

Title: D3/D7-Brane Inflation and Semilocal Cosmic Strings

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Abstract:

# D3/D7 - Inflation

and

# Semilocal Cosmic Strings

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(Stanford)

[  
Dasgupta, Hsu, Kallosh, Linde, M.Z.: hep-th/0405247  
Chen, Dasgupta, K. Narayan, Shmakova, M.Z.:  
hep-th/0501185  
]

## Outline

- ① Introduction
- ② D3/D7-brane inflation
  - ⇒ Hybrid D-term inflation in 4D
  - ⇒ Cosmic string problem
    - ("local" cosmic strings)  
 $U(1)_{\text{local}} \rightarrow \mathbb{1}$ )
- ③ Generalized D-term inflation
  - ⇒ Double Higgs content
  - $SU(2)_{\text{global}} \times U(1)_{\text{local}} \rightarrow U(1)_{\text{global}}$
  - ⇒ "semilocal" cosmic strings
  - ⇒ O.K. for CMB
- ④ Implementation in D3/D7-system
- ⑤ Conclusion

## ① Introduction

### Inflation in string theory?

A popular approach:

$$\text{Inflaton} = \alpha \text{ modulus}$$

#### (i) Closed string modulus

E.g., "racetrack" inflation (BPPCEGRKLQ)  
(Inflaton = volume modulus) 2004

#### (ii) open string modulus

↪ e.g. brane position/orientation

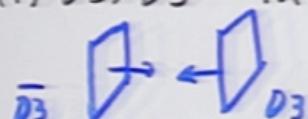
↪ "brane inflation" (Dvali, Tye 1999)

A very intuitive and minimalistic setup:

Movable D3-branes in IIB string theory

Two popular models:

(i) D3/ $\bar{D}_3$  - inflation



2001  
(Alexander, Burgess, Majumdar,  
Nolte, Quevedo,  
Rajesh, Zhang)

(ii) D3/D7 - inflation

(Dasgupta, Herdeiro,  
Hirano, Kallosh 2001)

## Inflation in string theory:

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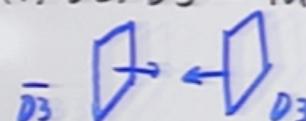
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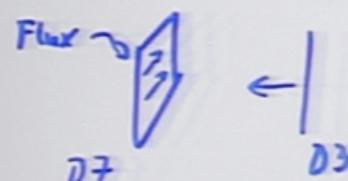
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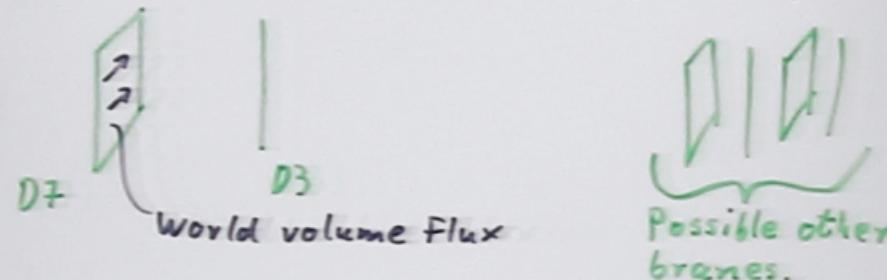


(Dasgupta, Herdeiro,  
Hirano, Kallosh, 2002)

## ② D3/D7-brane inflation

Basic configuration:

(i) An "isolated" D3/D7-system:



(ii) A compactification:

$$M^{(1,3)} \times K^{(6)}$$

$$D3: M^{(1,3)}$$

$$D7: M^{(1,3)} \times \underbrace{(4\text{-cycle of } K^{(6)})}_{\text{world volume flux}}$$

⇒ Anomaly cancellation requires care.

⇒ A well-understood example: (Dasgupta, Herdeiro, Hirano, Kallosh, 2002)

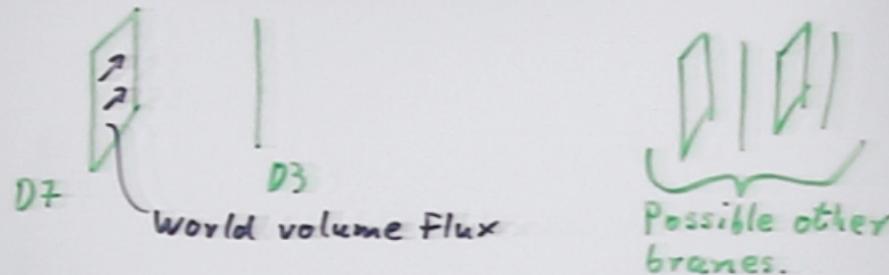
$$M^{(1,3)} \times k3 \times T^2/\mathbb{Z}_2$$

$$\Rightarrow 4D7 + 16D7 (+ mD3 + \text{flux})$$

$F = dA^{D7} - \text{fluxes}$       ⇒ F-theory  
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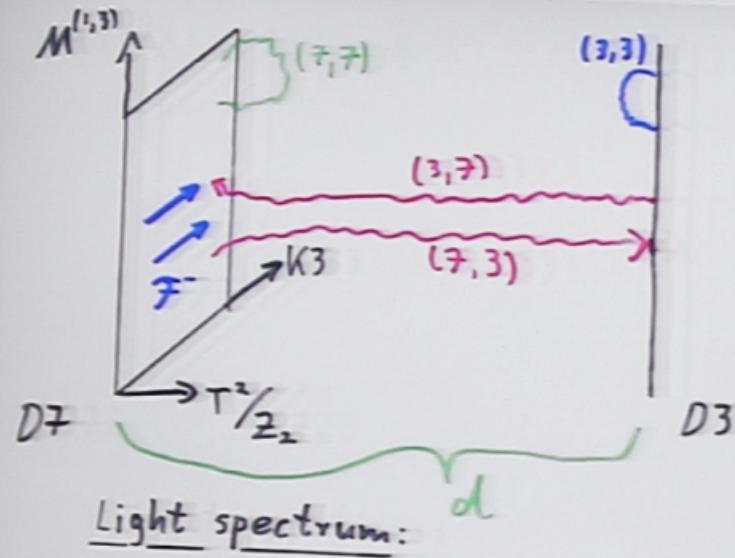
$$M^{(1,3)} \times k3 \times T^2/\mathbb{Z}_2 \quad \left( \begin{array}{l} \text{Dasgupta,} \\ \text{Herdeiro,} \\ \text{Hirano,} \\ \text{Kallosh, 2002} \end{array} \right)$$

⇒ 4D7 + 16D7 (+ mD3 + flux)

$\boxed{\text{D3}}$    .   .   } isolate  
 $\boxed{\text{D7 : } \uparrow\uparrow\uparrow}$    .   .   } ⇒ F-theory  
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$\boxed{\text{D7 : }} \quad \boxed{\text{D7 : }}$

$\tilde{F} := F - \star^k F$   
 $\langle F \rangle \neq 0 \Rightarrow \text{SUSY}$



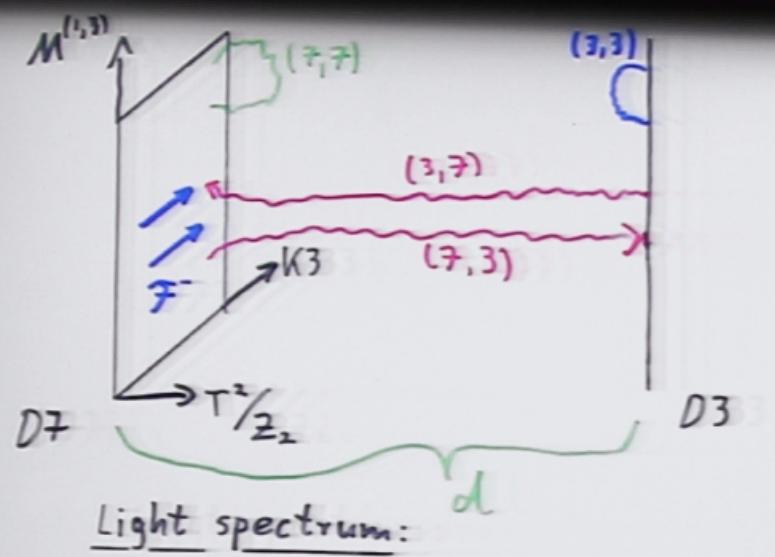
$K3$  large  
 $\Rightarrow$  decouples  $(7,7)$ -strings  $\Rightarrow N=2$  vector multiplet  
 $\Rightarrow U(1)_{D7}$

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 $\Rightarrow \phi_+, \phi_-$   
 $U(1)_{D3}: (+1), (-1)$

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$\Rightarrow$  mass splitting in hypermultiplet:  $m_{\phi_+}^2 = \frac{d^2}{2} \pm f(F)$



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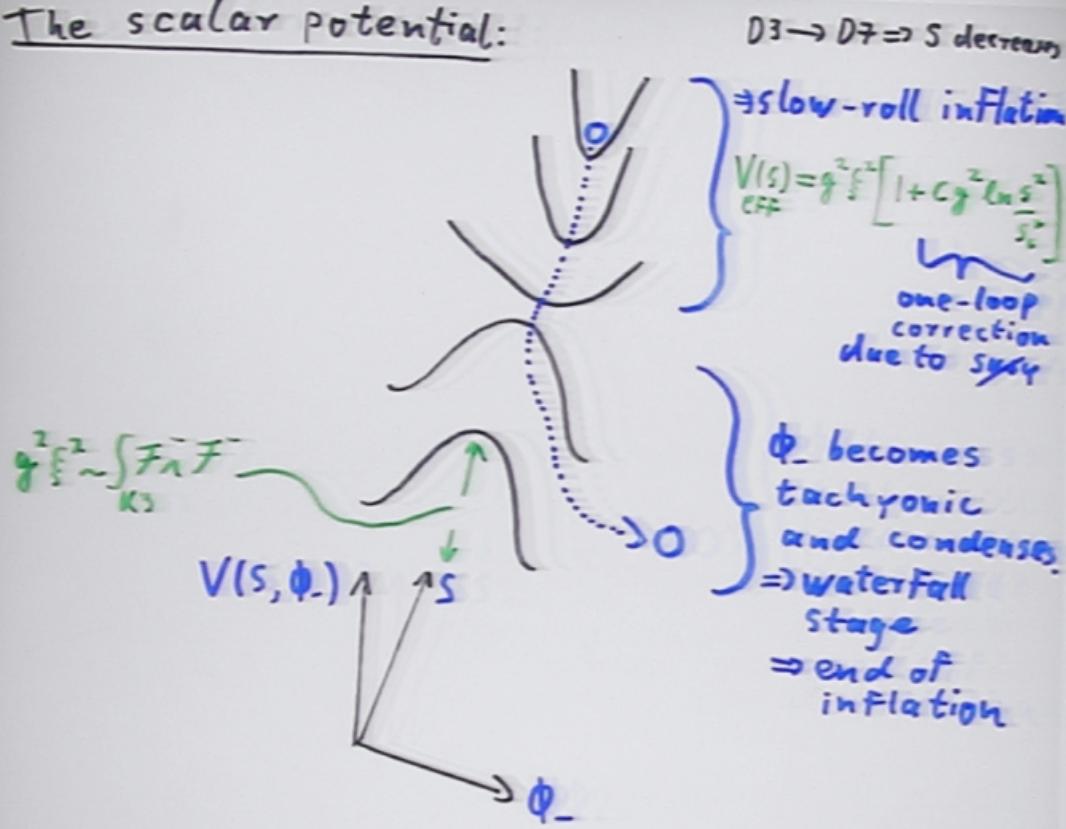
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$(\text{Str}(M^2) = 0)$   $m_{\phi_+}^2 = d^2$

The scalar potential:



Hybrid D-term inflation

( $q$ -problem, volume stabilization,  
shift symmetry, loop corrections...)

M. Haack's talk tomorrow

Unfortunately: This model has a cosmic string problem.

- $\phi_-$  is charged under  $U(1)_{D_3}^{\text{local}}$
- $\phi_-$  condenses  $\Rightarrow U(1)_{D_3}^{\text{local}} \rightarrow \mathbf{1}$
- $\Rightarrow$  "local" cosmic strings form  
  
("gauge strings") ("Nielsen-Olesen" strings)  
Thin magnetic flux tubes supported by a topologically non-trivial Higgs configuration.

[see also]  
H.Tye's  
talk  
tomorrow

$\Rightarrow$  spoil CMB predictions!

### Solutions?

- In  $D_3/\bar{D}_3$  inflation: (KULMANT 2003)  
Put  $\bar{D}_3$  at tip of warped throat  
→ string tension is red-shifted to acceptable values.  
But not for  $D_3/D_7$ .
- Assume  $g_{U(1)_{D_3}}^2 \leq 10^{-10}$  (or  $10^{-7}$ ) (Kallosh, Linde 2003)

But: Unnaturally small.

### ③ Generalized D-term inflation

Urrestilla, Achúcarro, Davis (2004):

"Double the Higgs extent"

one hypermultiplet  $\rightarrow$  two hypermultiplets

$$(\phi_+, \phi_-) \rightarrow \begin{matrix} SU(2)_{\text{global}} \\ \curvearrowright \end{matrix} (\phi'_+, \phi''_+)$$

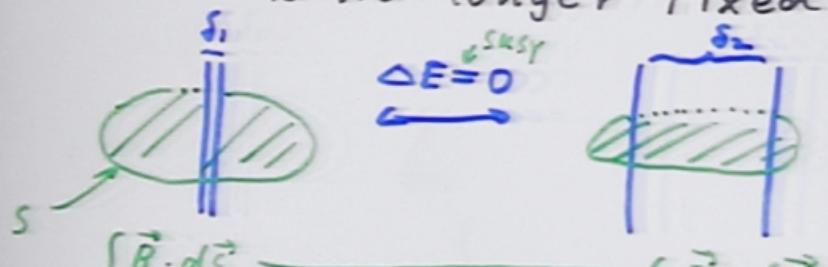
$$\Rightarrow G = SU(2)_{\text{global}} \times U(1)_{\text{local}} \rightarrow U(1)_{\text{global}}$$

"semilocal" strings.

$U(1)_{\text{local}} \rightarrow 1 \mathbb{I}$   $\Rightarrow$  Still topologically conserved fluxes.

$\Rightarrow$  cosmic strings can still exist.

But: The "width" of the flux tube is no longer fixed:



### ③ Generalized D-term inflation

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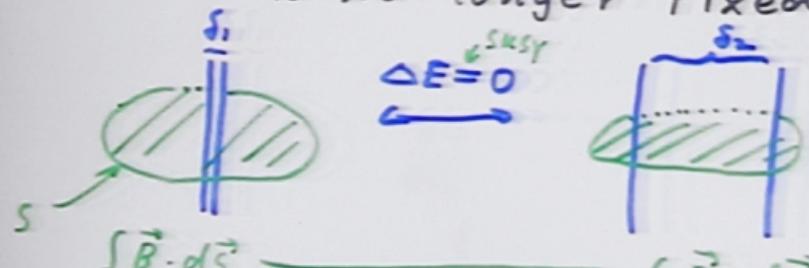
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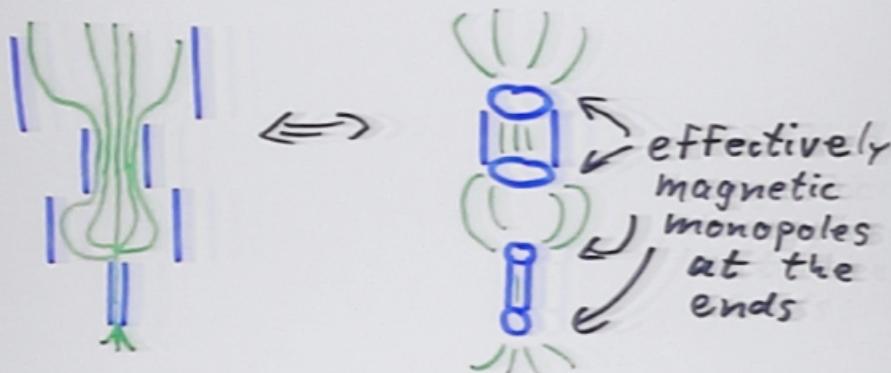
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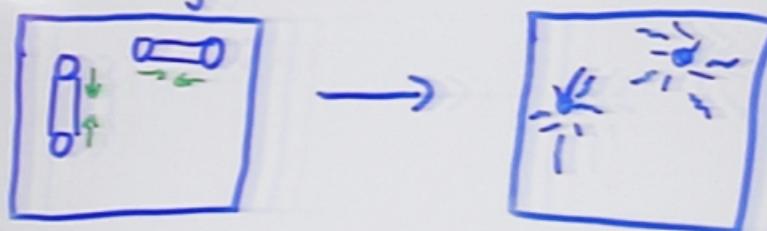


## Consequences for cosmic String Formation:

After the phase transition:  
string segments of different thicknesses:



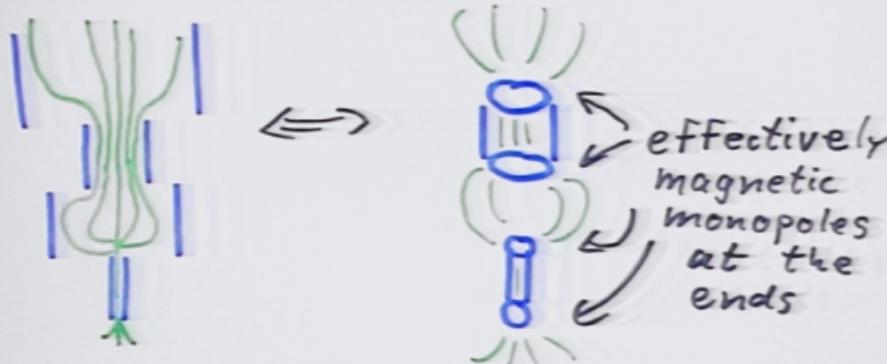
⇒ Most segments will shrink instead of combining with other segments:



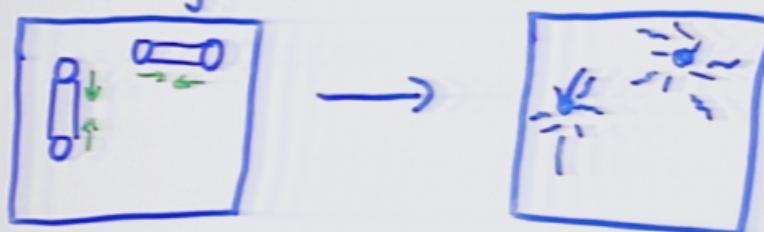
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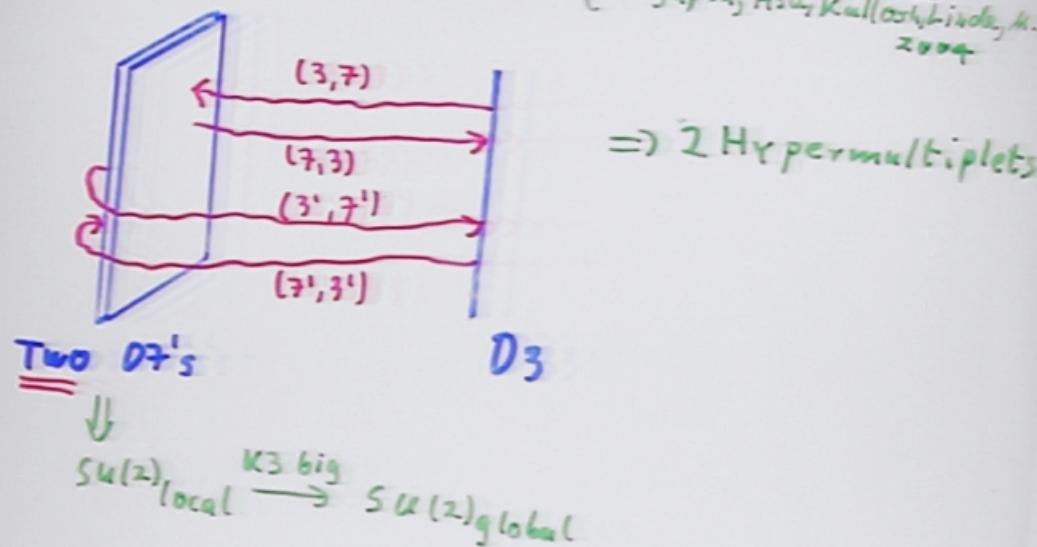
Urrestilla, Achúcarro, Borrill, Lidalle (2001)

Achúcarro, Vachaspati (1999)

⇒ ok for CMB + all good properties of D-term inflation preserved.

#### ④ Implementation in D3/D7 system

(Dasgupta, Hsu, Kallosh, Lindley, M. Z.,  
Zhang)



$\Rightarrow$  Effectively realizes  
Urrestilla, Achúcarro, Davis mechanism.  
F-theory analysis o.k.

## ⑤ Conclusions

- D3/D7 inflation: An alternative to D3/ $\bar{D}_3$  in IIB string theory.
- $\Rightarrow$  Hybrid D-term inflation in 4D
- $\Rightarrow$  Has a cosmic string problem
- A possible solution: Two coincident D7's
  - $\Rightarrow$  Doubles the Higgs content
  - $\Rightarrow$  semilocal cosmic strings
    - $\hookrightarrow$  stable solutions, but degenerate w.r.t. flux tube thickness.
    - $\Rightarrow$  Disappear soon after their formation.
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### Some open problems:

- Construct more realistic models
  - $\rightarrow$  moduli stabilization, quantum corrections, replace  $k_3 \propto T^2 / \beta_2$ ?
  - $\Rightarrow$  still consistent?
- Stringy description of semilocal strings?  
 $\langle$  Harmonic Teo  $\rangle$

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  - $\Rightarrow$  still consistent?
- Stringy description of semilocal strings? (Hanany, Tong, 2003)
- Other semilocal defects?
  - $\{$  Preskill, 1992 ; Hindmarsh, Holman, Kephart, Vachaspati, 1992 ...