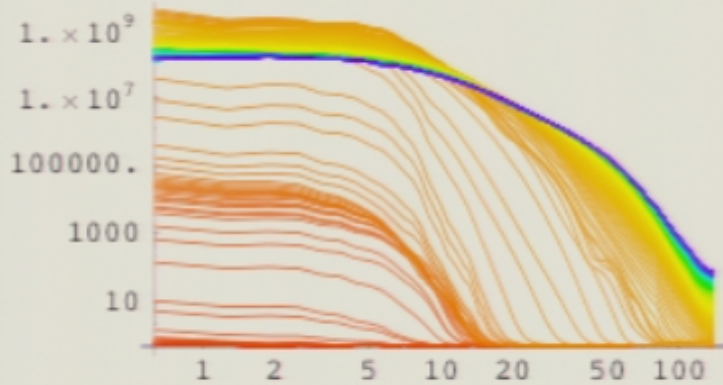
Classical lattice
simulations

Khlebnikov, Tkachev '96

Prokopec, Ross '96

Felder, Tkachev '00

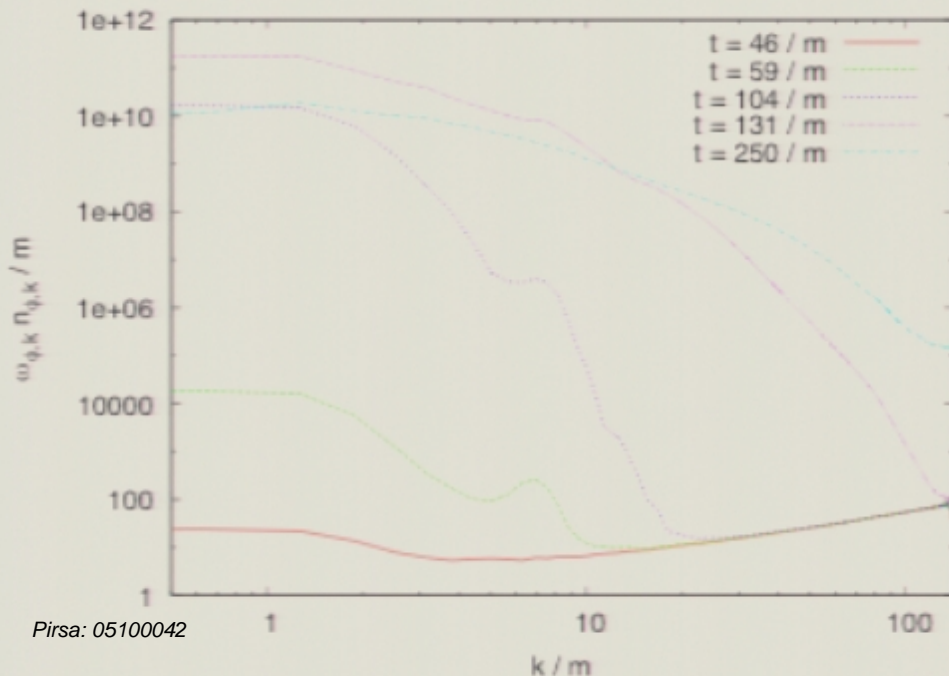
Number: ϕ



Distributions formed at rescattering much more populated in the IR than thermal distributions

$$n_k \sim 1/g^2 \gg 1$$

- Thermalization proceeds through particle fusion (slow motion towards UV)
- Excitations of fields not directly coupled to the inflaton, $\phi \leftrightarrow \chi \leftrightarrow \psi$



Saturated distribution, still very far from thermal

cf. Rayleigh–Jeans spectrum

$$n_k \approx \frac{T_{\text{eff}}}{\omega_k - \mu}$$

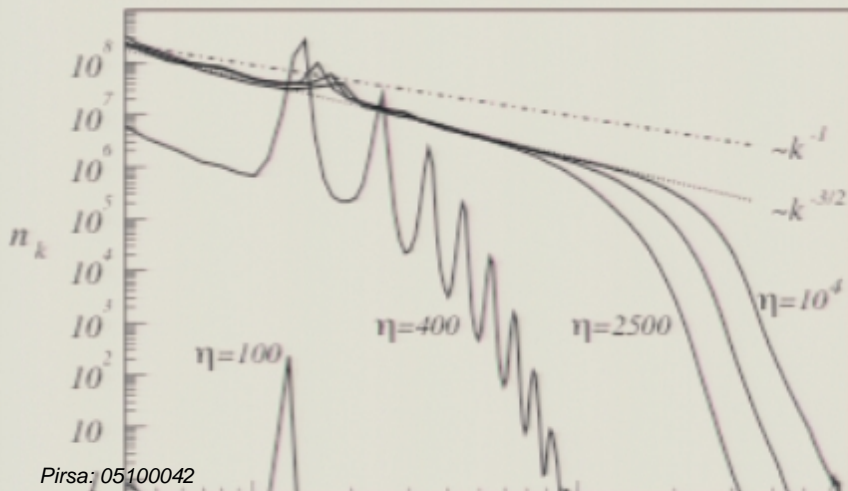
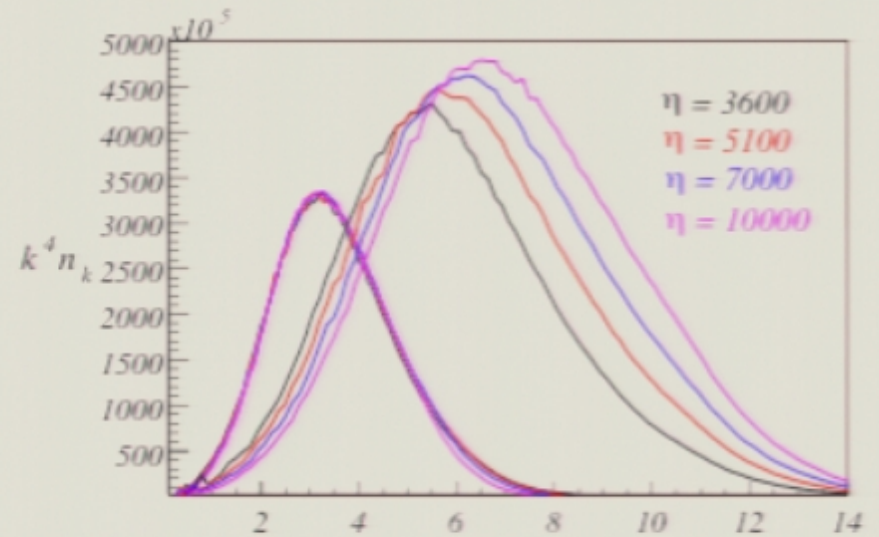
Thermalization occurs on a much longer timescale; lattice effective only for conformal cases, $\lambda \phi^4 + g^2 \phi^2 \chi^2$, or too much UV required

(Kolmogorov) **Turbulence**; distributions evolve self-similarly

$$n(k, \tau) = \tau^{-q} n_0(k \tau^{-p}),$$

$$q = 3.5p, \quad p = \frac{1}{2m-1}, \quad m = 3 \quad (\delta\phi\phi_0 \leftrightarrow \delta\phi\delta\phi)$$

Micha, Tkachev '04



$$n_k = k^{-3+m/(m-1)}$$

Kinetic equation

$$\dot{n}_k = \frac{\dot{\omega}_k}{\omega_k} \text{Re} \sigma_k + \text{Im} I_3(k) + \text{Im} I_4(k)$$

$$i\dot{\sigma}_k = 2\omega_k \sigma_k + \frac{i}{2} \frac{\dot{\omega}_k}{\omega_k} n_k + I_3^*(k) + I_4^*(k)$$

$$\langle a_{\mathbf{k}}^* a_{\mathbf{q}} \rangle = n_k \delta^{(d)}(\mathbf{k} - \mathbf{q})$$

$$\langle a_{\mathbf{k}} a_{\mathbf{q}} \rangle = \sigma_k \delta^{(d)}(\mathbf{p} + \mathbf{q}) \quad \text{Anomalous correlators (phases)}$$

Expanded around $\omega^2 = k^2 + 3\lambda\phi_0^2 + 3\lambda\langle\delta\phi^2\rangle$

$(1 + n_1)(1 + n_2)n_3n_4 - n_1n_2(1 + n_3)(1 + n_4)$ in the collisional integrals; usual dilute gas approximation, $n \ll 1$, does not apply !

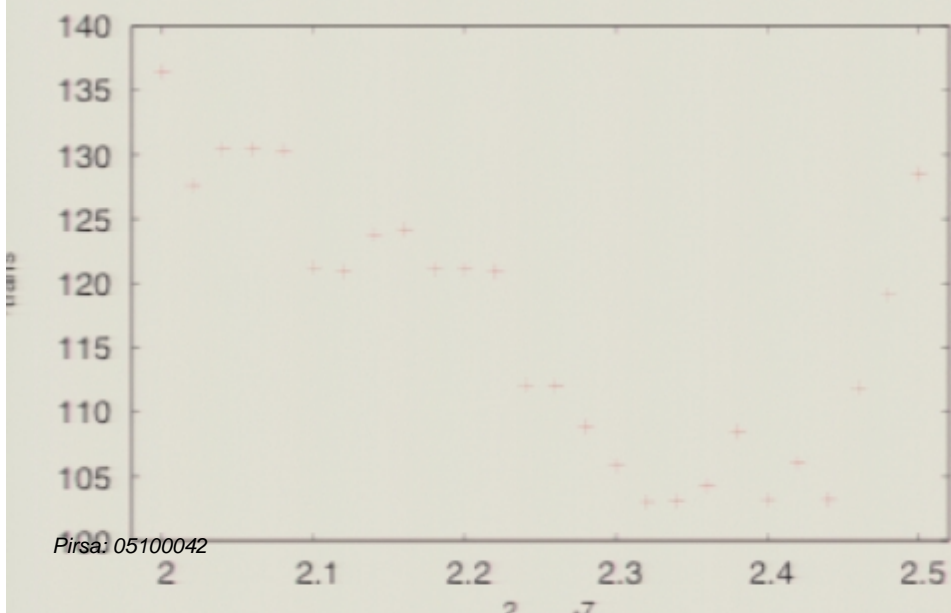
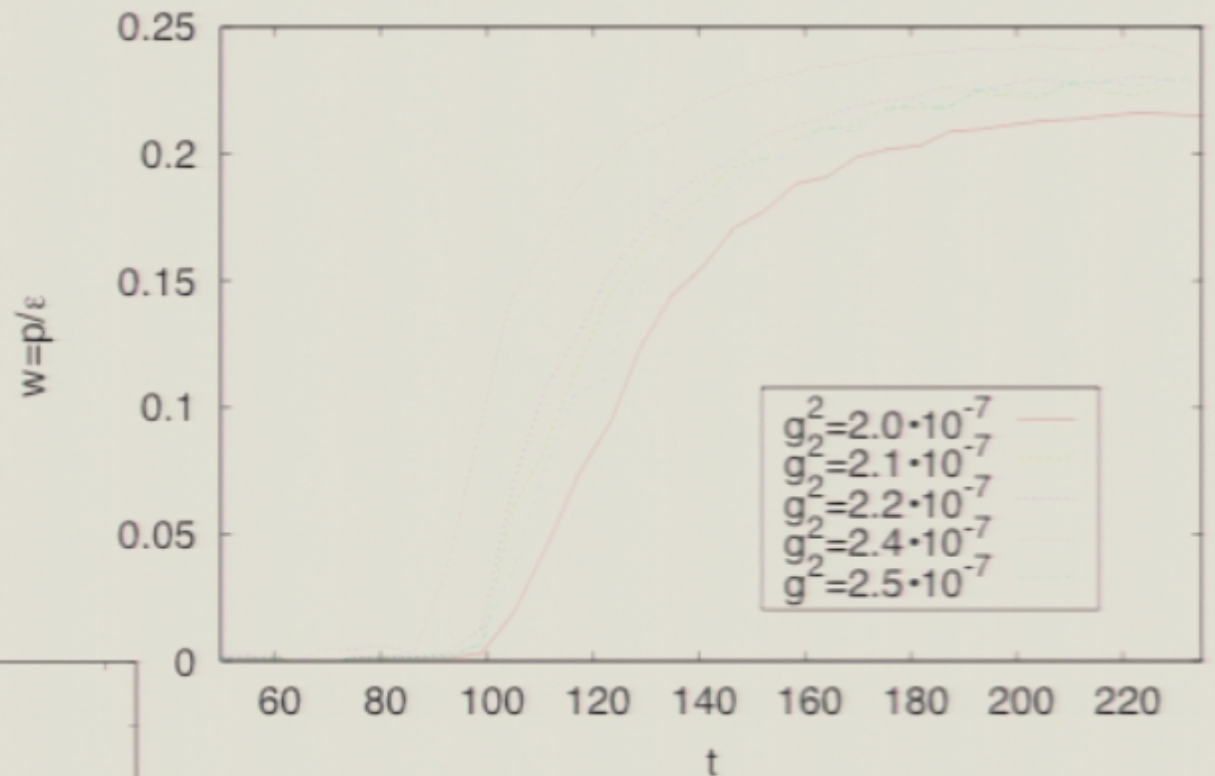
- Not clear speed up over the lattice; however, more suitable approach for (i) fermions, (ii) quantum regime

Intermediate equation of state

$$(n_k \simeq 1/g^2)$$

$$V = \frac{1}{2} m^2 \phi^2 + \frac{g^2}{2} \phi^2 \chi^2$$

At rescattering, EOS quickly "jumps" at an intermediate value between the ones of matter & radiation



Transition time ($w_{\text{trans}} = 0.15$)
non monotonic function of g^2

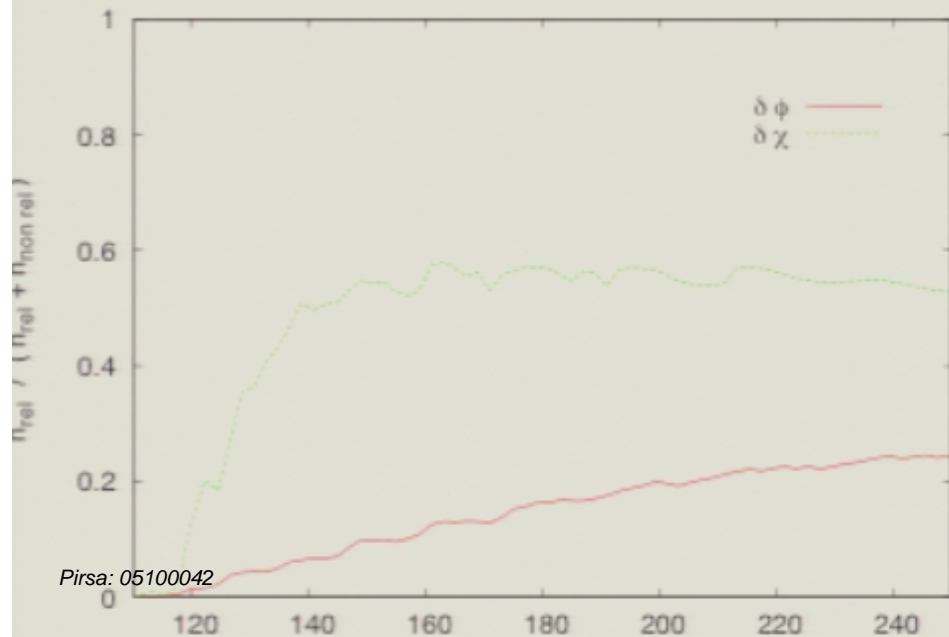
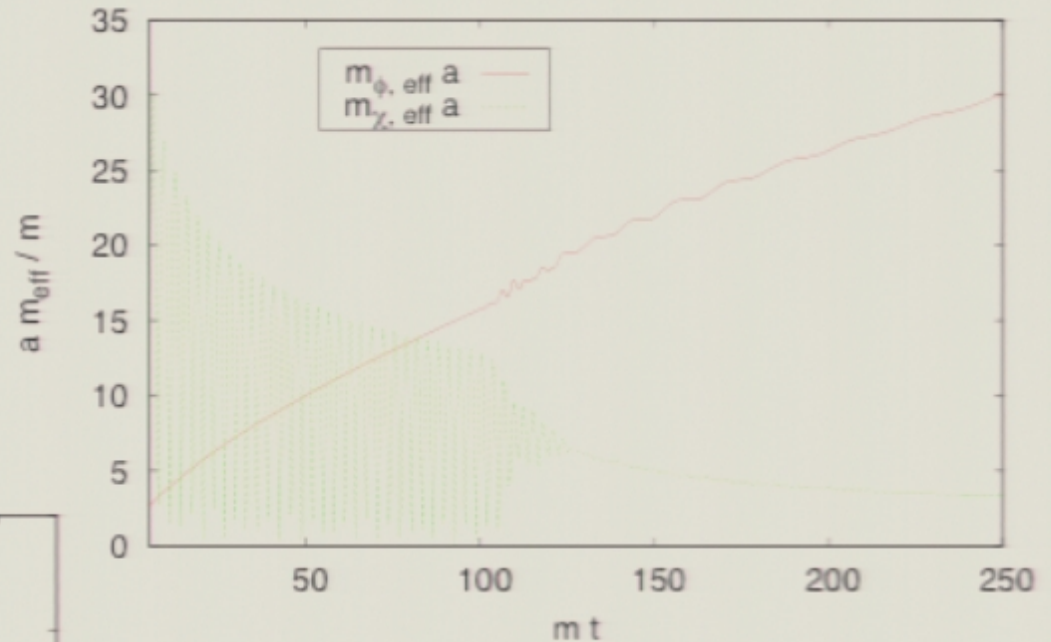
Effective masses

$$V = \frac{1}{2}m^2\phi^2 + \frac{g^2}{2}\phi^2\chi^2$$

$$m_{\phi,\text{eff}} = m^2 + g^2\langle\chi^2\rangle$$

$$m_{\chi,\text{eff}} = g^2\langle\phi^2\rangle$$

$$g^2 = 10^{-7}$$



Fraction of relativistic
quanta

$$k/a > m_{\text{eff}}$$

$$\Gamma(\phi\phi \rightarrow \chi\chi) \simeq \frac{g^4 \Phi^2}{8\pi m} \propto a^{-3} \quad \text{while } H \propto a^{-3/2}$$

Therefore, add trilinear term $\phi\chi^2$. Expected to speed up particle fusion, and thermalization

$$V = \frac{m^2}{2}\phi^2 + \frac{g^2}{2}\phi^2\chi^2 + \frac{\sigma}{2}\phi\chi^2 + \frac{\lambda}{4}\chi^4$$

New type of preheating. $m_{\text{eff},\chi}^2 < 0$ at negative ϕ .

Quartic interaction contrast this effect, but:

- Preheating effects mainly at $\phi \simeq 0$, where the trilinear term dominates
- Expansion reduces amplitude of ϕ

Tachyonic resonance

$$\omega_k^2 = k^2 + \sigma \phi$$

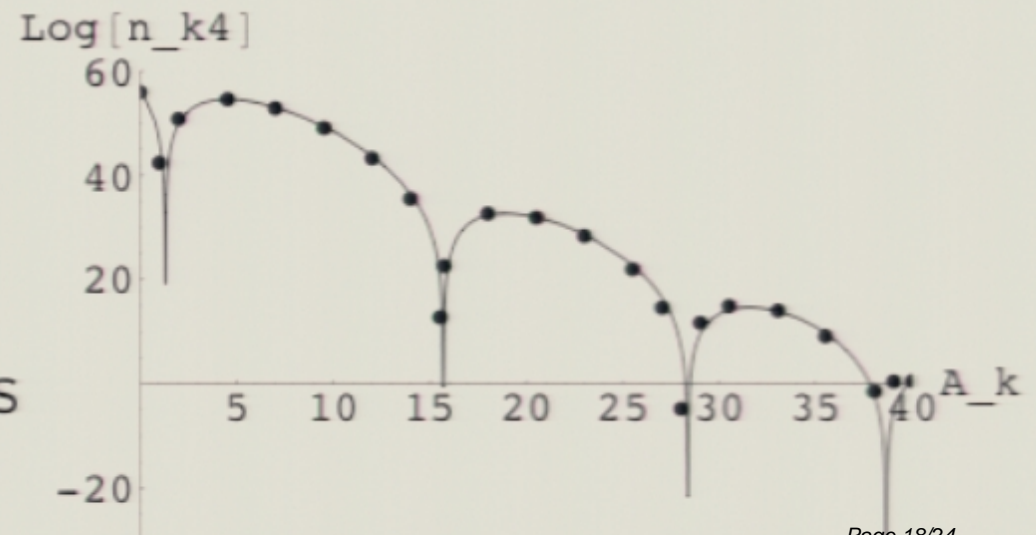
WKB approx.

$$\chi_k^j(t) = \frac{\alpha_k^j}{\sqrt{2\omega_k(t)}} \exp\left(-i \int_{t_0}^t \omega_k(t') dt'\right) + \frac{\beta_k^j}{\sqrt{2\omega_k(t)}} \exp\left(i \int_{t_0}^t \omega_k(t') dt'\right), \quad \omega_k^2 > 0$$

$$\chi_k(t) \simeq \frac{a_k^j}{\sqrt{2\Omega_k(t)}} \exp\left(-\int_{t_{k,j}^-}^t \Omega_k(t') dt'\right) + \frac{b_k^j}{\sqrt{2\Omega_k(t)}} \exp\left(\int_{t_{k,j}^-}^t \Omega_k(t') dt'\right), \quad \Omega_k^2 = -\omega_k^2 > 0$$

Parametric resonance: instability bands where $\phi(t)$ “resonate” with ω

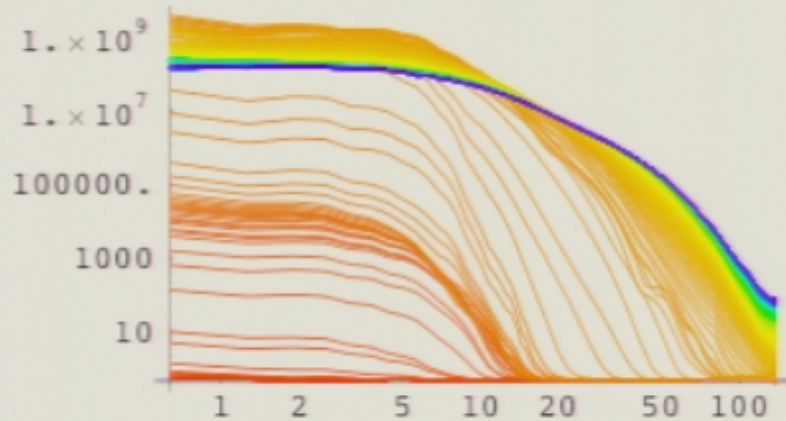
Tachyonic resonance:
stability bands where
 resonance counterbalances
 the tachyonic instability



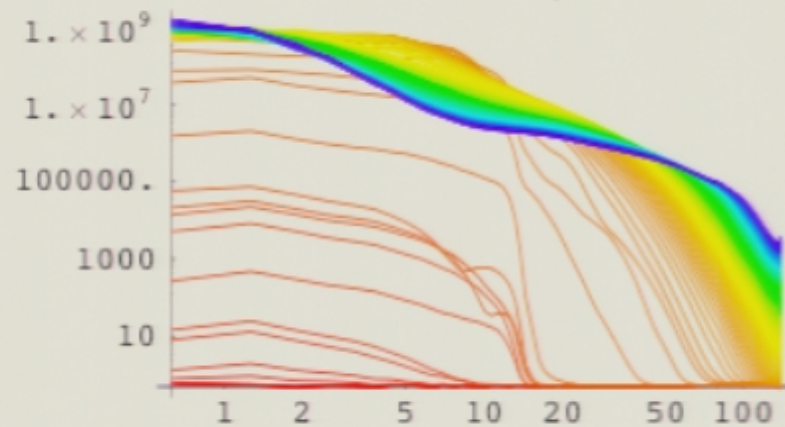
$$\frac{g^2}{2} \phi^2 \chi^2$$

$$\frac{g^2}{2} \phi^2 \chi^2 + \sigma \phi \chi^2$$

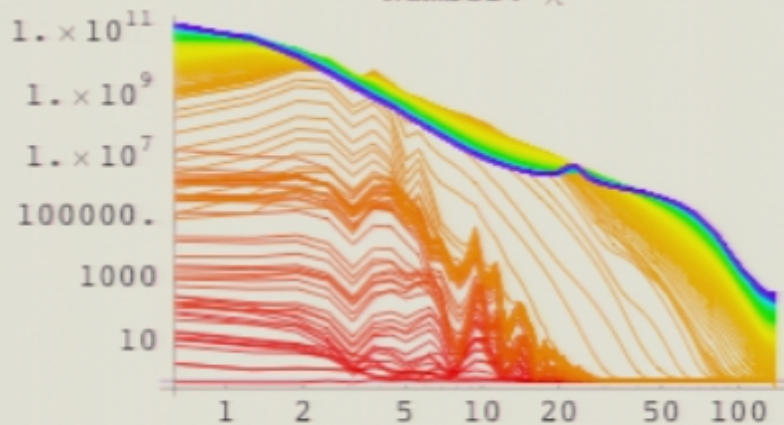
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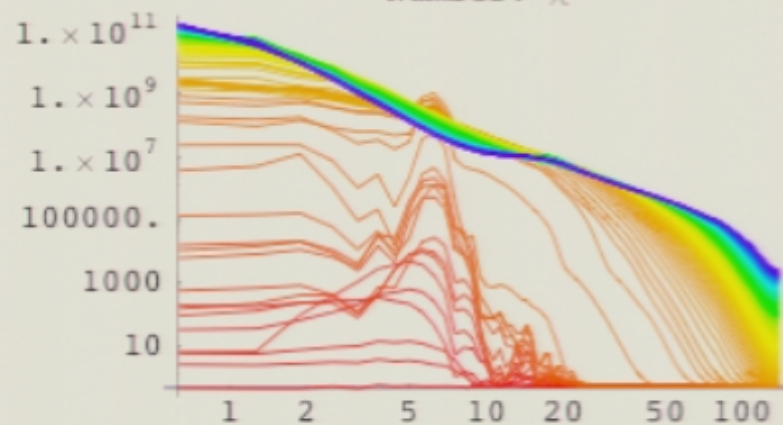
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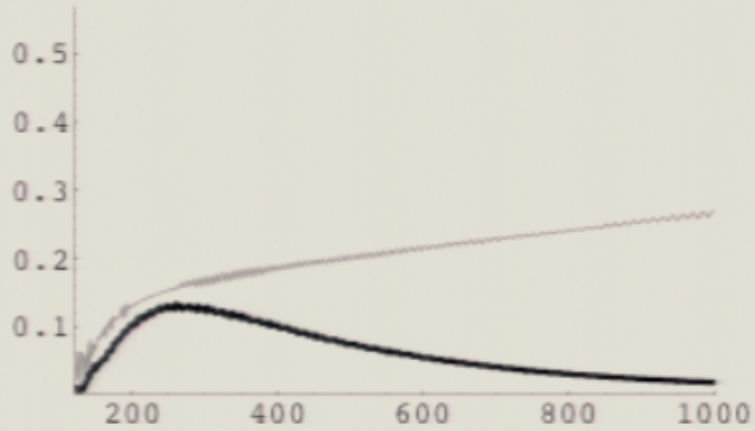
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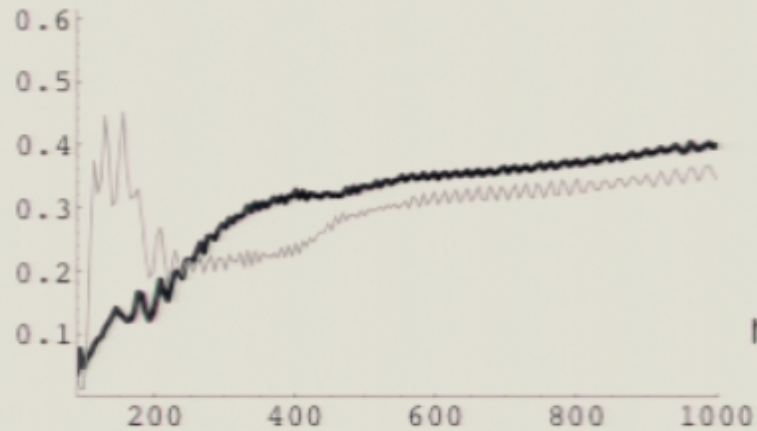
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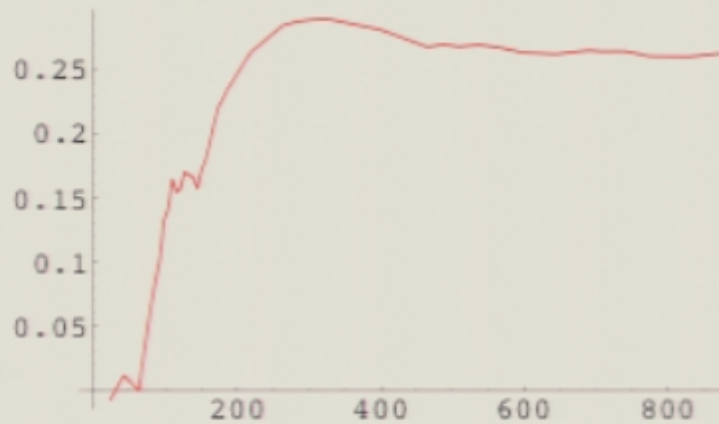
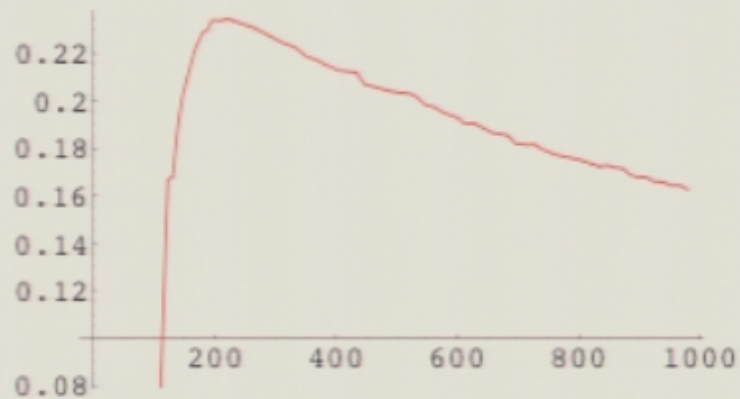
$$\frac{g^2}{2} \phi^2 \chi^2$$



$$\frac{g^2}{2} \phi^2 \chi^2 + \sigma \phi \chi^2$$



Fraction of
relativistic modes

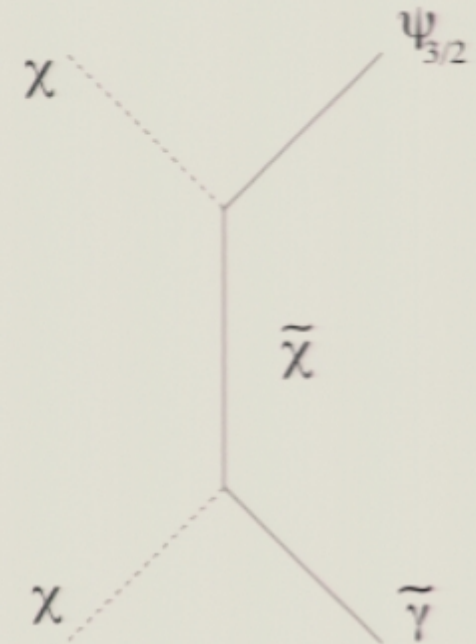


Equation
of state

Gravitino thermal production

$$\frac{dn_{3/2}}{dt} + 3Hn_{3/2} = \langle \sigma |v| \rangle n_T^2$$

- $3Hn_{3/2}$ negligible
- $\sigma \simeq \frac{10^{-2}}{M_p^2}$, $n_T^2 \simeq T^6$



$$\Rightarrow n_{3/2} \simeq \frac{10^{-2} T_{\text{rh}}^6}{M_p^2} \times H_{\text{rh}}^{-1} \simeq 10^{-2} \frac{T_{\text{rh}}^4}{M_p} , \quad Y_{3/2} = \frac{n_{3/2}}{s} \simeq 10^{-2} \frac{T_{\text{rh}}}{M_p}$$

BBN bound $Y_{3/2} \lesssim 10^{-13} \left(100 \text{ GeV} / m_{3/2} \right) \Rightarrow T_{\text{rh}} \lesssim 10^9 \text{ GeV}$

- Small $T_{\text{rh}} \equiv$ late inflaton decay; energy “frozen” in the coherent oscillations until diluted by expansion
- Rescattering \rightarrow distributions far from thermal; but $\rho \gg (10^9 \text{ GeV})^4$. Compute gravitino production when they form, $t_* \simeq 120/m$.

$$V = \frac{1}{2}m^2\phi^2 + \frac{g^2}{2}\phi^2\chi^2 + h\chi\bar{\psi}\psi$$

Yukawa interaction
as 2nd vertex

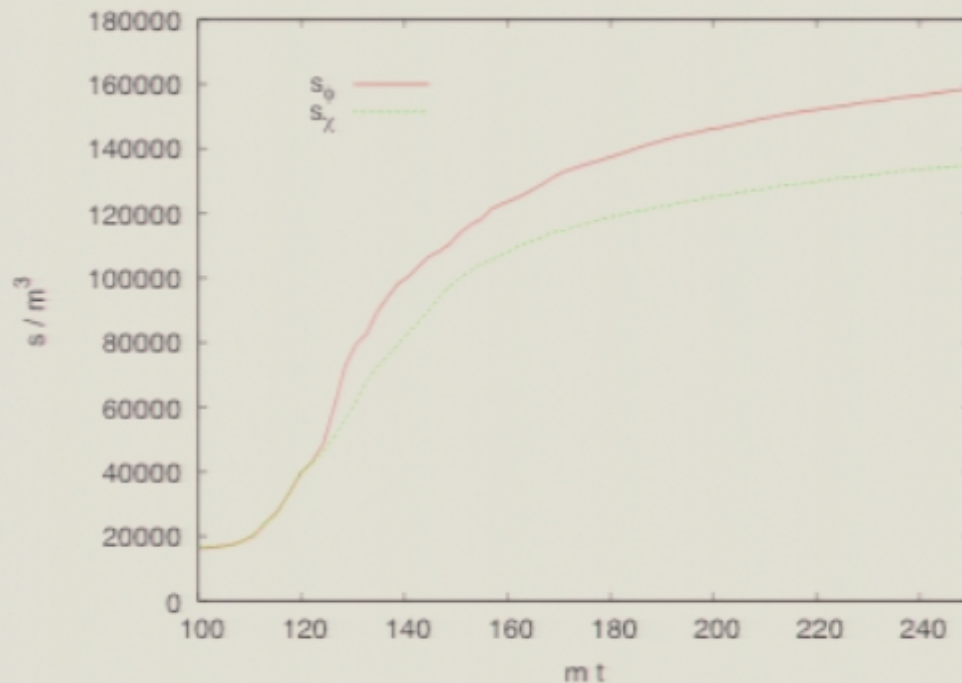
effective mass $m_\psi = h\sqrt{\chi^2(t_*)} \simeq 5 \cdot 10^2 h m$

Typical momenta χ quanta $k/a(t_*) \simeq 0.5 m$

$h \lesssim 10^{-3}$ effective production

$$n_{3/2}(t_*) \sim \frac{h^2}{M_p^2} N_\chi(t_*)^2 H(t_*)^{-1} \sim 10^7 h^2 m^3$$

Entropy $s = \int d^3k [(n_k + 1) \ln(n_k + 1) - n_k \ln(n_k)]$



$$s(t_*) \simeq 5 \cdot 10^4 m^3$$

increases during thermalization

$$s_{\text{th}} \equiv \rho^{3/4} \simeq 10^7 m^3$$

$$Y_{3/2} \gtrsim \frac{n_{3/2}}{\rho^{3/4}}|_{t=t_*} \simeq h^2 \quad \Rightarrow \quad h \lesssim 10^{-7}$$

Conclusions

- Reheating belongs to the standard paradigm of cosmology. Yet, it is the most uncertain stage in the history of the universe, $\text{MeV} \lesssim T_{\text{rh}} \lesssim 10^9 \text{ GeV}$
- Unsettled issues include generation of very massive particles, $M \lesssim T_{\text{reh}}$, gravitational relics, connection $N_{\text{infl}} \leftrightarrow \lambda_0$, modulated perturbations
- While basic formalism is known, major advance may require improvement of numerical techniques, or development of scaling solutions for more realistic cases