

Title: Physics From Loop Quantum Gravity

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Abstract:

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Physics from LQG

Lee Smolin

Perimeter Institute for Theoretical Physics

- 1 Questions about locality in LQG
- 2 Options
- 3 Effects and implications of non-locality in LQG
- 4 Conclusions

Work with Fotini Markopoulou gr-qc/0311059
hep-th/0411???

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Problems with locality in LQG:

Several speakers have referred to issues with locality in LQG and other approaches such as causal sets.

The basic worry is that when we study spin foams and weaves we impose locality because we believe in it. But this is not forced by the theory. We could make other choices that introduce arbitrary amounts of non-locality.

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Do weaves have to be local?

A state $|\Psi\rangle$ is a weave for a metric q_{ab} if the $\langle \rangle$'s of areas and volumes coincide for large regions with the classical values:

$$\begin{aligned}\langle \Psi | \hat{\mathcal{A}}[\mathcal{F}] | \Psi \rangle &= \left(a[\mathcal{F}] + O\left(\frac{l_{Pl}^2}{a[\mathcal{F}]}\right) \right) \\ \langle \Psi | \hat{\mathcal{V}}[\mathcal{R}] | \Psi \rangle &= \left(v[\mathcal{R}] + O\left(\frac{l_{Pl}^3}{a[\mathcal{R}]}\right) \right)\end{aligned}$$

Regular graph state: Γ be a graph, all edges have spin j
all nodes intertwiner I $|\Gamma, j, I\rangle$

Local weave: *all links connect nodes of order l_p apart in q_{ab}*

Superposed weaves:

$$|\Psi\rangle = \sum_{j=\frac{1}{2}}^{\infty} \sum_{I \in \mathcal{V}_{jjjj}} a_{j,I} |\Gamma, j, I\rangle$$

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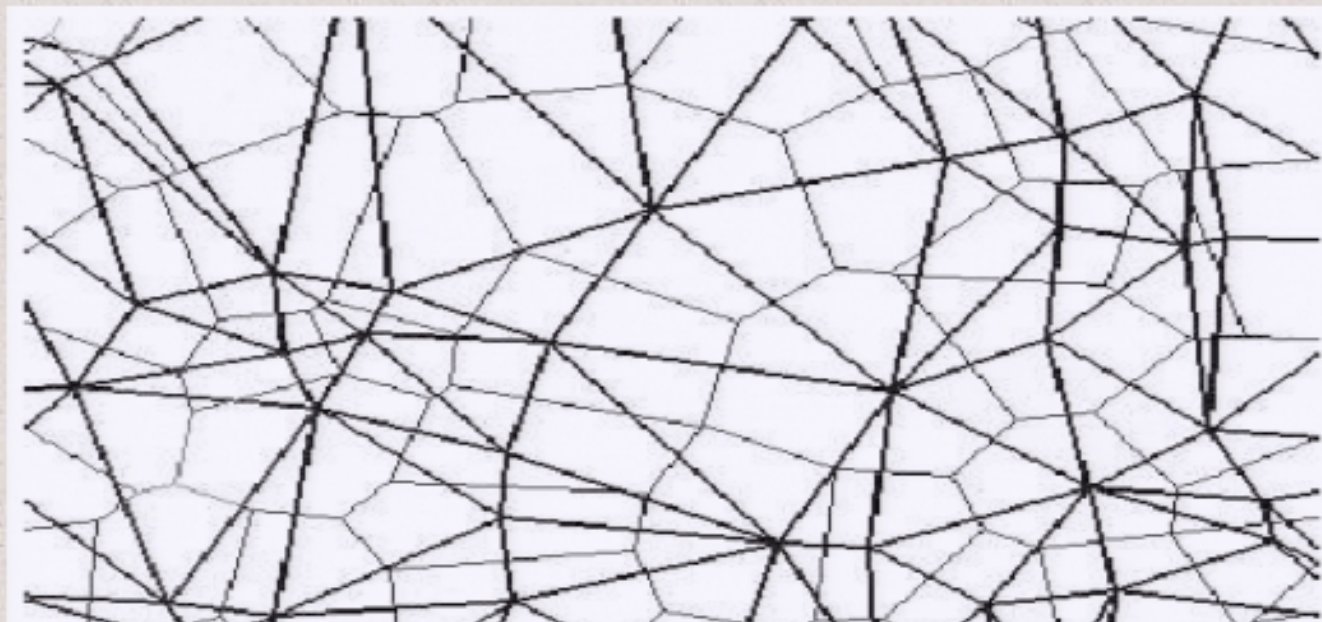
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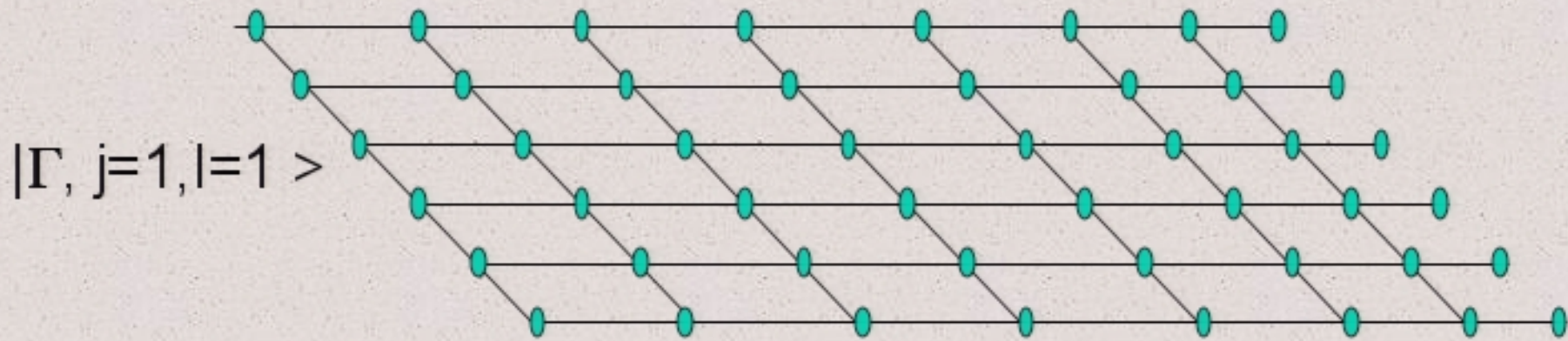


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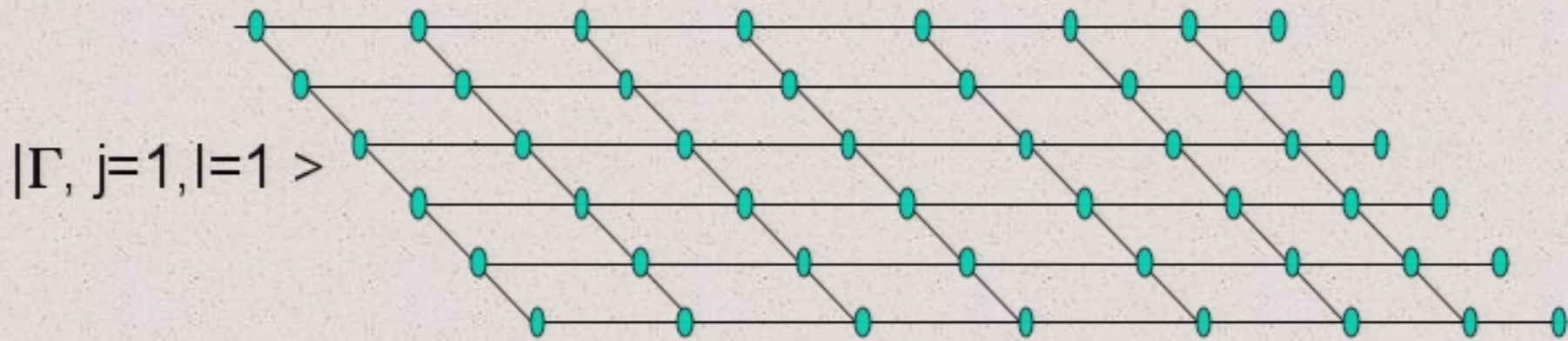
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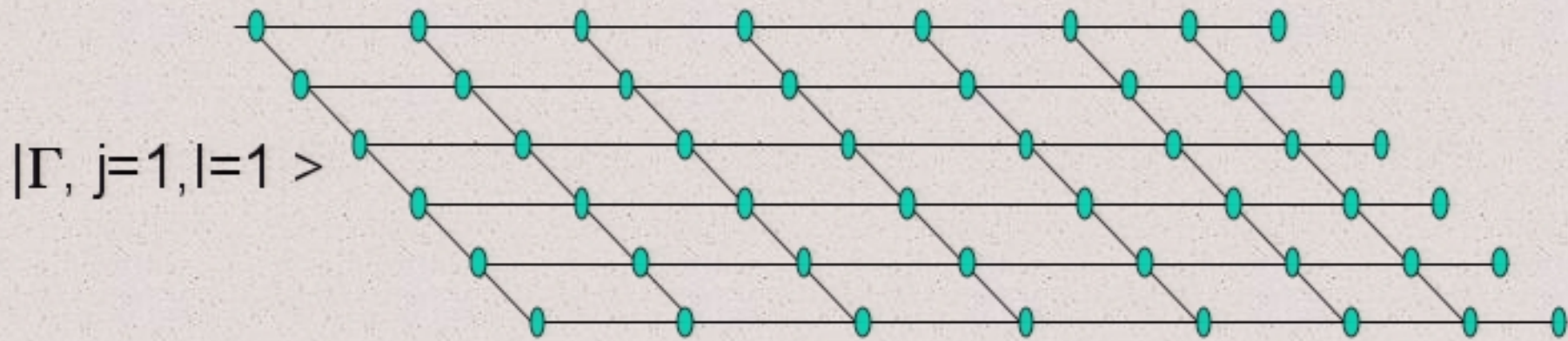
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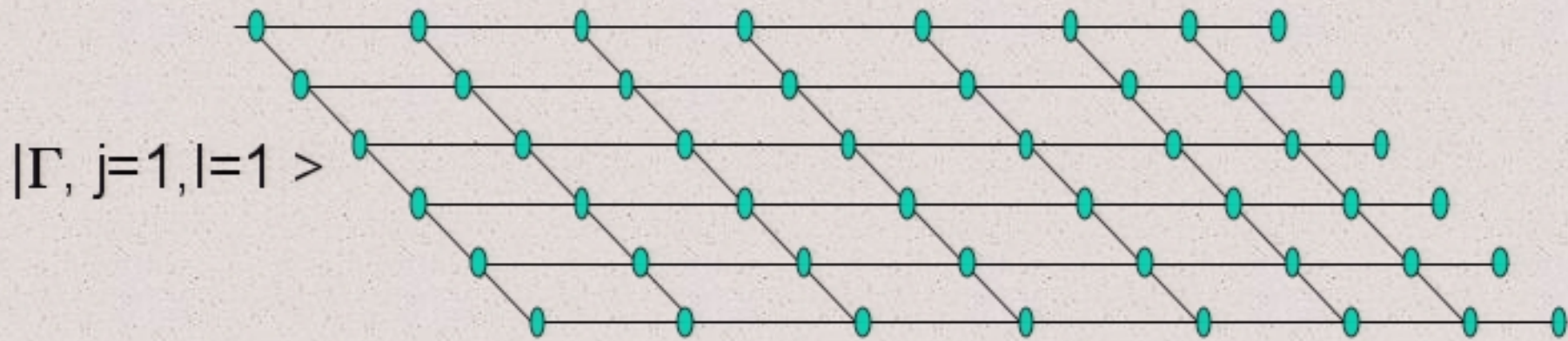
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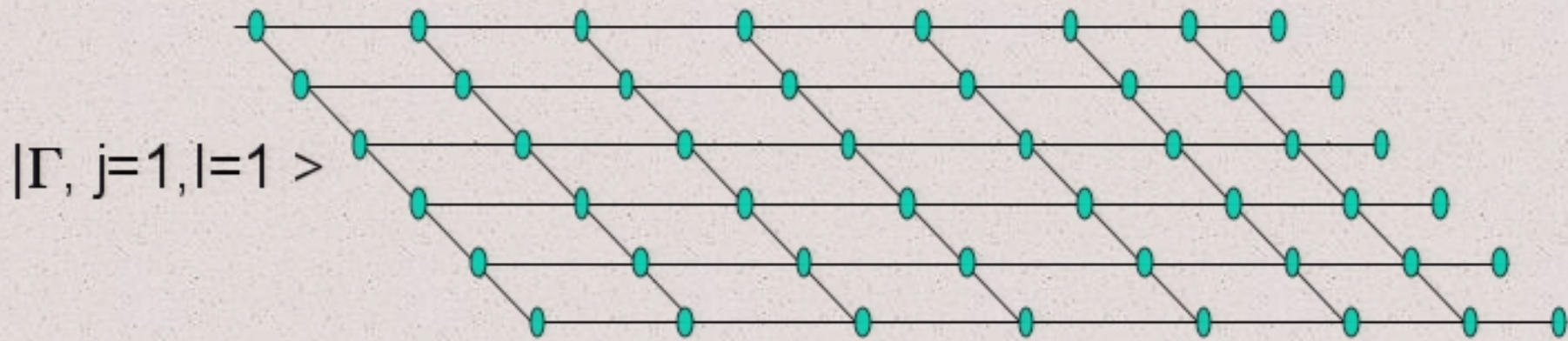
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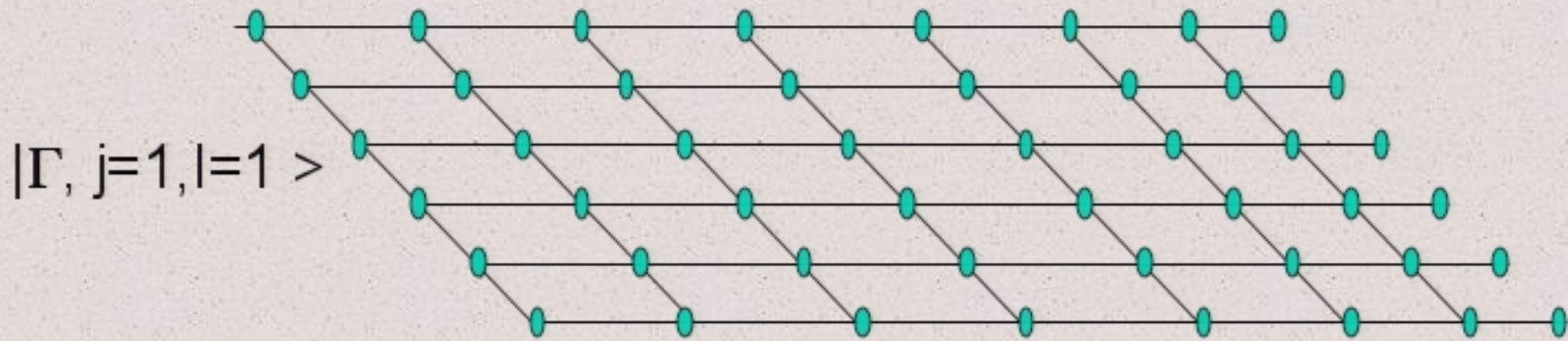
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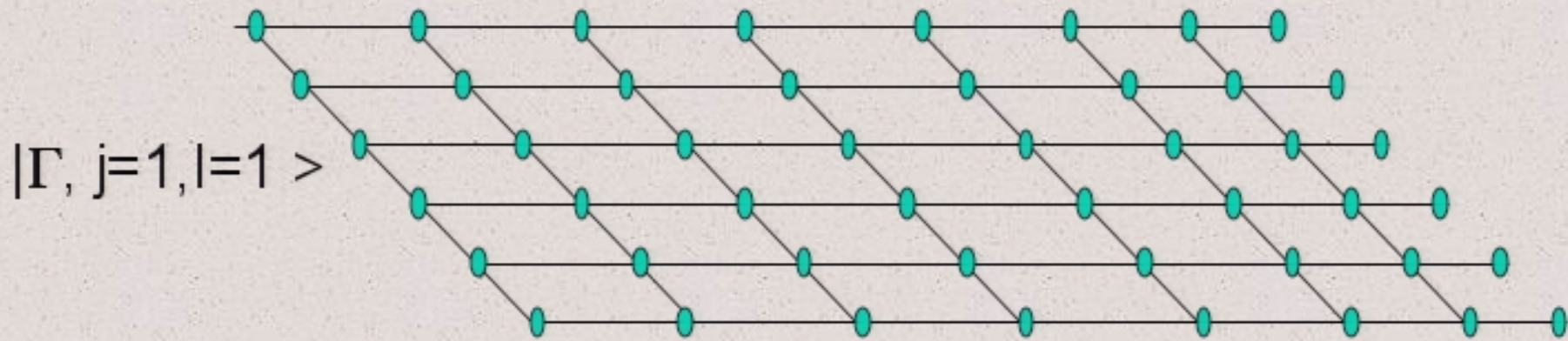
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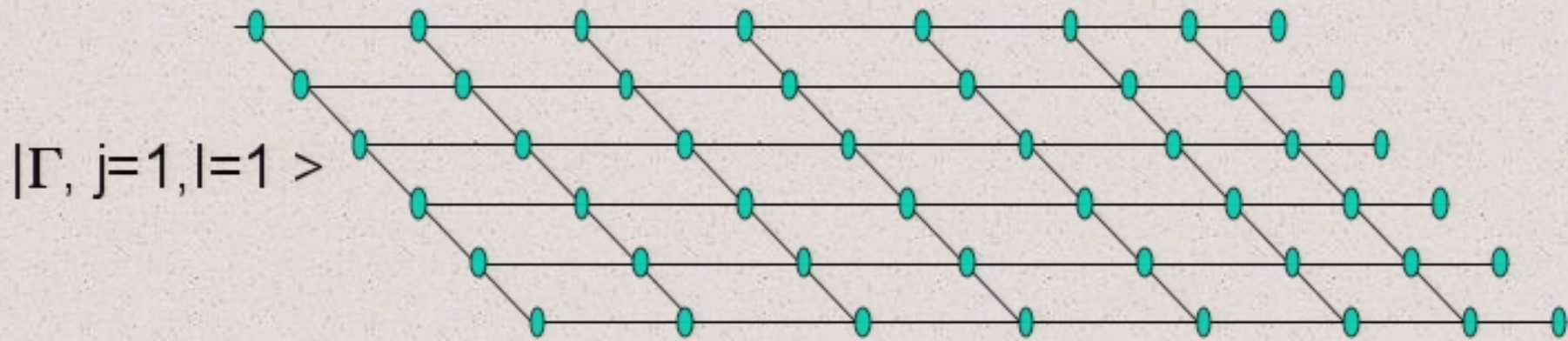
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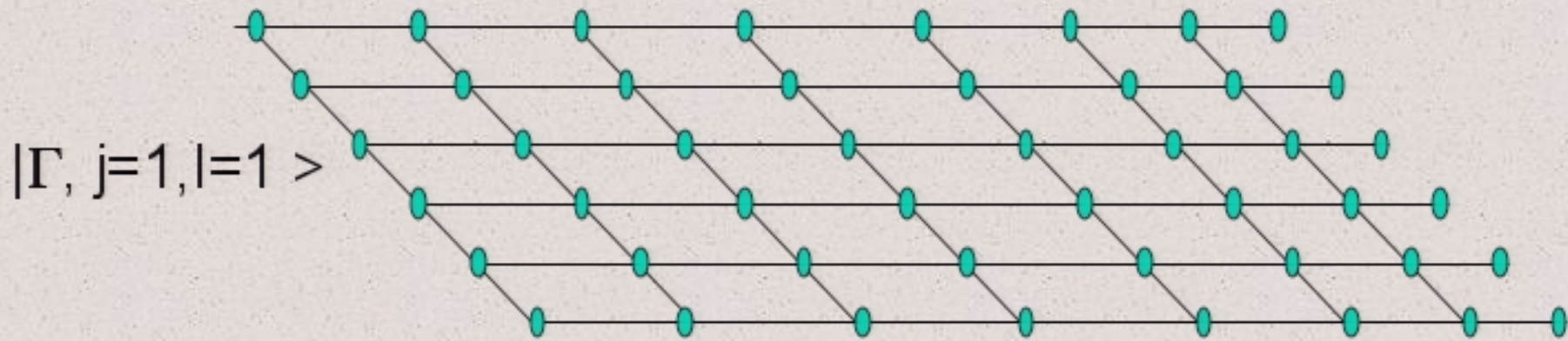
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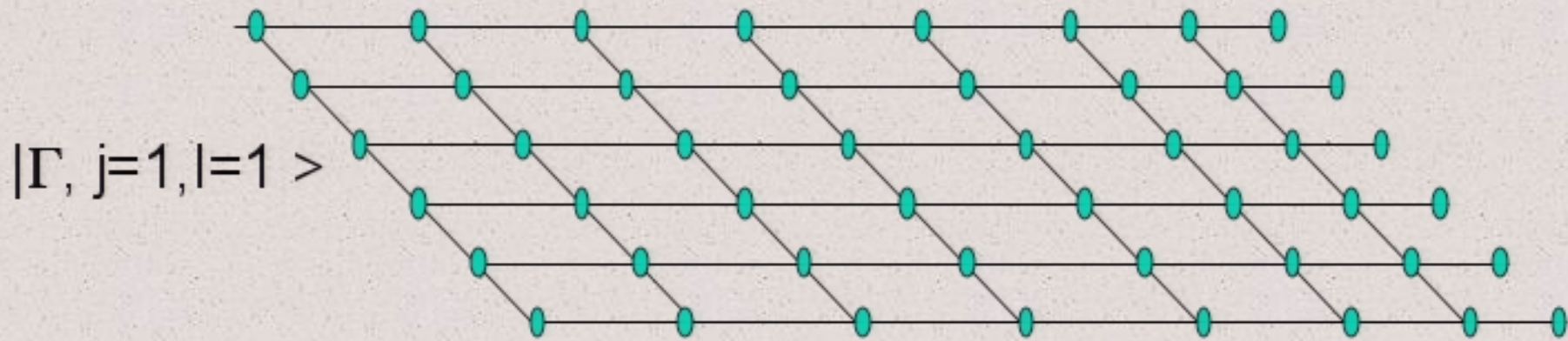
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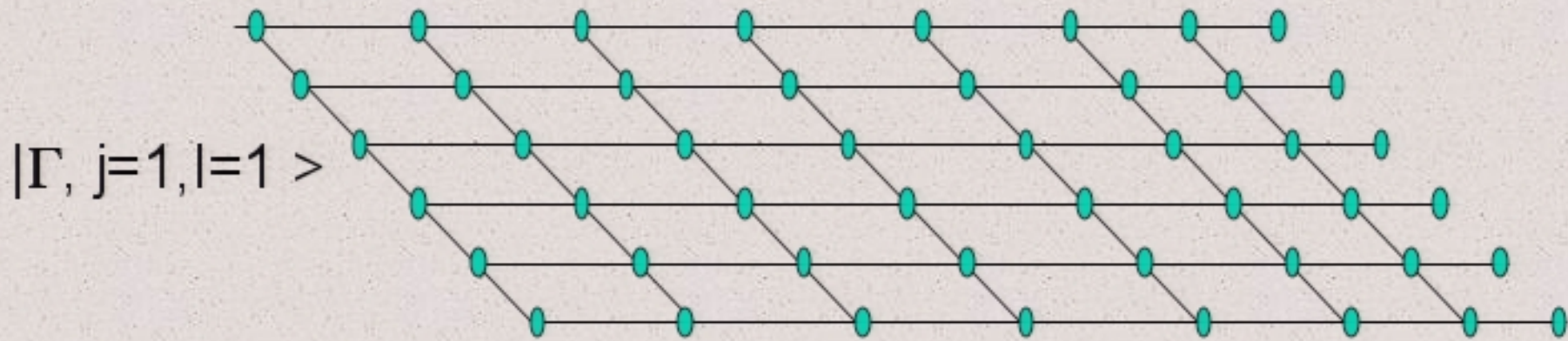
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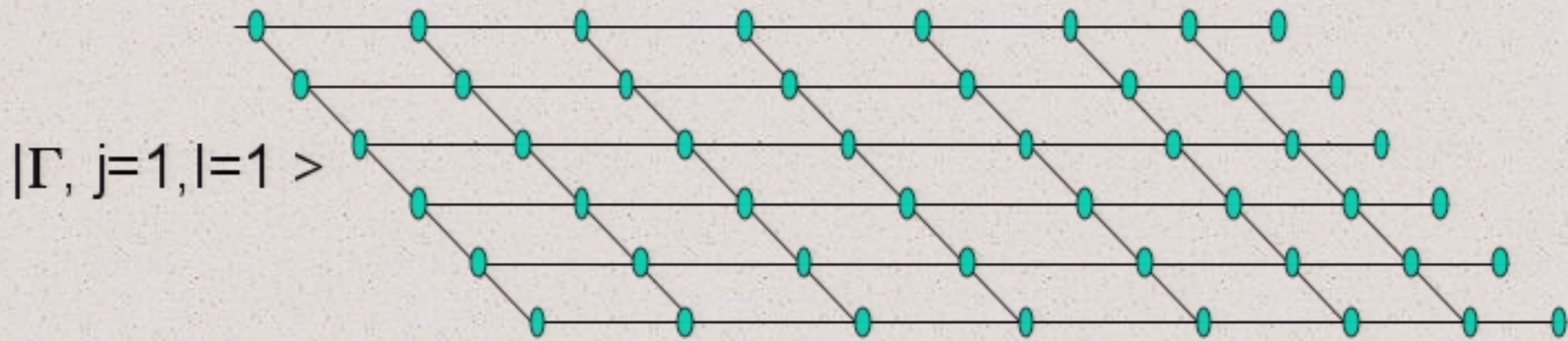
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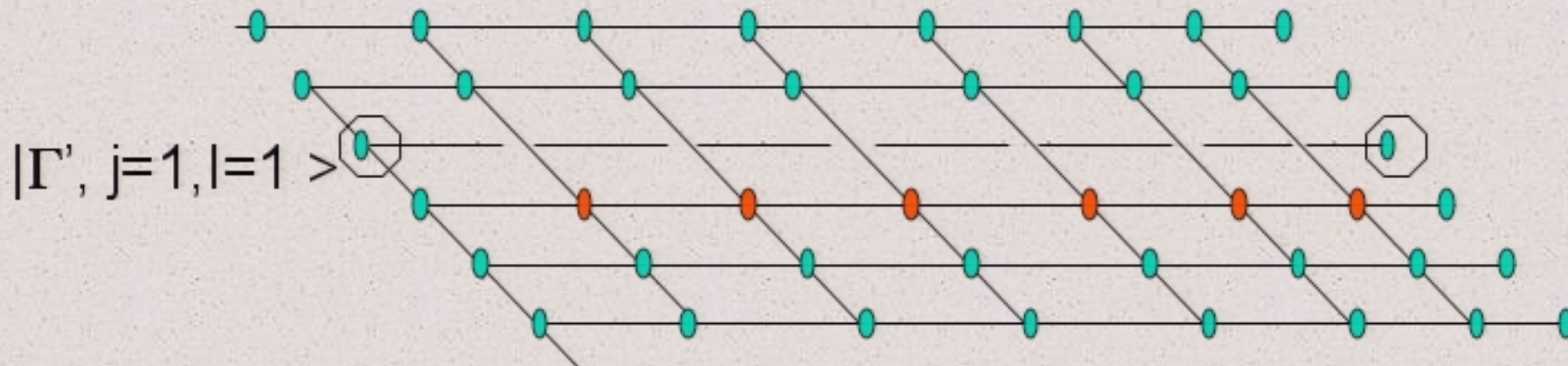
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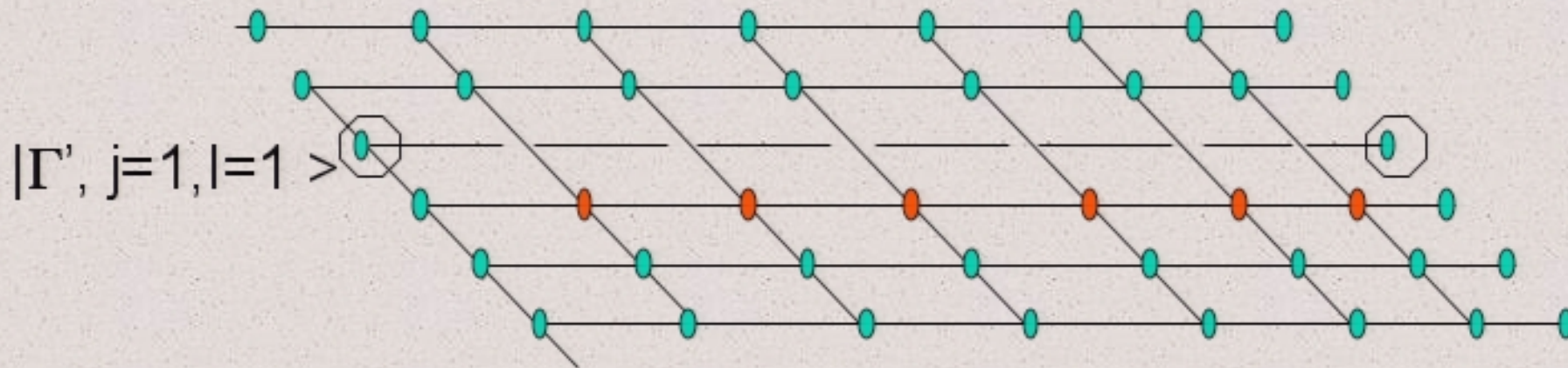
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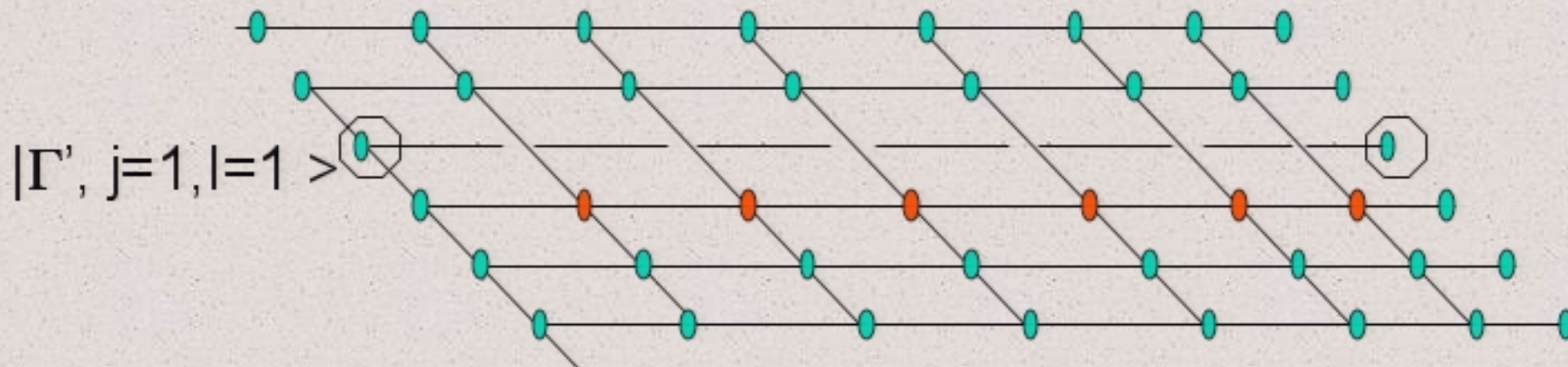
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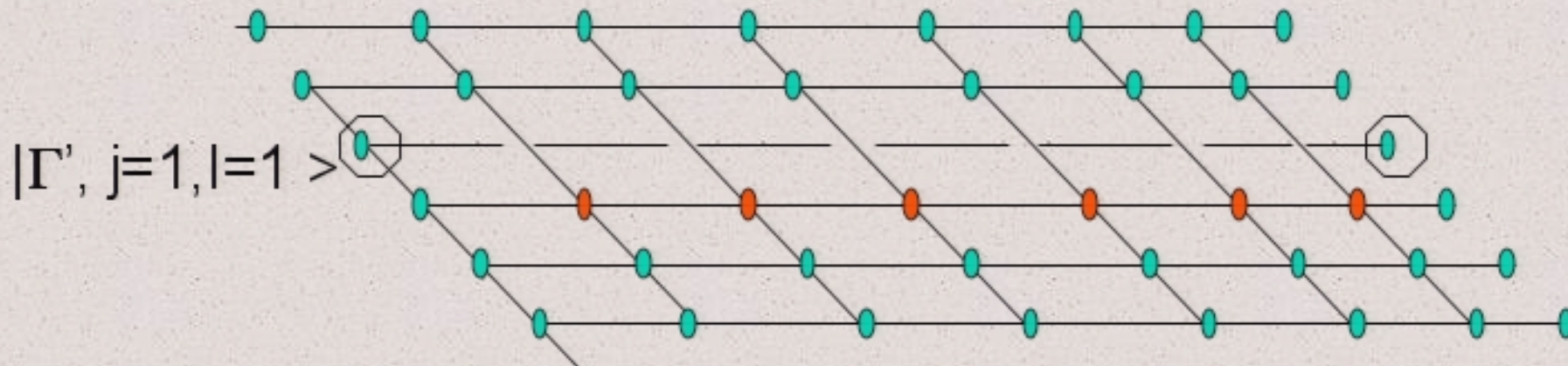
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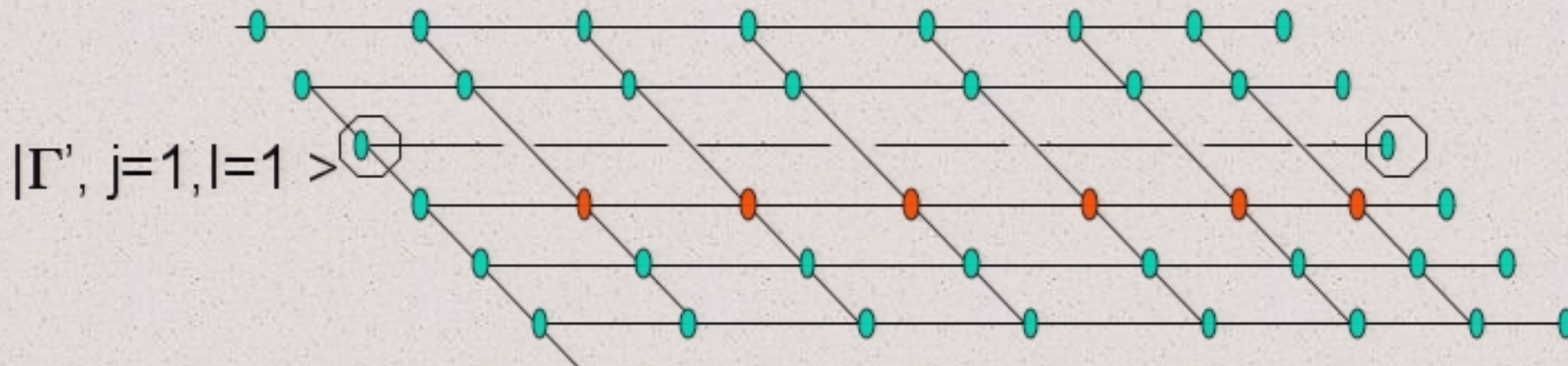
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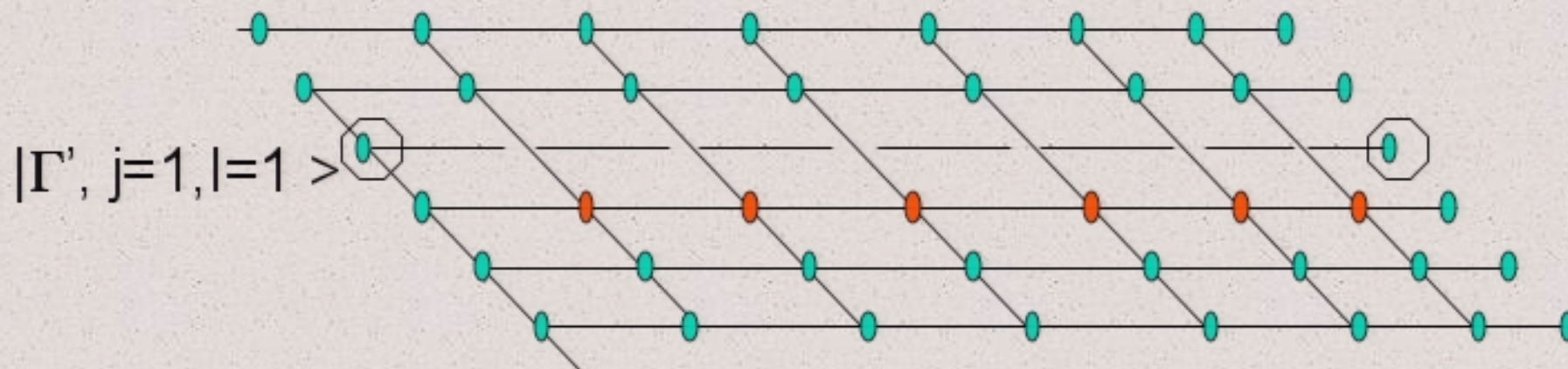
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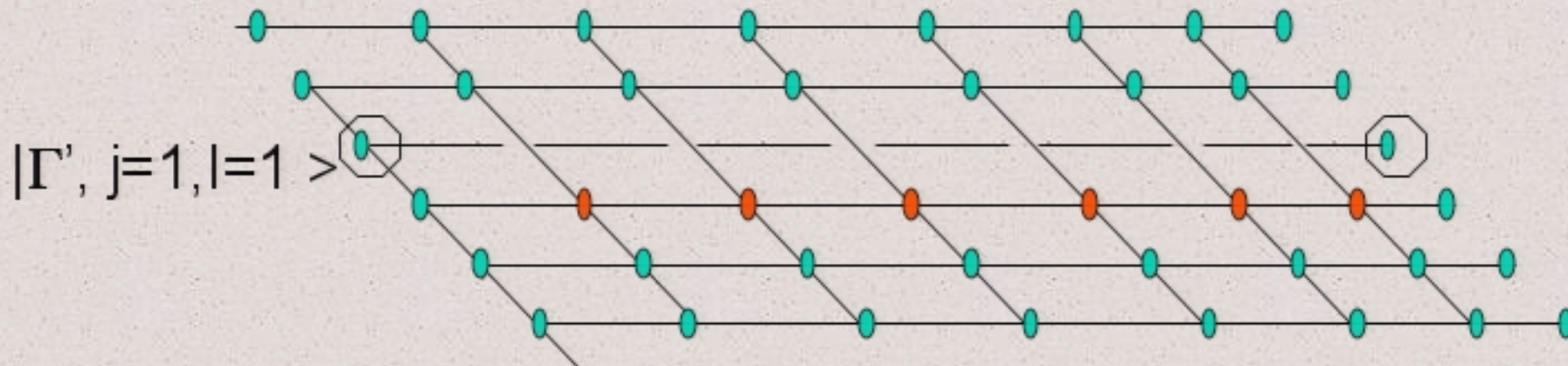
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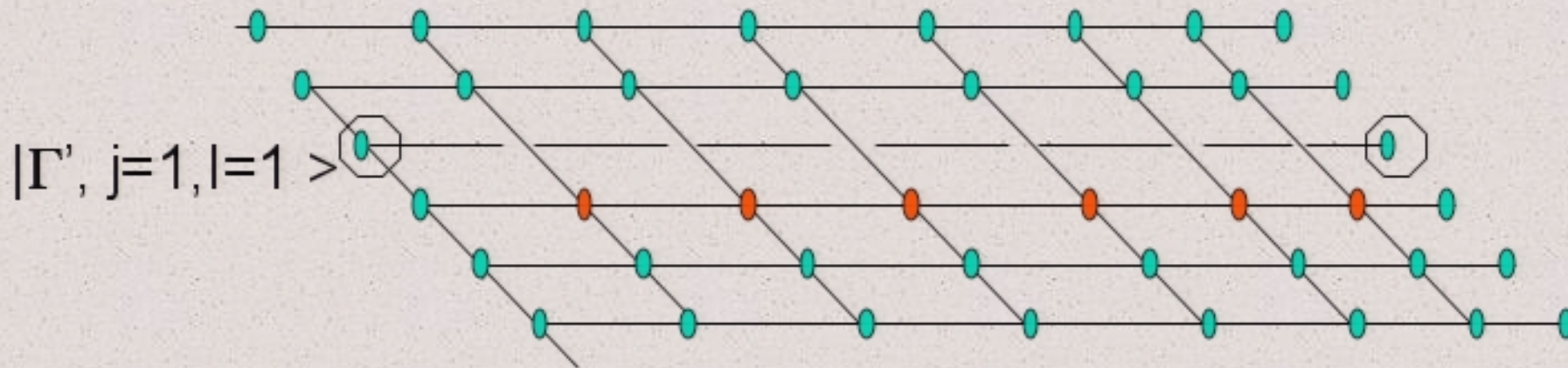
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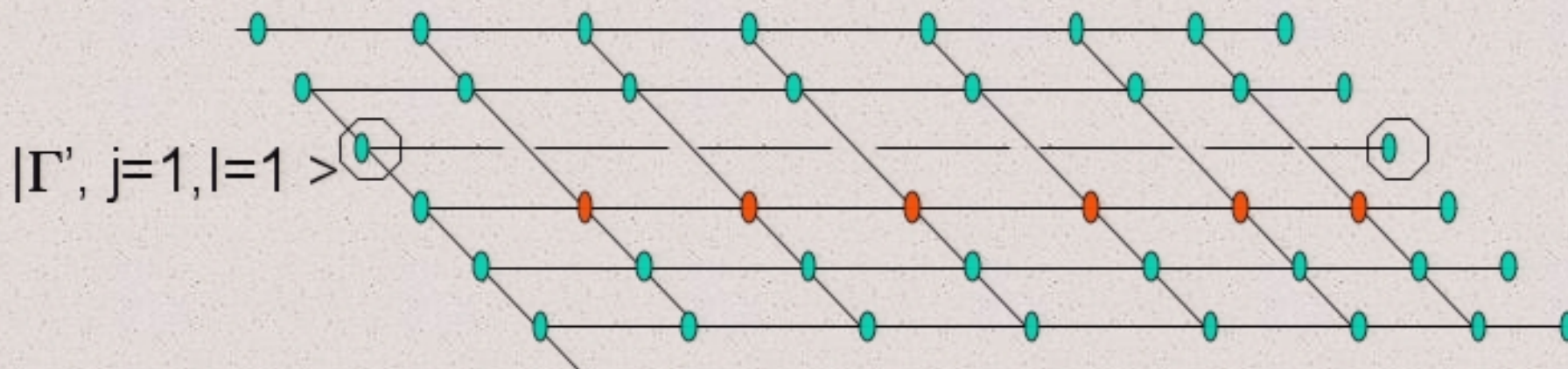
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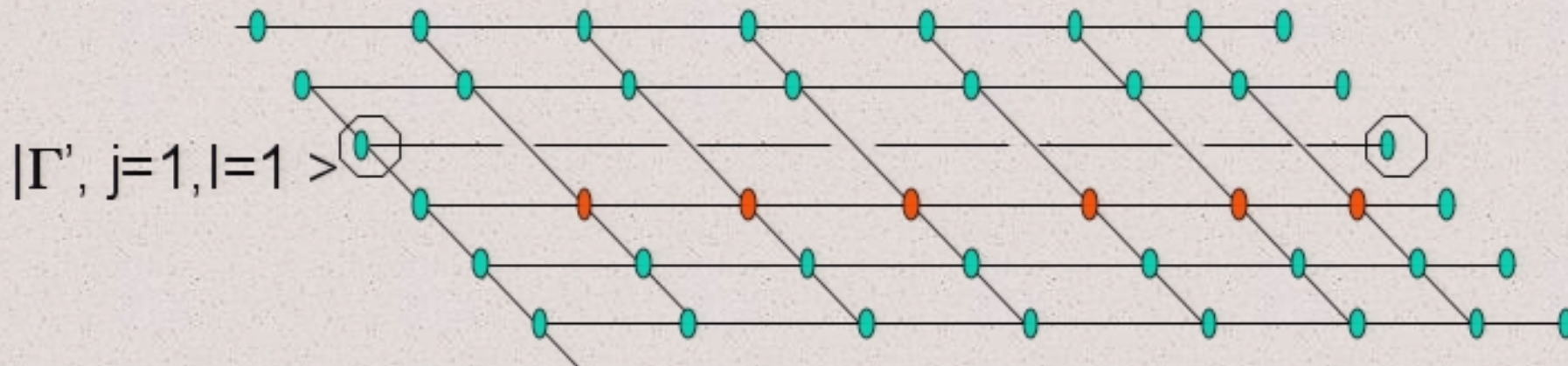
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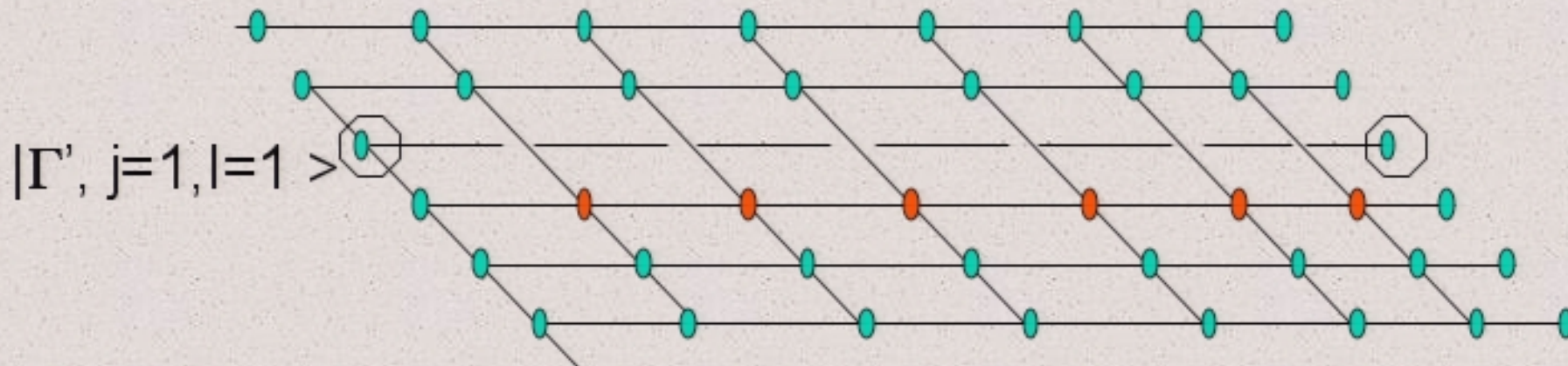
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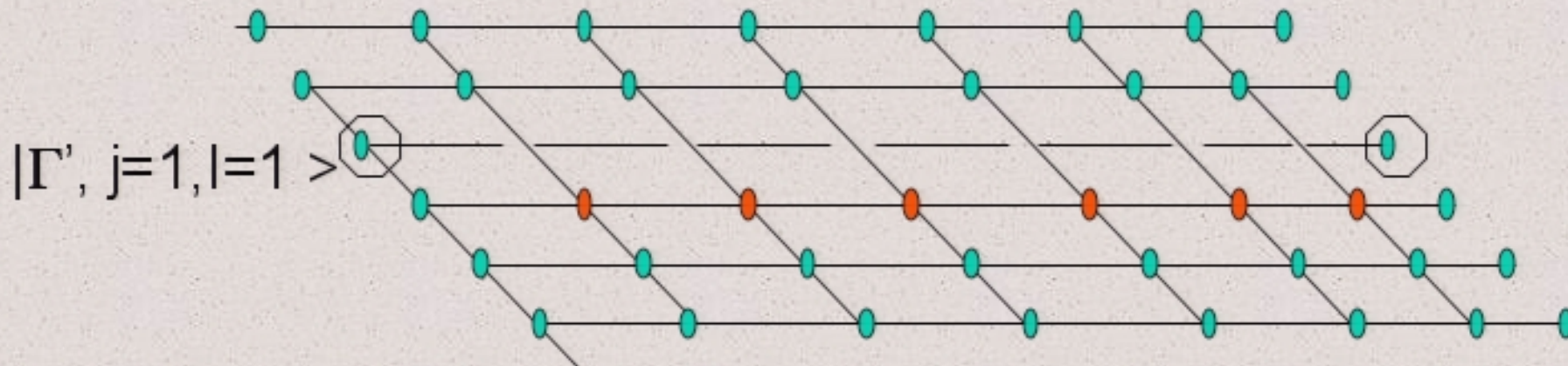
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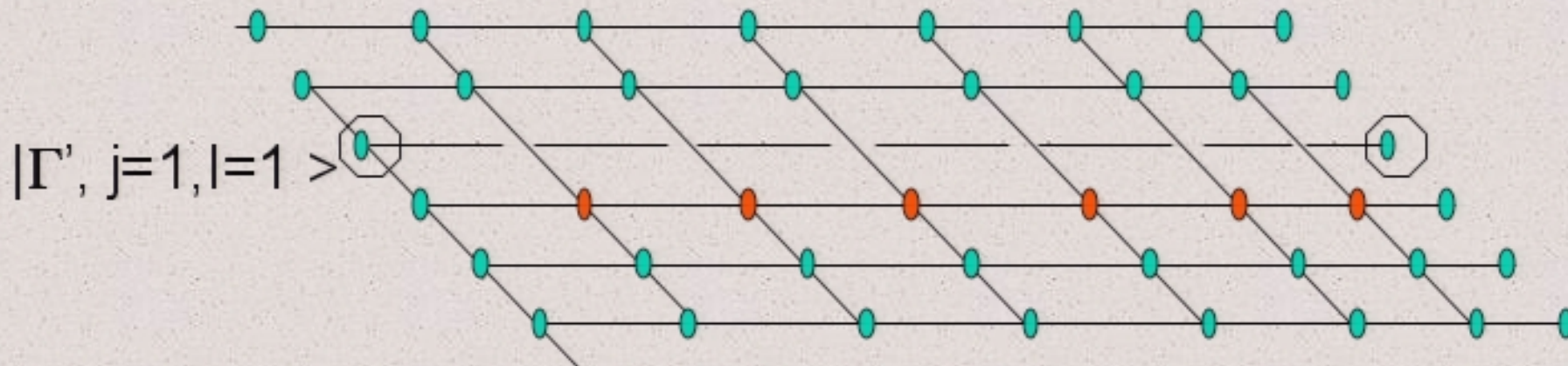
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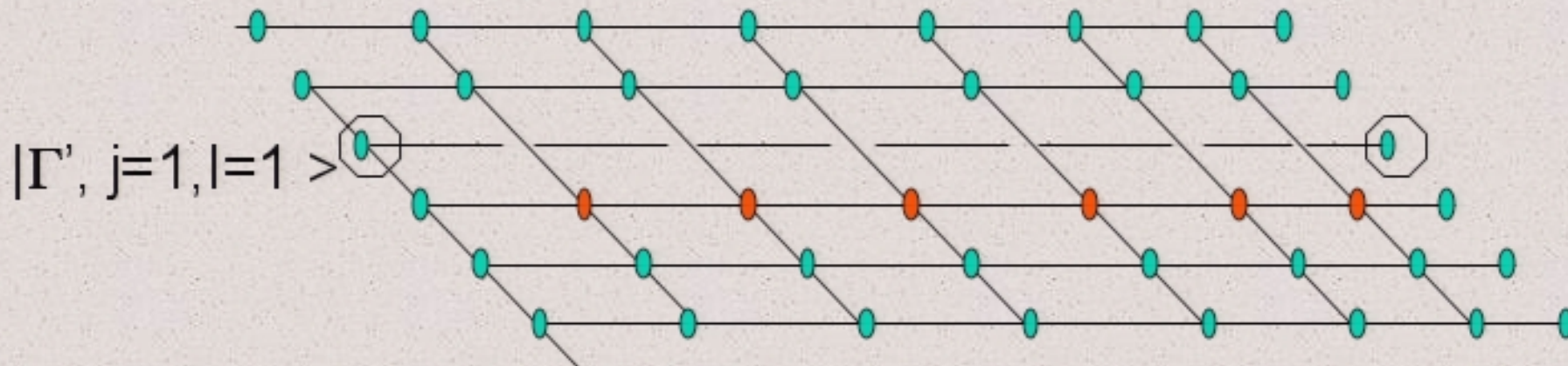
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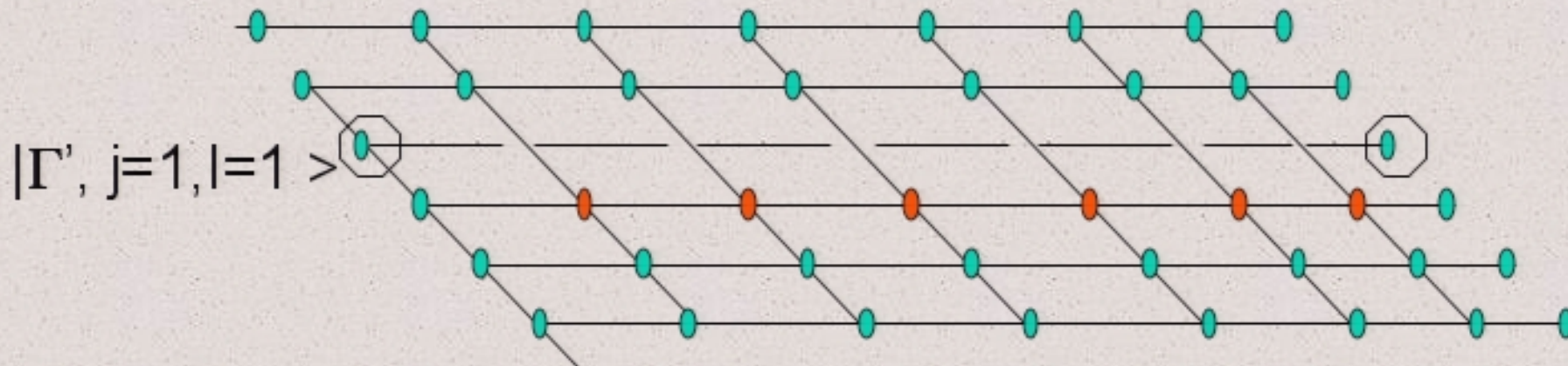
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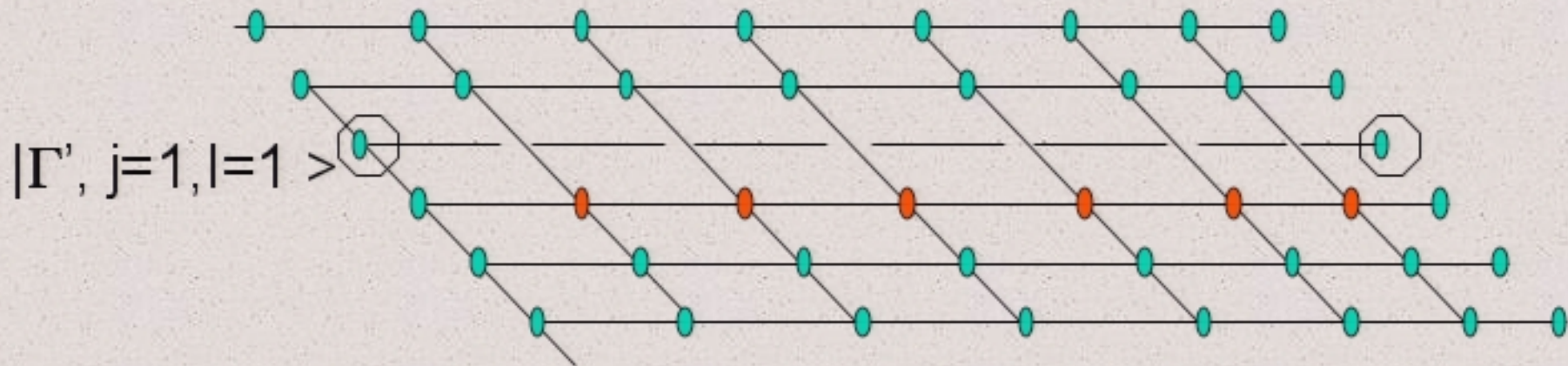
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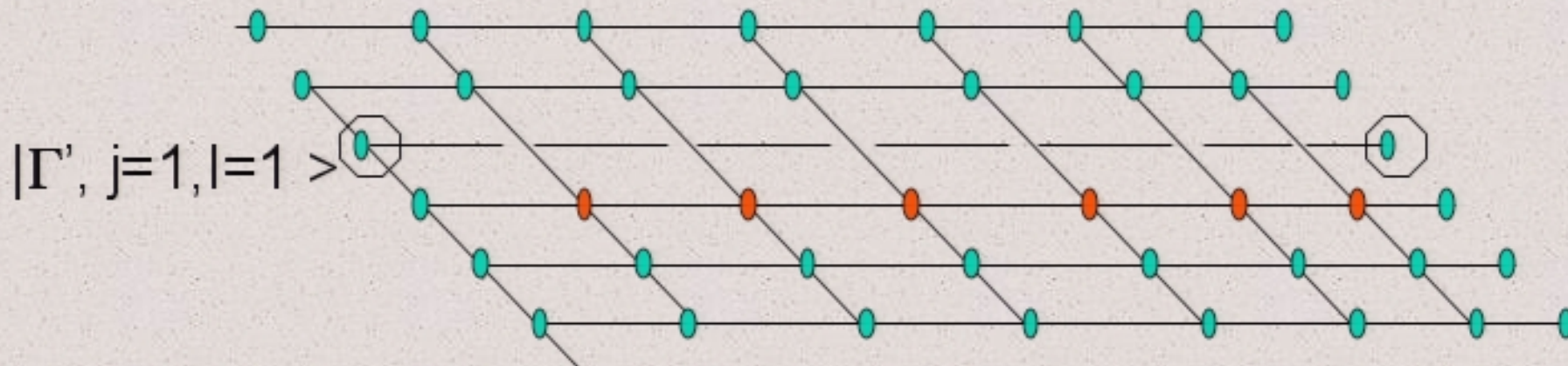
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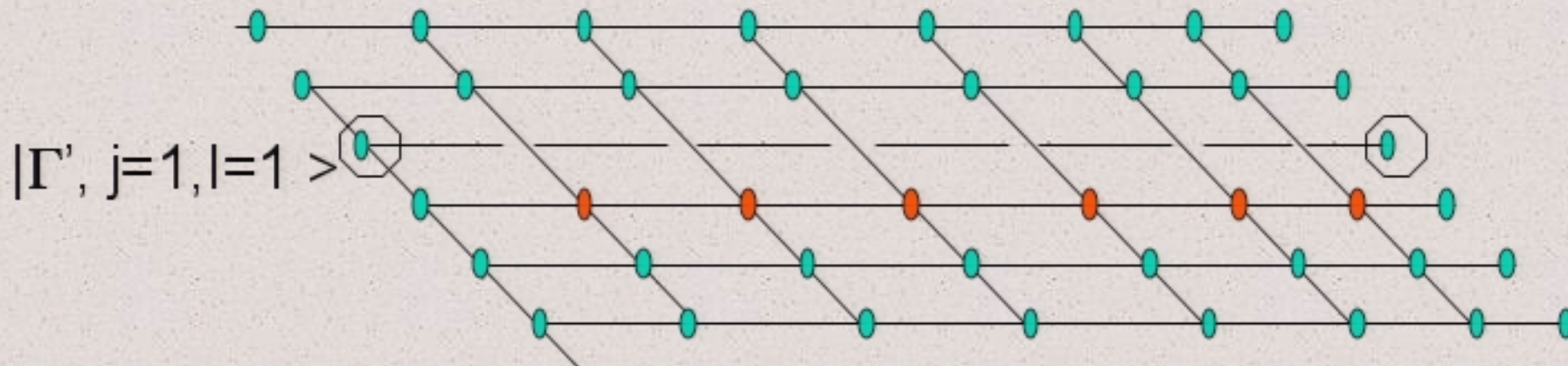
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So the weave conditions do not imply locality.

There seems nothing that guarantees that microscopic locality defined by the connectivity of a given spinnet goes over into locality of a semiclassical or coherent state from which classical geometry would emerge.

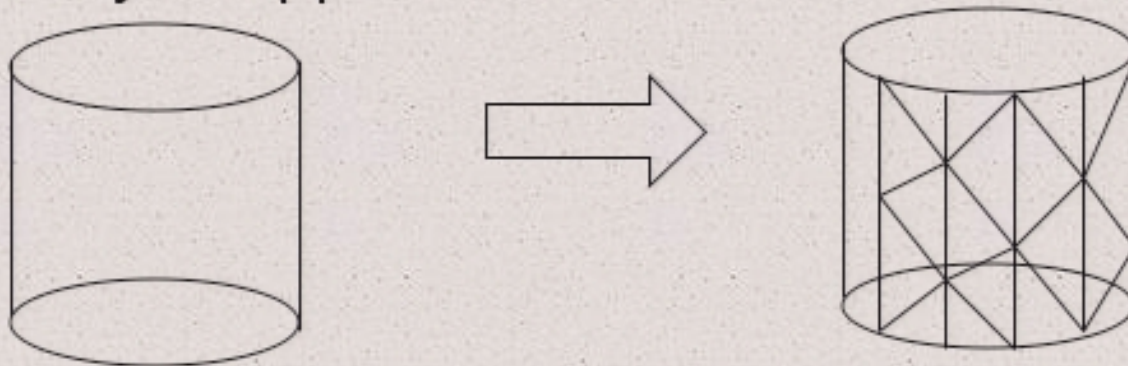
Similarly there is nothing that seems to guarantee that causality of spin foams goes over to causal structure of classical spacetime in the low energy limit.

Furthermore, there is a problem suppressing non-local links, as there are potentially so many more of them.

This is the inverse problem.

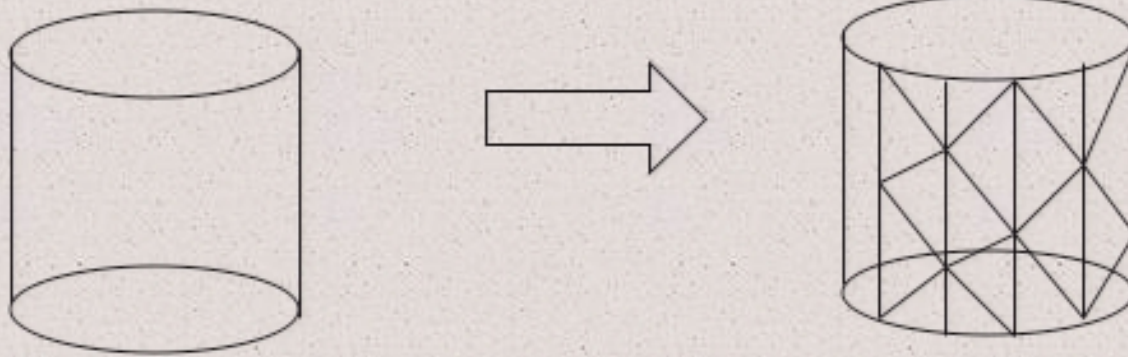
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Its easy to approximate smooth fields with discrete structures.



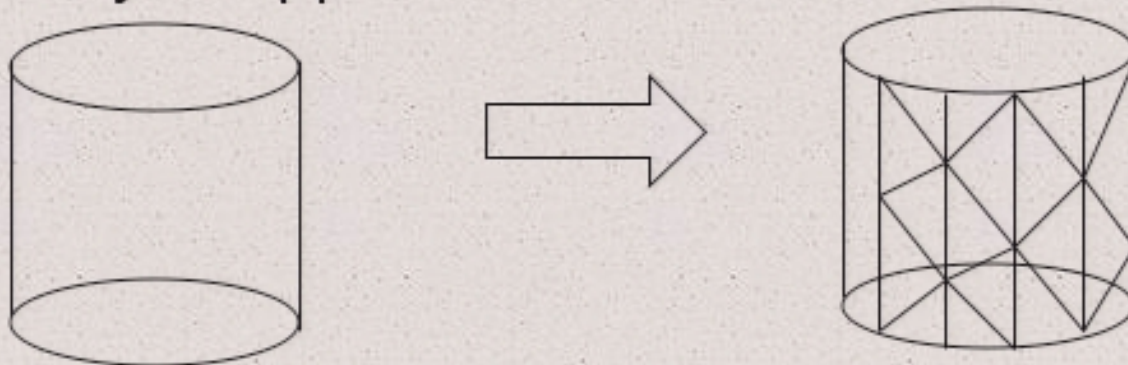
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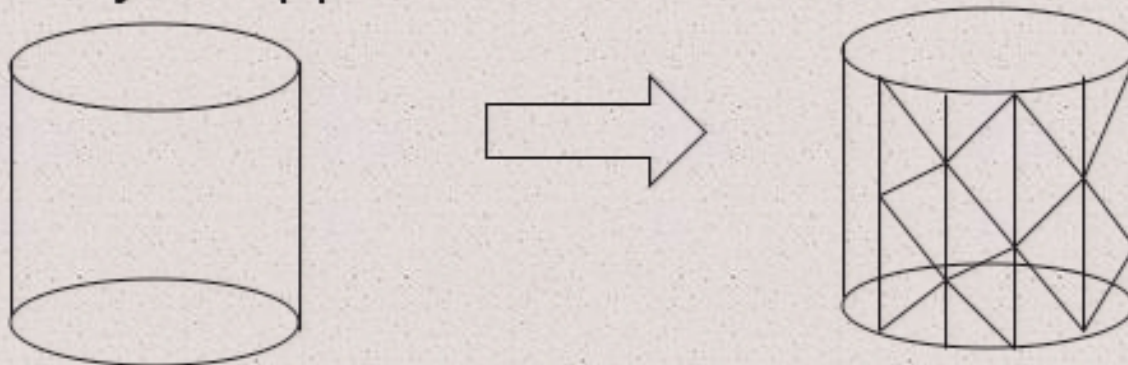
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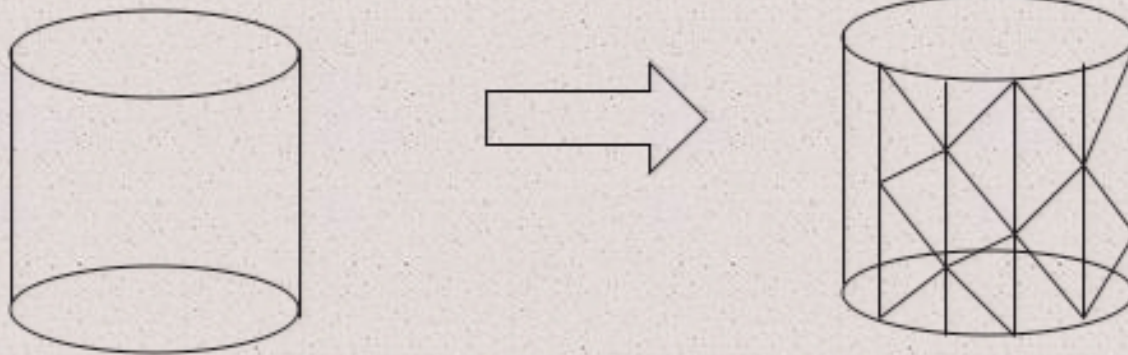
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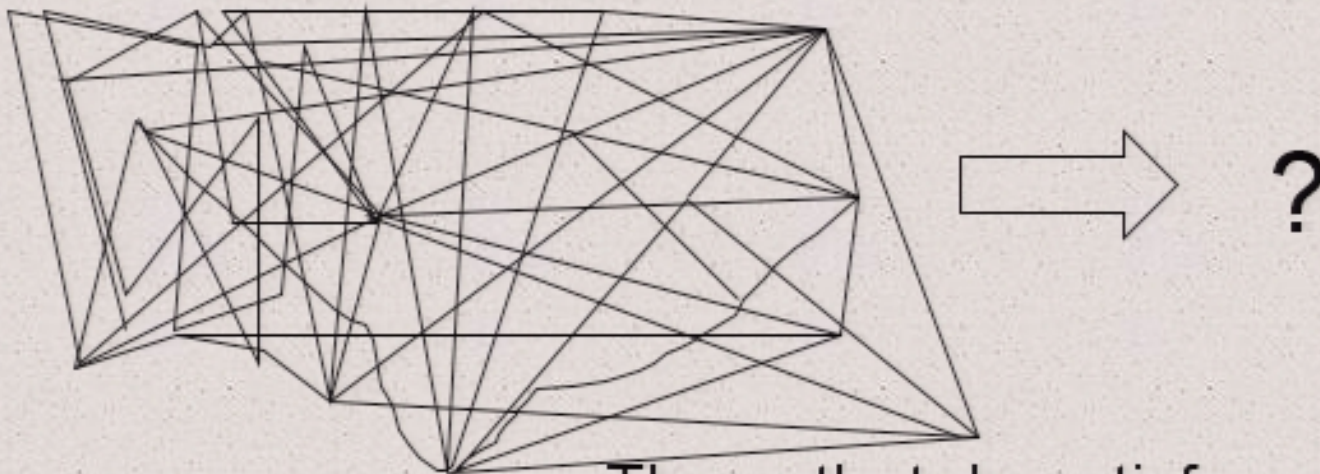


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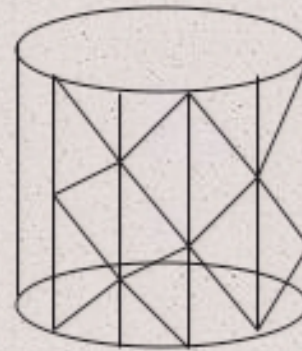
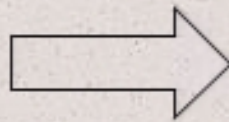
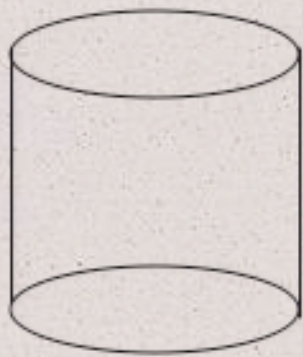
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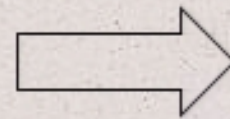
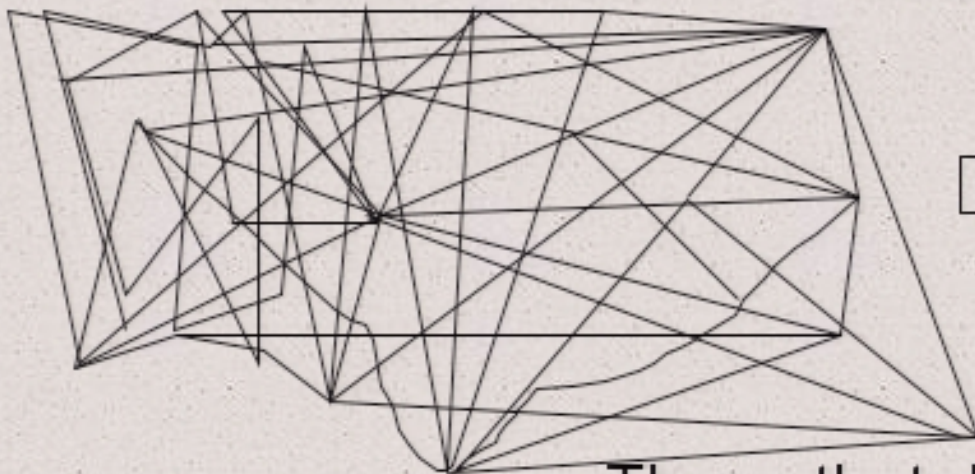
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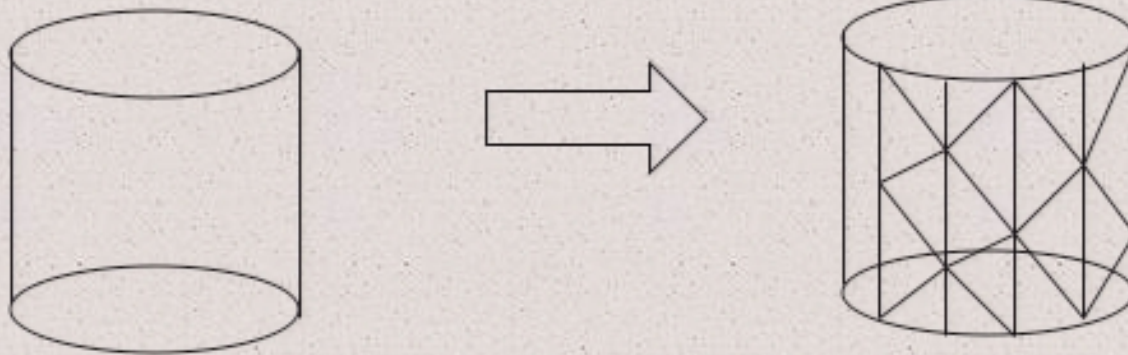


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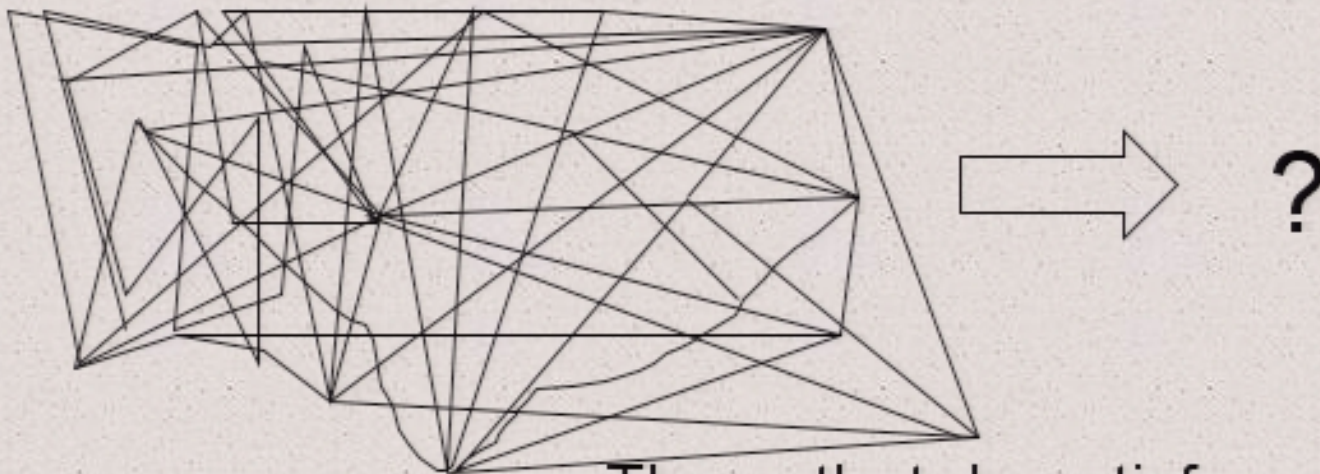
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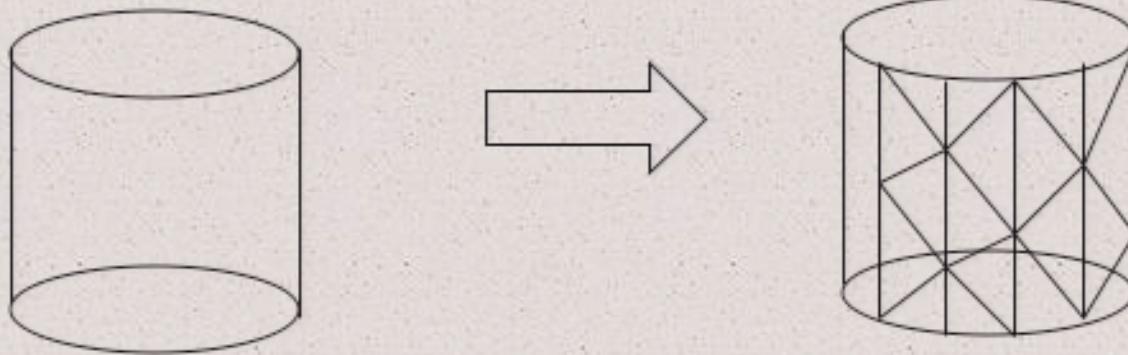
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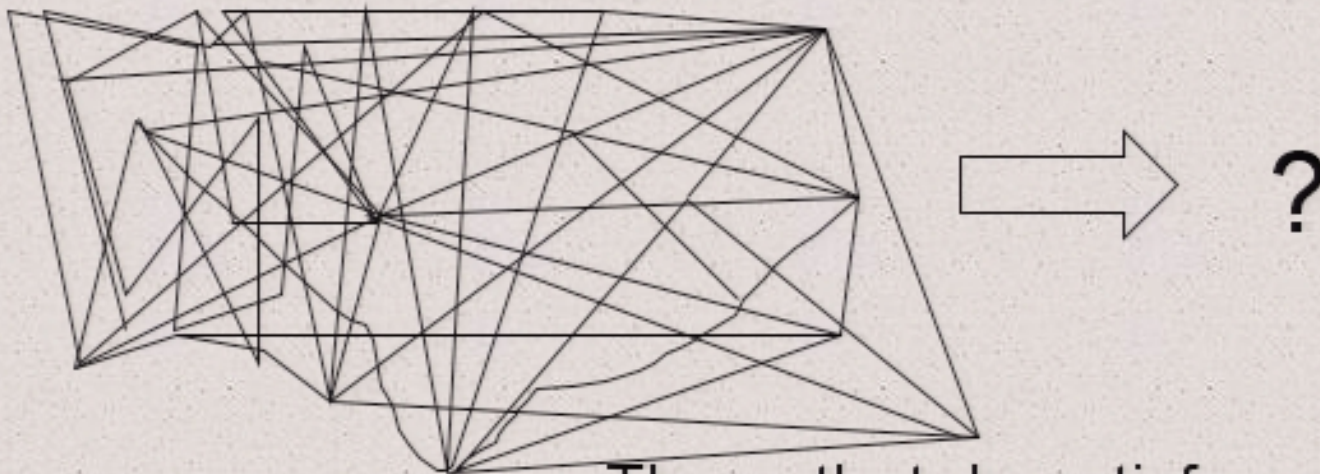
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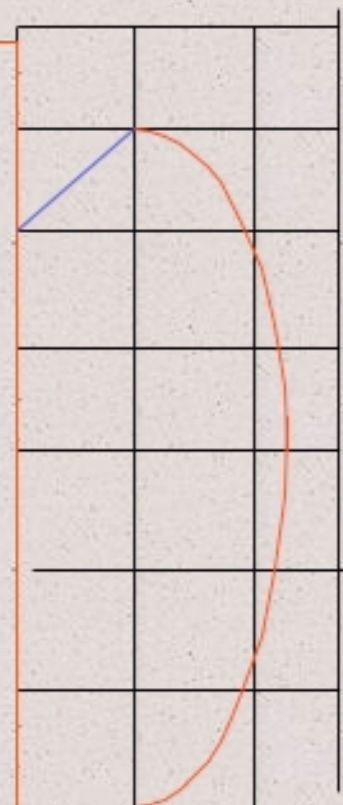
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Does it conflict with the locality of the embedding?

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Thus, if the low energy definition of locality comes from a coarse graining of a combinatorial graph, it will be easily violated in fluctuations.



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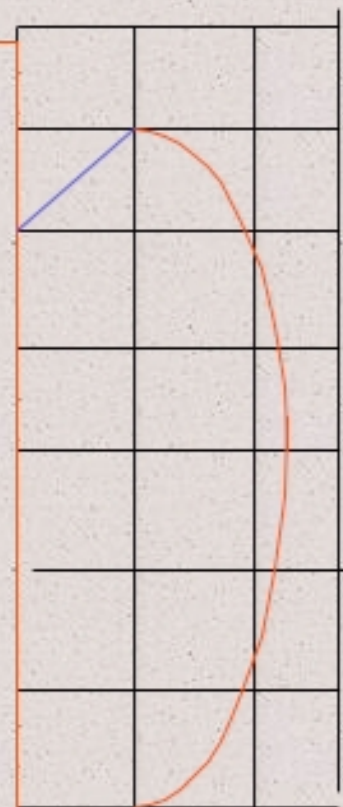
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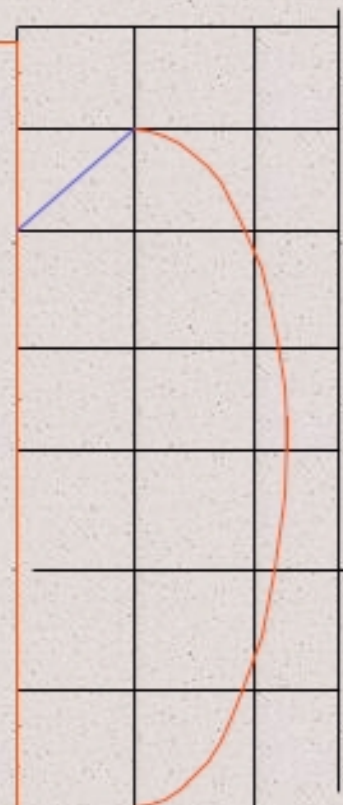
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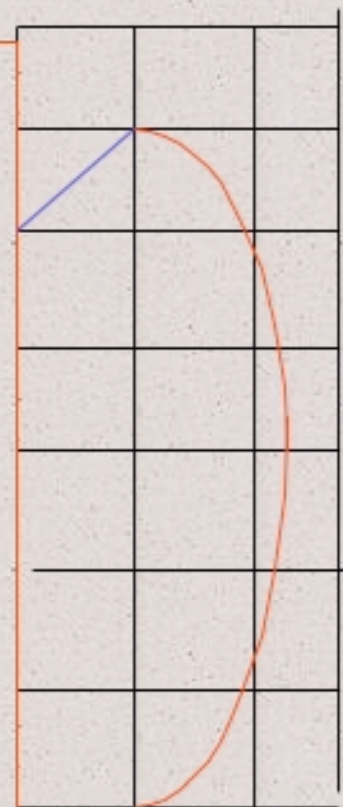
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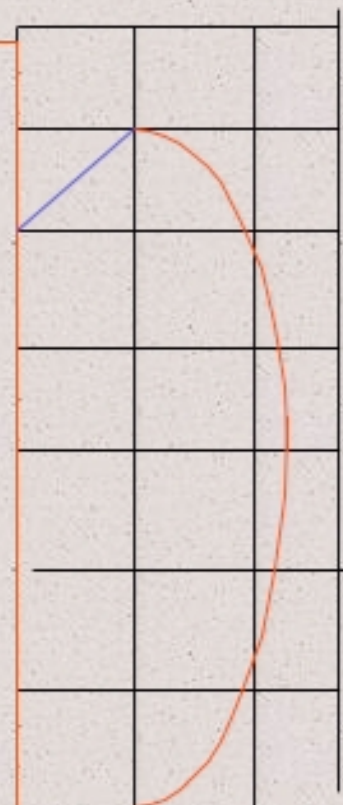
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But, almost no causal set approximates a low dimensional classical spacetime.
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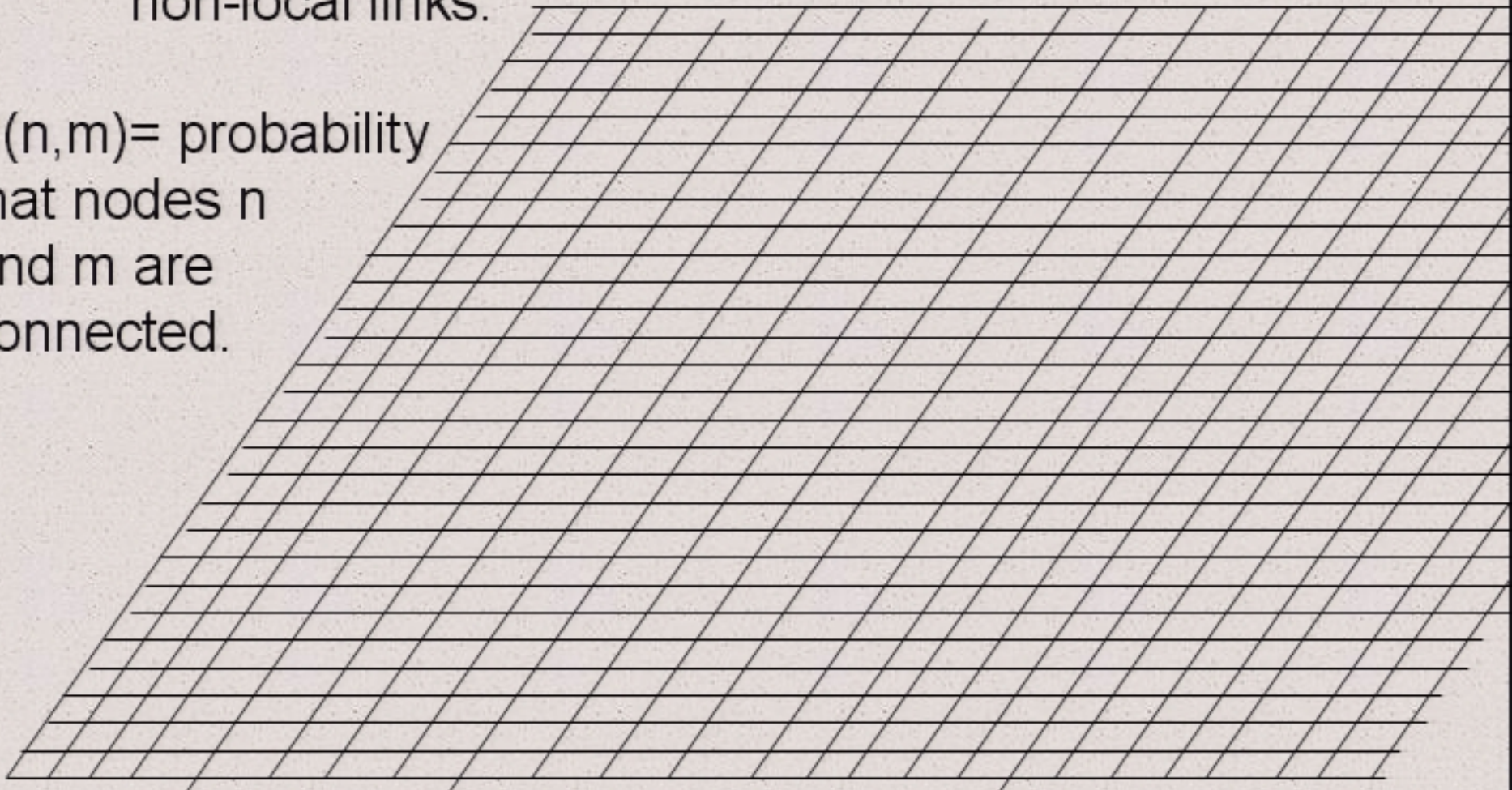
3. Learn to live with non-locality!!

Could non-locality be all around us?

We have been studying a model of non-locality in discrete spacetime models such as LQG:

A regular lattice or weave with a random distribution of non-local links.

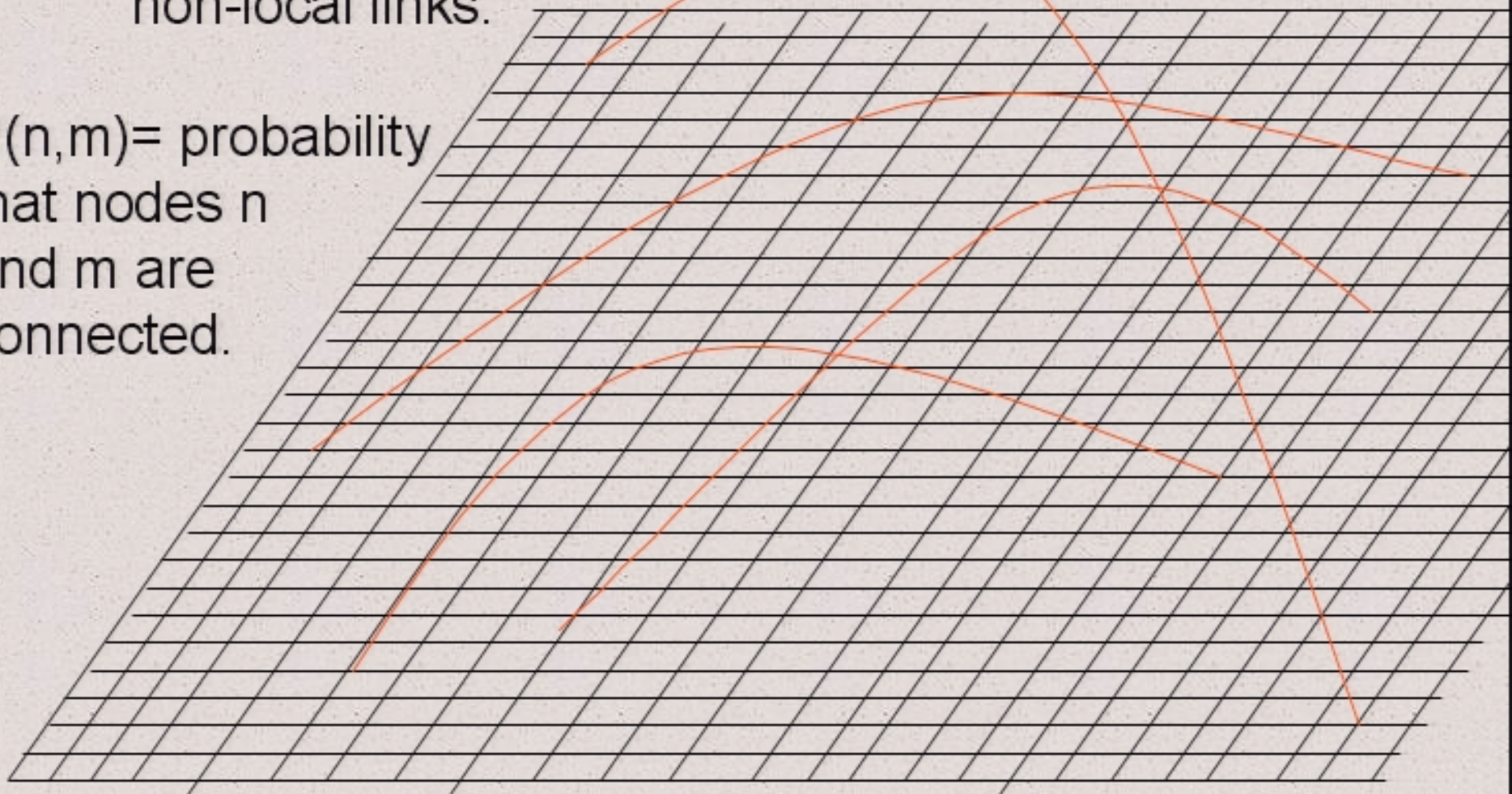
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We have found so far four applications of such a conflict between micro and macro locality:

1. matter fields from gauge fields + non-locality
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A spin network with a non-local link

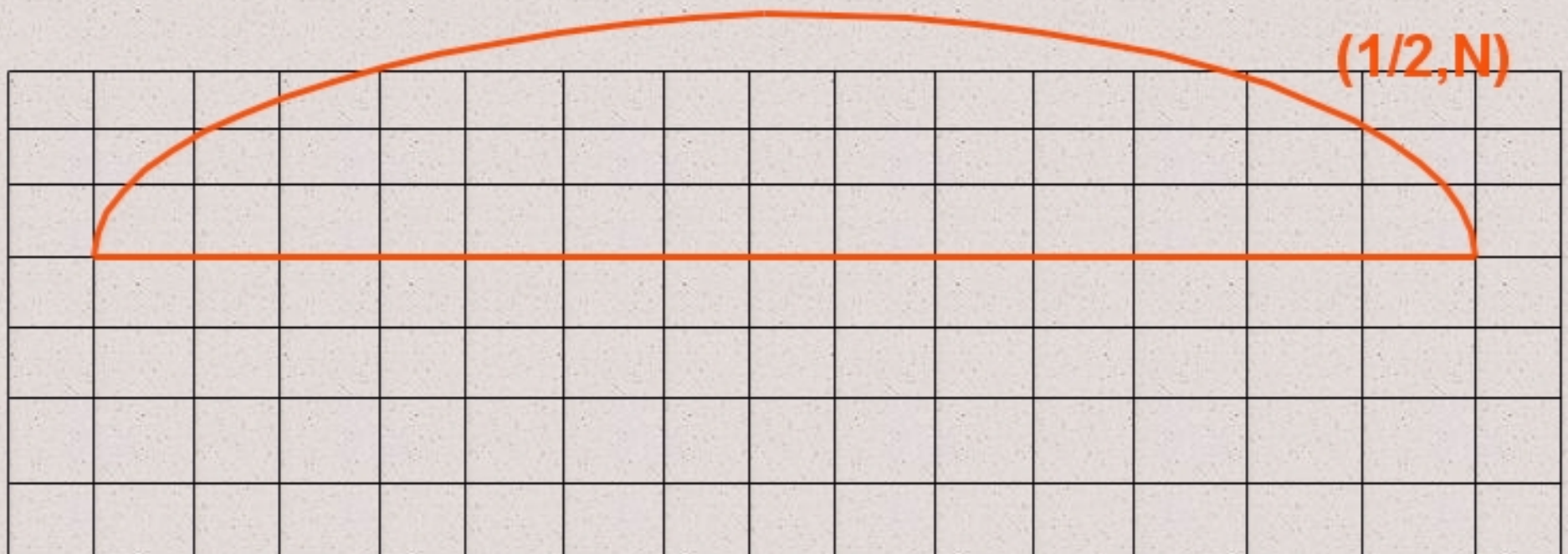
1/2



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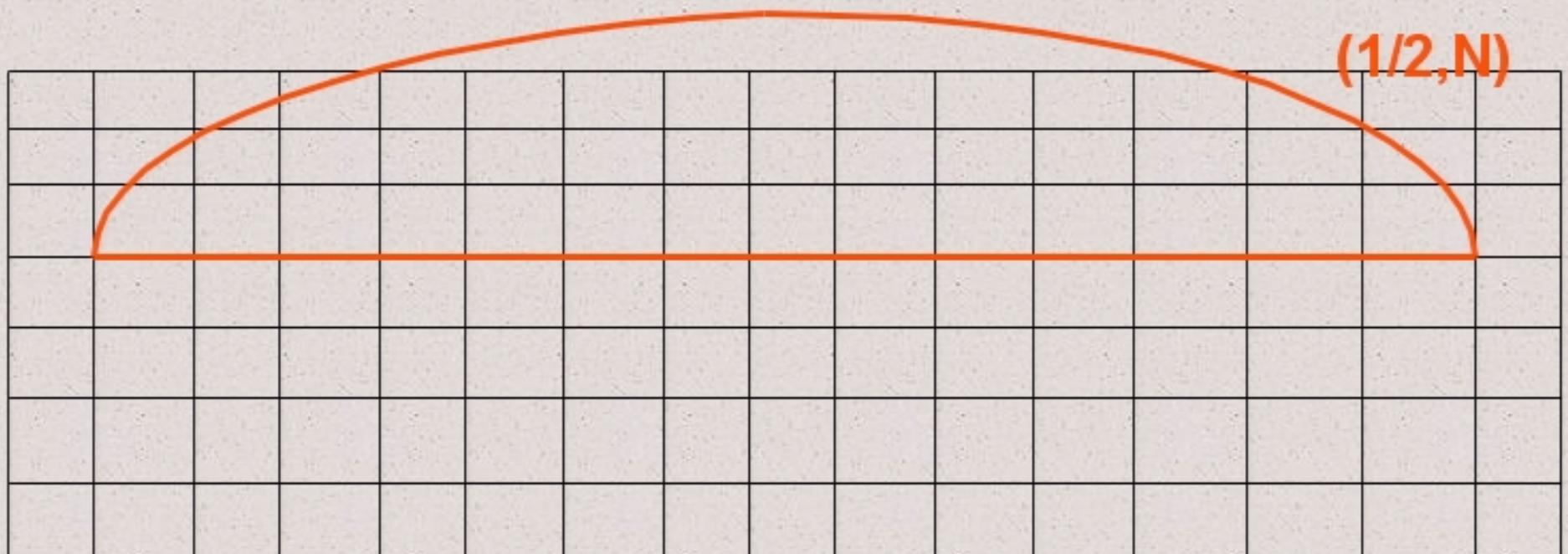
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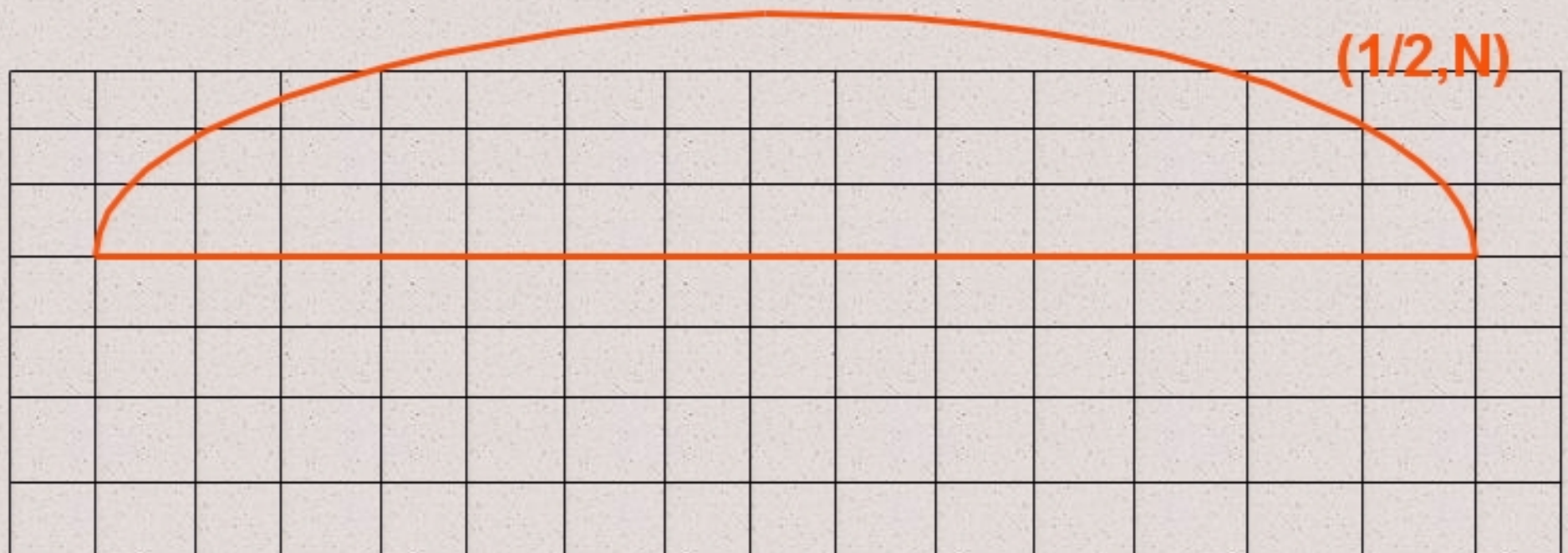
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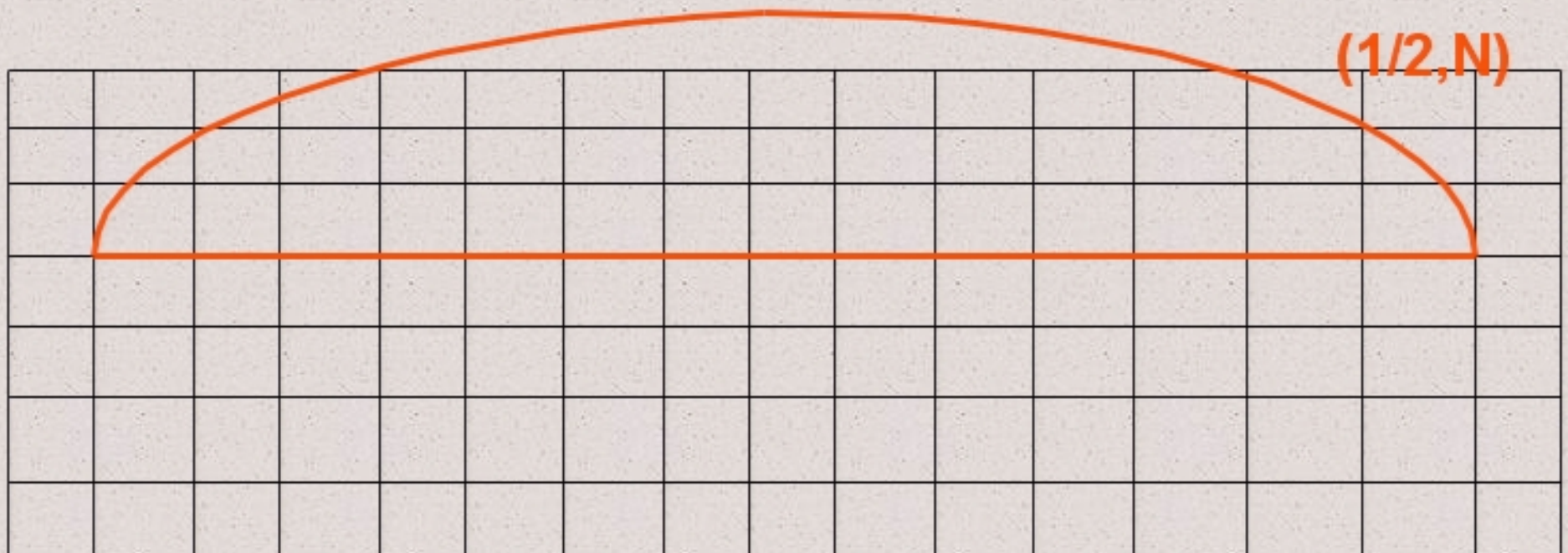
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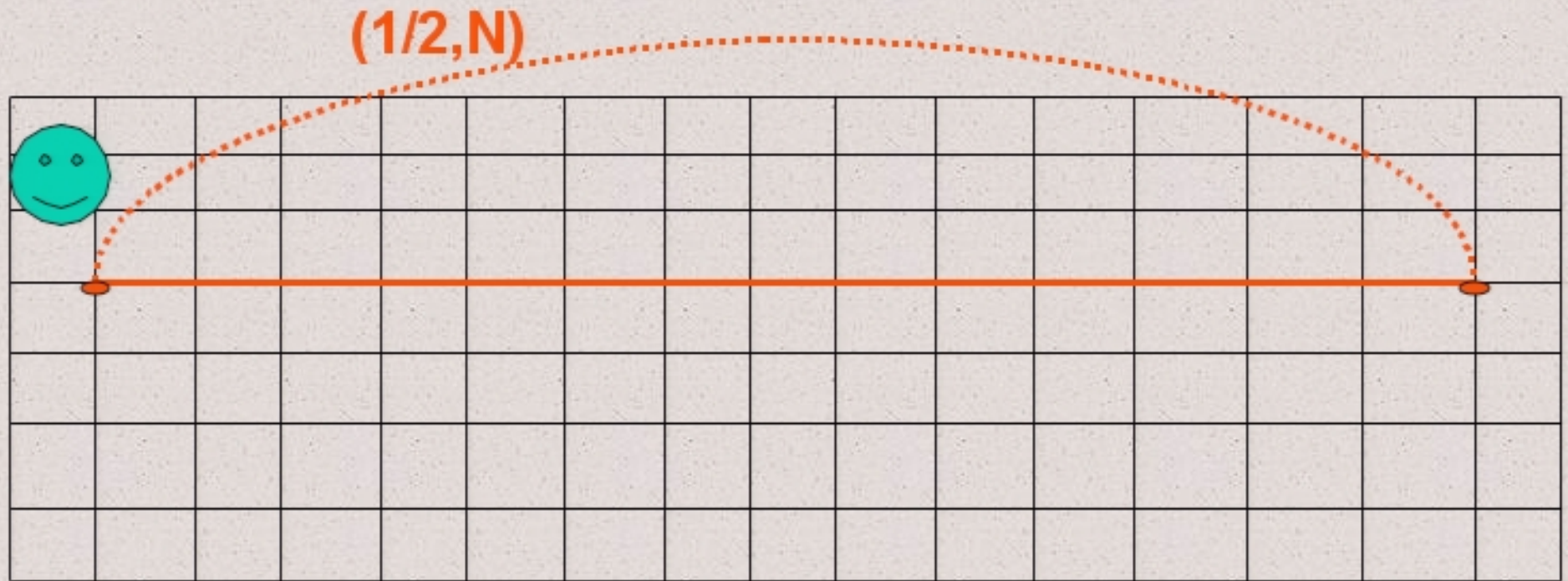
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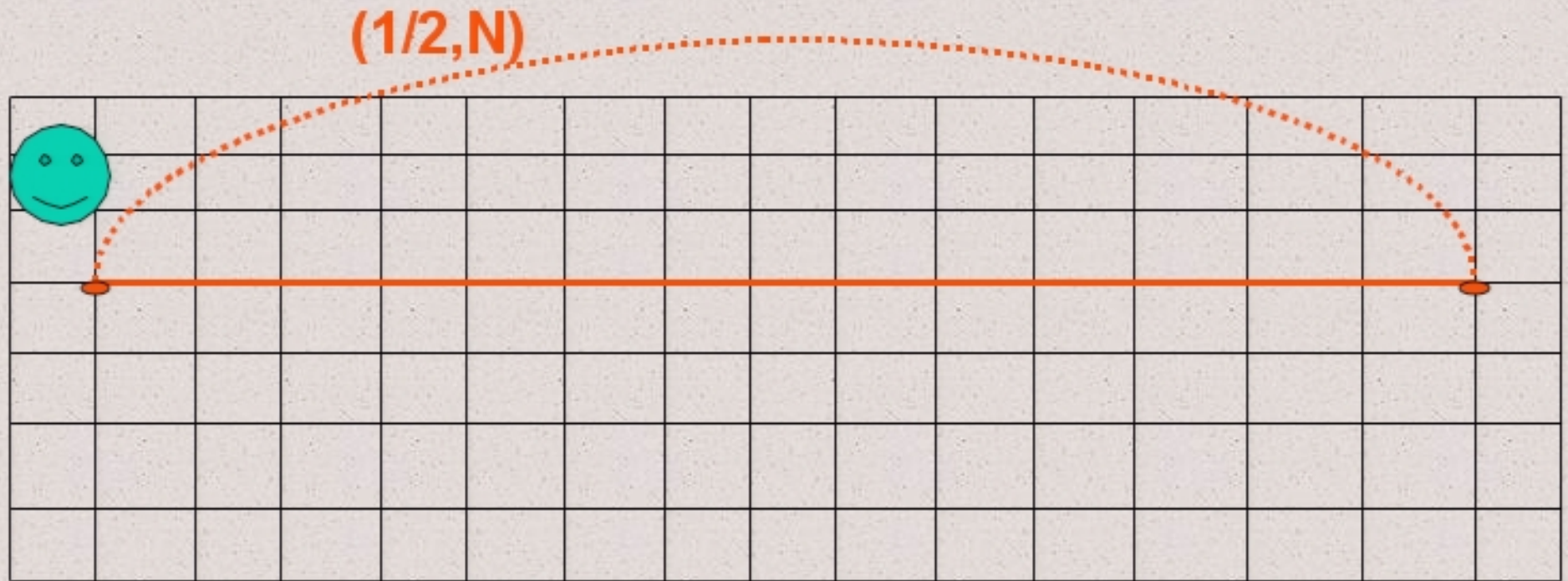
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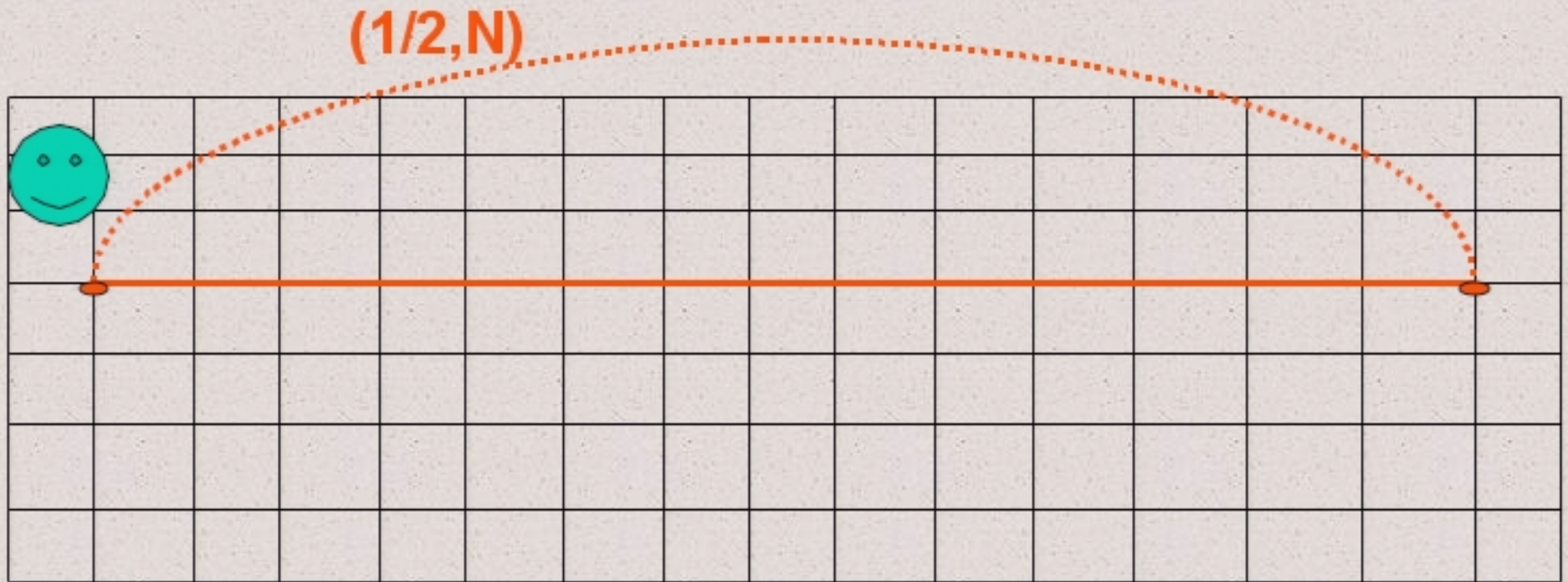
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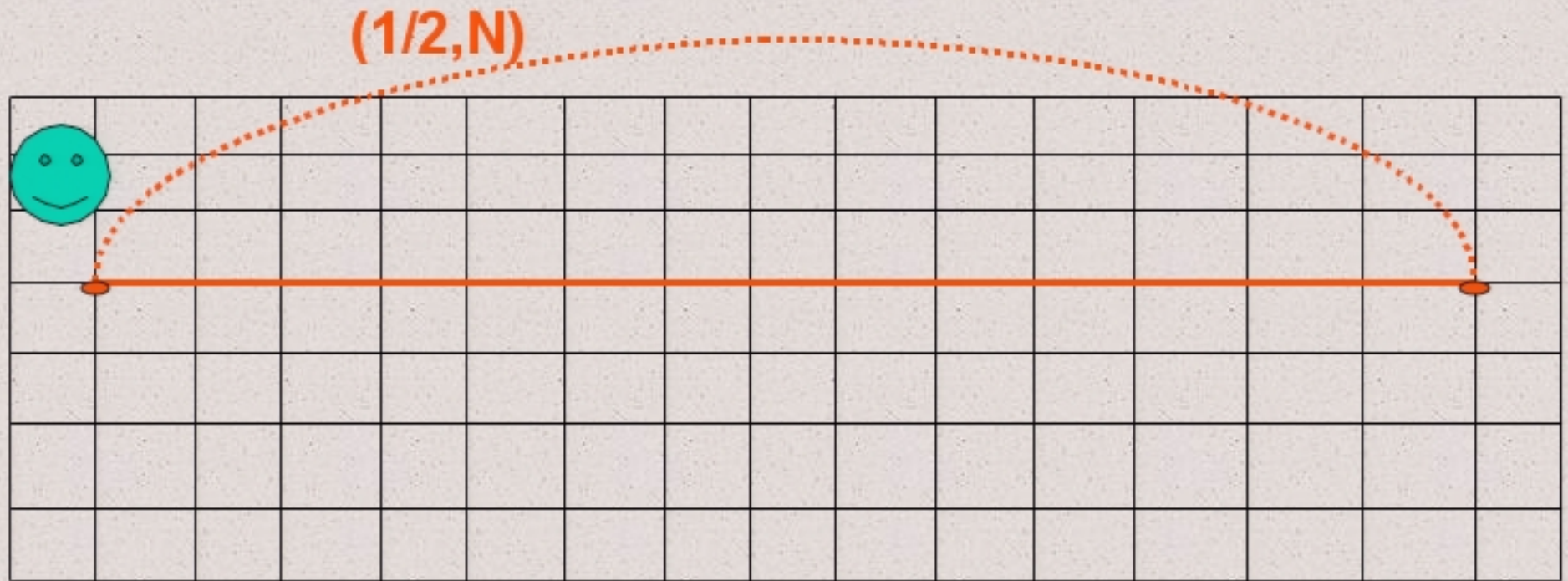
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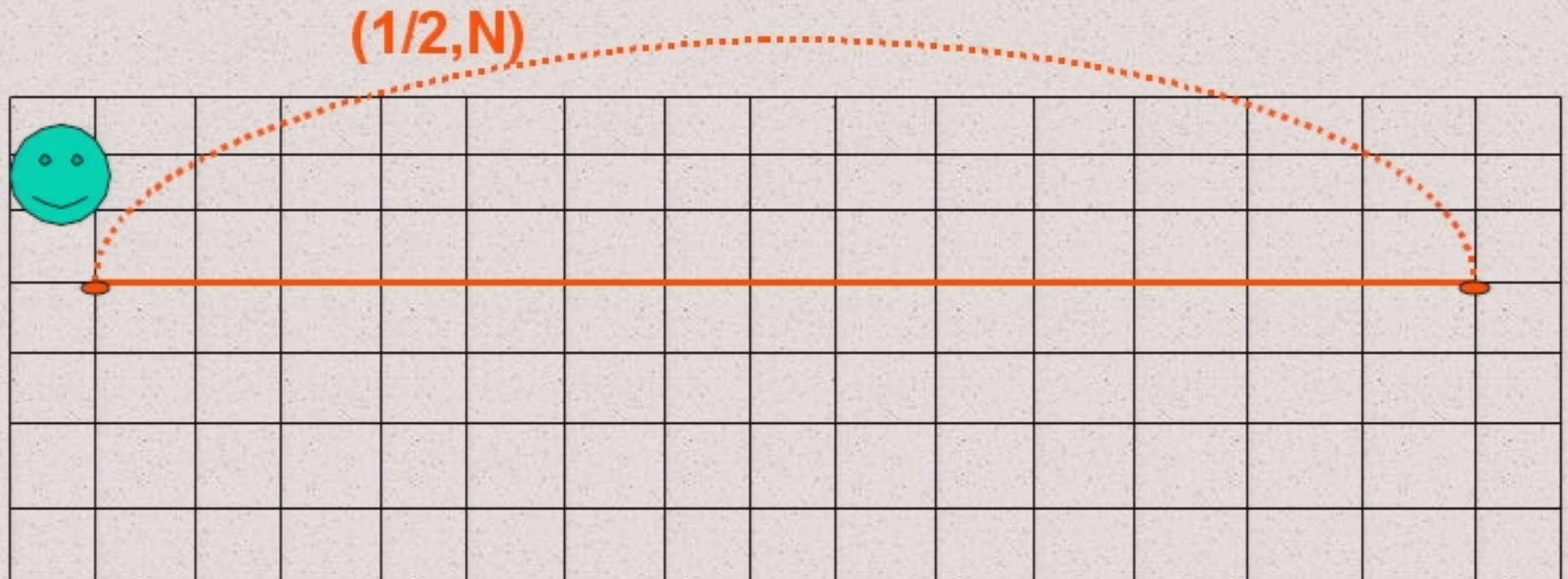
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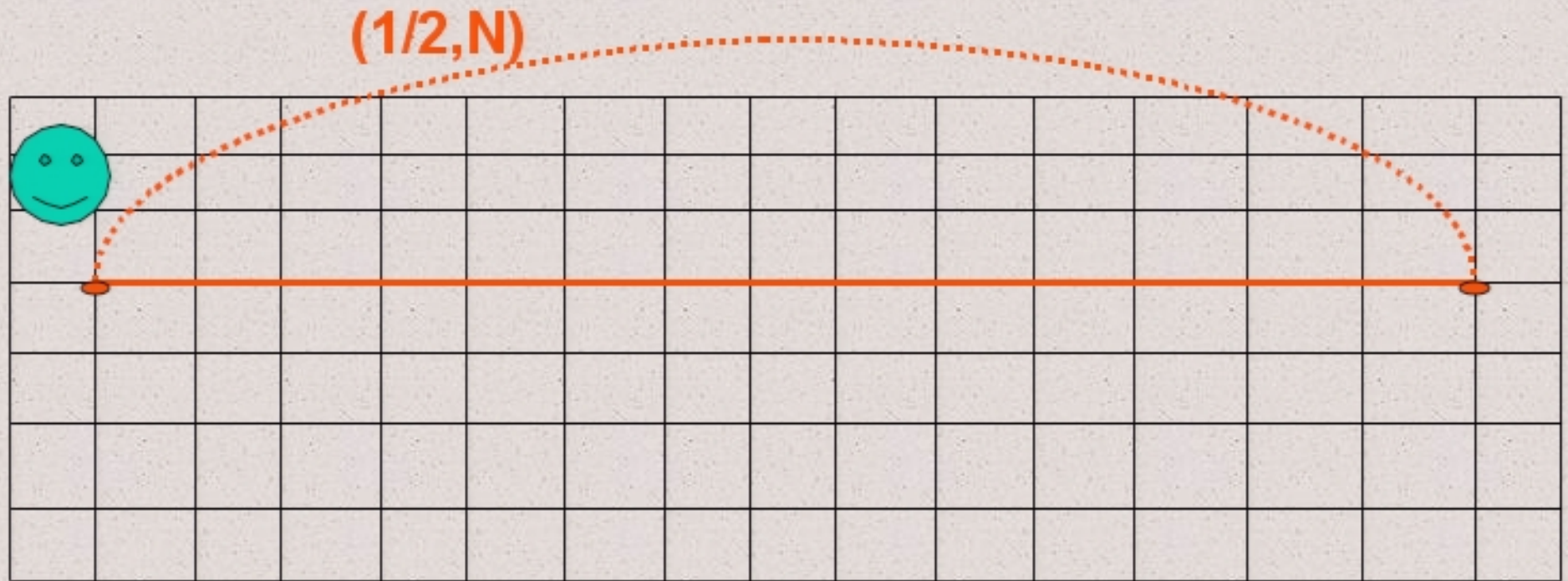
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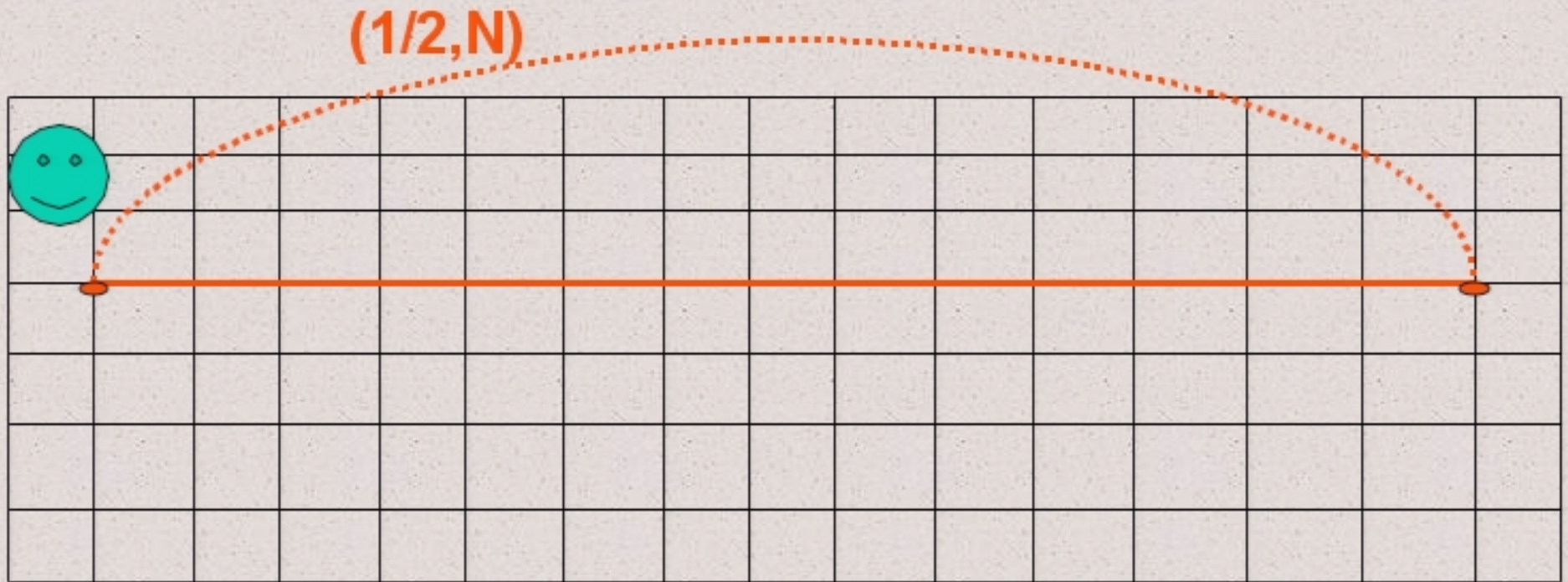
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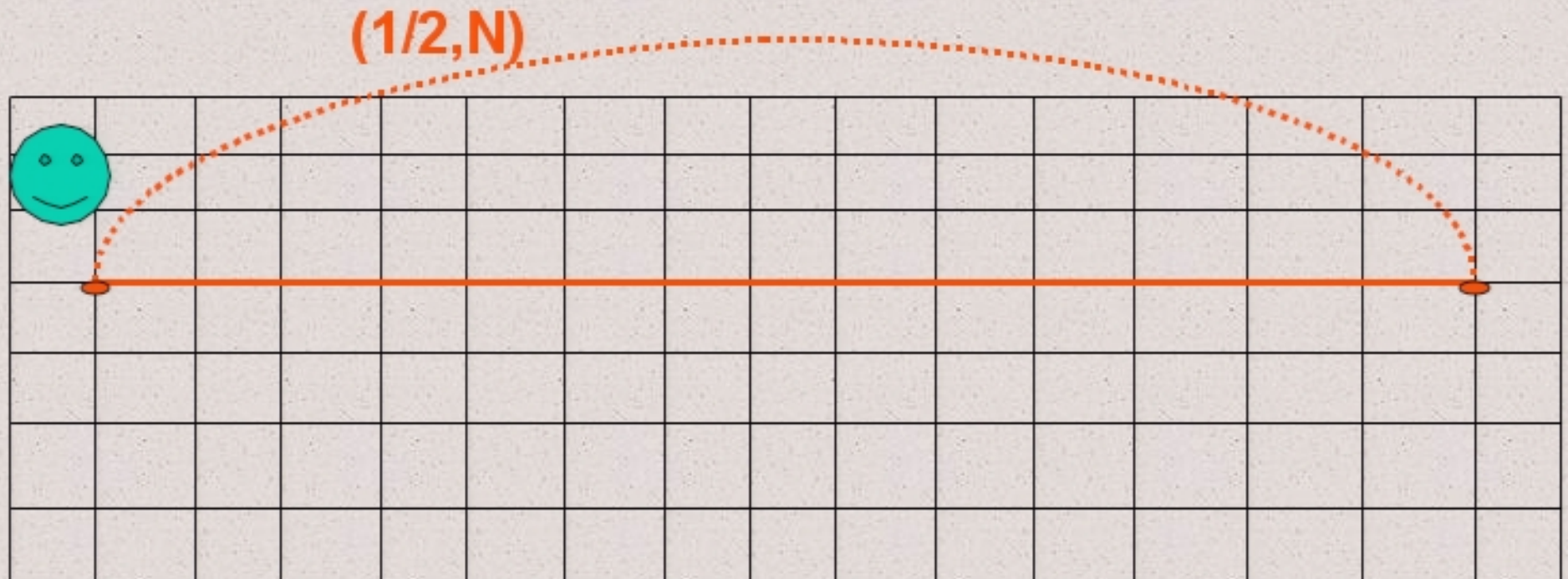
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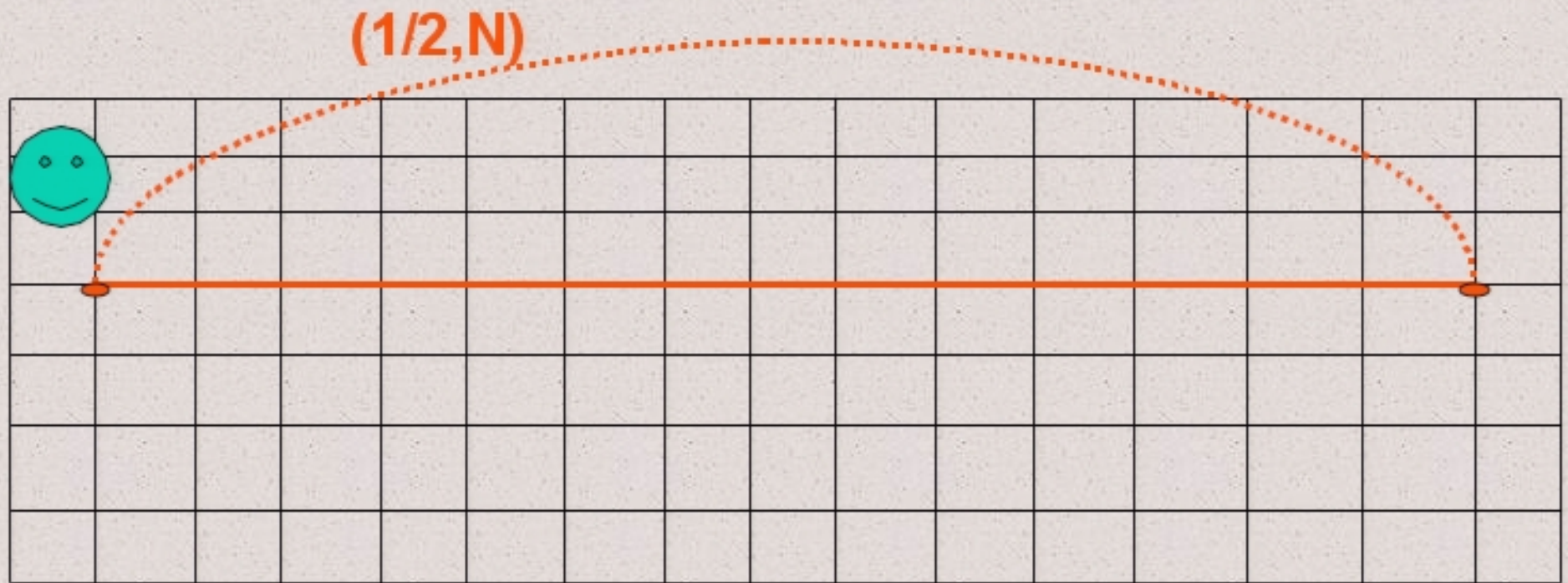
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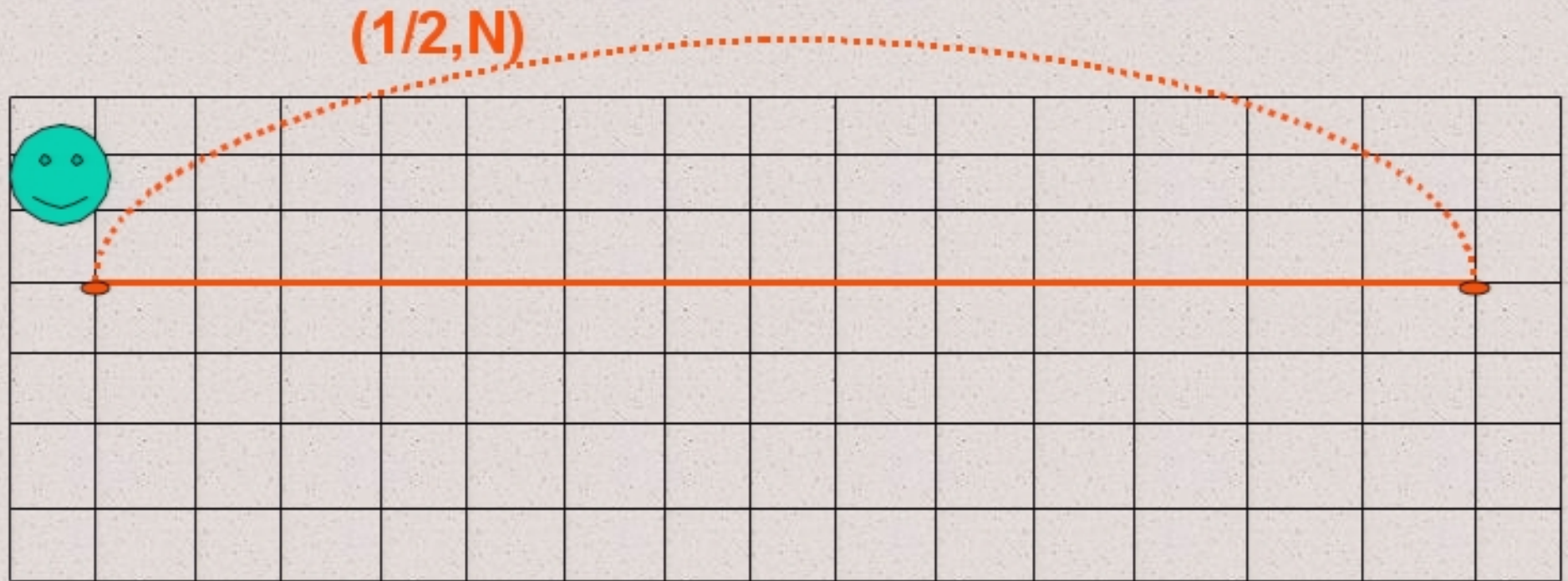


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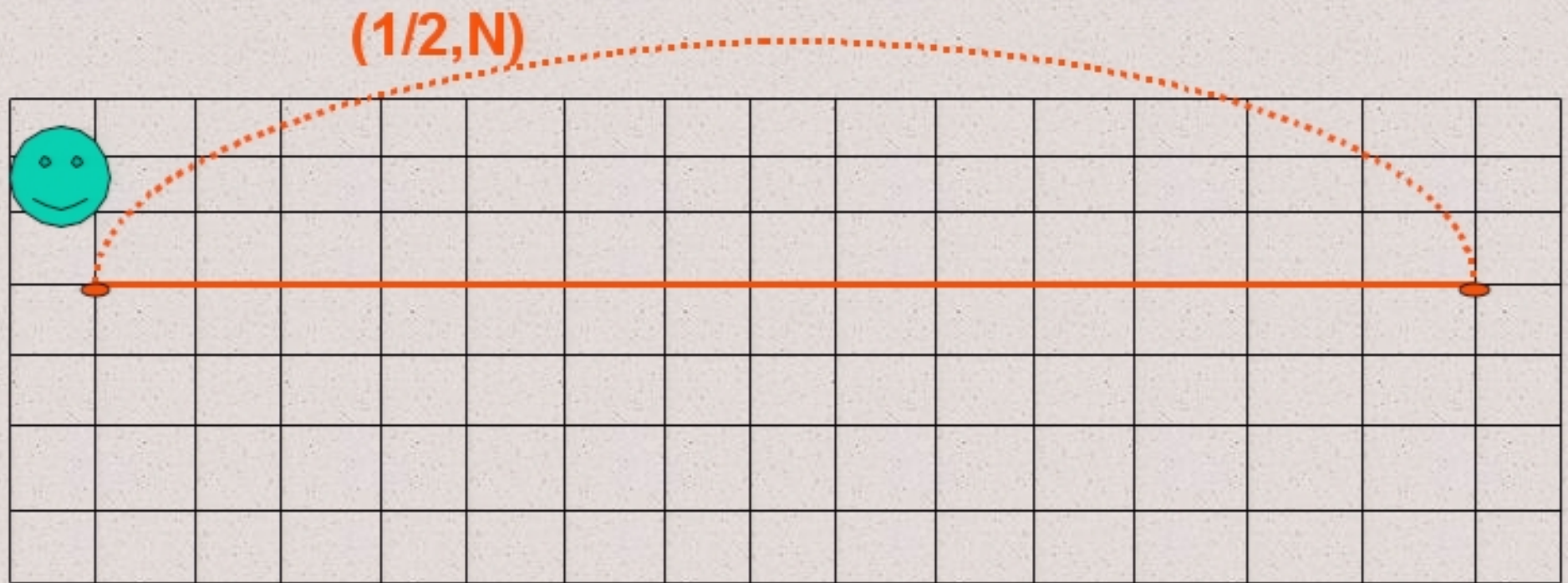


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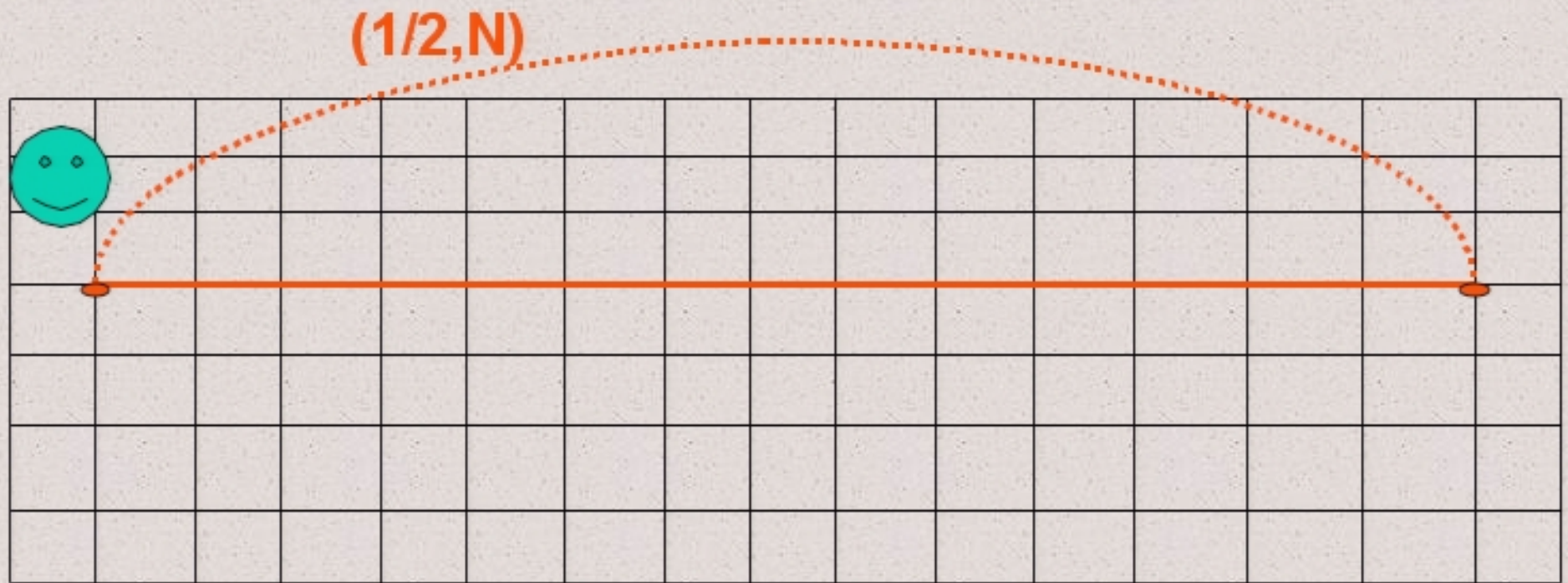


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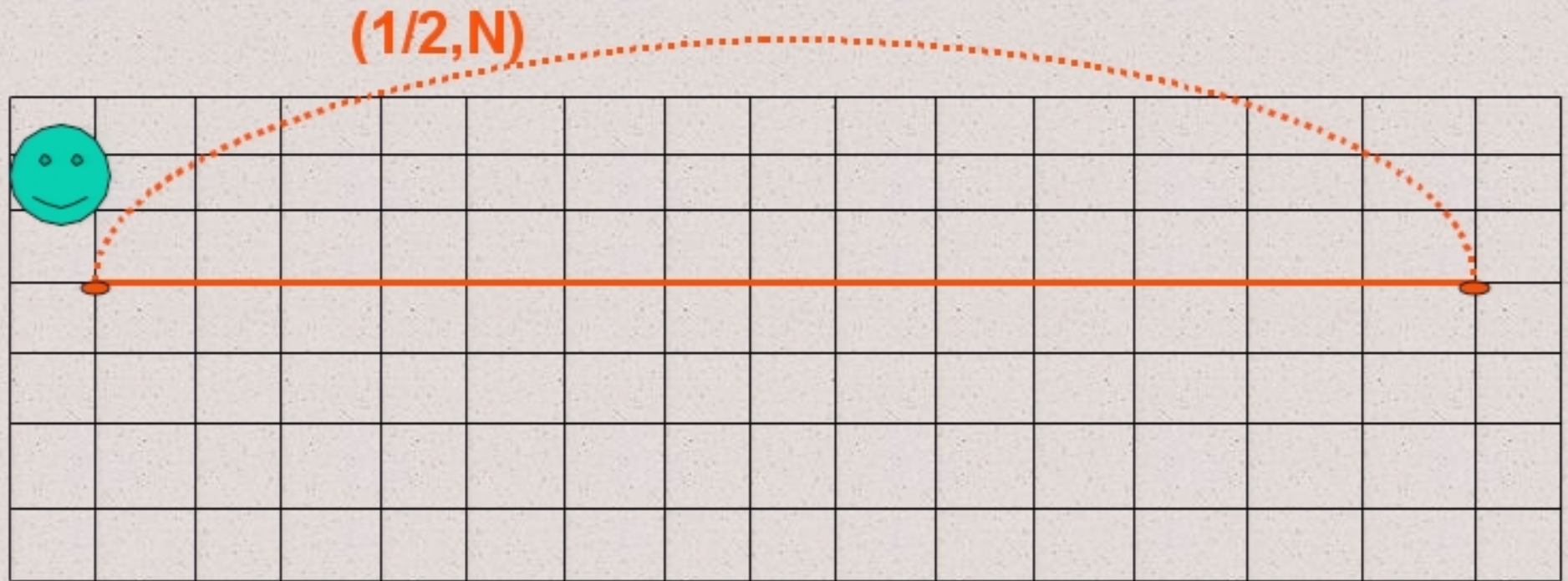


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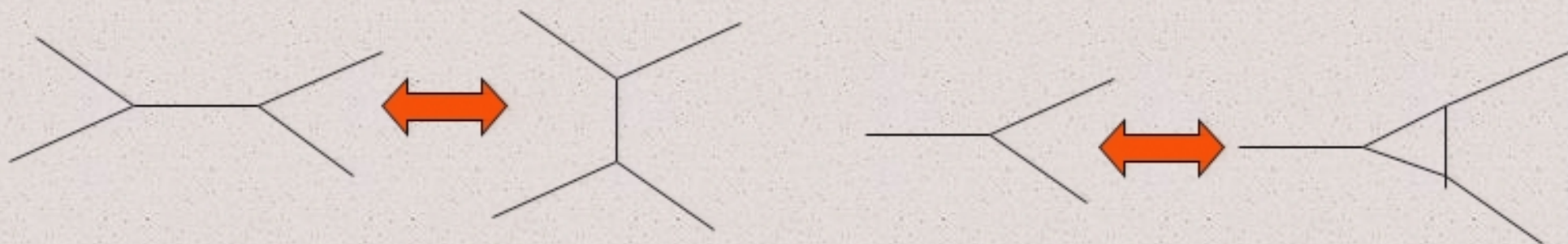
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Could this work?

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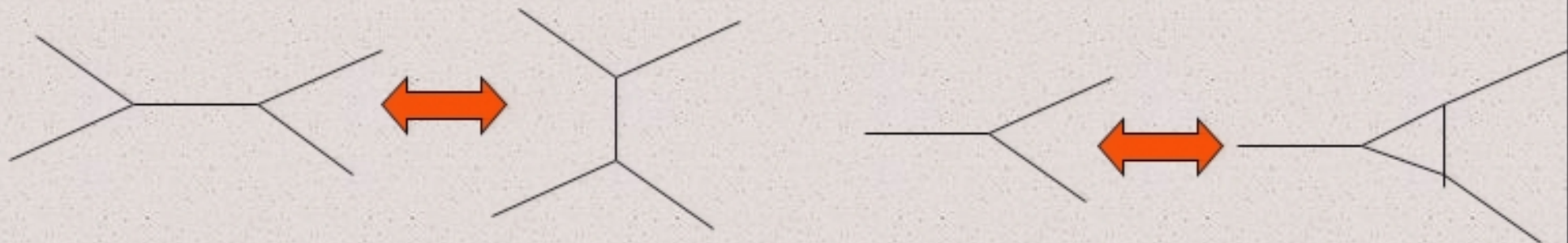


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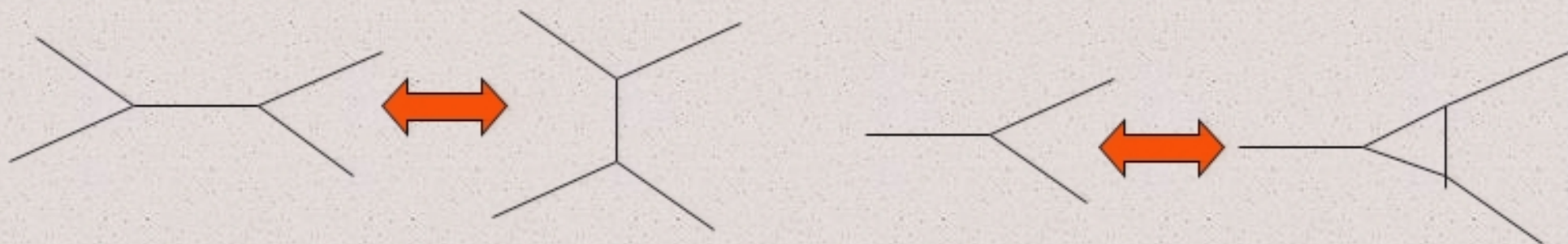


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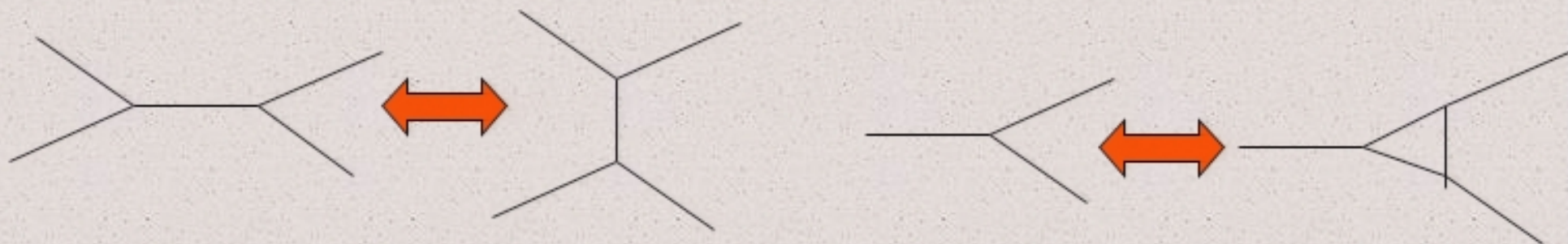


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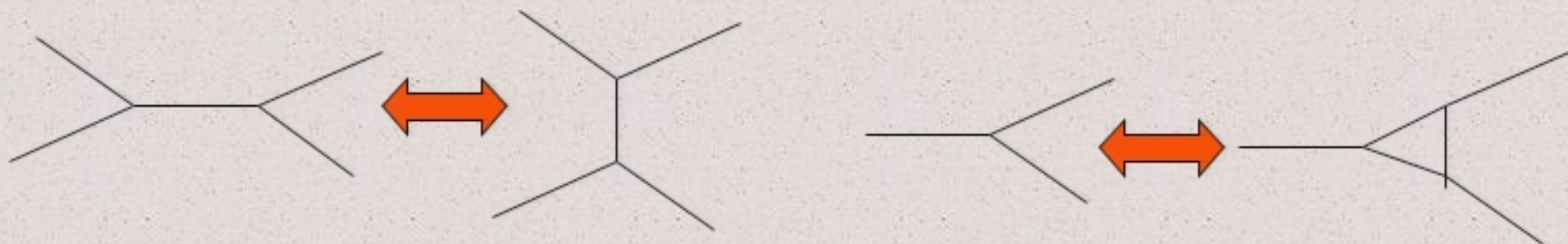


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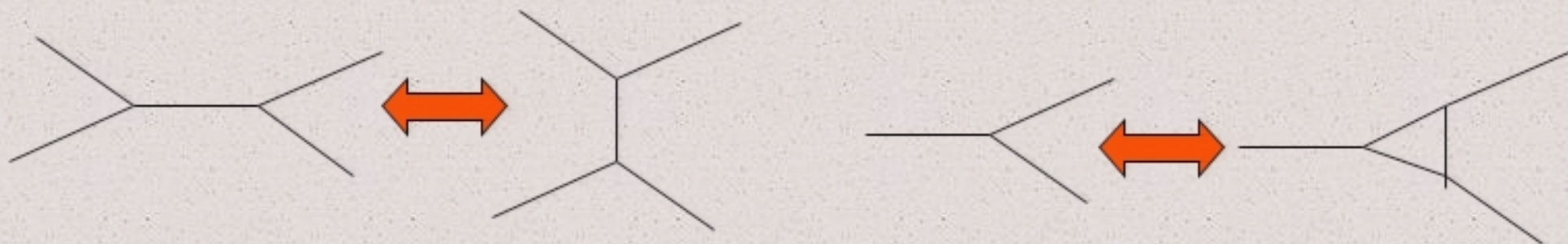


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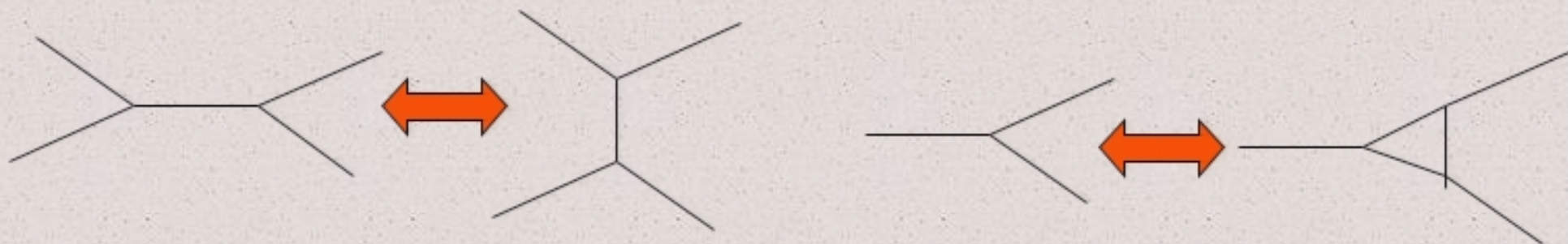


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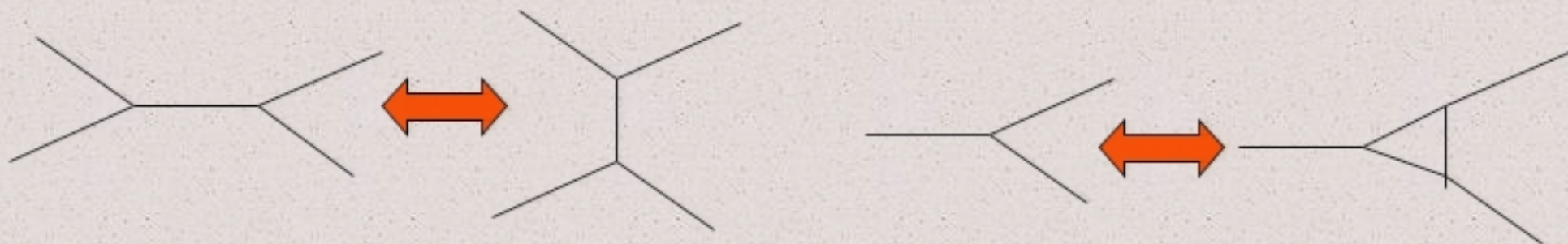


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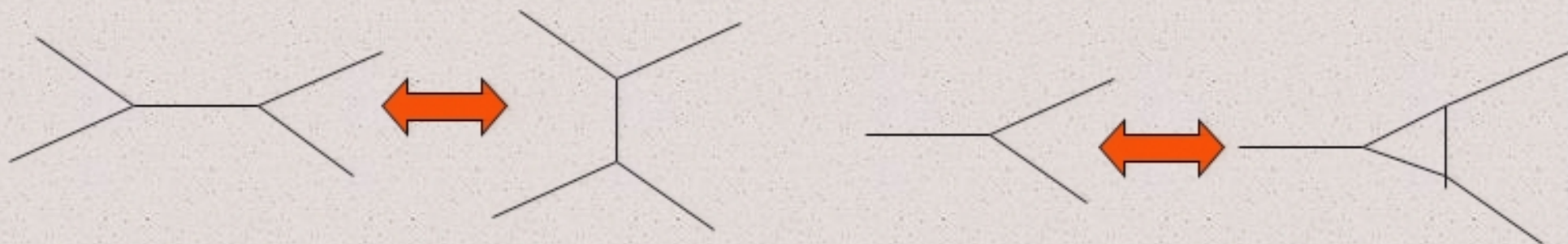


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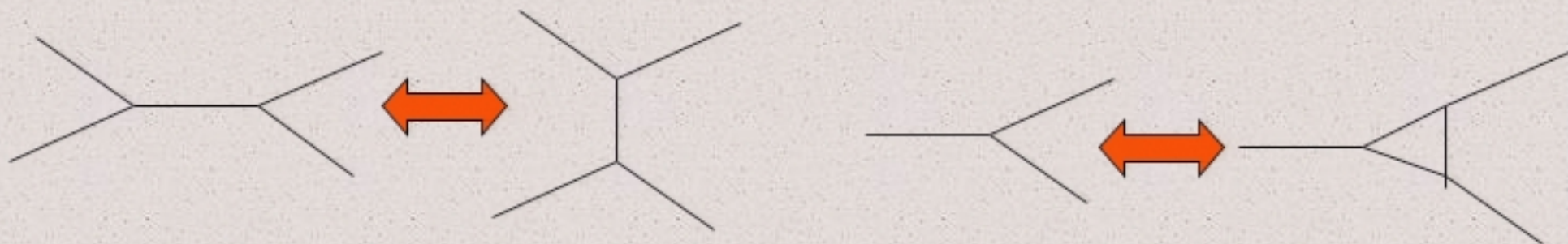


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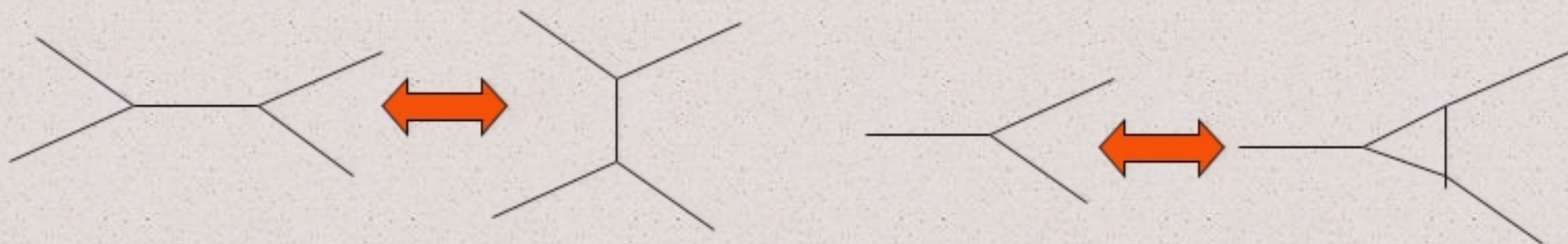


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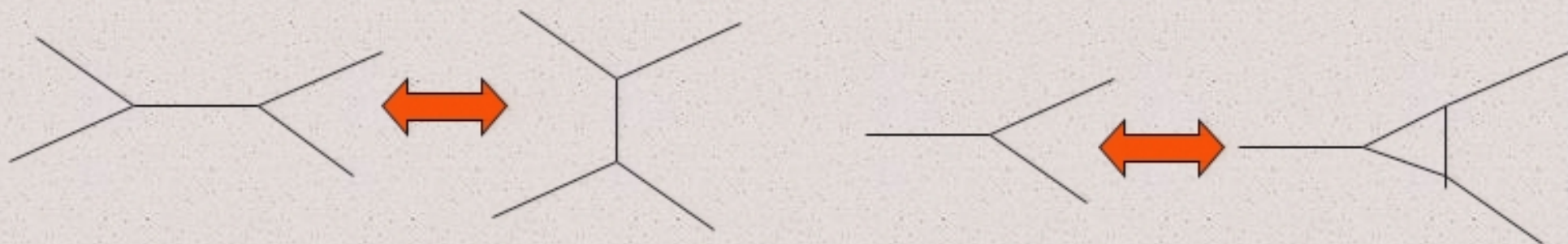


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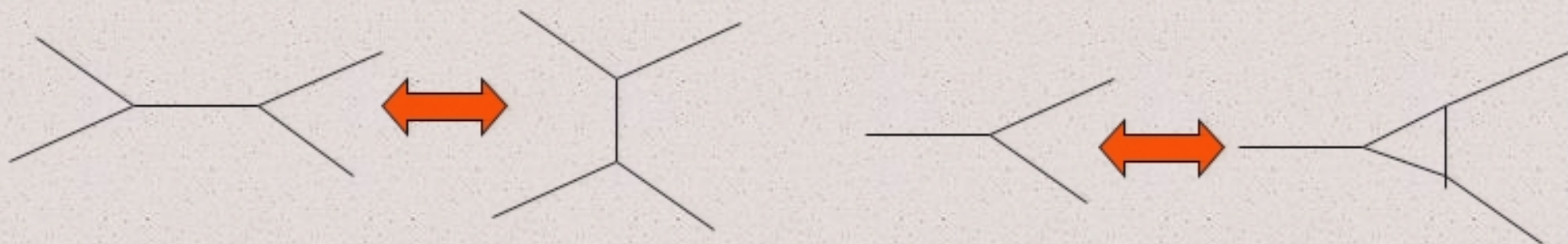


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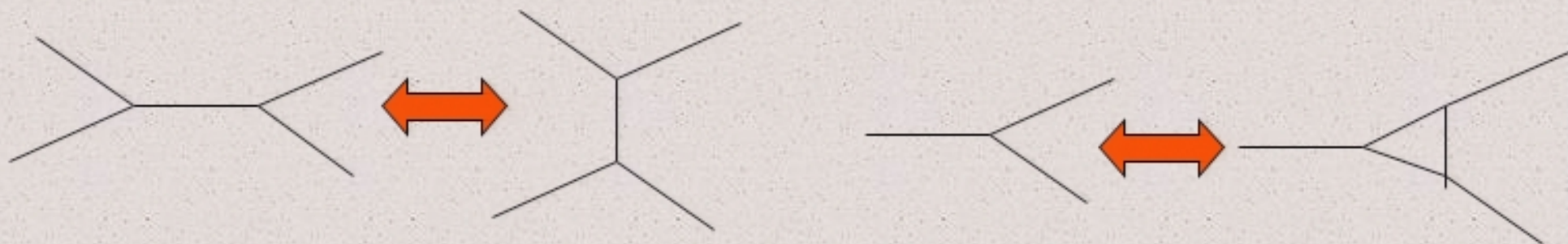


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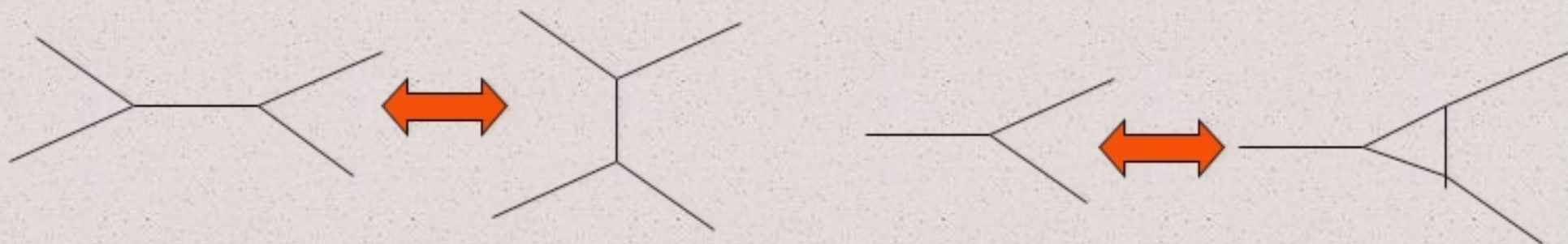


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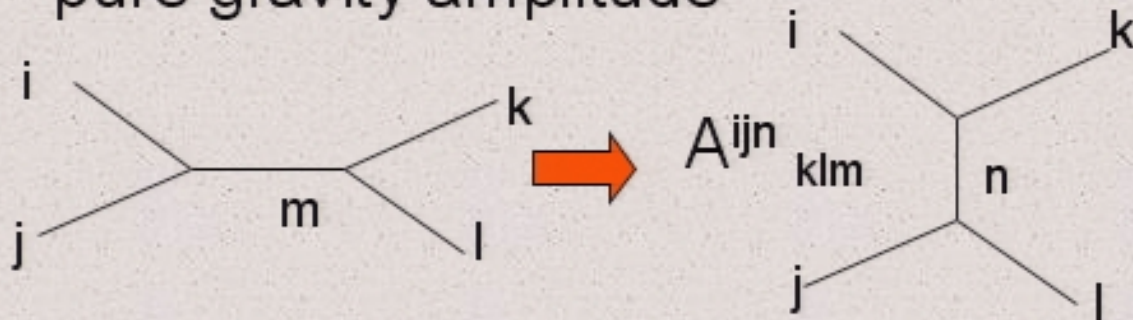
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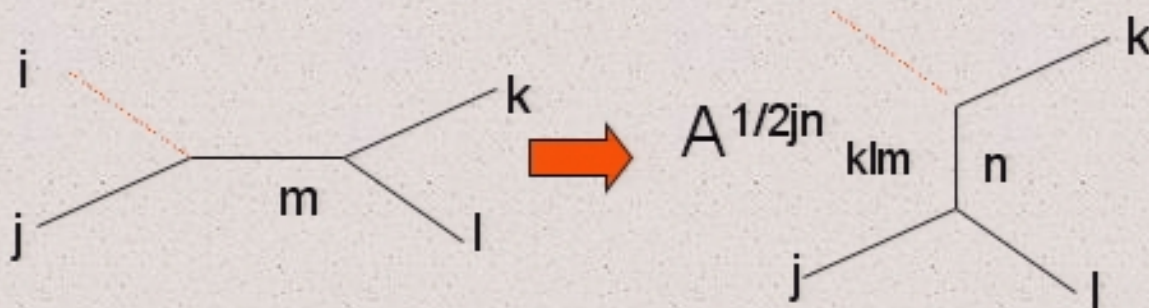


Relation between fermion and gravity dynamics:

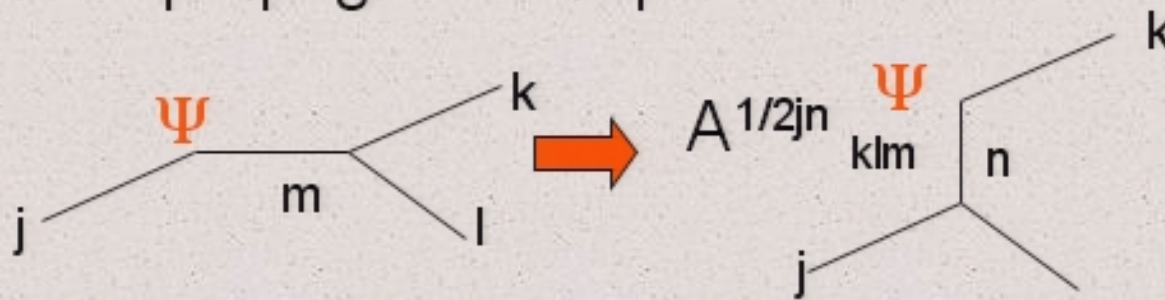
pure gravity amplitude



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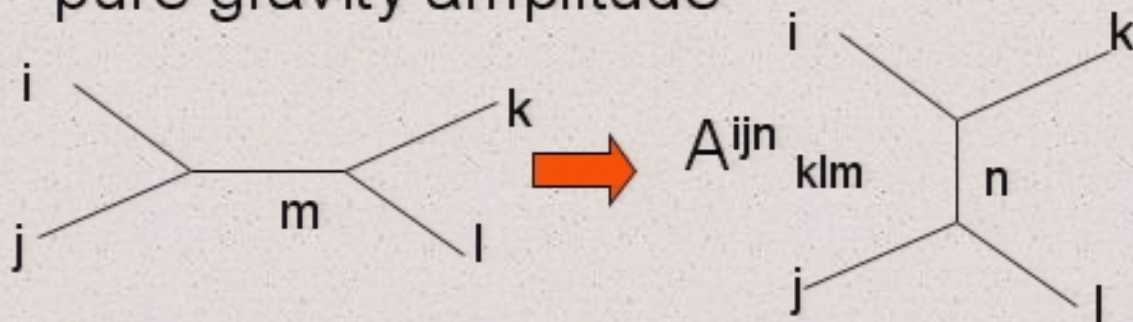


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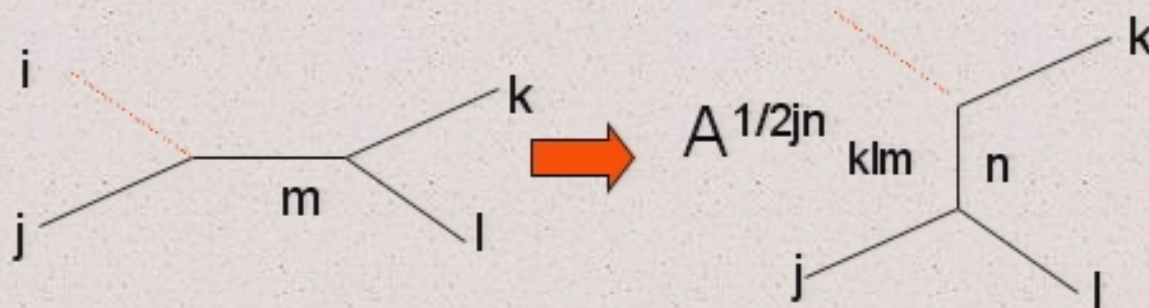


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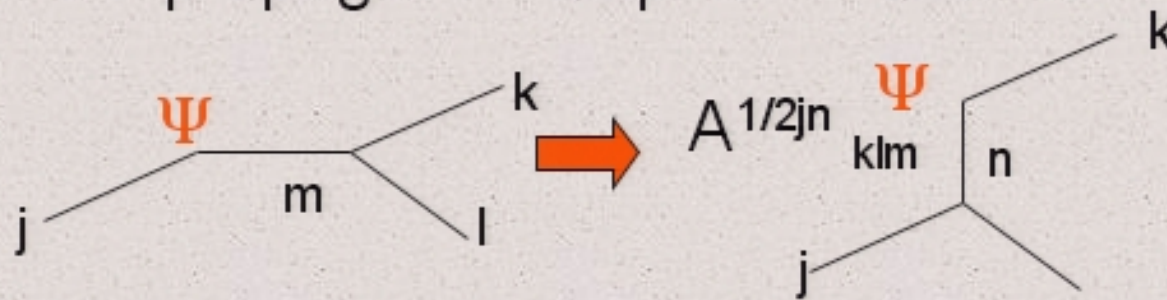
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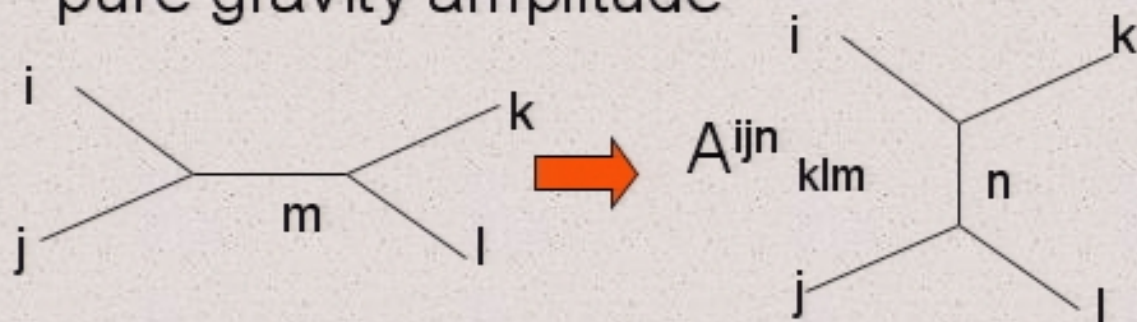


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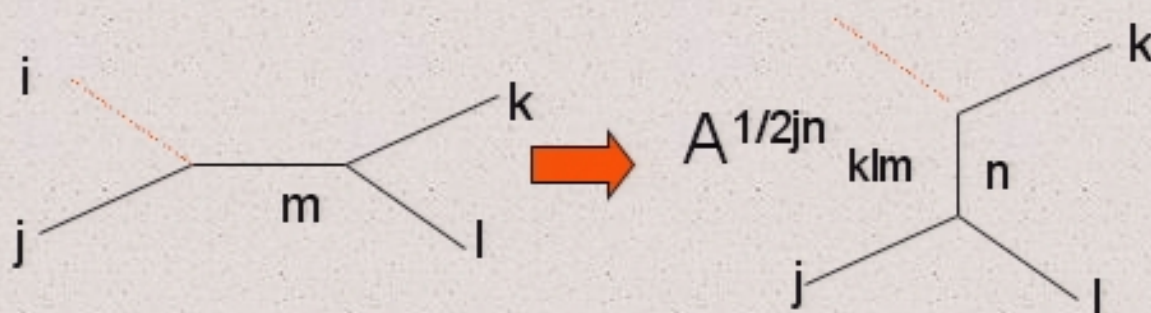


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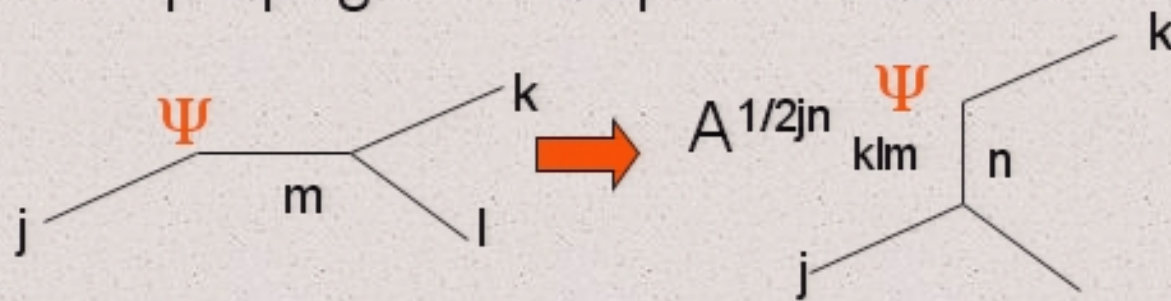
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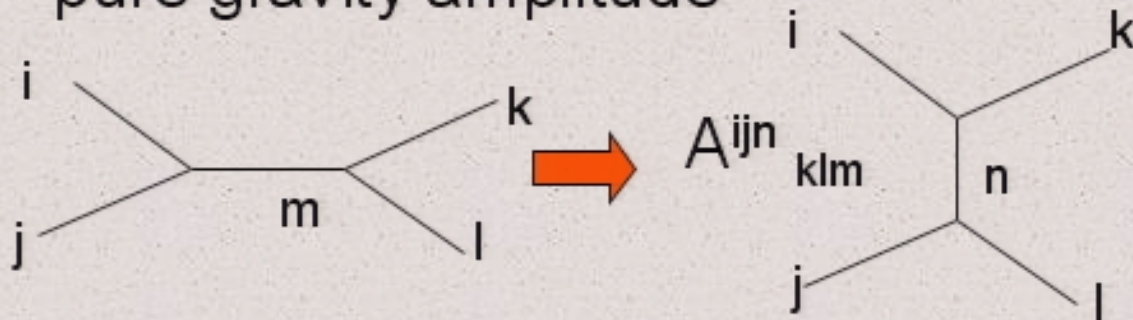


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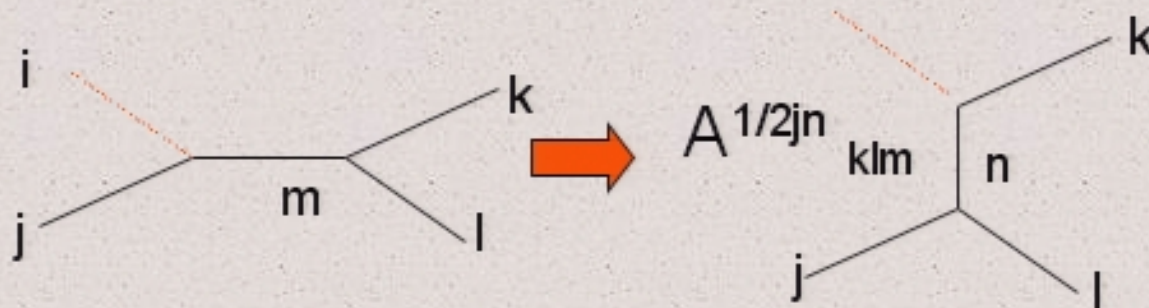


Relation between fermion and gravity dynamics:

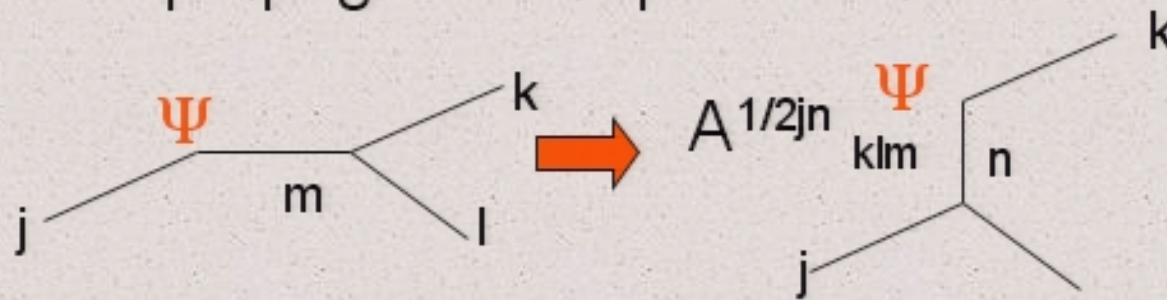
pure gravity amplitude



Let the $i=1/2$ line be non-local

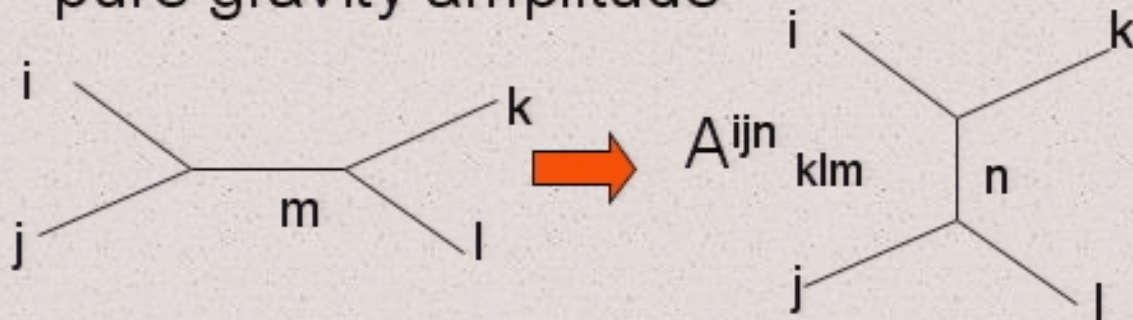


This is a propagation amplitude for a fermion

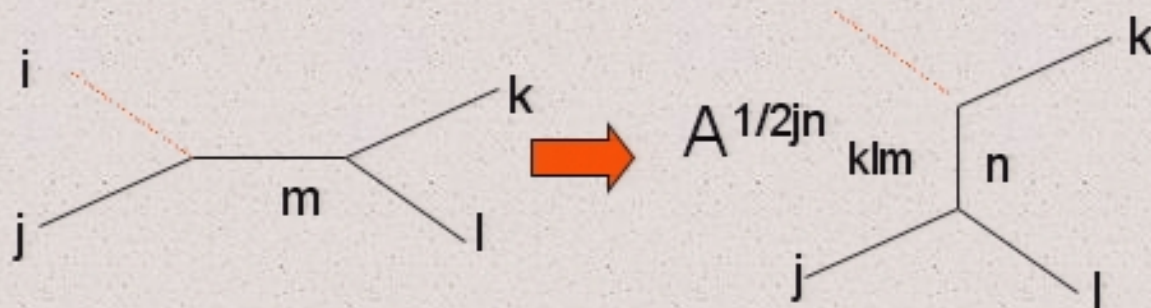


Relation between fermion and gravity dynamics:

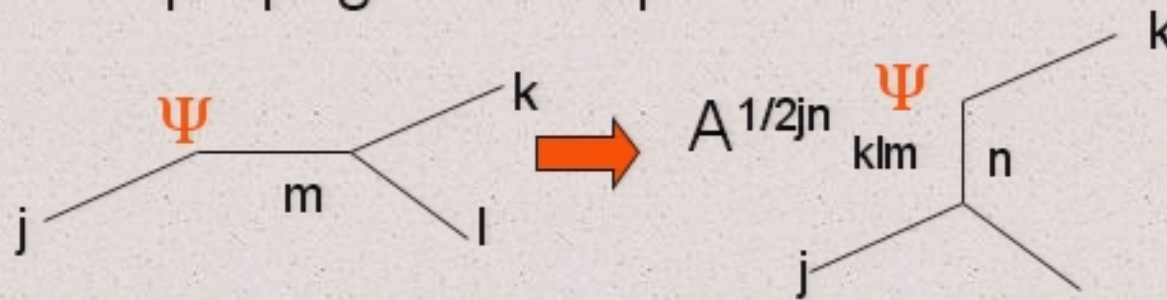
pure gravity amplitude



Let the $i=1/2$ line be non-local

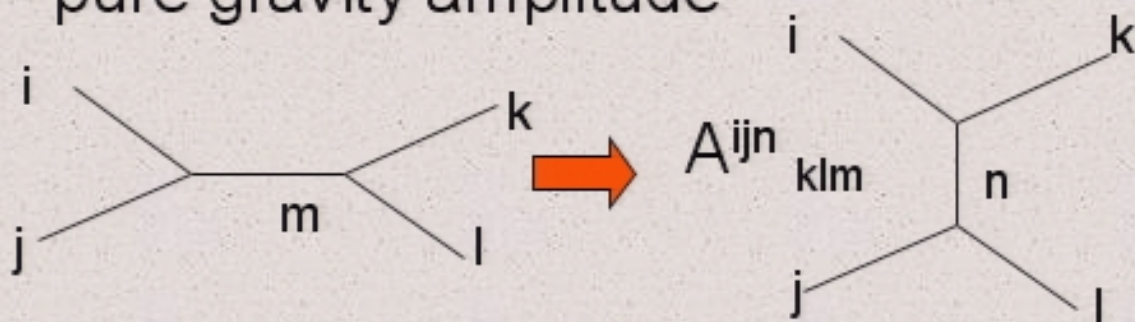


This is a propagation amplitude for a fermion

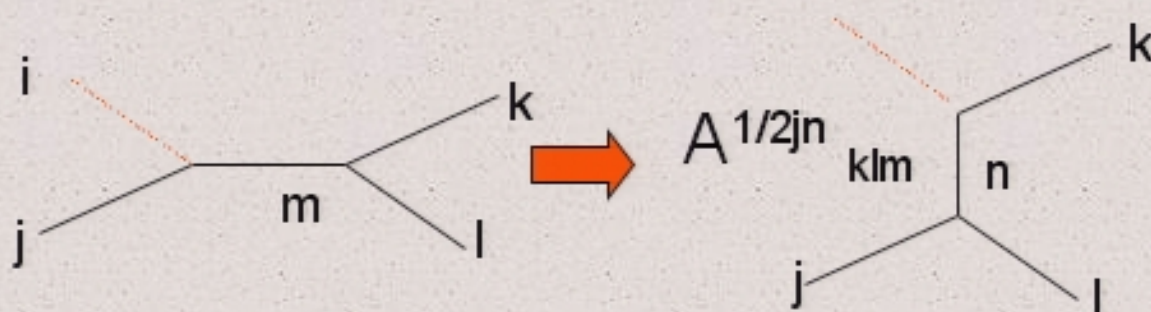


Relation between fermion and gravity dynamics:

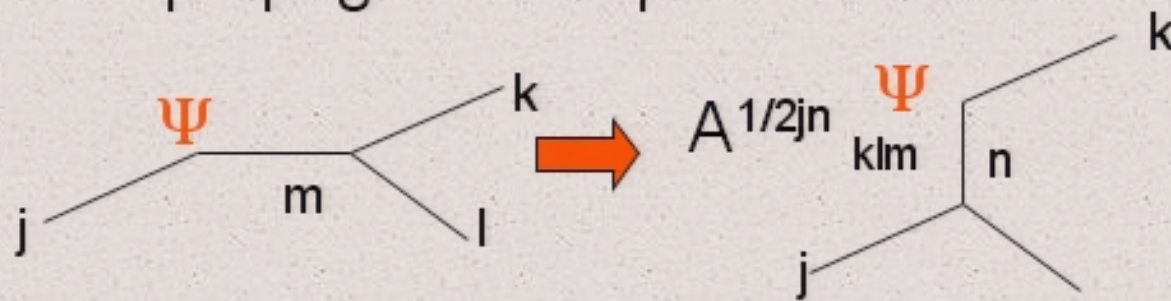
pure gravity amplitude



Let the $i=1/2$ line be non-local

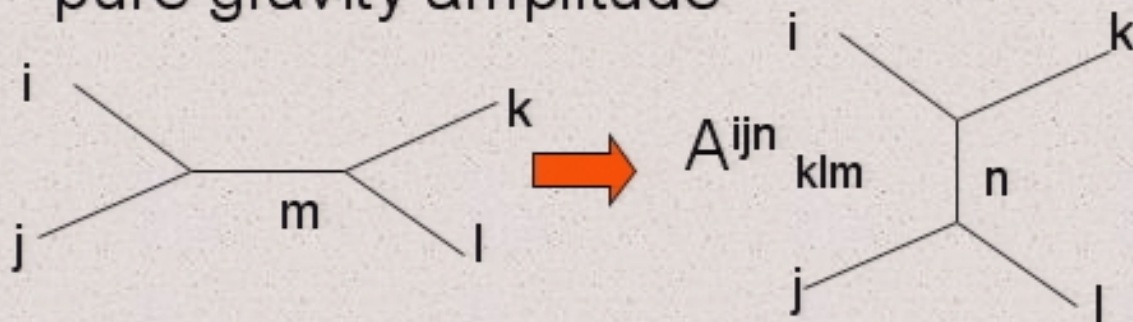


This is a propagation amplitude for a fermion

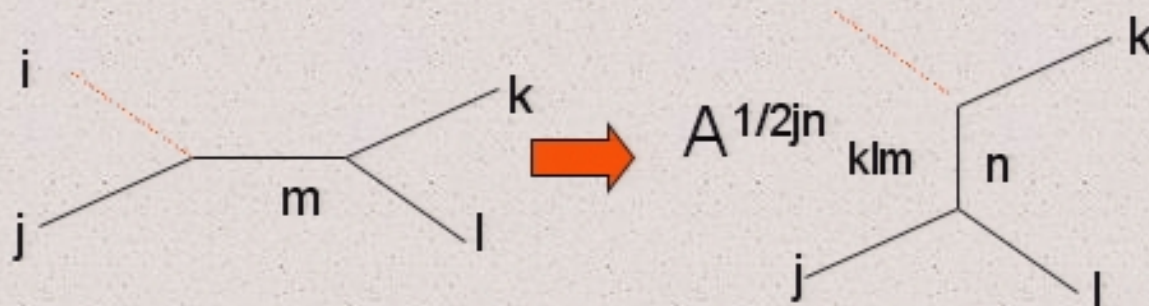


Relation between fermion and gravity dynamics:

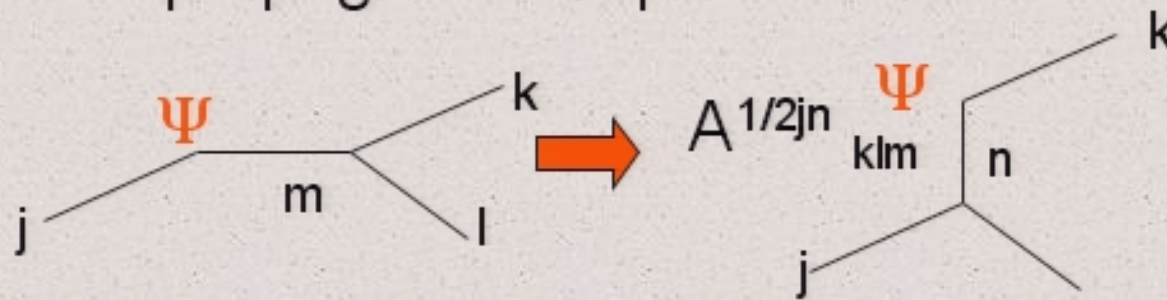
pure gravity amplitude



Let the $i=1/2$ line be non-local

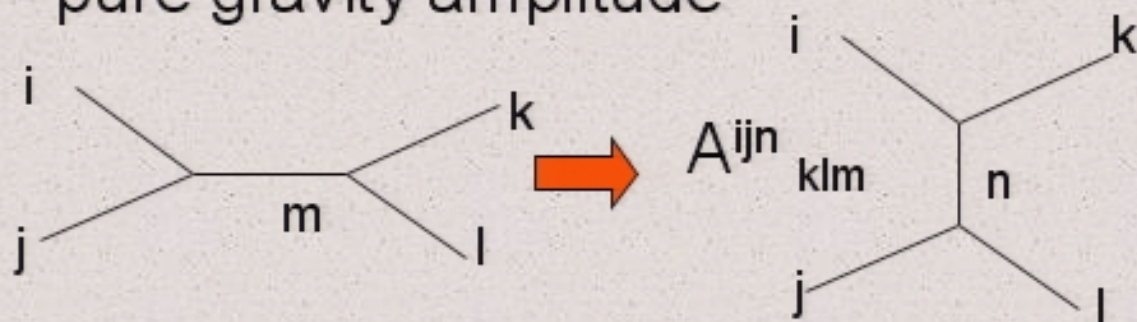


This is a propagation amplitude for a fermion

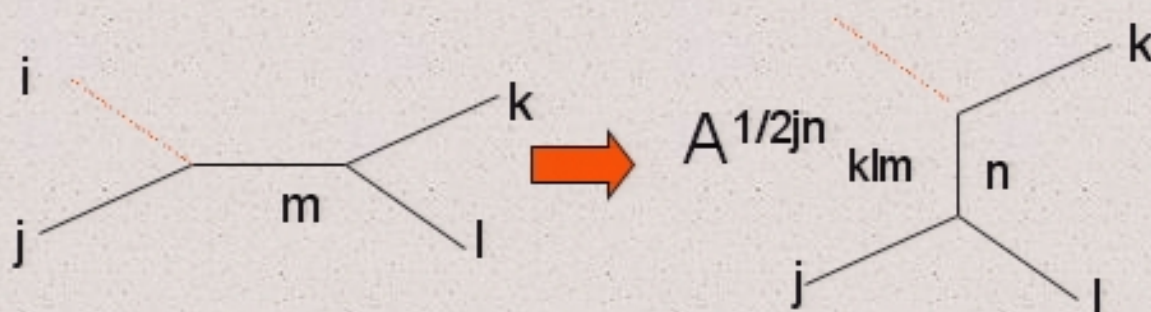


Relation between fermion and gravity dynamics:

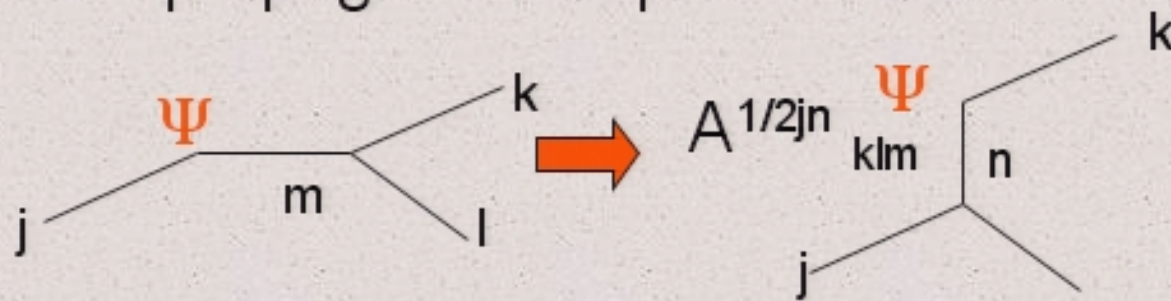
pure gravity amplitude



Let the $i=1/2$ line be non-local

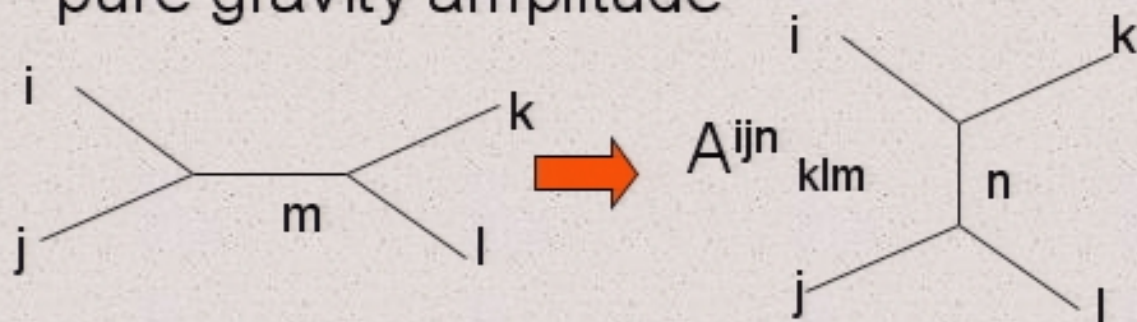


This is a propagation amplitude for a fermion

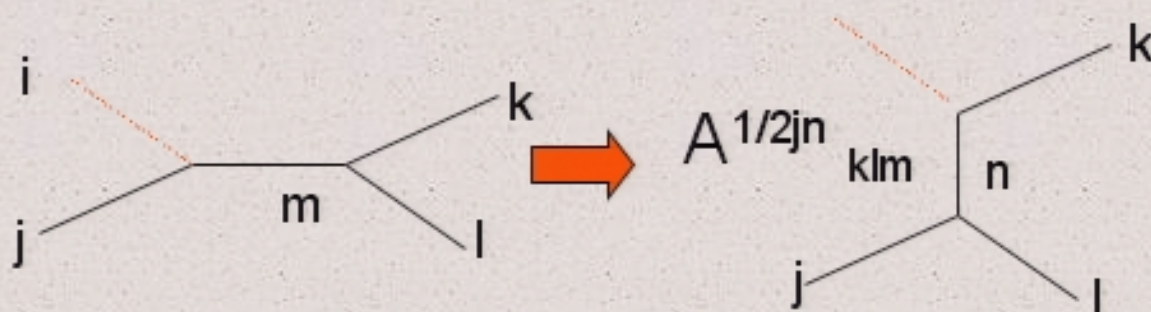


Relation between fermion and gravity dynamics:

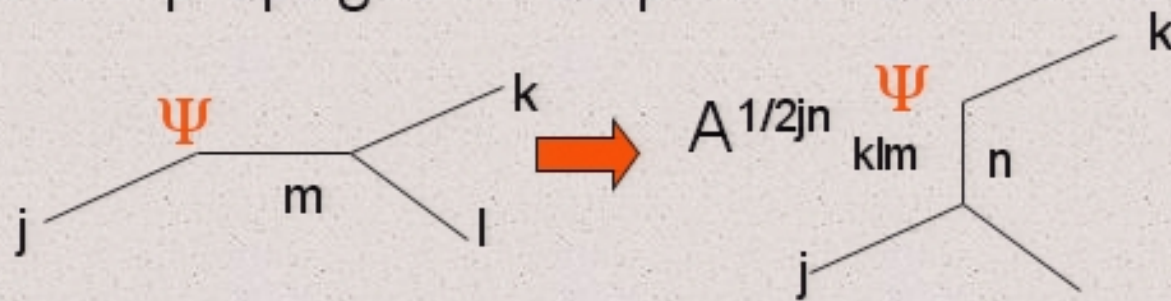
pure gravity amplitude



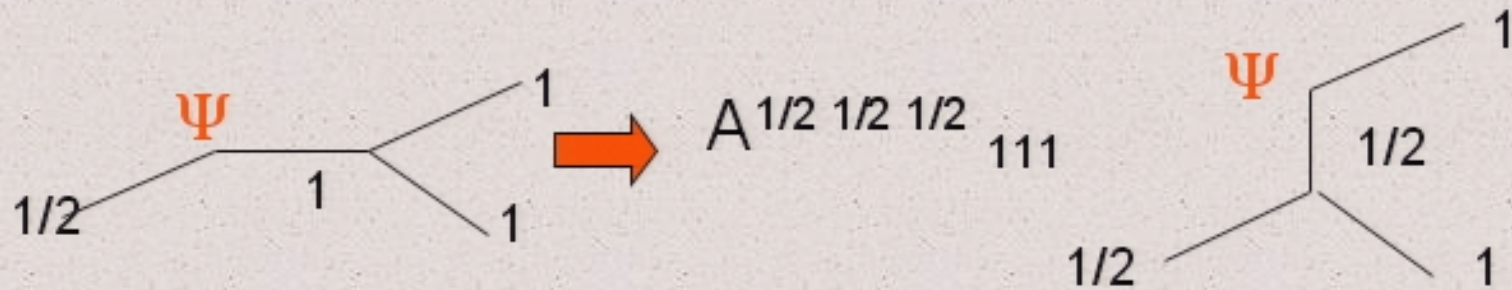
Let the $i=1/2$ line be non-local



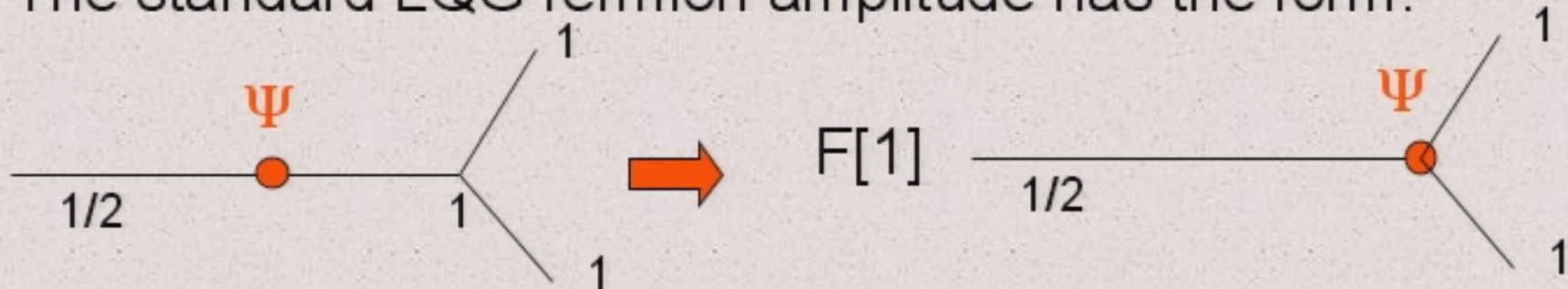
This is a propagation amplitude for a fermion



Lets look at this in detail:



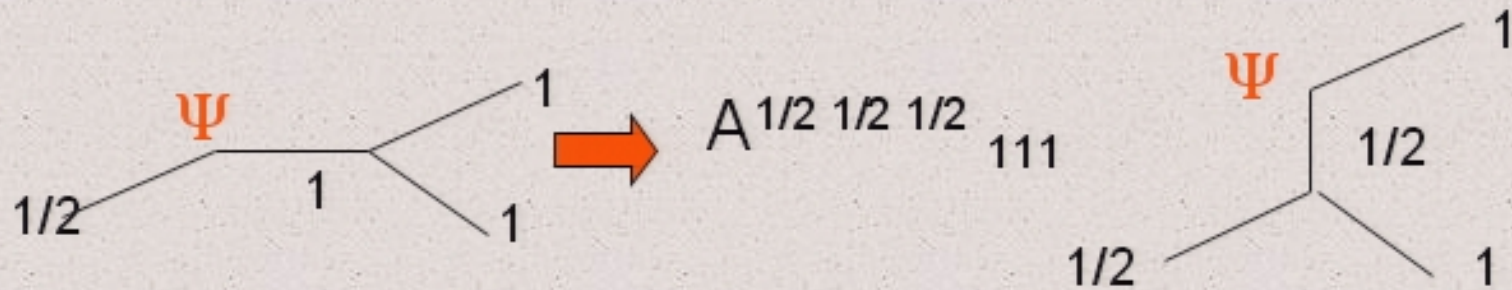
The standard LQG fermion amplitude has the form:



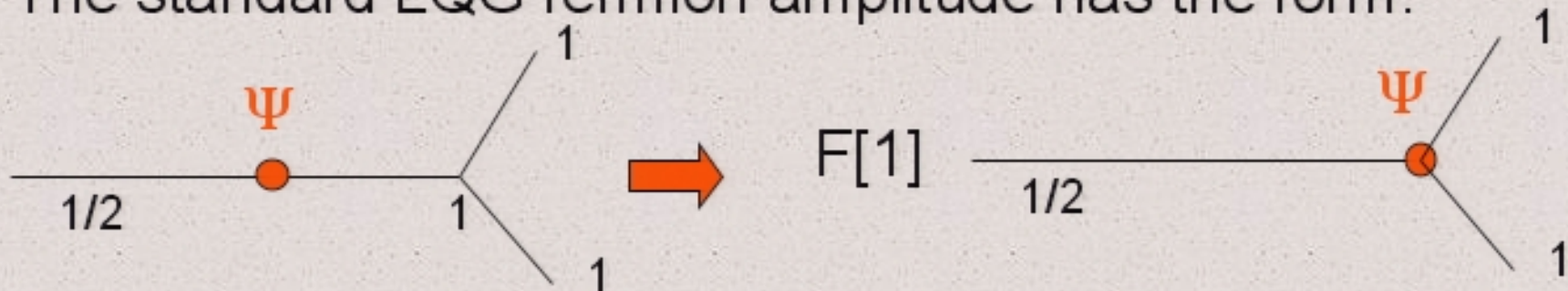
We have to do this twice to reproduce the pure gravity move:

$$\Rightarrow \boxed{F[1]^2 = A^{1/2 \ 1/2 \ 1/2}_{111}}$$

Lets look at this in detail:



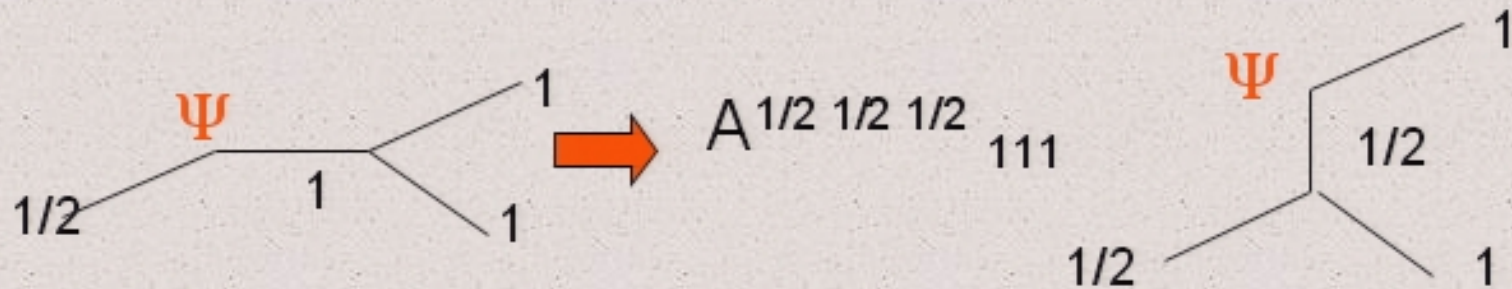
The standard LQG fermion amplitude has the form:



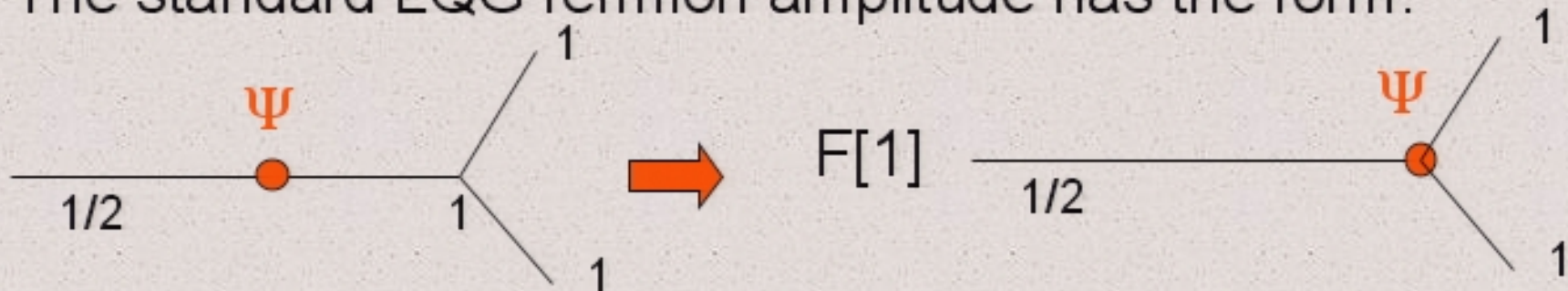
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Lets look at this in detail:



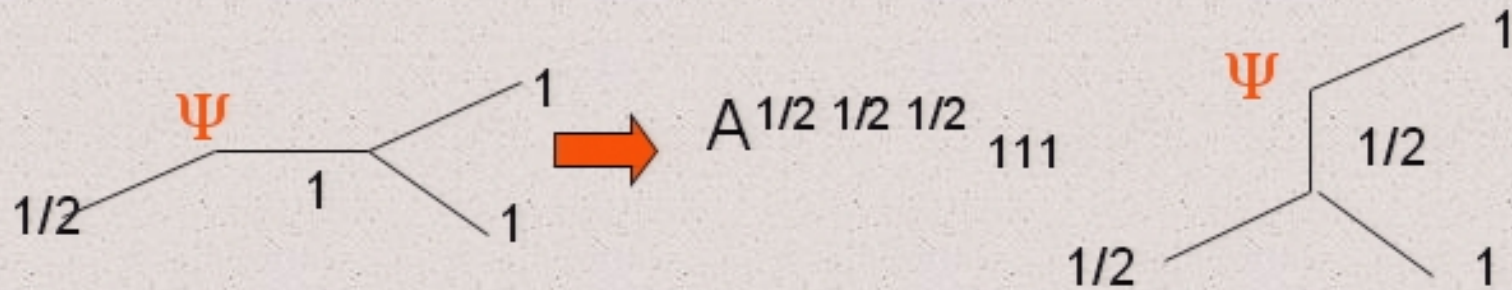
The standard LQG fermion amplitude has the form:



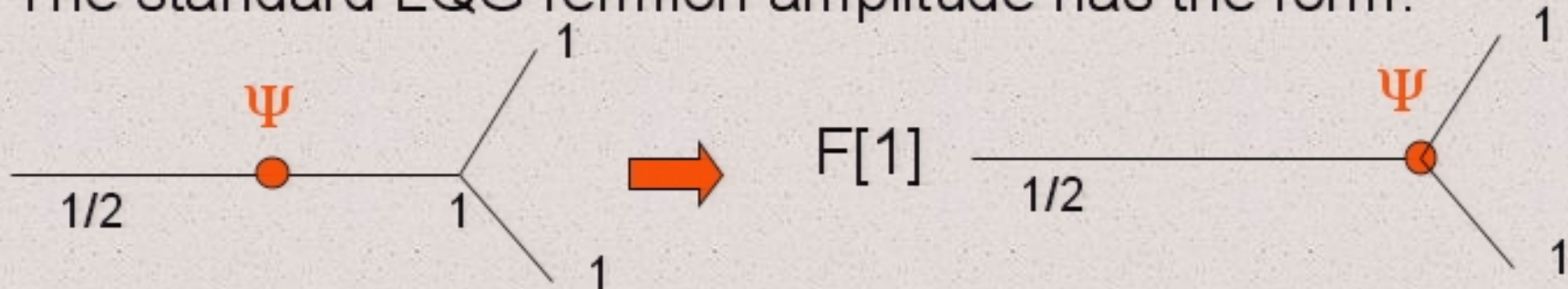
We have to do this twice to reproduce the pure gravity move:

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Lets look at this in detail:



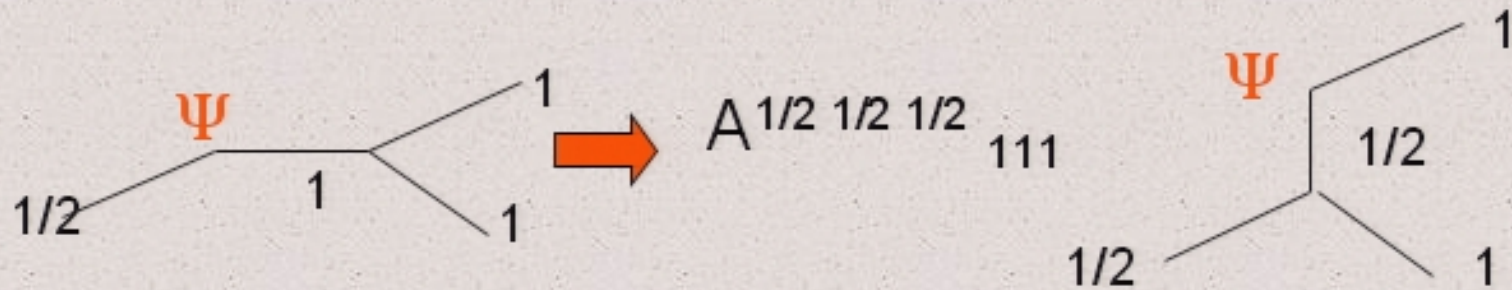
The standard LQG fermion amplitude has the form:



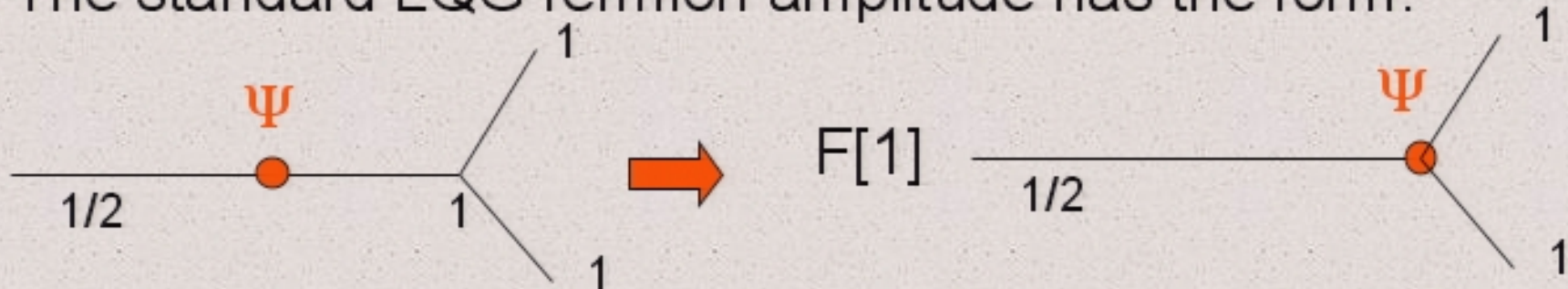
We have to do this twice to reproduce the pure gravity move:

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Lets look at this in detail:



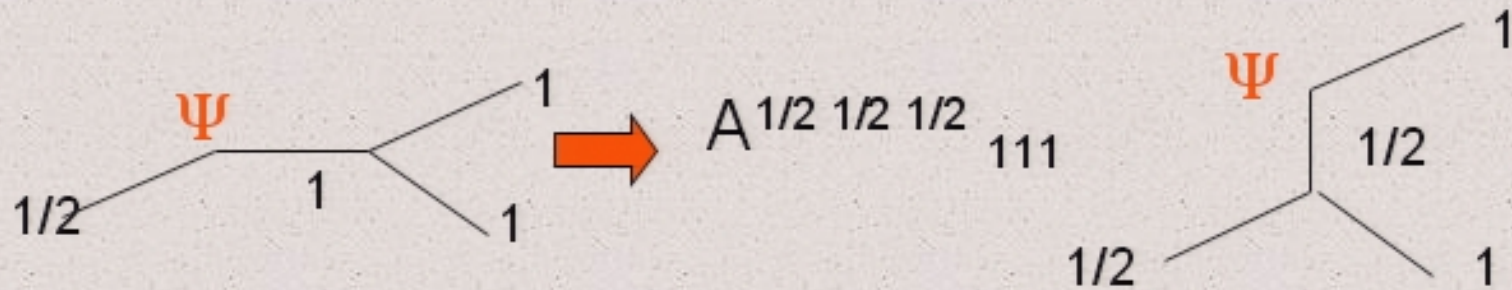
The standard LQG fermion amplitude has the form:



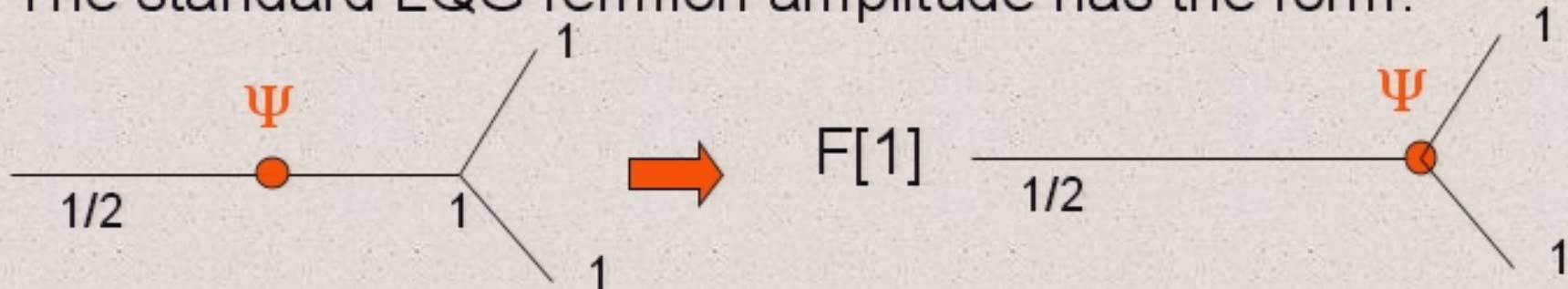
We have to do this twice to reproduce the pure gravity move:

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Lets look at this in detail:



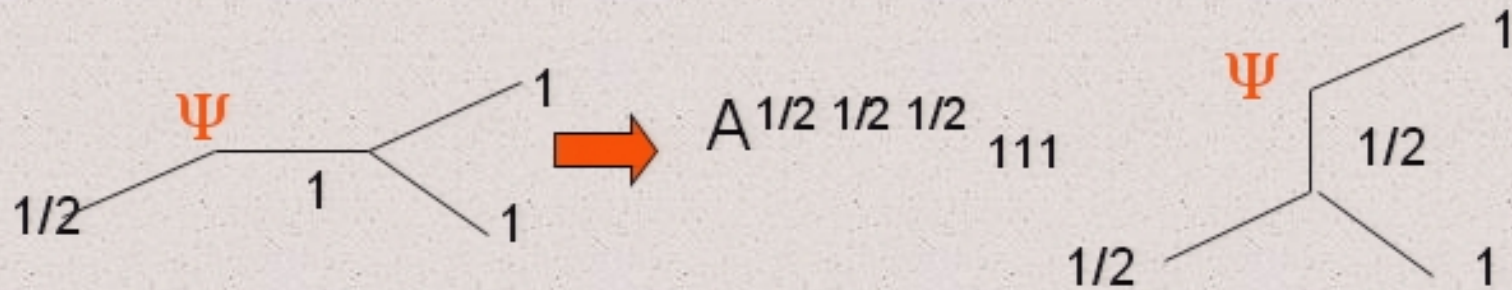
The standard LQG fermion amplitude has the form:



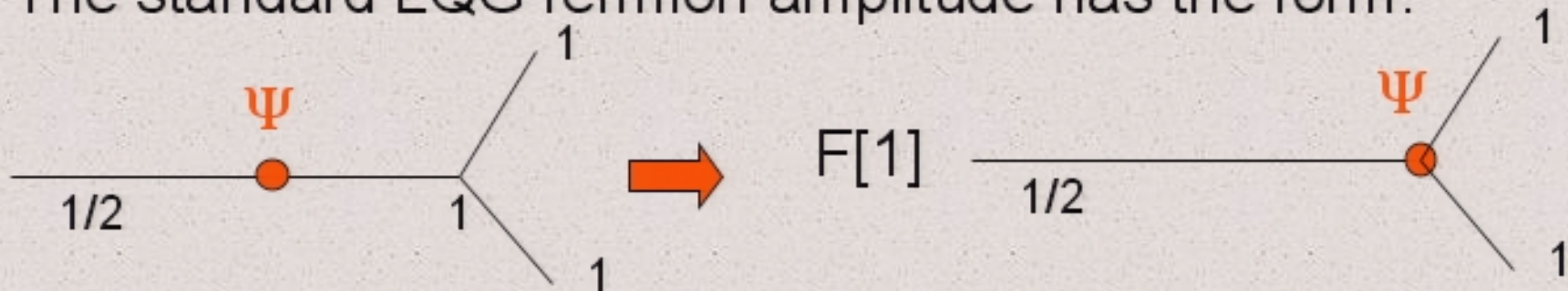
We have to do this twice to reproduce the pure gravity move:

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Lets look at this in detail:



The standard LQG fermion amplitude has the form:

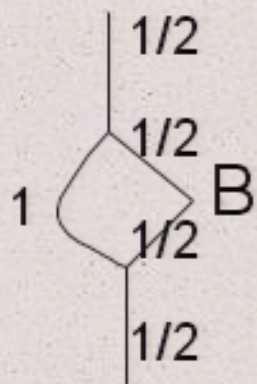


We have to do this twice to reproduce the pure gravity move:

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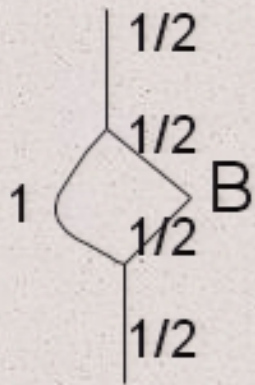
Interactions come from moves that are local microscopically,
but non local macroscopically:

A spin-1 boson:



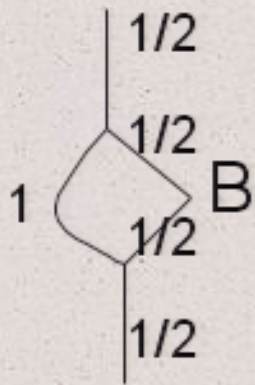
Interactions come from moves that are local microscopically,
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A spin-1 boson:



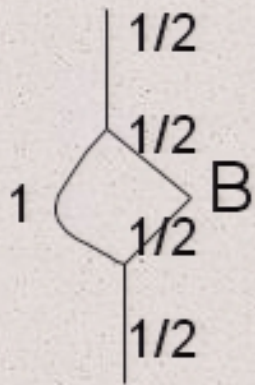
Interactions come from moves that are local microscopically,
but non local macroscopically:

A spin-1 boson:



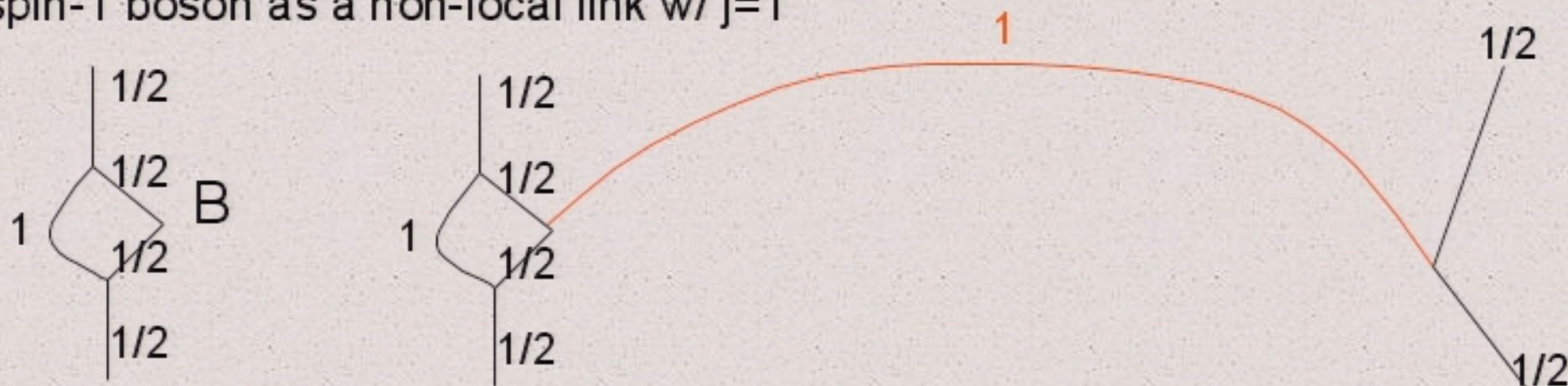
Interactions come from moves that are local microscopically,
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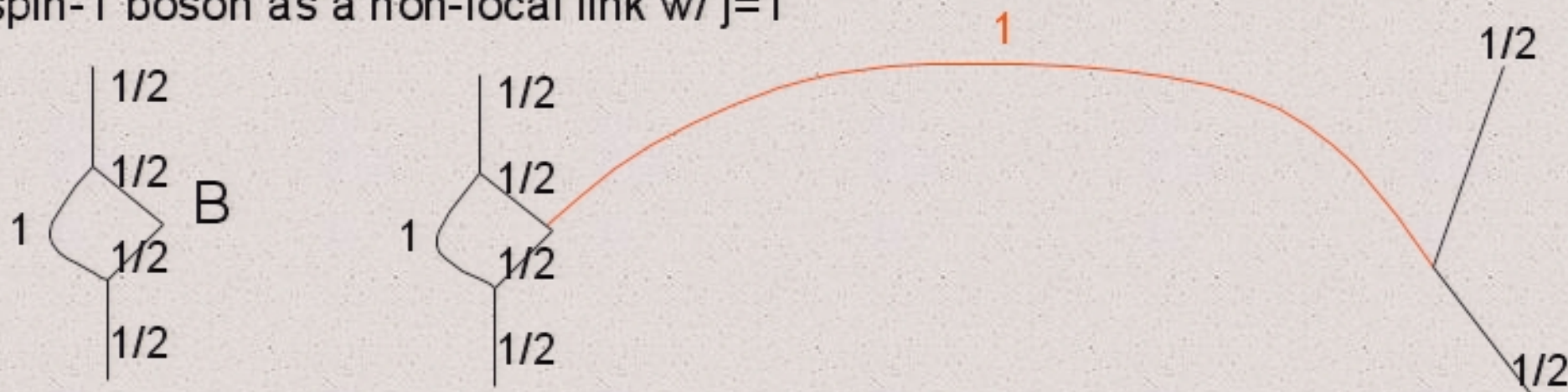
Interactions come from moves that are local microscopically,
but non local macroscopically:

A spin-1 boson as a non-local link w/ $j=1$



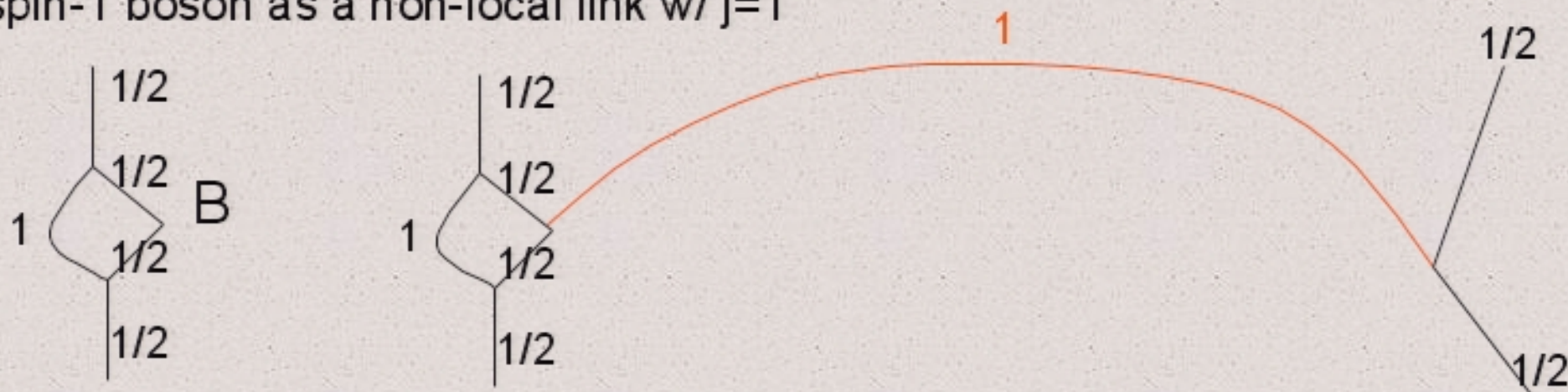
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A spin-1 boson as a non-local link w/ $j=1$



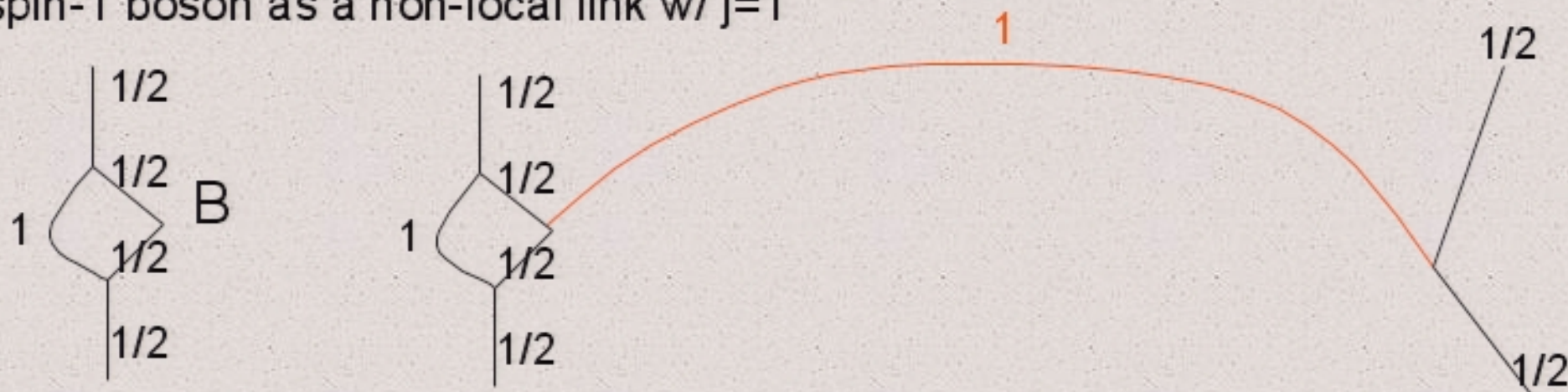
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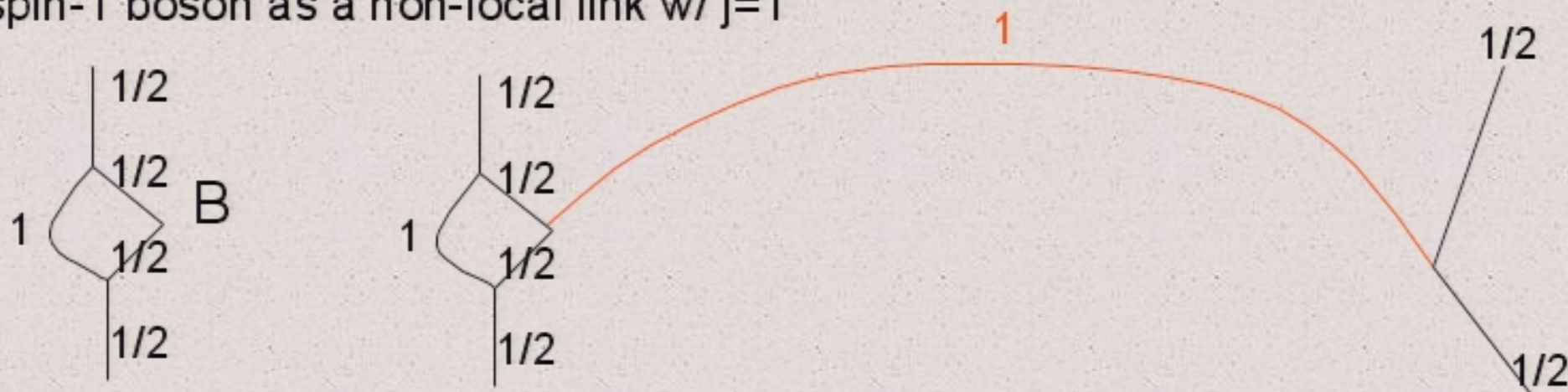
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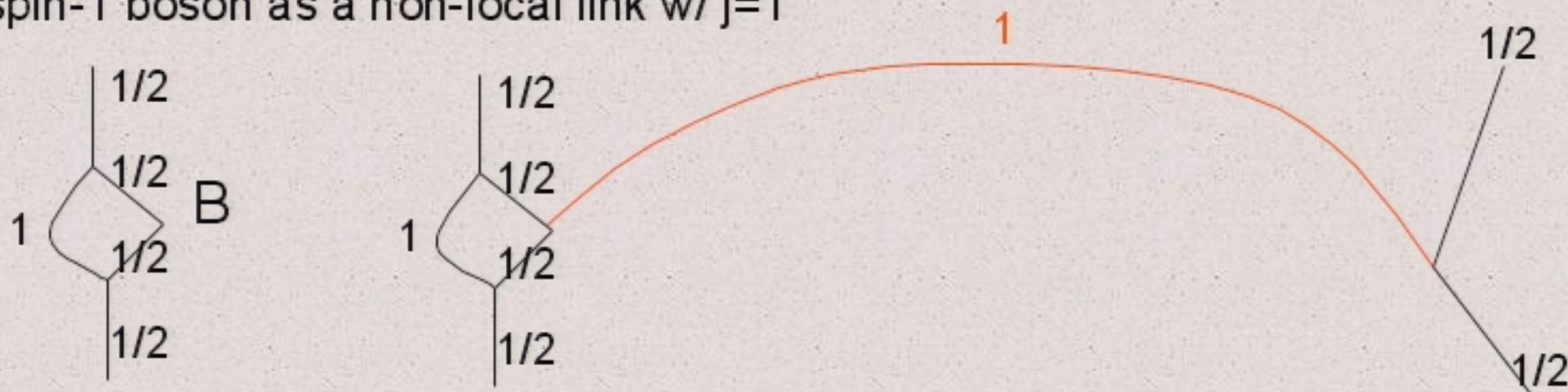
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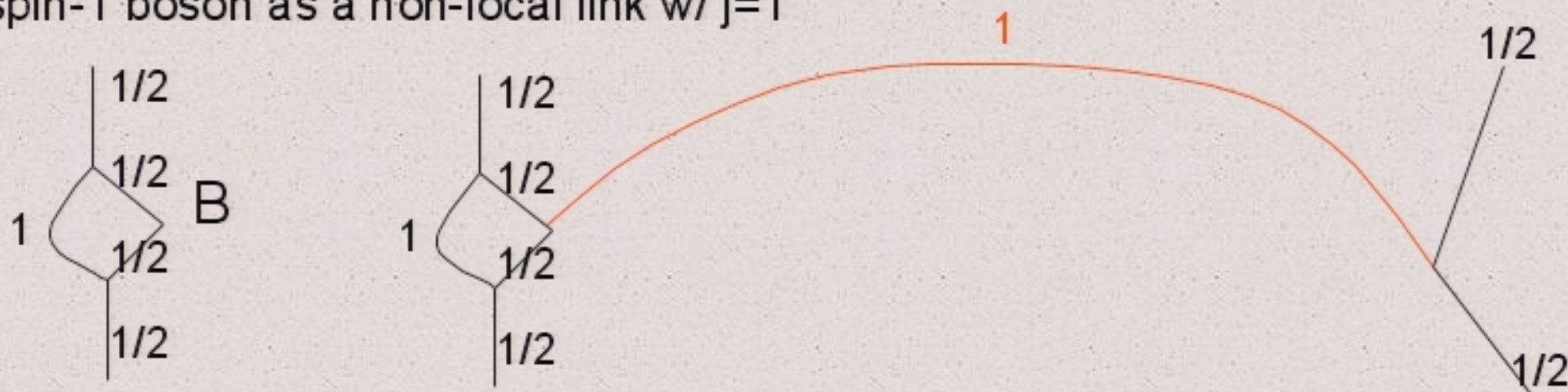
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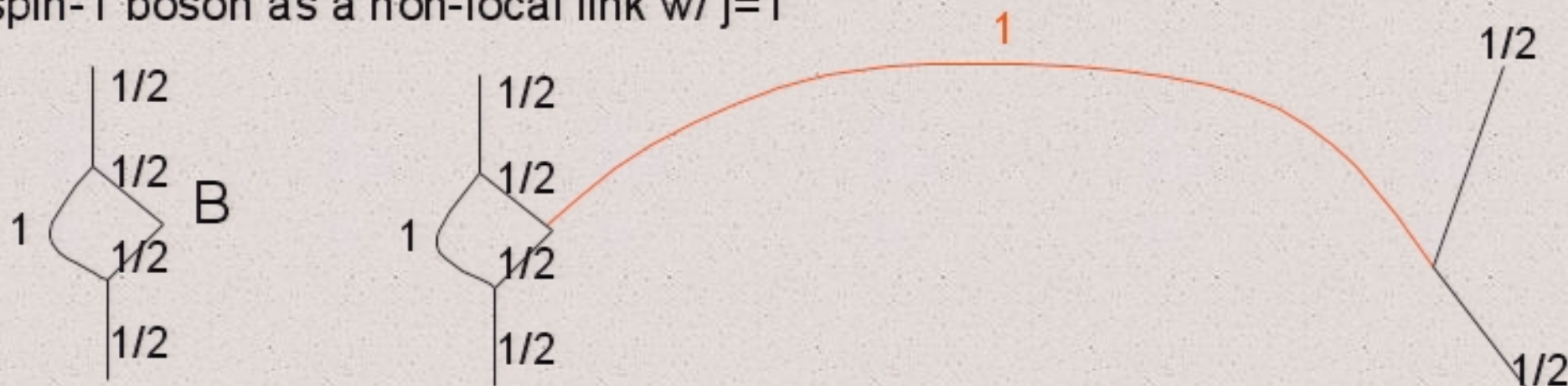
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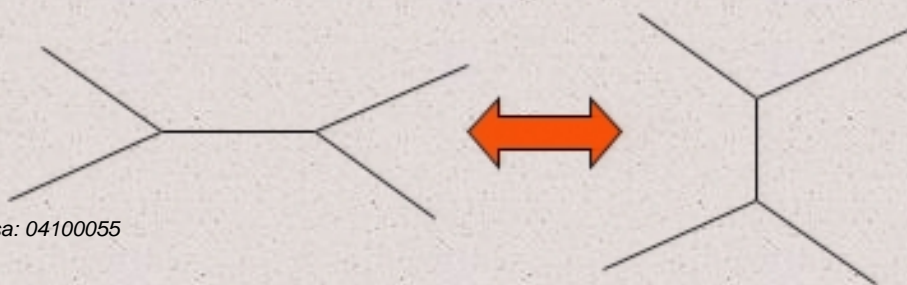
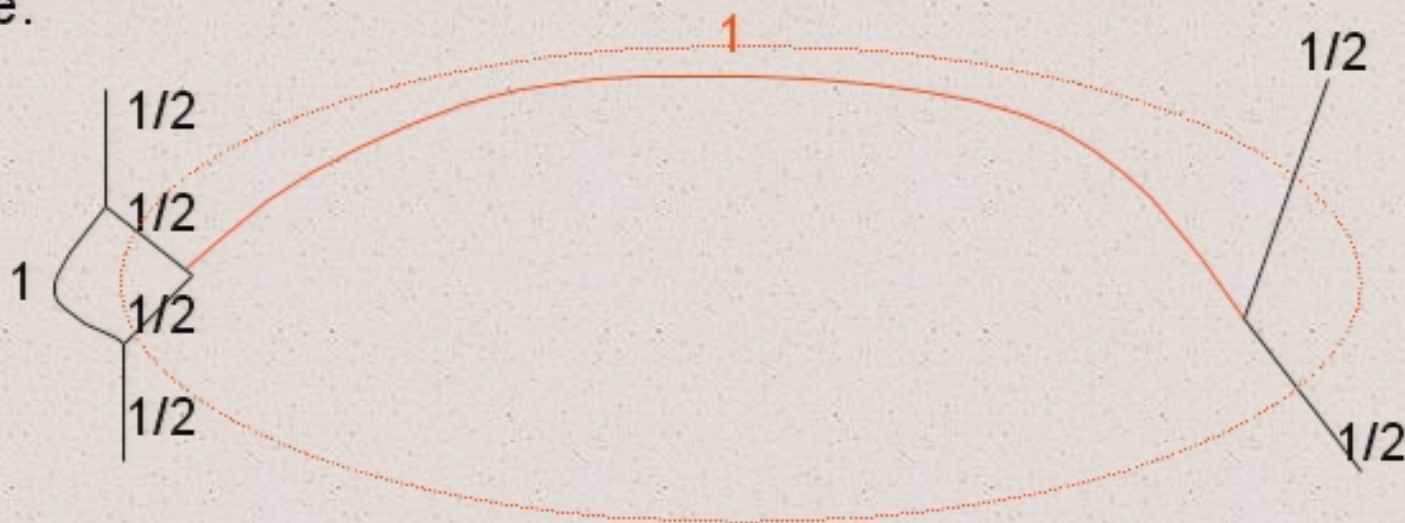
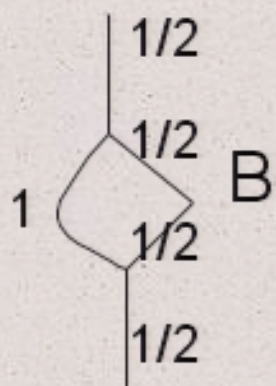
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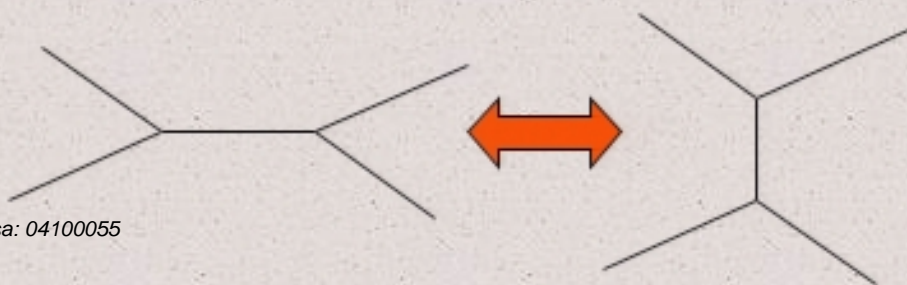
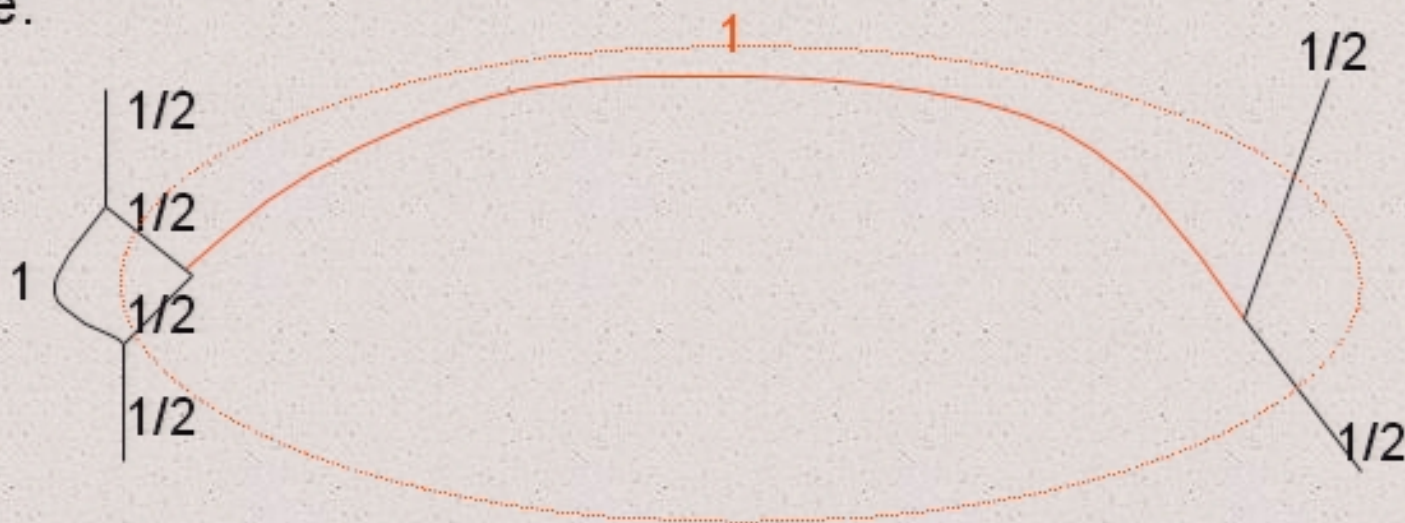
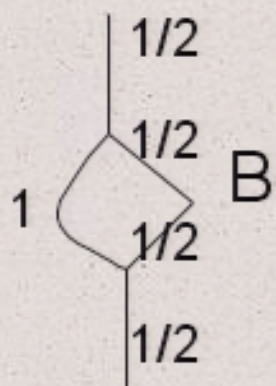
Interactions come from moves that are local microscopically,
but non local macroscopically:

Perform a 2 to 2 move:



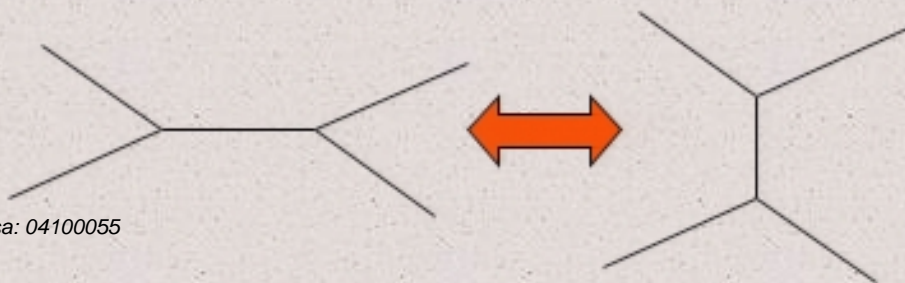
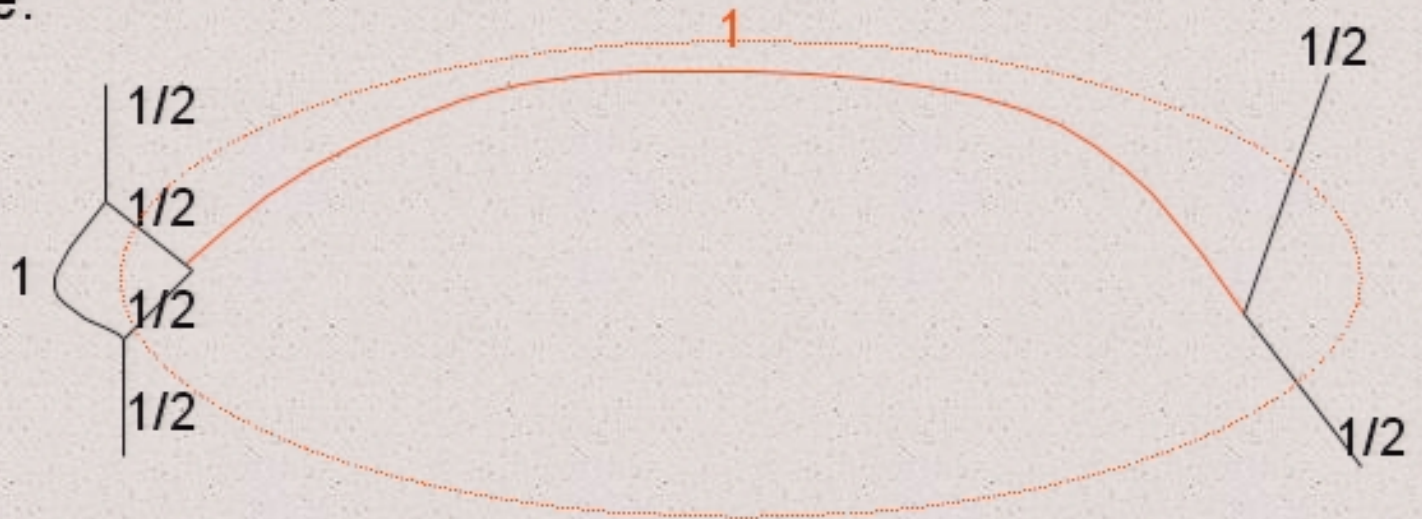
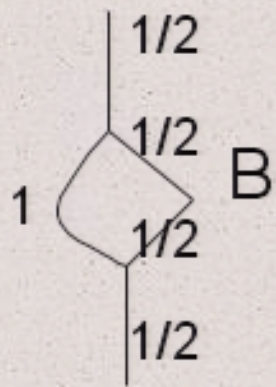
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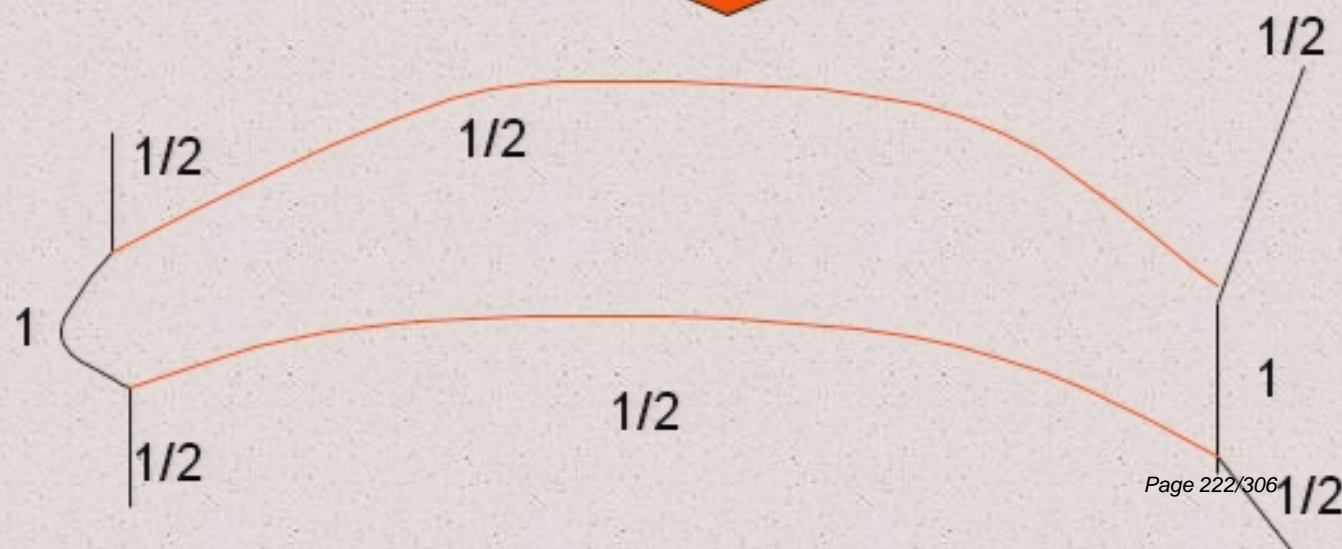
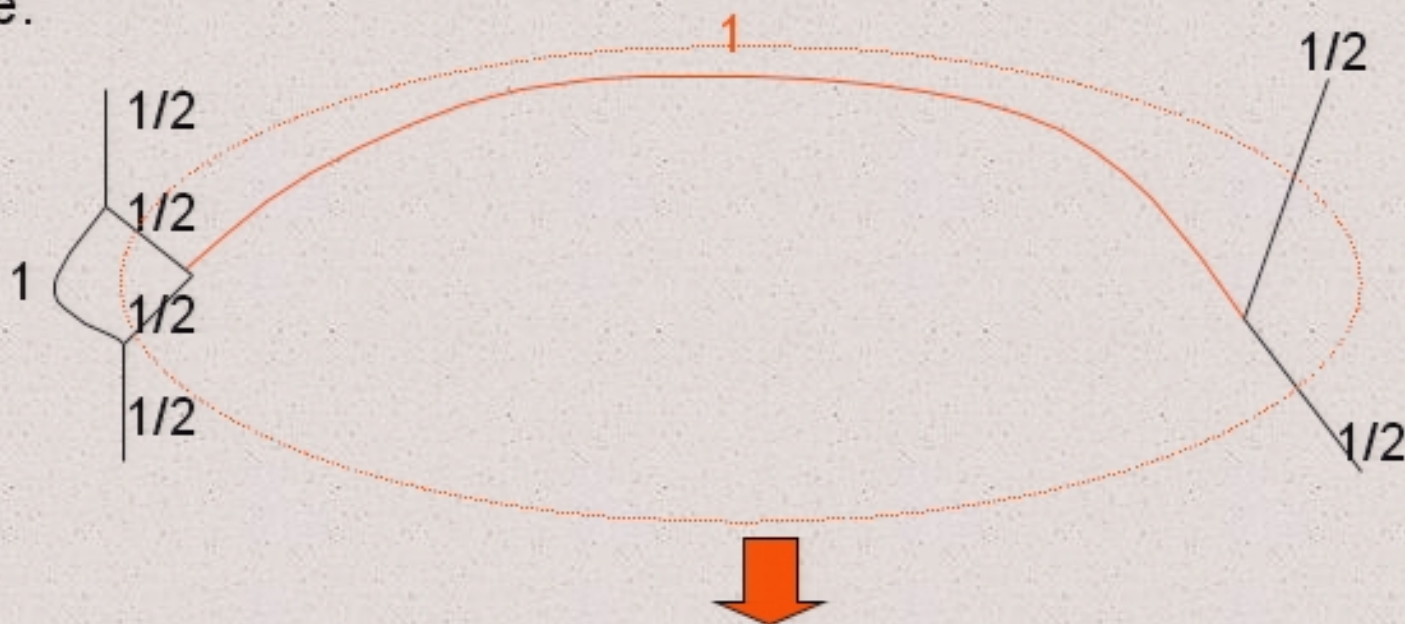
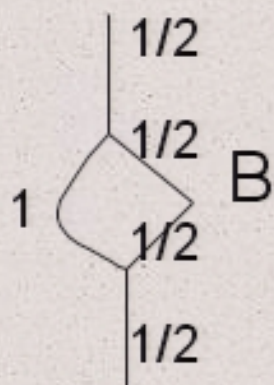
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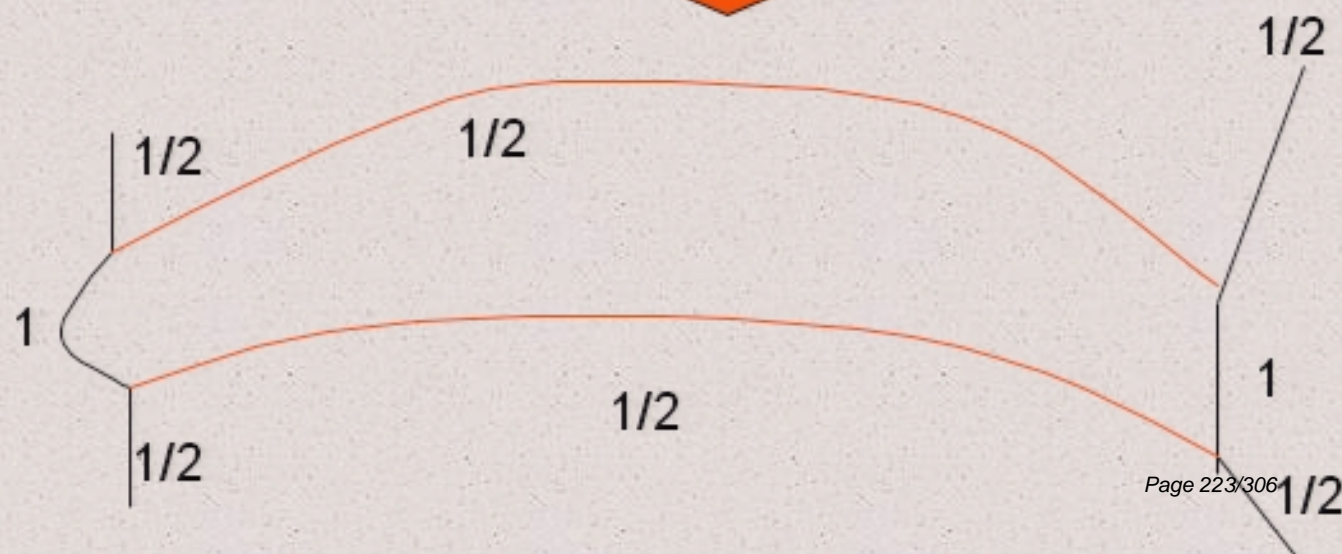
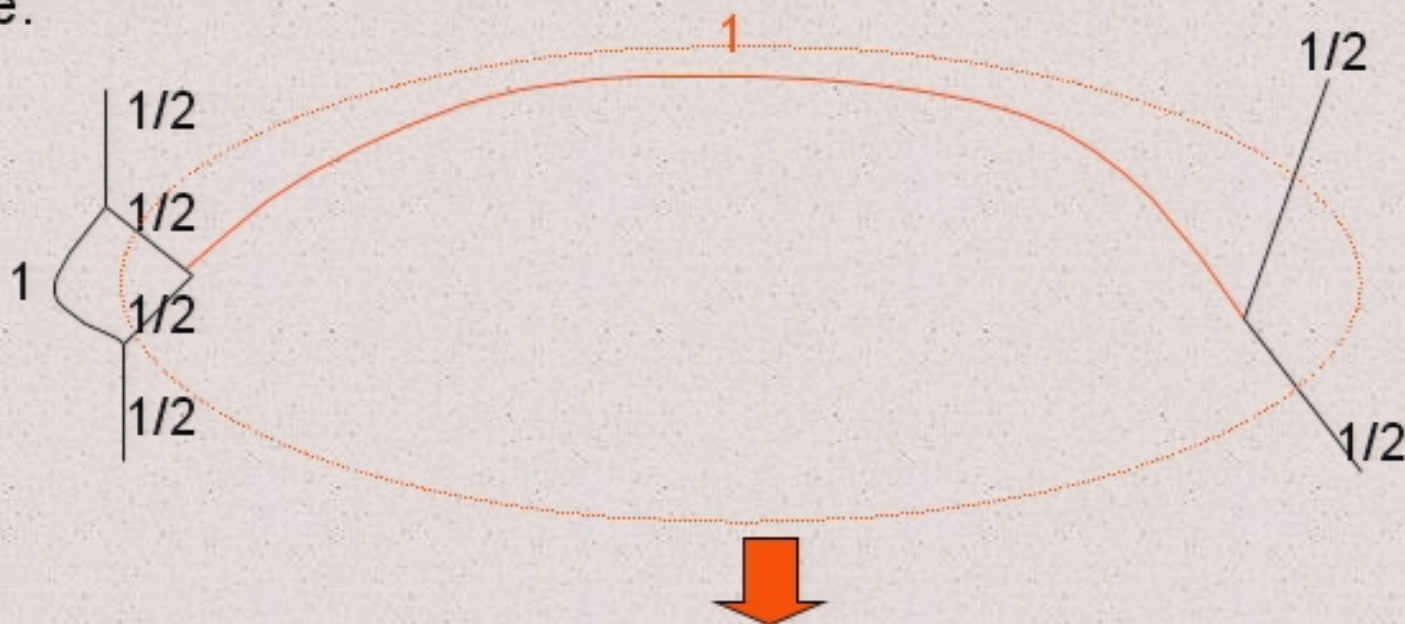
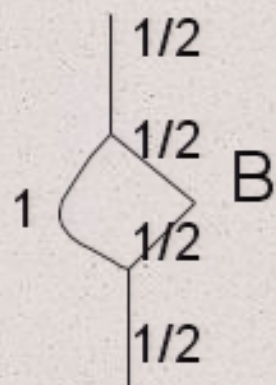
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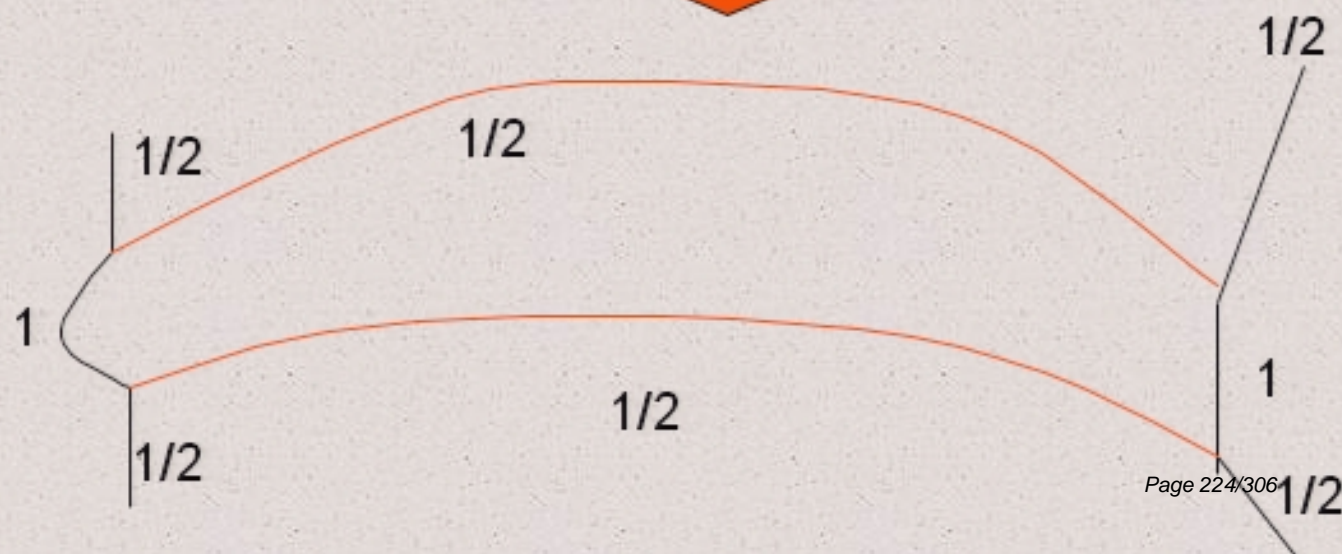
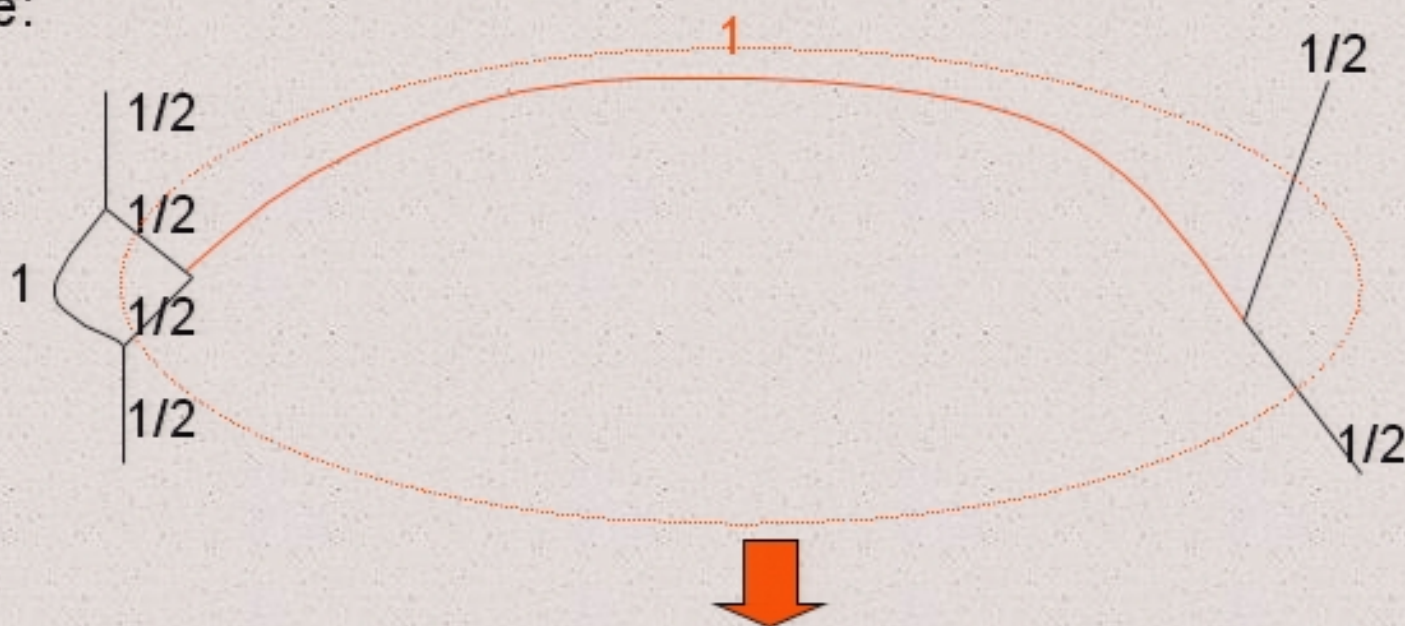
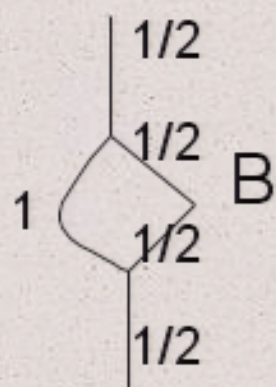
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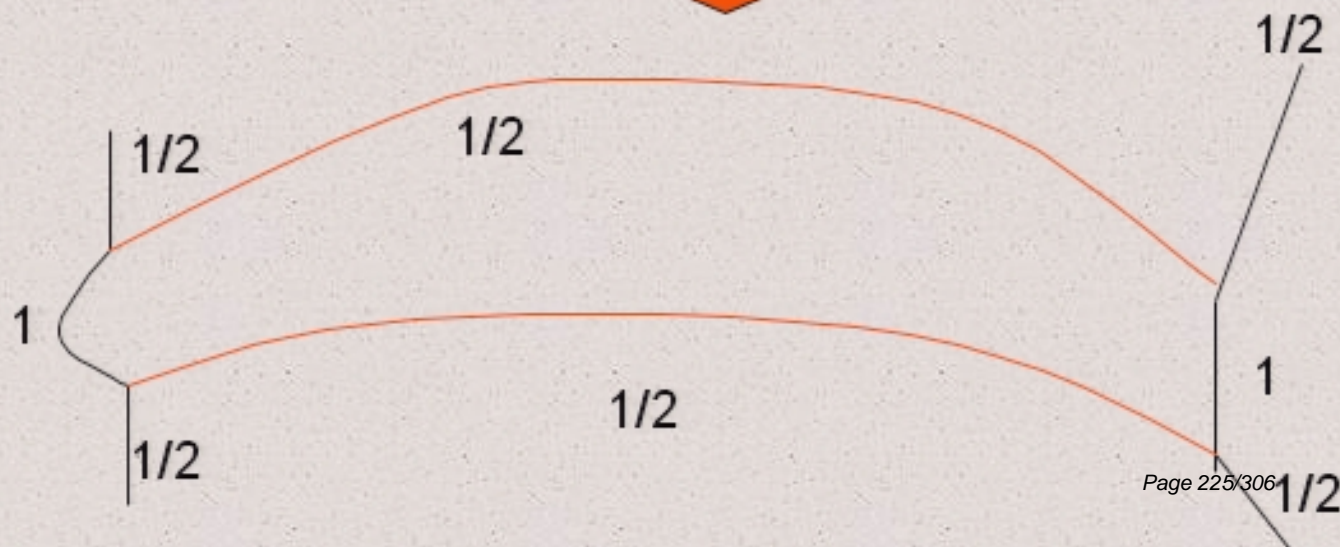
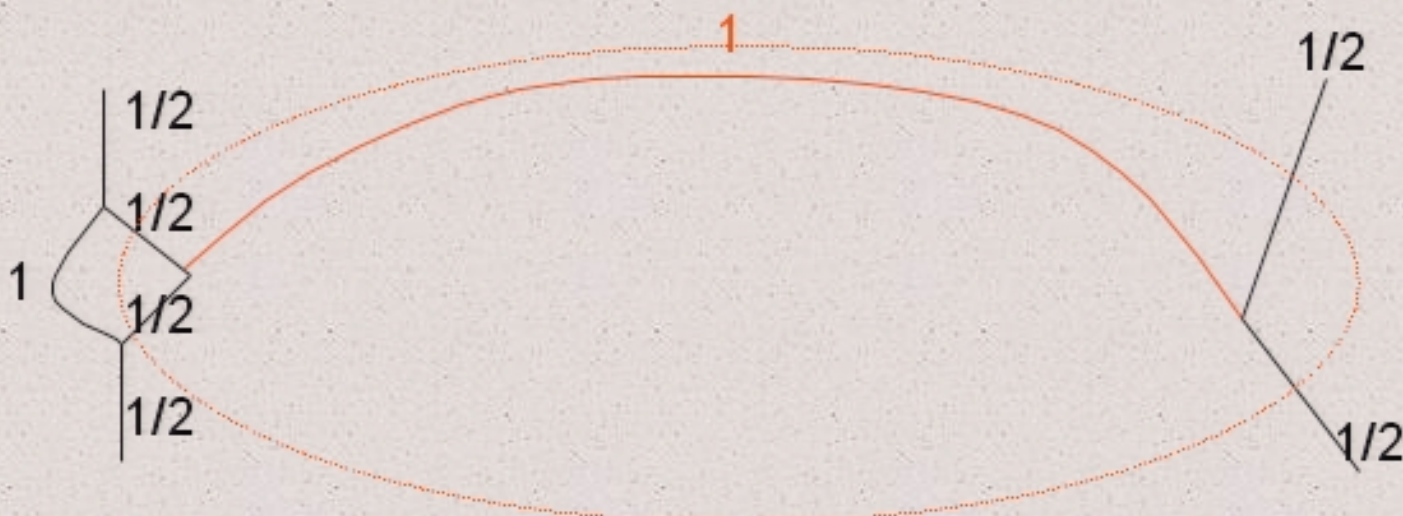
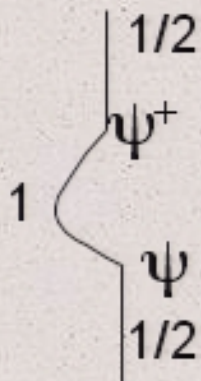
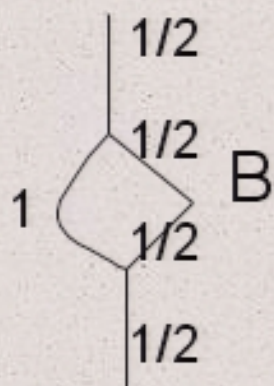
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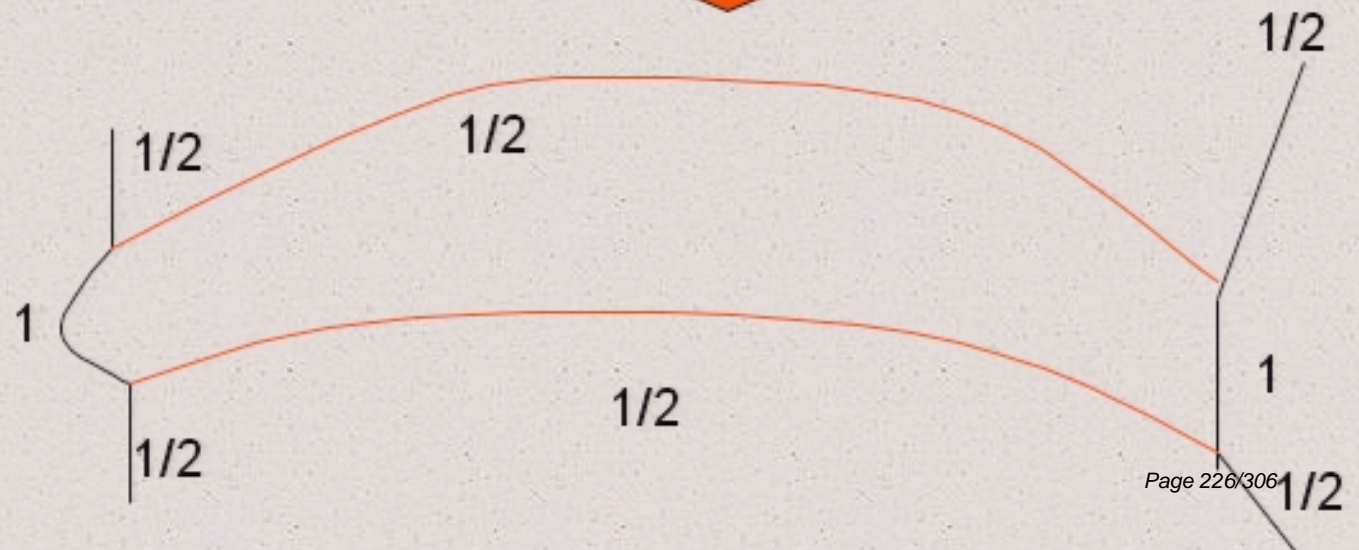
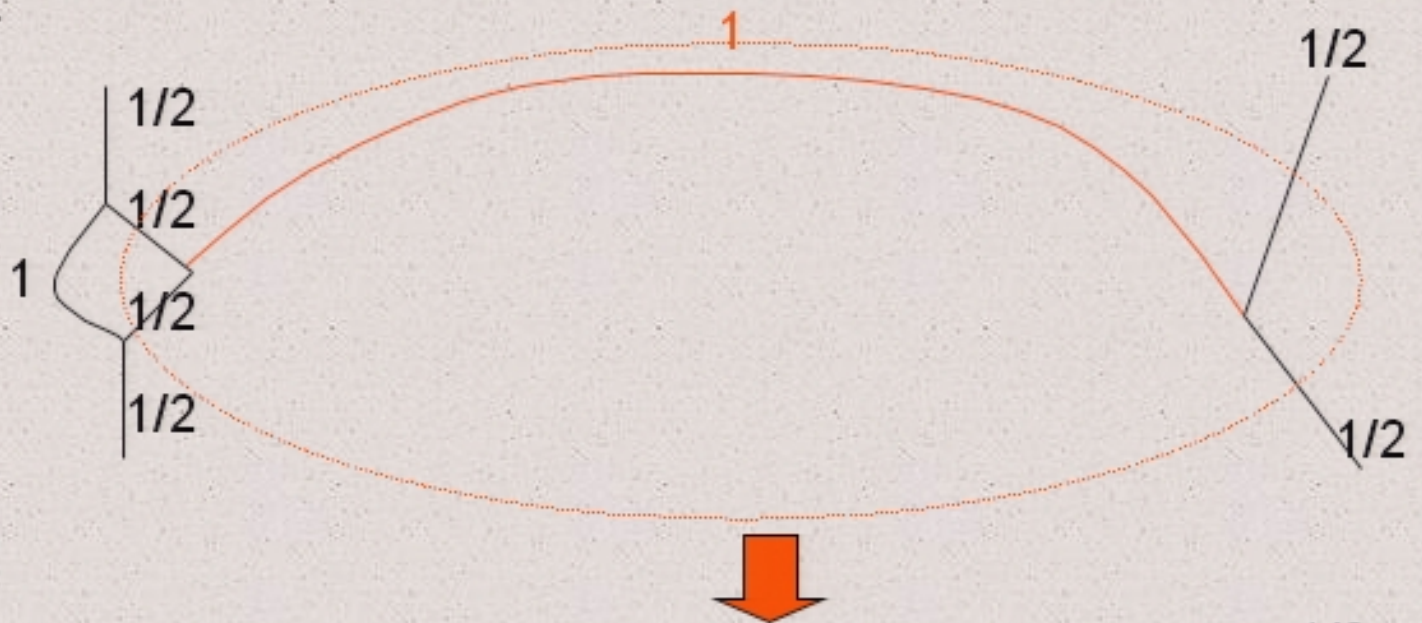
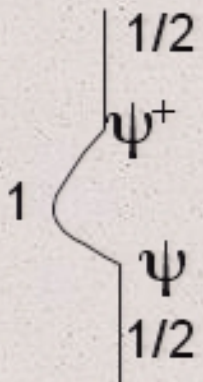
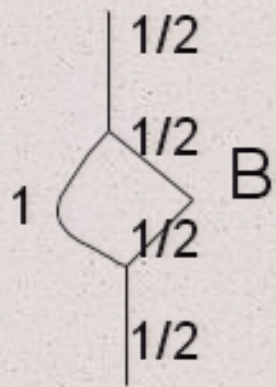
Interactions come from moves that are local microscopically,
but non local macroscopically:

Locally this looks like:



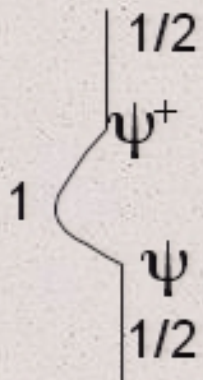
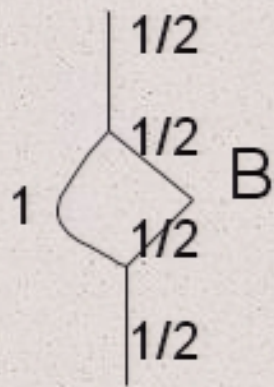
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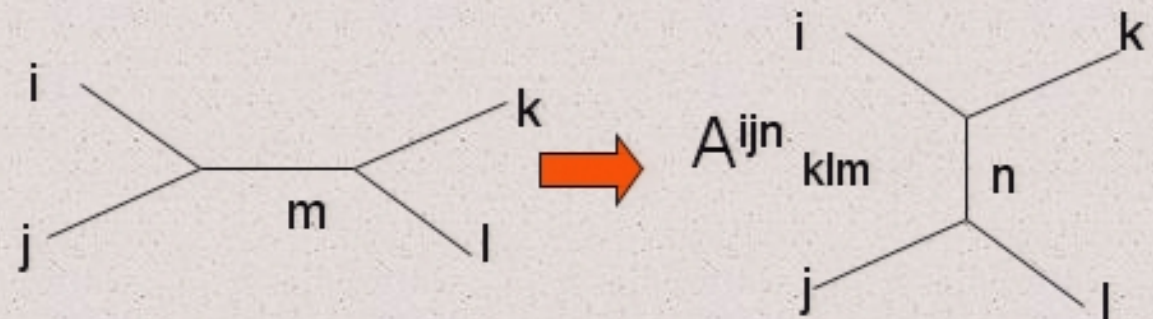


Interactions come from moves that are local microscopically,
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Locally this looks like:



So if the pure gravity amplitude is:

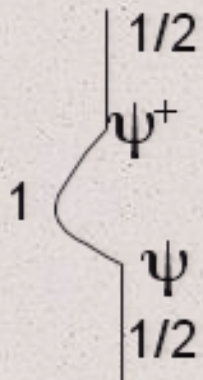
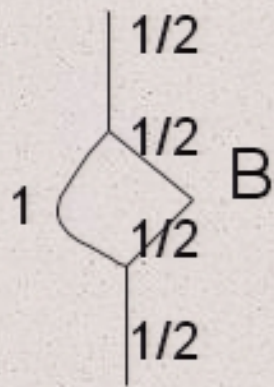


The amplitude for matter interaction
comes from the pure gravity evolution
amplitude.

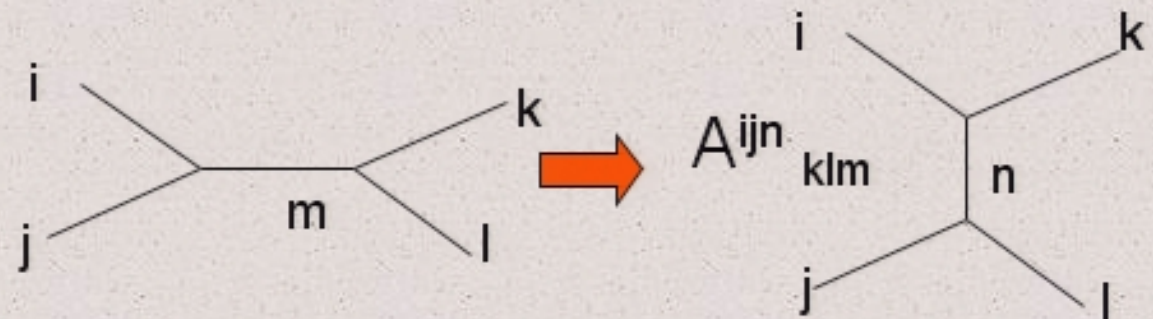
$$\text{Amp}_{B \rightarrow \psi^+ \psi} = A^{1/2 \ 1/2 \ 1}_{1/2 \ 1/2 \ 1}$$

Interactions come from moves that are local microscopically,
but non local macroscopically:

Locally this looks like:



So if the pure gravity amplitude is:

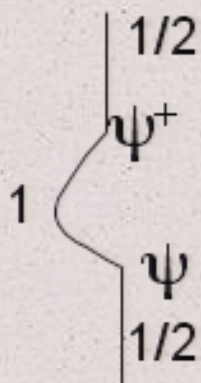
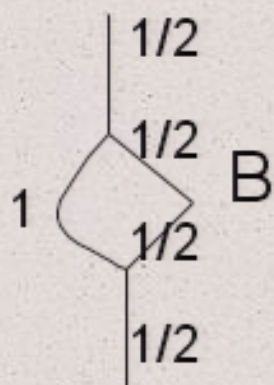


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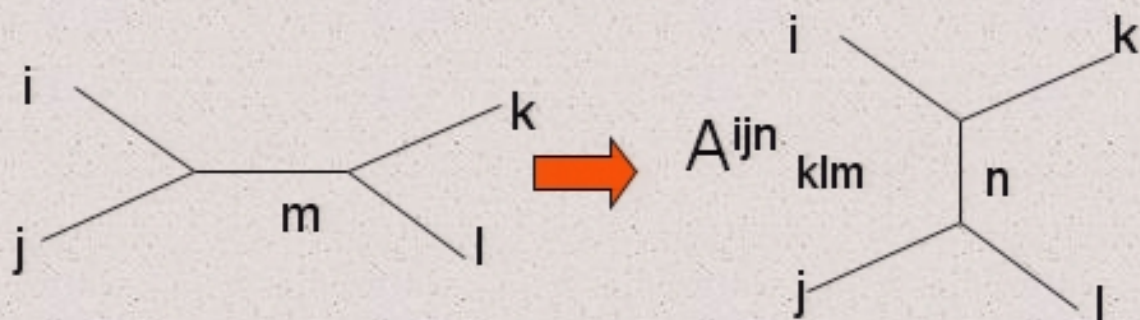
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Interactions come from moves that are local microscopically,
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Locally this looks like:



So if the pure gravity amplitude is:

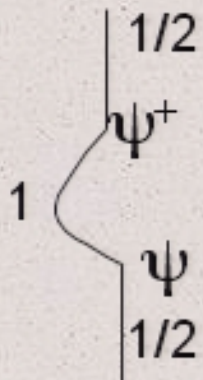
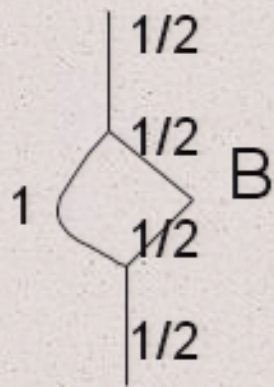


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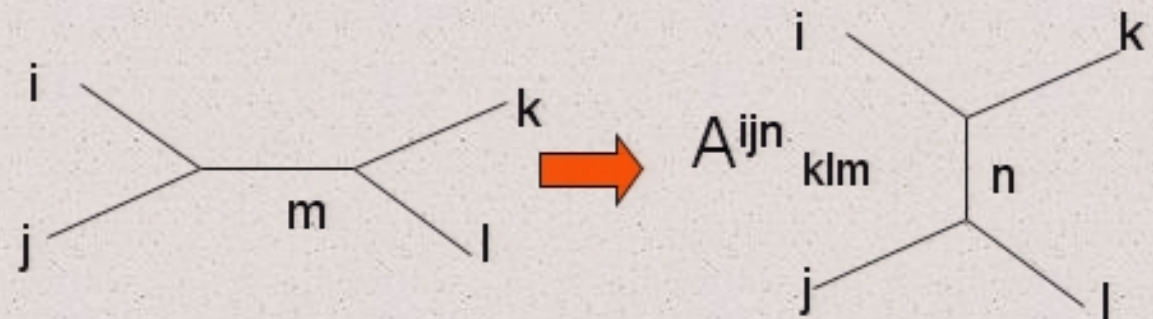
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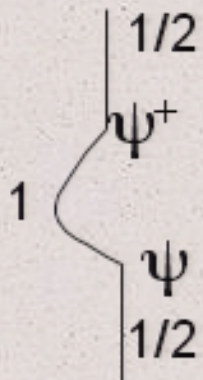
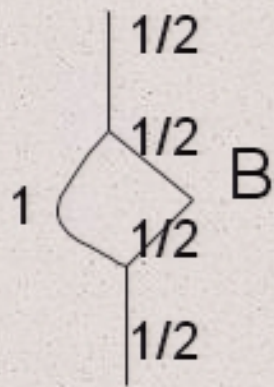


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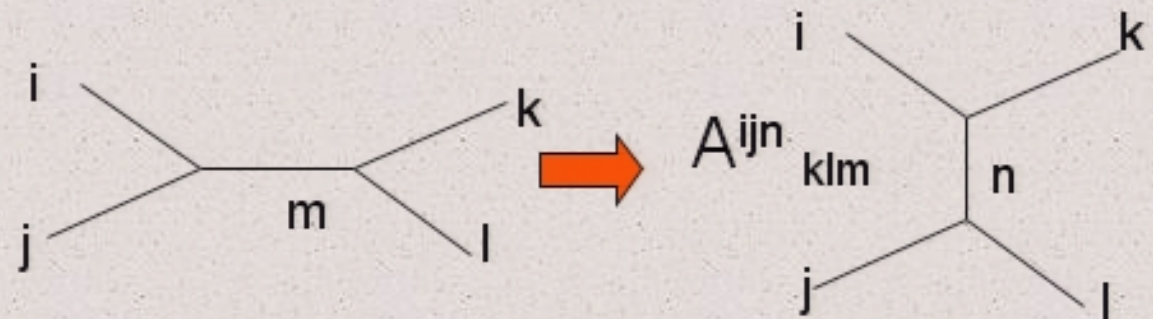
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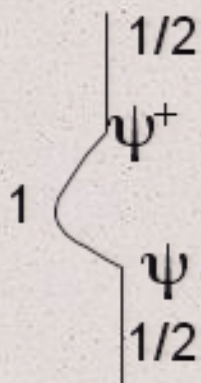
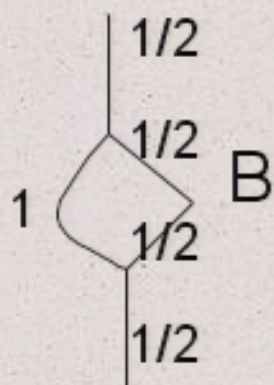


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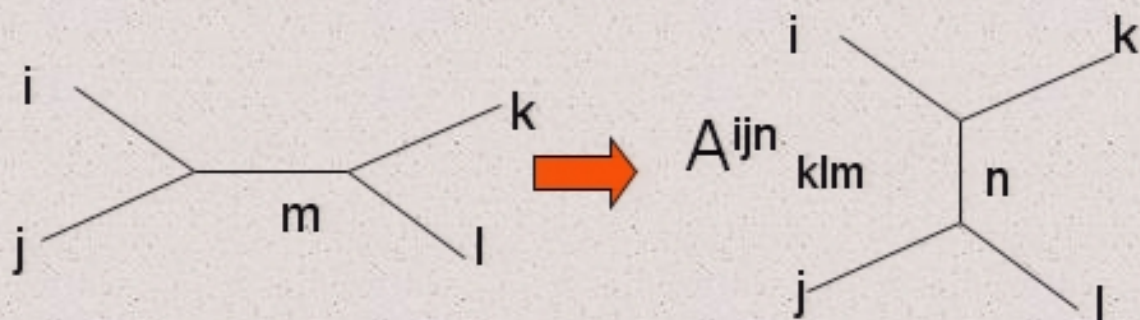
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JAW

- Works also when coupling to gauge fields are included.
Just label edges by reps of $SU(2) \times G$.

- Pair creation possibly implies spin-statistics connection.

Dowker, Sorkin, Balachandran.....

- $CPT_{\text{gravity}} \longrightarrow CPT_{\text{matter}}$ same for CP, T etc

- *Does CP breaking in matter imply CP breaking in gravity?*

- We get a tower of particles of increasing spin, just like
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- This gives a unification in which fermions appear in
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$$N_{\text{nodes}} \sim 10^{180}$$

$$N_{\text{nl}} \sim N_{\text{baryon}} \sim 10^{80}$$

$$P = N_{\text{nl}} / N_{\text{nodes}}^2 \sim 10^{-280}$$

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Evidence for non-local effects in very low energy astrophysics:

The Tully Fischer Relation:

- Galaxies have flat rotation curves, with velocity V .
- Total luminosity L

astro-ph/0204521

$$CL = V^a \quad a=3.9 \pm 0.2$$

- $K = L/M$ (M-total mass)

$$CKM = V^4$$

- CK should be prop to G*
- $CK = Ga_0$

$$a_0 = 1.2 \cdot 10^{-8} \text{ cm/sec}^2$$

$$= \sqrt{\Lambda} c^2/6$$

Pirsa: 04100055

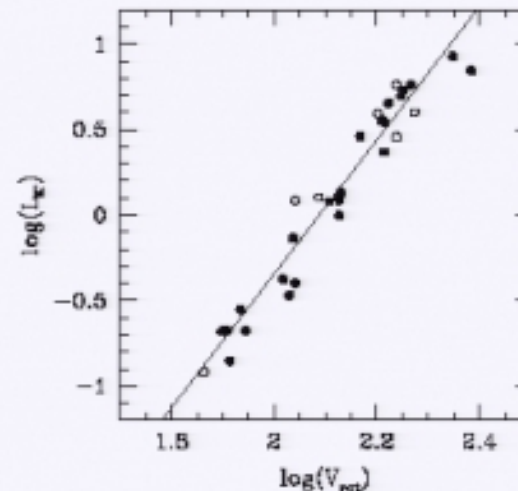


Figure 2: The near-infrared Tully-Fisher relation of Ursa Major spirals ((Sanders & Verheijen 1998)). The rotation velocity is the asymptotically constant value. The velocity is in units of kilometers/second and luminosity in $10^{10} L_{\odot}$. The unshaded points are galaxies with disturbed kinematics. The line is a least-square fit to the data and has a slope of 3.9 ± 0.2

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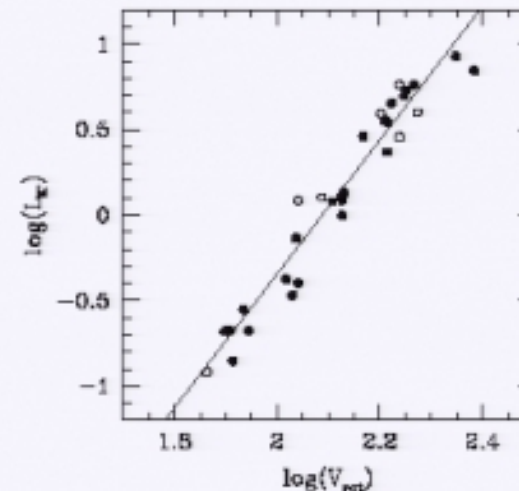


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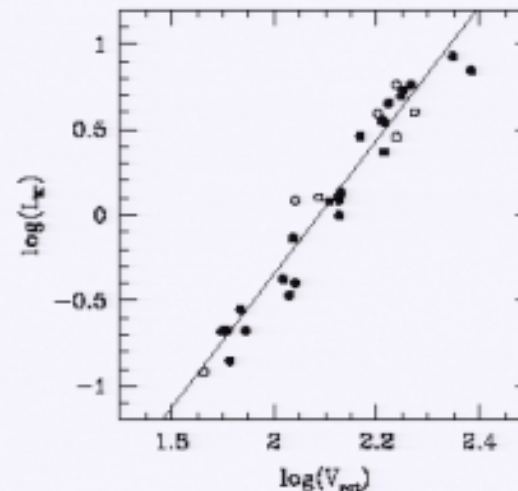


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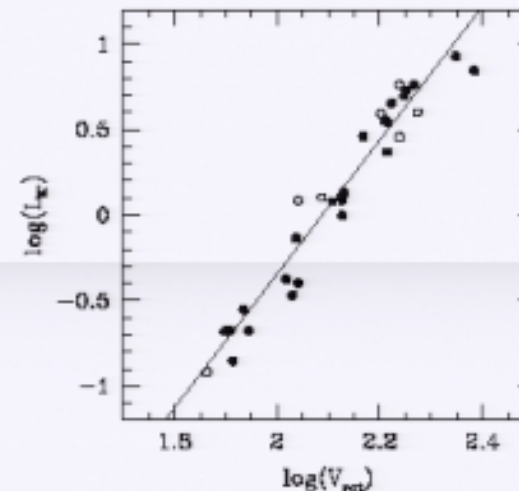


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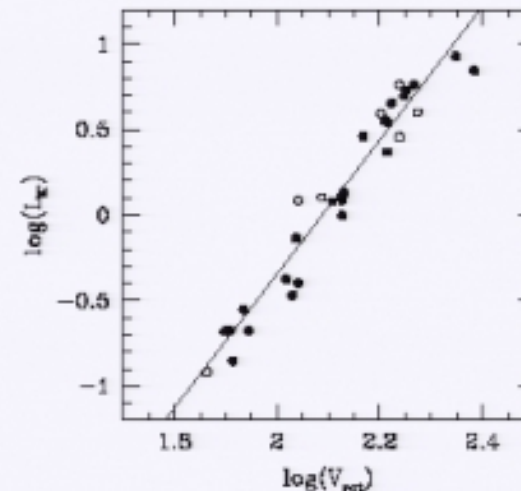


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There is a critical acceleration $a_0 = 1.2 \cdot 10^{-8} \text{ cm/sec}^2 \sim c^2/L$

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$$a_N = GM/r^2$$

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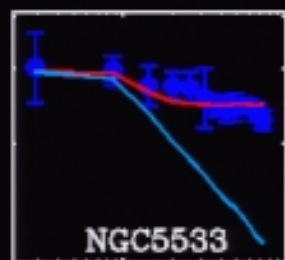
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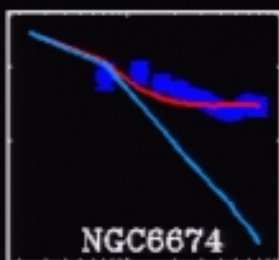
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The MOND potential:

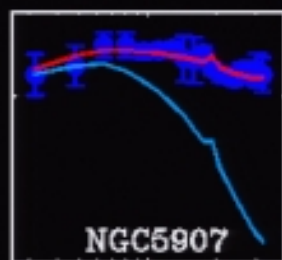
$$\phi_{MOND}(r) = \sqrt{GMa_0} \left[\ln\left(\frac{r}{r_0}\right) - 1 \right]$$



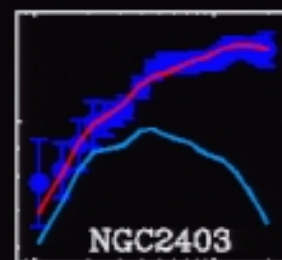
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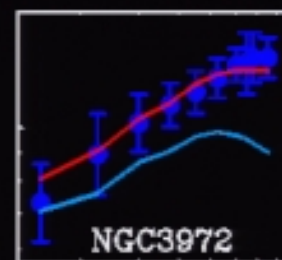
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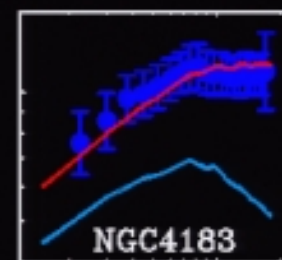
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NGC2403



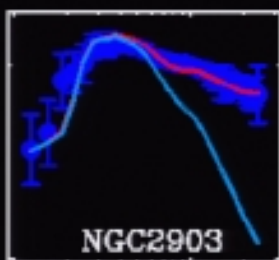
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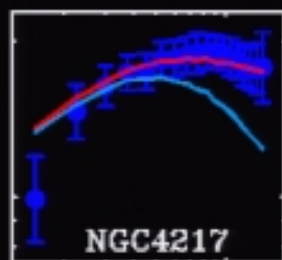
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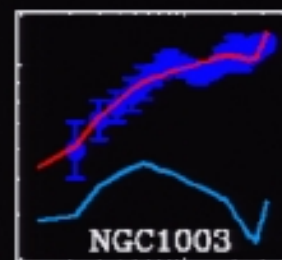
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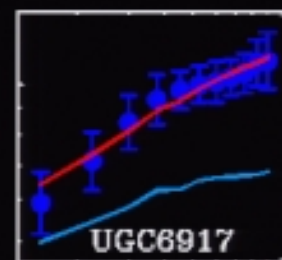
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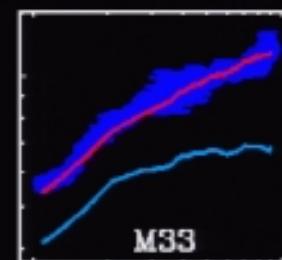
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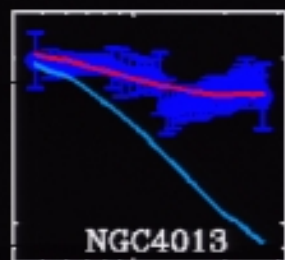
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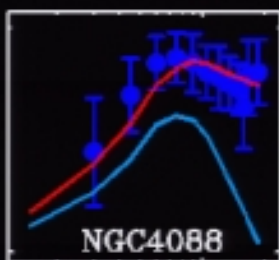
UGC6917



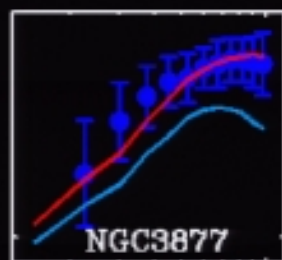
M33



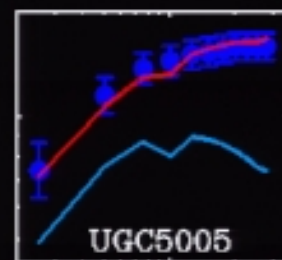
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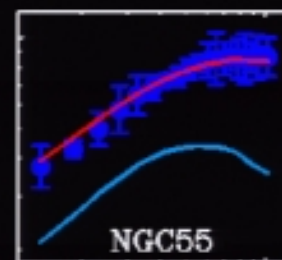
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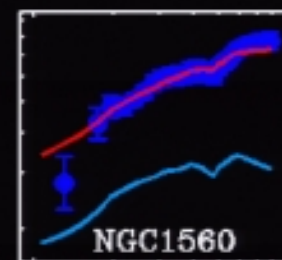
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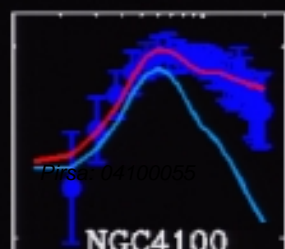
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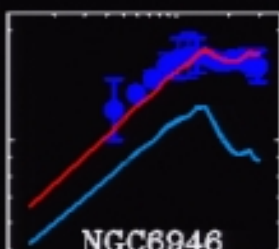
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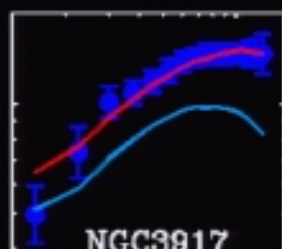
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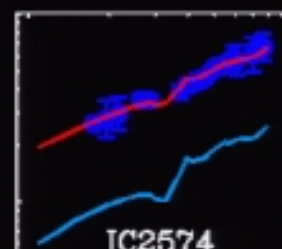
NGC4100



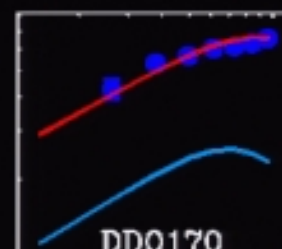
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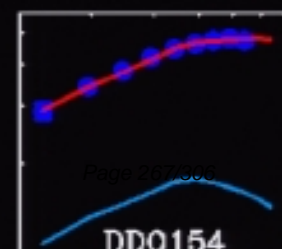
NGC3917



IC2524



DD0170



DD0154

- The MOND formula does embarrassingly well!
- Dark matter calculations do not do nearly as well:
 - Don't account for Tully-Fischer
 - Have cusps, dark matter should dominate in the centers of galaxies, but in the data they don't
- Doesn't explain the occurrence of an acceleration scale as the threshold for breakdown of Newton's laws with visible matter.
- Doesn't explain why it involves Λ .

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Bimetrics for graphs:

r_{nm} = distance between n and m in metric q_{ab} .

- The weave can be chosen so the graph metric matches r_{nm}

$P(r)$ probability that nodes n and m are connected if they are a distance r apart in the metric q_{ab}

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Prob of path w one jump:

$$\left(\frac{4\pi^2 z^2}{l_p^2} \right)^2 P(r)$$

$$z < r \quad w \sim r$$

We want z st the prob from a region around n and m are so connected. This means

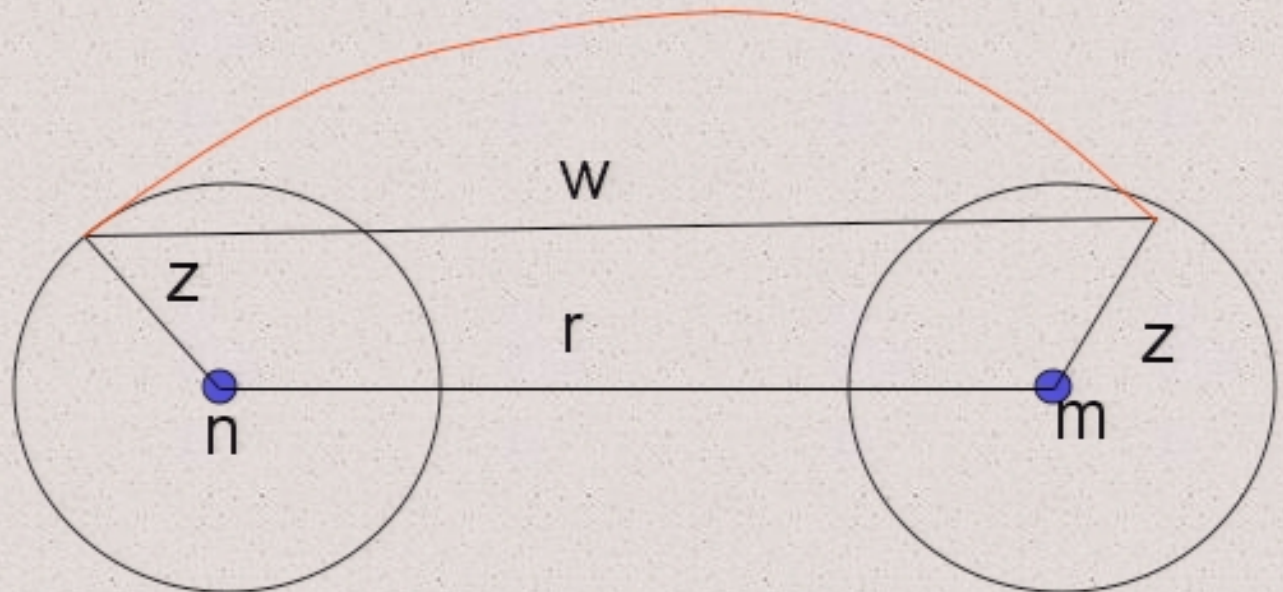
$$N \left(\frac{4\pi^2 z^2}{l_p^2} \right)^2 P(r) = 1$$

This gives

$$z(r) = \frac{l_p}{2\pi} \frac{1}{(NP(r))^{1/4}}$$

When this is true

$$\bar{d}(r) = 2z(r) + 1$$



This tells us the relationship between $P(r)$ and $d(r)$

$$\bar{d}(r) = \frac{l_p}{\pi} \frac{1}{(NP(r))^{1/4}}$$

•Our physical ansatz requires that $\phi_{\text{MOND}}(r) = -GM/d(r)$

•Mond:

$$\phi_{\text{MOND}}(r) = \sqrt{GMa_0} \left[\ln\left(\frac{r}{r_0}\right) - 1 \right]$$

•Our calculation found:

$$\bar{d}(r) = \frac{l_p}{\pi} \frac{1}{(NP(r))^{1/4}}$$

•These imply:

$$P(r) = \frac{1}{N} \left(\frac{l_p}{4\pi r_0} \right)^4 \left[\ln\left(\frac{r}{r_0}\right) - 1 \right]^4$$

So there is a wormhole distribution that leads to MOND

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- Quantum mechanics from the classical statistical mechanics of such weaves.**
- Coarse graining leads to bi-metric theories, possible relevance for early universe cosmology, inflation etc**

Dreyer, FM in progress

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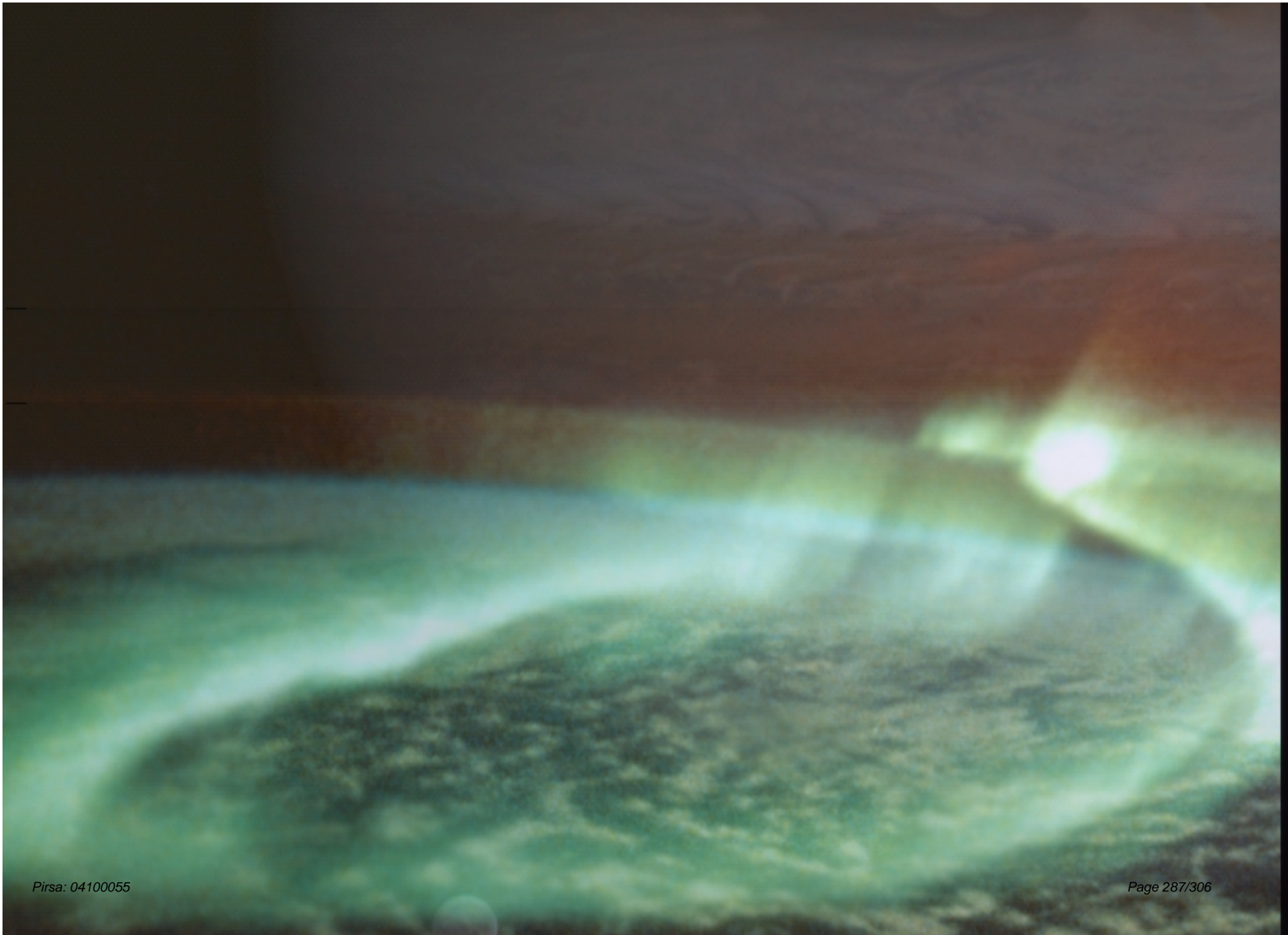
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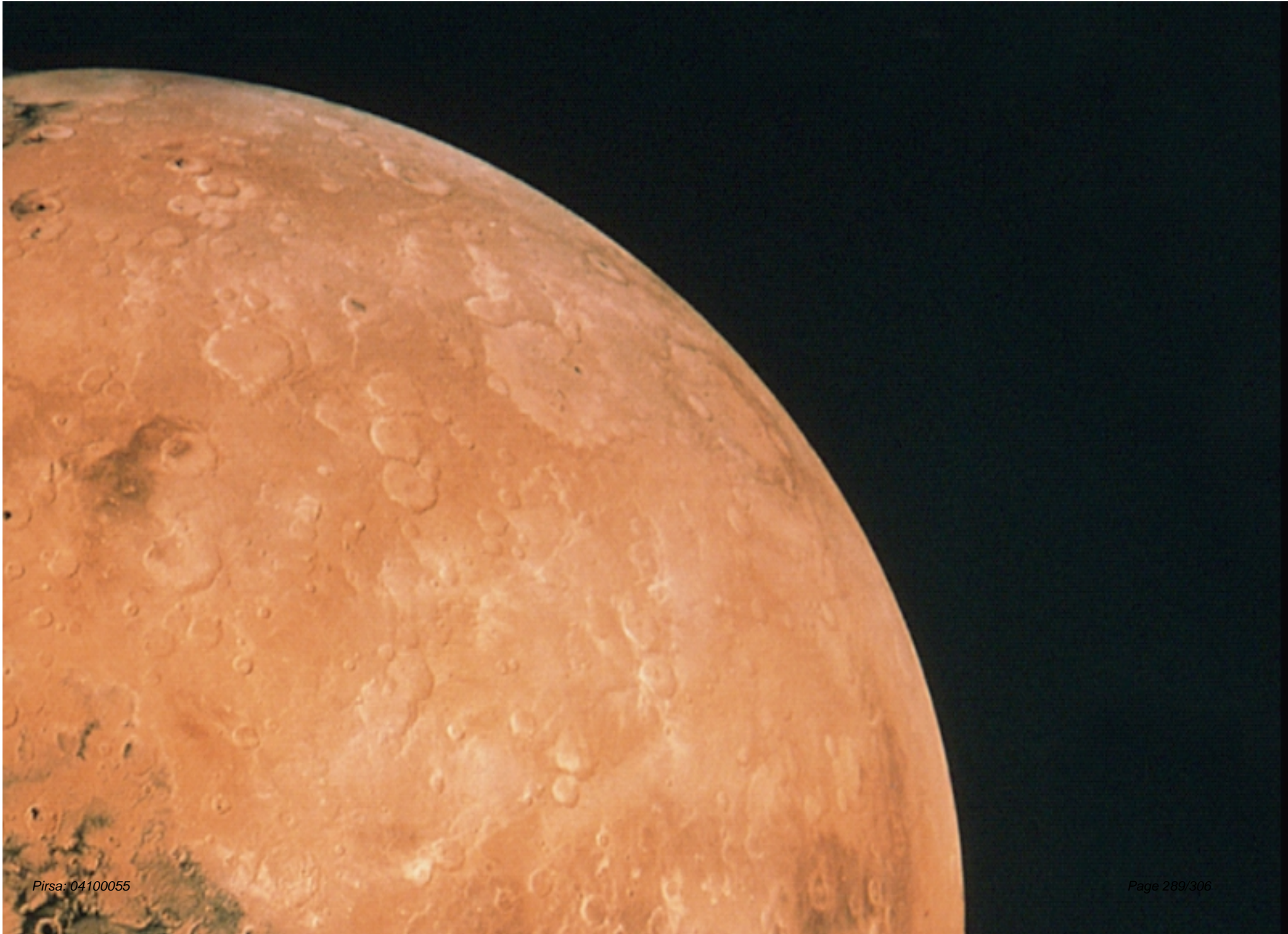
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