

Title: Building chiral flux vacua

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Abstract:

Building Chiral Flux Vacua

Fernando Marchesano

University of Wisconsin-Madison

String Theory Seminars
Perimeter Institute, March 8, 2004

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Outline

● Motivation

- Why Fluxes?
- Why D-branes?

● Model Building

- Magnetized D-branes
- $\mathcal{N} = 1$ and $\mathcal{N} = 0$ models

● MSSM-like vacua

- Higgsing as D-brane recombination
- μ -term and Yukawas

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$D = 4$ Compactifications:

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 - Moduli stabilization
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 - Moduli stabilization
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- Generalizations to compactifications with background fluxes may help solving both since
 - Most moduli get lifted by an effective potential
 - SUSY can be broken in a controlled way

Fluxes in Type IIB

- Type IIB flux compactifications provide an interesting framework for realizing these ideas. Introducing a non-trivial 3-form flux

$$G_3 = F_3 - \tau H_3 \quad \left\{ \begin{array}{ll} F_3 & \text{RR flux} \\ H_3 & \text{NSNS flux} \\ \tau & \text{complex dilaton} \end{array} \right.$$

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→ Generates a superpotential W which freezes the complex structure moduli and dilaton

[Gukov, Vafa, Witten]

[Dasgupta, Rajesh, Sethi]

→ Induces soft terms in gauge theories living on D-branes

[Cámara, Ibáñez, Uranga]

[Graña, Grimm, Jockers, Louis]

[Lüst, Reffert, Stieberger]

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→ Generates a superpotential W which freezes the complex structure moduli and dilaton [GVW,DRS]

→ Induces soft terms in gauge theories living on D-branes [CIU,GGJL,LRS]

- In addition, this class of supergravity backgrounds
 - Embed the Randall-Sundrum scenario by means of a warped metric [Giddings, Kachru, Polchinski]
 - Admit the construction of de Sitter vacua [Kachru, Kallosh, Linde, Trivedi]

D-branes & chirality

- Type IIB flux compactifications naturally involve **D-branes**, which yield $U(N)$ gauge theories at low energies.
- In order to get a realistic vacuum, however, we need these gauge theories to be **chiral**.

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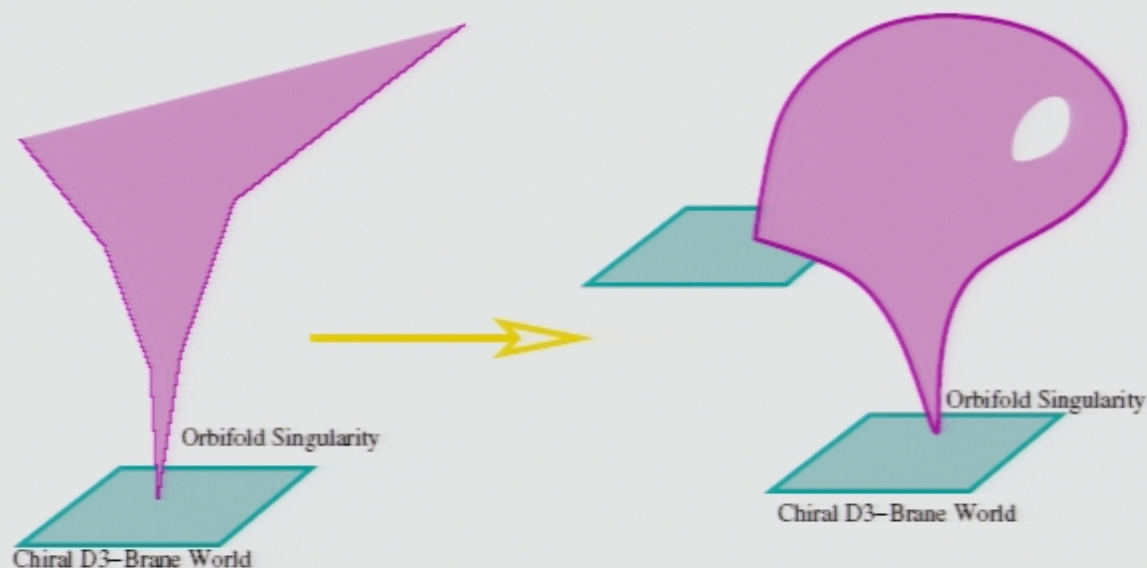
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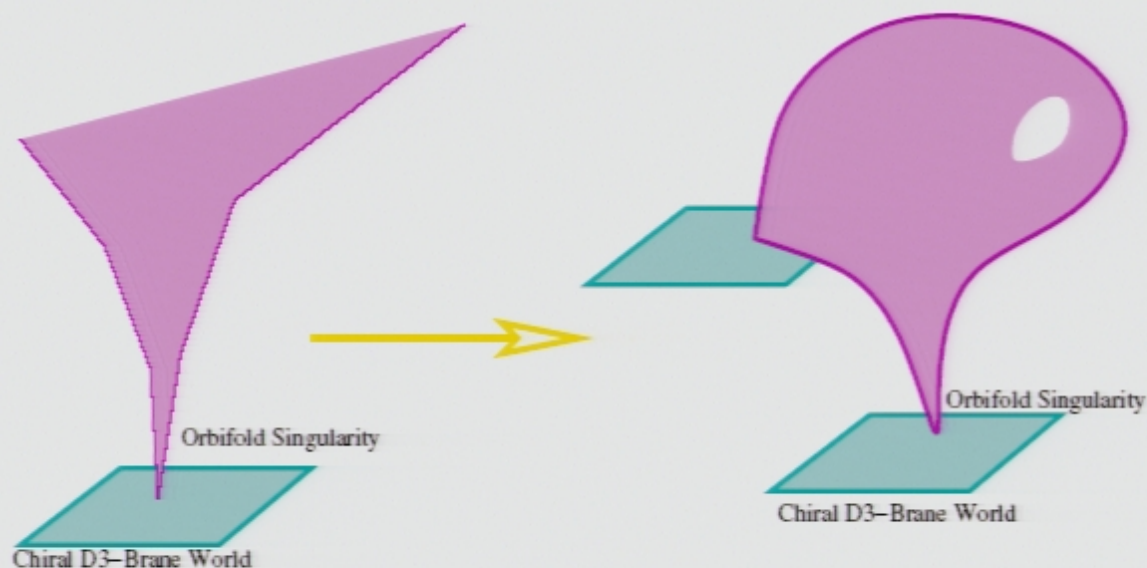
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- Two known ways to achieve **chirality** in type IIB flux compactification
 - **D-branes at singularities** [Cascales, García del Moral, Quevedo, Uranga]



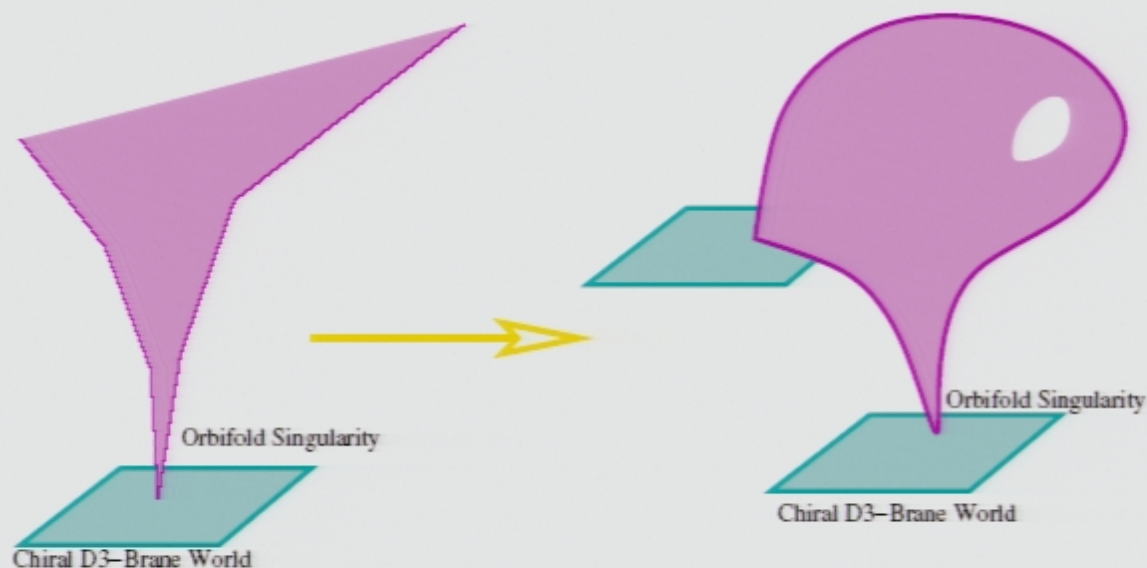
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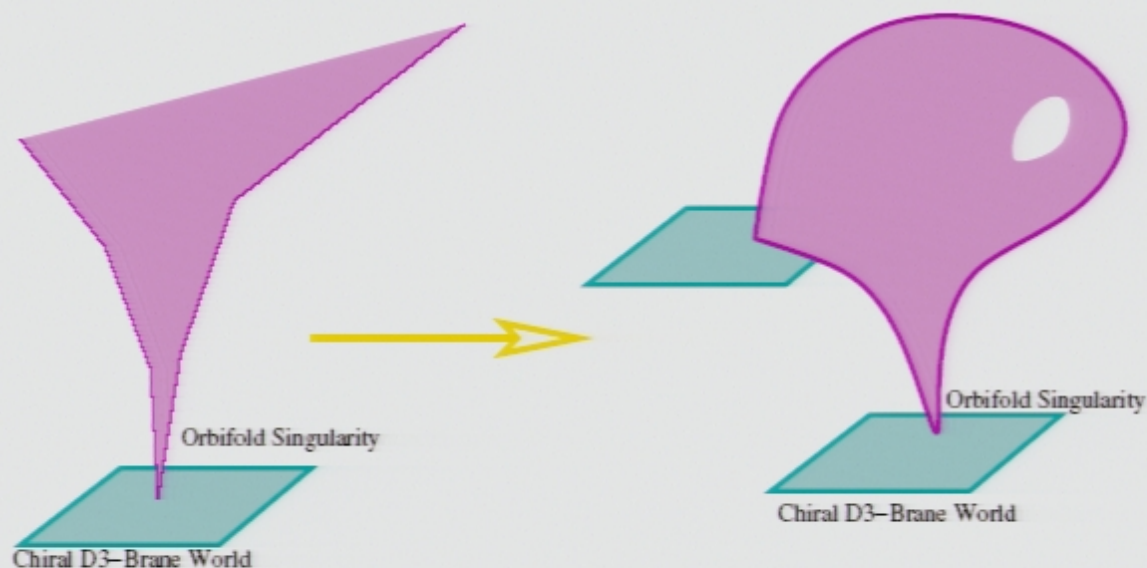
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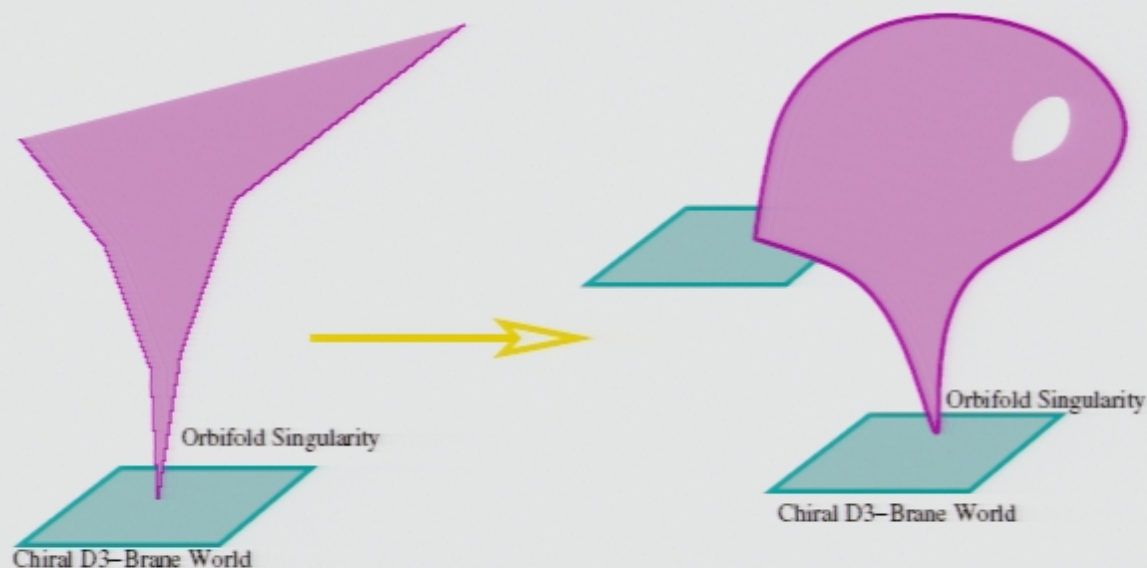
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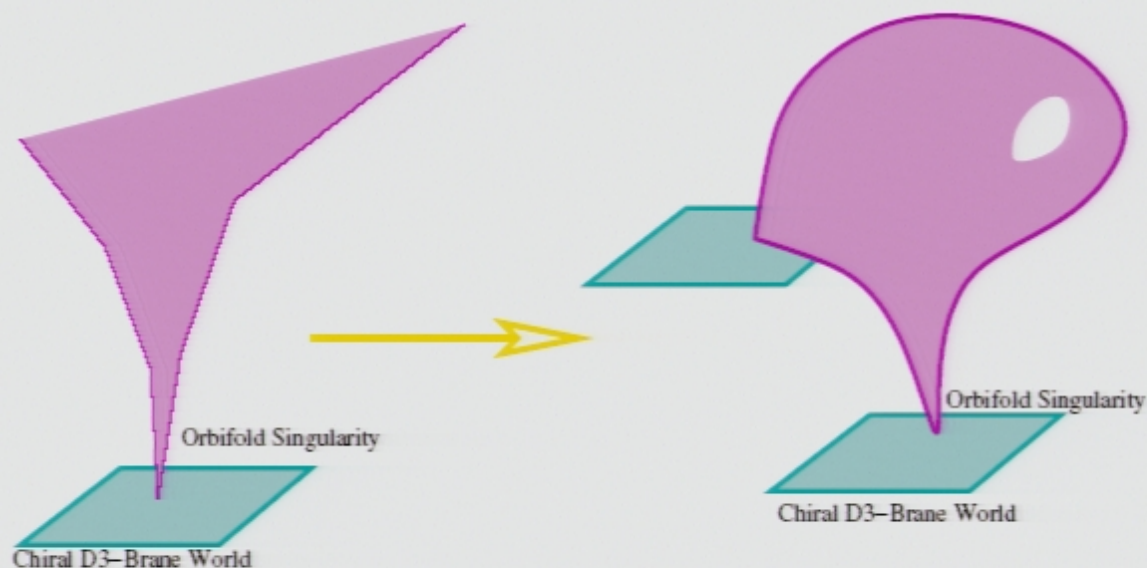
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Singus vs. Magnus

- Both types of constructions are based on B-type branes, so they are essentially the same from an stringy point of view.
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- D3's at singularities are easier to embed in warped throat constructions in a 'bottom-up' fashion, and the soft terms are easier to understand.
- Magnetized D7's have a richer and more interesting soft-term pattern, and SUSY can be broken while still satisfying supergravity equations of motion.

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Towards realistic vacua

- Much of the flux physics in the literature is based on $\mathcal{N} = 1$ vacua, over which we have a better theoretical control.
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no chiral $D = 4$, $\mathcal{N} = 1$ flux compactification as above has been found.

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- The aim of this talk is to describe the first examples of such vacua.
- In particular, we find $\mathcal{N} = 1$ and $\mathcal{N} = 0$ chiral flux vacua solving the supergravity equations, by means of magnetized D-branes.
- Moreover, these vacua are not only chiral, but also yield gauge theories remarkably close to the MSSM.

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Talk based on:

F. M. and Gary Shiu

“Building MSSM Flux Vacua”, hep-th/0409132

“MSSM vacua from Flux compactification”, hep-th/0408059

General Flux Vacua

- There is a wide class of type IIB flux compactifications yielding $D = 4$ Minkowski vacua.

[DRS,GKP]

- The necessary ingredients are:
 - A (warped) compact Calabi-Yau background metric X_6
 - O3-planes (and O7-planes) localized in X_6
 - D-branes filling M_4 and not breaking supersymmetry
 - A 3-form flux G_3 on X_6 such that

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- Two possibilities
 - G_3 is a (2,1)-form $\Rightarrow \mathcal{N} = 1$
 - G_3 contains a (0,3) component $\Rightarrow \mathcal{N} = 0$

An orientifold example

- A simple example of CY_3 is given by a $\mathbf{T}^6/(\mathbf{Z}_2 \times \mathbf{Z}_2)$ orbifold

$$T^6 = T^2 \times T^2 \times T^2$$

$$\theta : (z_1, z_2, z_3) \mapsto (-z_1, -z_2, z_3)$$

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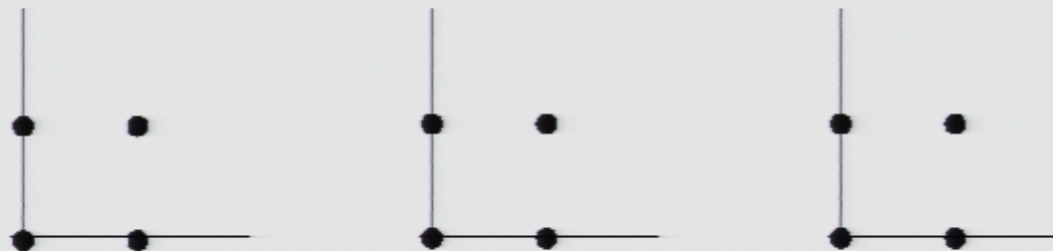
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- By further quotienting by the orientifold action $\Omega\mathcal{R}$

Ω : World-sheet parity

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we introduce **O3-planes** and **O7-planes** at \mathbf{Z}_2 fixed points.



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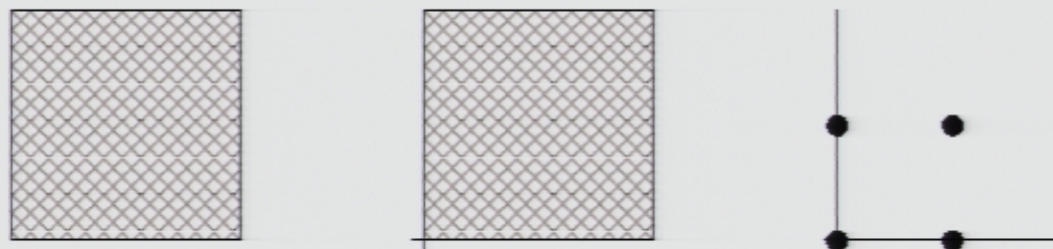
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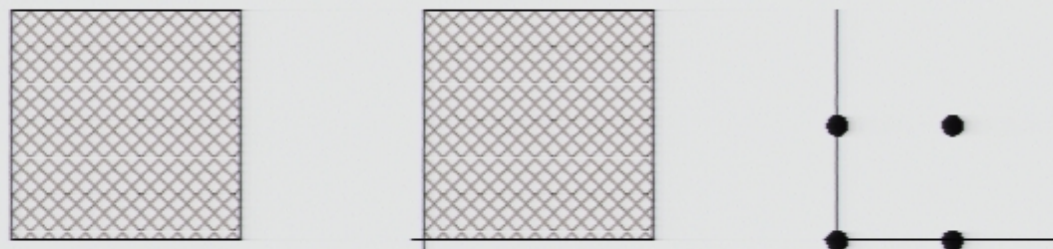
$$\omega : (z_1, z_2, z_3) \mapsto (z_1, -z_2, -z_3)$$

- By further quotienting by the orientifold action $\Omega\mathcal{R}$

Ω : World-sheet parity

$$\mathcal{R} : (z_1, z_2, z_3) \mapsto (-z_1, -z_2, -z_3)$$

we introduce $O3$ -planes and $O7$ -planes at Z_2 fixed points.



Adding D-branes

- Absence of **tadpole** divergences requires that we **add D-branes** in our compactification.
- The simplest way to cancel O-plane charges is to consider **D3 and D7-branes parallel** to the O3 and O7-planes. [Berkooz and Leigh]

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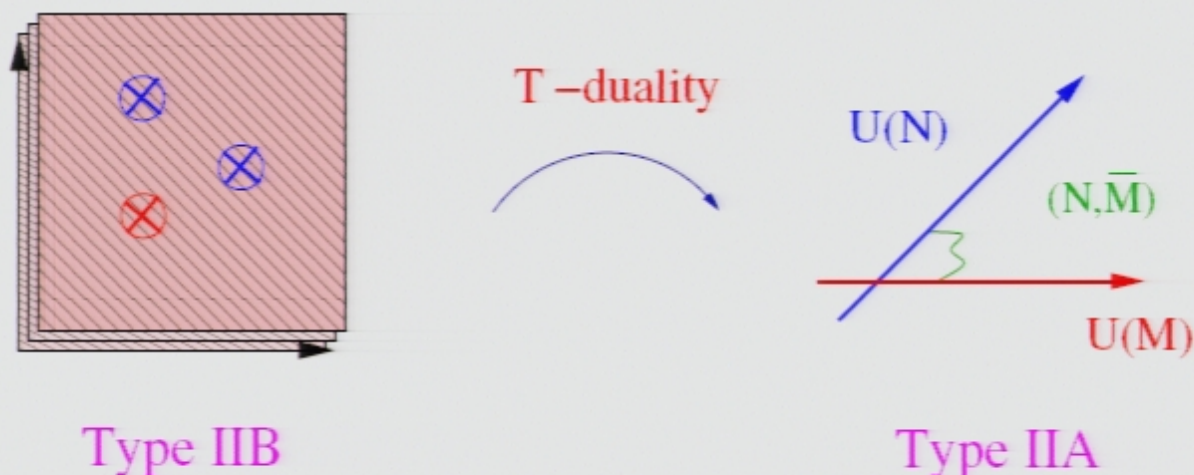
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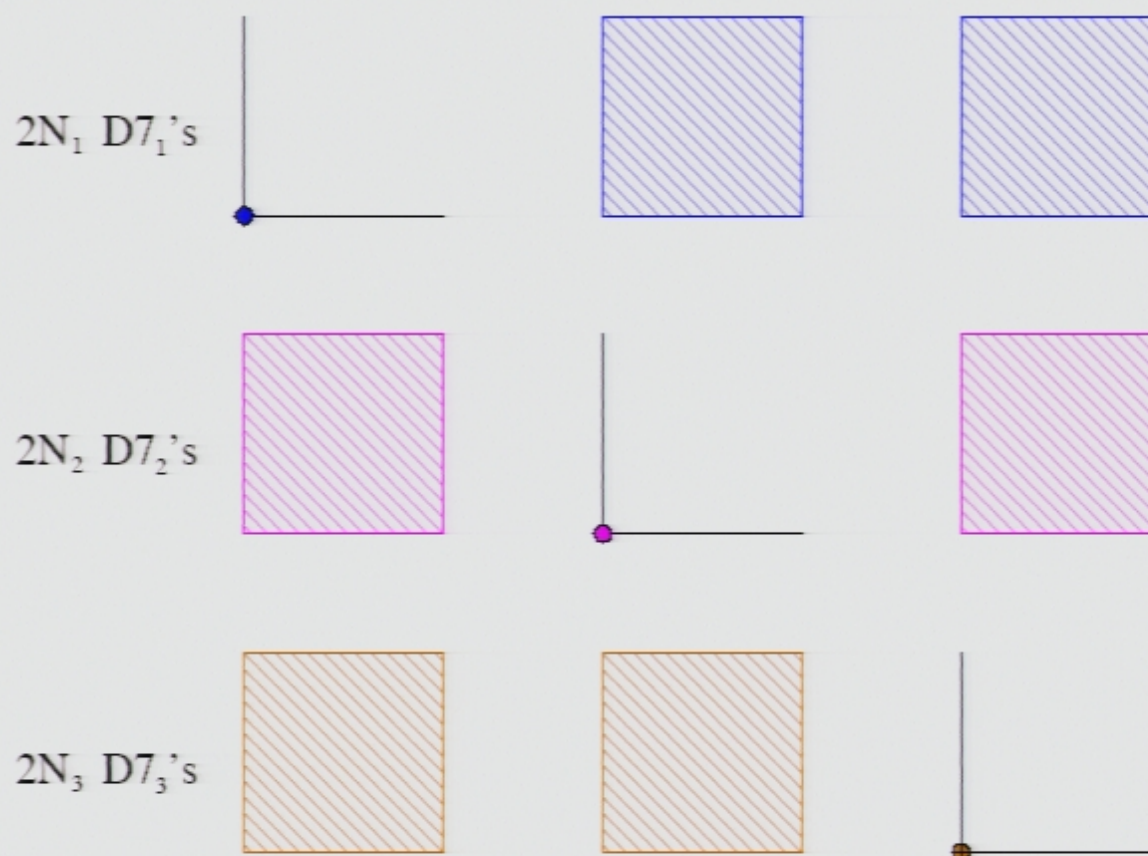
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- This theory is however non-chiral. We may achieve **chirality** by introducing internal **magnetic fluxes** $F_{\mu\nu}$ on D7-branes. [Bachas, BGKL, AADS]
- T-dual to **D6-branes at angles** in $\mathbb{Z}_2 \times \mathbb{Z}_2$. [Berkooz, Douglas, Leigh]
[Cvetič, Shiu, Uranga]



Magnetizing D-branes

$$USp(2N_1) \times USp(2N_2) \times USp(2N_3)$$

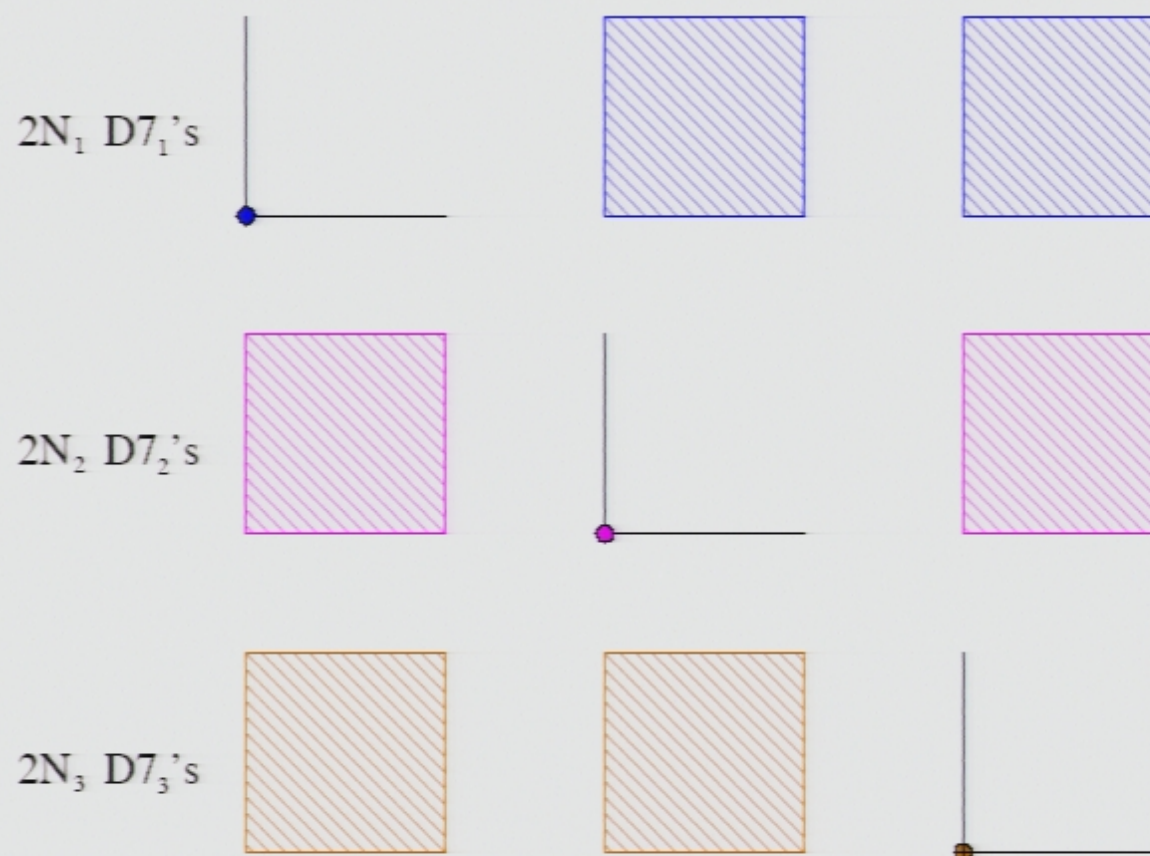
$$(2N_1, 2N_2, 1) + (2N_1, 1, 2N_3) + (1, 2N_2, 2N_3)$$



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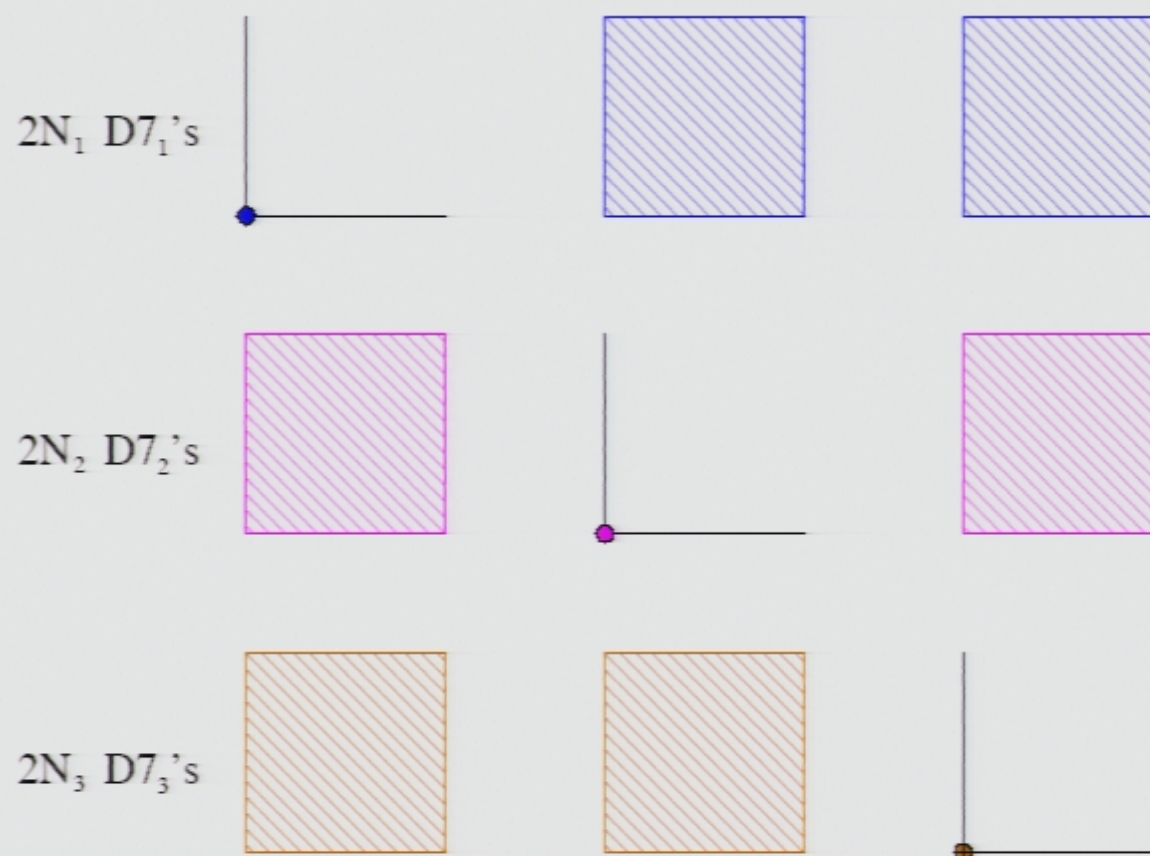
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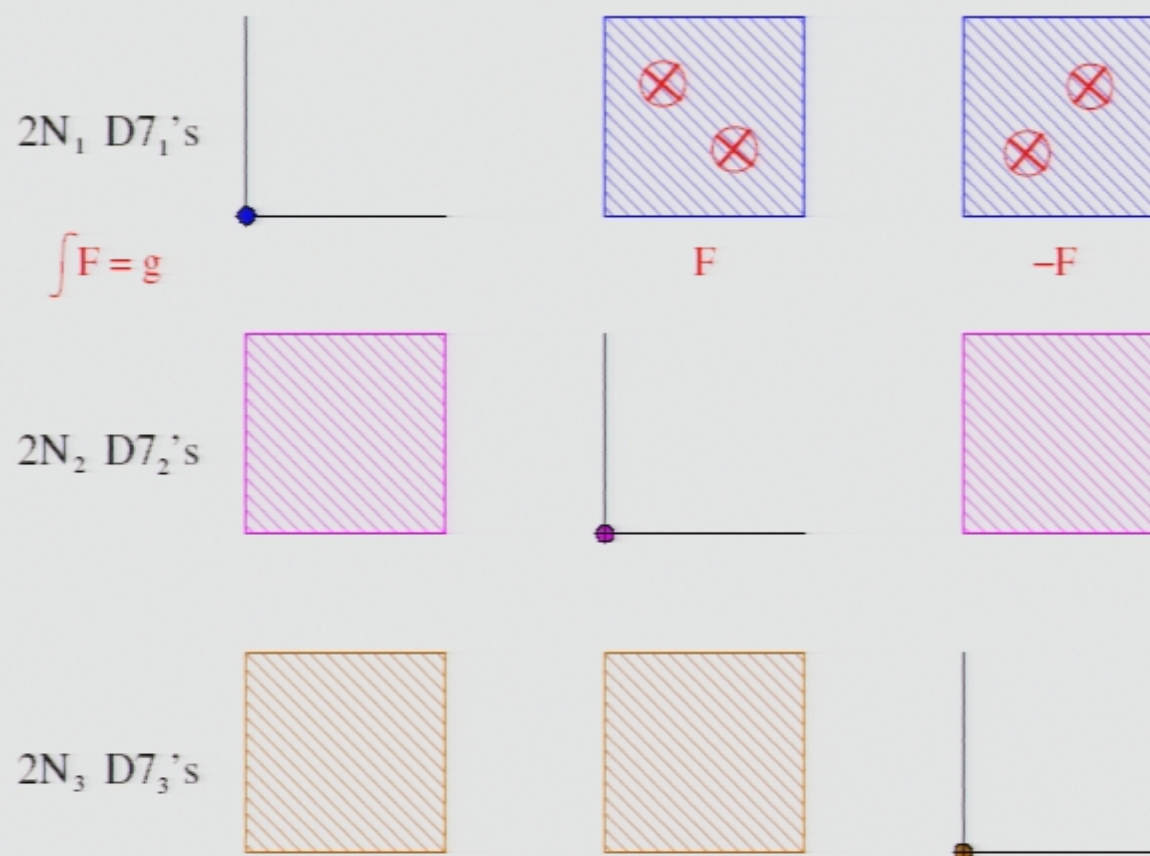
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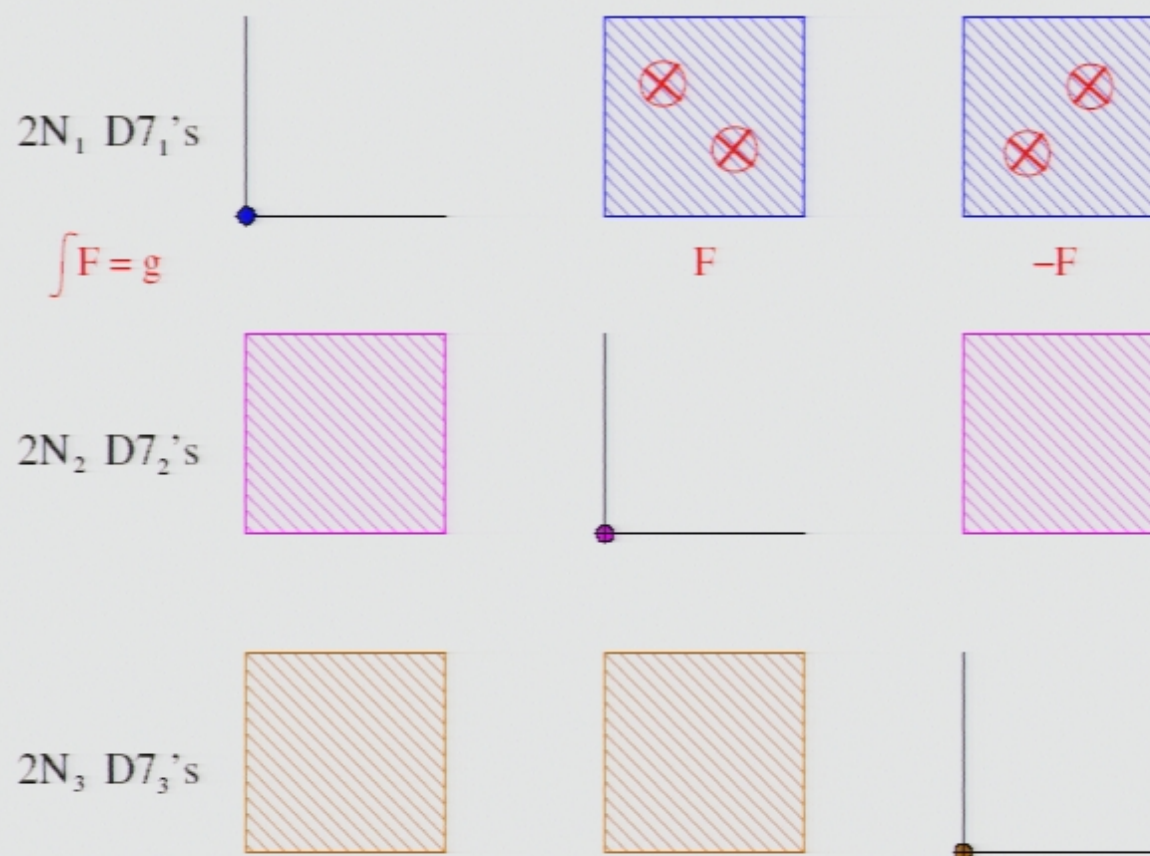
$$g(N_1, 2N_2, 1) + g(\overline{N}_1, 1, 2N_3) + (1, 2N_2, 2N_3)$$



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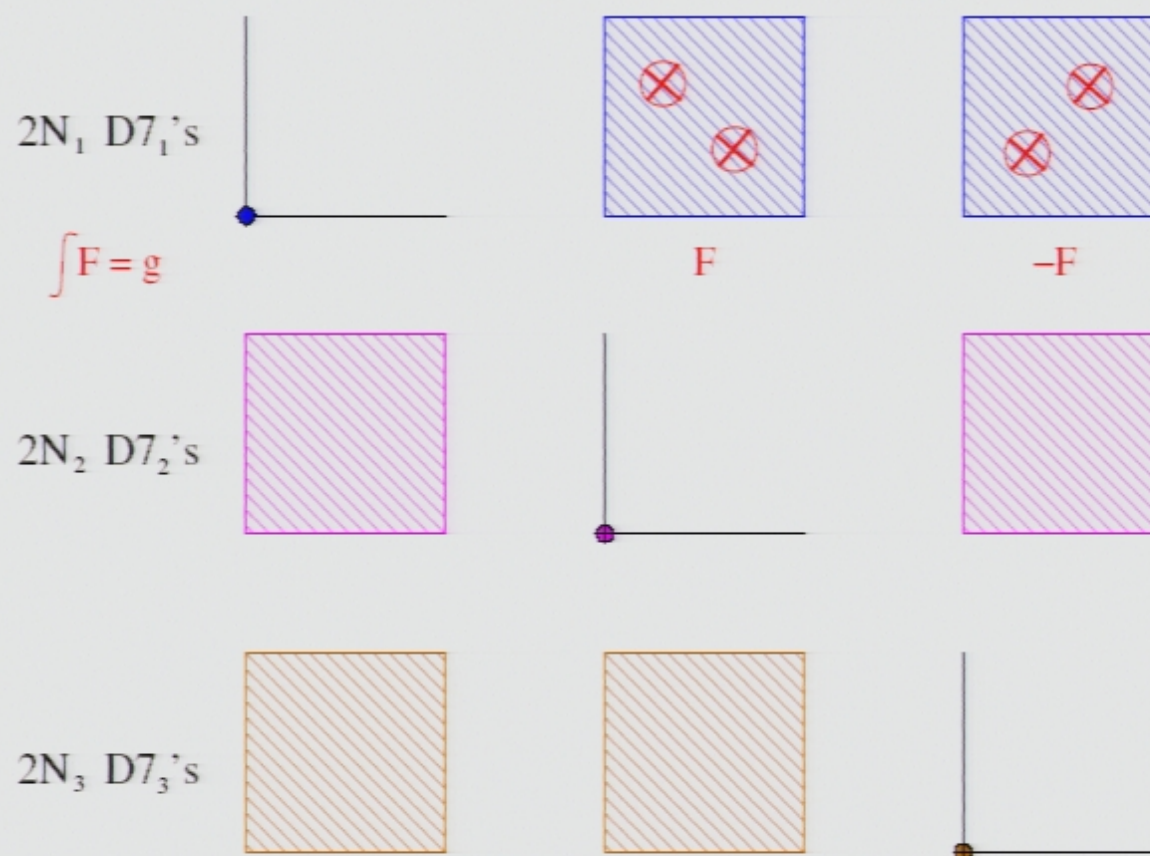
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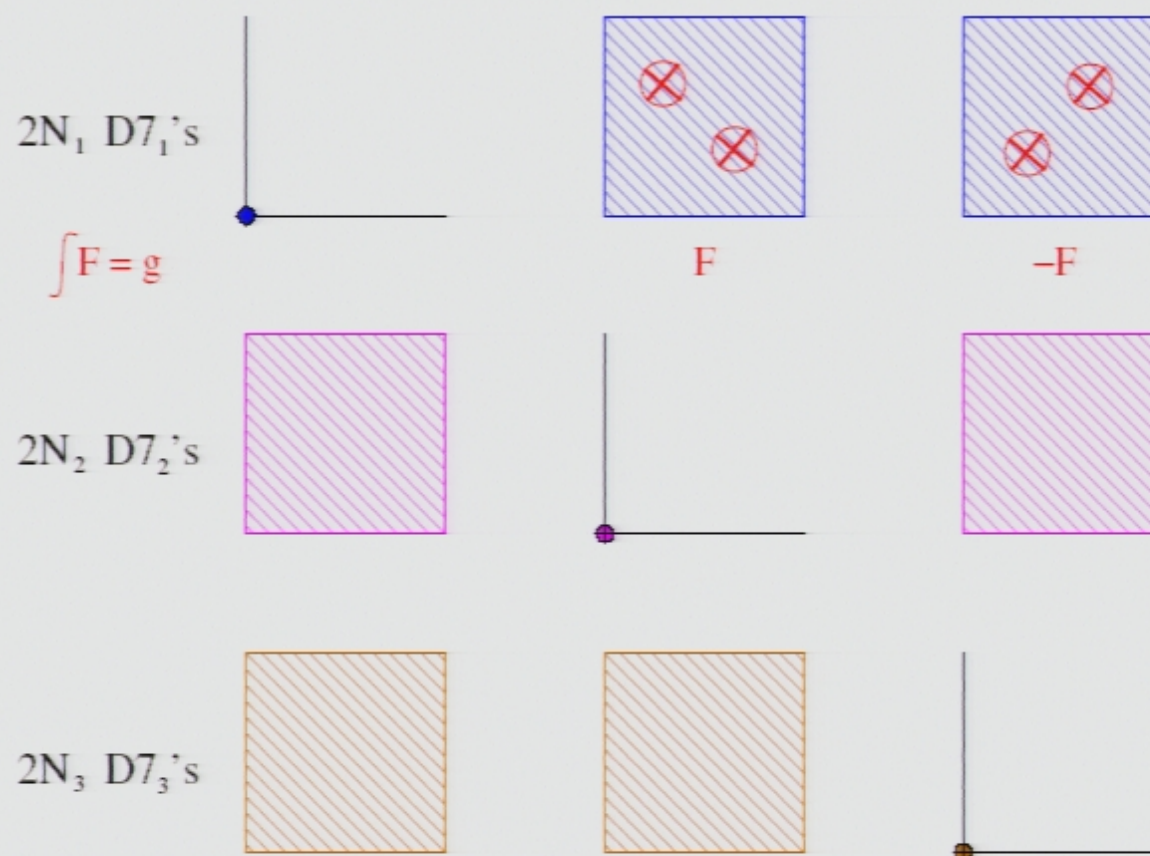
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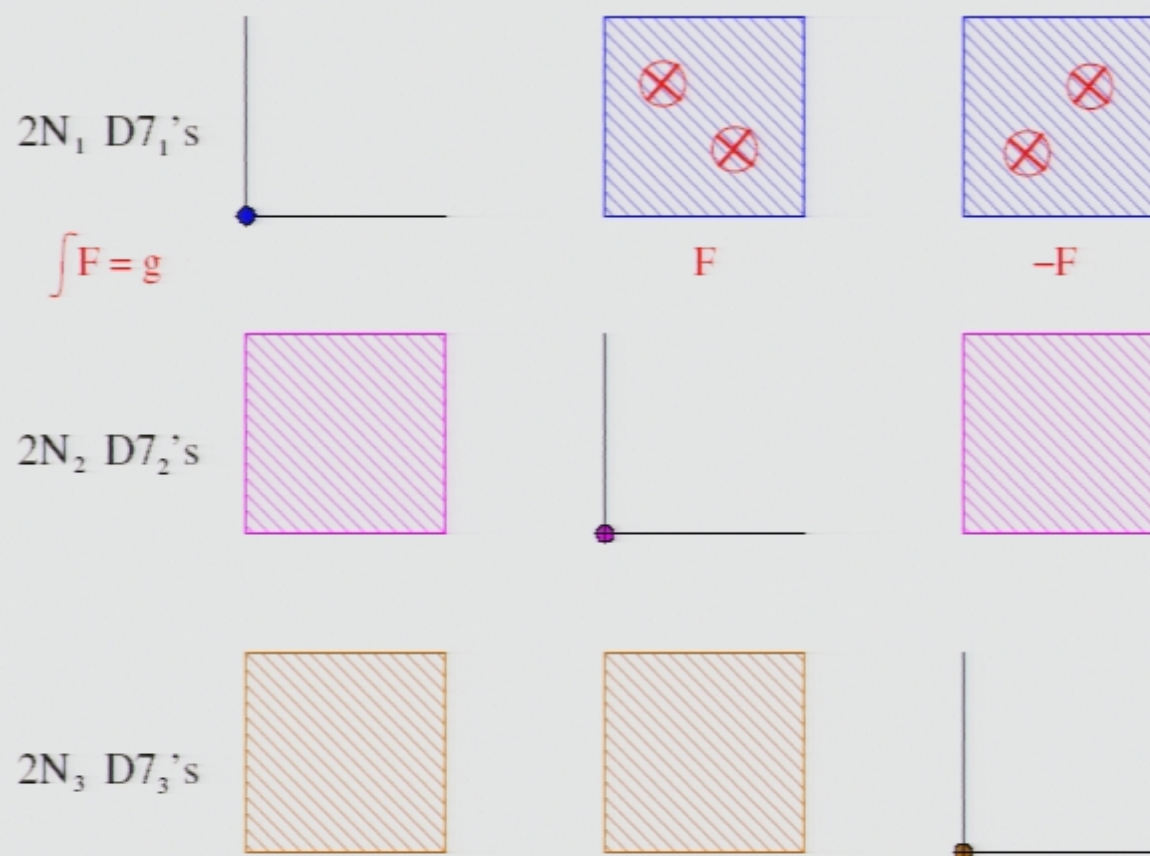
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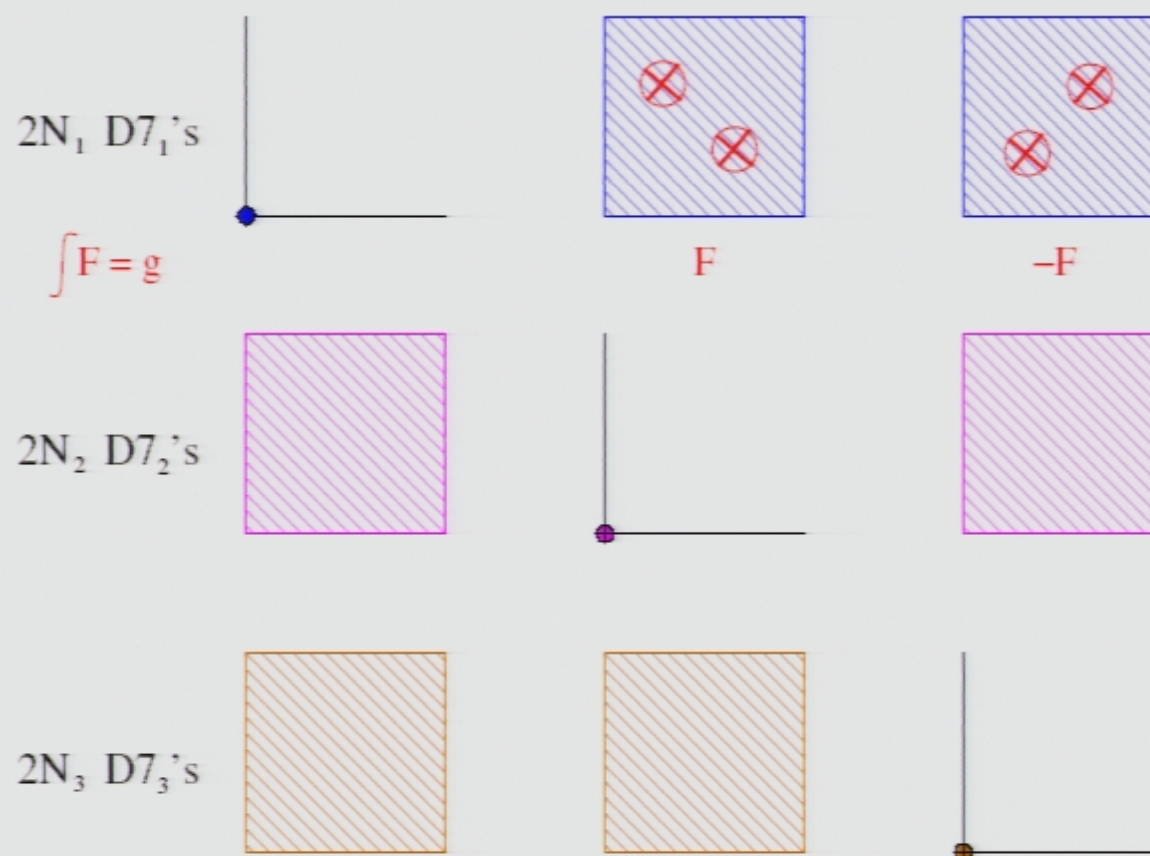
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A Left-Right MSSM Example

- The previous example allow us to achieve a semi-realistic spectrum, by using the identity $USp(2) \simeq SU(2)$

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- By performing an adjoint Higgsing of $U(4)$, we obtain a Left-Right MSSM spectrum with g generations of chiral matter

[Cremades, Ibáñez, F.M.]

$$SU(3) \times SU(2) \times SU(2) \times U(1)_{B-L}$$

$$g(3, 2, 1)_{1/3} + g(\bar{3}, 1, 2)_{-1/3}$$

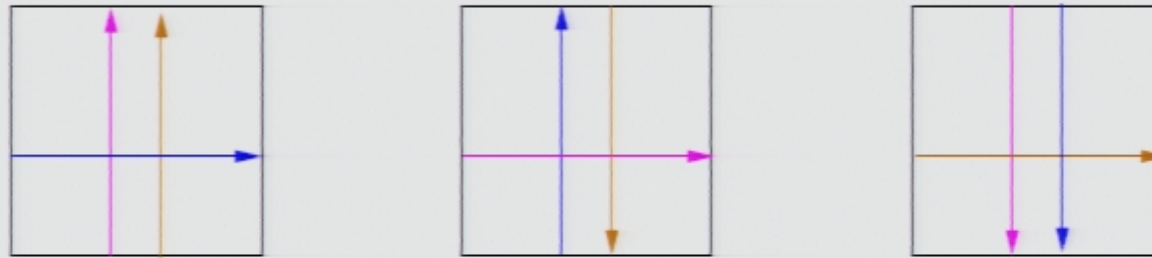
$$g(1, 2, 1)_1 + g(1, 1, 2)_{-1}$$

$$(1, 2, 2)$$

T-dual picture

- The appearance of **chirality** is easier to visualize in the **intersecting D-brane** picture

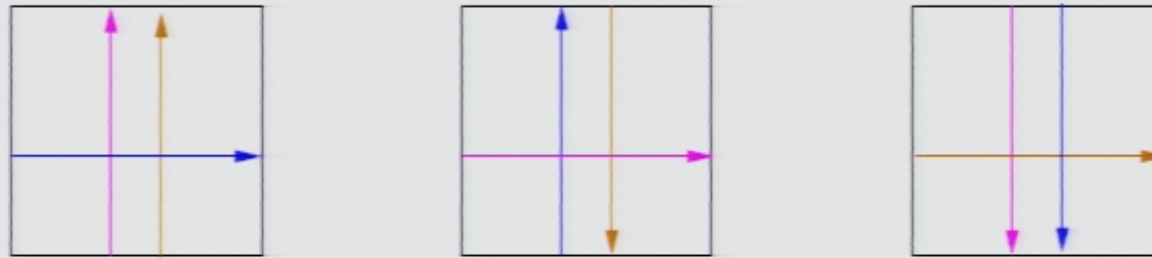
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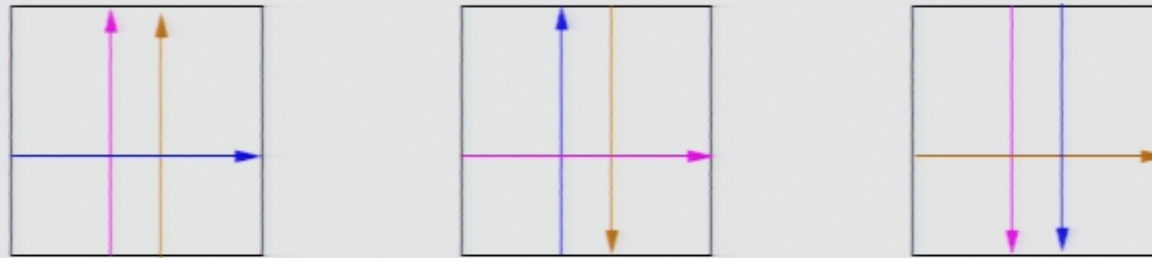
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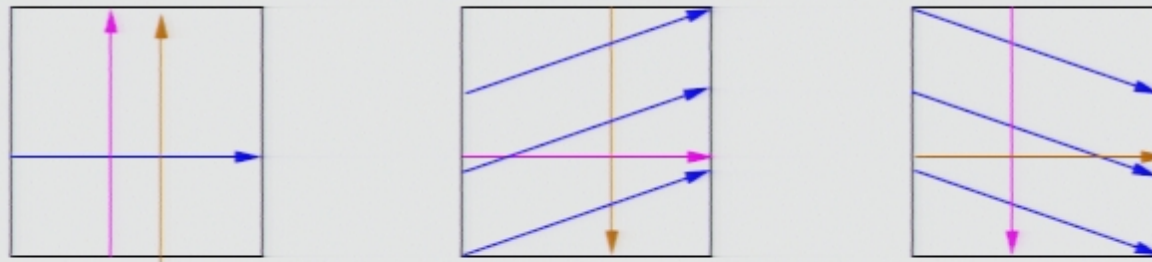
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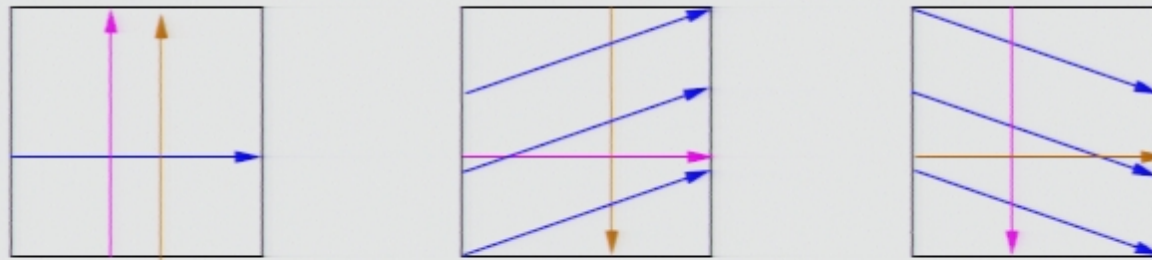
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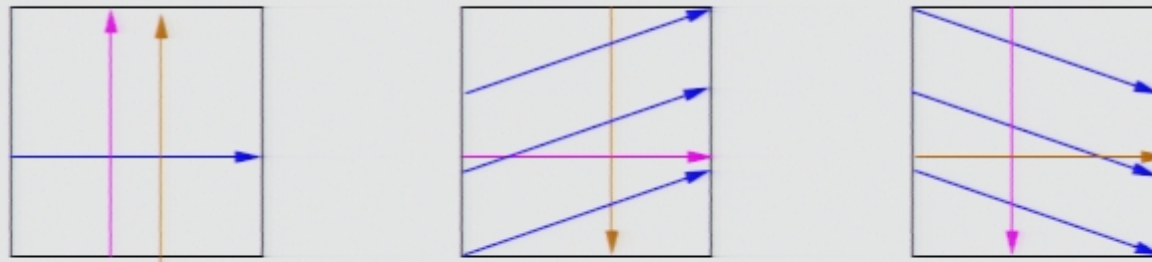
after



T-dual picture

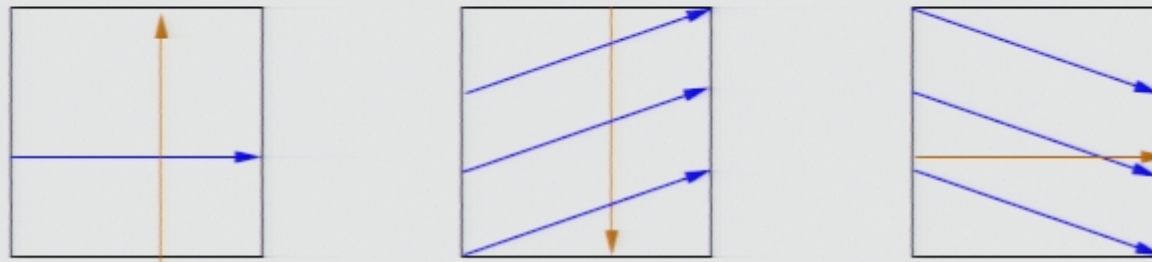
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after



- As well as the adjoint **Higgsing**

before



Magnetic Numbers

- Intersecting branes also inspire a **description** of these models in terms of **topological quantities**

N_a	Number of D – branes	
m_a^i	Number of times wrapped on $(T^2)_i$	} $\frac{m_a^i}{2\pi} \int_{T^2_i} F_a^i = n_a^i.$
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		$(T^2)_1$	$(T^2)_2$	$(T^2)_3$
$D9 \rightarrow N_a$		(n_a^1, m_a^1)	(n_a^2, m_a^2)	(n_a^3, m_a^3)
$D7_1 \rightarrow N_a$		$(1, 0)$	(n_a^2, m_a^2)	(n_a^3, m_a^3)
$D5_1 \rightarrow N_a$		(n_a^1, m_a^1)	$(1, 0)$	$(1, 0)$
$D3 \rightarrow N_a$		$(1, 0)$	$(1, 0)$	$(1, 0)$

- The **orientifold action** maps these numbers as

$$\Omega\mathcal{R} : (n_a^i, m_a^i) \mapsto (n_a^i, -m_a^i)$$

Magnetic Numbers II

- In this notation, our previous **Left-Right example** reads

N_α	(n_α^1, m_α^1)	(n_α^2, m_α^2)	(n_α^3, m_α^3)
$N_a = 6$	$(1, 0)$	$(g, 1)$	$(g, -1)$
$N_b = 2$	$(0, 1)$	$(1, 0)$	$(0, -1)$
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- The **chiral spectrum** can be computed by means of the **intersection product**

$$I_{ab} = [Q_a] \cdot [Q_b] = \prod_{i=1}^3 (n_a^i m_b^i - m_a^i n_b^i)$$

Adding Background Fluxes

- We now want to include a background 3-form flux $G_3 = F_3 - \tau H_3$. It must satisfy

- Bianchi identities: $dF_3 = dH_3 = 0$
- Quantization conditions: $\int_{\Sigma} F_3, \int_{\Sigma} H_3 \in \mathbb{Z}, \quad \forall \Sigma \in H_3(X_6, \mathbb{Z})$

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- The orientifold modding $\Omega\mathcal{R}$ adds an extra factor of 2, unless Σ contains an odd number of exotic O3-planes (i.e., O3's with positive tension and/or RR charge)

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- We choose a constant ISD flux of the form

$$G_3 = G_{\bar{1}23} d\bar{z}_1 dz_2 dz_3 + G_{1\bar{2}3} dz_1 d\bar{z}_2 dz_3 + G_{12\bar{3}} dz_1 dz_2 d\bar{z}_3 + G_{\bar{1}\bar{2}\bar{3}} d\bar{z}_1 d\bar{z}_2 d\bar{z}_3$$

SUSY breaking

Tadpoles

- In order to build a consistent D-brane model, RR tadpoles must cancel. In particular, D3-brane tadpoles read

$$\sum_{\alpha} N_{\alpha} n_{\alpha}^1 n_{\alpha}^2 n_{\alpha}^3 + \frac{1}{2} N_{\text{flux}} = \frac{1}{4} N_{O3}$$

- In the present context we have

$$\left. \begin{array}{l} N_{O3} = 64 \\ N_{\text{flux}} = n \cdot 64, \quad n \in \mathbb{N} \end{array} \right\} \Rightarrow \sum_{\alpha} N_{\alpha} n_{\alpha}^1 n_{\alpha}^2 n_{\alpha}^3 < 0 \text{ for } G_3 \neq 0$$

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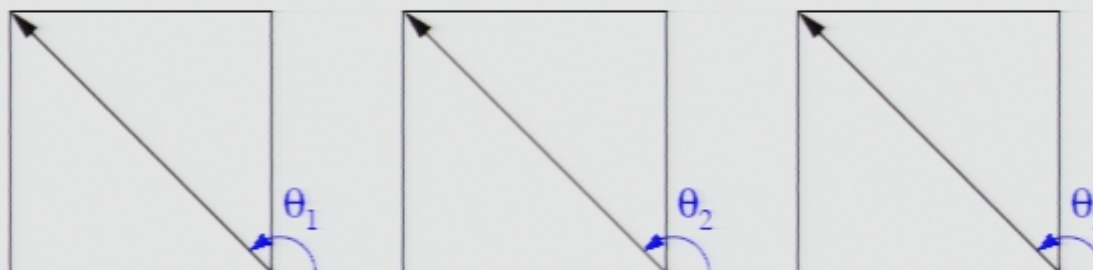
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The $D9 - \overline{D9}$ mirror system

- Let us consider the magnetic numbers

$$(-1, 1) (-1, 1) (-1, 1)$$

- In the mirror picture



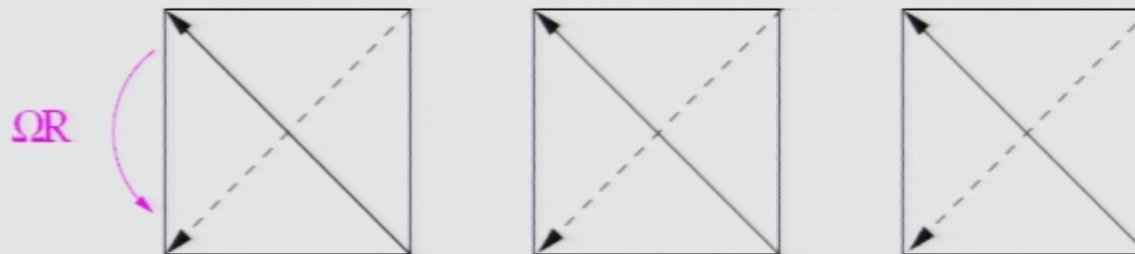
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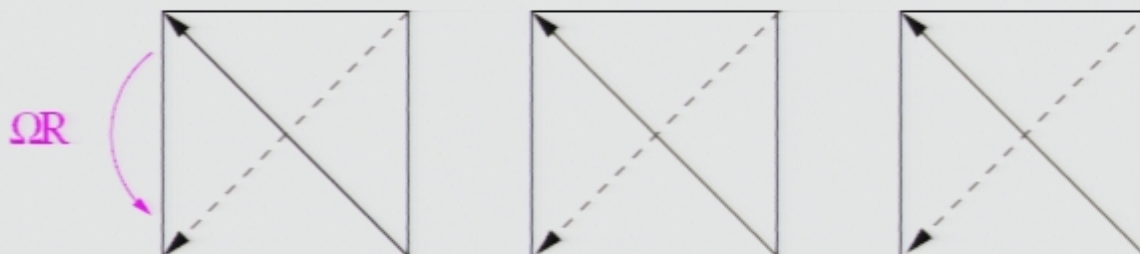


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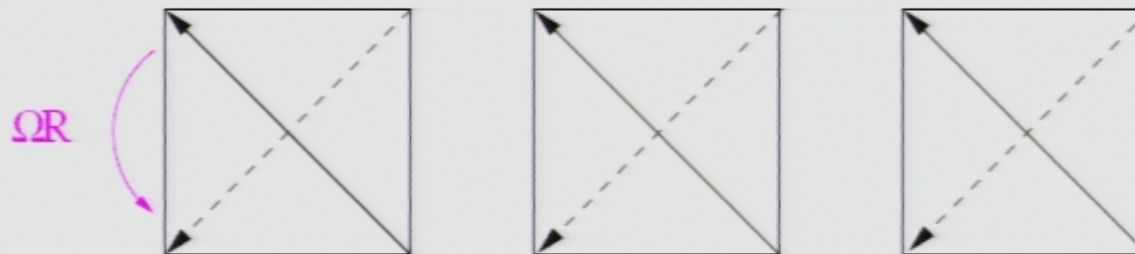


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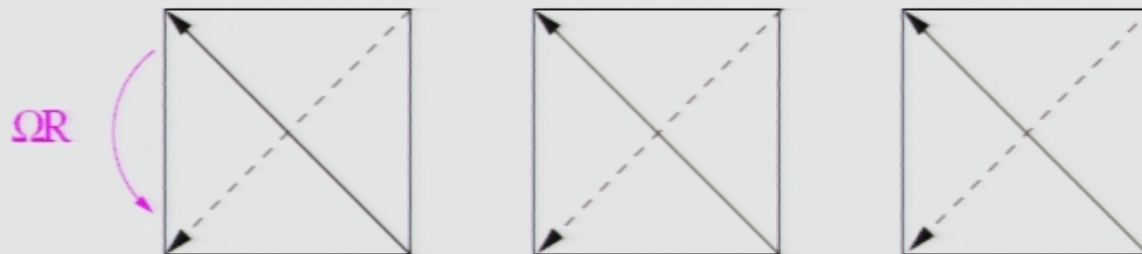


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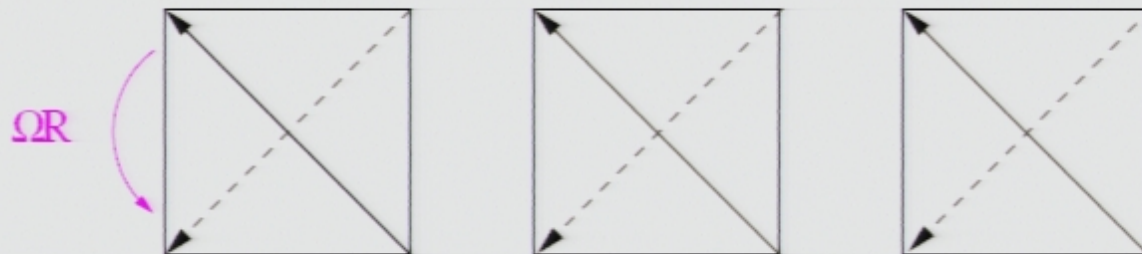


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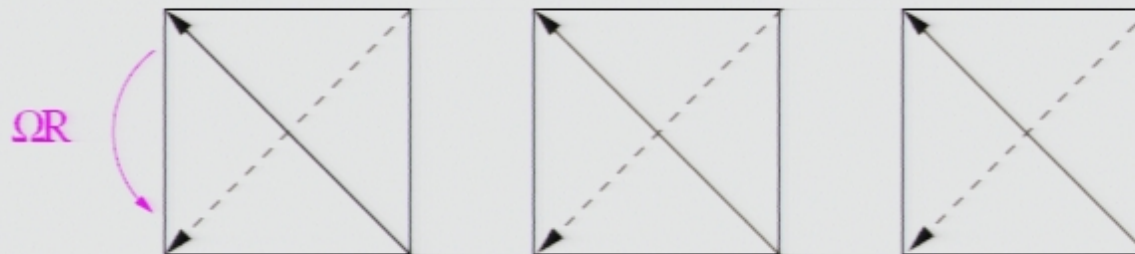


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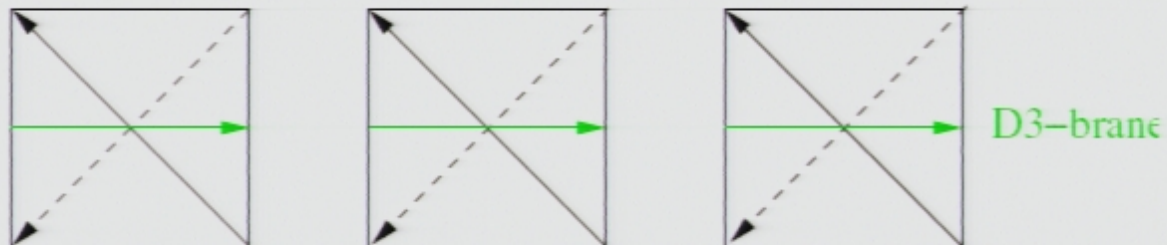


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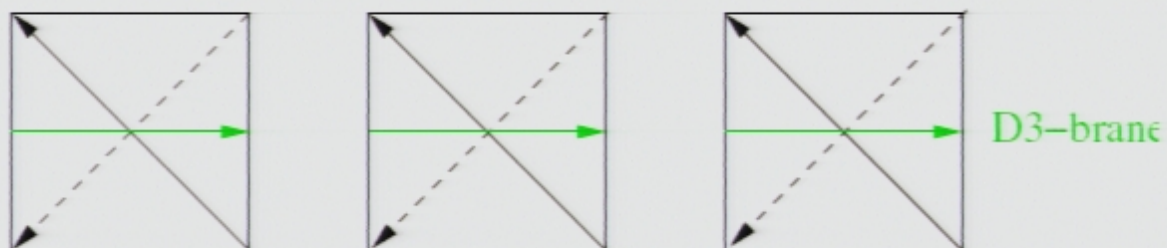


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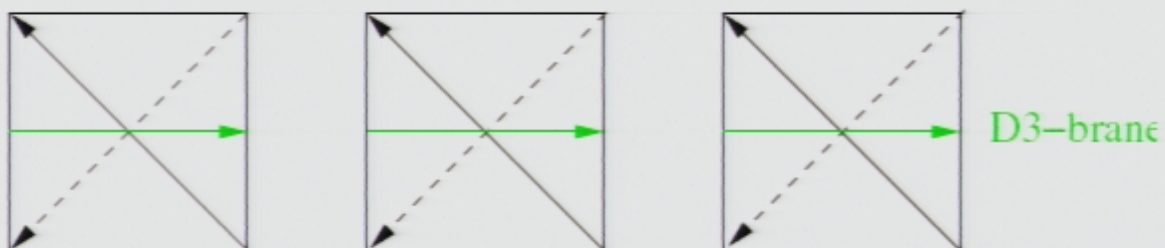


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The model

- An **example** of all the above is given by the magnetic numbers

N_α	(n_α^1, m_α^1)	(n_α^2, m_α^2)	(n_α^3, m_α^3)
$N_a = 6$	$(1, 0)$	$(g, 1)$	$(g, -1)$
$N_b = 2$	$(0, 1)$	$(1, 0)$	$(0, -1)$
$N_c = 2$	$(0, 1)$	$(0, -1)$	$(1, 0)$
$N_d = 2$	$(1, 0)$	$(g, 1)$	$(g, -1)$
$N_{h1} = 2$	$(-2, 1)$	$(-3, 1)$	$(-4, 1)$
$N_{h2} = 2$	$(-2, 1)$	$(-4, 1)$	$(-3, 1)$
$8N_{D3}$	$(1, 0)$	$(1, 0)$	$(1, 0)$

which contains the **Left-Right MSSM** system described before

The model II

- RR tadpoles are satisfied if

$$g^2 + N_{D3} + 4n = 14 \quad (g \leq 3)$$

The model

- An **example** of all the above is given by the magnetic numbers

N_α	(n_α^1, m_α^1)	(n_α^2, m_α^2)	(n_α^3, m_α^3)
$N_a = 6$	$(1, 0)$	$(g, 1)$	$(g, -1)$
$N_b = 2$	$(0, 1)$	$(1, 0)$	$(0, -1)$
$N_c = 2$	$(0, 1)$	$(0, -1)$	$(1, 0)$
$N_d = 2$	$(1, 0)$	$(g, 1)$	$(g, -1)$
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$8N_{D3}$	$(1, 0)$	$(1, 0)$	$(1, 0)$

which contains the **Left-Right MSSM** system described before

- This D-brane system preserves $\mathcal{N} = 1$ **supersymmetry** if we impose

$$\mathcal{A}_2 = \mathcal{A}_3$$

$$\tan^{-1}(\mathcal{A}_1/2) + \tan^{-1}(\mathcal{A}_2/3) + \tan^{-1}(\mathcal{A}_3/4) = \pi$$

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$$G_3 = \frac{8}{\sqrt{3}} e^{-\frac{\pi i}{6}} (d\bar{z}_1 dz_2 dz_3 + dz_1 d\bar{z}_2 dz_3 + dz_1 dz_2 d\bar{z}_3)$$

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- $n = 2, \quad g = 2, \quad N_{D3} = 2$
- $n = 1, \quad g = 3, \quad N_{D3} = 1 \Rightarrow$ 3-gen. $\mathcal{N} = 0$ flux compactification
- $n = 0, \quad g = 3, \quad N_{D3} = 5$

$$G_3 = 2(d\bar{z}_1 dz_2 dz_3 + dz_1 d\bar{z}_2 dz_3 + dz_1 dz_2 d\bar{z}_3 + d\bar{z}_1 d\bar{z}_2 d\bar{z}_3)$$

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The spectrum

- The low energy gauge group of these models is given by

$$SU(3) \times SU(2) \times SU(2) \times U(1)_{B-L} \times [U(1)' \times USp(8N_{D3})],$$

$$U(1)' = \frac{1}{g} [U(1)_a + U(1)_d] - 2[U(1)_{h_1} - U(1)_{h_2}]$$

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- The extra pairs of $D9 - \overline{D9}$'s induce extra chiral matter beyond the Left-Right spectrum
- Most of these chiral exotics disappear after giving a v.e.v. to some scalar fields in the hidden sector
- In terms of D-brane physics, this can be understood as the process of D-brane/gauge bundle recombination

$$h_1 + h'_2 \rightarrow h$$

Higgsing away chiral exotics

- Let us consider a Pati-Salam spectrum in the case $g = 3$, $N_f = 5$

Sector	Matter	$SU(4) \times SU(2) \times SU(2) \times [USp(40)]$	Q_a	Q_{h_1}	Q_{h_2}	Q'
(ab)	F_L	$3(4, 2, 1)$	1	0	0	$1/3$
(ac)	F_R	$3(\bar{4}, 1, 2)$	-1	0	0	$-1/3$
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- Besides chiral exotics, these models also present non-chiral matter beyond the MSSM, like
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[Cámara, Ibáñez, Uranga]

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MSSM + soft terms induced by G_3

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Type IIB recipe for chiral flux vacua

Let us describe the strategy that we have followed:

- Choose a **CY₃ background** that admits **O3-planes** and/or O7-planes
- Introduce **B-type D-branes** such that they preserve $\mathcal{N} = 1$ supersymmetry in this background. Try to build a **chiral** (semi-realistic) **spectrum** from them.
- Introduce **ISD 3-form fluxes**. Look at the effects that it creates on the metric background and on the D-branes.
- Look for **new BPS-like objects** that need to be introduced to build tadpole-free models as, e.g. $D9 - \overline{D9}$ pairs, and analyze their properties.

Conclusions

- We have constructed $\mathcal{N} = 1$ and $\mathcal{N} = 0$ chiral four-dimensional vacua of flux compactification by means of magnetized D-branes.
- Even in the $\mathcal{N} = 0$ case (first order) NSNS tadpoles cancel, so the instabilities associated with them are not present.
- In addition, these models admit a low energy spectrum remarkably close to the MSSM, with 3 generations of chiral matter.
- In the $\mathcal{N} = 0$ case, SUSY is broken by the flux, which not only lifts moduli but also induces soft terms in the MSSM sector.
- We have analyzed some phenomenological features of these models, like the Higgsing processes, which can be understood in terms of D-brane physics.

What have we learnt?

- $D = 4$ $\mathcal{N} = 1$ chiral Minkowski vacua with fluxes can indeed be constructed. $\mathcal{N} = 0$ chiral models as well, and without first order NSNS tadpoles.
- Their construction is remarkably simple compared to most chiral string vacua, while still being quite close to realistic physics.
- This simplicity encourages to extend this construction to most involved CY geometries. We expect the appealing features to survive, while including new ones (warped throats, etc.)
- A key ingredient in these constructions is the presence of magnetised $D9 - \overline{D9}$ pairs. It would be interesting to study the properties of these objects in general flux compactifications.
- Not only do these $D9 - \overline{D9}$ pairs help finding flux vacua, but also new $\mathcal{N} = 1$ vacua, like in $\mathbb{Z}_2 \times \mathbb{Z}_2$ orientifolds with 'brane supersymmetry breaking'.