

Title: Challenging the Alternative Perspectives in Dark Energy

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URL: <http://pirsa.org/05030102>

Abstract: The existence, and enigmatic nature, of 'Dark Energy' is one of the biggest theoretical upsets of recent times. In this seminar we present ideas on alternative theoretical and phenomenological approaches to the Dark Energy problem, in particular the issue of whether dark energy is a matter or gravity-based phenomenon, and the ways in which such approaches can be constrained and guided by observation. We also focus on some of the exciting future approaches that could provide unprecedented insights into the fundamentals of Dark Energy

## The key dark energy questions

- ☐ What is the underlying nature of dark energy?
- ☐ What dark energy properties can we measure observationally?



## The key dark energy questions

- What is the underlying nature of dark energy?

$$G_{\mu\nu} = -\frac{8\pi G}{c^4} T_{\mu\nu}$$



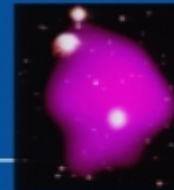
### Cosmological constant?

- Early phase transitions?
- Holographic?
- Anthropic?



### Adjustment to matter?

- An 'exotic', dynamical matter component?
- 'Unified Dark Matter'?

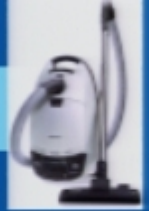


### Adjustment to gravity?

- Non-minimal couplings to gravity?
- Higher dimensional gravity?
- Inhomogeneous metric?



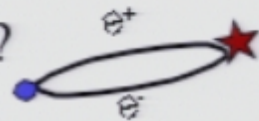
# $\Lambda$ - The problems with it



Why so small?

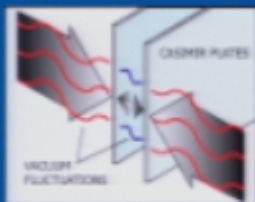
- UV divergences are the source of a dark energy fine-tuning problem

$$\Lambda \propto \int_0^\infty \sqrt{k^2 + m^2} k^2 dk = ?$$



- |                                    |                                 |
|------------------------------------|---------------------------------|
| a) QFT                             | = $\infty$ ?                    |
| b) regularized at the Planck scale | = $10^{76}$ GeV <sup>4</sup> ?  |
| c) regularized at the QCD scale    | = $10^{-3}$ GeV <sup>4</sup> ?  |
| d) 0 until SUSY breaking then      | = 1 GeV <sup>4</sup> ?          |
| e) all of the above                | = $10^{-47}$ GeV <sup>4</sup> ? |
| f) none of the above               | = $10^{-47}$ GeV <sup>4</sup> ? |
| g) none of the above               | = 0 ?                           |

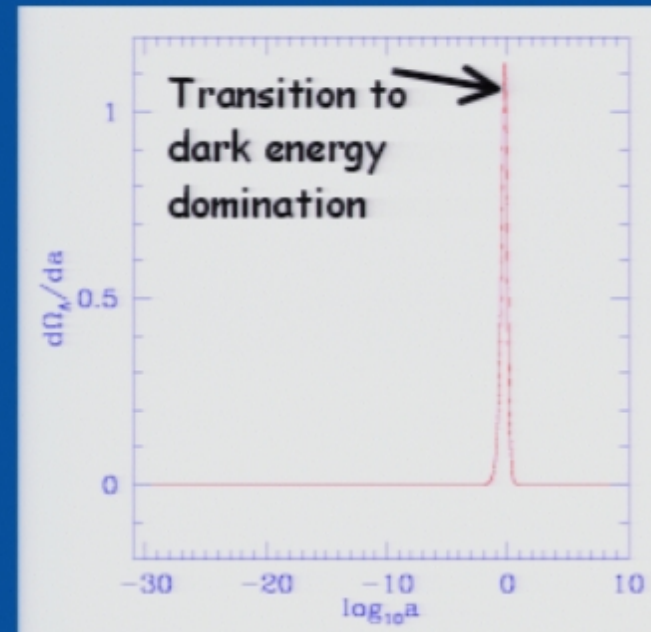
- The cut off scale would have to be way below the scales currently in agreement with QFT (Casimir effect, Lamb shift)



Why now?

- Coincidence problem

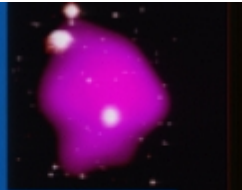
- Any later  $\rightarrow \Omega_\Lambda$  still negligible, we would infer a pure matter universe
- Any earlier  $\rightarrow$  chronically affects structure formation; we wouldn't be here



- Inevitably led to anthropic arguments

- At most basic predict  $\Omega_\Lambda/\Omega_m < 125$



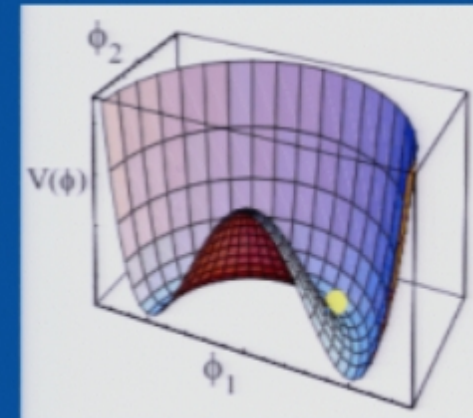


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## Scalar $\phi$ - spin 0 particle, like the Higgs

- with kinetic energy  $\dot{\phi}^2/2$ , Potential energy  $V(\phi)$
- Accelerative expansion when potential dominates

$$w = \frac{p}{\rho} = \frac{\frac{1}{2}\dot{\phi}^2 - V(\phi)}{\frac{1}{2}\dot{\phi}^2 + V(\phi)}$$



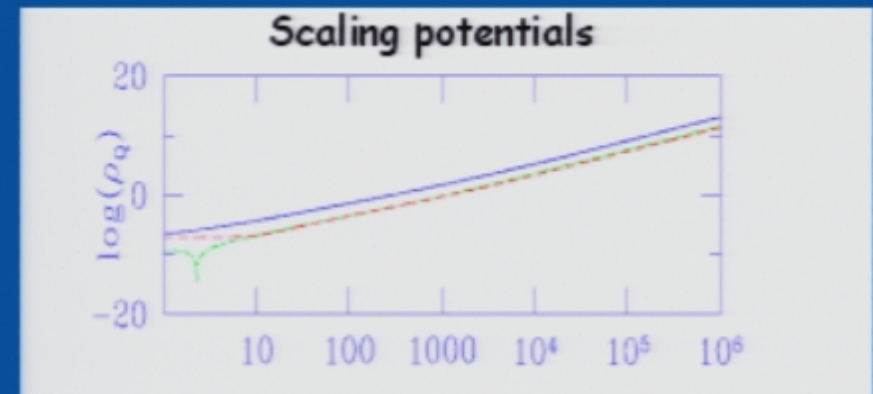
## Scaling potentials

- Evolve as dominant background matter

$$V \sim e^{-\lambda\phi}$$

Wetterich 1988,  
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- Need corrections to create eternal or transient acceleration Barrow, Bean, Magueijo 2000



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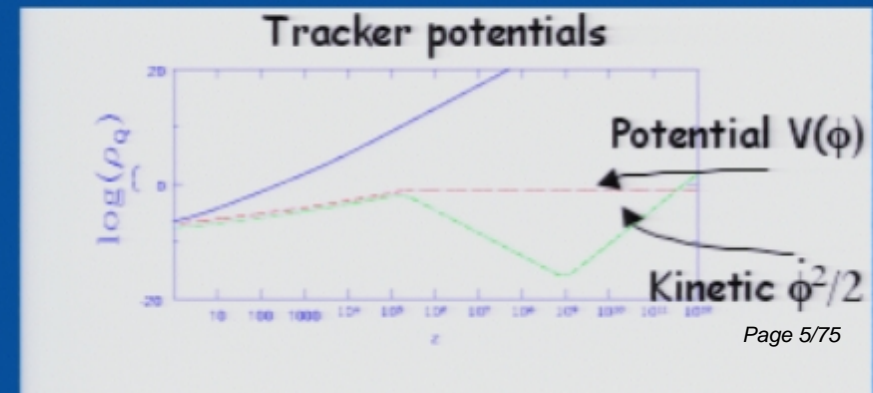
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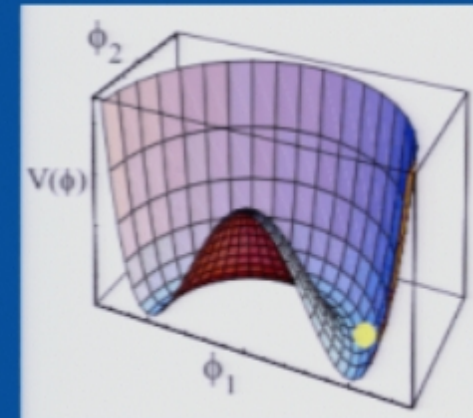


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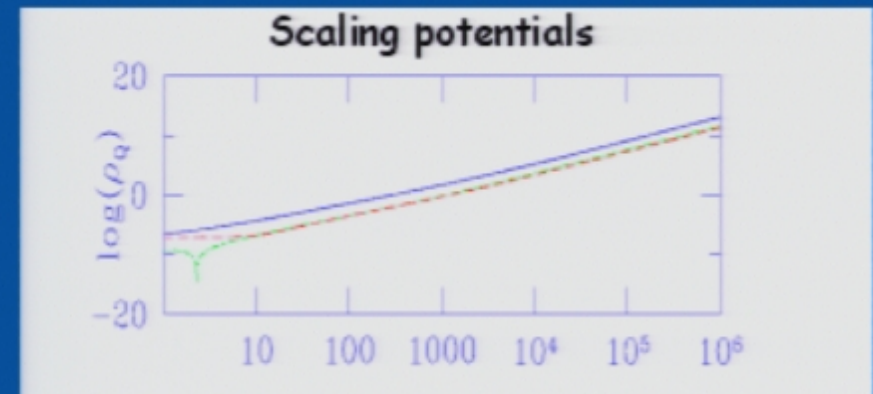
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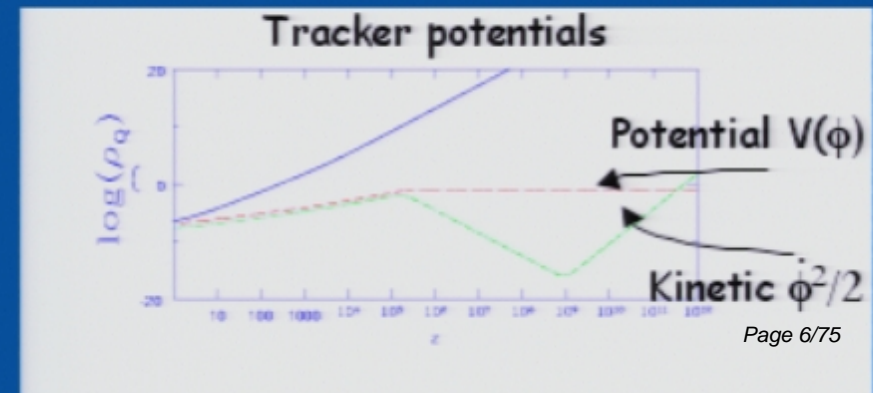
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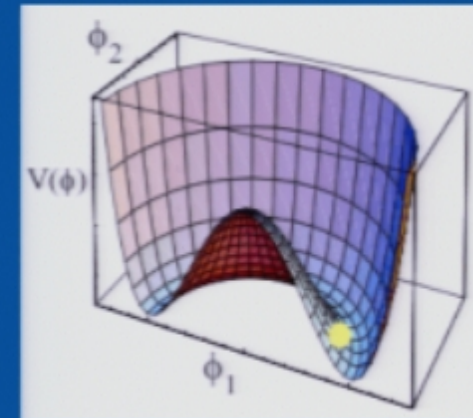
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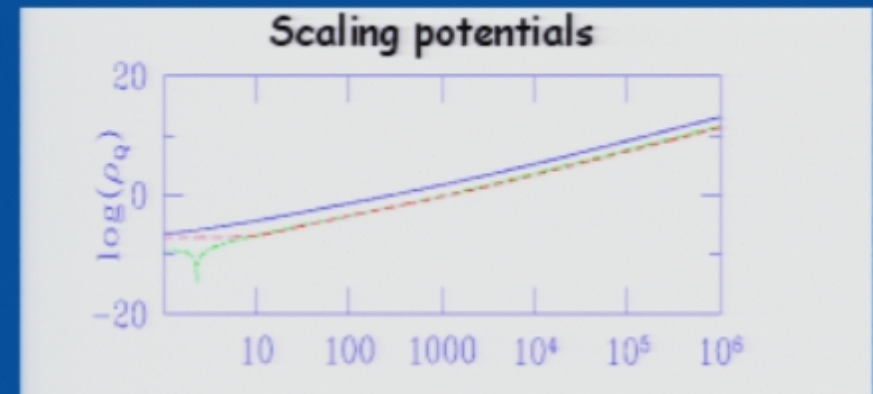
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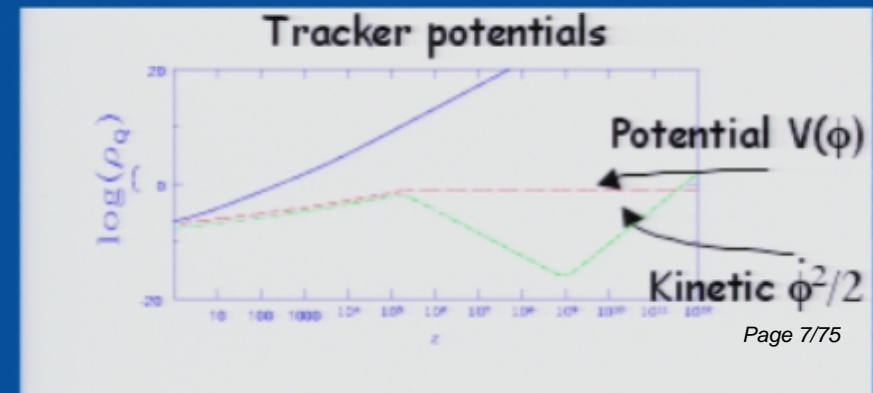
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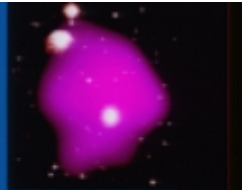
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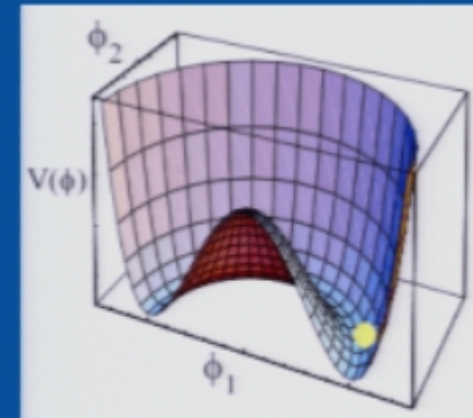
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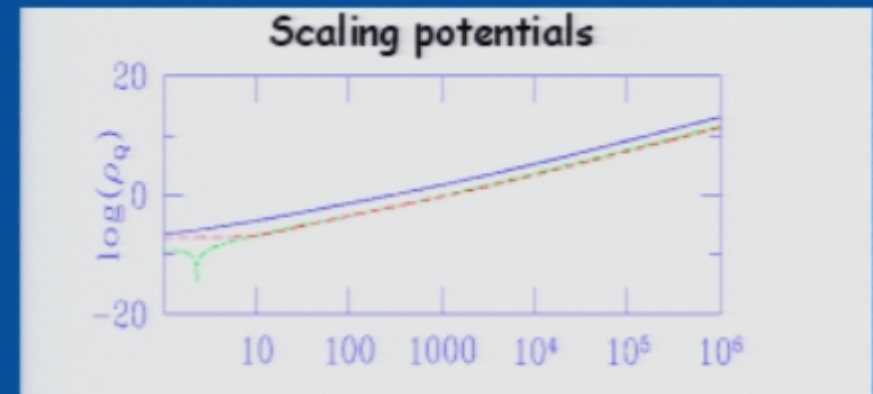
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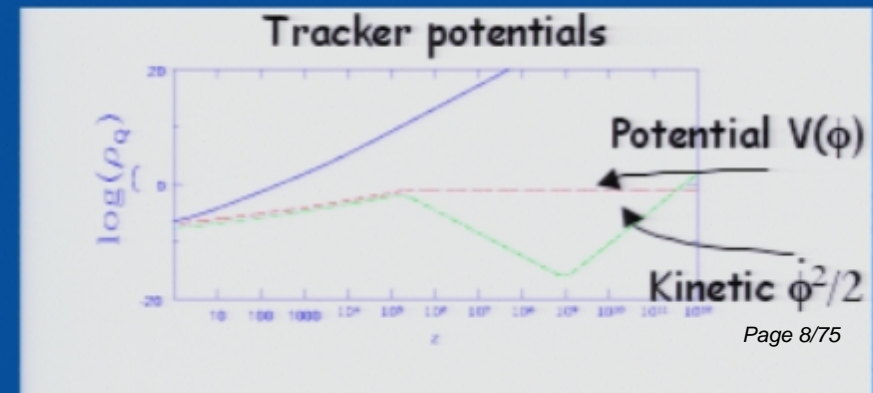
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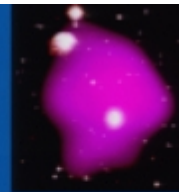
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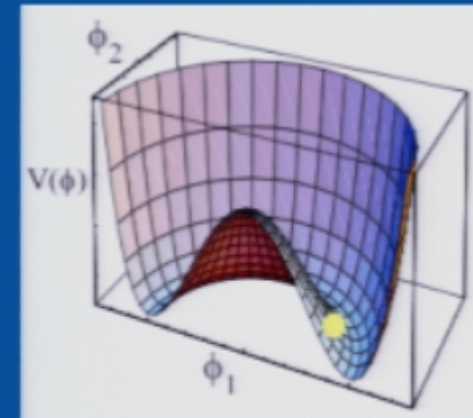


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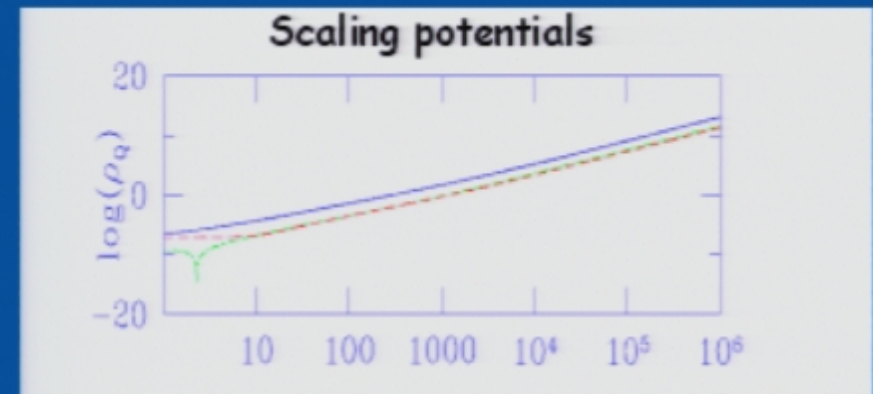
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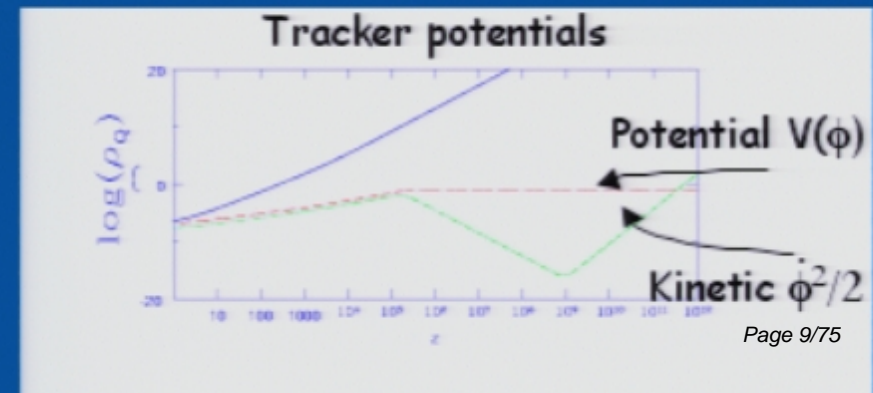
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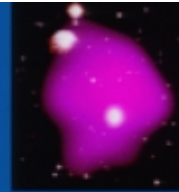
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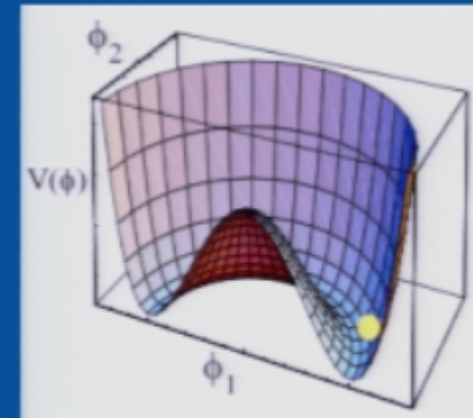


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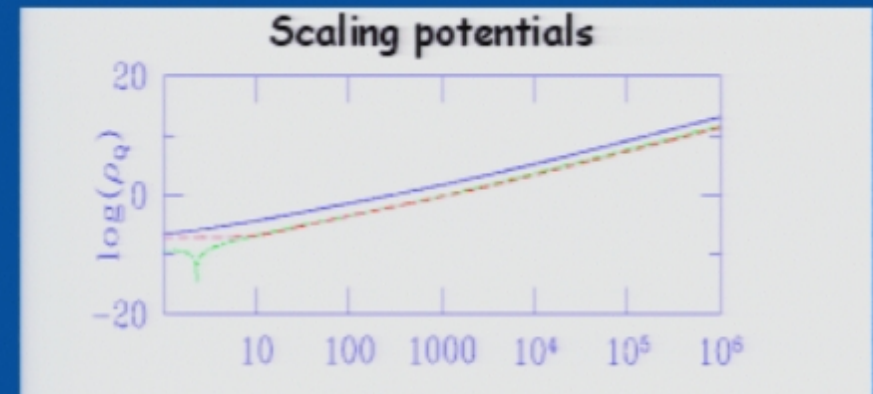
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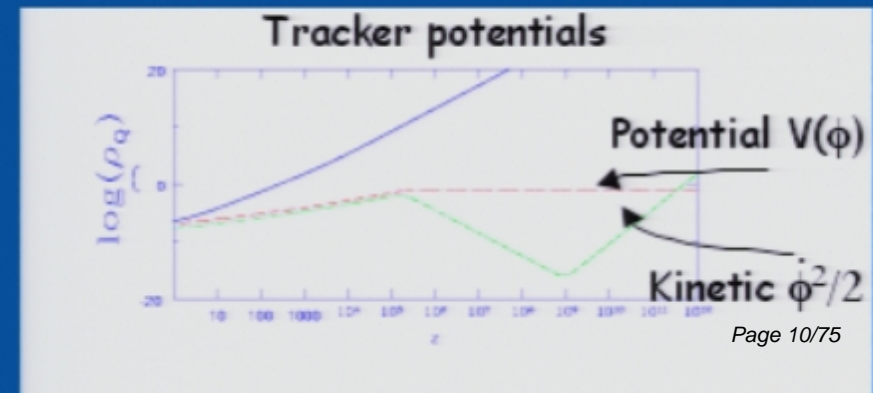
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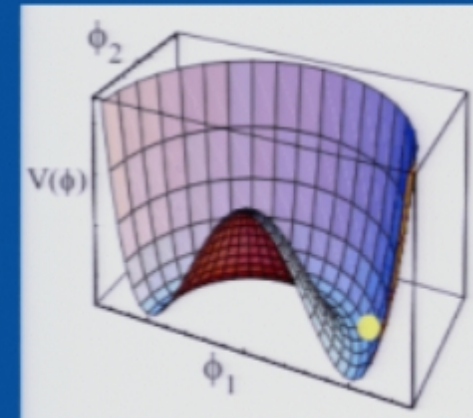


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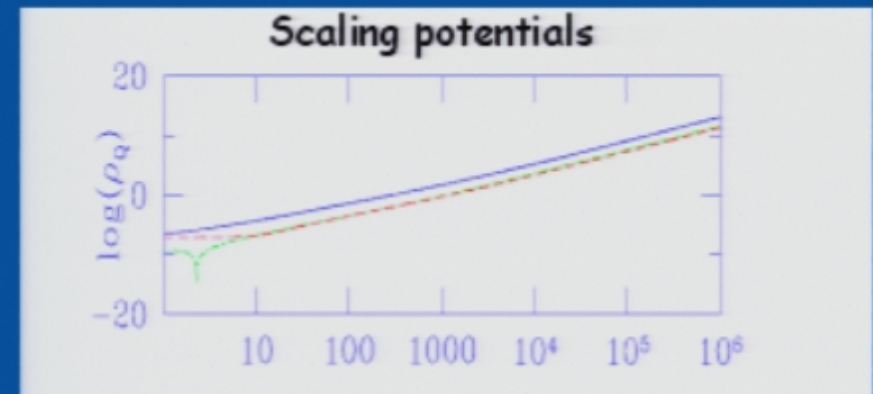
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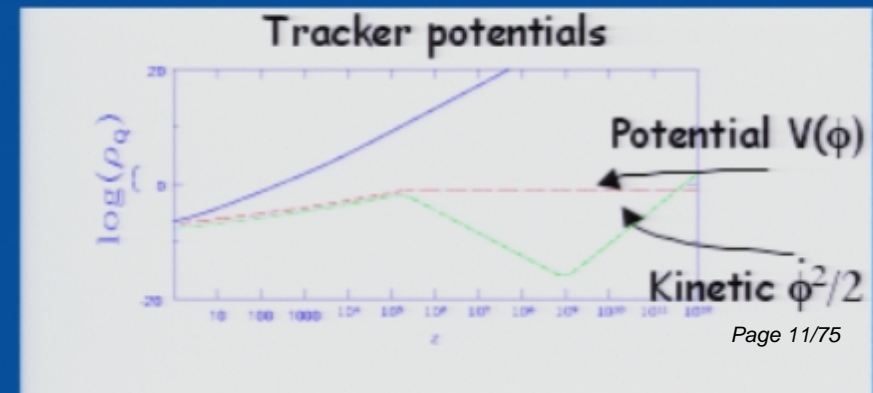
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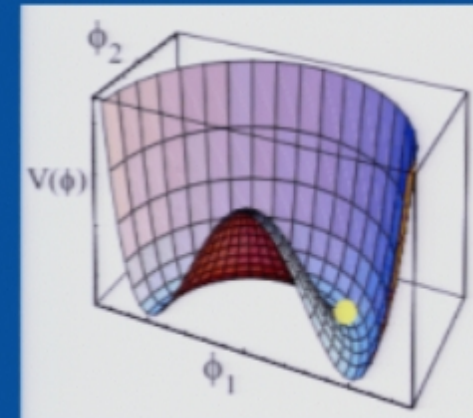


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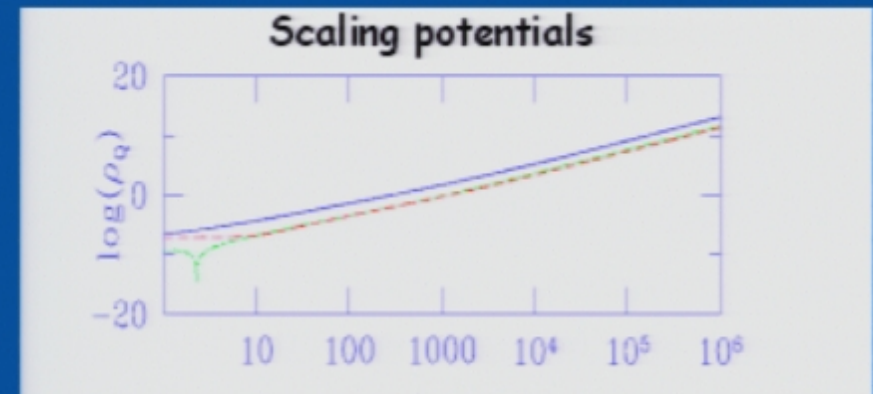
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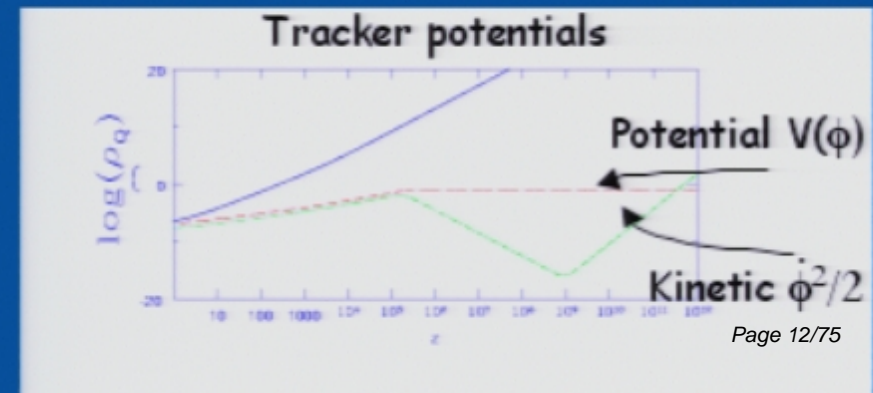
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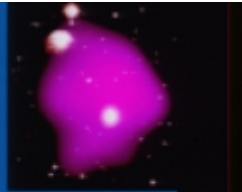
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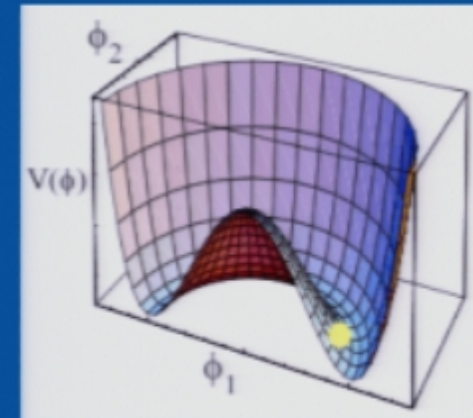
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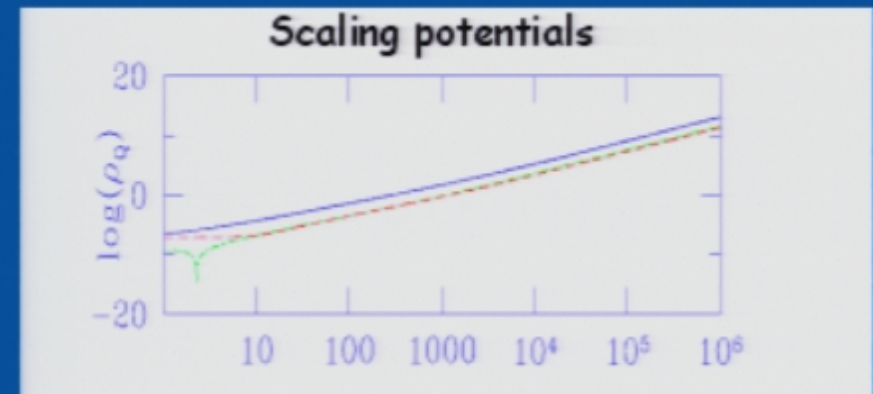
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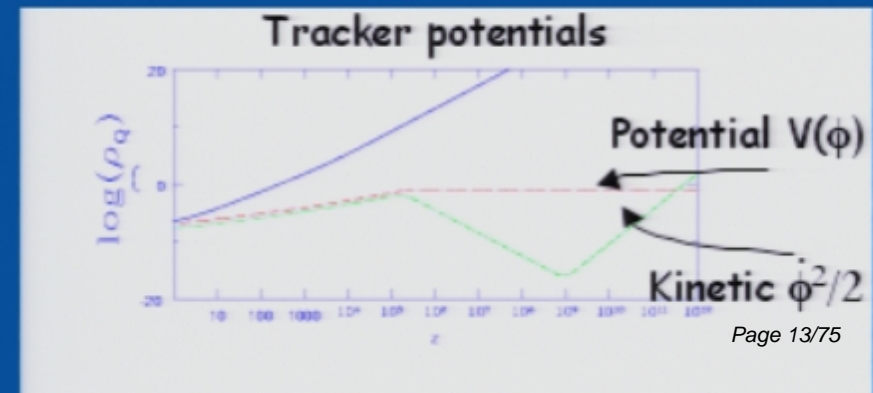
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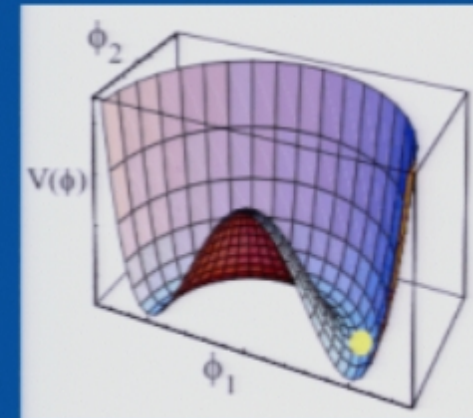


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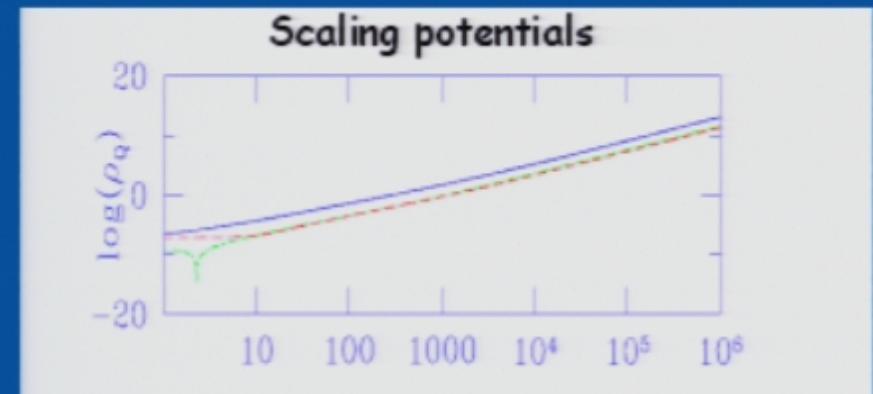
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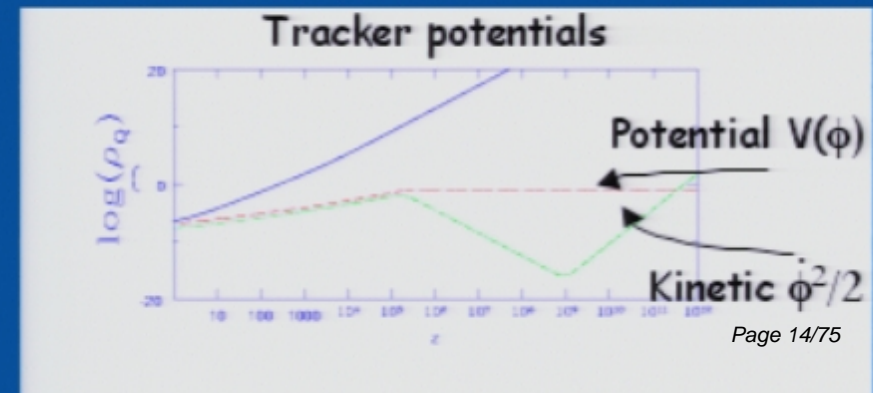
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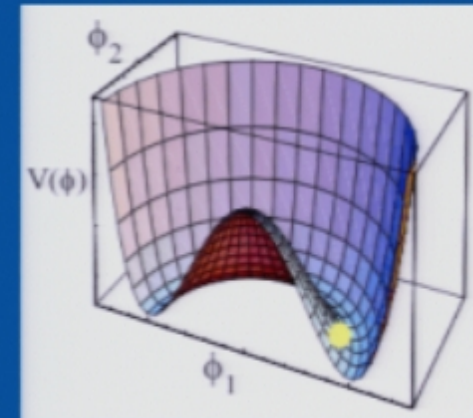


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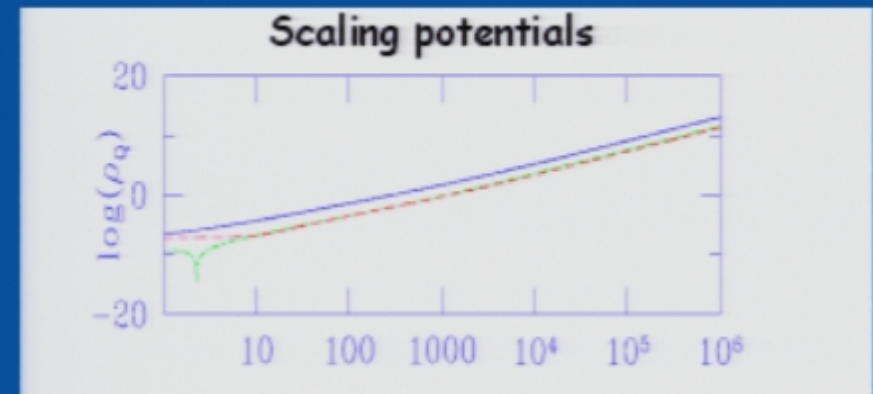
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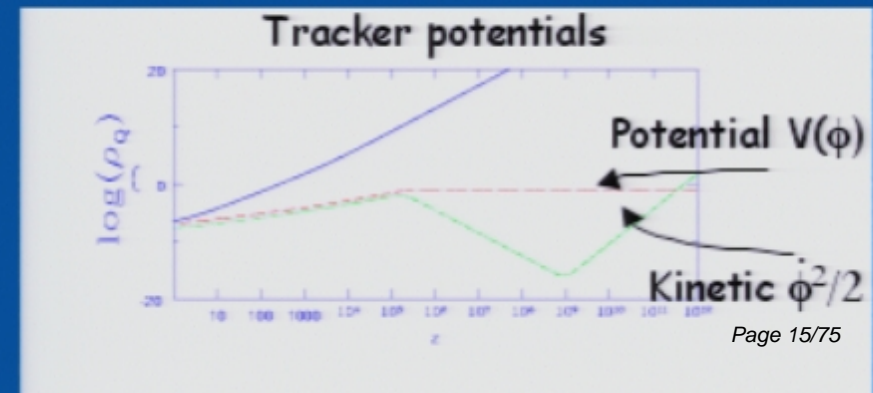
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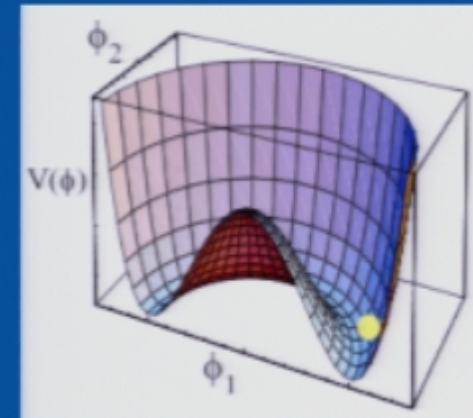


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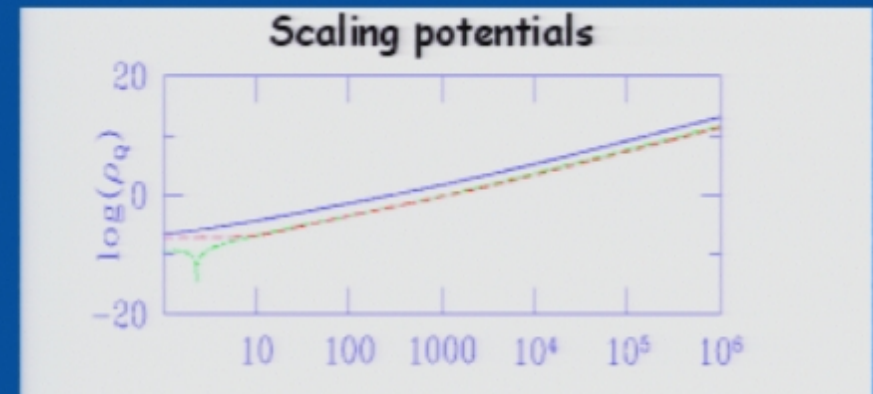
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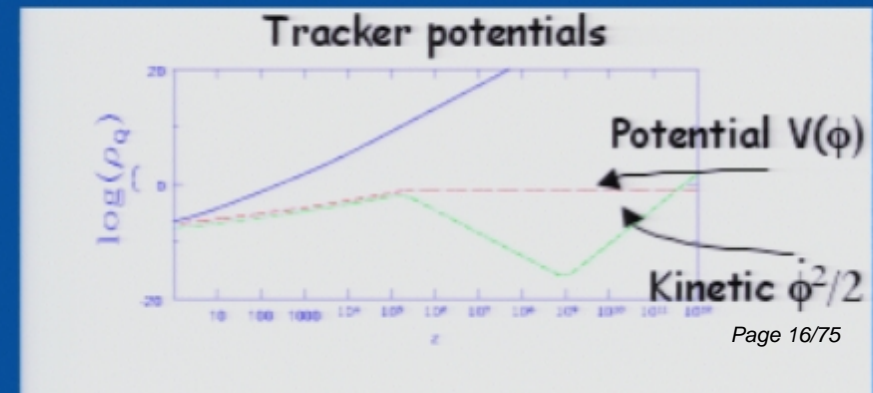
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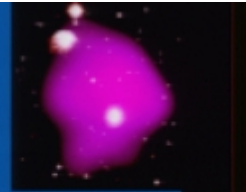
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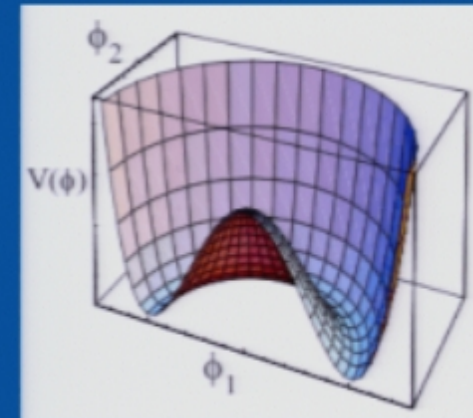


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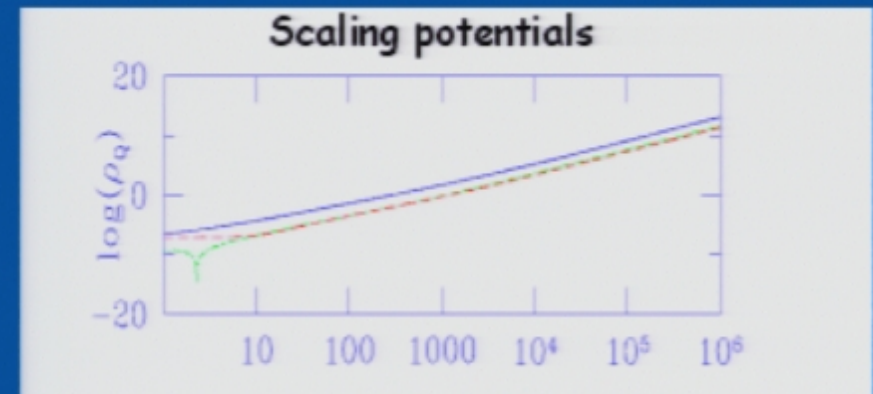
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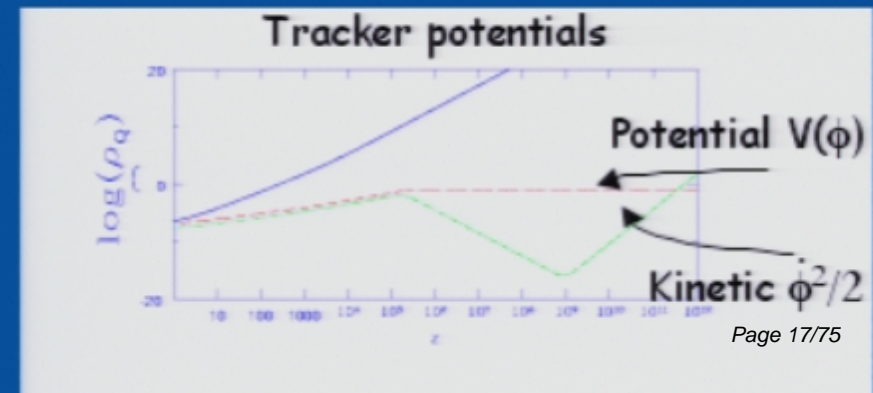
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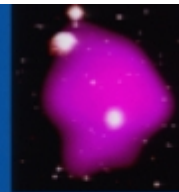
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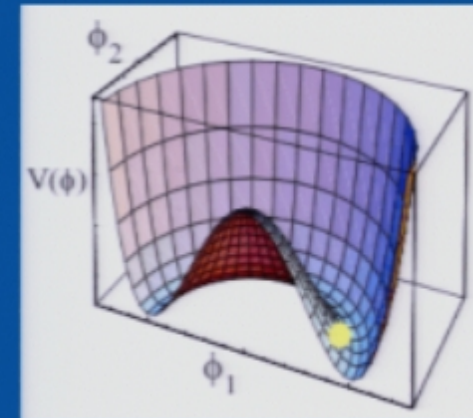


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- with kinetic energy  $\dot{\phi}^2/2$ , Potential energy  $V(\phi)$
- Accelerative expansion when potential dominates

$$w = \frac{p}{\rho} = \frac{\frac{1}{2}\dot{\phi}^2 - V(\phi)}{\frac{1}{2}\dot{\phi}^2 + V(\phi)}$$



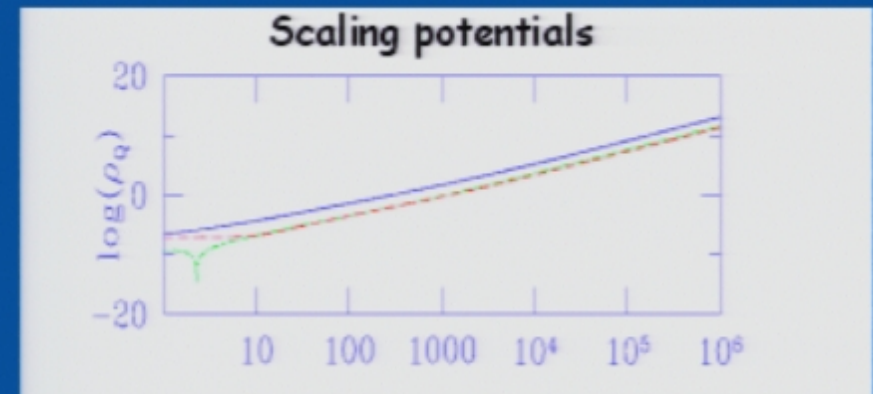
## Scaling potentials

- Evolve as dominant background matter

$$V \sim e^{-\lambda\phi}$$

Wetterich 1988,  
Ferreira & Joyce 1998

- Need corrections to create eternal or transient acceleration Barrow, Bean, Magueijo 2000



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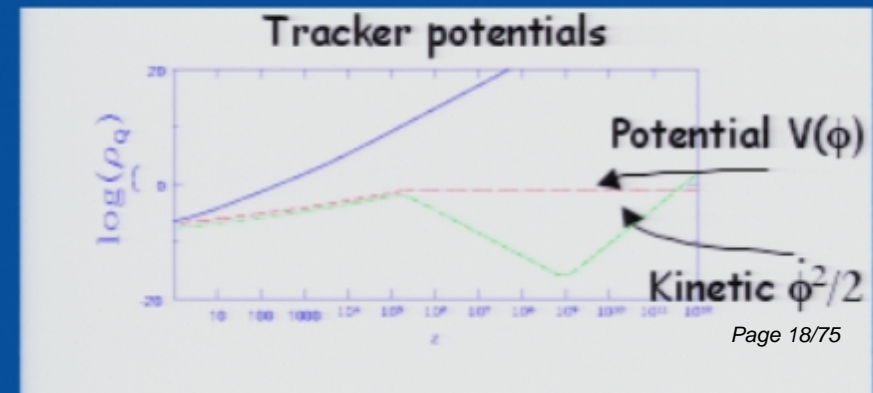
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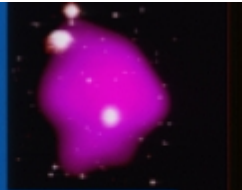
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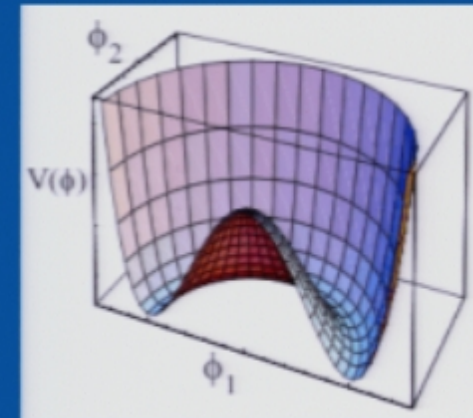
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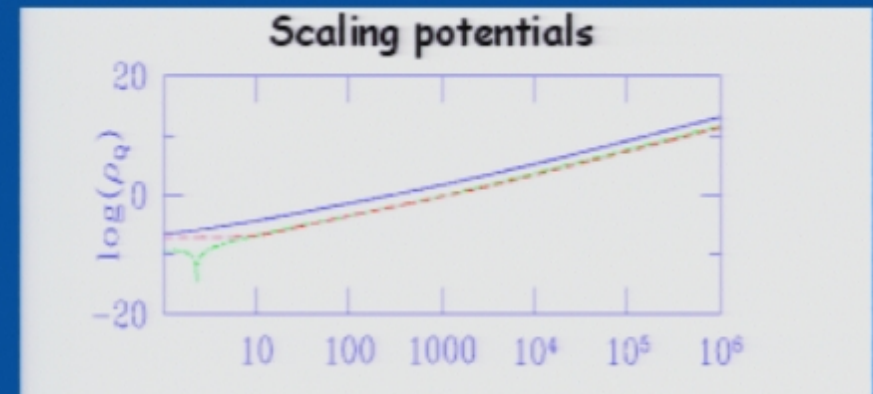
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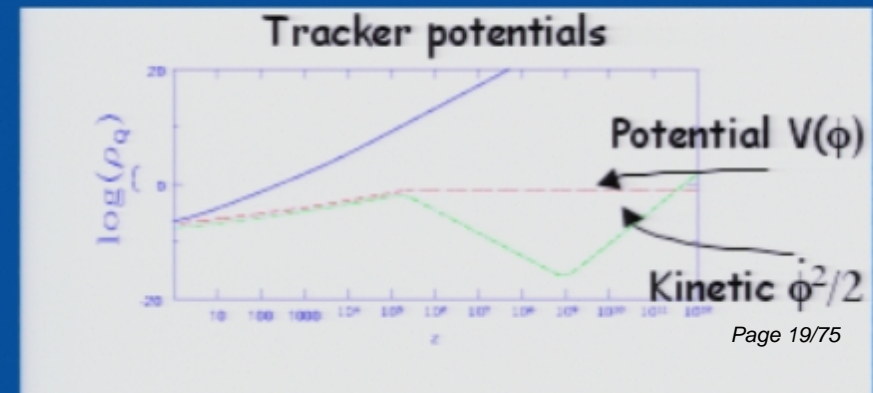
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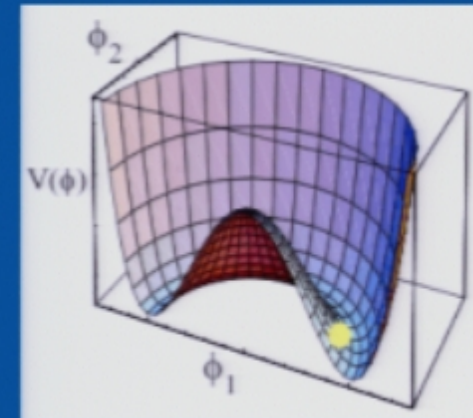


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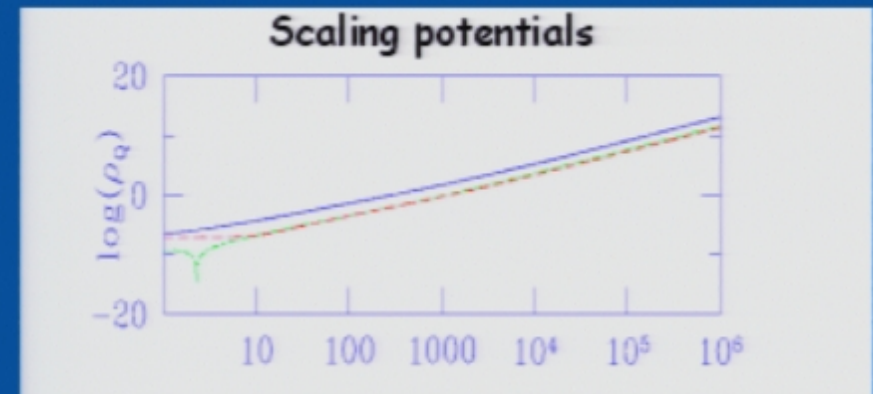
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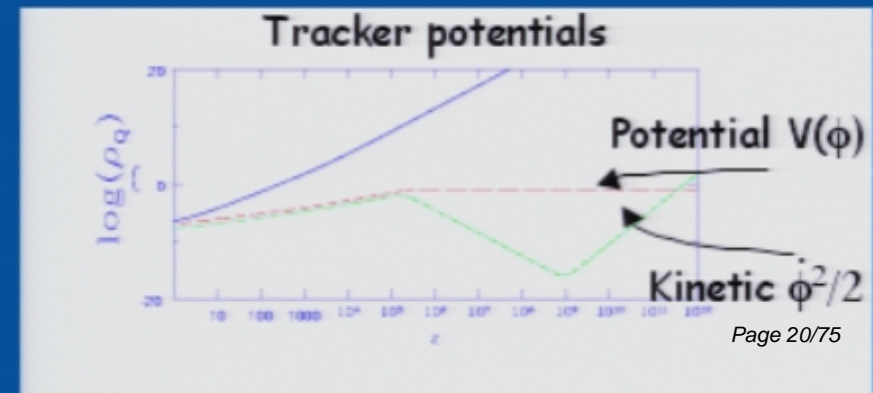
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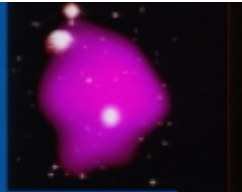
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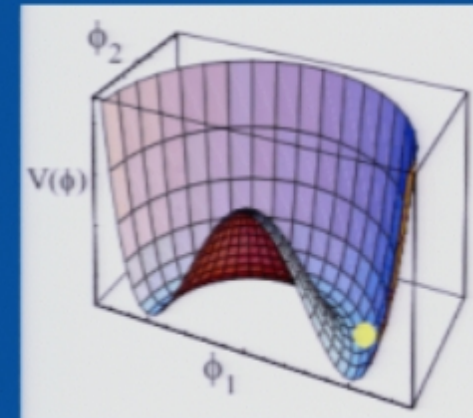
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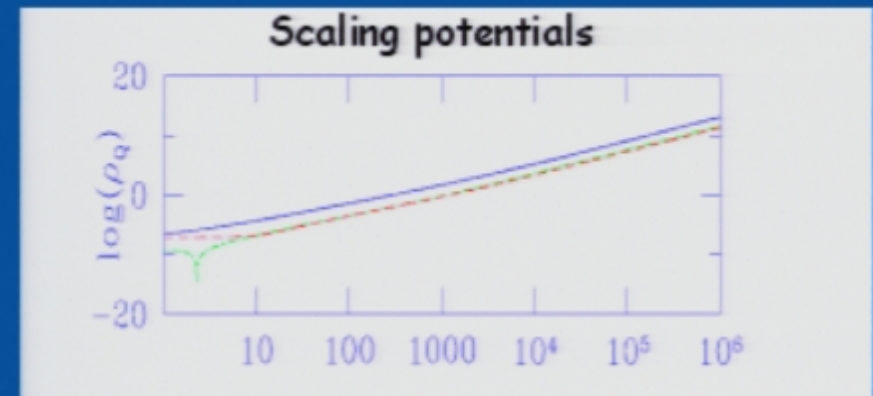
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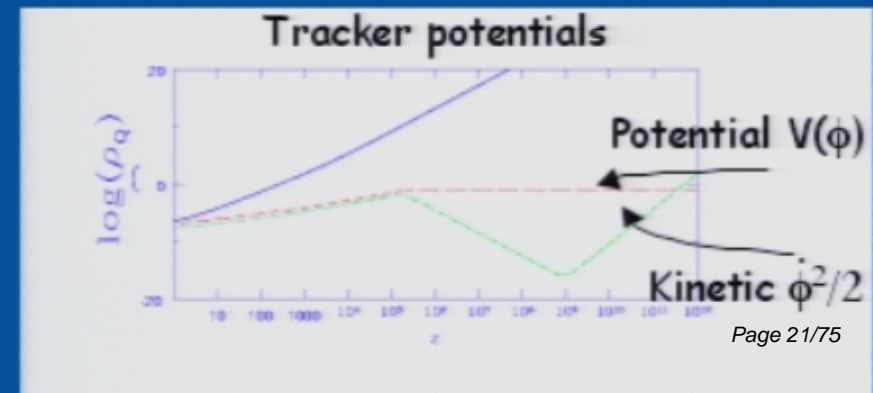
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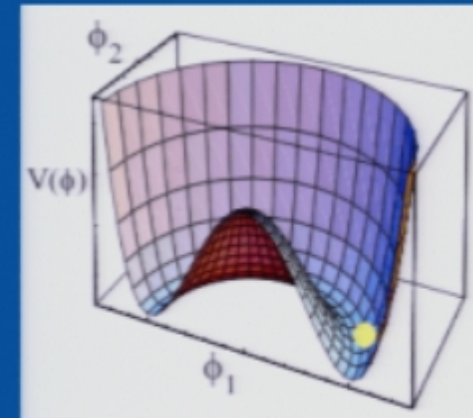


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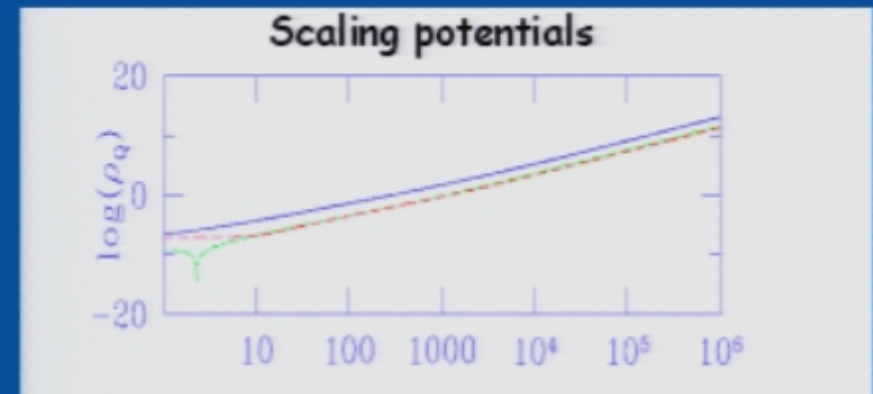
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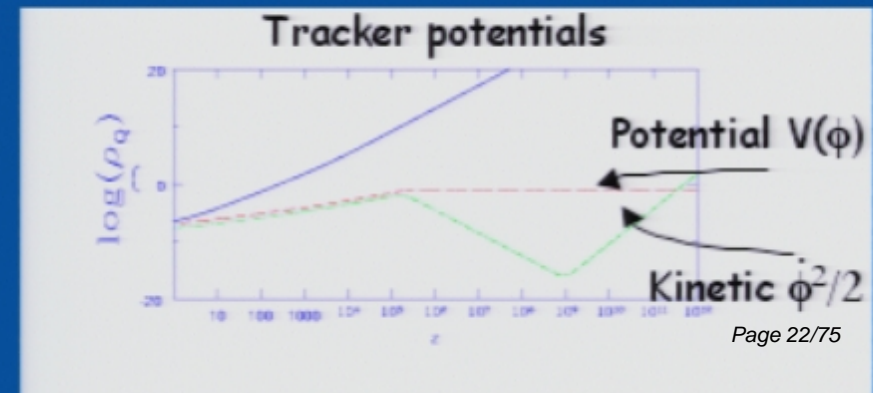
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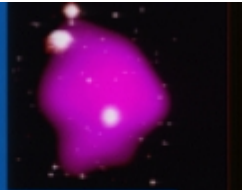
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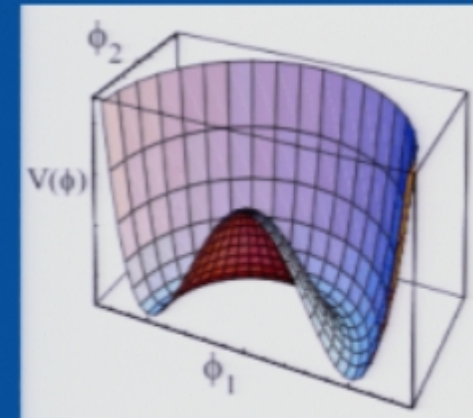


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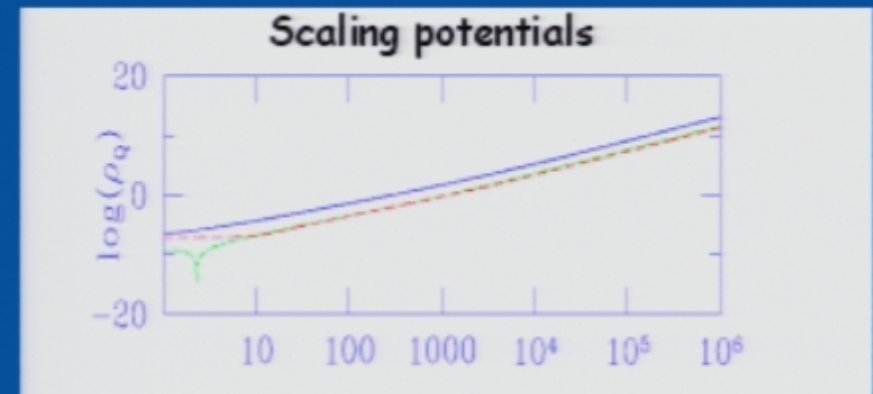
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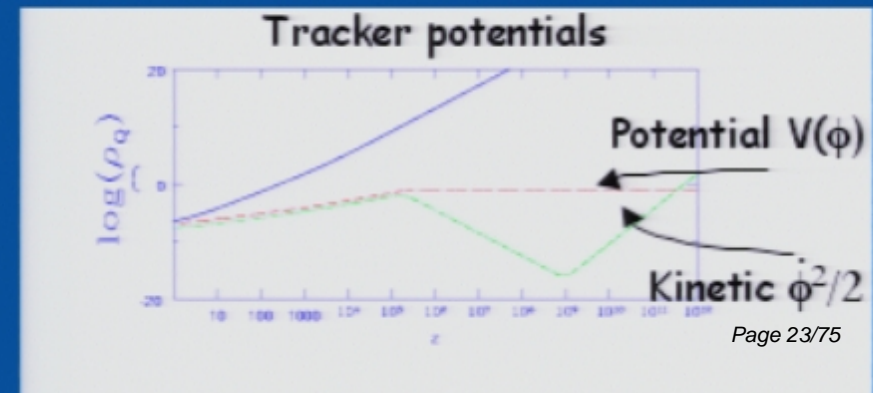
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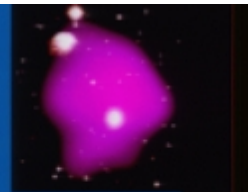
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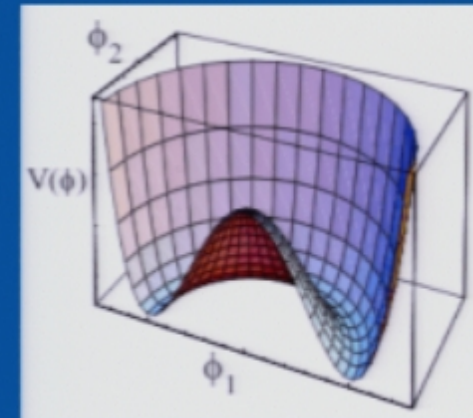


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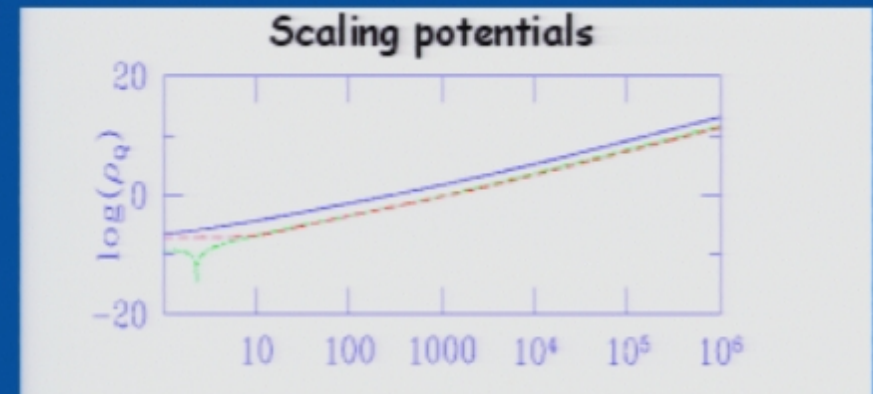
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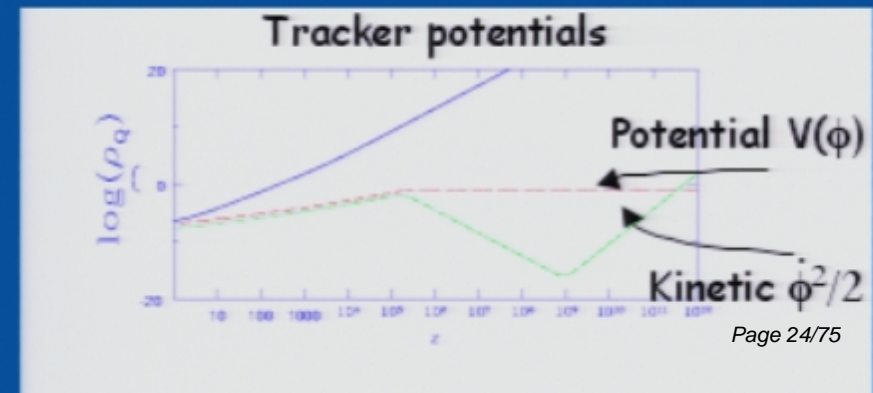
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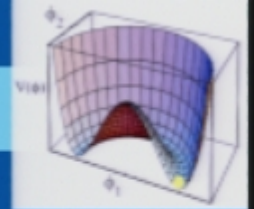
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# Tackling the coincidence problem: are we special?



- We're not special: universe sees periodic epochs of acceleration

$$V \sim M^4 e^{-\lambda Q} (1 + A \sin vQ)$$

Dodelson, Kaplinghat, Stewart 2000

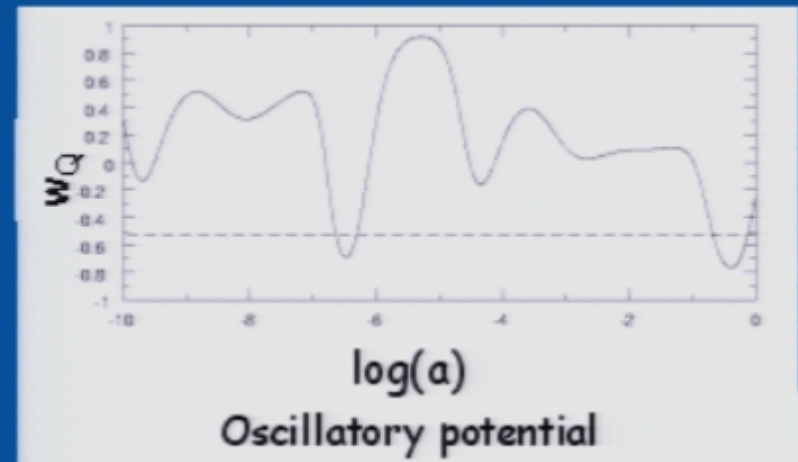
- We are special: the key is our proximity to the matter/ radiation equality

-Non-minimal coupling to matter (Bean & Magueijo 2001, Bean 2002)

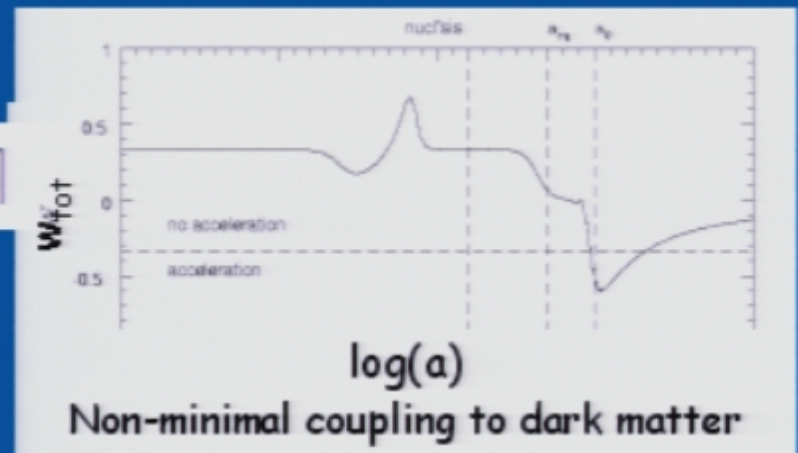
$$= \int d^4x \sqrt{-\bar{g}} \left[ B_g(\phi) \bar{R} + B_\phi(\phi) \bar{g}_{\mu\nu} \partial_\mu \phi \partial_\nu \phi - \frac{\alpha'}{4} B_F(\phi) \bar{F}^2 \dots \right]$$

$$\mathcal{L} = -\frac{R}{2} + \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - f(\phi) \mathcal{L}_c + \mathcal{L}_v$$

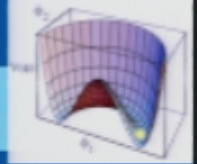
-k-essence : A dynamical push after  $z_{eq}$  with non-trivial kinetic Lagrangian term (Armendariz-Picon, et al 2000)



Dodelson, Kaplinghat, Stewart 2000



Bean & Magueijo 2001



## Tackling the $\Delta$ problems: implications for BBN

Scaling potentials can predict significant dark energy at earlier times treating  $\Omega_Q$  as  $\Delta N_{\text{rel}}$ .

Bean, Hansen, Melchiorri 2001

Bounds on Helium mass fraction,  $Y_{\text{He}}$

$-Y_{\text{He}} = 0.234 \pm 0.003 \rightarrow 0.244 \pm 0.002$  (used higher value as more relaxed bound) Olive et al. (1995), Isotov et al (1998)

-But more recently  $Y_{\text{He}} = 0.243 \pm 0.0009$  Olive et al. (2004)

Relative Deuterium abundance  $D/H$

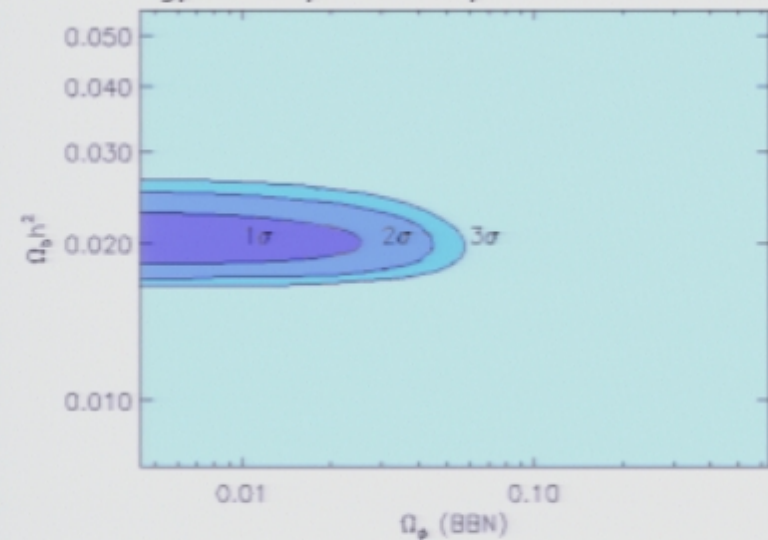
$-D/H = (3.0 \pm 0.4) \cdot 10^{-5}$  Burles et al (1998)

-But collated more recent value  $D/H = 2.6 \pm 0.4) \cdot 10^{-5}$  Kirkman et al (2003)

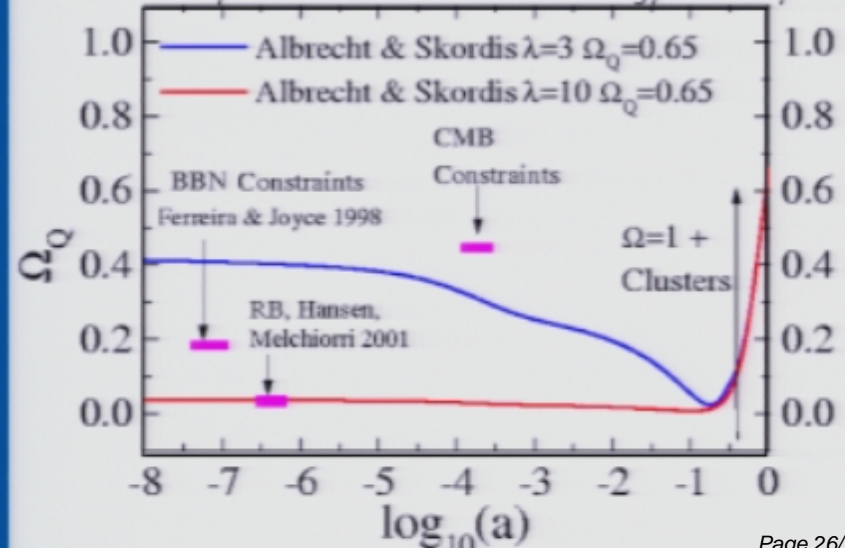
Abundance limits correspond to  $\Delta N_{\text{rel}} < 0.2$

-This translates into  $\Omega_Q \text{ (MeV)} < 0.05$  ( $2\sigma$ )

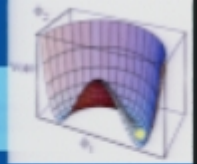
Dark energy vs baryon density BBN constraints



Early constraints on dark energy density







# Tackling the $\Delta$ problems: implications for primordial black holes

Early dark energy could be source for feeding primordial black holes (Bean and Magueijo 2002)

-can lead to alternative structure formation model where PBHs form the seeds for structure

Assuming gravitational field from scalar  $\ll$  BH so that we can impose a Schwarzschild metric around PBH

-flux of scalar into BH  $\sim \dot{\phi}^2$  determined in cosmological sol<sup>n</sup>

Scalar field will be accreted into a black hole and can have a significant effect.

$$\frac{dM}{dt} = -\frac{\alpha}{M^2} + \kappa \frac{M^2}{t^2}$$

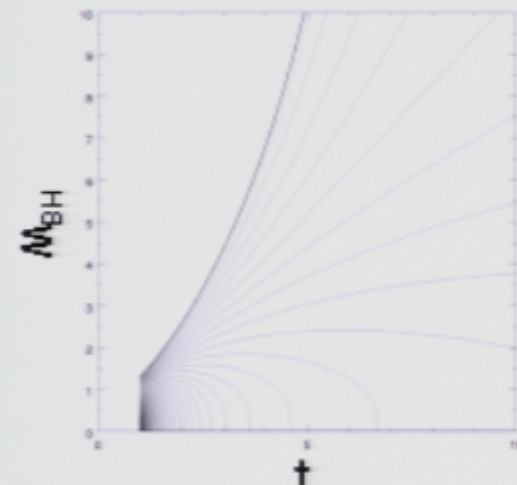
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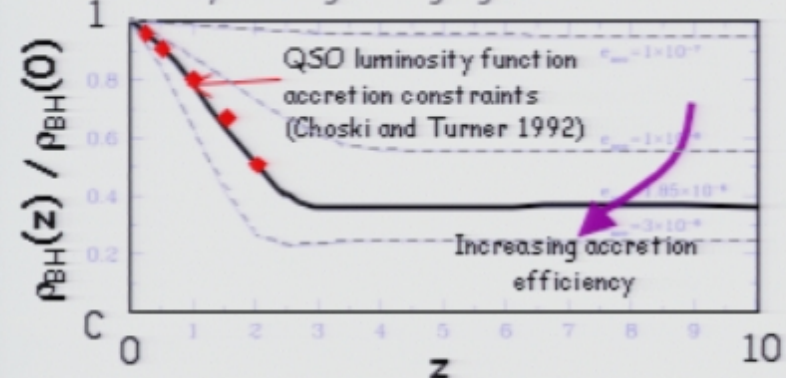
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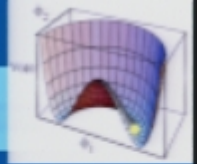
-Give number density and SMBH/halo mass relation  
consistent with observations

Evolution of BH mass with quintessence accretion and evaporation



Late-time evolution of cosmological BH energy density through merging and accretion





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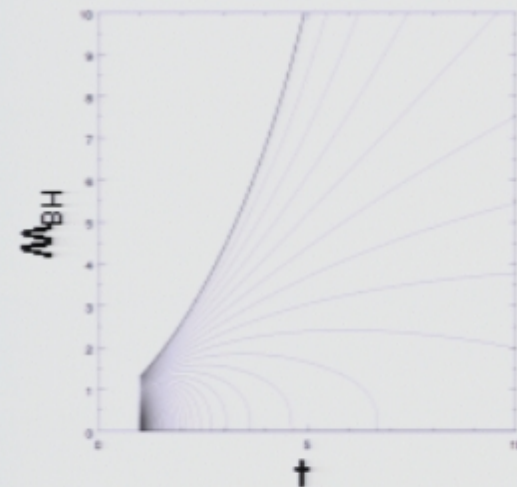
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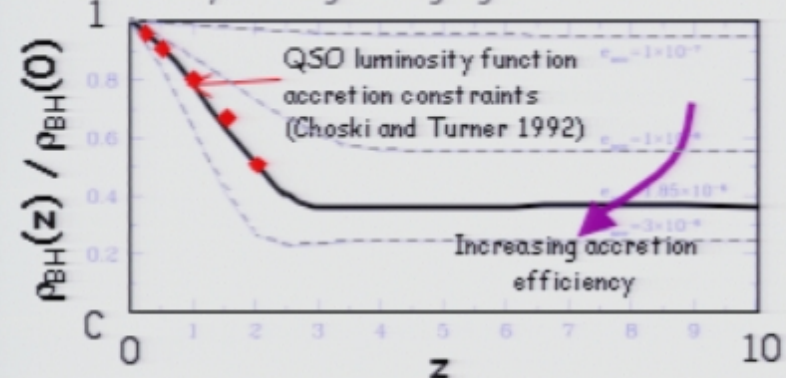
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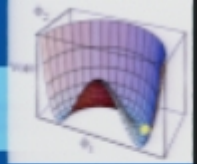
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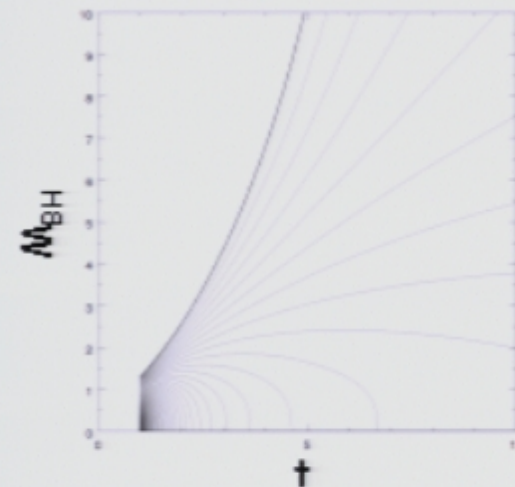
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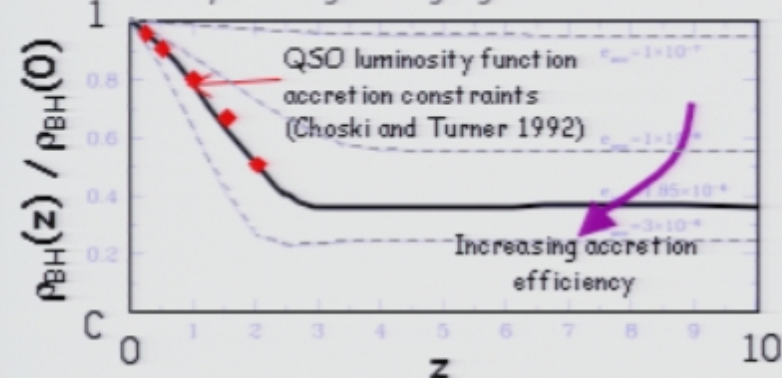
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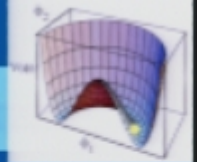
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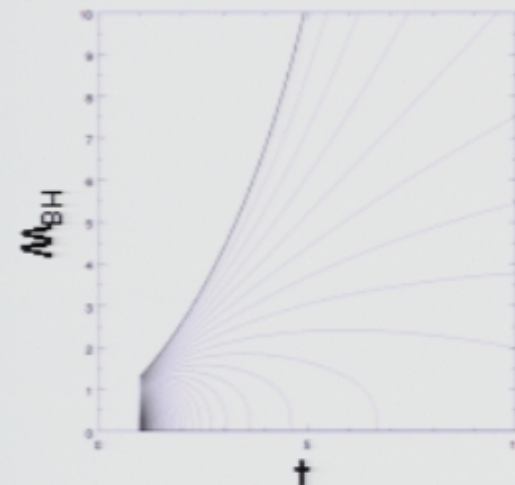
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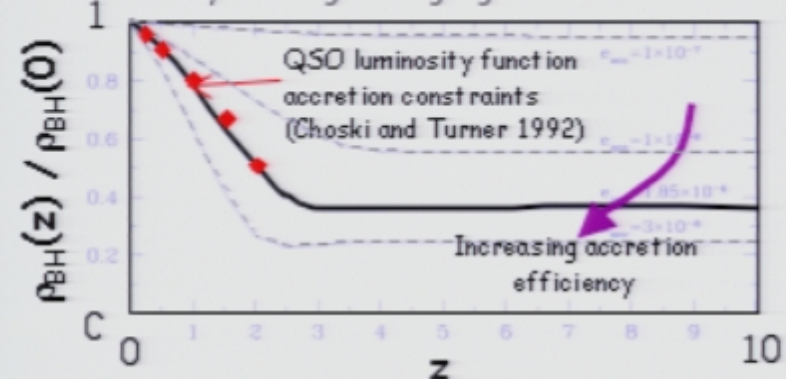
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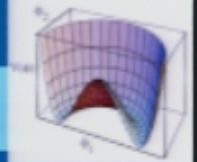
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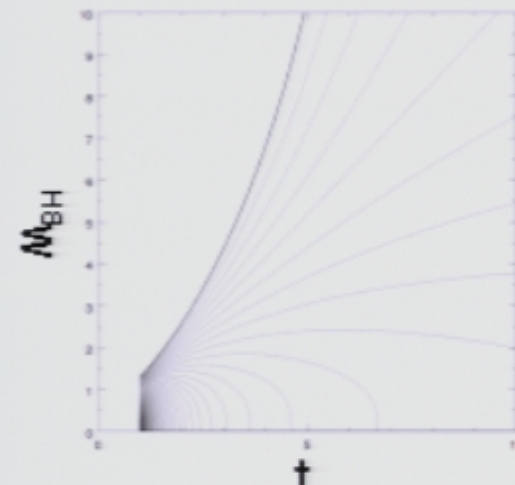
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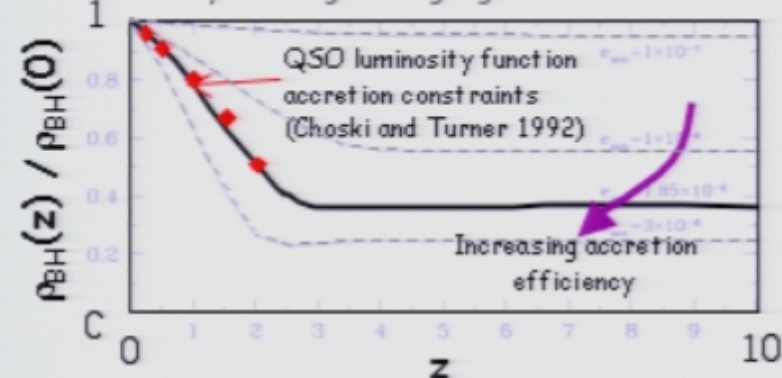
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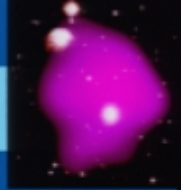


## Dark energy perturbations: an important discriminator?

- Natural extension to looking for  $w \neq -1$ ,  $dw/dz \neq 0$
- To distinguish between theories ...
  - only effecting the background ( $\Lambda$ , alterations to FRW cosmology )
  - with negligible clustering...(minimally coupled quintessence)
  - that could contribute to structure formation (non-minimally coupled DE, k-essence)
- To test if dark matter and dark energy are intertwined?
  - unified dark matter?
- From a theorist's perspective, to decipher the dark energy action
  - probing the dark energy external and self-interactions (or lack of) bound up in an effective potential
- From an observational perspective, to check that a prior assuming no perturbations is fair
  - Does it effect the combination of perturbation independent (SN) and potentially dependent (CMB/LSS/WL) observations?



## Expect little, but not necessarily no, clustering of dark energy



### □ Clustering properties determined by Jeans length and speed of sound

- maximize clustering by having low  $c_s^2$  and large Jean's length

$$\ddot{\delta} + 3H\dot{\delta} = -(k^2 c_s^2 - \lambda_J^2)\delta$$

### □ Consider from a scalar field perspective.....

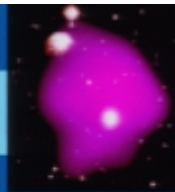
- Perturbing the continuity equation we get an expression like that for conventional matter but with little clustering ....

$$\ddot{\phi} + 3H\dot{\phi} = -(k^2 + V'')\phi + \delta_c \dot{\phi}$$

Notice that  $c_s^2=1$  for scalar field theories disfavoring clustering

Simple scalar field Jean's length imaginary: scalar doesn't cluster on its own

but it can cluster for large scales through gravitational feedback from a growing CDM mode...



## General clustering properties influenced by speed of sound

### □ Perfect fluids specified adiabatic speed of sound, $c_a^2$

- Purely determined by background (gauge independent)
- e.g. Particulate, elastic interactions  $\gamma$  and CDM

$$c_a^2 = \frac{\dot{p}}{\dot{\rho}} = w - \frac{\dot{w}}{3H(1+w)}$$

### □ For imperfect fluids, intrinsic entropy perturbations $\Gamma_{int}$ are also important

- $\Gamma \neq 0$  means dissipative self-interactions (bundled up in effective potential)

$$w\Gamma_{int} = 3H(1+w)c_a^2\left[\frac{\delta\rho}{\dot{\rho}} - \frac{\delta p}{\dot{p}}\right]$$

Internal isocurvature mode

- Gauge dependent speed of sound

$$c_s^2 = \frac{\partial p}{\partial \rho}$$

$$w\Gamma_{int} = [c_s^2(k, t) - c_a^2(t)]\delta(k, t)$$

Any frame: Gauge dependent  $c_s^2$  and density fluctuation

Rest-frame: Gauge independent  $c_s^2$  and density fluctuation





## $c_s^2$ in scalar field theories

- For a scalar field, minimally coupled to gravity with a simple kinetic term  $c_s^2=1$
- Consider a homogenous scalar field, simply coupled to gravity, with kinetic variable  $X=(\partial_\mu\phi)^2/2$

$$\mathcal{L}(\phi, X) = \sqrt{-g} [f_1(X) + f_2(X, \phi) - V(\phi) + f_3(\phi)\mathcal{L}_m]$$

- General speed of sound,

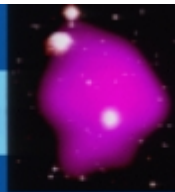
$$\frac{\delta p}{\delta \rho} = \frac{\mathcal{L}_{,X}\delta X + \mathcal{L}_{,\phi}\delta\phi}{(2X\mathcal{L}_{,XX} + \mathcal{L}_{,X})\delta X + (2X\mathcal{L}_{,\phi X} - \mathcal{L}_{,\phi})\delta\phi}$$

- In the rest frame  $v=0 \rightarrow \delta\phi=0$ , only kinetic terms determine speed sound

$$\delta T_j^0 = (1+w)\rho v_j = \frac{k}{a^2}\dot{\phi}\delta\phi Y_j$$

$$c_s^2 = \frac{\mathcal{L}_{,X}}{2X\mathcal{L}_{,XX} + \mathcal{L}_{,X}}$$

- For general scalar field actions  $c_s^2$  can be less than 1 (encouraging clustering), if
  - have a non-trivial kinetic term
  - have a non-minimal coupling to gravity or matter other than CDM



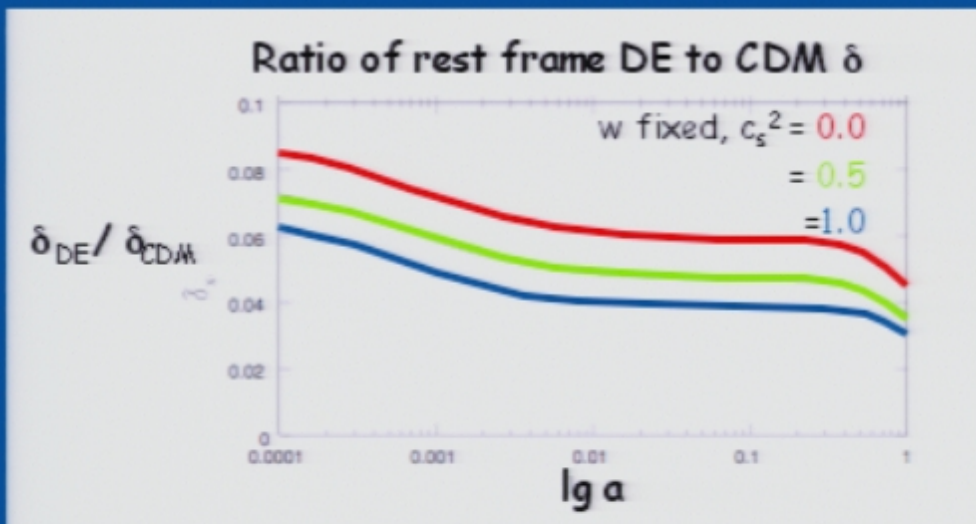
# Dark energy clustering and its affects structure formation

- Sound horizon associated with rest frame  $c_s^2$

$$s_{eff}(\tau) = \int_0^\tau d\tau' c_s$$

-outside horizon DE perturbations have growing mode driven by dominant background component.

- DE perturbations only affect structure at times when  $\Omega_\chi > \Omega_b$  (at late times)
- Including DE perturbations has an effect on dark matter growth

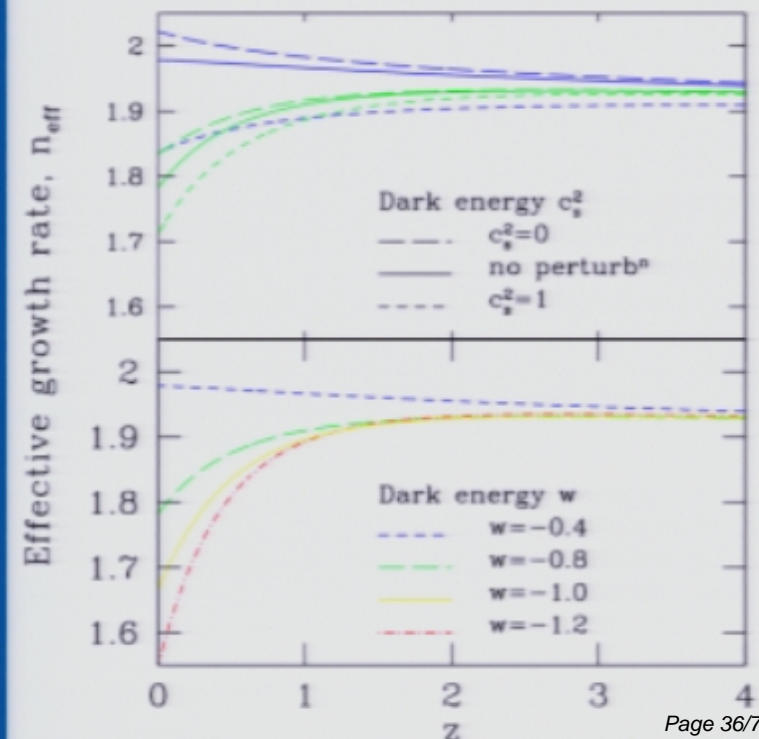


Bean and Dore PRD 69 2003

$$\delta_{DE} \approx A(c_s^2, w)(1 + w)\delta_{CDM}$$

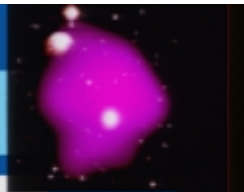
-inside horizon perturbations decay, and dark energy component is smoothed on these scales

## Evolution of the effective dark matter growth rate $\delta_{CDM}(\tau) \propto \tau^{n_{eff}}$





## $c_s^2$ in scalar field theories : k-essence



- Explain coincidence problem using attractor properties of scalar field action

- Non trivial kinetic term drives dark energy evolution

$$\mathcal{L}(\phi, X) = \sqrt{-g} [f_1(X) + f_2(X, \phi)]$$

$$c_s^2 = \frac{\mathcal{L}_{,\phi}}{2X\mathcal{L}_{,XX} + \mathcal{L}_{,\phi}}$$

- Recently been applied to "ghost condensates" (e.g. Piazza and Tsujikawa 2004)

-Start with a general action

$$= \int d^4x \sqrt{-g} [B_g(\phi) \bar{R} + B_\phi(\phi) \bar{g}_{\mu\nu} \partial_\mu \phi \partial_\nu \phi - \frac{\alpha'}{4} B_F(\phi) \bar{F}^2 \dots]$$

-Taylor expansion ...

$$\int d^4x \sqrt{-g} \left[ \frac{M_p^2}{2} R \pm \frac{1}{2} (\partial\phi)^2 - V(\phi) + \text{HOTS} \right] + S_m[\phi, g_{\mu\nu}, \Phi_i]$$

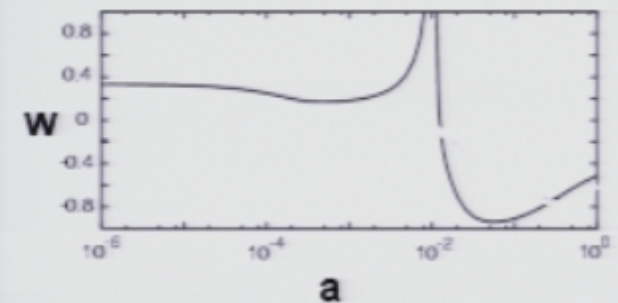
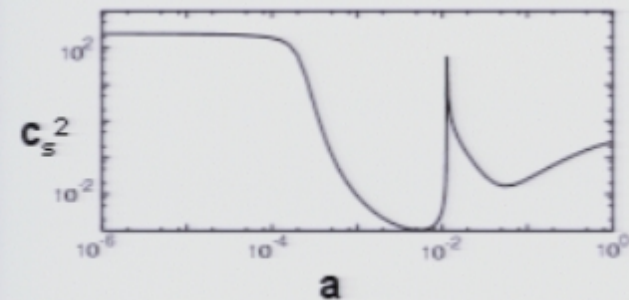
-K-essence like action

$$\frac{A}{m^4} (\partial\phi)^4 e^{\lambda\phi/M_P}$$

$$\mathcal{L} = p(\phi, X) + \mathcal{L}_m[\phi, \Psi_i, g_{\mu\nu}]$$

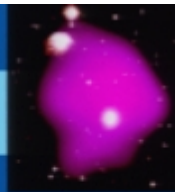
$$p(\phi, X) = -X + c_1 e^{\lambda\phi} X^2 - c_2 e^{-\lambda\phi}$$

Example of redshift evolution of  $w$  and  $c_s^2$  for a k-essence model



Erickson et. al [astro-ph/0112438](#)  
Steinhardt et. al. [astro-ph/0004134](#)

# $c_s^2$ in scalar field theories : "extended quintessence"



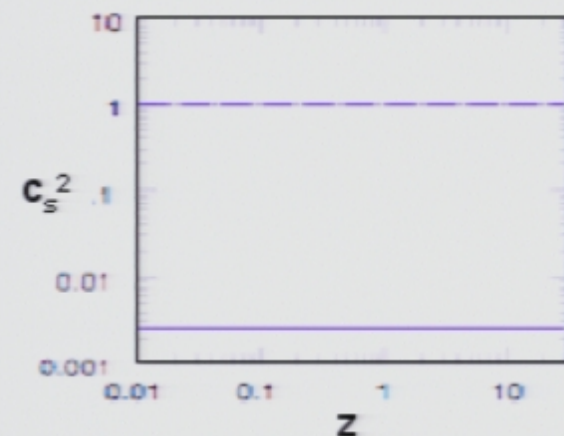
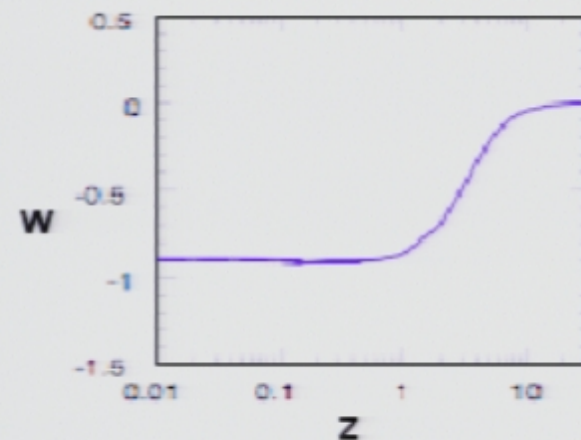
- Late time acceleration and varying Newton's constant produced by same scalar field

$$\mathcal{L}(\phi, X) = \sqrt{-g} \left( \frac{f(\phi, R)}{2\kappa} - \omega(\phi)X - V(\phi) \right)$$

$$f(\phi, R) = (1 - \xi\phi^2)R$$

- At early times an R-boost generates gravitational dragging which results in scalar tracking dominant matter component ( $w \sim 0$  and  $c_s^2 \sim 0$ ).
  - constraints from CMB experiments
  - limits on gravitational coupling from local gravitation experiments
- Could lead to non-linear  $\phi$  and  $\delta\phi$  over-densities and cavities on sub-horizon scales
  - Detectable large scale structure /lensing signature?

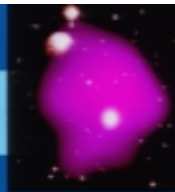
Redshift evolution of equation of state and speed of sound



Minimal quintessence

Extended quintessence





# Tackling the dark matter and dark energy problems as one

## □ 'Unified' dark matter / dark energy

- Clustering at early times like CDM  $w \sim 0, c_s^2 \sim 0$
- Accelerating expansion at late times like  $\Lambda$   $w < 0$

## □ Phenomenology: Chaplygin gases (Bean and Dore PRD 68 2003)

-an adiabatic fluid, parameters  $w_0, \alpha$

$$p = -\frac{|w_0|}{\rho^\alpha}$$

$$c_s^2 = \alpha |w|$$

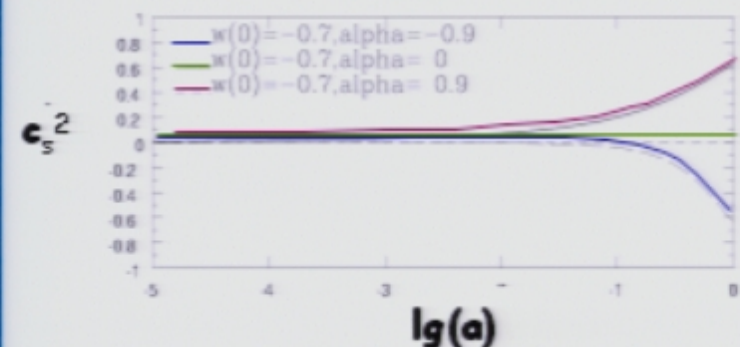
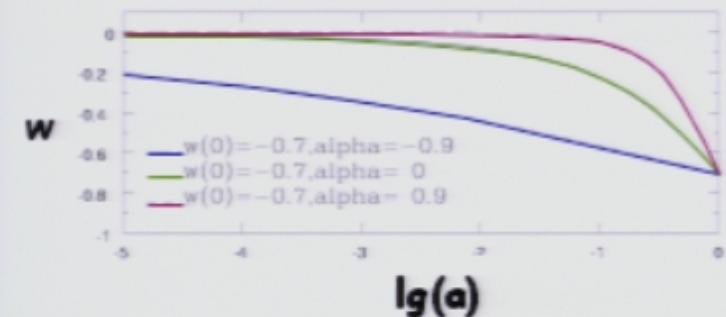
## □ Particle physics interpretation? Condensates with low Compton wavelength (Bassett et al 2002)

## □ Strings interpretation? Born-Infeld action is of this form with $\alpha=1$ (e.g. Gibbons astro-ph/0204008)

$$\mathcal{L}(\phi, X) = \sqrt{-g} V(\phi) (1 + X)^{\frac{1}{2}}$$

$$V(\phi) = \frac{\lambda}{\cosh(\phi/\phi_0)}$$

Evolution of equation of state and speed of sound for Chaplygin Gas



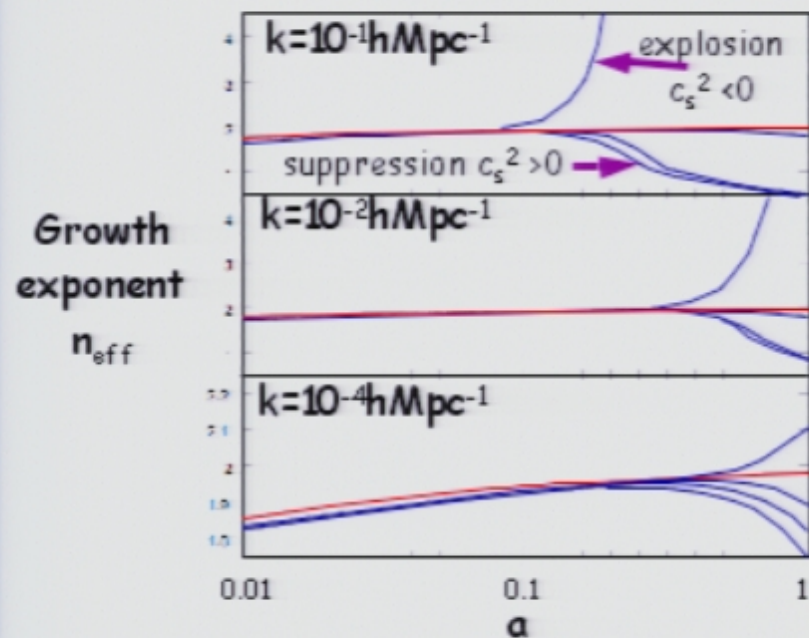
Bean and Dore PRD 68 2003

## Tight bounds on unified dark matter candidates

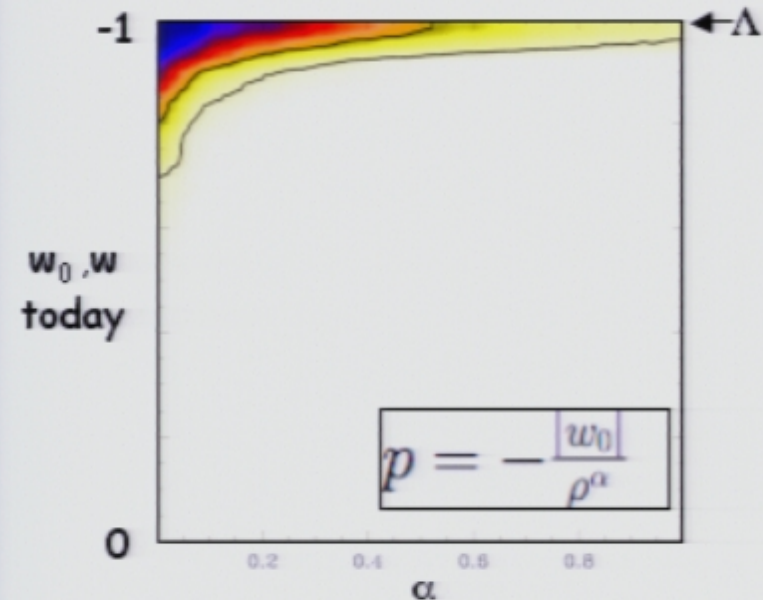


- Evolution of dark energy perturbations highly sensitive to  $c_s^2$  - can lead to chronic suppression or explosion of clustering

Evolution of effective growth rate  $\delta_c(\tau) \propto \tau^{n_{\text{eff}}}$



Allowed parameter space of clustering Dark Energy from CMB+ LSS+SN data



Bean & Dore PRD 68 2003

- Entropy perturbations ensuring  $c_s^2=0$  could stabilise DE perturbations and reinvigorate Chaplygin gases as a unified dark matter approach (Reis et al astro-ph/0306004)





## Modifications to gravity rather than matter

### Quintessential inflation (e.g. Copeland et al 2000)

- Randall Sundrum scenario
- $\rho^2$  term increases the damping of  $\phi$  as rolls down potential at early (inflationary) times
- inflation possible with  $V(\phi)$  usually too steep to produce slow-roll

$$H^2 = \frac{8\pi G_A}{3} \left( \rho + \frac{\rho^2}{2\sigma} \right) + \frac{\Lambda_4}{3} + \frac{\mathcal{E}}{a^4}$$

$$\epsilon \approx 4\epsilon_{FRW} \left( \frac{V}{\sigma} \right)^{-1} \quad \eta \approx 2\eta_{FRW} \left( \frac{V}{\sigma} \right)^{-1}$$

### Curvature on the brane (Dvali, Gabadadze, Porrati 2001)

- Gravity 5D (Minkowski) on large scales  $|>l_c \sim H_0^{-1}$  i.e. only visible at late times
- Although 4D on small scales not Einstein gravity
- Potential implications for solar system tests as well as horizon scales ...

$$H = \sqrt{\frac{8\pi G}{3} \rho + \frac{1}{l_c^2} + \frac{1}{l_c}}$$

### Inhomogeneous metric (Moffat 2005)

- Local kinematics are observer position dependent
- Intrinsic cosmic variance in observables
- Broader implications for perturbation evolution e.g. CMB, LSS

$$ds^2 = dt^2 - R'^2(t, r) f^{-2}(r) dr^2 - R^2(t, r) d\Omega^2$$

$$H_{eff}^2 = \frac{1}{3} (H_{\perp}^2 + 2H_{\perp}H_r) = \frac{8\pi G}{3} \rho$$

## Many outstanding issues

### □ Perturbation evolution in modified gravity theories

- Currently often using spherical collapse prescriptions but would be useful to have general, covariant approach

-How do the CMB and structure power spectra look in these scenarios with a theoretical precision to match measured errors?

-Extend formalism in presence of inhomogeneous metric

### □ Are the modifications from the standard LCDM scenario large enough that they might be detected in upcoming experiments?

### □ What does the non-linear structure formation regime look like in clustering dark energy models/ modified gravity theories?

- Weak lensing occurs in the mildly non-linear regime, if we hope to detect dark energy properties need to understand this!

### □ Unified dark matter/dark energy from a scalar field (imperfect fluid) still a possibility?

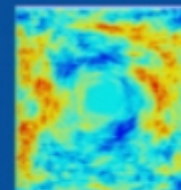
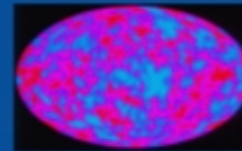


## The key dark energy questions

□ What is the underlying nature of dark energy?

□ What dark energy properties can we measure observationally?

- Overview
- Prospective constraints from the CMB
- Prospective constraints from cluster number counts
- Prospective constraints from weak lensing



## What are the different dark energy constraints?

### □ Late time probes of $w(z)$

- Luminosity distance vs.  $z$
- Angular diameter distance vs.  $z$

SN 1a HST Legacy, Essence,  
DES, SNAP

Alcock-Paczynski test  
Baryon Oscillations SDSS

### □ Probes of $w_{\text{eff}}$

- Angular diameter distance to last scattering  
Bean & Melchiorri PRD 65 (2002)
- Age of the universe

CMB WMAP

CMB/ Globular cluster

Tests probing  
background evolution  
only



## What are the different dark energy constraints?

### □ Late time probes of $w(z)$

- Luminosity distance vs.  $z$
- Angular diameter distance vs.  $z$

Tests probing  
perturbations and  
background

### □ Probes of $w_{\text{eff}}$

- Angular diameter distance to last scattering  
**Bean & Melchiorri PRD 65 (2002)**
- Age of the universe

### □ Late time probes of $w(z)$ and $c_s^2(z)$

- Comoving volume \* no. density vs.  $z$  **Bean and Dore, PRD 68(2003)**
- Shear convergence
- Late time ISW **Bean & Dore PRD 69 (2003)**

Galaxy /cluster surveys, SZ and  
X-rays from ICM  
SDSS, ACT, APEX, DES, SPT

Weak lensing CFHTLS, SNAP, DES, LSST

CMB and cross correlation  
WMAP, PLANCK, with SNAP, LSST, SDSS

## What are the different dark energy constraints?

### □ Late time probes of $w(z)$

- Luminosity distance vs.  $z$
- Angular diameter distance vs.  $z$

### □ Early time probes of $\Omega_Q(z)$

$-N_{\text{eff}}$  Bean, Hansen, Melchiorri (2001)

BBN/ CMB WMAP

### □ Probes of $w_{\text{eff}}$

- Angular diameter distance to last scattering
- Bean & Melchiorri PRD 65 (2002)
- Age of the universe

### □ Late time probes of $w(z)$ and $c_s^2(z)$

- Comoving volume \* no. density vs.  $z$  Bean and Dore, PRD 68 (2003)
- Shear convergence
- Late time ISW Bean & Dore PRD 69 (2003)

Tests probing early  
behavior of dark  
energy



## What are the different dark energy constraints?

- Late time probes of  $w(z)$ 
  - Luminosity distance vs.  $z$
  - Angular diameter distance vs.  $z$
- Probes of  $w_{\text{eff}}$ 
  - Angular diameter distance to last scattering  
Bean & Melchiorri PRD 65 (2002)
  - Age of the universe
- Late time probes of  $w(z)$  and  $c_s^2(z)$ 
  - Comoving volume \* no. density vs.  $z$  Bean and Dore, PRD 68 (2003)
  - Shear convergence
  - Late time ISW Bean & Dore PRD 69 (2003)
- Early time probes of  $\Omega_Q(z)$ 
  - $N_{\text{eff}}$  Bean, Hansen, Melchiorri (2001)
- Alternate probes of non-minimal couplings between dark energy and R/ matter or deviations from Einstein gravity
  - Varying alpha tests Martins et al (2002), Rocha et al (2004)
  - Equivalence principle tests
  - Deviation of solar system orbits

Tests probing wacky  
nature of dark  
energy

## Evolution of $H(z)$ is the primary observable

- In a flat universe, many measures based on the comoving distance

$$r(z) = \int_0^z dz' / H(z')$$

- Luminosity distance

$$d_L(z) = r(z) (1+z)$$

- Angular diameter distance

$$d_A(z) = r(z) / (1+z)$$

- Comoving volume element

$$dV/dz d\Omega(z) = r^2(z) / H(z)$$

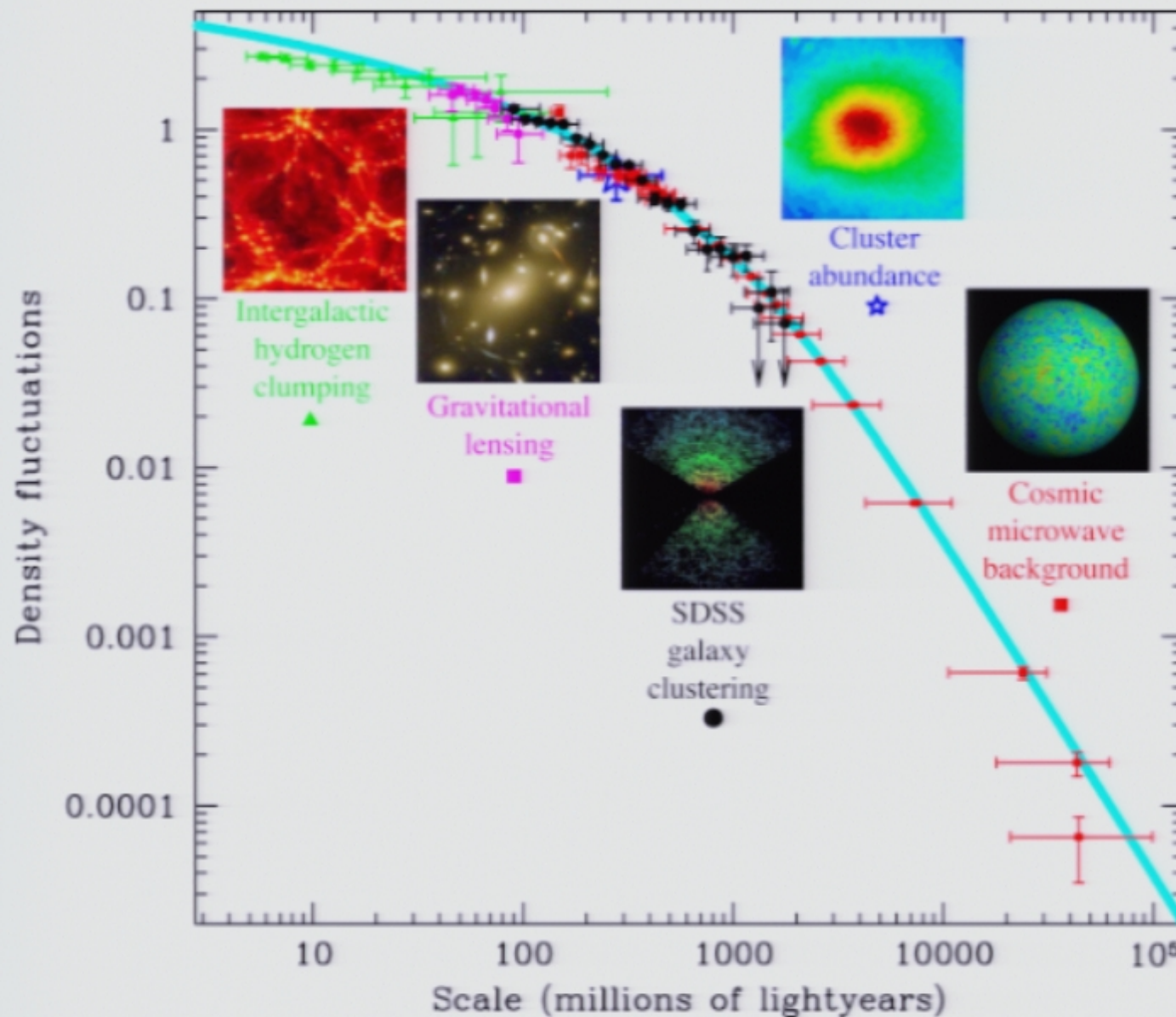
- Age of universe

$$t(z) = \int_z^\infty dz / [(1+z)H(z)]$$

But effect of fluctuations promises to be significant ....

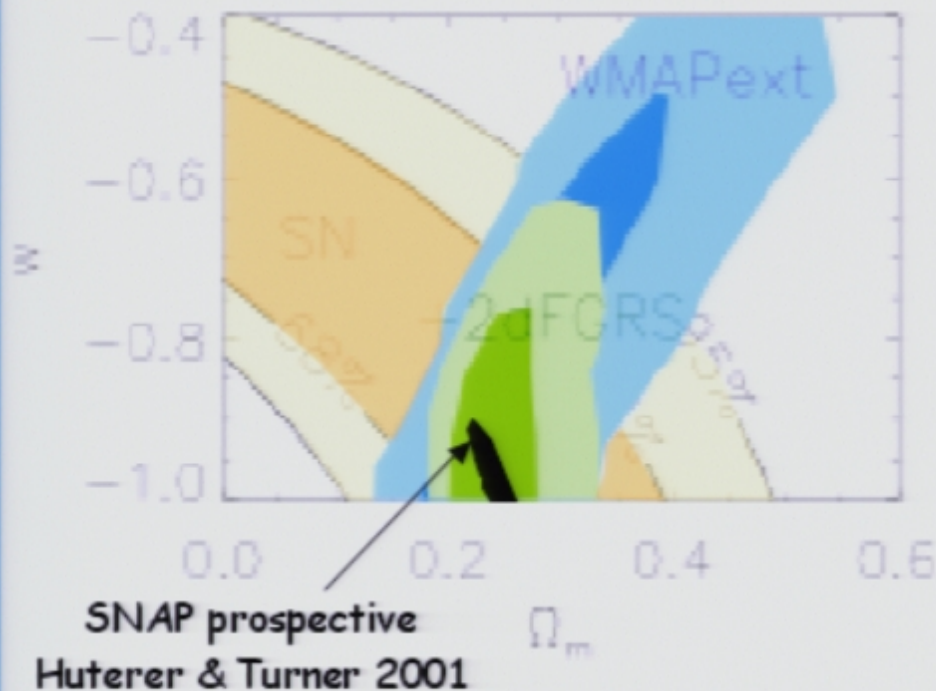


## ... And leveraging evolution on different spatial scales



## But could equally signal deviations from FRW

Combined constraints on equation of state

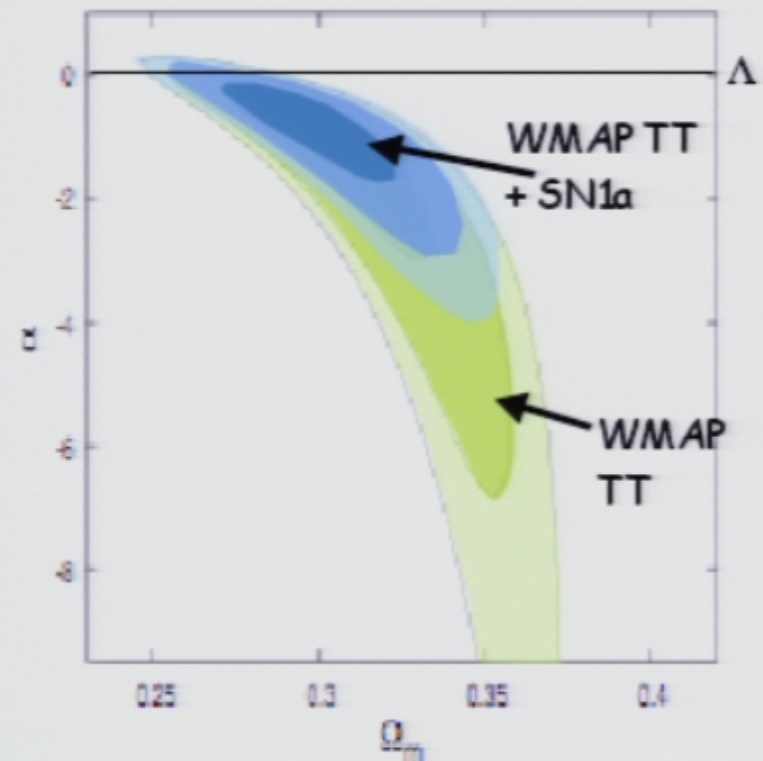


Spiegel et al. 2003

But, implicit priors in this 'consistent' picture:

- Assuming a constant  $w$
- Assuming no dark energy clustering
- Assuming Einstein gravity

Alternative constraints on  $w$  ...



$$\left(\frac{H}{H_0}\right)^2 = \Omega_m(1+z)^3 + (1 - \Omega_m) \left(\frac{H}{H_0}\right)^\alpha$$

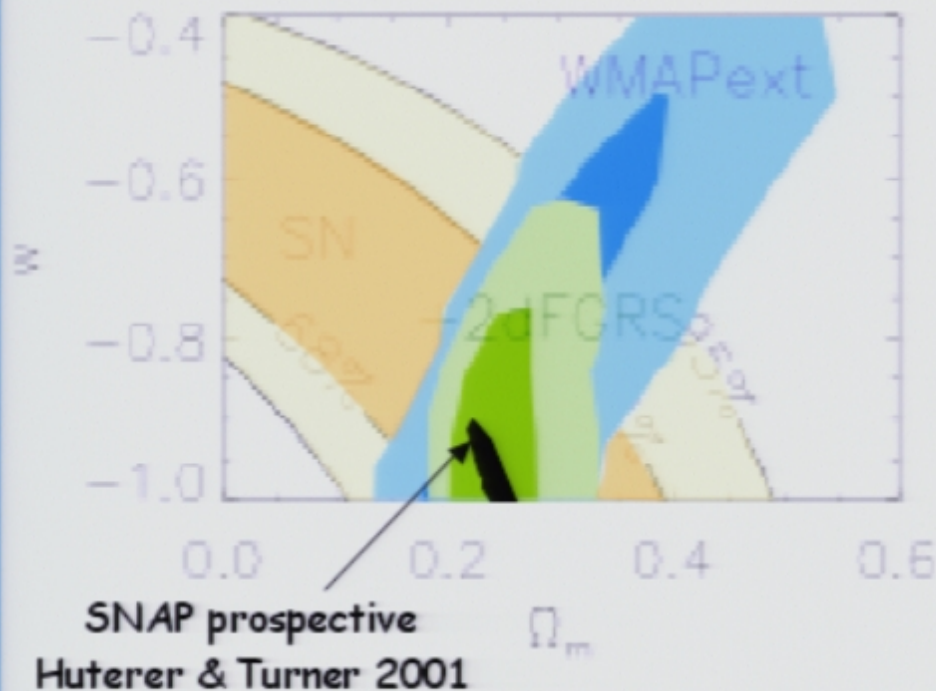
Elgarøy and Multimäki 2004

- How can we test for different properties of dark energy rather than making implicit assumptions?



## But could equally signal deviations from FRW

Combined constraints on equation of state

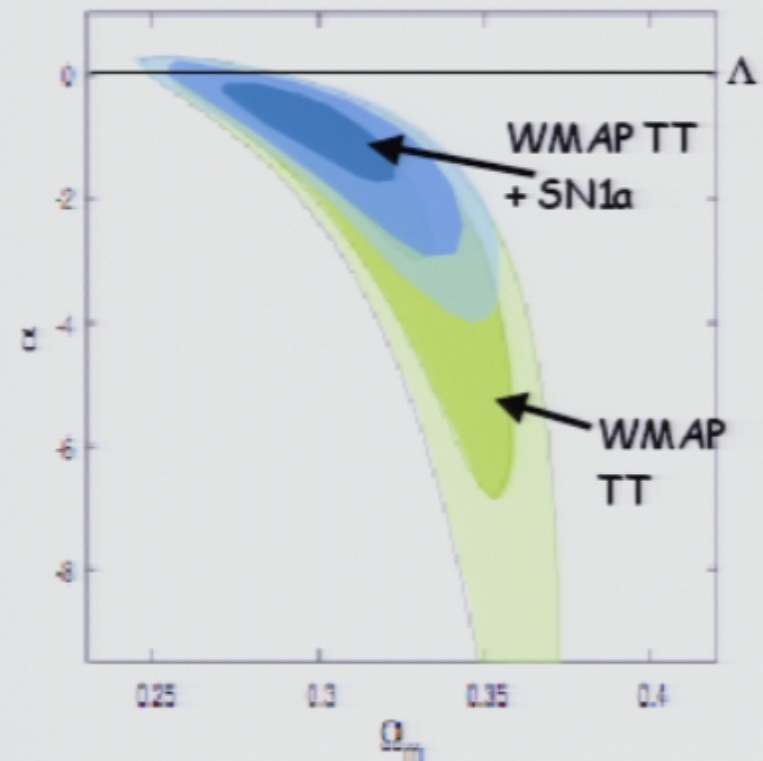


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Elgarøy and Multimäki 2004

- How can we test for different properties of dark energy rather than making implicit assumptions?

## Reconstructing dark energy : a cautionary note

- Ansatz for  $H(z)$ ,  $d_l(z)$  or  $w(z)$
- $w(z)$  applies well to scalar fields as well as many extensions to gravity Linder 2003

$$\Delta = H^2 - \frac{8\pi G}{3} \rho_m$$

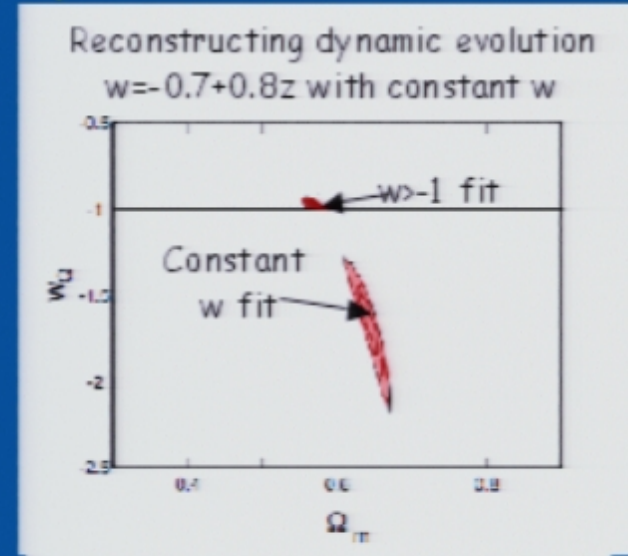
$$w(z) = -1 + \frac{1}{3} \frac{d \ln(\Delta/H_0^2)}{d \ln(1+z)}$$

-Taylor expansions robust for low- $z$

$$w(z) = w_0 + w_a(1 - a)$$

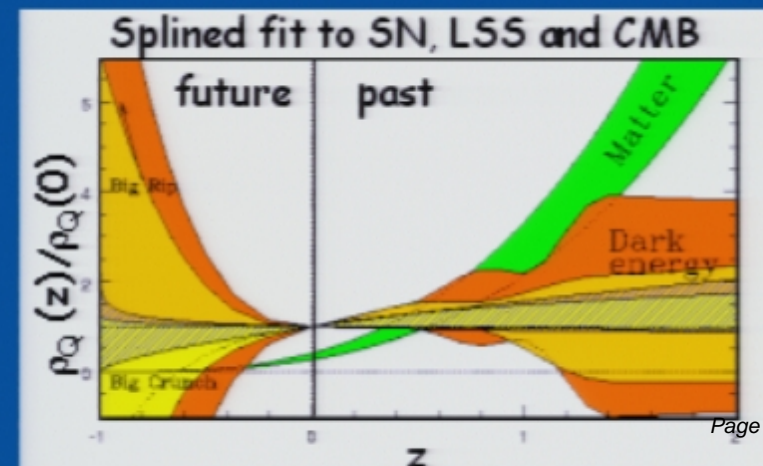
- But remember we are just parameterizing our ignorance, any number of options
  - Statefinder parameters (Sahni et al 2003)
  - expansions in  $H^n$
  - as matter with  $w=p/\rho$ , and  $c_s^2 = \delta p/\delta \rho$ ...

- But, parameterizations can mislead

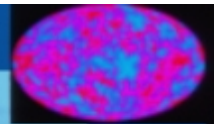


Maor et al 2002

- Can reconstruct making minimal assumptions, but ultimately want to connect to a theory







## Dark energy domination induces signature in CMB photons

- When dark energy dominates it acts to suppress growth in the CDM and gravitational potential wells,  $\Psi$

$$\nabla^2 \Phi = 4\pi G a^2 \rho \delta$$

- late time Integrated Sachs-Wolfe effect (ISW) in CMB photons results

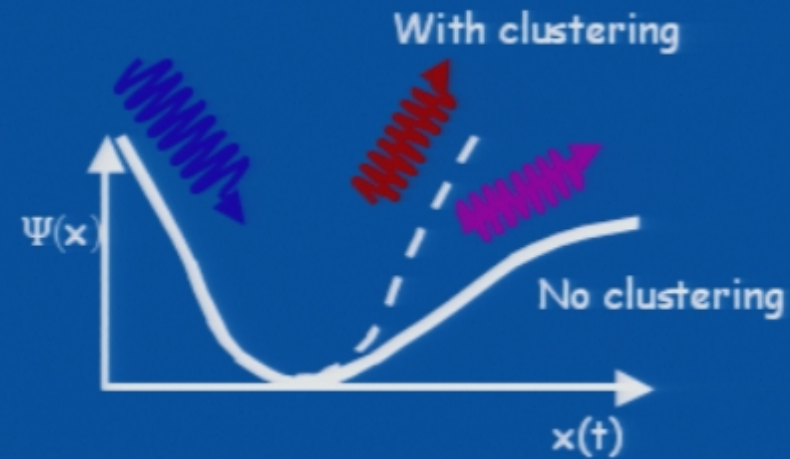
= Net blue shifting of photons as they traverse gravitational potential well of baryonic and dark matter on way.

- ISW important at large scales

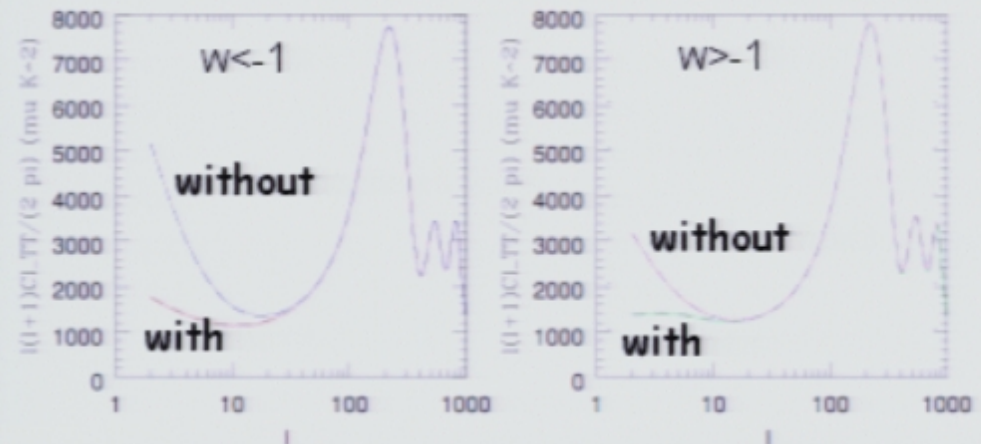
- Cancellation of effects on small scales
- At scales of key importance for DE perturbations

- Dark energy clustering counters suppression due to accelerative expansion

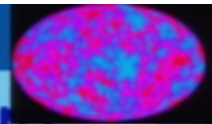
- Decreases ISW signature



CMB spectra for DE models incl/excl perturbations



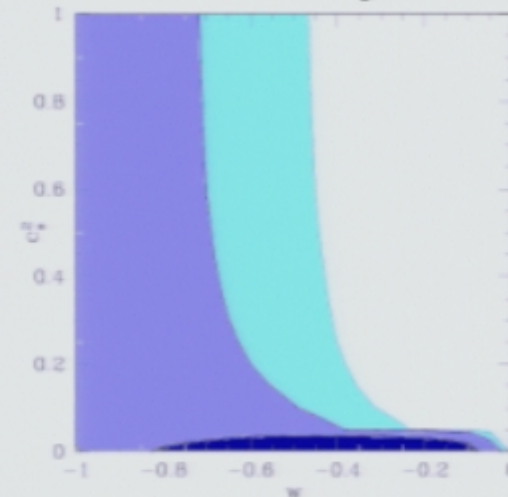
Bean & Dore PRD 69 2003



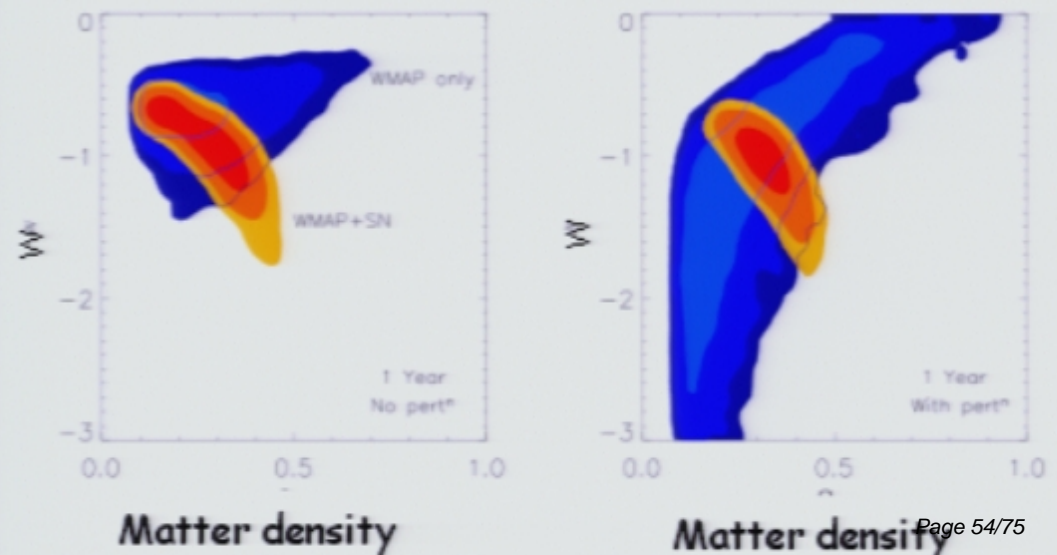
## Dark energy perturbations can affect CMB and LSS predictions

- **Degeneracies & cosmic variance prevent constraints on clustering itself**
  - Large scale anisotropies also altered by spectral tilt, running in the tilt and tensor modes
- **Dark energy clustering will be factor in combining future high precision CMB with supernova data.**
- **Avoid degeneracies by cross correlating ISW with other observables ...**
  - galaxy number counts
  - Radio source counts
  - Weak lensing of galaxies or CMB ...

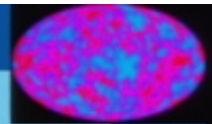
'Constraints' on  $w$  and  $c_s^2$  from WMAP



Constraints on  $w$  from CMB+ SN1a incl/excl perturbations





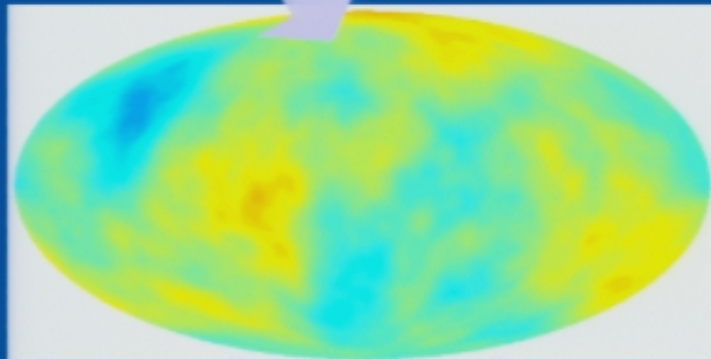


## Dark energy prospects : CMB cross correlation

- ISW intimately related to matter distribution

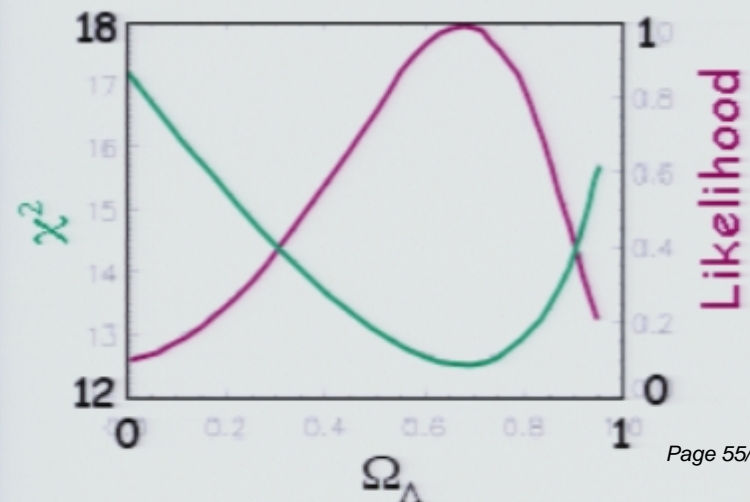
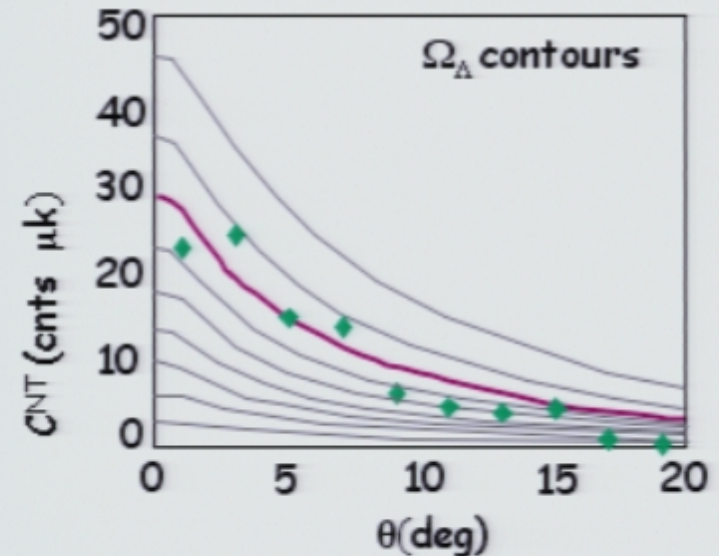


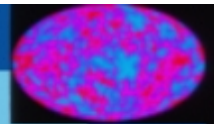
colless/2dF 2003



- Should see cross-correlation of CMB ISW with LSS. e.g. NVSS radio source survey (Boughn & Crittenden 2003 Nolta et al 2003, Scranton et al 2003)

Cross correlation of radio source number counts and WMAP ISW





## Cross correlation of CMB with large scale structure

- Although current observations cannot distinguish dark energy features (Bean and Dore PRD 69 2003), future large scale surveys which are deep,  $z \sim 2$ , and use weak lensing can avoid bias uncertainties such as LSST might well be able to

$$C_{NT}(\theta) = \frac{1}{4\pi} \sum_{l=2}^{\infty} (2l+1) C_l^{NT} P_l(\cos\theta)$$

$$\propto \delta_c(c_s^2, w, z=0)$$

Dark energy clustering  $w, c_s^2$  dependence

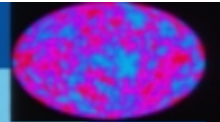
$$C_l^{NT} = 4\pi \int_0^\infty \frac{dk}{k} \Delta^2(k) f_l^N(k) f_l^T(k)$$

Purely background ( $w$ ) dependent

$$b_r \int_0^z \frac{d\tilde{N}}{dz} D(z) j_l(k\eta) dz$$

$$\frac{3H_0^2 \Omega_m^0}{c^2 k^2} \int_0^z \frac{d[D(z)(1+z)]}{dz} j_l(k\eta) dz$$





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$$C_l^{NT} = 4\pi \int_0^\infty \frac{dk}{k} \Delta^2(k) f_l^N(k) f_l^T(k)$$

Purely background ( $w$ ) dependent

$$b_r \int_0^z \frac{d\tilde{N}}{dz} D(z) j_l(k\eta) dz$$

$$\frac{3H_0^2 \Omega_m^0}{c^2 k^2} \int_0^z \frac{d[D(z)(1+z)]}{dz} j_l(k\eta) dz$$

# Dark energy prospects : Galaxy / cluster number counts

- Volume element has better sensitivity to  $w$  and  $w'$  than luminosity distance

$$dV/dz d\Omega(z) = r^2(z) / H(z)$$

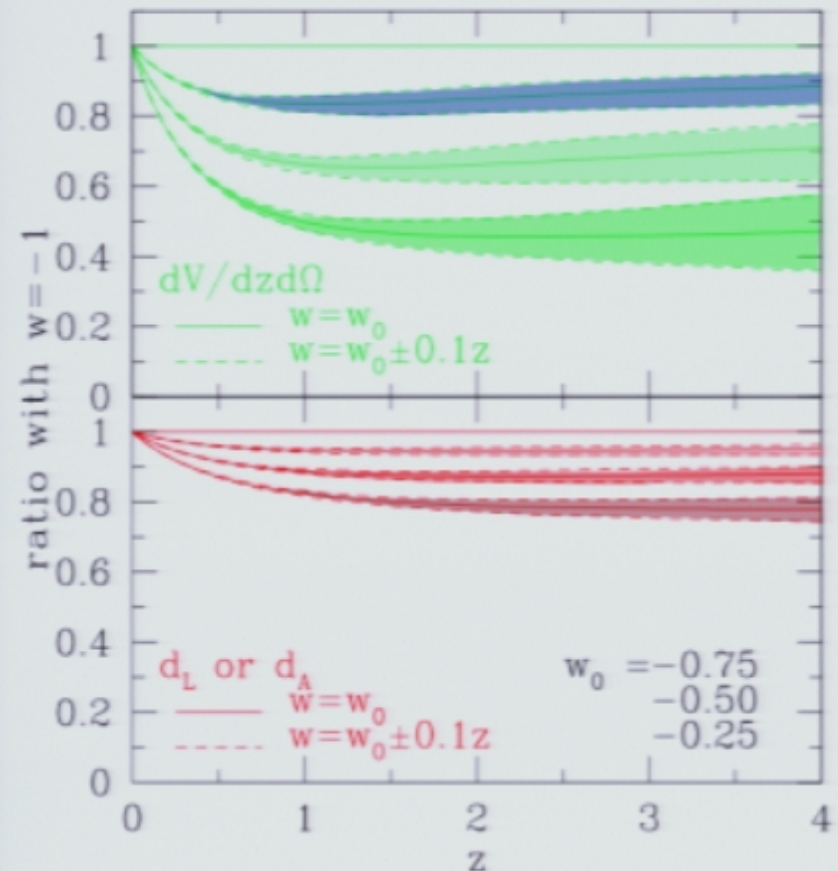
- Number counts related to underlying matter distribution and  $\delta_c(z)$ 
  - inherent modeling sensitivity

$$\frac{dN}{dz d\Omega} = \frac{dV}{dz d\Omega} \int_{m_{lim}(z)}^{\infty} dM \frac{dn(M, z)}{dM}$$

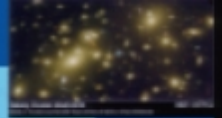
e.g. cluster mass function Jenkins et. al 2000

$$\frac{dn(M, z)}{dM} \propto \exp \left\{ - \left| 0.61 - \log \left( \frac{\delta_c(z) \sigma_M}{\delta_c(0)} \right) \right|^{3.8} \right\}$$

Comparison against  $w=-1$  for same  $h, \Omega_b h^2$





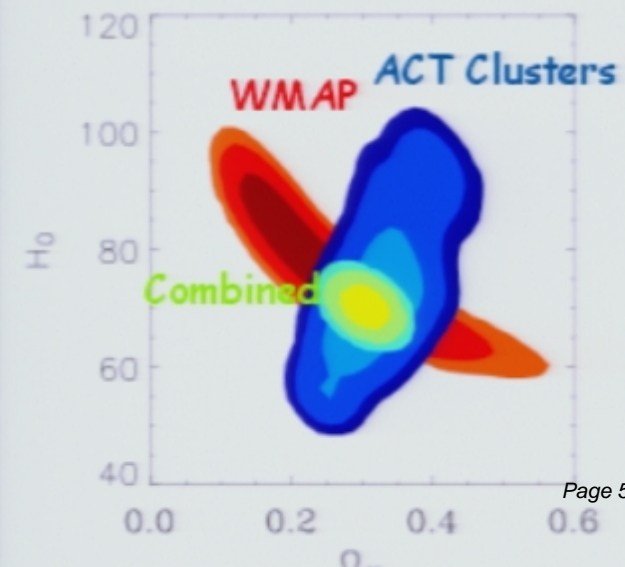
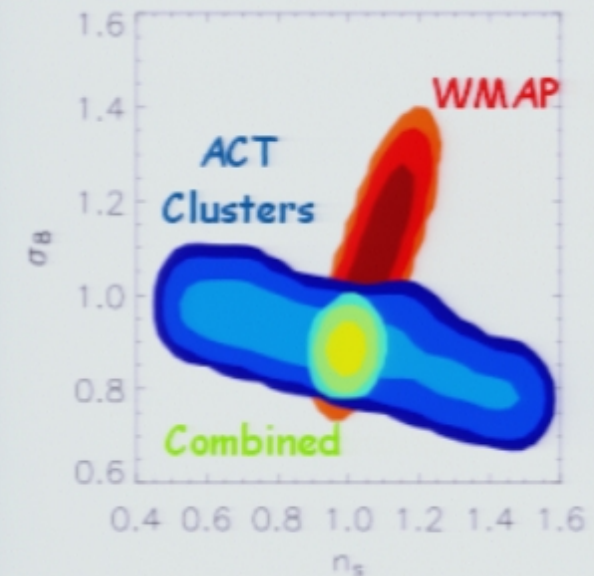


## Dark energy prospects : cluster number counts from SZ

### Advantages:

- Degeneracy directions complementary to CMB, SN1a
- Clusters exponentially sensitive to growth factor
  - e.g. sensitive to suppressions due to dark energy or neutrinos
- Multiple mass estimates
  - Velocity dispersion of cluster galaxies
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Parameter degeneracies for CMB and clusters



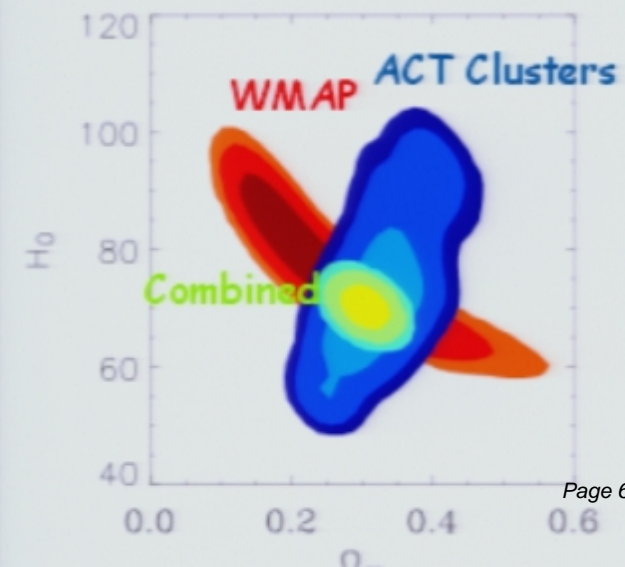
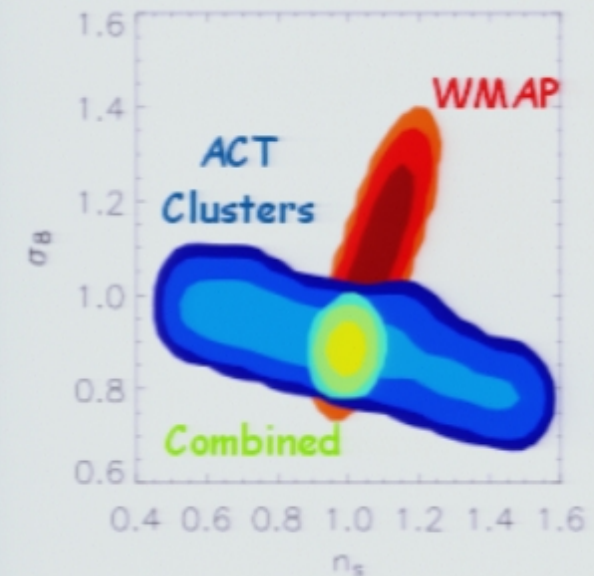


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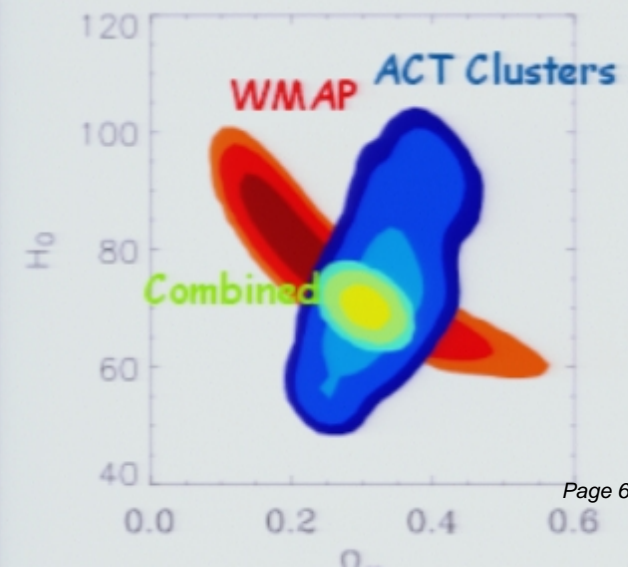
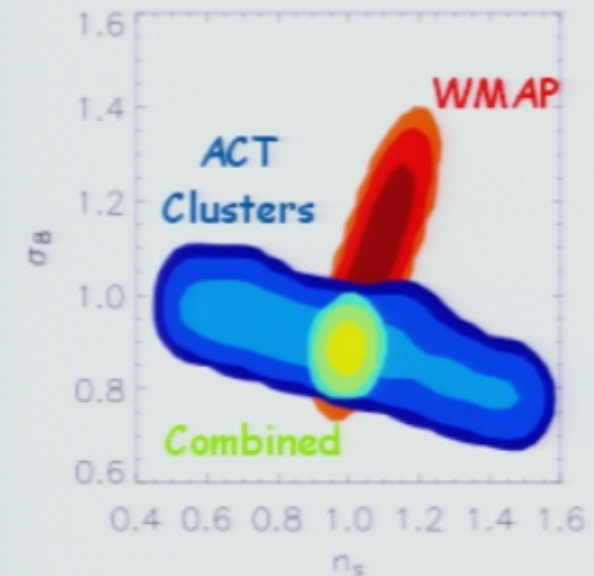


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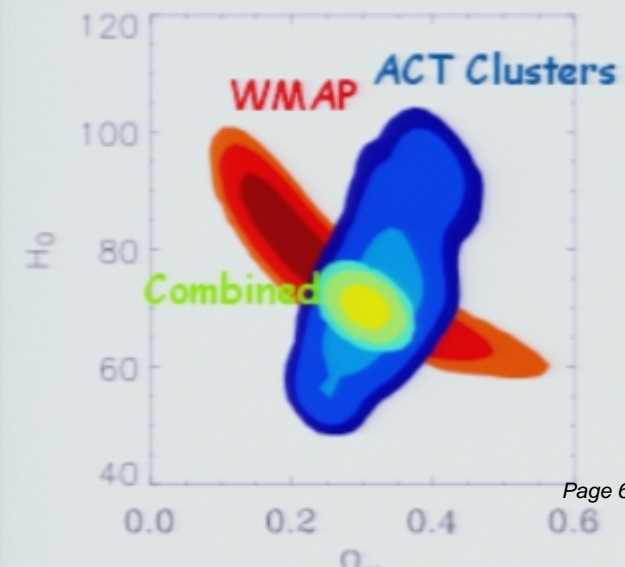
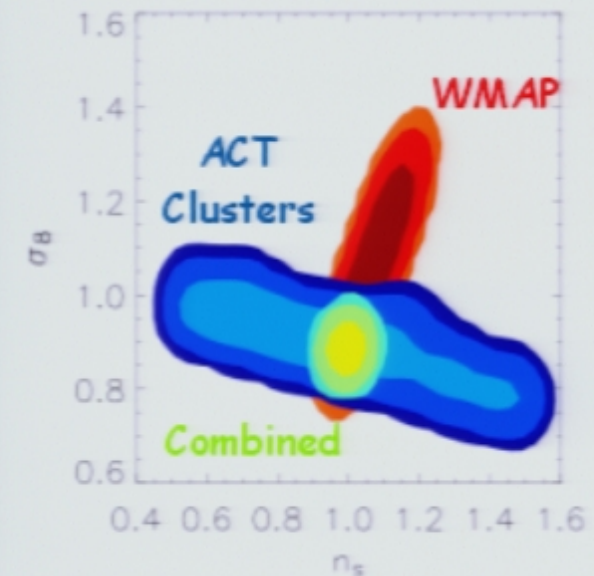


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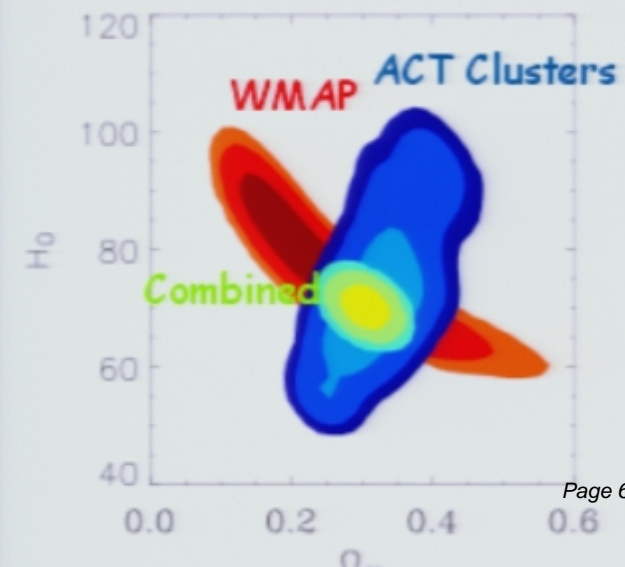
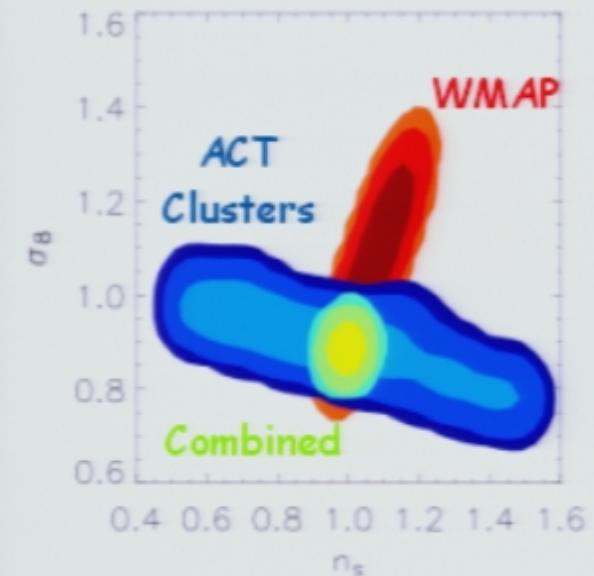


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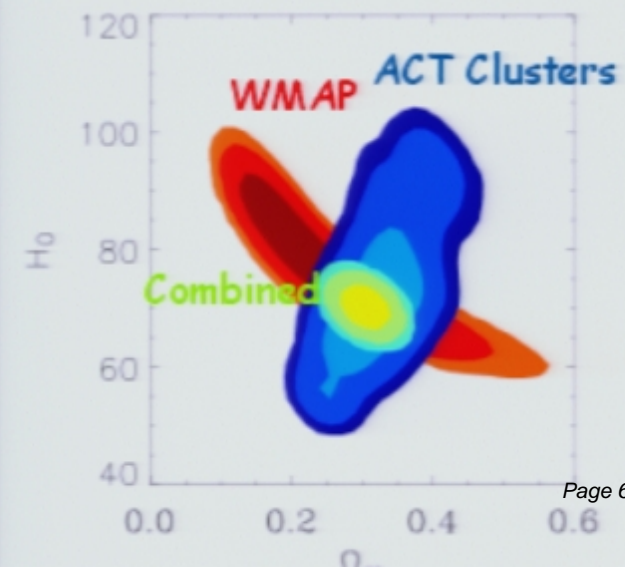
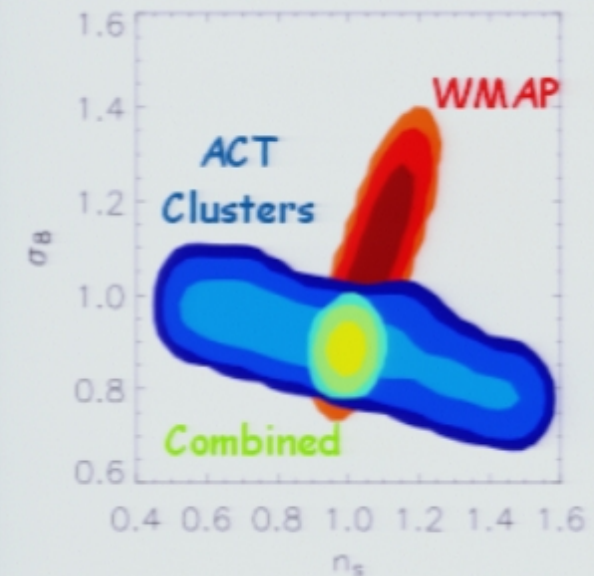


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## Dark Energy Prospects : Cluster counts from SZ

The passage of the CMB through a hot  $e^-$  cloud distorts the spectrum of the  $\gamma_{\text{CMB}}$  due to Compton interactions

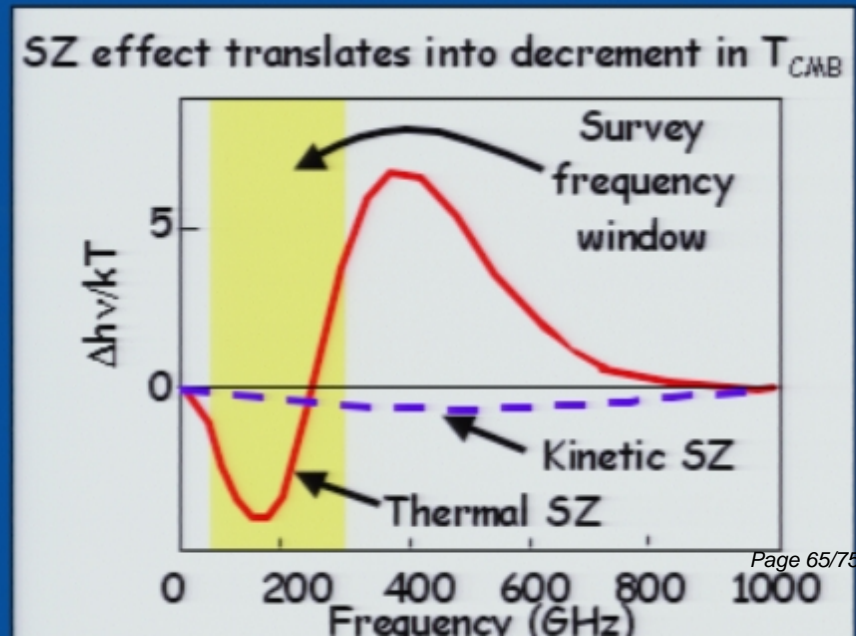
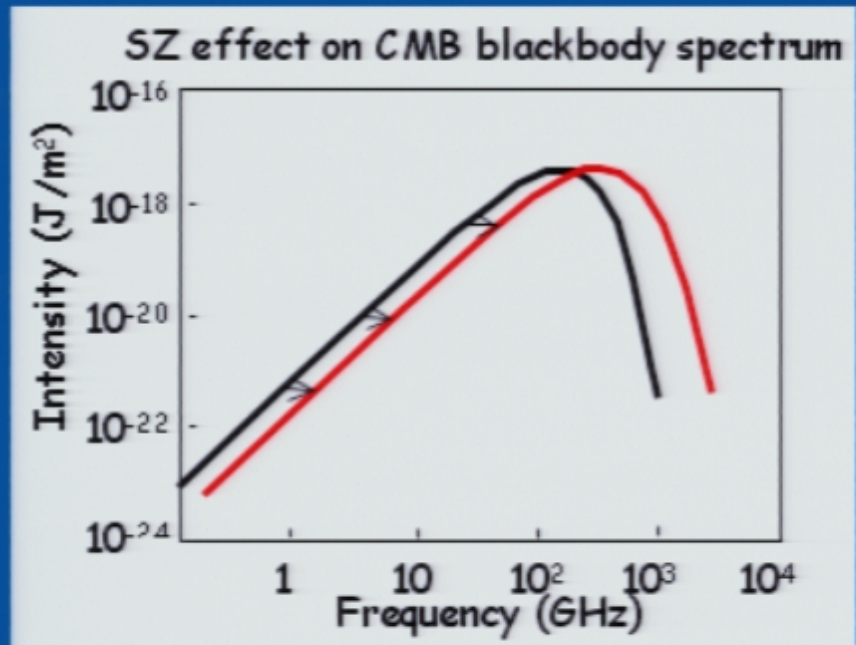
Due to the high energy of the  $e^-$ 's, and the homogeneity and isotropy of the CMB, the  $\gamma$  gain energy.

- Rayleigh-Jeans regime (at low  $\nu$ ) the change can also be produced with a lower temperature of the radiation.

- In the Wien part of the spectrum (at high  $\nu$ ) one can interpret the change with a higher radiation temperature.

If one measures  $T_{\text{CMB}}$  towards a region containing hot  $e^-$  one expects a decrement at low  $\nu$  and an increment at high  $\nu$  compared to the normal brightness temperature (2.73 Kelvin).

SZ signal not attenuated with  $z$





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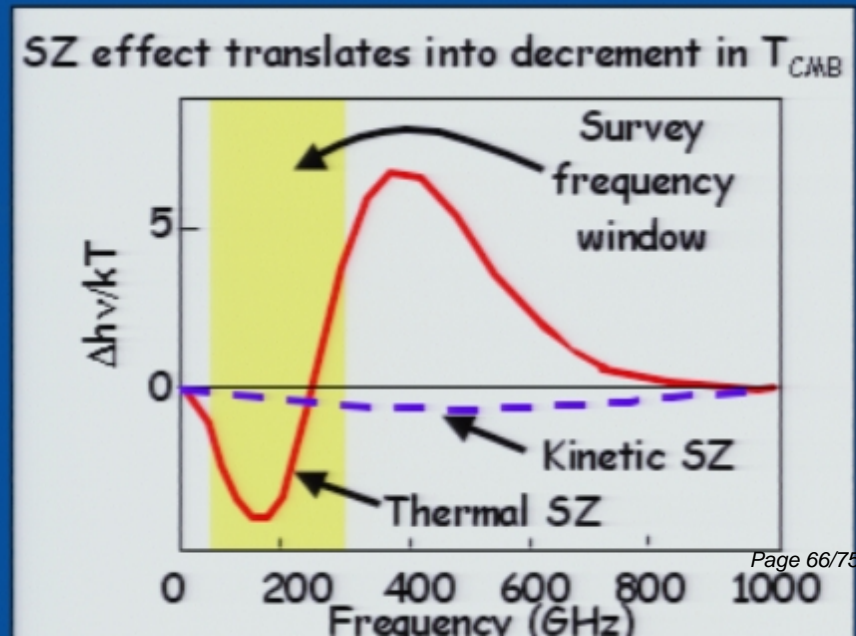
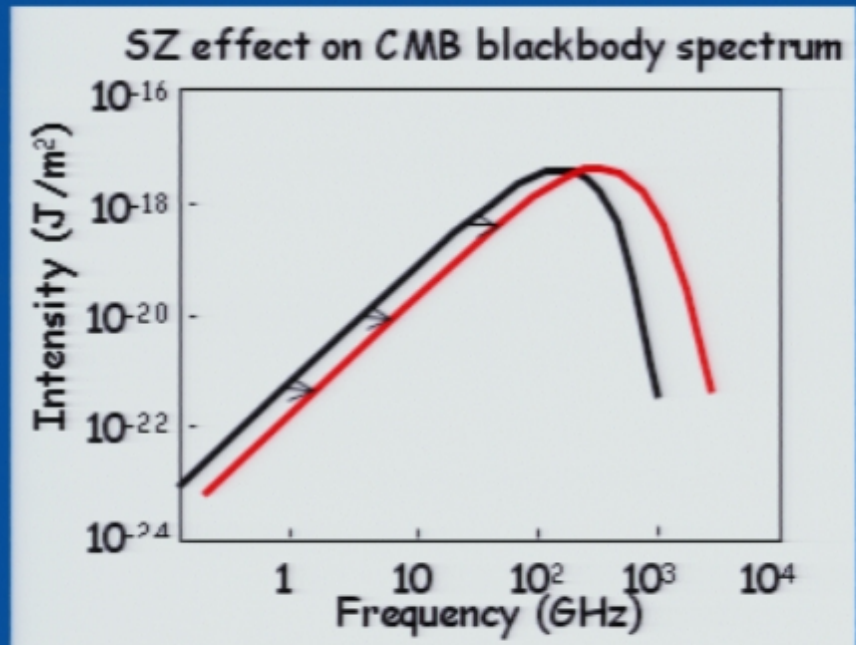
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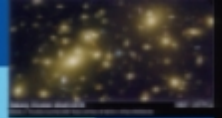
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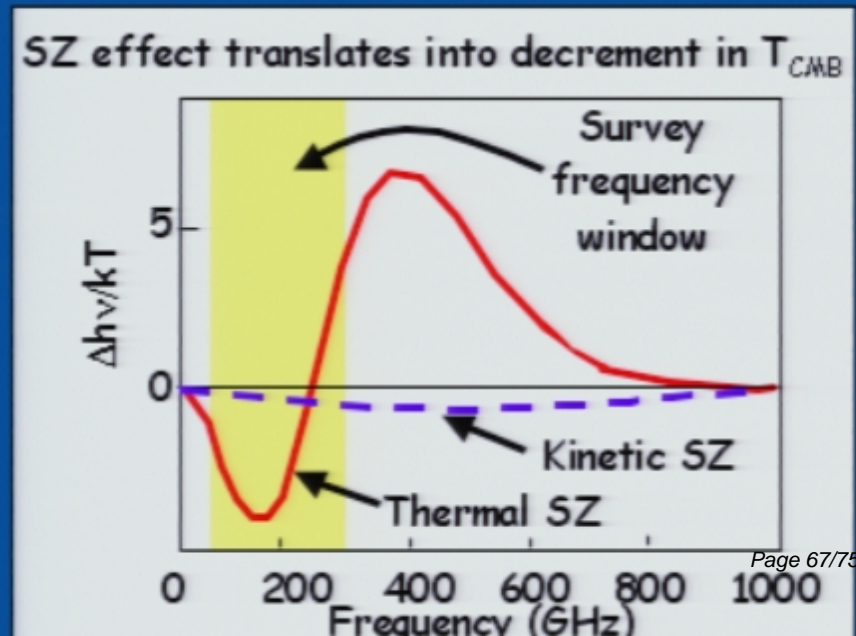
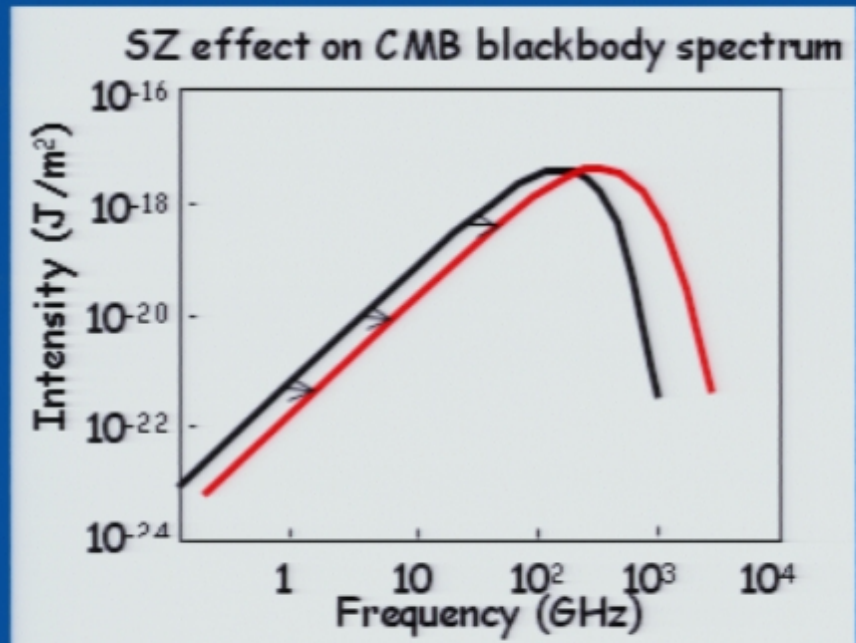
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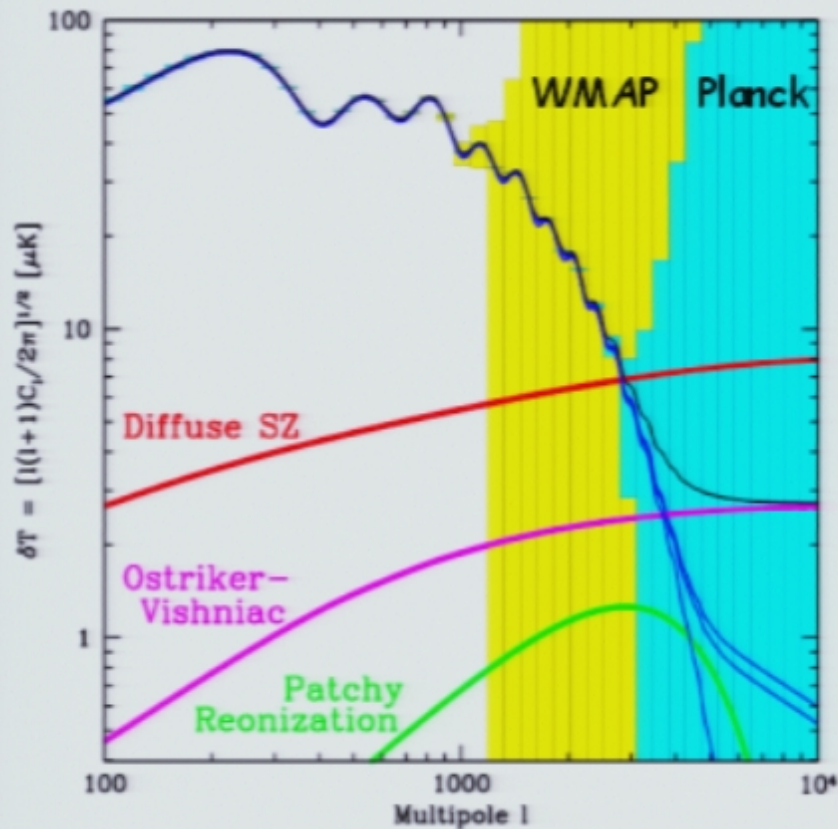
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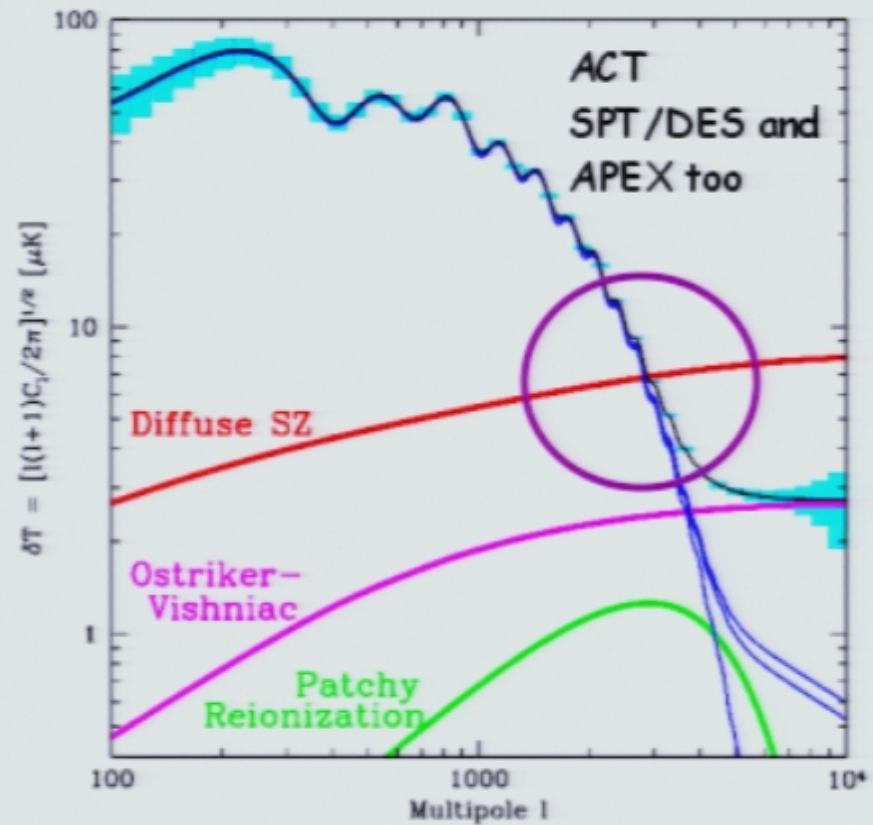


# SZ surveys set up to probe entirely new regime of CMB

CMB power spectrum for WMAP and Planck



CMB power spectrum for ACT



de Oliveira-Costa

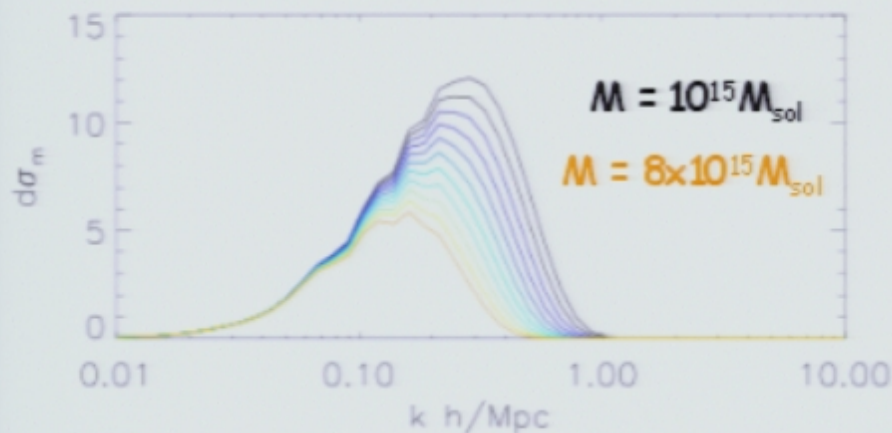


# Cluster number counts from SZ : ACT

- Investigating dark energy and neutrino constraints for ACT using redshift and mass slicing to increase information extracted

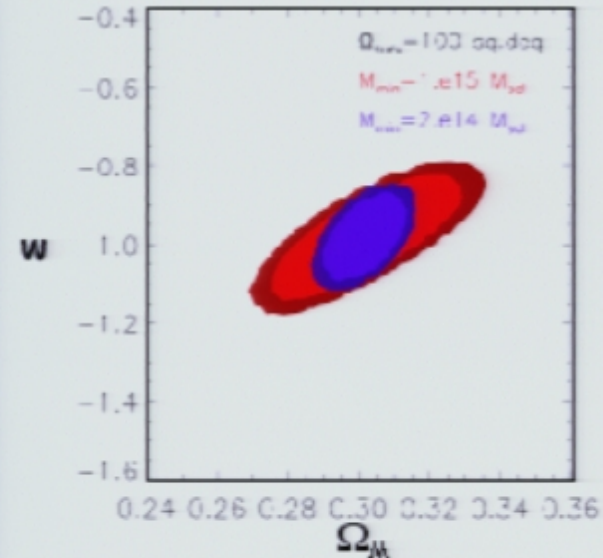
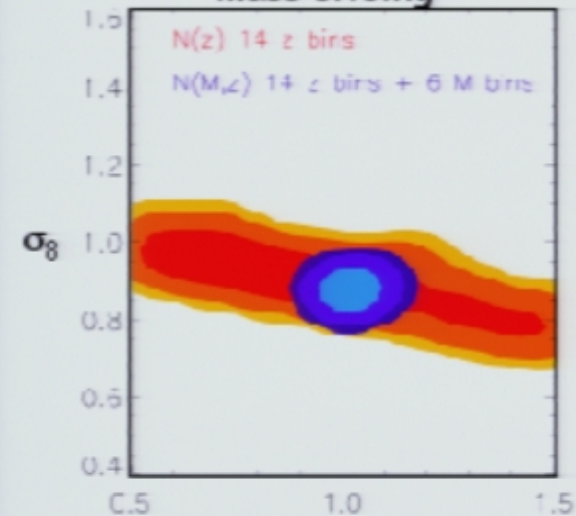
- mass weight functions for  $dN/dz$  peak at larger scales for more massive clusters, so able to separate out evolution at scales  $k \sim 0.1-1 h/\text{Mpc}$

Mass weight function spatial dependency



-Using  $z$  and mass slices breaks key degeneracies in SZ measurements

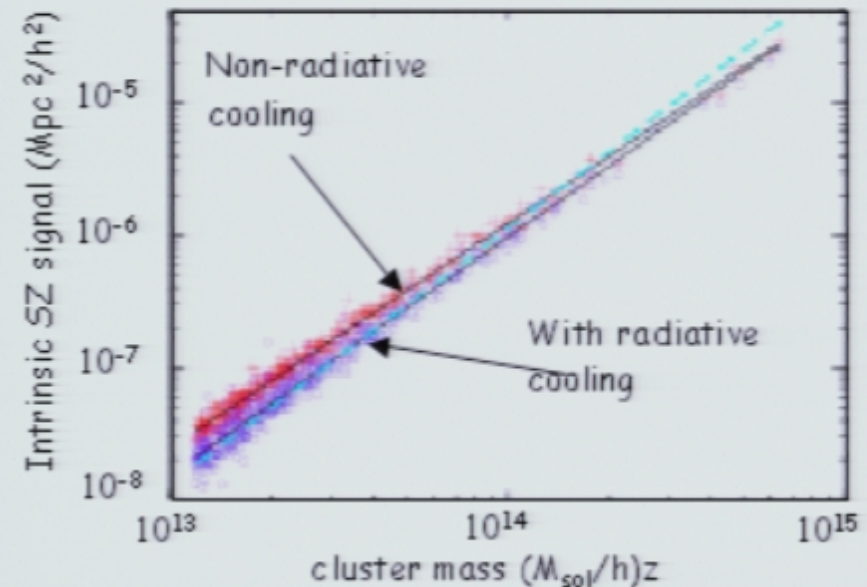
Cluster contour with and without mass slicing



## Cluster number counts from SZ : systematic uncertainties

- Uncertainty in mass-scaling relations from theoretical cluster physics modeling is an important systematic
- How do radiative cooling effects and pre-heating within the cluster affect mass - SZ/ Xray luminosities scaling relations?
- How does cluster evolution affect redshift evolution in mass-scaling relationship for SZ, X-ray?
- How can we combine/ parameterize these theoretical modelling uncertainties in the cosmological parameter estimation codes for future SZ surveys?

Cluster mass- SZ scaling relation dependency on cluster model



daSilva et al 2003





## Small scale CMB : Many SZ surveys planned

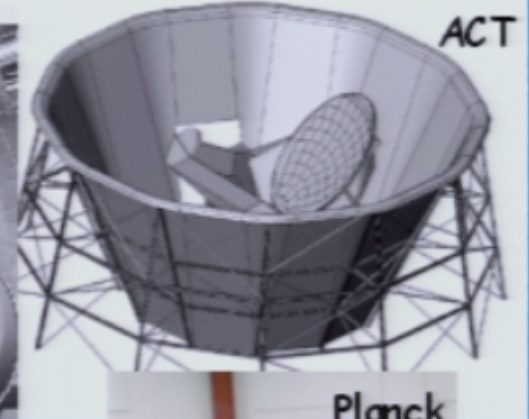
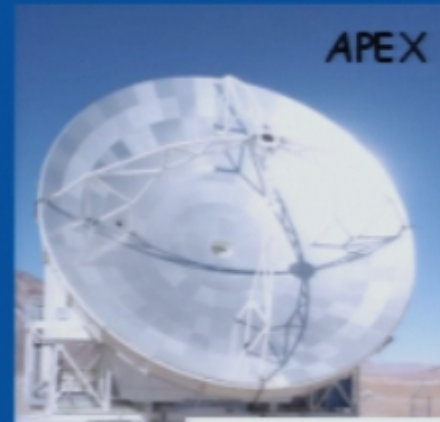
### Ground based e.g.:

- SZA ~100 clusters, 12 sqdeg,  $z \sim 1$ , 2004
- APEX ~1000, 200sqdeg, 2005
- ACT ~1000 clusters, 100 sqdeg,  $z \sim 1.4$ , early 2006, photometric support from SALT
- SPT ~10,000 clusters, 40,000 sqdeg,  $z \sim 1.2$ , 2007, photometric support from DES

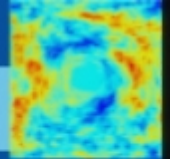
### Satellite :

- Planck, ~15,000 clusters,  $z \sim 1$ , 2007

- And many others ... AmI, SuZIE, Polarbear I, QUIET, CLOVER, ALMA, BiCEP ...







## Dark Energy Prospects : Weak lensing

CHFLT, SNAP and LSST offer promising prospects for WL

- many millions of galaxies over hundreds of square degrees
- Using all the mass information not just luminous matter

Tomography => bias independent  $z$  evolution of DE  
Jain and Taylor 03, Zhang, Hui, Stebbins 03

- Ratios of growth factor (perturbation) dependent observables at different  $z$  give growth factor (perturbation) independent measurement of  $w, w'$
- e.g. tangential shear - galaxy cross correlation

Would like to see if technique could probe dark energy clustering in the SNAP wide survey or with LSST?

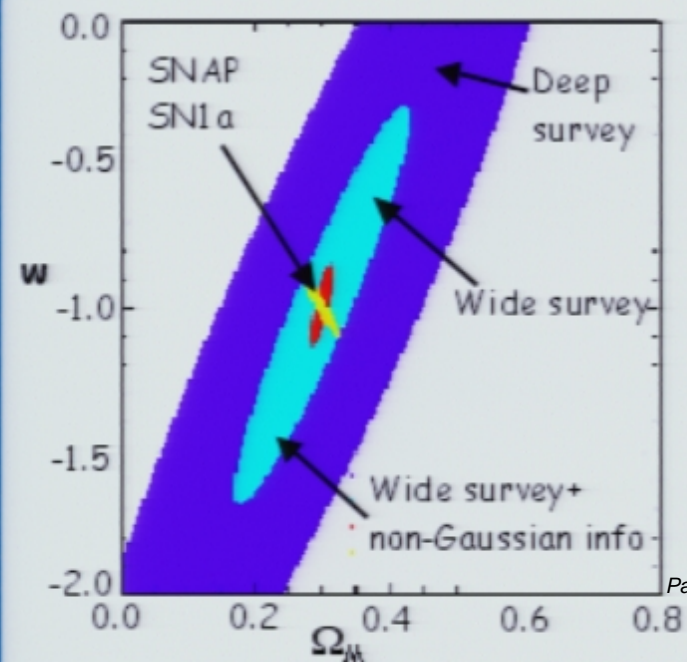
- What kind of survey strategy would be best to test this?

- What kind of statistical estimators would best

□ Understanding theoretical and observational systematics key

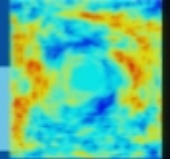
- effect of non-linearities in power spectrum
- Accurately reconstructing anisotropic point spread function
- $z$ -distribution of background sources and foreground halo
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Prospective constraints on  $w$  from the SNAP SN1a + WL measurements





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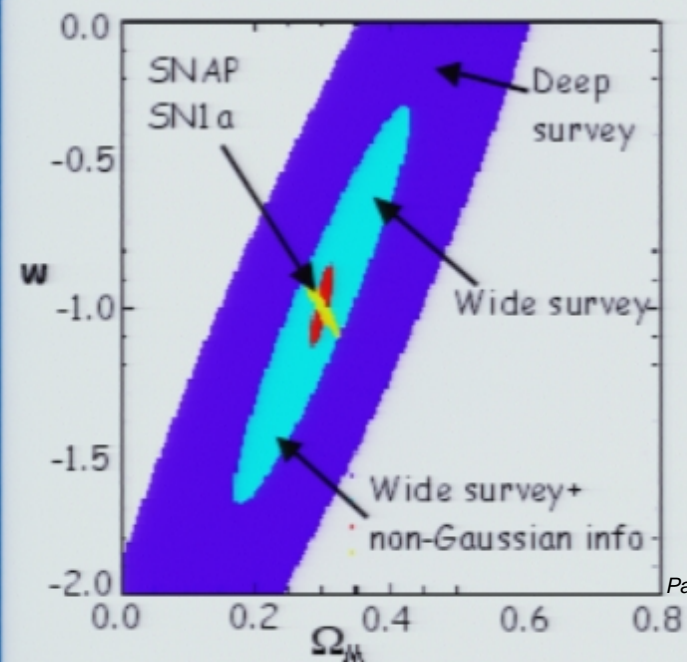
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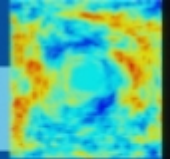
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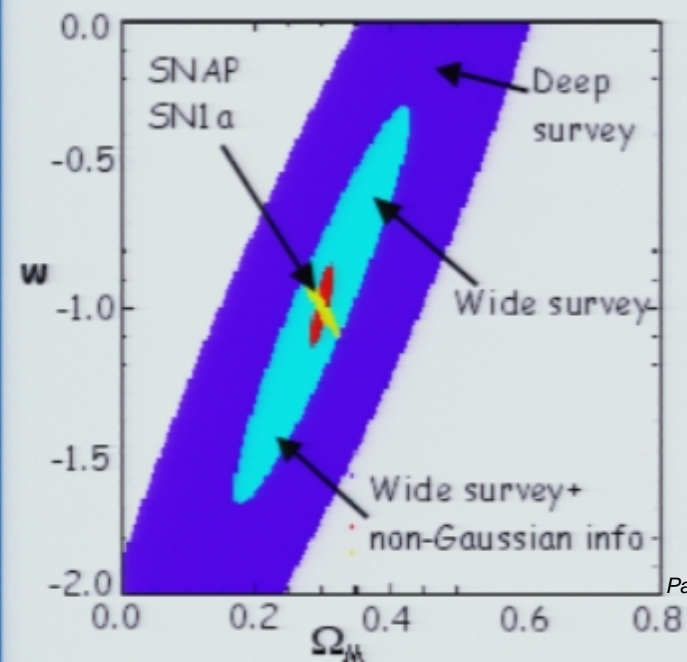
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## To conclude

- **A wealth of theoretical activity**

- investigating dark energy explanations as a cosmological constant, an adjustment to gravity or a strange matter component.

- **Theories are making testable predictions**

- from horizon scales (dark matter perturbations) down to solar system scales (modified gravity)

- **Observations are promising unprecedented precision in the next 5-10 years**

- with a lever arm tying down both large (ISW) and small scale (SZ, weak lensing) anisotropies

- **We have a very exciting decade ahead of us both theoretically and experimentally!**

